

Session IV : Beyond axions

(More fundamental physics with axion technologies)

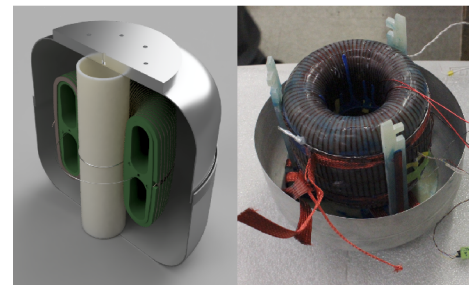
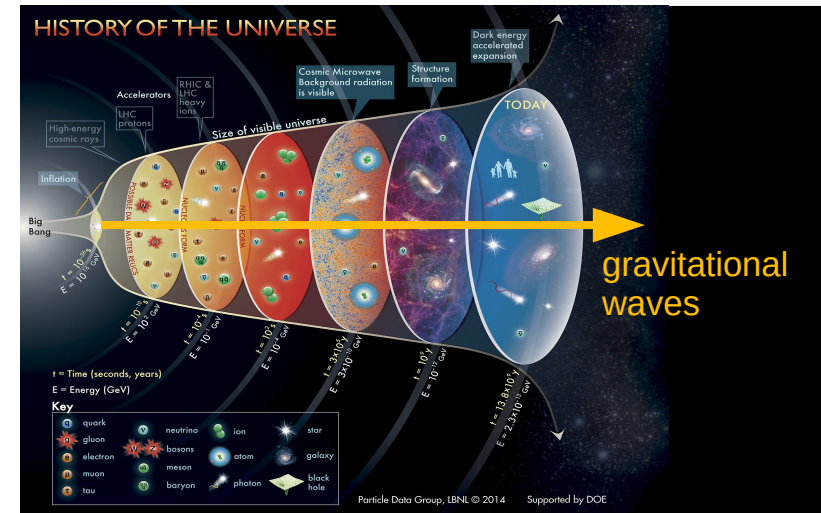
Axionfest DESY: Axions beyond the DM paradigm

Jan 29 - 31, 2024

- Overview: High frequency GW searches with axion detectors Valerie Domcke
- Overview: Vacuum magnetic birefringence Laura Roberts
- High frequency GW @ ALPs Aldo Ejili
- Vacuum magnetic birefringence searches @ ALPs Aaron Spector
- Polarometry for DM (pseudo)scalar searches Qazal Rokn
- **More** questions and discussion **Everyone**

High frequency GW searches with axion detectors

- UHF GW sources
- Theory of GW to photon conversion
- recasting axion bounds



high frequency ($> \text{kHz}$) GW sources

Cosmological

- sourced by violent cosmological event in the early Universe
- stochastic GW background (SGWB): stationary, isotropic, broad spectrum
- GW frequency determined by Hubble horizon at sourcing time
→ high frequency = early Universe
- observationally bounded by BBN and CMB (extra radiation)
- vanilla cosmology: SGWB from cosmic inflation & CGWB very small. But in many BSM models, saturating BBN bound is easy

Astrophysical

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Astrophysical

- localized GW sources, both coherent and incoherent signals possible
- no known astrophysical objects emit (significantly) in UHF band
- eg mergers of light primordial black holes or exotic compact objects, superradiance
- large signals require near-by events
→ rare events with GW strain far above BBN bound are possible
- SGWB from unresolved sources, typically harder to detect

UHF GW searches are always a search for New Physics

high frequency ($> \text{kHz}$) GW sources

Cosmological

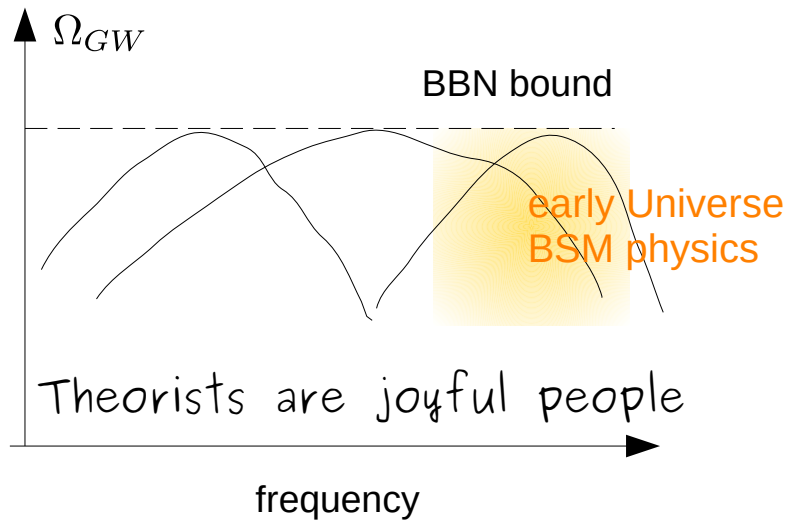
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Astrophysical

- localized GW sources, both coherent and incoherent signals possible
- no known astrophysical objects emit (significantly) in UHF band
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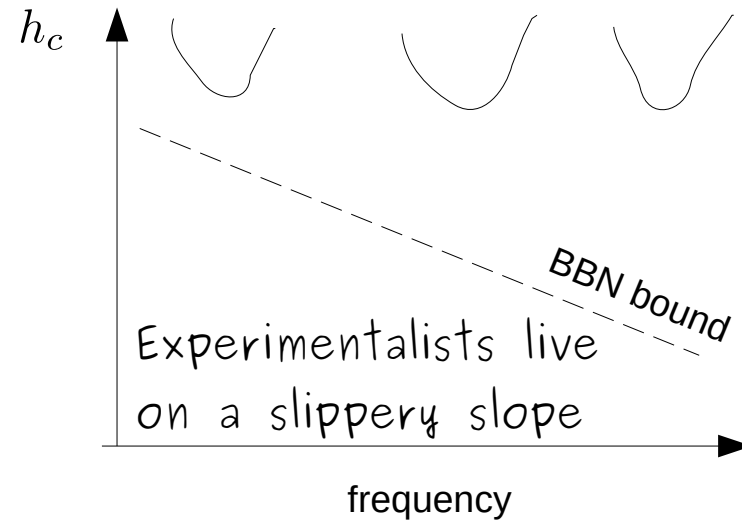
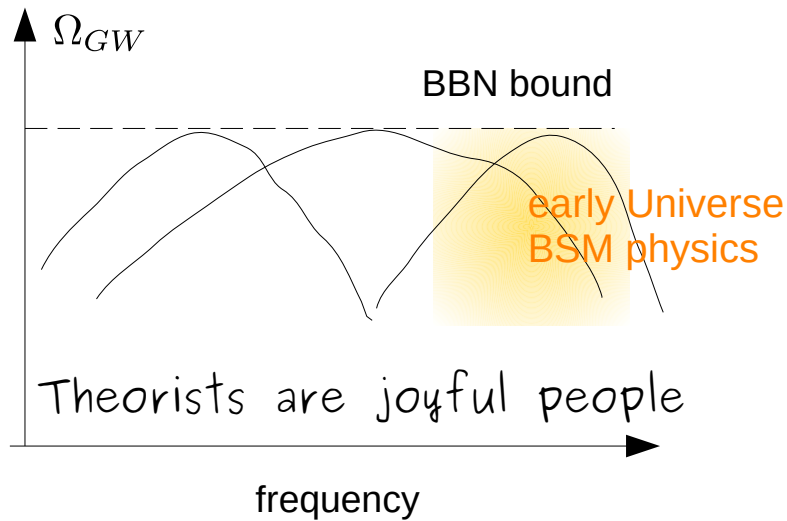
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challenges in UHF GW detection



CMB/BBN bound constrains energy

challenges in UHF GW detection



$$\Omega_{GW} \propto f^2 h_c^2$$

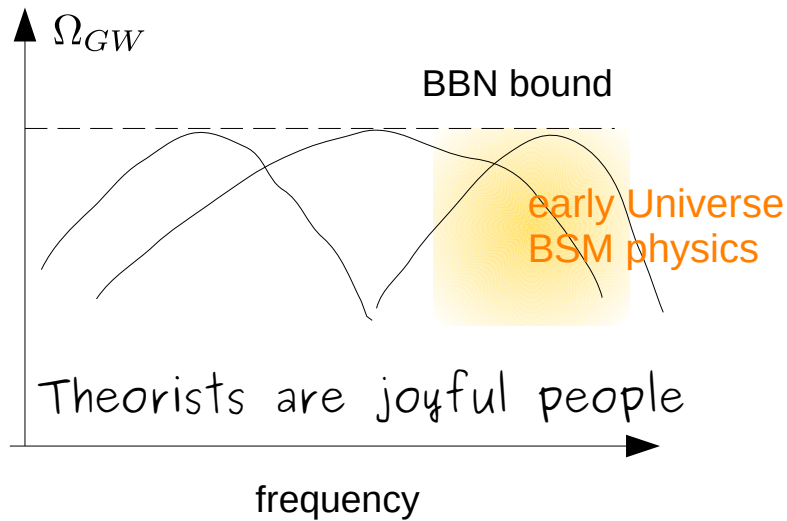
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experiments measure displacement

UHF GW initiative: <https://www.ctc.cam.ac.uk/activities/UHF-GW.php>

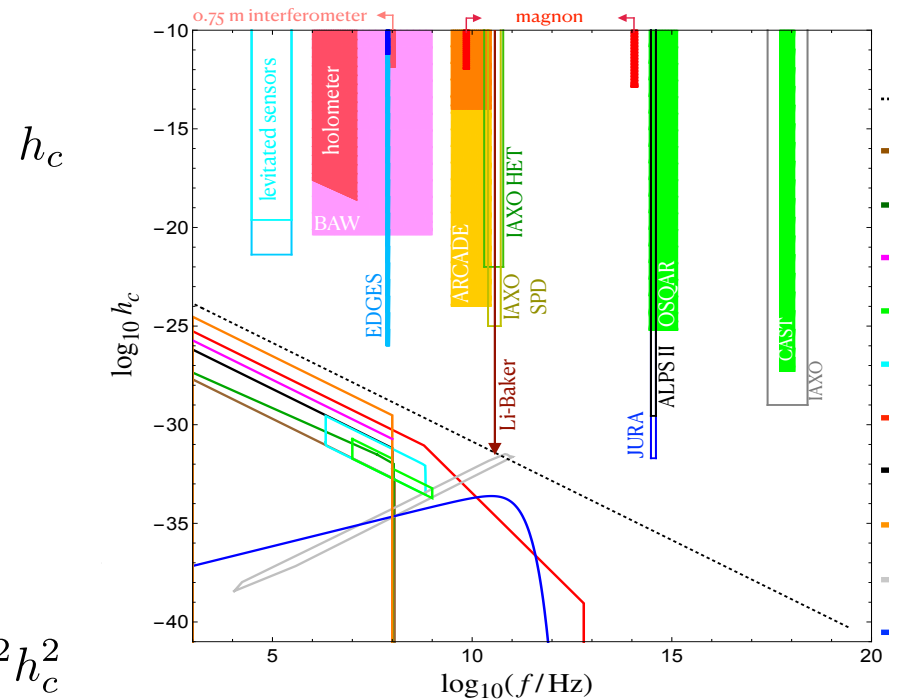
Living Review on sources & detectors: <https://arxiv.org/abs/2011.12414>

