

# News from CTEQ-TEA PDF analysis

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# CT10.1 global PDF analysis

Tentative release: this summer

General-purpose CT10 and CT10W NLO PDFs: published in  
Physical Review D82, 074024 (2010)

- CT10.1 NLO set: extension of the CT10W analysis, with alternative treatment of some data sets
  - ▶ Tevatron Run-2 electron charge asymmetry ( $A_\ell$ )
  - ▶ Inclusive jet production
- CT10.2 NNLO PDFs
  - ▶ Validation of heavy-quark S-ACOT scheme at  $O(\alpha_s^2)$
  - ▶  $\alpha_s(M_Z) = 0.118$ ,  $m_c^{pole} = 1.3$  GeV,  $m_b^{pole} = 4.75$  GeV  
(same as in CT10.1 NLO PDFs)

## CT10.2 NNLO fit

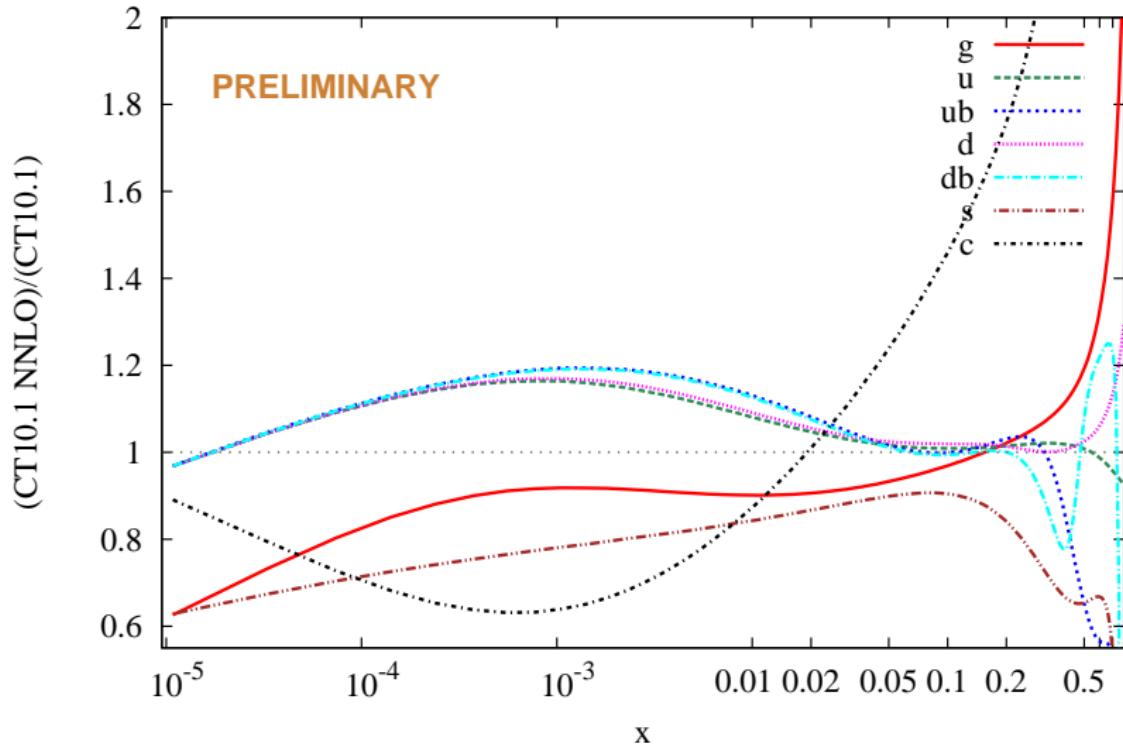
- Candidate central fits are available (cf. the next slide)
- In progress: studies of parametrization dependence, PDF errors,  $\alpha_s$  and  $m_Q$  dependence
- Slightly worse  $\chi^2$  at NNLO, due to no particular data set:

$$\chi^2_{NNLO}/N_{pt} \approx 3154/2765 \approx 1.14 ; \chi^2_{NLO} \approx 3090$$

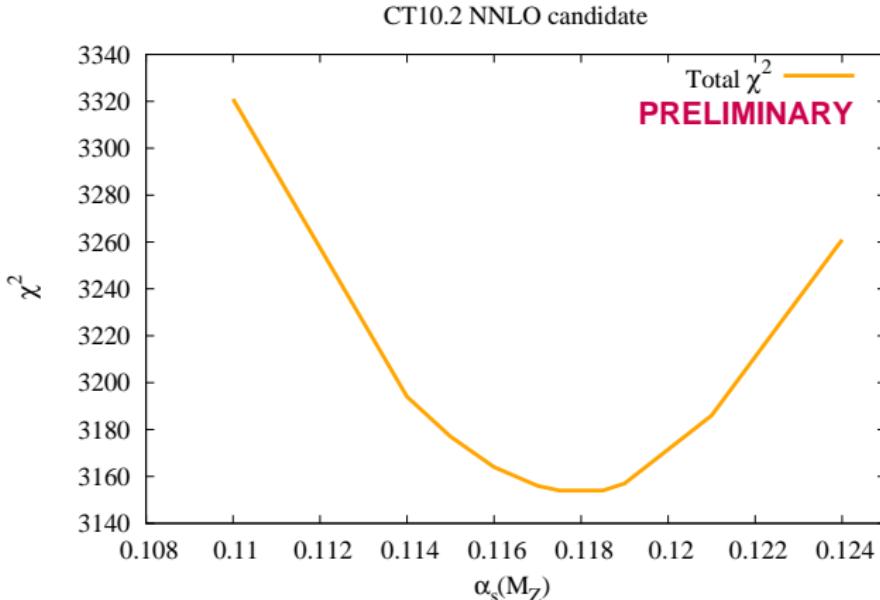
- ▶ Within  $\chi^2$  tolerance from CT10 NLO
- Differences between NLO and NNLO sets are comparable to such differences in ABM & MSTW NNLO PDF sets
- Reduced gluon at  $x \rightarrow 0$ ; increased light quarks at  $x \approx 10^{-3}$ ; lower strangeness

# Candidate NNLO fit (compared to CT10.1 NLO)

Ratios of central CT10.1 PDFs  $\mu = 2$  GeV



# Dependence on $\alpha_s$ in the CT10.1 fit

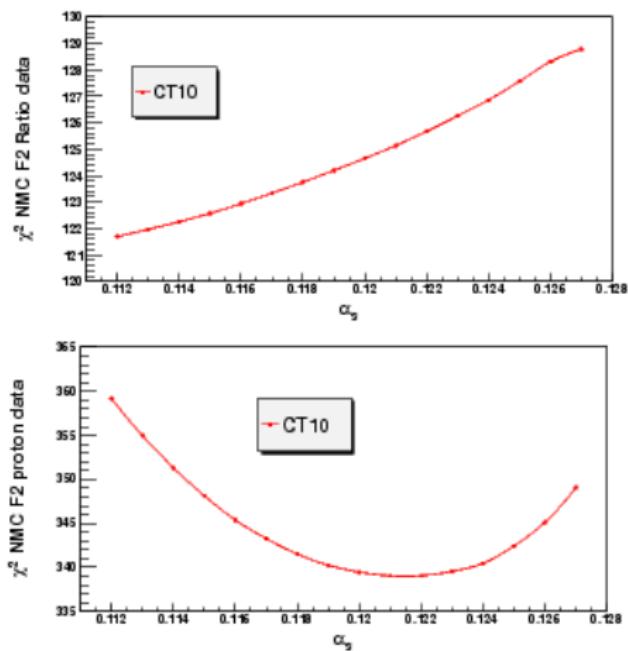


$\alpha_s$  decreases slightly at NNLO, has about the same PDF uncertainty as at NLO

- NLO:  $\alpha_s(M_Z) = 0.11964 \pm 0.0064$  at 90% c.l.
- NNLO:  $\alpha_s(M_Z) = 0.118 \pm 0.005$

# CT10AS fit: NMC $F_2^d/F_2^p$ and $F_2^p$ data vs. $\alpha_s$

Total  $\chi^2$  vs.  $\alpha_s(M_Z)$   
in the CT10AS series



- We did not find a significant effect of the NMC  $F_2^d/F_2^p$  data on  $\alpha_s$ , even though a smaller value is mildly preferred.  
 $\chi^2(F_2^d/F_2^p) \approx N_{points} = 123$ .
- NMC  $F_2^p$  data prefer a larger  $\alpha_s$ , but  $\chi^2$  is larger than  $N_{points} = 201$ .
- Replacing  $F_2^p$  by the NMC reduced cross section does not significantly change the best-fit value of  $\alpha_s$  and its error.

# Simplified Aivazis-Collins-Olness-Tung scheme

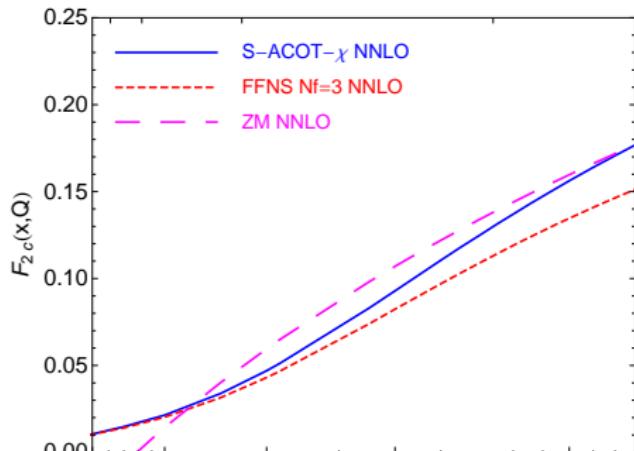
ACOT, PRD 50 3102 (1994); Collins, PRD 58 (1998) 094002; Kramer, Olness, Soper, PRD (2000) 096007

- Derivation is based upon, and closely follows, the proof of QCD factorization for DIS with massive quarks (*Collins, 1998*)
- Relatively simple
  - ▶ One value of  $N_f$  (and one PDF set) in each  $Q$  range
  - ▶ Straightforward matching based on kinematical rescaling
  - ▶ Sets  $m_Q = 0$  in ME with incoming  $c$  or  $b$
- Reduces to the ZM  $\overline{MS}$  scheme at  $Q^2 \gg m_Q^2$ , without additional renormalization
- Reduces to the FFN scheme at  $Q^2 \approx m_Q^2$ 
  - ▶ has reduced dependence on tunable parameters at NNLO

