

Time-of-Flight Estimation using Machine Learning Techniques

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HELMHOLTZ



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Overview

Time-of-Flight Measurements at the International Large Detector

Data & Preprocessing

Benchmark Time-of-Flight Estimator

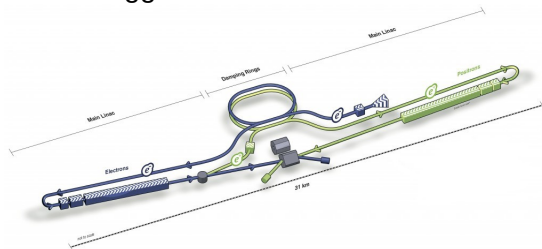
Machine Learning-Based Time-of-Flight Regression

Summary & Outlook

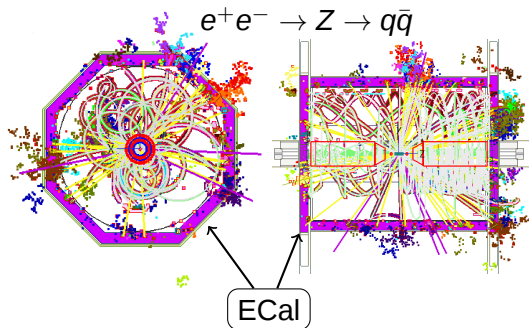
Time-of-Flight Measurements at the International Large Detector

The Setup: ILC and ILD

- > International Linear Collider (ILC)
- > proposed, but not build yet
- > colliding polarised e^+e^- @ 250 GeV centre-of-mass energy
- > designed for precision electroweak and Higgs measurements

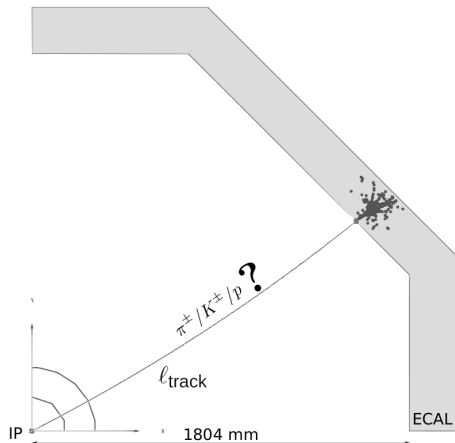


- > International Large Detector (ILD)
- > highly granular electromagnetic and hadronic calorimeters (ECal & HCal)
- > optimised for Particle Flow calorimetry



TOF at ILD

- > time-of-flight (TOF) estimation using ML
 - > used in particle identification of particles with $p \lesssim \mathcal{O}(10 \text{ GeV})$
 - > particle identification reduces to $\pi^\pm$ vs. $K^\pm$ vs. $\bar{p}$
 - > particle identified by mass and electric charge
- $$\Rightarrow m_0 = \frac{p \cdot \text{TOF}}{\ell_{\text{track}}} \sqrt{1 - \left(\frac{\ell_{\text{track}}}{(\text{TOF} \cdot c)} \right)^2}$$
- > need to know p (from curvature in magnetic field), ℓ_{track} (from tracker), TOF (now from ML)



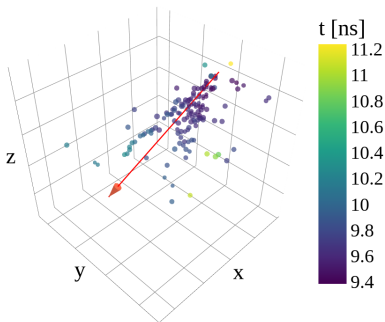
Data & Preprocessing

Data & Rotations

> data preprocessing essential, since we follow a data-centric ML approach

> MC generated unordered 5D point cloud $\oplus$ track information:

$$\underbrace{\{ [x, y, z, e, t]_i \}}_{\text{coordinates, per hit}} \oplus \underbrace{[\ell_{\text{track}}, p, p_T, p_x, p_y, p_z, \text{ECal}_x, \text{ECal}_y, \text{ECal}_z]}_{\text{reconstructed track information, per shower}} \mid i = 1 \dots n_{\text{hits}} \} \times n_{\text{showers}}$$