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GW electrodynamics

Classical electrodynamics + linearized GR, $g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$: Landau Lifshitz, ...

$$\partial_\nu F^{\mu\nu} = j_{\text{eff}}^\mu = (-\nabla \cdot \mathbf{P}, \nabla \times \mathbf{M} + \partial_t \mathbf{P})$$

$$\partial_\nu \tilde{F}^{\mu\nu} = 0$$

effective current
effective polarization vector
effective magnetization vector

with

$$P_i = -h_{ij}E_j + \frac{1}{2}hE_i + h_{00}E_i - \epsilon_{ijk}h_{0j}B_k,$$

$$M_i = -h_{ij}B_j - \frac{1}{2}hB_i + h_{jj}B_i + \epsilon_{ijk}h_{0j}E_k,$$

induced at linear order in h
in presence of external E,B field
VD, Garcia-Cely, Rodd `22

Direct analogy with axion electrodynamics

$$\mathcal{L} \supset g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B} \quad \rightarrow \quad \mathbf{P} = g_{a\gamma\gamma} a \mathbf{B}, \quad \mathbf{M} = g_{a\gamma\gamma} a \mathbf{E}$$

McAllister et al `18
Tobar, McAllister, Goryachev `19
Ouellet, Bogorad `19

effective source terms in Maxwell's equation due to GW

GW – EM oscillations

(inverse) Gertsenshtein effect:

[Gertsenshtein '62, Boccaletti et al '70, Raffelt, Stodolsky '88]

include backreaction of EM on Einsteins equations:

$$(\square + \omega_{\text{pl}}^2/c^2) A_\lambda = -B \partial_z h_\lambda, \quad \square h_\lambda = \kappa^2 B \partial_z A_\lambda$$

A_λ = photon

h_λ = GW

B = ext. transv. B - field

ω_{pl} = plasma frequency

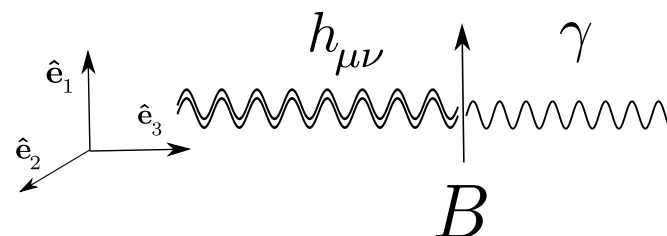
$$\mu^2 = 1 - \omega_{\text{pl}}^2/\omega^2$$

plane waves:

$$\rightarrow \psi(t, z) \equiv \begin{pmatrix} \sqrt{\mu} A_\lambda \\ \frac{1}{\kappa} h_\lambda \end{pmatrix} = e^{-i\omega t} e^{iKz} \psi(0, 0),$$

$$K = \begin{pmatrix} \frac{\mu}{c} \sqrt{\omega^2 + \left(\frac{\kappa B}{1+\mu}\right)^2} & -i \frac{\sqrt{\mu} \kappa B}{1+\mu} \\ i \frac{\sqrt{\mu} \kappa B}{1+\mu} & \frac{1}{c} \sqrt{\omega^2 + \left(\frac{\kappa B}{1+\mu}\right)^2} \end{pmatrix}$$

EM wave in curved space time
(i.e. classical linearized general
relativity) \rightarrow purely SM process

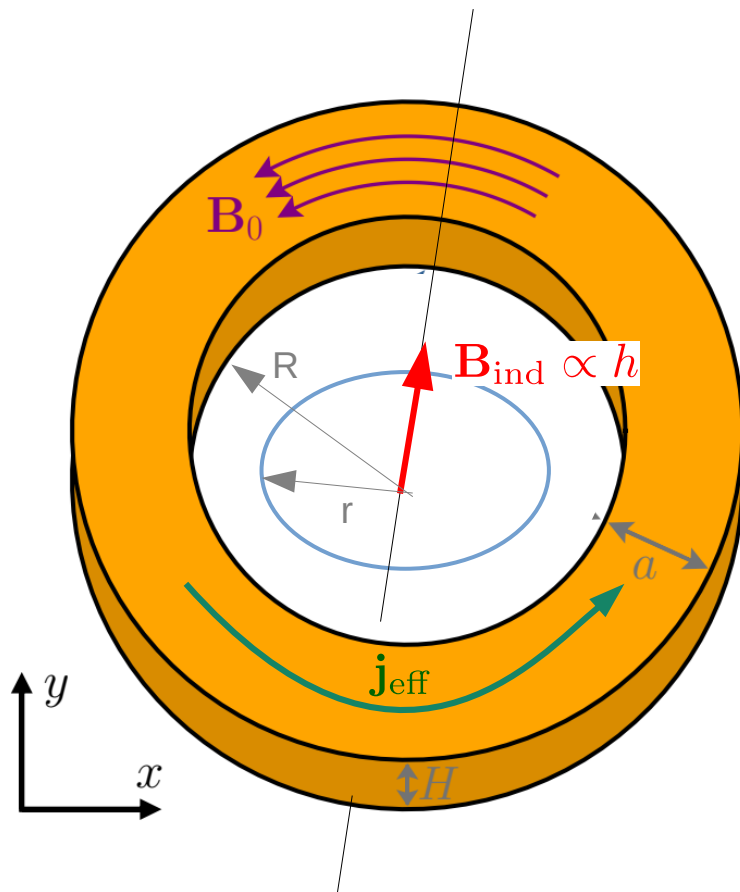


analogous to axion to photon conversion

low mass axion haloscopes

eg ABRACADABRA, SHAFT, DM Radio:

VD, Garcia-Cely, Rodd '22



static magnetic field (i.e. rigid detector)

effective current

induced oscillating magnetic field

measure magnetic flux ($\sim h$)
through pickup loop

at leading order in (ωR) :

$$\Phi_{\text{gw}} = \frac{i e^{-i\omega t}}{16\sqrt{2}} h \times \omega^3 B_0 \pi r^2 R a (a + 2R) s_{\theta_h}^2$$

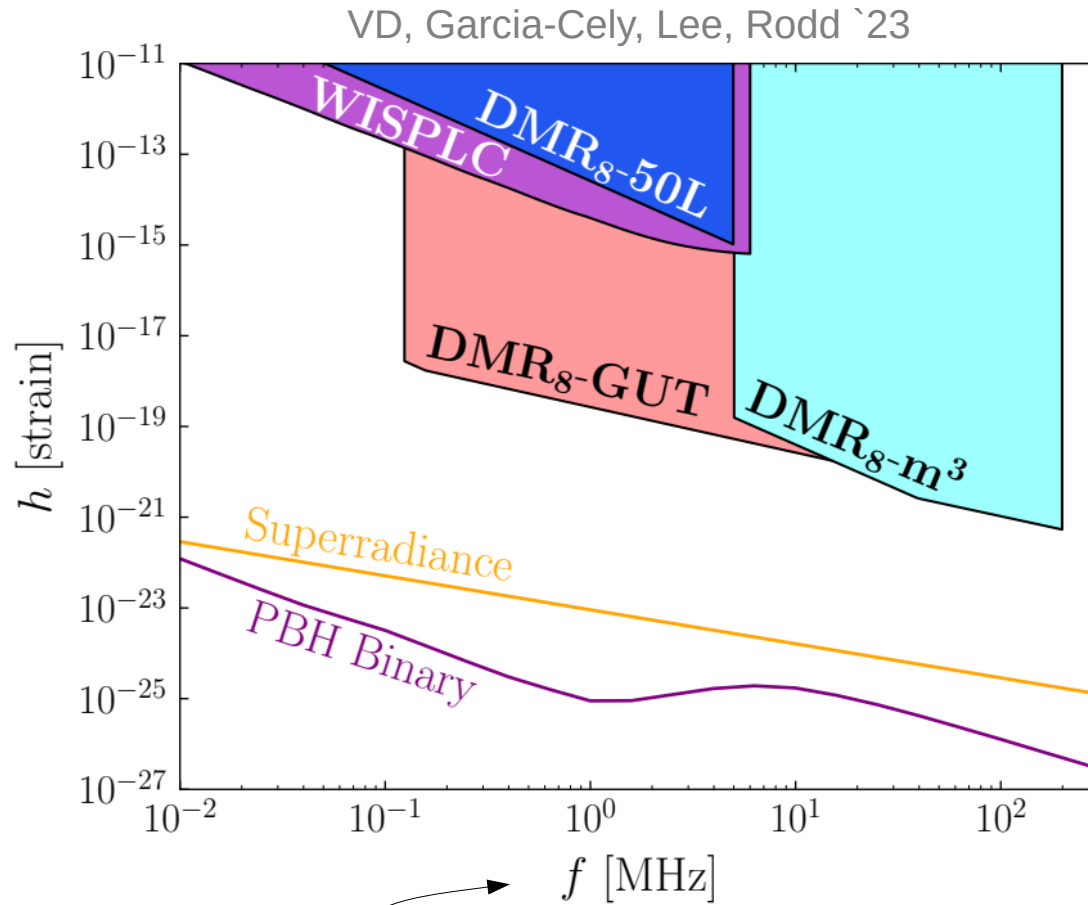
$$\sim (\omega L)^3 h B_0 L^2$$

$$\Phi_a = e^{-i\omega t} g_{a\gamma\gamma} \sqrt{2\rho_{\text{DM}}} B_0 \pi r^2 R \ln(1 + a/R)$$

$$\sim (\omega L) g_{a\gamma\gamma} B_0 L^2$$

match to axion induced flux to recast
axion-photon coupling bounds as GW bounds:

Low mass haloscopes



$$\Phi_h(h^+, h^\times; \phi_h, \theta_h) = \mathcal{R}_c \Phi_a(g_{a\gamma\gamma}),$$

coherence ratio factor:
coherence & observation time

← sensitivity to signal with
 $\mathcal{R}_c = 1$

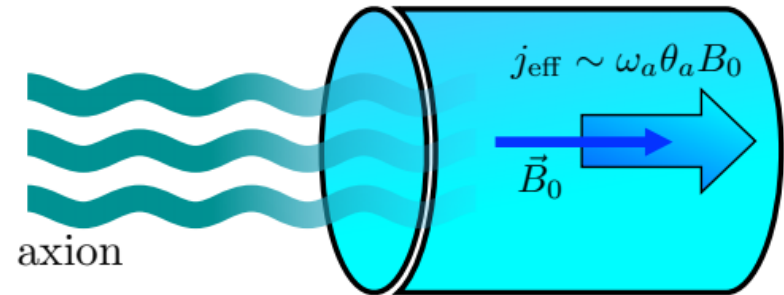
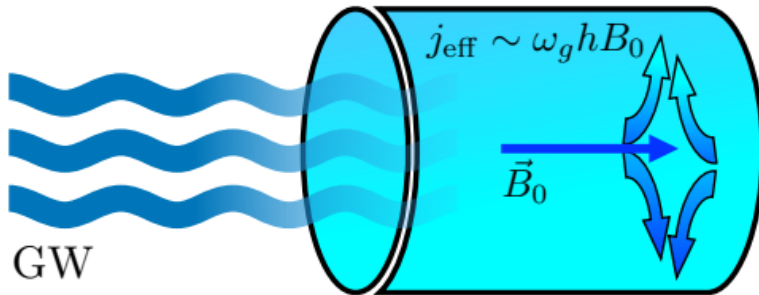
← \mathcal{R}_c computed assuming
 $Q_r = 10^4, T_m = 10^3 \text{ s} (10^{-3} \text{ s})$

axion haloscopes as **high frequency** GW detectors

still far away from BBN bound, but clear synergies of UHF GW and axion searches

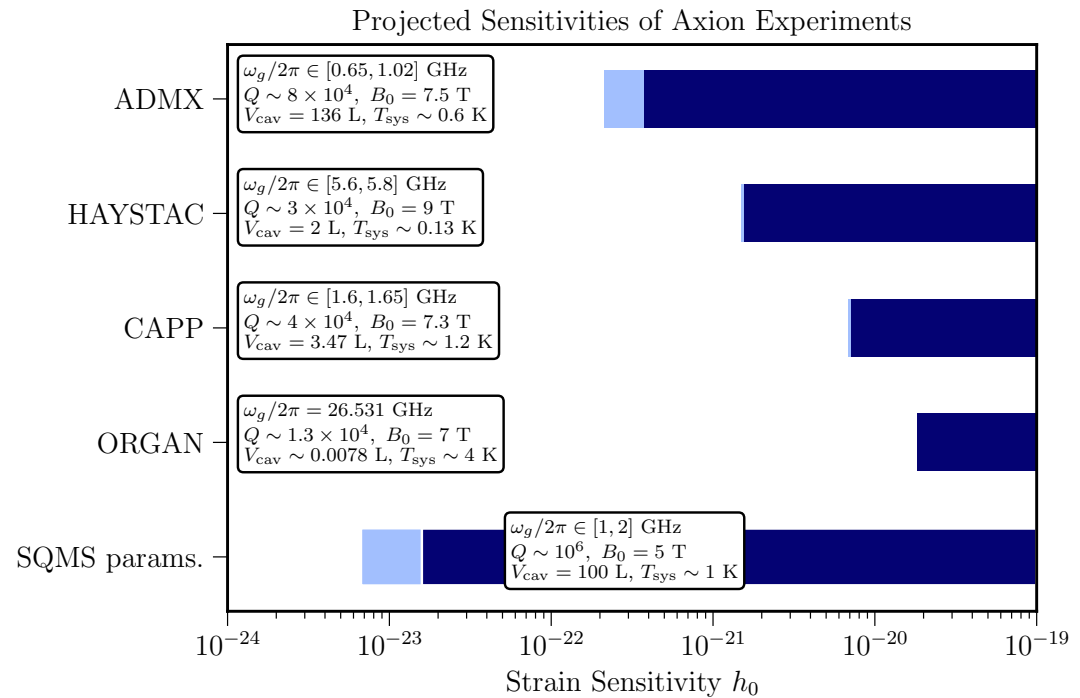
microwave cavities

[Berlin et al `21]



→

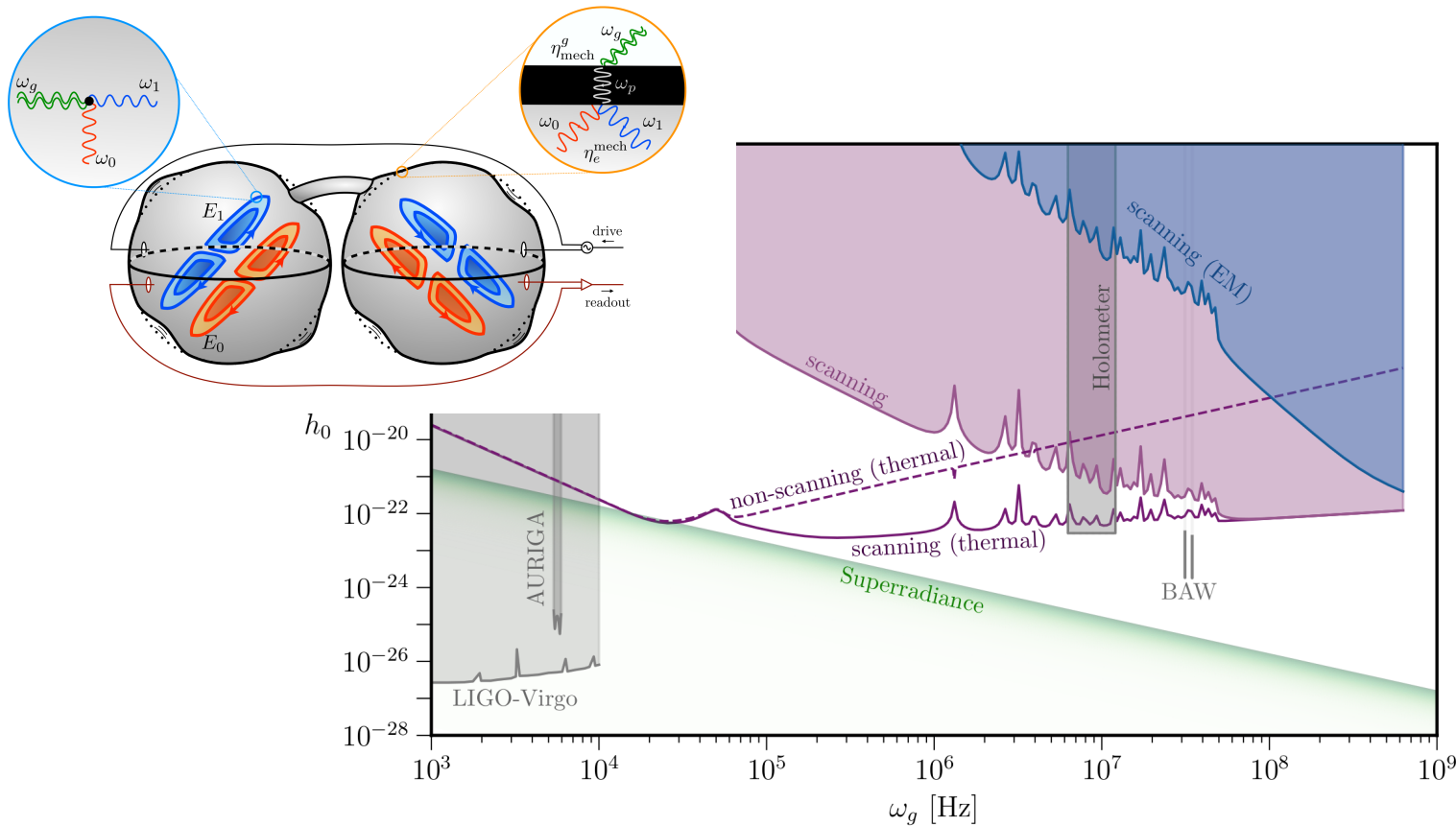
bound on
monochromatic
coherent GW



microwave cavities

effective current can also induce power in microwave cavities, in addition consider mechanical deformation of cavity walls:

Berlin, Blas, D'Agnolo et al '23

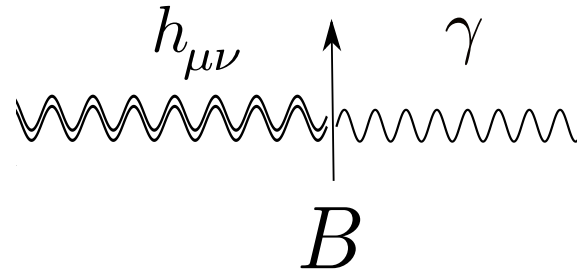


MAGO 2.0

bound on
monochromatic
coherent GW

photon (re-)generation experiments

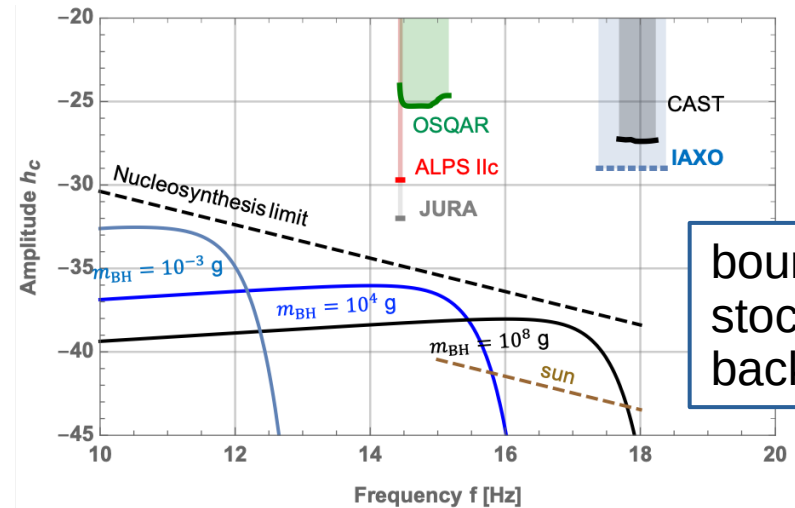
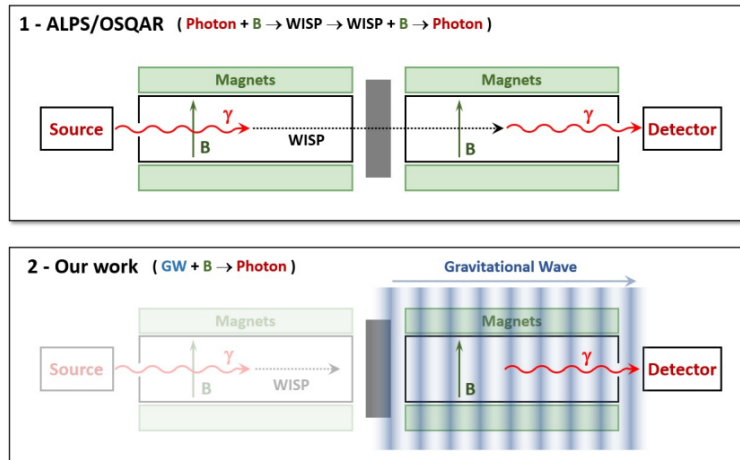
[Gertsenshtein '62, Boccaletti et al '70, Raffelt, Stodolsky '88]



see Aldo's talk

Light-shining-through-the-wall (LSW) experiments, helioscopes:

Ejilli et al '19



bound on stochastic GW background

astro/cosmo environments: Fujita et al '20, VD, Garcia-Cely '21, Feng et al '22, Liu et al '23, Ito et al '23, Ramazanov et al '23,...