# S-ACOT scheme: merging FFN and ZM

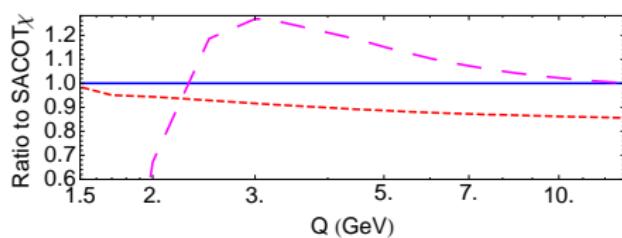
Preliminary

$x=0.01$



ACOT reduces  
to FFNS at  $Q \approx m_c$   
and to ZM at  $Q \gg m_c$

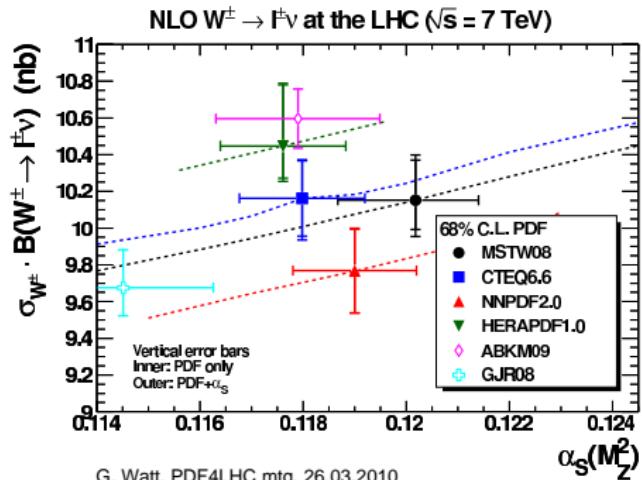
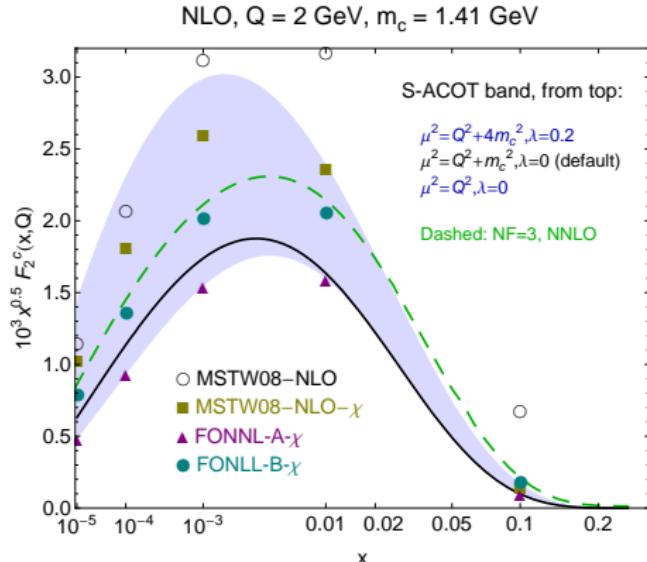
Les Houches toy PDFs, evolved  
at NNLO with threshold  
matching terms



Cancellations between  
subtractions and other terms at  
 $Q \approx m_c$  and  $Q \gg m_c$ ; details in  
backup slides

# Input parameters of the S-ACOT scheme

At NLO, the charm mass  $m_c$ , factorization scale  $\mu$ , and rescaling variable  $\zeta$  of CTEQ PDFs are **tuned** to best describe the DIS data



2009 Les Houches HQ benchmarks  
with toy PDFs; default  $\mu = Q$

$W, Z$  cross sections;  
 $m_c = 1.3 \text{ GeV}$  in CTEQ6.6

# NNLO results for $F_2^{(c)}(x, Q^2)$ - Preliminary

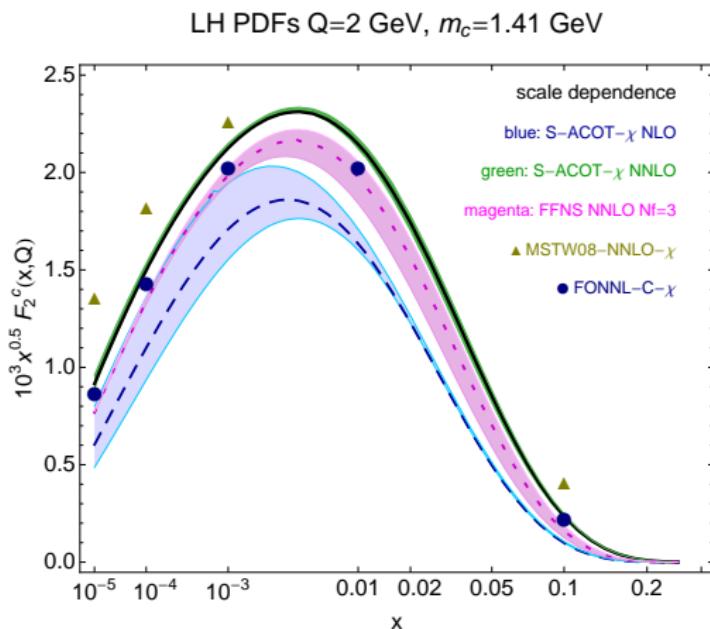
At NNLO and  $Q \approx m_c$ :

S-ACOT- $\chi$  ( $N_f = 4$ )  $\approx$  FFN ( $N_f = 3$ )  
without tuning

- S-ACOT is numerically close to other NNLO schemes
- NNLO expressions are close to the FONLL-C scheme

(Forte, Laenen, Nason, arXiv:1001.2312).

- ACOT formalism provides recipe-like formulas for implementing NNLO in the GM scheme



## Components of inclusive $F_{2,L}(x, Q)$

Components of inclusive  $F_{2,L}(x, Q^2)$  are classified according to the quark couplings to the photon

$$F = \sum_{l=1}^{N_l} F_l + F_h \quad (1)$$

$$F_l = e_l^2 \sum_a [C_{l,a} \otimes f_{a/p}] (x, Q), \quad F_h = e_h^2 \sum_a [C_{h,a} \otimes f_{a/p}] (x, Q). \quad (2)$$



At  $\mathcal{O}(\alpha_s^2)$ :

$$F_h^{(2)} = e_h^2 \left\{ c_{h,h}^{NS,(2)} \otimes (f_{h/p} + f_{\bar{h}/p}) + C_{h,l}^{(2)} \otimes \Sigma + C_{h,g}^{(2)} \otimes f_{g/p} \right\}$$
$$F_l^{(2)} = e_l^2 \left\{ C_{l,l}^{NS,(2)} \otimes (f_{l/p} + f_{\bar{l}/p}) + c^{PS,(2)} \otimes \Sigma + c_{l,g}^{(2)} \otimes f_{g/p} \right\}. \quad (3)$$

Structure of factorized expressions is reminiscent of the ZM scheme (e.g., in MVV 2005)

# Components of inclusive $F_{2,L}(x, Q)$

- Lower case  $c_{a,b}^{(2)}, \hat{f}_{a,b}^{(k)} \rightarrow$  ZM expressions  
Zijlstra and Van Neerven PLB272 (1991), NPB383 (1992)  
S. Moch, J.A.M. Vermaseren and A. Vogt, NPB724 (2005)
- Upper case  $C_{a,b}^{(2)}, F_{a,b}^{(k)}, A_{a,b}^{(k)} \rightarrow$  coeff. functions, structure functions and subtractions with  $m_c \neq 0$ ,  
Buza *et al.*, NPB 472 (1996); EPJC1 (1998);  
Riemersma, *et al.* PLB 347 (1995); Laenen *et al.* NPB392 (1993)
- All building blocks are available from literature

## Components of inclusive $F_{2,L}(x, Q)$

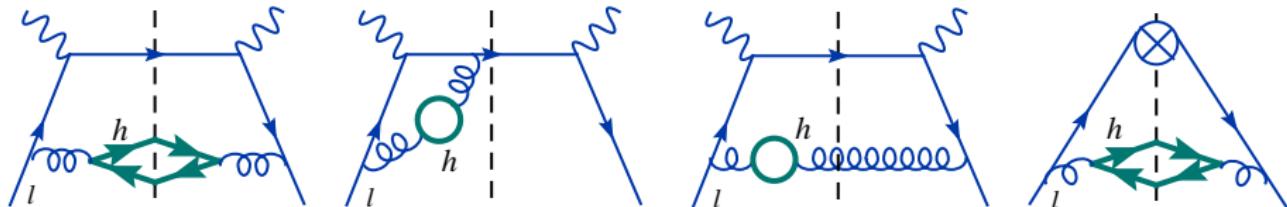
The separation into  $F_l$  and  $F_h$  (according to the quark's electric charge  $e_i^2$ ) is valid at all  $Q$

The "light-quark"  $F_l$  contains some subgraphs with heavy-quark lines, denoted by " $G_{l,l,heavy}$ ".

The "heavy-quark"  $F_h \neq F_2^c$ :

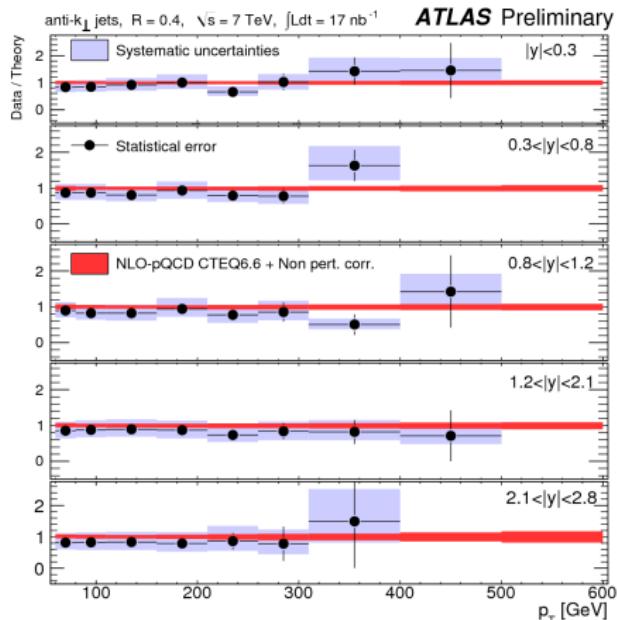
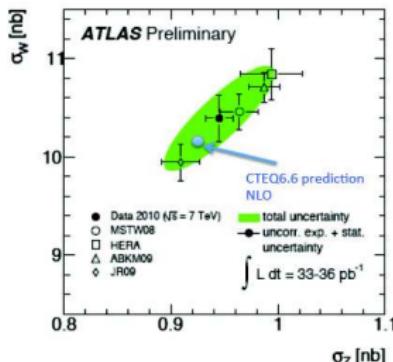
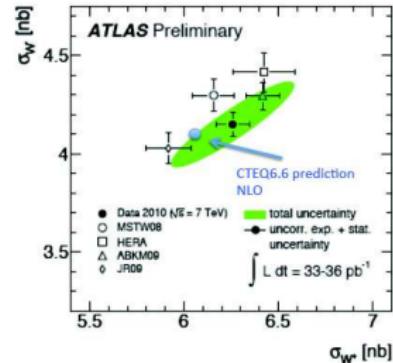
$$F_2^c = F_h + (G_{l,l,heavy})_{real},$$

where  $G_{i,j} = C_{i,j}^{(2)}$ ,  $F_{i,j}^{(2)}$ , and  $A_{i,j}^{(2)}$



# CTEQ PDFs vs. the latest data: LHC

Agreement with many LHC measurements



+data on  $\sigma_W/\sigma_Z$ ,  $t\bar{t}$ ,  $\gamma\gamma$ , etc.