> assumed hit time t_i resolution ± 50 ps in all ECal layers

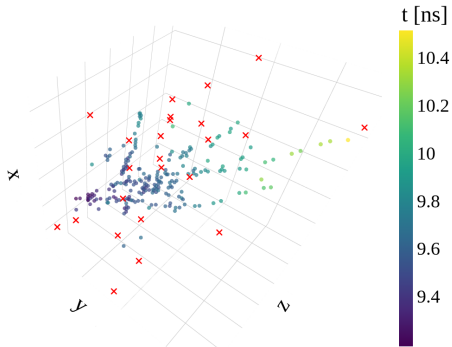
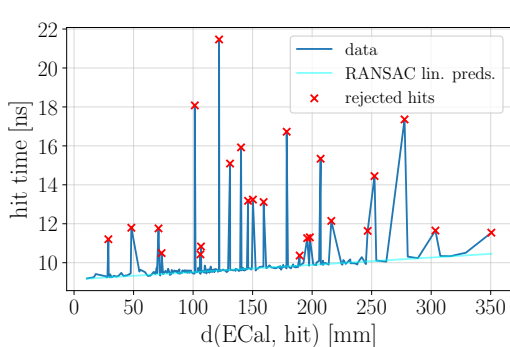
> define distances using 3D euclidean metric + two extra channels:
 $(x, y, z)^T \oplus (e, t)$

> order hits by distance to ECal surface

> transform barrel and endcap showers differently: rotations, scaling, ...

RANSAC

- outliers in space and time through backscattering, delayed nuclear reactions, ...
- random sample consensus (RANSAC) algorithm used for outlier rejection
- estimate parameters of an affine function: t_i vs $d(\text{ECal}, \text{hit}_i)$
- if $(t_i - \text{affine pred.}_i) \leq 0.5 \text{ ns}$: keep hit, else: reject $\rightarrow$ cuts away $\simeq 10\%$ of hits



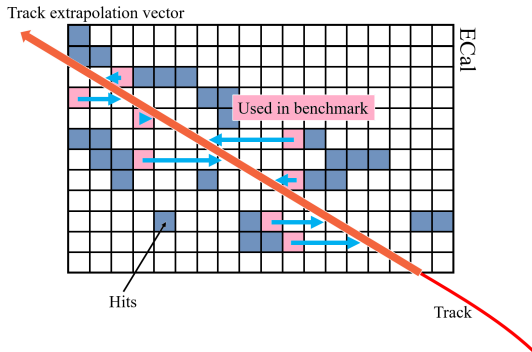
Benchmark Time-of-Flight Estimator

Benchmark TOF Estimator

- > select hits closest to momentum extrapolation into ECal in the first 10 layers
- > correct measured hit time by travel time to detection position, assuming velocity c

$$t_{\text{corrected},i} = t_i - \frac{d(\text{ECal}, (x,y,z)_i)}{c}$$

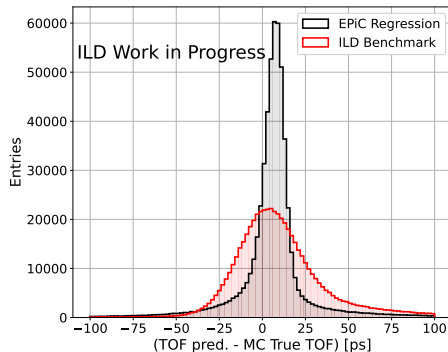
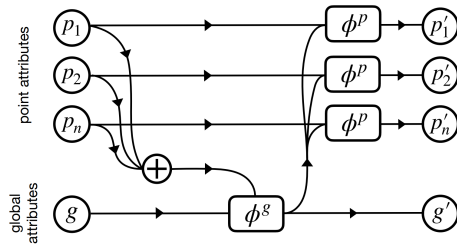
$$\text{TOF} = \frac{1}{n_{\text{hits}}} \sum_{i=1}^{n_{\text{hits}}} t_{\text{corrected},i}$$