HFGWs at axion detectors

current status

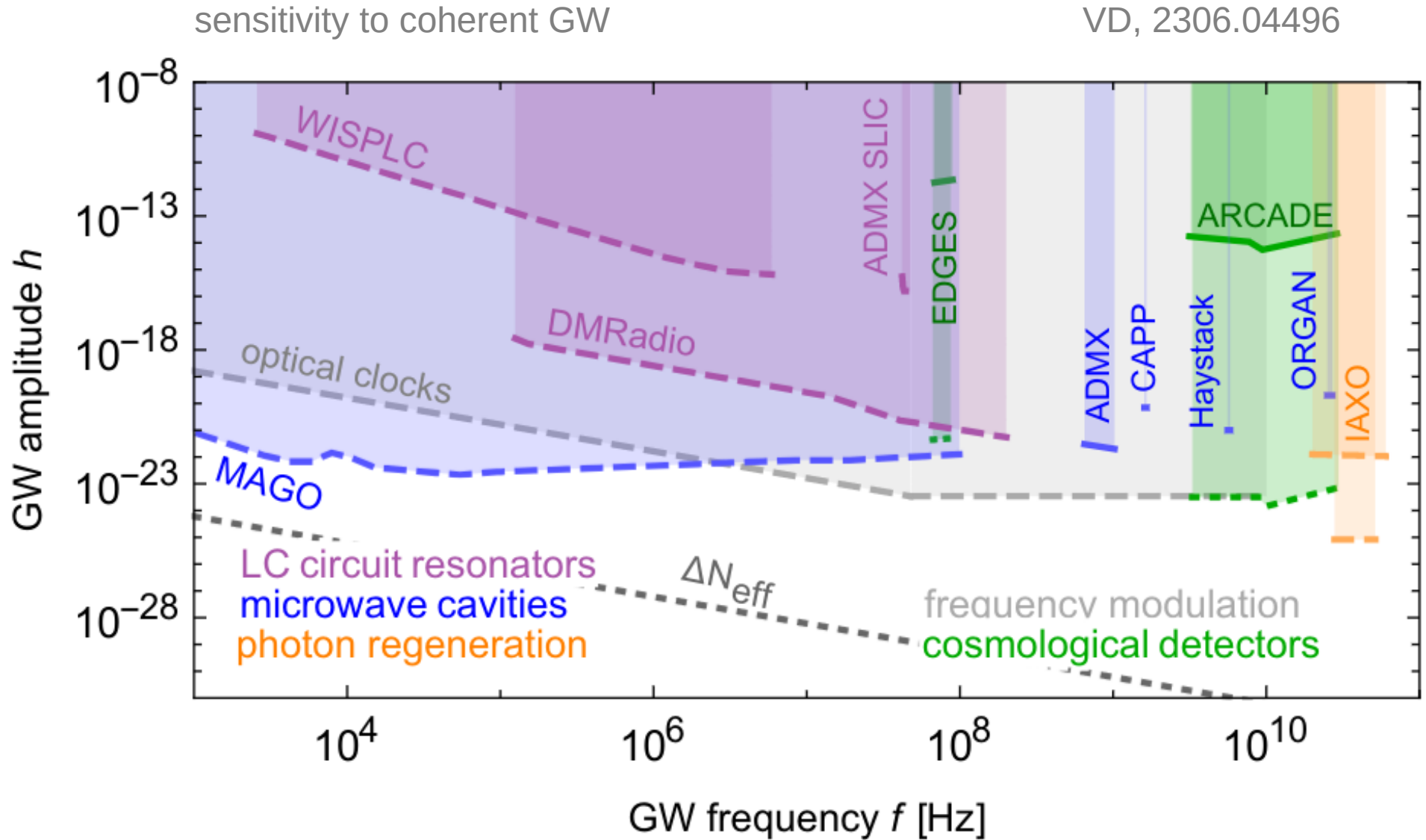
note of caution: different experiments and sources on the same plot is often misleading,
many hidden parameters

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.... but let's do it anyway...

current status



Conclusions and Outlook

GW sources at high frequencies

- GW signals \gg kHz would be a smoking gun of BSM physics
- Cosmological signals well motivated, but amplitude constrained by BBN and CMB
- Larger astrophysical signals from rare exotic events possible, e.g. light PBHs

GW searches with axion detectors

- GW electrodynamics has clear similarities with axion electrodynamics:
Important synergies between axion searches and UHF GW searches
- low-mass axion haloscopes, SRF cavities, LSW experiments,... as GW detectors

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„such detectors [laser interferometers] have so low sensitivity that they are of little experimental interest“ [Misner, Thorne, Wheeler 1974]

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Thank you!

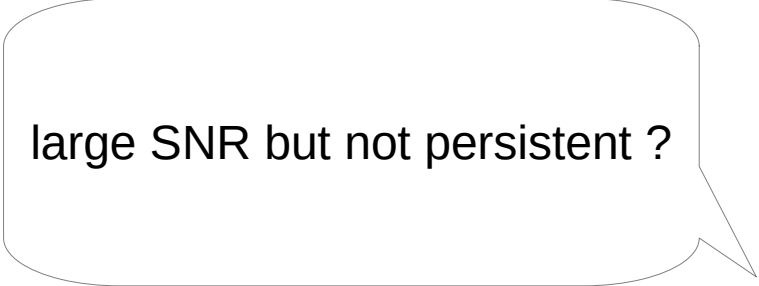
„such detectors [laser interferometers] have so low sensitivity that they are of little experimental interest“ [Misner, Thorne, Wheeler 1974]

Some questions for discussion:

- Different data taking and analysis techniques compared to axion searches?
- Development of tools for estimating HFGW sensitivities



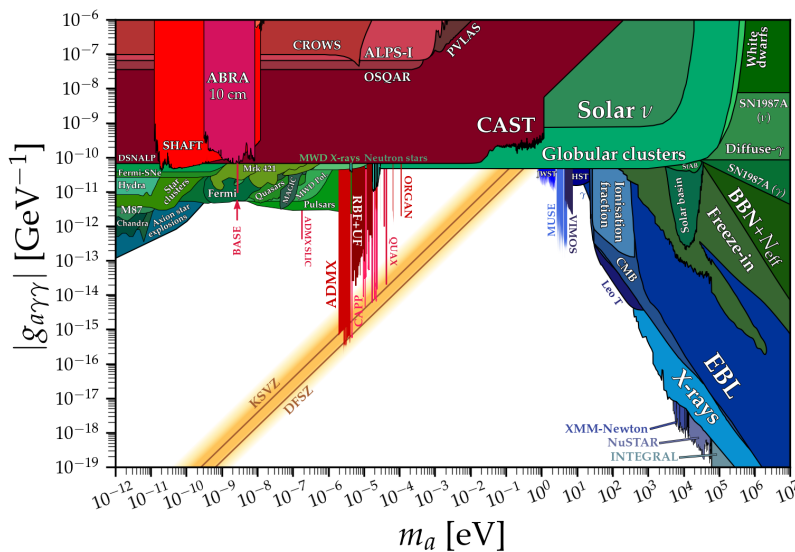
persistent and coherent ?



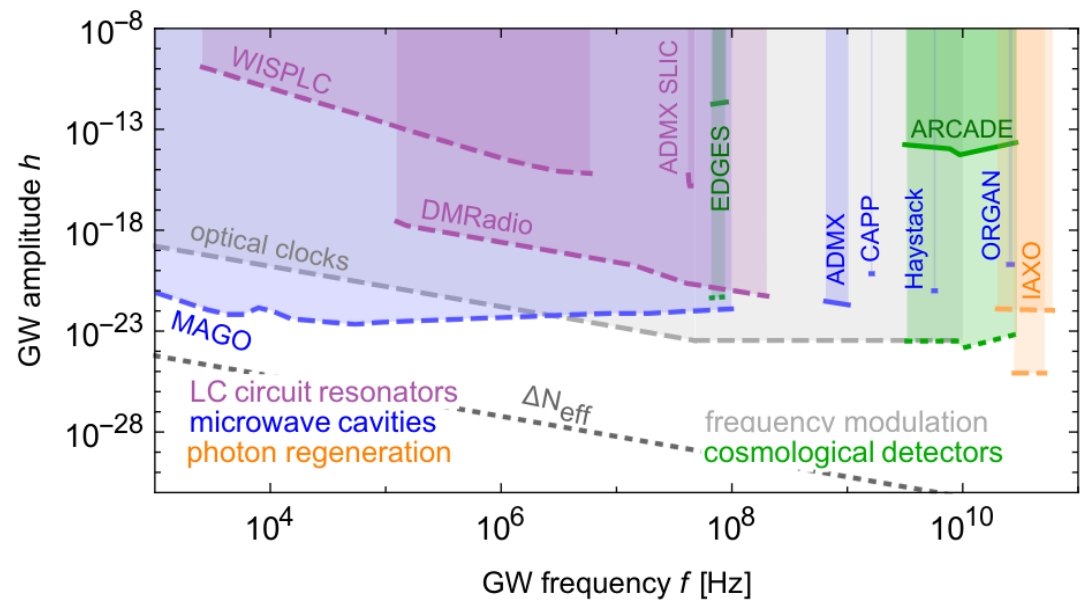
large SNR but not persistent ?

Some questions for discussion:

- Overlooked opportunities for existing axion experiments?
- Potential of (minor) modifications to existing experiments versus dedicated GW instruments?



HFGWs at axion detectors



Some questions for discussion:

- Potential for two-way synergies?
- Other BSM fundamental physics that might be probed?

backup slides

GW electrodynamics

homogeneous Maxwell equation

$$0 = \nabla_{\mu} F_{\nu\rho} + \nabla_{\nu} F_{\rho\mu} + \nabla_{\rho} F_{\mu\nu} = \partial_{\mu} F_{\nu\rho} + \partial_{\nu} F_{\rho\mu} + \partial_{\rho} F_{\mu\nu}$$

$$\rightarrow F_{\alpha\beta} = \partial_{\alpha} A_{\beta} - \partial_{\beta} A_{\alpha} \quad \text{independent of background metric}$$

inhomogeneous Maxwell equation

$$\nabla_{\nu} (g^{\alpha\mu} F_{\alpha\beta} g^{\beta\nu}) = j^{\mu} \quad \rightarrow \partial_{\nu} (\sqrt{-g} g^{\alpha\mu} F_{\alpha\beta} g^{\beta\nu}) = \sqrt{-g} j^{\mu}$$

$$\text{expand in } h: \quad g^{\alpha\mu} F_{\alpha\beta} g^{\beta\nu} \simeq F^{\mu\nu} - F_{\alpha}^{\nu} h^{\alpha\mu} - F^{\mu}_{\beta} h^{\beta\nu}, \quad \sqrt{-g} \simeq 1 + h/2$$

$$\partial_{\nu} \left(\left(1 + \frac{h}{2} \right) F^{\mu\nu} - F_{\alpha}^{\nu} h^{\alpha\mu} - F^{\mu}_{\beta} h^{\beta\nu} \right) = \left(1 + \frac{h}{2} \right) j^{\mu} + \mathcal{O}(h^2),$$

$$\partial_{\nu} F^{\mu\nu} = \left(1 + \frac{1}{2} h \right) j^{\mu} + \partial_{\nu} \left(-\frac{1}{2} h F^{\mu\nu} + F_{\alpha}^{\nu} h^{\alpha\mu} + F^{\mu}_{\beta} h^{\beta\nu} \right) + \mathcal{O}(h^2)$$

j_{eff}^{μ}

[a note on frames]