Figures are from ATLAS. Similar results from CMS

# Role of assumptions in fits to the Tevatron data

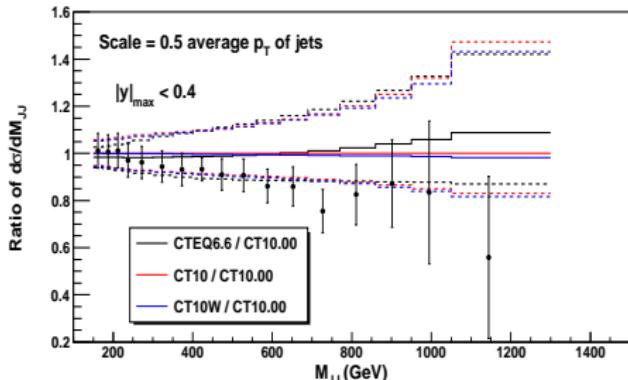
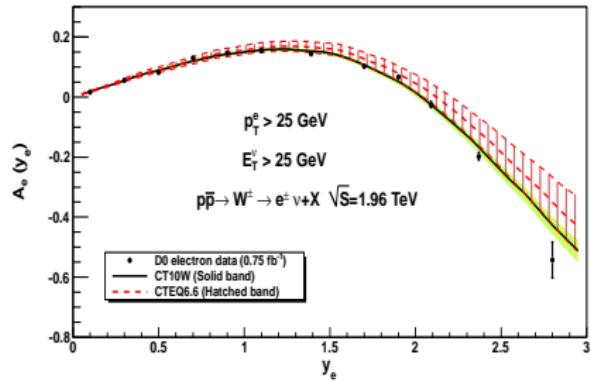
Explored by the CT10.1 analysis

- Only one bin of D0 Run-2 electron charge asymmetry  $A_e(y_e)$  with the weakest  $p_{Te}$  cut is included

- reduced theoretical uncertainty

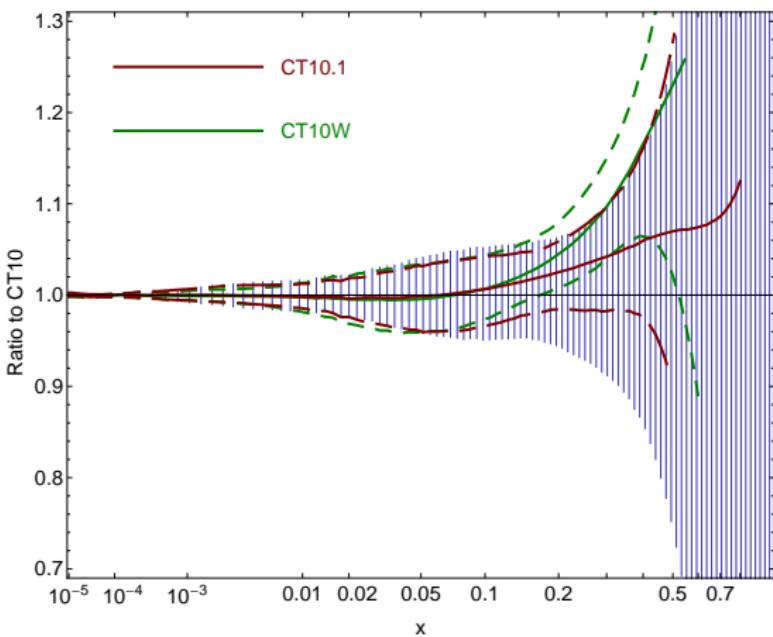
- No D0 Run-2 muon  $A_\mu(y_\mu)$  (experim. data for  $4.9 \text{ fb}^{-1}$  still preliminary)

- Fact. scale  $\mu = p_T$  (instead of  $p_T/2$ ) in Tevatron jet cross sections



# $d(x, Q)/u(x, Q)$ at $Q = 85$ GeV

d/u at Q=85. GeV  
PRELIMINARY



CT10W set:

- is fitted to 3  $p_T^e$  bins of  $A_e(y_e)$  and one bin of  $A_\mu(y_\mu)$
- prefers a larger slope of  $d/u$  than CT10
- has reduced  $d/u$  uncertainty
- shows tension with NMC, BCDMS  $F_2^{p,d}$  data

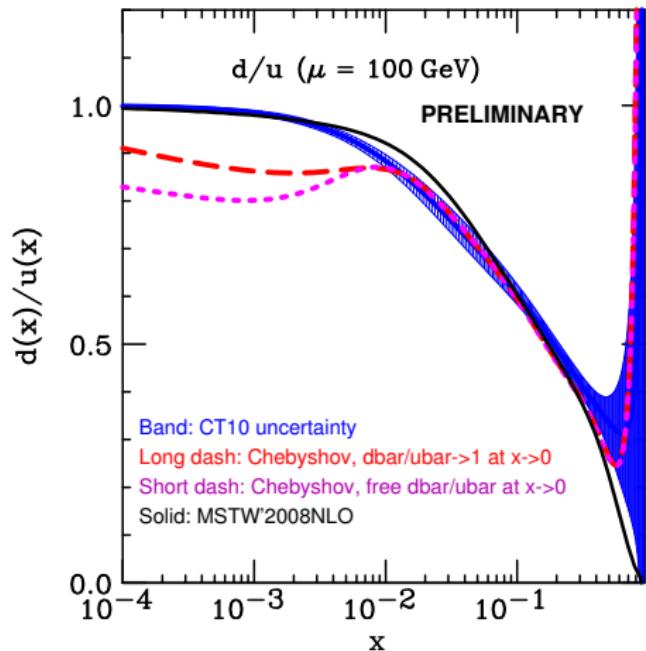
- CT10.1 is fitted only to the  $p_T^e > 25$  GeV bin of CDF Run-2  $A_e(y_e)$ ; does not include  $A_\mu(y_\mu)$ ; has a smaller  $d/u$  than CT10W

## $A_\ell(y_\ell)$ and PDF parametrization dependence

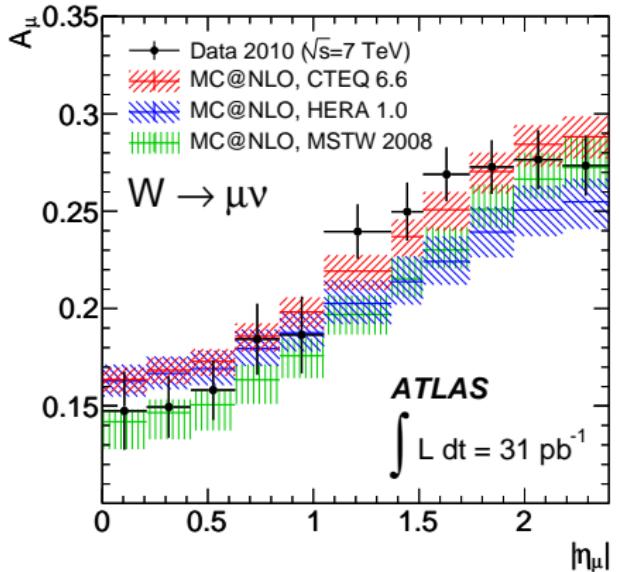
At  $x > 0.5$ , the slope of  $d/u$  is not constrained by the data.  
Existing parametrizations underestimate the PDF uncertainty on  
 $d/u$  at  $x > 0.1$  and  $\bar{u}/\bar{d}$  at  $x < 0.01$ .

PDFs based on Chebyshov polynomials improve agreement with D0 Run-2  $A_e$ , but are outside of current CTEQ/MSTW bands (*Pumplin*)

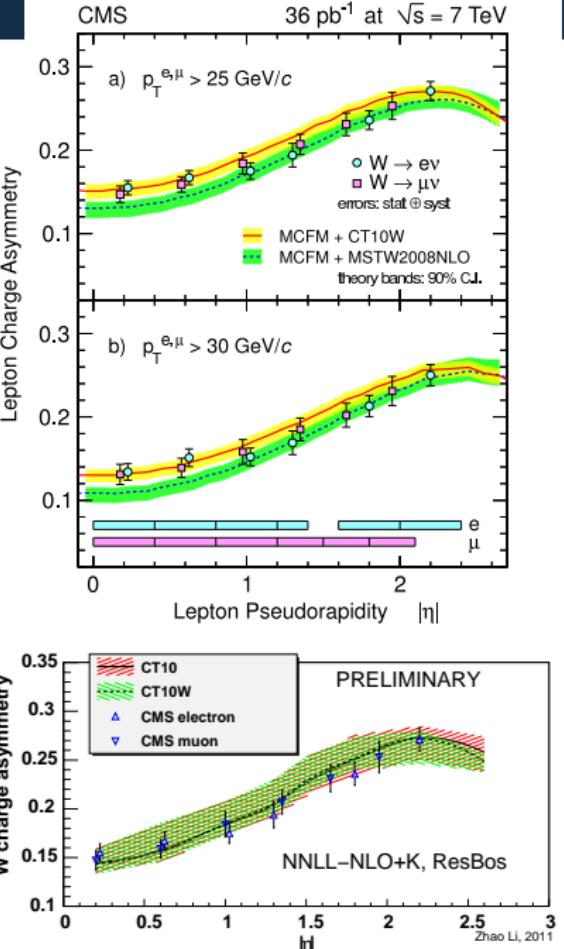
This ambiguity is reduced by  $A_\ell(y_\ell)$  at the LHC, which constrains  $d/u$  and  $\bar{d}/\bar{u}$  at  $x \sim 0.01$ .



# CT10(W) vs. $A_\ell$ at the LHC

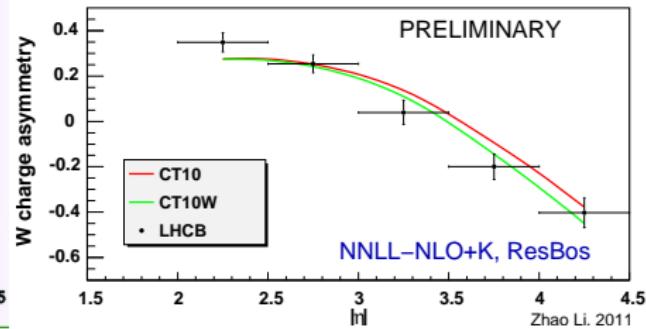
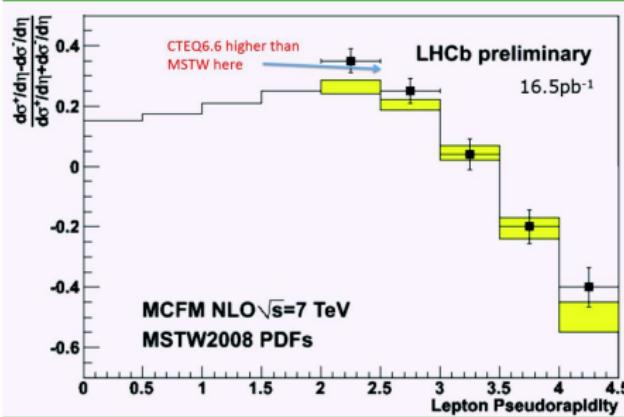


CT10(W) agrees well with the LHC  $A_\ell$ ; some differences between NLO and NNLL+NLO



# CT10(W) vs. $A_\ell$ : LHC-B

LHCb asymmetry measurement; from PDF4LHC Mar 7



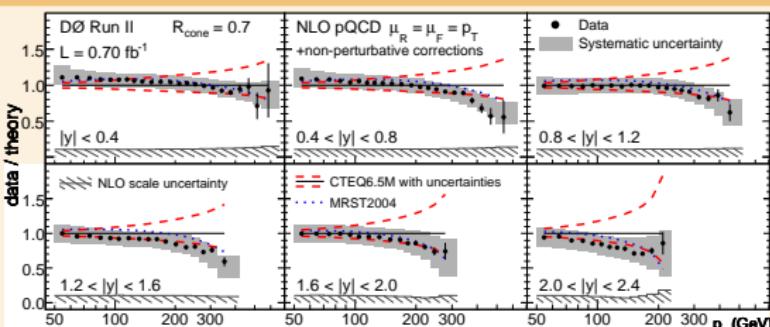
LHC-B marginally prefers CT10W to CT10

# Do CTEQ PDFs disagree with D0 (di)-jet data?

Pumplin et al., PRD 80 (2009) 014019: no significant tension between CTEQ PDFs and incl. jet data; D0 presentation exaggerates the “discrepancy”

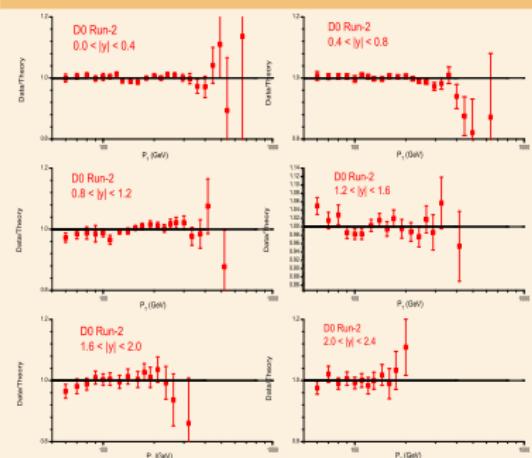
Data and NLO theory, from the D0 paper and CT09 analysis

D0 Coll., arXiv:0802.2400 (700 pb<sup>-1</sup>)



“Discrepancy”?