Machine Learning-Based Time-of-Flight Regression

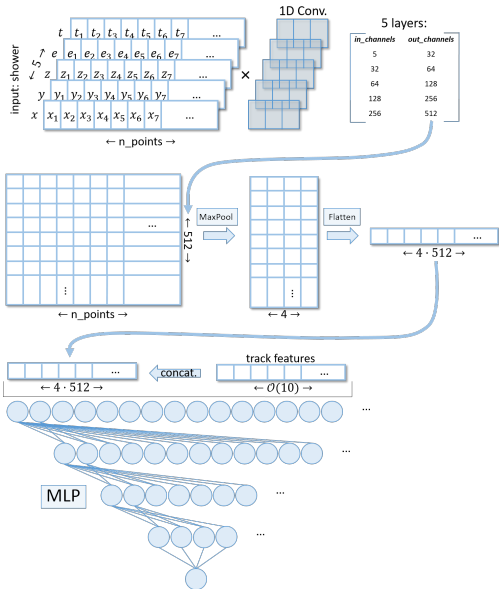
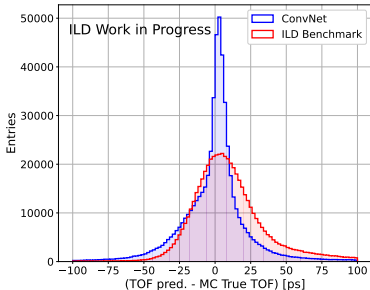
The First Shot: EPiC Regression

- > 3 equivariant point cloud (EPiC) layers from EPiC-GAN, Buhmann, Kasieczka, Thaler for encoding of input
- > EPiC layers connect global information with local shower information
- > 4 layer MLP for TOF regression based on encoded input
- > results - very good! Architecture too overkill?

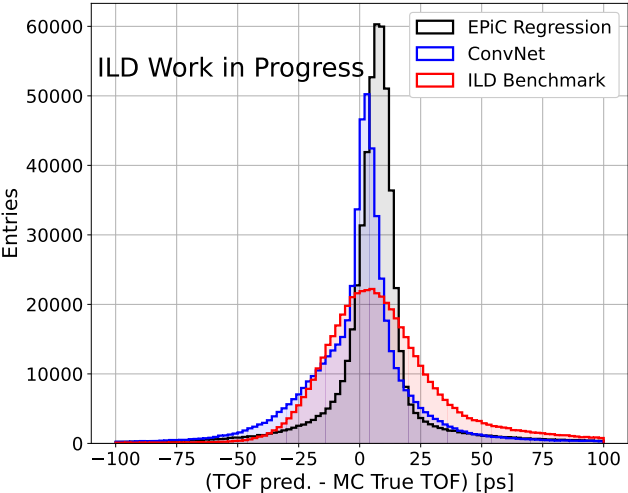


Simpler: ConvNet

- > 1D convolutions along x, y, z, e, t separately
- > (adaptive) max pooling to deal with varying numbers of hits in the shower + encoding focus on only most important features
- > 4 layer MLP for TOF regression



Results



Network	RMS90	RMS90 mean
Benchmark	23.62 ± 0.02	9.73 ± 0.03
EPiC	15.00 ± 0.02	6.17 ± 0.01
ConvNet	18.18 ± 0.02	-0.48 ± 0.02