GR is invariant under coordinate transformations, but linearized GR is not

Transverse traceless (TT) gauge

- coordinates fixed by freely falling test masses
- GW takes very simple form $h_{0\mu} = 0, h_i^i = 0, \partial_j h^{ij} = 0$
- rigid body seems to 'oscillate' in presence of GW

$$h_{ij}^{TT} = (h^+ e_{ij}^+(\phi_h, \theta_h) + h^\times e_{ij}^\times(\phi_h, \theta_h)) e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t)}$$

Proper detector frame

- coordinates fixed by laboratory frame
- GW takes a more involved form
- description of experimental setup and observables is straightforward

$$\begin{aligned} h_{00} &= \omega^2 F(\mathbf{k} \cdot \mathbf{r}) \mathbf{b} \cdot \mathbf{r}, & b_j &\equiv r_i h_{ij}^{TT} \Big|_{\mathbf{r}=0}, \\ h_{0i} &= \frac{1}{2} \omega^2 [F(\mathbf{k} \cdot \mathbf{r}) - iF'(\mathbf{k} \cdot \mathbf{r})] (\hat{\mathbf{k}} \cdot \mathbf{r} b_i - \mathbf{b} \cdot \mathbf{r} \hat{k}_i), \\ h_{ij} &= -i\omega^2 F'(\mathbf{k} \cdot \mathbf{r}) (|\mathbf{r}|^2 h_{ij}^{TT} \Big|_{\mathbf{r}=0} + \mathbf{b} \cdot \mathbf{r} \delta_{ij} - b_i r_j - b_j r_i), \end{aligned}$$

VD, Garcia-Cely, Rodd '22
s.a. Berlin et al '21

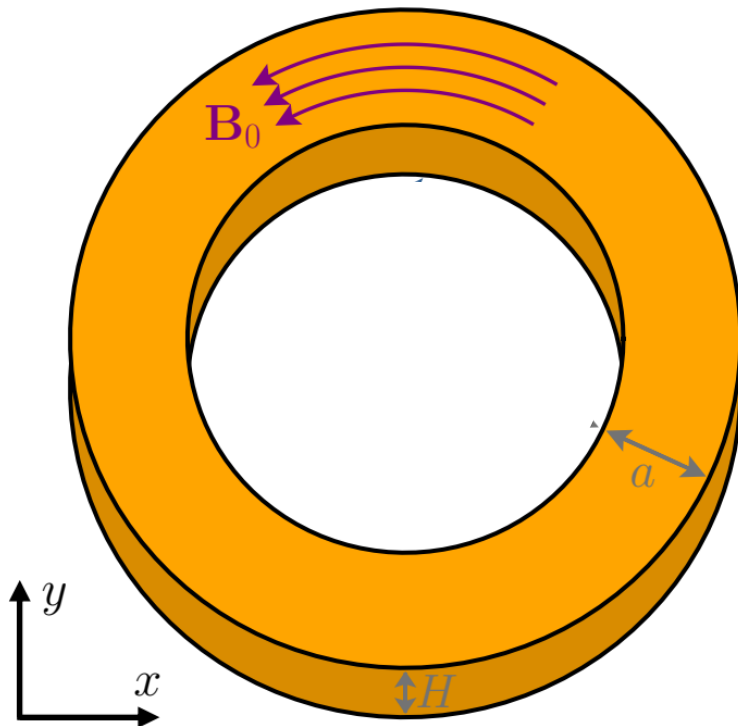
we will consider a plane wave plane wave in the proper detector frame

GW signal in axion haloscopes

eg ABRACADABRA, SHAFT, DM Radio:

VD, Garcia-Cely, Rodd '22

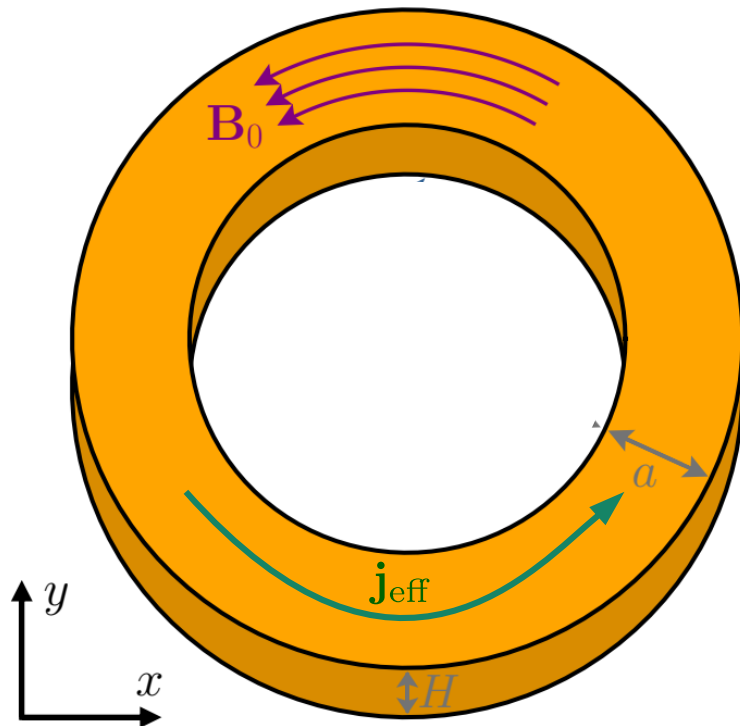
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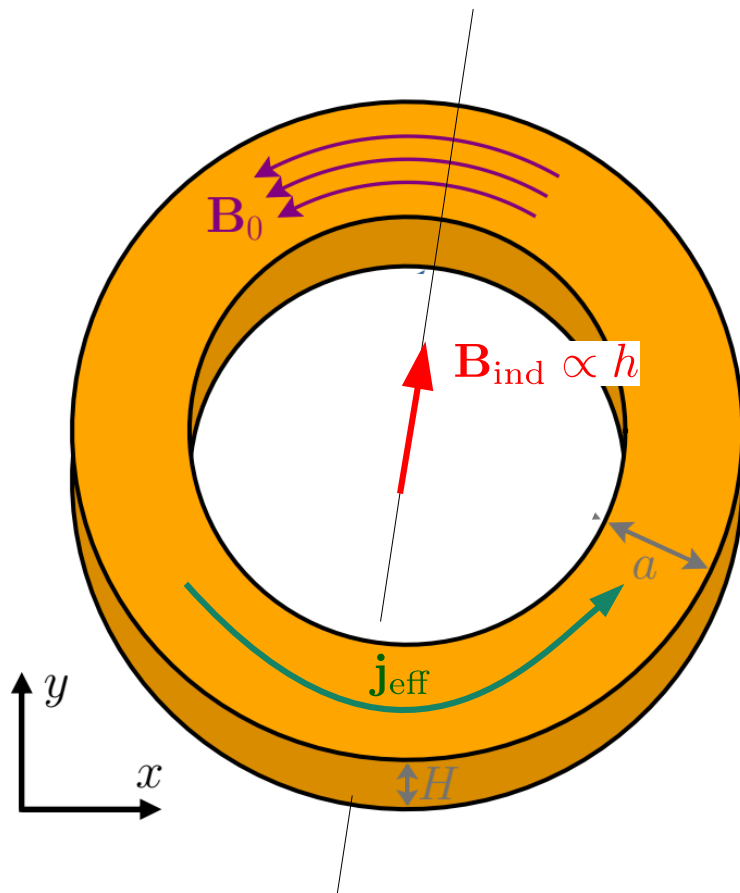
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effective current

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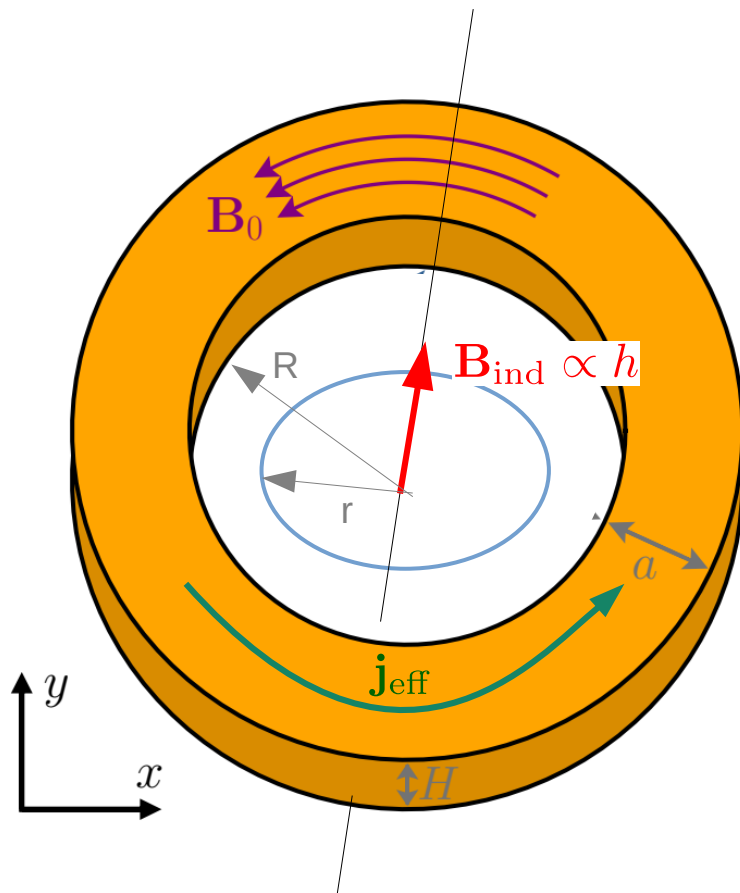
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measure magnetic flux ($\sim h$)
through pickup loop

at leading order in (ωR) :

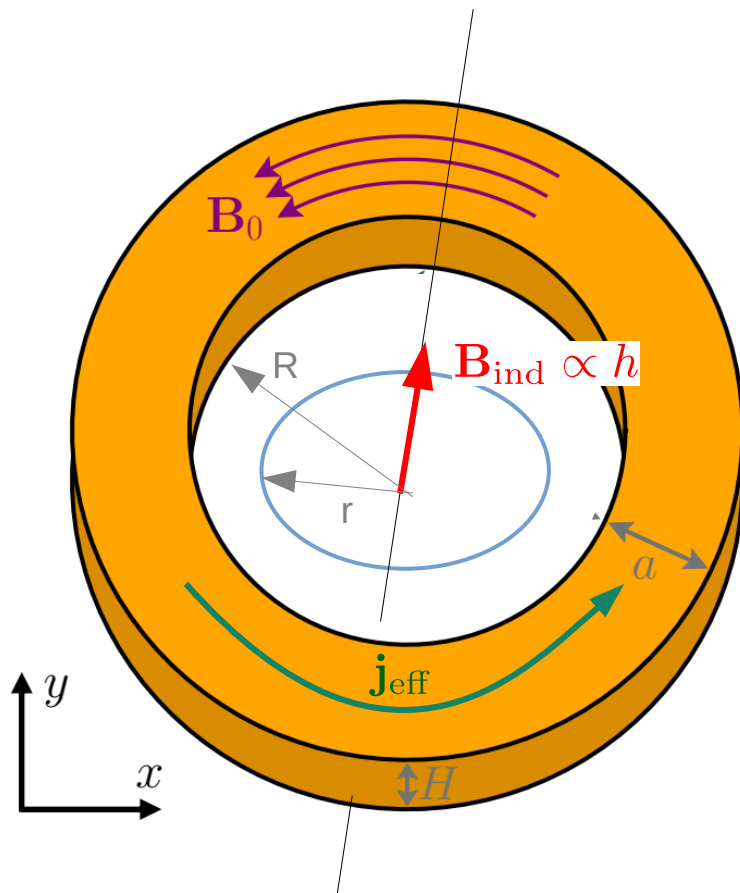
$$\Phi_{\text{gw}} = \frac{i e^{-i\omega t}}{16\sqrt{2}} h^\times \omega^3 B_0 \pi r^2 R a (a + 2R) s_{\theta_h}^2$$