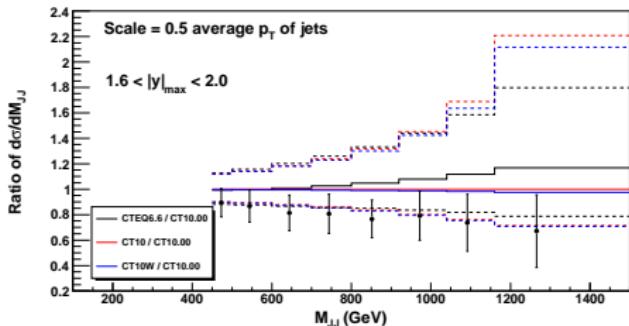
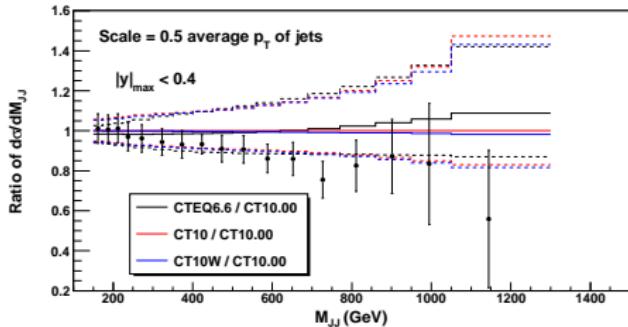
(Shifted D0-Run 2 data)/CT09



Good agreement

# Jet production: issues to consider

- Significant scale dependence
  - ▶ Comparisons to CT10 PDFs must use  $\mu = p_T^{jet}/2$ , the same scale as in the CT10 fit
- Differences between NLO codes; sensitivity to resummation of jet differential distributions  
*(Alioli et al., arXiv:1012.3380)*
- Correlated systematic shifts reconcile the data with a wider range of PDFs than in the standalone experimental analysis



# Resummation effects in (di)jet production

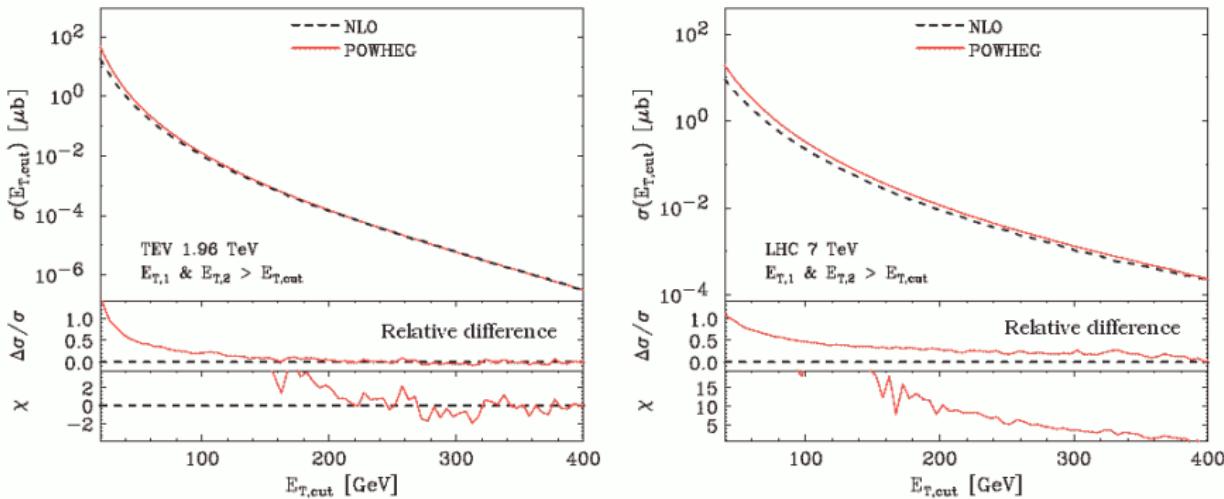


Figure 8: Predictions for the fixed-order NLO cross sections to the analogous POWHEG hardest-emission one, for symmetric cuts on the transverse energies of both the highest and second highest  $E_T$  jets, at the Tevatron and LHC, in the left- and right-hand plots respectively.

Alioli et al., arXiv:1012.3380

**Les Houches 2011 workshop:** ongoing benchmark comparisons of codes for jet cross section calculations

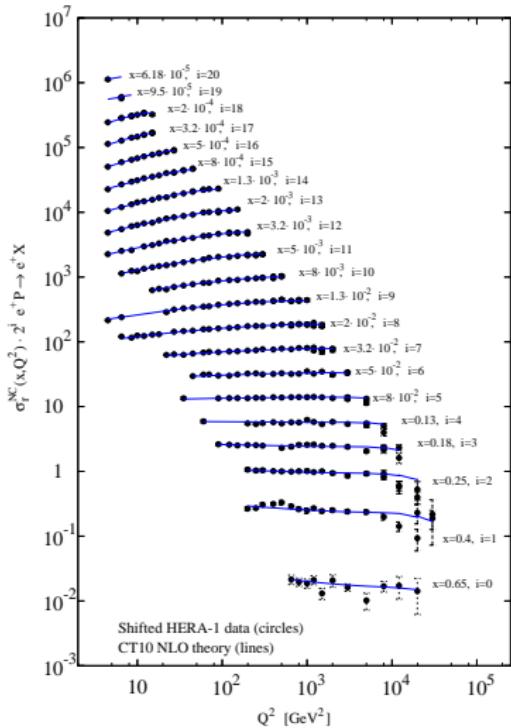
# Conclusions

- In the CTEQ-TEA fit, an NNLO calculation for  $F_{2,L}^{c,b}$  in the S-ACOT scheme is demonstrated to be viable.
- First NNLO fits are being investigated
- CT10.1: a study of new Tevatron data sets, PDF parametrization issues
- **arXiv:1101.0561**: synopsis of recent CTEQ-TEA publications
  - ▶ Search for deviations from DGLAP evolution at small  $x$  (not found); PDFs for leading-order showering programs; constraints on color-octet fermions

# Backup slides

# CT10 parton distribution functions (PRD82, 074024 (2010))

- General-purpose NLO PDFs
- include combined HERA-1 DIS and Tevatron Run-2 inclusive jet data
- detailed analysis of the Tevatron Run-2  $W$  asymmetry ( $A_\ell$ ) data
  - ▶ CT10 and CT10W sets, with different treatment of  $A_\ell$
- Additional PDF sets with a varied  $\alpha_s$  and for 3 and 4 active flavors



## Backup slides

### 1. Details on S-ACOT- $\chi$ scheme at NNLO

## S-ACOT input parameters

At  $Q \approx m_c$ ,  $F_2^c$  depends significantly on

- 1. Charm mass:**  $m_c = 1.3$  GeV in CT10
- 2. Factorization scale:**  $\mu = \sqrt{Q^2 + \kappa m_c^2}$ ;  $\kappa = 1$  in CT10
- 3. Rescaling variable**  $\zeta(\lambda)$  for matching in  $\gamma^* c$  channels

(Tung et al., hep-ph/0110247; Nadolsky, Tung, PRD79, 113014 (2009))

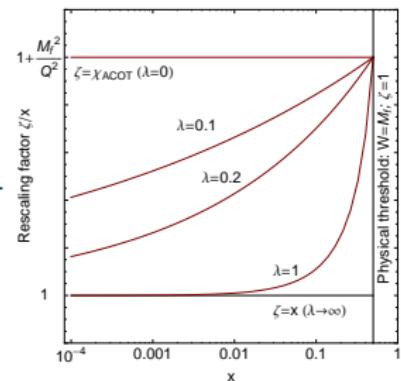
$$F_i(x, Q^2) = \sum_{a,b} \int_{\zeta}^1 \frac{d\xi}{\xi} f_a(\xi, \mu) C_{b,\lambda}^a \left( \frac{\zeta}{\xi}, \frac{Q}{\mu}, \frac{m_i}{\mu} \right)$$

$$x = \zeta / \left( 1 + \zeta^\lambda \cdot (4m_c^2)/Q^2 \right), \text{ with } 0 \leq \lambda \lesssim 1$$

CT10 uses

$$\zeta(0) \equiv \chi \equiv x \left( 1 + 4m_c^2/Q^2 \right),$$

motivated by momentum conservation



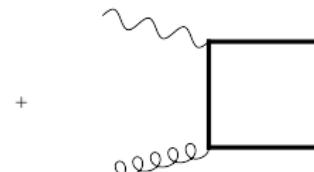
# Details of the NNLO computation

- NNLO evolution for  $\alpha_s$  and PDFs (HOPPET)
  - ▶ matching coefficients relating the PDFs in  $N_f$  and  $N_{f+1}$  schemes (*Smith, van Neerven, et al.*)
- NNLO Wilson coefficient functions for  $F_2(x, Q)$ ,  $F_L(x, Q)$
- Pole quark masses or  $\overline{MS}$  quark masses as an input
- CT10.1: pole masses  $m_c = 1.3$  GeV,  $m_b = 4.75$  GeV (as in CT10)

# Classes of Feynman diagrams I



NLO Subtraction

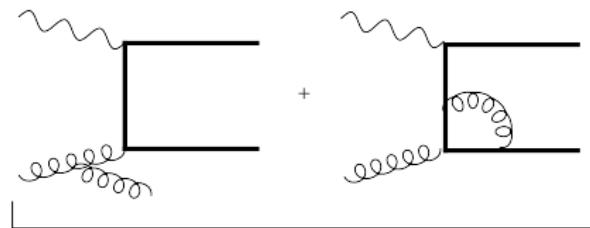


NLO  $\gamma^* g$

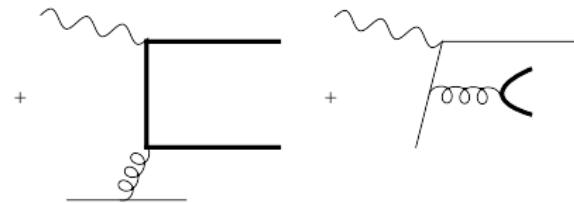


NLO  $\gamma^* c$

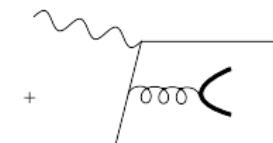
ACOT I: Phys.Rev.D50:3085–3101,1994  
ACOT II: Phys.Rev.D50:3102–3118,1994