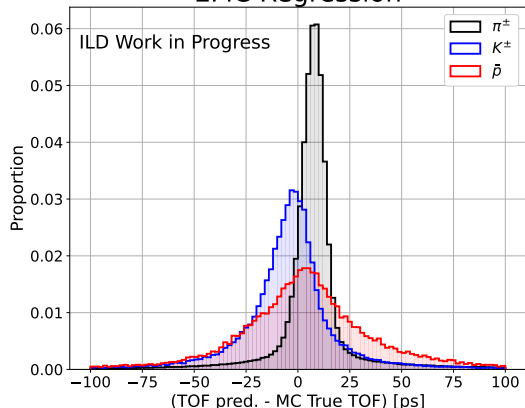
A Closer Look at the Results ... #1

$$\begin{aligned}m_{\pi^\pm} &\simeq 140 \text{ MeV} \\m_{K^\pm} &\simeq 490 \text{ MeV} \\m_{\bar{p}} &\simeq 940 \text{ MeV}\end{aligned}$$

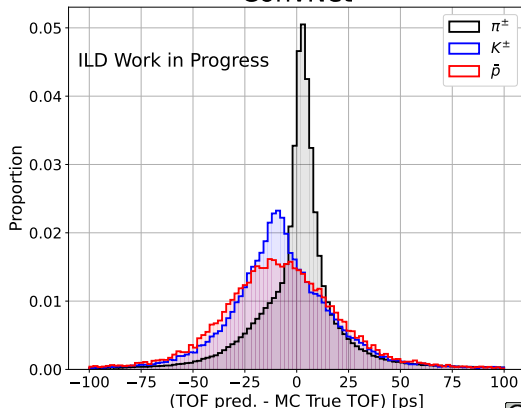
> particle abundance in $e^+e^- \rightarrow Z \rightarrow q\bar{q}$ @ 250 GeV:

85% $\pi^\pm$ 10% $K^\pm$ 5% $\bar{p}$

EPiC Regression



ConvNet



A Closer Look at the Results ... #2

$$\begin{aligned}m_{\pi^\pm} &\simeq 140 \text{ MeV} \\m_{K^\pm} &\simeq 490 \text{ MeV} \\m_{\frac{(-)}{p}} &\simeq 940 \text{ MeV}\end{aligned}$$

- > pay attention to the location of the distributions
- > network learned that the dataset has two 'mass classes':

$$m_1 \simeq m_{\pi^\pm} \text{ and } m_2 \simeq m_{\frac{(-)}{p}}$$

- > $\{ [x, y, z, e, t]_i \oplus [\ell_{\text{track}}, \rho, p_T, p_x, p_y, p_z, \text{ECal}_x, \text{ECal}_y, \text{ECal}_z] \mid i = 1 \dots n_{\text{hits}} \} \times n_{\text{showers}}$
- > it learned the two mass classes $m_{1,2}$ and c , then:

1. estimated the TOF roughly, based on $t_i, i = 1, \dots, n_{\text{hits}}$

2. estimated the corresponding mass class via: $m_{1,2} = \frac{\rho \cdot \text{TOF}}{\ell_{\text{track}}} \sqrt{1 - \left(\frac{\ell_{\text{track}}}{(\text{TOF} \cdot c)} \right)^2}$

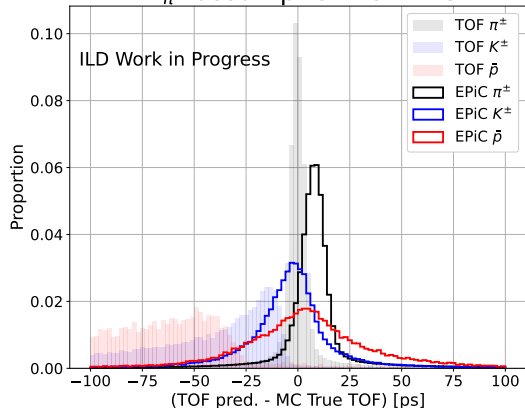
3. corrected the estimated TOF, based on: $\text{TOF} = \sqrt{\left(\frac{m_{1,2} \ell_{\text{track}}}{\rho} \right)^2 + \left(\frac{\ell_{\text{track}}}{c} \right)^2}$