$$\sim (\omega L)^3 h B_0 L^2$$

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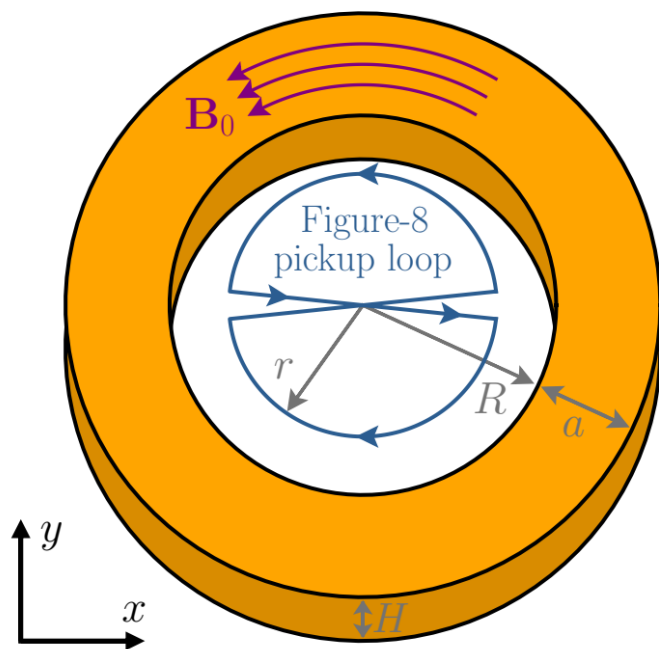
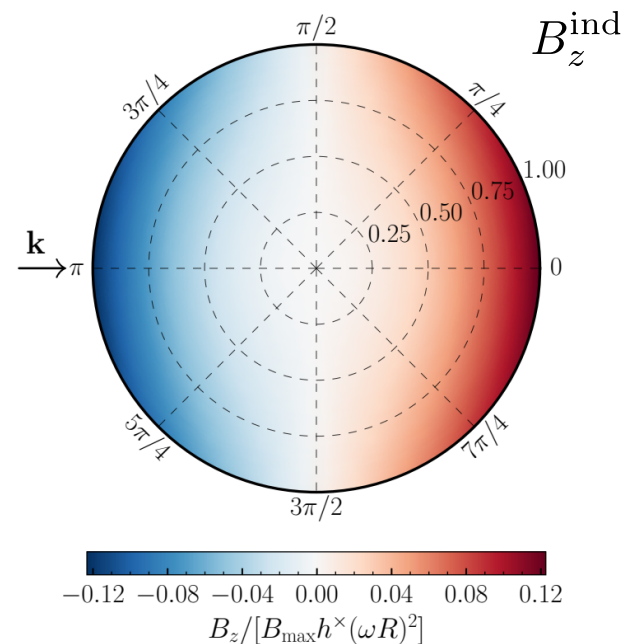
match to axion induced flux to recast
axion-photon coupling bounds as GW bounds:

optimized pickup loop geometry

spin 2 structure of GW : angular modulation of induced B field

leading order $(\omega R)^2$ contribution captured by breaking cylindrical symmetry, e.g. using a figure-8 pickup loop

[VD, Garcia-Cely, Lee, Rodd `23] Symmetries and selection rules



$$\begin{aligned} \Phi_{\text{gw},8} &= \frac{e^{-i\omega t}}{3\sqrt{2}} \omega^2 B_0 r^3 R \ln(1 + a/R) s_{\theta_h} \\ &\quad \times (h^\times s_{\phi_h} - h^+ c_{\theta_h} c_{\phi_h}) \\ &\sim (\omega L)^2 h B_0 L^2 \end{aligned}$$

parametric improvement for modified pickup loop

geometry and time scales

VD, Garcia-Cely, Lee, Rodd `23

Symmetries and selection rules:

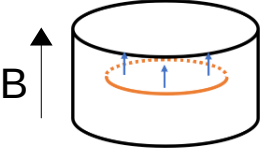
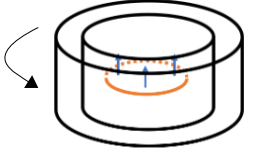
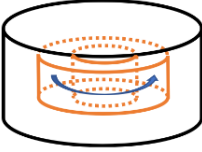
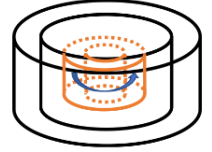
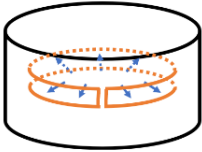
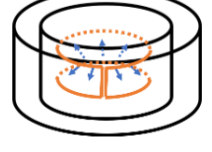
- For an instrument with azimuthal symmetry, at leading $\mathcal{O}[(\omega L)^2]$: $\Phi_h \propto h^+$
- For an instrument with azimuthal symmetry, the flux is proportional to either h^+ or h^\times
- For an instrument with full cylindrical symmetry, ϕ_h contains only even or odd powers of ω

geometry and time scales

VD, Garcia-Cely, Lee, Rodd '23

Symmetries and selection rules:

- For an instrument with azimuthal symmetry, at leading
- For an instrument with azimuthal symmetry, the flux is
- For an instrument with full cylindrical symmetry, ϕ_h cor

	Solenoid: $\mathbf{B}_0 \propto \hat{\mathbf{e}}_z$ ($\eta_y = +1, \eta_z = -1$)	Toroid: $\mathbf{B}_0 \propto \hat{\mathbf{e}}_\phi$ ($\eta_y = -1, \eta_z = +1$)
$\hat{\mathbf{n}}' \propto \hat{\mathbf{e}}_z$ ($\kappa_y = +1, \kappa_z = -1$)	$h^+, n \text{ even} \Rightarrow \mathcal{O}[(\omega L)^2]$ $\Phi_h = \frac{e^{-i\omega t}}{48\sqrt{2}} h^+ \omega^2 B_0 s_{\theta_h}^2 \pi r^2 (11r^2 + 14R^2 + 16R^2 \ln \frac{R}{r})$ 	$h^\times, n \text{ odd} \Rightarrow \mathcal{O}[(\omega L)^3]$ $\Phi_h = \frac{ie^{-i\omega t}}{48\sqrt{2}} h^\times \omega^3 B_{\max} \pi r^2 a R (a + 2R) s_{\theta_h}^2$ 
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$\hat{\mathbf{n}}' \propto \hat{\mathbf{e}}_\rho$ ($\kappa_y = +1, \kappa_z = +1$)	$h^+, n \text{ odd} \Rightarrow \mathcal{O}[(\omega L)^3]$ $\Phi_h = \frac{ie^{-i\omega t}}{96\sqrt{2}} h^+ B_0 \omega^3 c_{\theta_h} s_{\theta_h}^2$ $\times \pi r^2 l (3l^2 - 22(r^2 + 2R^2) - 36R^2 \ln \frac{R}{r})$ 	$h^\times, n \text{ even} \Rightarrow \mathcal{O}[(\omega L)^4]$ $\Phi_h = \frac{e^{-i\omega t}}{32\sqrt{2}} h^\times \omega^4 B_{\max} \pi r^2 a R l (a + 2R) c_{\theta_h} s_{\theta_h}^2$ 

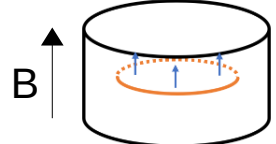
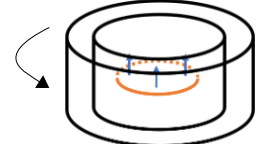
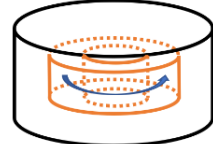
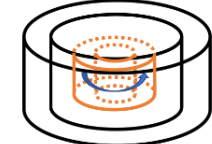
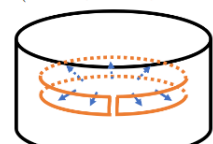
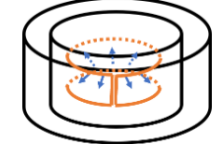
geometry and time scales

VD, Garcia-Cely, Lee, Rodd '23

Symmetries and selection rules:

- For an instrument with azimuthal symmetry, at leading
- For an instrument with azimuthal symmetry, the flux is
- For an instrument with full cylindrical symmetry, ϕ_h cor

Time scales:

	Solenoid: $\mathbf{B}_0 \propto \hat{\mathbf{e}}_z$ ($\eta_y = +1, \eta = -1$)	Toroid: $\mathbf{B}_0 \propto \hat{\mathbf{e}}_\phi$ ($\eta_y = -1, \eta = +1$)
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$$\Phi_h(h^+, h^\times; \phi_h, \theta_h) = \mathcal{R}_c \Phi_a(g_{a\gamma\gamma}),$$

$$\mathcal{R}_c = \left(\frac{T_m}{\tau_h}\right)^{1/4} \left(\frac{Q_a}{Q_h}\right)^{1/4} \begin{cases} 1 & Q_r < Q_a, Q_h, \\ (Q_a/Q_r)^{1/4} & Q_a < Q_r < Q_h, \\ Q_r/Q_h & Q_h < Q_r < Q_a, \\ (Q_a/Q_r)^{1/4} Q_r/Q_h & \text{otherwise.} \end{cases}$$

signal duration, coherence time < ring up time, axion coherence time, measurement time

➔ will reduce detectability

cosmological sources

Amplitude: BBN / CMB bound

$$\frac{\rho_{GW}^0}{\rho_c^0} = \Omega_\gamma^0 \left(\frac{g_s^0}{g_s(T)} \right)^{4/3} \underbrace{\frac{\rho_{GW}(T)}{\rho_\gamma(T)}}_{\lesssim 10\%} \Big|_{T_{\text{CMB, BBN}}} \leq 10^{-5} \Delta N_{eff} \simeq 10^{-6}$$

for a broadband SGWB: $\rightarrow h_{c,sto} \lesssim 10^{-29} (100 \text{ MHz}/f) \Delta N_{eff}^{1/2}$

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during radiation era: $f \sim 100 \text{ MHz}/\epsilon_* (T_*/10^{15} \text{ GeV}), \quad \epsilon_* \lesssim 1$

during inflation: $f \sim 10^{-18} \text{ Hz } e^{N_{\text{CMB}} - N} \lesssim 10^8 \text{ Hz } e^{-N}, \quad N_{\text{CMB}} \lesssim 60$