NNLO:  $\gamma^* g$



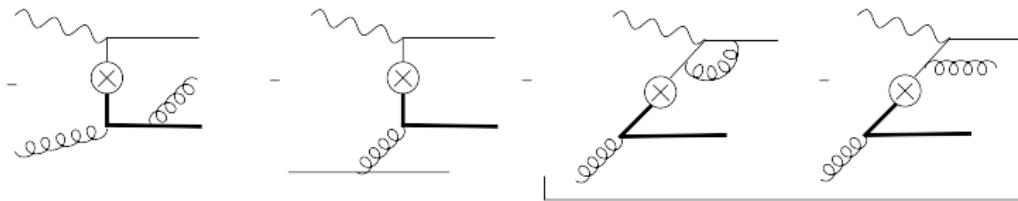
NNLO:  $\gamma^* \Sigma$



NNLO:  $\gamma^* q$  NS

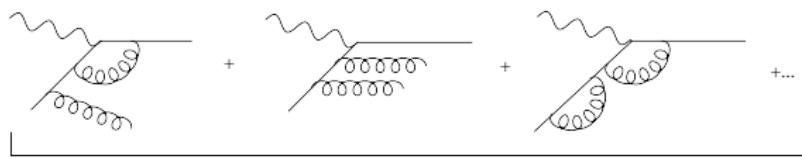
Riemersma et. al. Phys.Lett. B347 (1995)

# Classes of Feynman Diagrams II



NNLO Subtractions

Buza, Matiounine, Smith, Van Neerven, Eur. Phys. J. C 1998



NNLO  $\gamma^*$  c

Moch, Vermaseren and Vogt, Nucl.Phys.B724, 2005

# Cancellations between Feynman diagrams

Validity of the S-ACOT calculation was verified by checking for certain cancellations at  $Q \approx m_c$  and  $Q \gg m_c$

- $Q \approx m_c$ :

$$D_{C1}^{(2)} \ll D_{C0}^{(2)} \ll D_{C0}^{(1)} \leq F_2^c(x, Q)$$

- $Q \gg m_c$ :

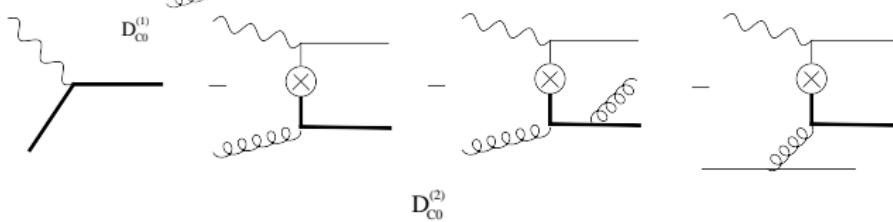
$$D_g^{(2)} \ll D_g^{(1)} < F_2^c(x, Q)$$

These cancellations are indeed observed in our results

# NNLO: Cancellations at $Q^2 \approx m_c^2$

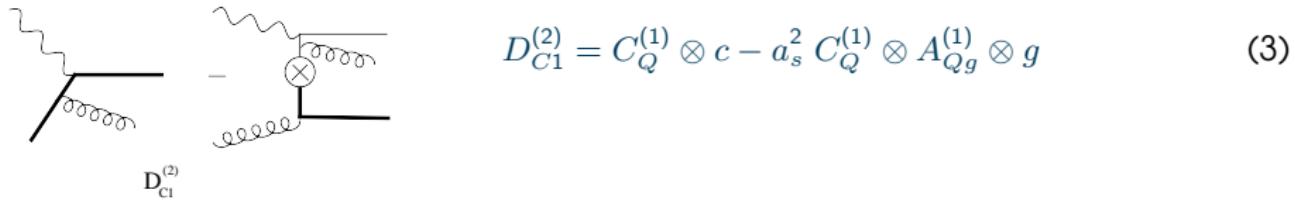


$$D_{C0}^{(1)} = C_Q^{(0)} \otimes c - a_s C_Q^{(0)} \otimes A_{Qg}^{(1)} \otimes g; \quad a_s = \frac{\alpha_s}{(4\pi)} \quad (1)$$



$$D_{C0}^{(2)}$$

$$D_{C0}^{(2)} = D_{C0}^{(1)} - a_s^2 C_Q^{(0)} \otimes A_{Qg}^{(2),S} \otimes g - a_s^2 C_Q^{(0)} \otimes A_{Q\Sigma}^{(2),PS} \otimes \Sigma \quad (2)$$

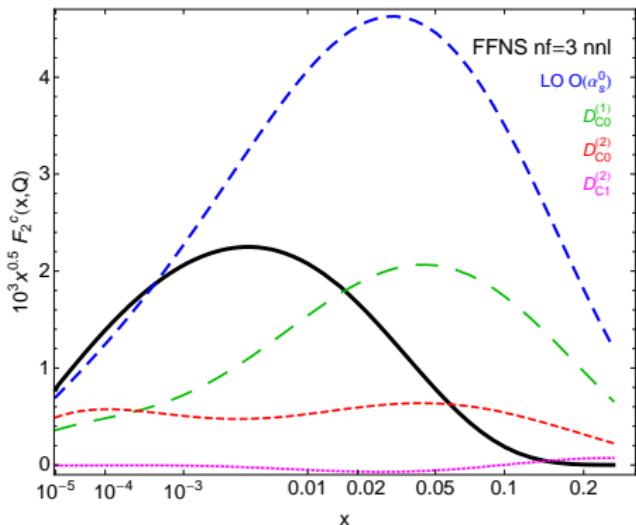


$$D_{C1}^{(2)}$$

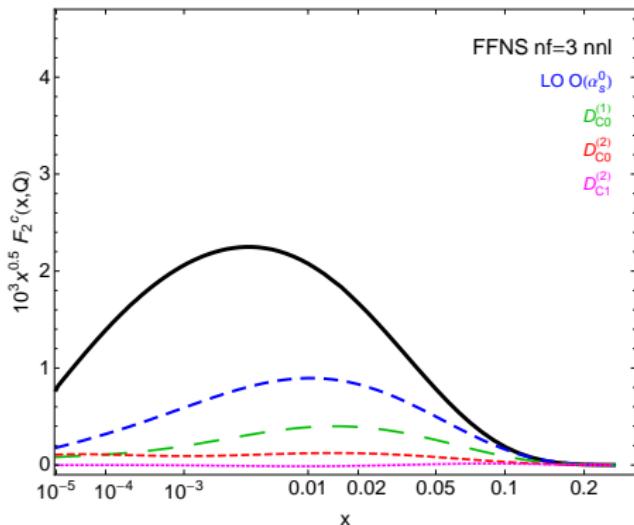
$$D_{C1}^{(2)} = C_Q^{(1)} \otimes c - a_s^2 C_Q^{(1)} \otimes A_{Qg}^{(1)} \otimes g \quad (3)$$

# NNLO: Cancellations at $Q^2 \approx m_c^2$

LH PDFs  $Q=2$  GeV  $\text{Acot}-X$   $\zeta=x$

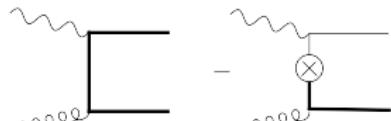


LH PDFs  $Q=2$  GeV  $\text{Acot}-\chi$   $\zeta=\chi$

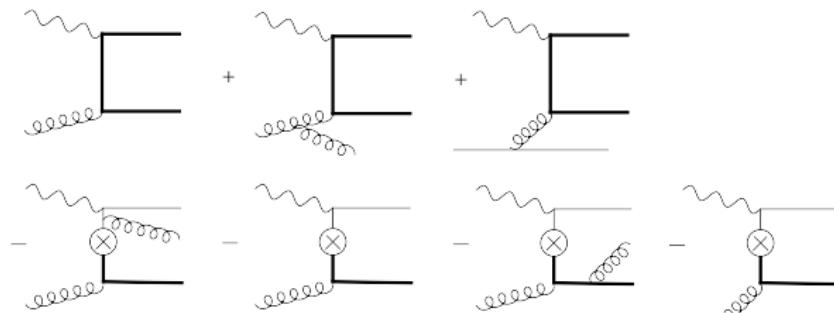


$D_{C1}^{(2)} \ll D_{C0}^{(2)} \ll D_{C0}^{(1)} \leq \text{FFN}$  at NNLO both for  $\zeta = x$  and  $\zeta = \chi$ .

# NNLO: Cancellations at $Q \gg m_c$



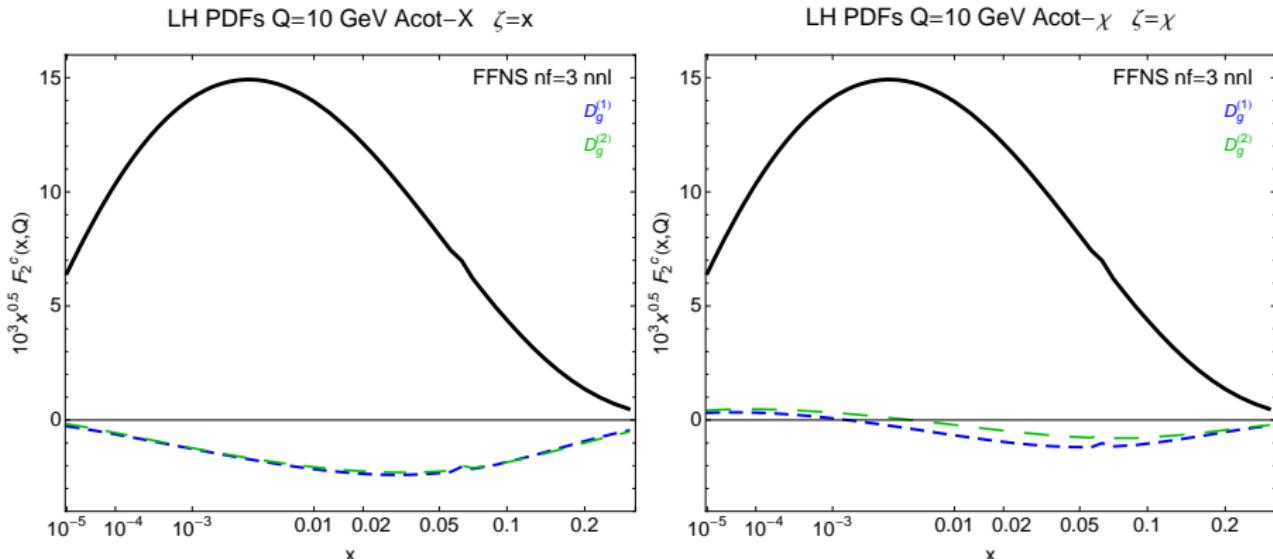
$$D_g^{(1)} \equiv C_g^{(1)} = a_s \left( F_g^{(1)} \otimes g - C_Q^{(0)} \otimes A_{Qg}^{(1),S} \otimes g \right) \quad (4)$$



$$D_g^{(2)} = D_g^{(1)} + a_s^2 \left[ \tilde{F}_g^{(2)} \otimes g + \tilde{F}_\Sigma^{(2)} \otimes \Sigma - C_Q^{(1)} \otimes A_{Qg}^{(1),S} \otimes g \right. \\ \left. - C_Q^{(0)} \otimes A_{Qg}^{(2),S} \otimes g - C_Q^{(0)} \otimes A_{Q\Sigma}^{(2),PS} \otimes \Sigma \right] \quad (5)$$

$D_g^{(1)}$  is of order of  $\alpha_s^2$  while  $D_g^{(2)}$  is of order of  $\alpha_s^3$ .