A Closer Look at the Results ... #3

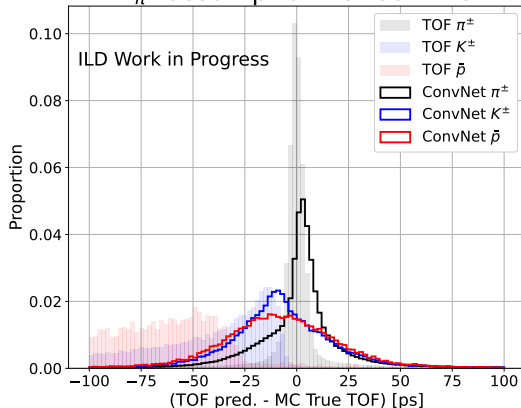
Assuming all Particles are $\pi^\pm$

$$\begin{aligned}m_{\pi^\pm} &\simeq 140 \text{ MeV} \\m_{K^\pm} &\simeq 490 \text{ MeV} \\m_{\rho^\pm} &\simeq 940 \text{ MeV}\end{aligned}$$

$m_{\pi^\pm}$ assumption vs. EPiC



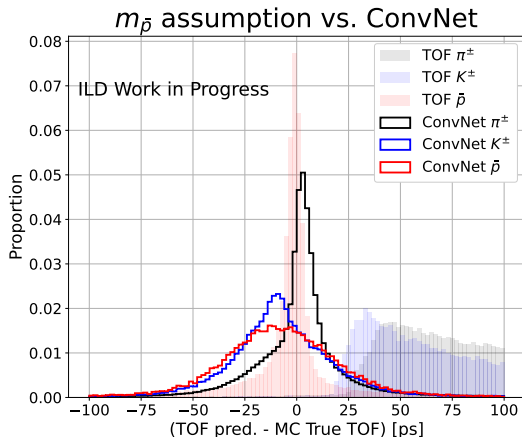
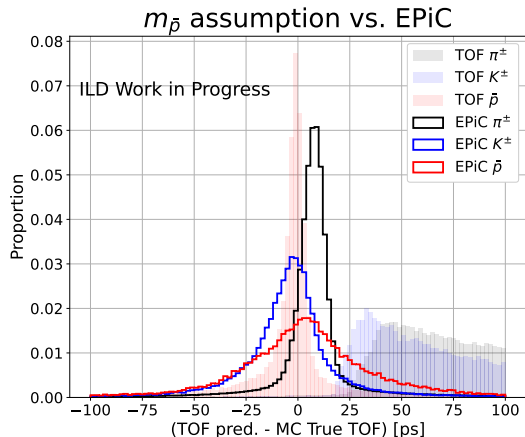
$m_{\pi^\pm}$ assumption vs. ConvNet



A Closer Look at the Results ... #4

Assuming all Particles are $\bar{p}$

$$\begin{aligned}m_{\pi^\pm} &\simeq 140 \text{ MeV} \\m_{K^\pm} &\simeq 490 \text{ MeV} \\m_{\bar{p}} &\simeq 940 \text{ MeV}\end{aligned}$$



Summary & Outlook

Summary & Outlook

Summary:

- > idea: build a TOF regression network



- > predict TOF



- > use $\text{TOF} + p + \ell_{\text{track}}$ for particle identification

EPIC Regression, ConNet

Outlook:

- > investigate which and how many masses the networks identify
- > train on an equal ratio dataset (we're on it)
- > remove track length or normalise momentum
- ⋮
- > skip TOF regression, classify $\pi^\pm$ vs. $K^\pm$ vs. $\overset{(-)}{p}$ directly

Thank you!