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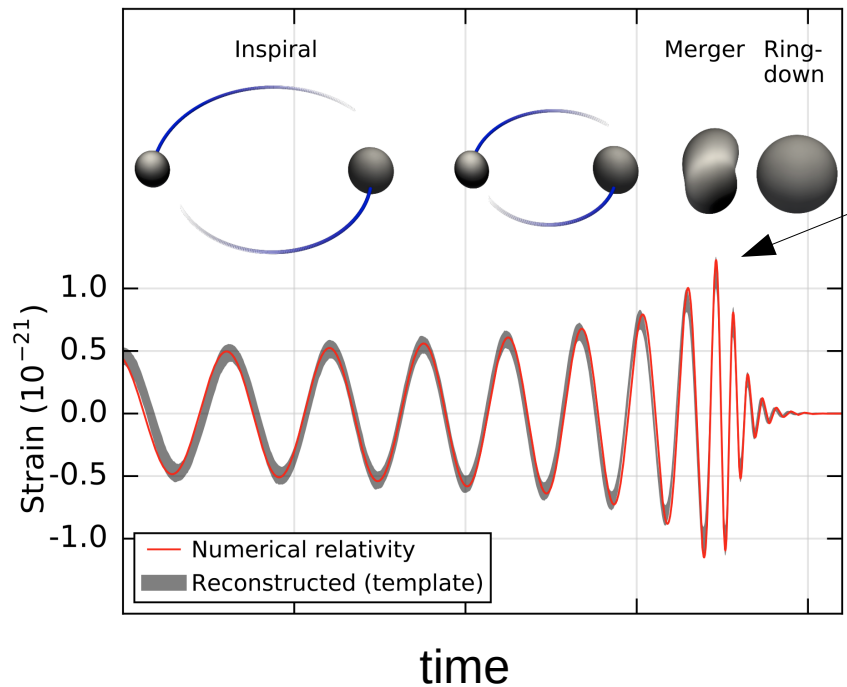
Examples: (Axion) inflation, (p)reheating, relic cosmic GW background, phase transitions (first order PT and/or topological defects from PTs) ,...

see Living Review: <https://arxiv.org/abs/2011.12414>

astrophysical sources

Example:
mergers of light primordial black holes

$$h_{+, \times}^{\text{PBH}} \simeq 10^{-23} \left(\frac{10 \text{ kpc}}{D} \right) \left(\frac{m_{\text{PBH}}}{10^{-5} M_{\odot}} \right)^{5/3} \left(\frac{f}{100 \text{ MHz}} \right)^{2/3}$$



$$f_{\text{ISCO}} = 220 \text{ MHz} \left(\frac{10^{-5} M_{\odot}}{m_{\text{PBH}}} \right)$$

astrophysical sources

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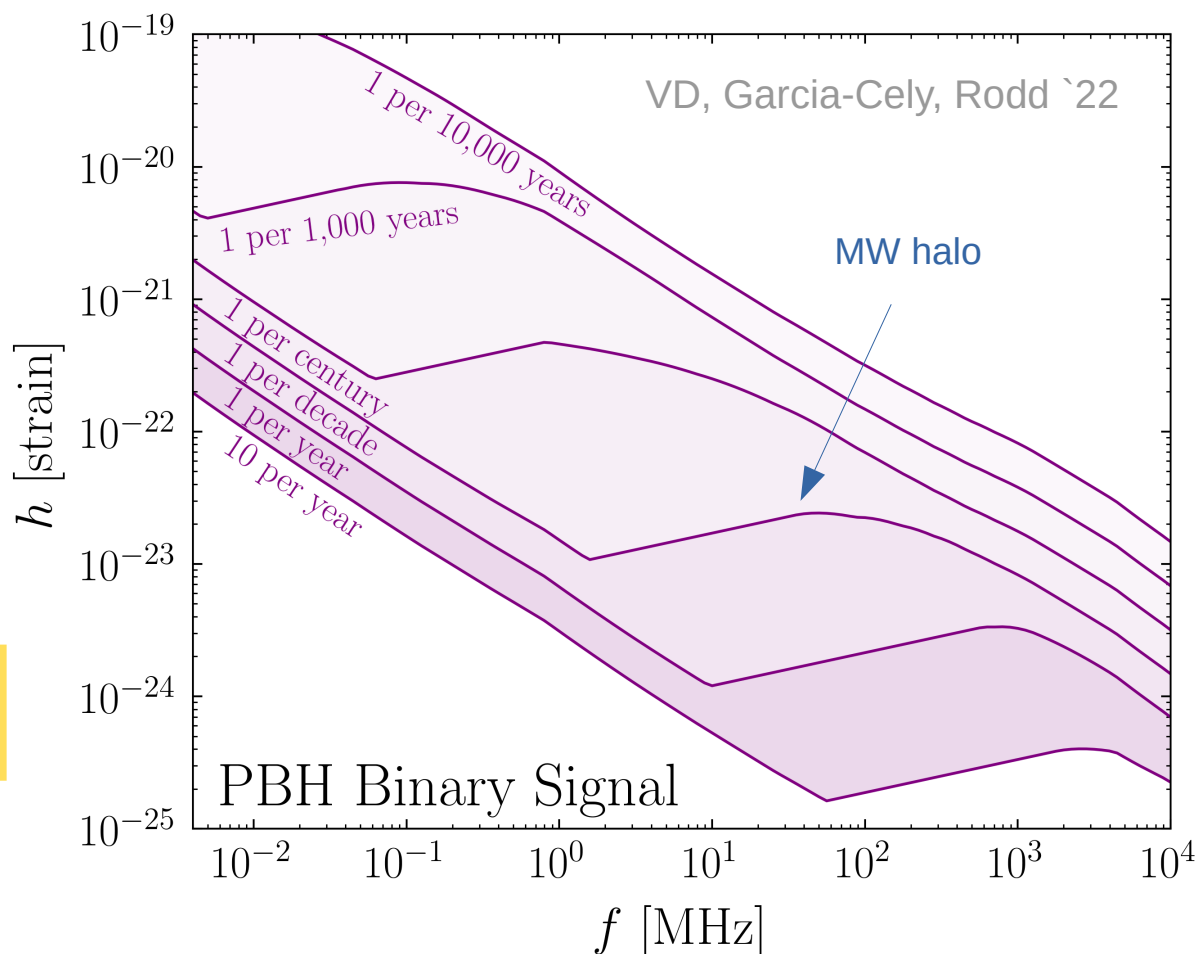
event rate:

$$\langle \Gamma \rangle = \int_0^{\infty} dr 4\pi r^2 \delta(r) R_0(m_{\text{PBH}}, f_{\text{PBH}})$$

MW halo merger rate

$$\times \Theta \left[Q^{1/4} h_{+, \times}^{\text{PBH}}(f, m_{\text{PBH}}, r) - h_{\text{th}} \right]$$

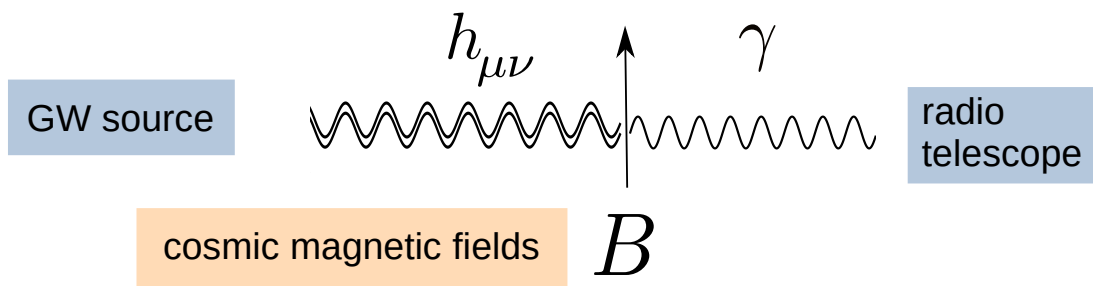
large GW amplitudes possible
for rare events



see also Franciolini, Maharana, Muia `22
HFGWs at axion detectors

a cosmic GW detector

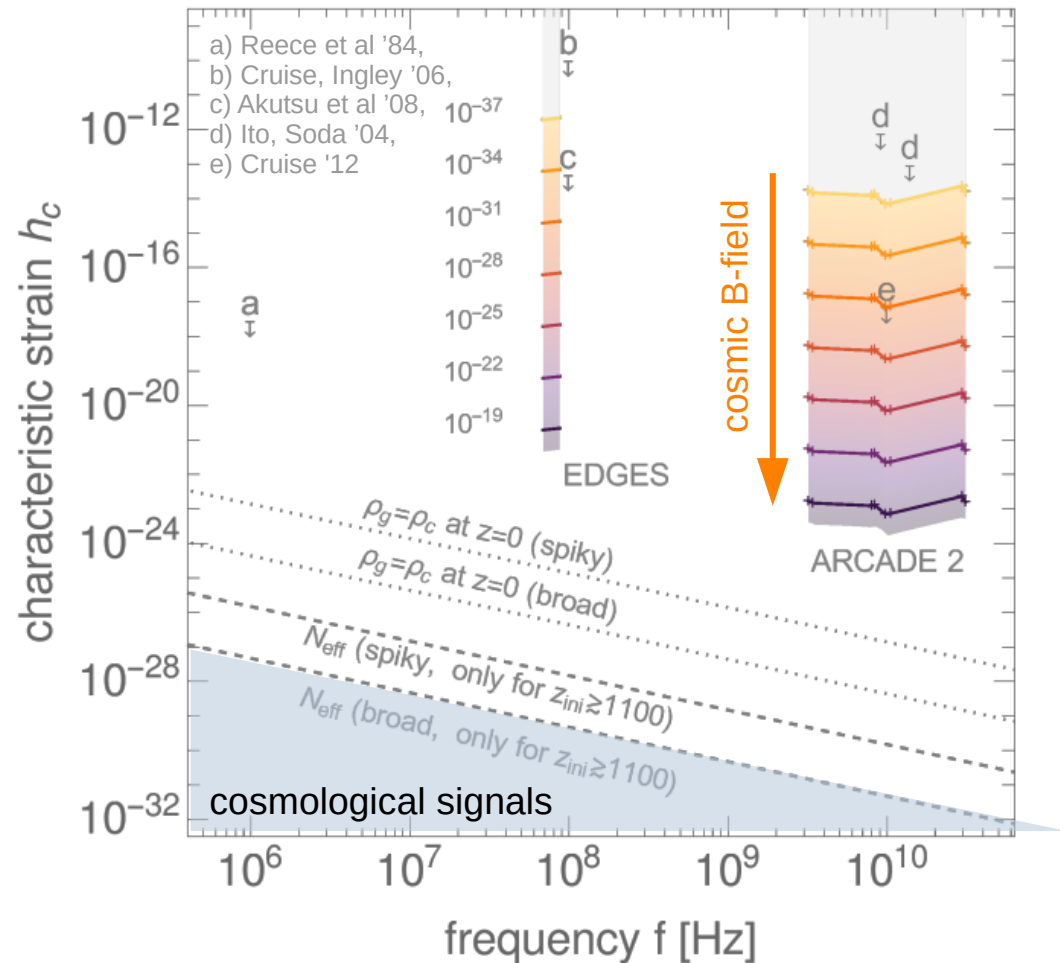
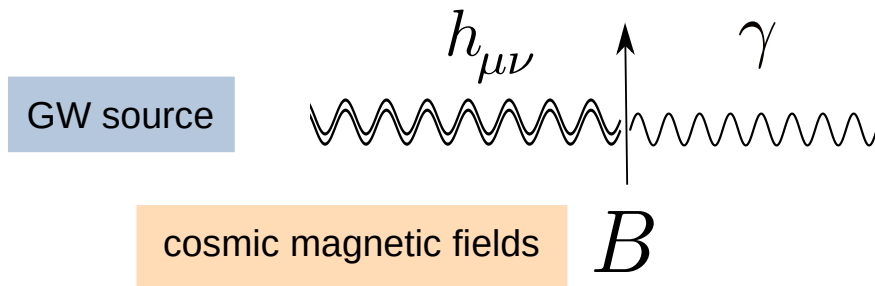
idea: compensate small GW to EM coupling with cosmologically big detector: VD, Garcia-Cely
PRL 126 (2021) 2, 021104



a cosmic GW detector

idea: compensate small GW to EM coupling with cosmologically big detector:

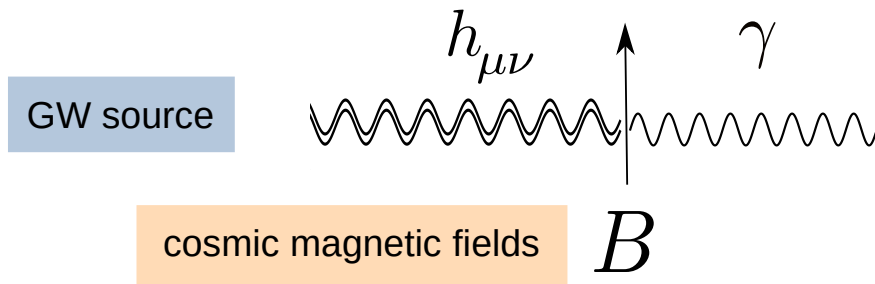
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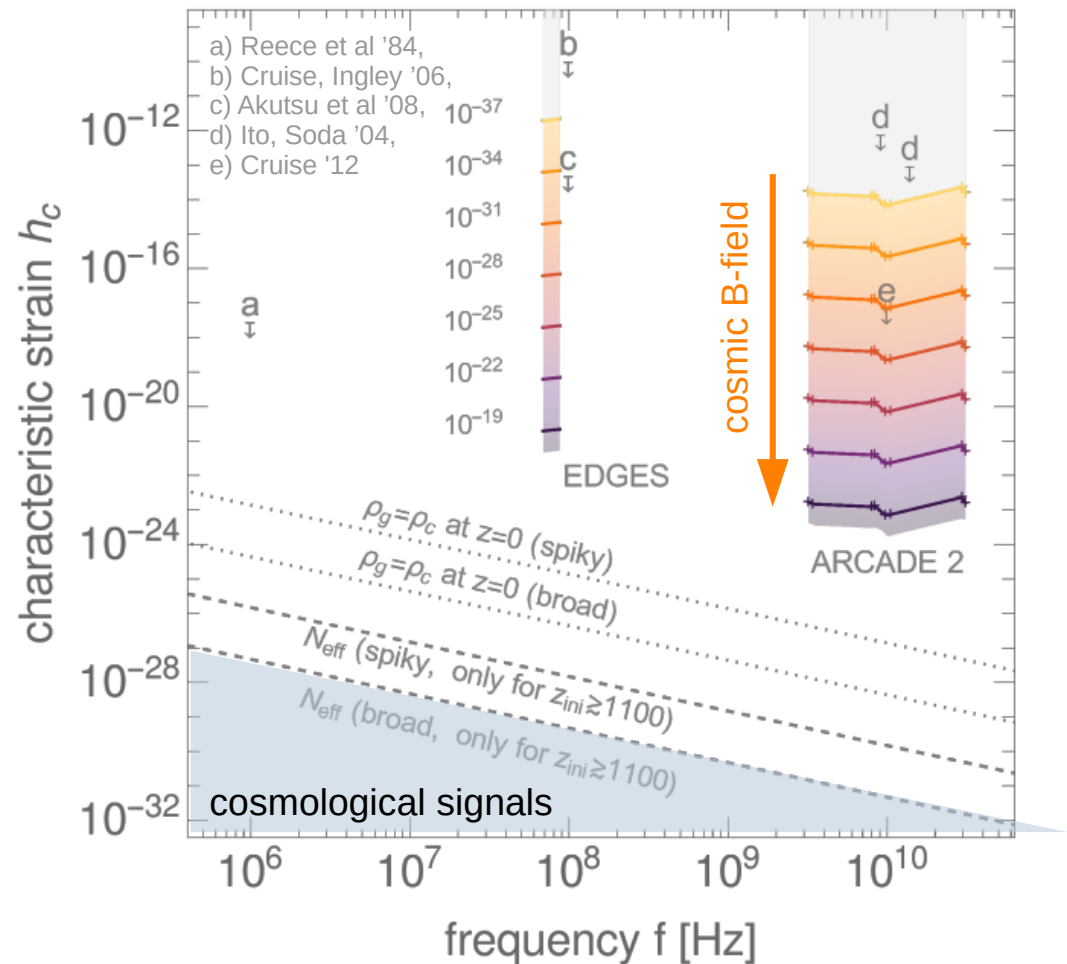
a cosmic GW detector

idea: compensate small GW to EM coupling with cosmologically big detector:

VD, Garcia-Cely
PRL 126 (2021) 2, 021104



- promising, but significant improvements needed
- a lot of room for new ideas (laboratory & cosmo)



wave versus particle regime

energy density of GW:

$$\rho \sim h^2 \omega^2 M_{\text{pl}}^2$$

number of GW 'quanta' in de-Broglie volume:

$$n = \rho/\omega, \quad \lambda_{\text{dB}} \sim 1/\omega \quad \Rightarrow \quad n \lambda_{\text{dB}}^3 \sim h^2 M_{\text{pl}}^2 / \omega^2$$

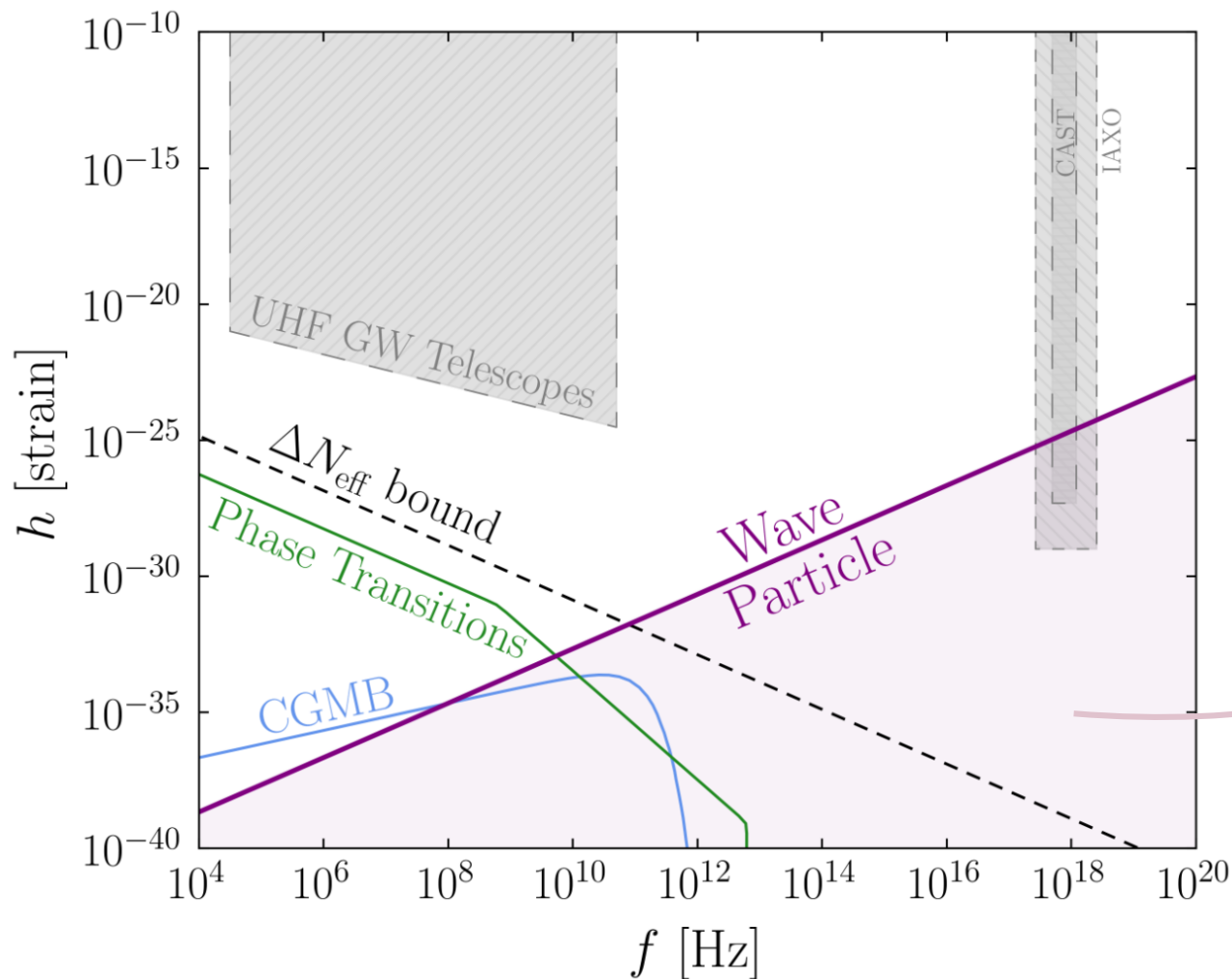
single graviton limit:

$$N = n \lambda_{\text{dB}}^3 < 1 \quad \Rightarrow \quad h \lesssim \omega / M_{\text{pl}}$$

(at LIGO, $N \sim 10^{37} (h/10^{-22})^2$)

single graviton detection ?

Carney, VD, Rodd '23



- dilute graviton gas vs classical GW
- CAST has the *sensitivity* to detect single gravitons (the source is the issue)

see also F. Dyson '13

test of quantum gravity ?

Carney, VD, Rodd `23

Do ‚discrete clicks‘ in CAST (assuming perfect noise control) imply quantum gravity ?

test of quantum gravity ?

Carney, VD, Rodd `23

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Does the photo electric effect (discrete clicks due to EM wave) prove EM quantization ?

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Carney, VD, Rodd `23

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No. Classical EM model + quantum detector can give same response.
(though classical model may need to be a bit baroque)

test of quantum gravity ?

Carney, VD, Rodd `23

Do ‚discrete clicks‘ in CAST (assuming perfect noise control) imply quantum gravity ?

No. Need to measure e.g.

- sub-Poisson distribution (requires ‚quantum‘, e.g. squeezed GW state!)
→ de facto impossible
- or other entanglement measurement (similarly difficult)
- or sufficiently convincing circumstantial evidence (CMB tensor modes)

Does the photo electric effect (discrete clicks due to EM wave) prove EM quantization ?

No. Classical EM model + quantum detector can give same response.
(though classical model may need to be a bit baroque)