# $F_2^c$ at NNLO: Cancellations at $Q = 10$ GeV



$D_g^{(2)} \ll D_g^{(1)} < \text{FFN at NNLO} < \text{ACOT}$

$\log \frac{Q^2}{m_c^2}$  terms in FFN are cancelled well by subtractions.

# NNLO results for $F_2^{(c)}(x, Q^2)$ - Preliminary

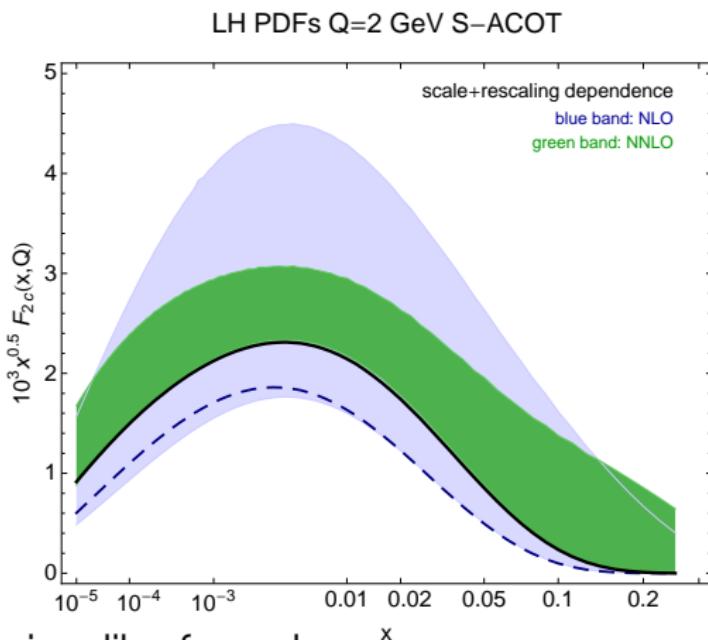
At NNLO and  $Q \approx m_c$ :

S-ACOT- $\chi$  ( $N_f = 4$ )  $\approx$  FFN ( $N_f = 3$ )  
without tuning

■ S-ACOT is numerically close to other NNLO schemes

■ NNLO expressions are close to the FONLL-C scheme

(Forte, Laenen, Nason, arXiv:1001.2312).



■ ACOT formalism provides recipe-like formulas for implementing NNLO in the GM scheme

■ Dependence on rescaling is also reduced

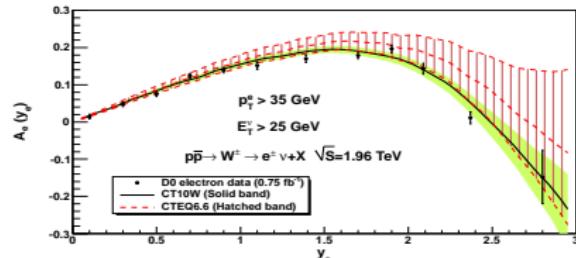
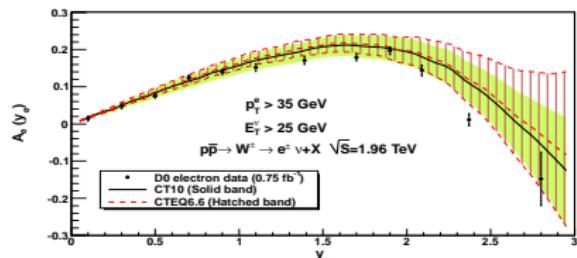
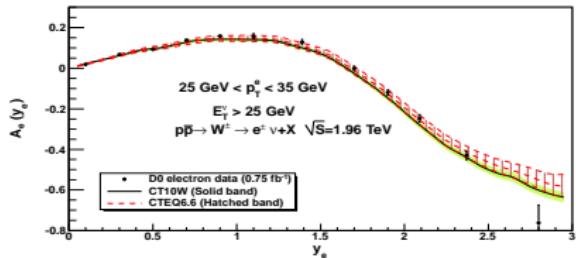
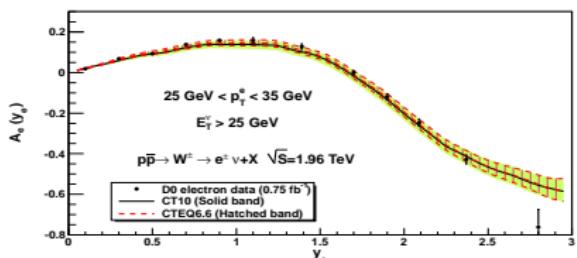
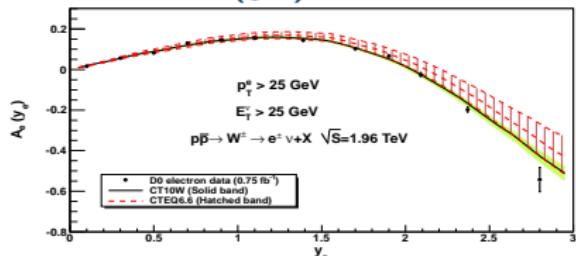
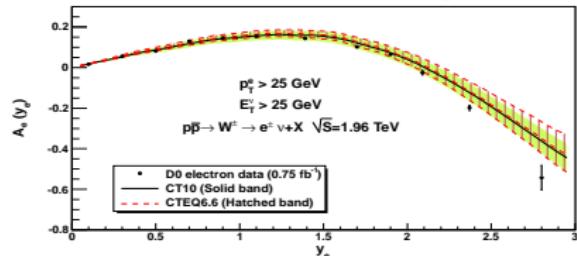
## Backup slides

### 2. $W$ charge asymmetry

## CT10(W): radiative contributions to $A_\ell(y_\ell)$

- **Default calculation:**  $A_\ell(y)$  at NNLL-NLO, using lookup tables for  $\sigma(p_T^\ell, y_\ell)_{NNLL+NLO}/\sigma(p_T^\ell, y_\ell)_{LO}$  from ResBos (*Balazs, Yuan, PRD 56, 5558 (1997); Landry, Brock, P.N. Yuan, PRD67, 073016 (2003)*).
- **Cross check:** include NNLO corrections at  $Q_T \approx M_W$  (*Arnold & Reno, 1989*);  $A_\ell(y_\ell)$  changes by a few percent at the highest  $y_\ell$  and  $p_T > 35$  GeV
  - ▶ magnitude of changes is comparable with full NNLO terms (*Catani, Ferrera, and Grazzini, JHEP 05, 006 (2010)*)
  - ▶ changes are small compared to the experimental errors

# CT10 and CT10W predictions for $A_e(y_e)$ (D0 Run-2)



# CDF Run-2 and D0 Run-2 $W$ lepton asymmetry

- CT10 does not include the Run-2  $A_\ell \Rightarrow$  disagrees with  $A_\ell$ , due to tension between  $A_\ell$  and DIS  $F_2^d/F_2^p$ .
- CT10W includes 3  $p_{T\ell}$  bins of the electron  $A_e(y_e)$  and one bin of  $A_\mu(y_\mu)$  from D0 Run-2 (2008).
- CT10.1 includes only the  $p_T > 25$  bin of  $A_e(y_e)$
- Many other PDFs fail.

Agreement of PQCD with D0 $A_e(y_e)$	$\chi^2/npt$	Source or comments
CTEQ6.6, NLO	191/36=5.5	<i>Our study; Resbos, NNLL-NLO</i>
<b>CT10W, NLO</b>	<b>78/36=2.2</b> <b>With <math>A_\mu(y_\mu)</math>: 88/47=1.9</b>	
ABKM'09, NNLO	540/24=22.5	<i>Catani, Ferrera, Grazzini, JHEP 05, 006 (2010)</i>
MSTW'08, NNLO	205/24=8.6	
JR09VF, NNLO	113/24=4.7	

## Why difficulties with fitting $A_\ell(y_\ell)$ ?

1.  $A_\ell(y_\ell)$  is very sensitive to the average slope  $s_{du}$  of  $d(x, M_W)/u(x, M_W)$

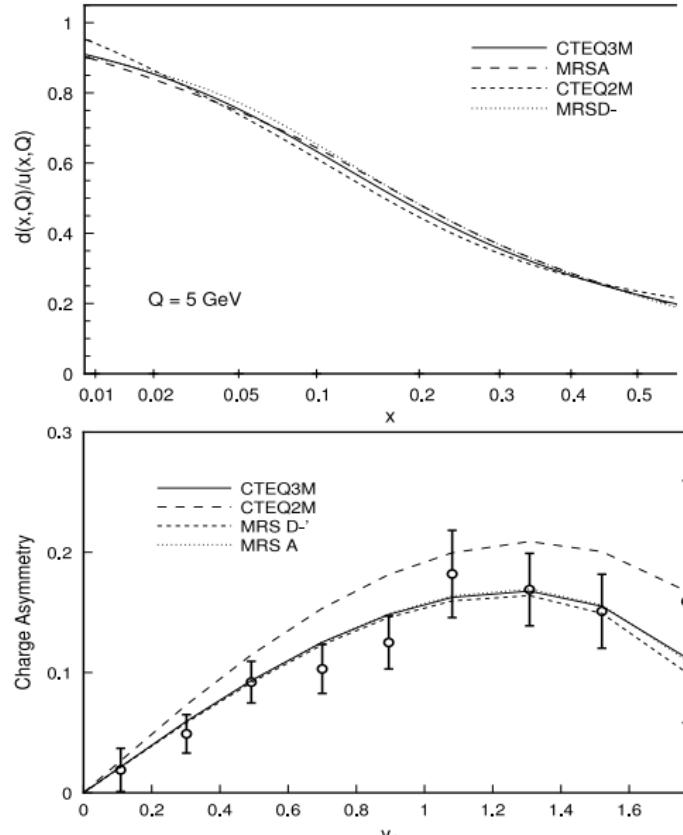
$$A_\ell(y_\ell) \sim A_\ell(y_W)|_{LO} \propto \frac{1}{x_1 - x_2} \left[ \frac{d(x_1)}{u(x_1)} - \frac{d(x_2)}{u(x_2)} \right]; \quad x_{1,2} = \frac{Q}{\sqrt{s}} e^{\pm y_W}$$

Berger, Halzen, Kim, Willenbrock, PRD 40, 83 (1989); Martin, Stirling, Roberts, MPLA 4, 1135 (1989); PRD D50, 6734 (1994);  
Lai et al., PRD 51, 4763 (1995)

2. Constraints on  $s_{du}$  by fixed-target  $F_2^d(x, Q)/F_2^p(x, Q)$  are affected by nuclear and higher-twist effects

Accardi, Christy, Keppel, Monaghan, Melnitchouk, Morfin, Owens, PRD 81, 034016 (2010)