Contact

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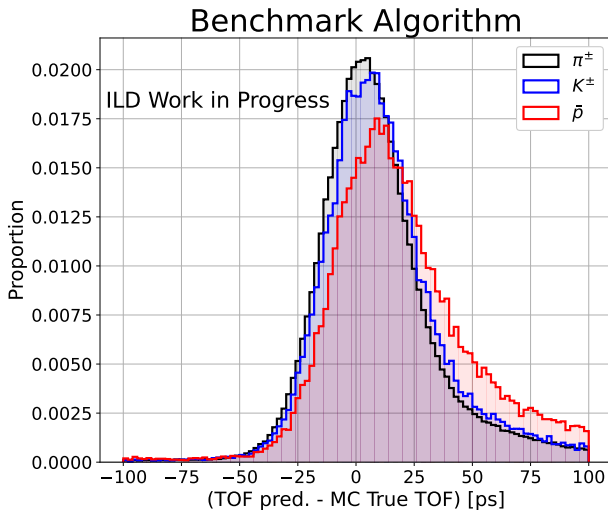
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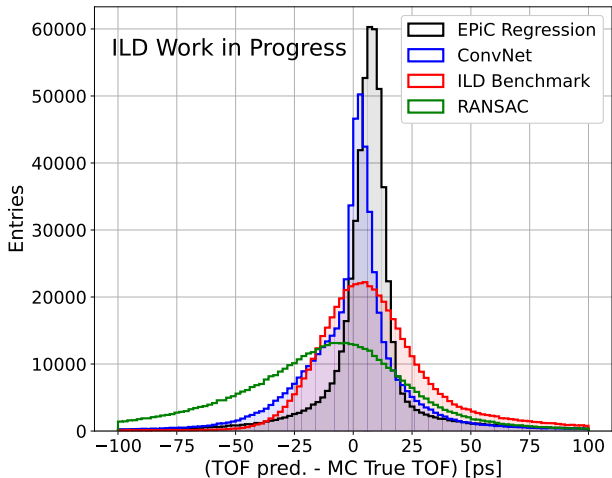
Backup

A Closer Look at the Benchmark Algorithm

$$\begin{aligned}m_{\pi^\pm} &\simeq 140 \text{ MeV} \\m_{K^\pm} &\simeq 490 \text{ MeV} \\m_{\rho^\pm} &\simeq 940 \text{ MeV}\end{aligned}$$



Performance Comparison to RANSAC

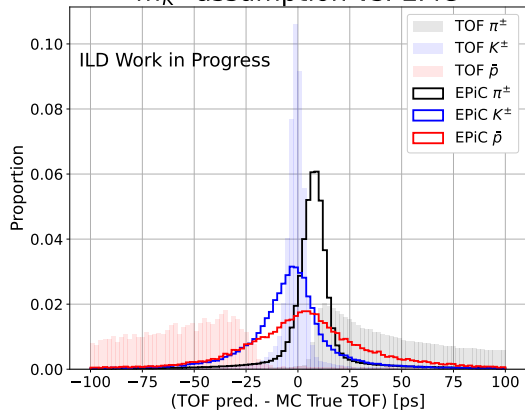


A Closer Look at the Results ... #5

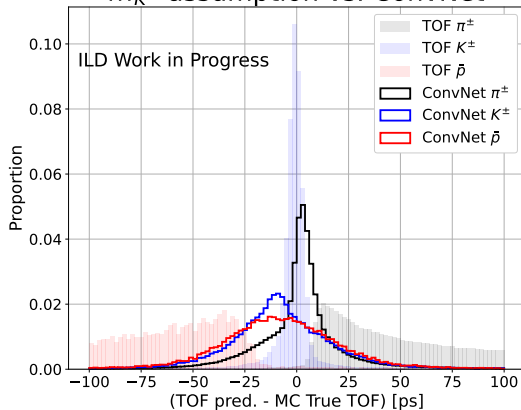
Assuming all Particles are $K^\pm$

$$\begin{aligned} m_{\pi^\pm} &\simeq 140 \text{ MeV} \\ m_{K^\pm} &\simeq 490 \text{ MeV} \\ m_{\rho^-} &\simeq 940 \text{ MeV} \end{aligned}$$

$m_{K^\pm}$ assumption vs. EPiC



$m_{K^\pm}$ assumption vs. ConvNet



Problems