# Challenges with fitting $A_\ell(y_\ell)$



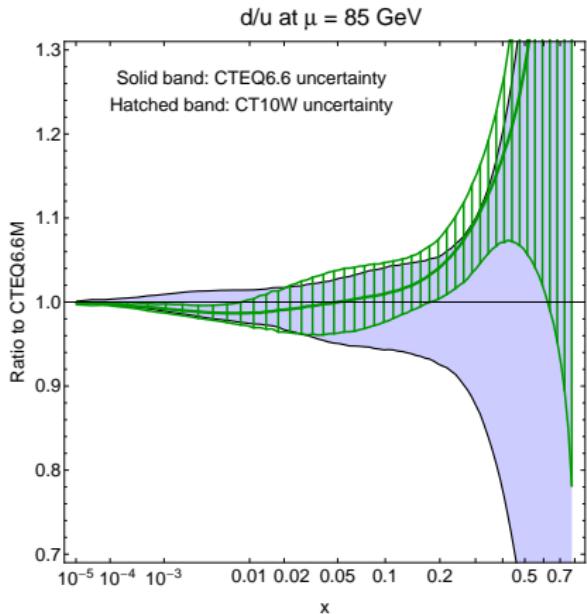
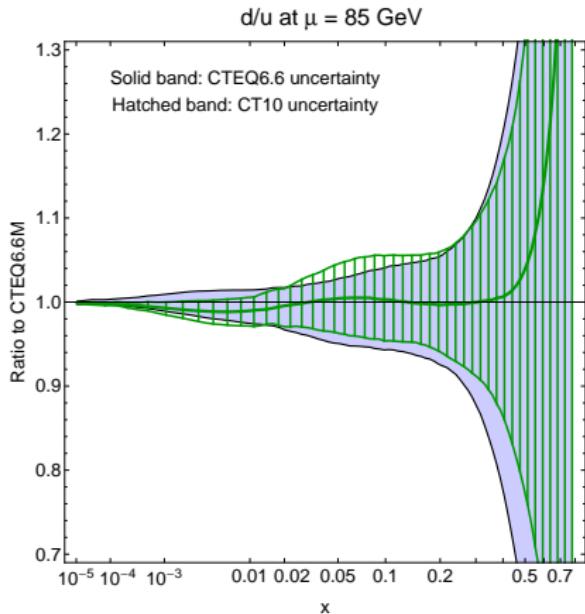
Small changes in  $s_{du}$  cause significant variations in  $A_\ell$

Lai *et al.*, PRD 51, 4763 (1995)

Alternative constraints on  $d/u$  by  $F_2^d(x,Q)/F_2^p(x,Q)$  from fixed-target DIS are affected by nuclear and higher-twist effects

Accardi, Christy, Keppel, Monaghan, Melnitchouk, Morfin, Owens, PRD 81, 034016 (2010)

# $d(x, Q)/u(x, Q)$ at $Q = 85$ GeV



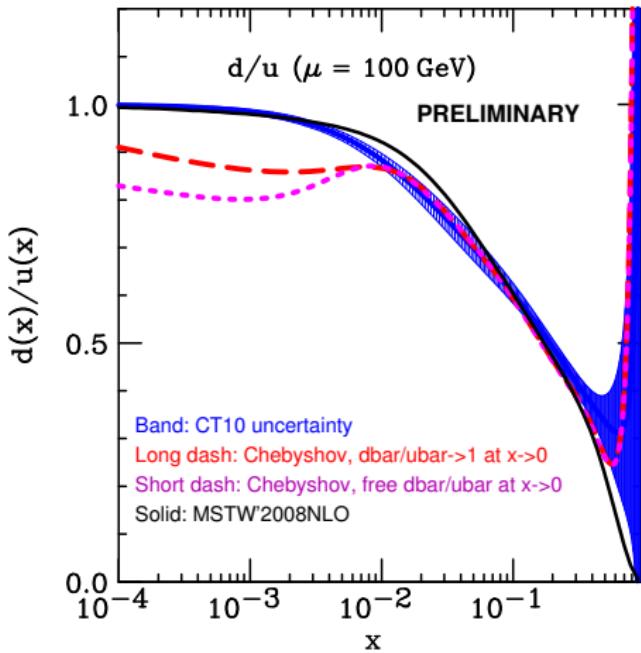
- CT10W prefers a larger slope of  $d/u$ , has a smaller uncertainty than CTEQ6.6 or CT10
- CT10W shows tension with NMC, BCDMS  $F_2^{p,d}$  data

## Why difficulties with fitting $A_\ell(y_\ell)$ ?

3. Existing parametrizations underestimate the PDF uncertainty on  $d/u$

PDFs based on Chebyshov polynomials improve agreement with D0 Run-2  $A_e$ , but are outside of current CTEQ/MSTW bands (*Pumplin*)

This ambiguity is reduced by  $A_\ell(y_\ell)$  at the LHC, which constrains  $d/u$  and  $\bar{d}/\bar{u}$  at  $x \sim 0.01$ .



## Why difficulties with fitting $A_\ell(y_\ell)$ ?

4. Experimental  $A_\ell$  with lepton  $p_{T\ell}$  cuts is sensitive to  $d\sigma/dq_T$  of  $W$  boson at transverse momentum  $q_T \rightarrow 0$ .

- Fixed-order (N)NLO calculations (DYNNLO, FEWZ, MCFM,...) predict a wrong shape of  $d\sigma/dq_T$  at  $q_T \rightarrow 0$ .
- Small- $q_T$  resummation correctly predicts  $d\sigma/dq_T$  in this limit.
- CT10(W) PDFs are fitted using a NNLL-NLO+K resummed prediction for  $A_\ell$  (ResBos); **must not be used with fixed-order predictions for  $A_\ell$** .

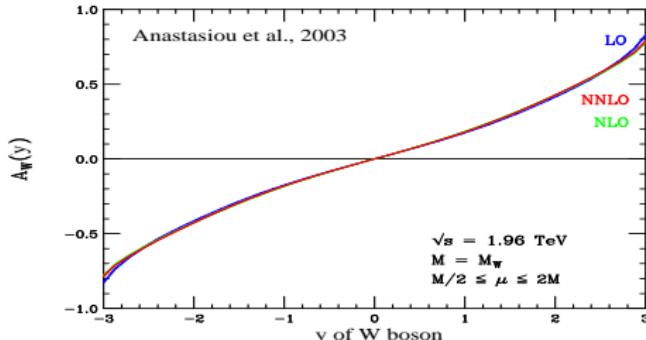
For example:

$$\chi^2(\text{CT10W+ResBos}) = 1.9 N_{pt \text{ (us)}};$$

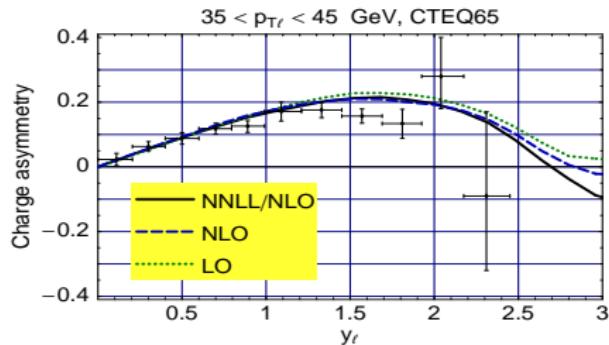
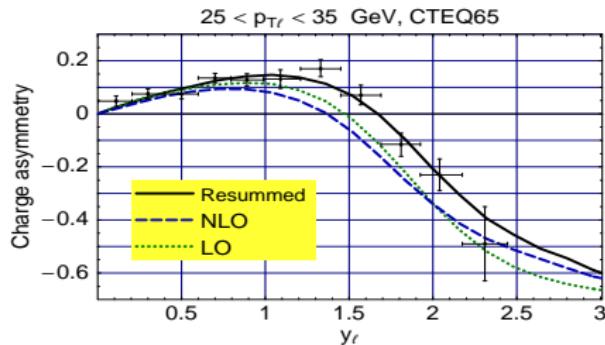
$$\chi^2(\text{CT10W+DYNLL}) = 8.4 N_{pt \text{ (NNPDF)}}$$

# Charge asymmetry in $p_T^e$ bins (CDF Run-2, 207 pb $^{-1}$ )

Without the  $p_T^e$  cut (FEWZ):

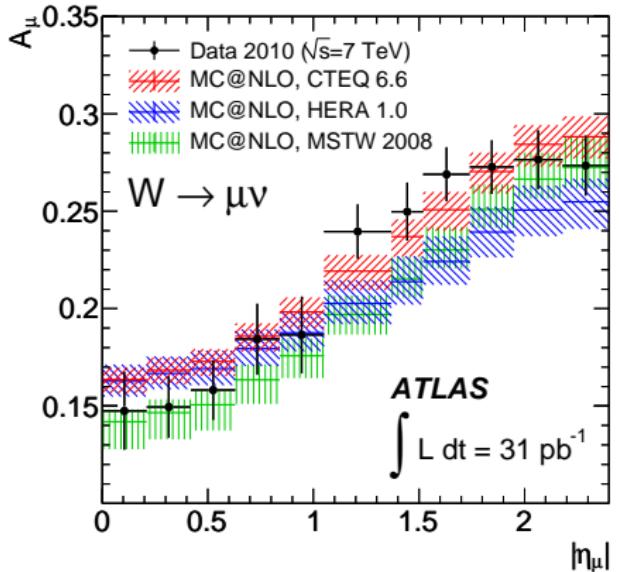


With  $p_{Te}$  cuts imposed,  $A_{ch}(y_e)$  is sensitive to small- $Q_T$  resummation

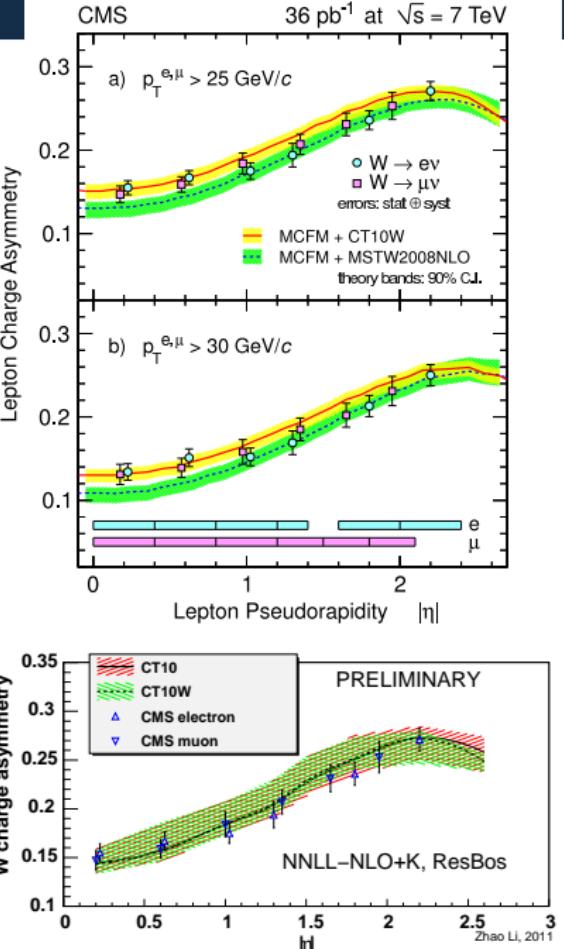


PN, 2007, unpublished; arXiv:1101.0561

# CT10(W) vs. $A_\ell$ at the LHC

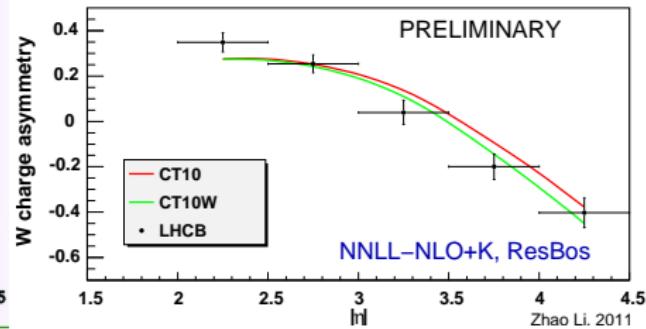
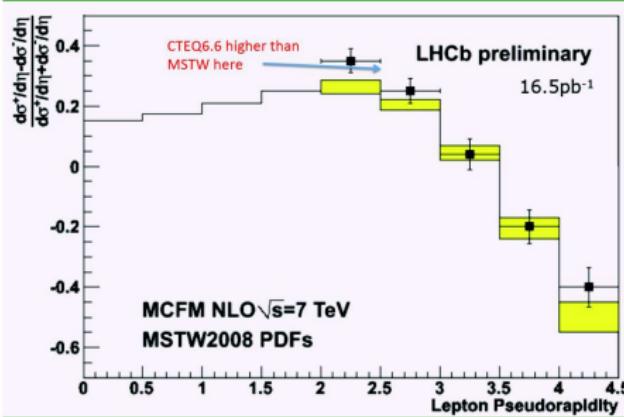


CT10(W) agrees well with the LHC  $A_\ell$ ; some differences between NLO and NNLL+NLO



# CT10(W) vs. $A_\ell$ : LHC-B

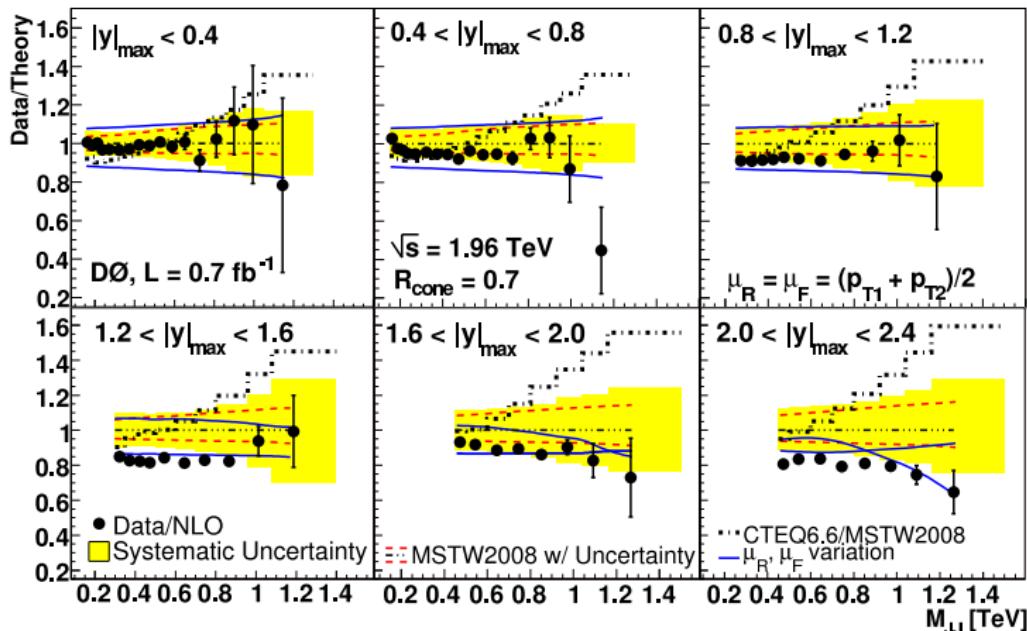
LHCb asymmetry measurement; from PDF4LHC Mar 7



LHC-B marginally prefers CT10W

# Dijet mass distributions from D0 Run-2

0.7  $\text{fb}^{-1}$ , arXiv:1002.4594

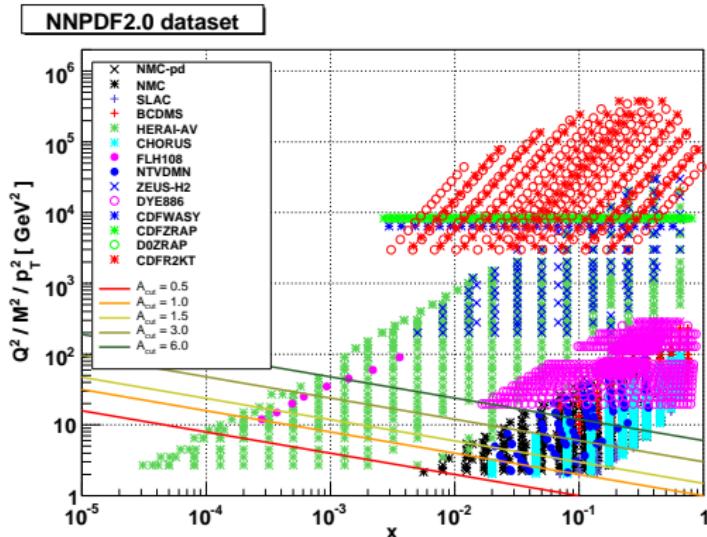


The data appear to disfavor CTEQ6.x/CT10 NLO predictions, for the selected theory parameters

## Backup slides

### 3. Search for deviations from DGLAP evolution at small $x$ and $Q$

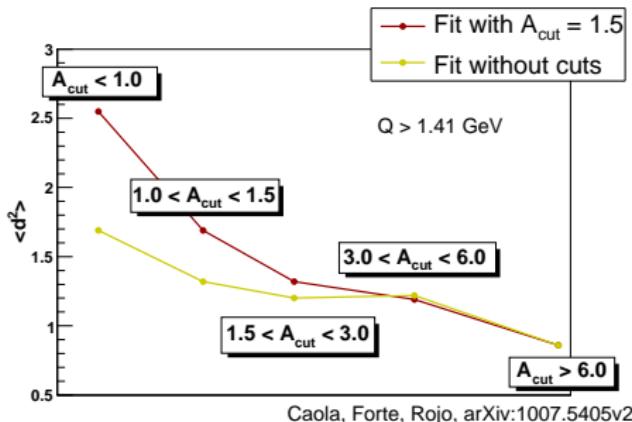
# $A_{cut}$ fits to combined HERA data



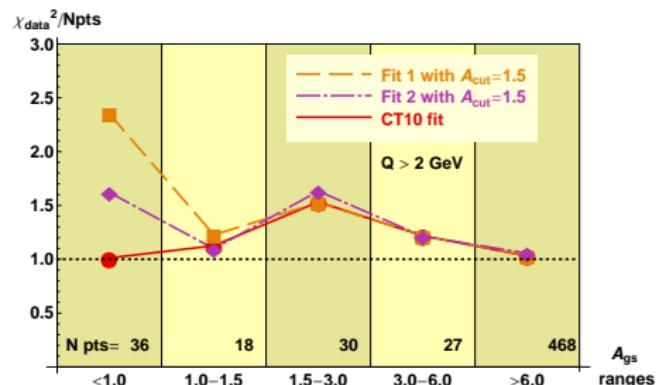
## Fitting procedure:

- Include only DIS data above an  $A_{cut}$  line
- Compare the resulting PDFs with DIS data below the  $A_{cut}$  line, in a region that is “connected” by DGLAP evolution

# CT10: $A_{cut}$ fits to DIS data at $Q > Q_0 = 2$ GeV



Caola, Forte, Rojo, arXiv:1007.5405v2

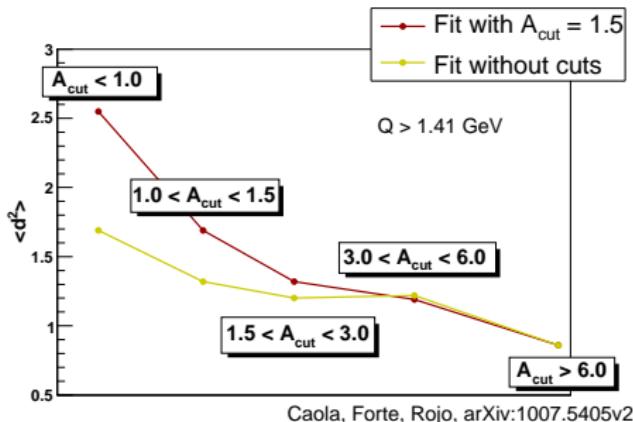


## Motivation

Search for deviations from DGLAP evolution at smallest  $x$  and  $Q$

- Follow the procedure proposed by NNPDF (Caola, Forte, Rojo, arXiv:1007.5405)

# CT10: $A_{cut}$ fits to DIS data at $Q > Q_0 = 2$ GeV

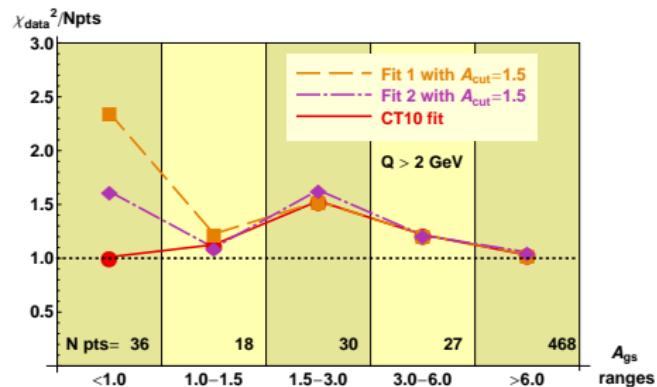


Caola, Forte, Rojo, arXiv:1007.5405v2

## CT10

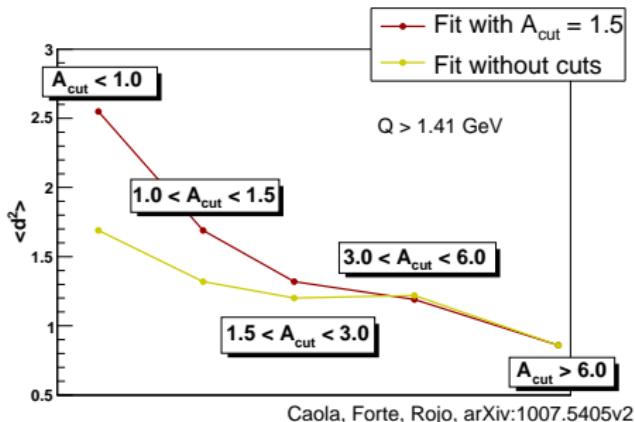
Two CT10-like fits to data at  $A_{gs} > 1.5$ , with different parametrizations of  $g(x, Q)$

$$\chi_i^2 = \frac{(\text{Shifted Data} - \text{Theory})^2}{\sigma_{uncor}^2}$$

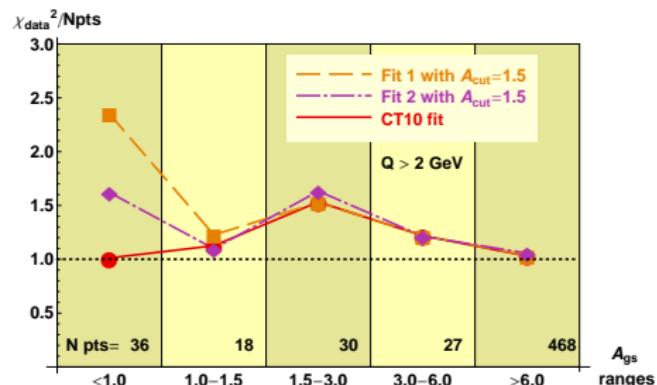


Large syst. shifts at  $A_{gs} < 1.0$ , in a pattern that could mimic a slower  $Q^2$  evolution

# CT10: $A_{cut}$ fits to DIS data at $Q > Q_0 = 2$ GeV



Caola, Forte, Rojo, arXiv:1007.5405v2



## CT10, cont.

$\delta\chi^2 \sim 0$  at  $A_{gs} > 1.0$   
**(no difference)**

$\delta\chi^2 = 0 - 1.5$  at  $A_{gs} < 1.0$ ,  
**with large uncertainty**

⇒ Disagreement with the “DGLAP-connected” data at  $A_{gs} < A_{cut}$  is not supported by the CT10 fit