Dealing with negatively weighted Events in DNN-based LHC Analyses

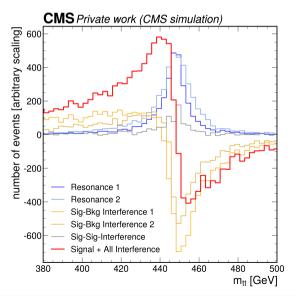
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Negatively weighted Events



- This projected was motivated by a search for heavy Higgs bosons with CP violation
- There are a variety of interference scenarios in such a case



$$|S_{A/H} + B|^2 = |S_{A/H}|^2 + 2Re(S_{A/H}B) + |B|^2$$

- Overall yield is positive!
- Signal can be partly negative (destructive interference)
- If we split into signal and background for a DNN training: (physically) truly negative parts of phase space!

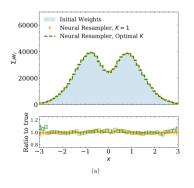
Negatively weighted Events

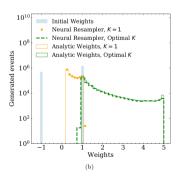


There are negative events due to Monte-Carlo fixed order simulations – "Counter Terms"

$$d\sigma_{\text{NLO}} = d\sigma_{\text{LO}} + \underbrace{d\sigma_{\text{V}}}_{=\infty} + \underbrace{\int d\Phi_{1} d\sigma_{\text{R}}}_{=\infty} = d\sigma_{\text{LO}} + \underbrace{d\sigma_{\text{V}} - \int d\Phi_{1} C}_{\neq\infty} + \underbrace{\int d\Phi_{1} (C + d\sigma_{\text{R}})}_{\neq\infty}$$

- This is a technical problem and there are solutions to this in literature "Reweighting"
- For example ,neural reweighting (from Phys. Rev. D 102, 076004 (2020))

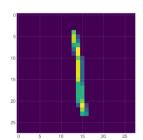


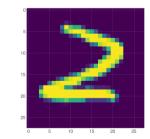


How do we consistently build a DNN based analysis for this?



- DNNs have problems when trained on samples with 'a number of' negative weights
- We can see this in a simple experiment:
 - request a DNN to classify pictures of handwritten numbers
 - Weight all the samples from a class negatively
 - Evaluate on all of the other classes

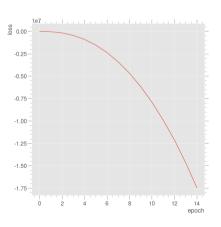




(all "weighted" with w = 1), now artificially weight (for example the 2s) with w=-1

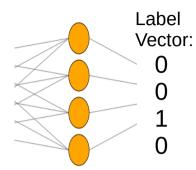
→ divergence!

Accuracy drops from ~100% to 50%



We can fix the training!





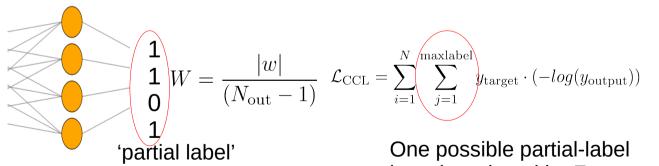
Weights:

Loss:

$$W = -w$$

$$W = -w$$
 $\mathcal{L}_{\text{CCE}} = \sum_{i=1}^{N} y_{\text{target}} \cdot (-log(y_{\text{output}}))$

Equivalent to:

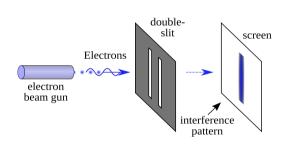


One possible partial-label loss, introduced by Feng et al (arxiv: 2007.08929)

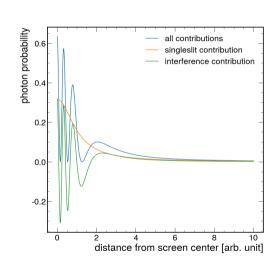
→ restores performance in MNIST toy model: Accuracy: $50\% \rightarrow 99\%$

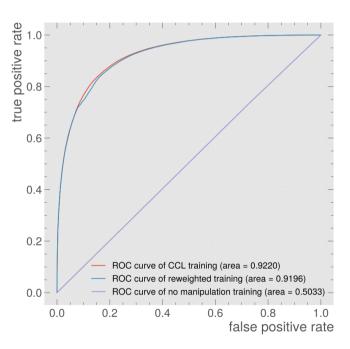
We checked it in a scenario where we have full control





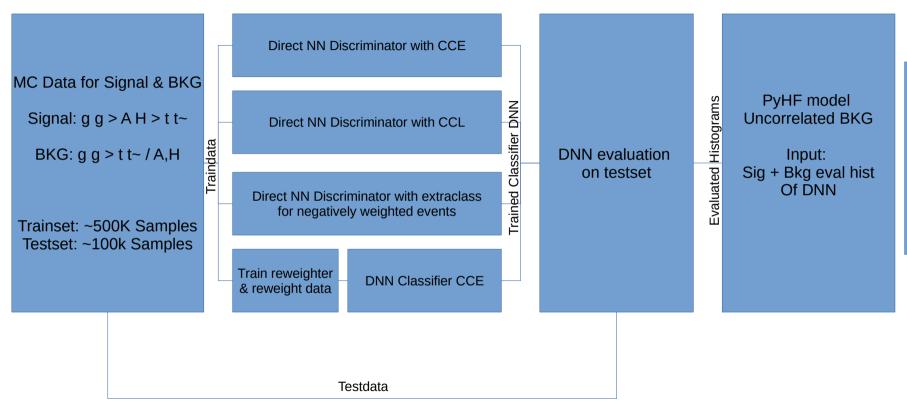
From By Original: NekoJaNekoJa Vector: Johannes Kalliauer - File:Double-slit.PNG, CC BY-SA 4.0, https://commons.wikimedia.org/w/index.php?curid=61496401





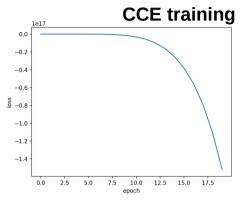
What about an analysis benchmark scenario?

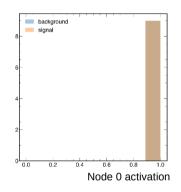


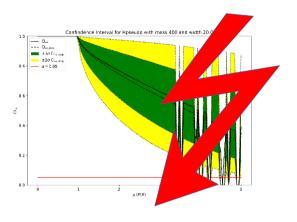


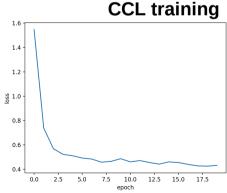
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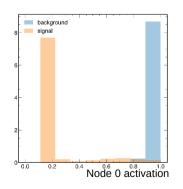


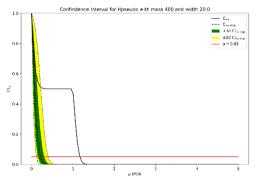








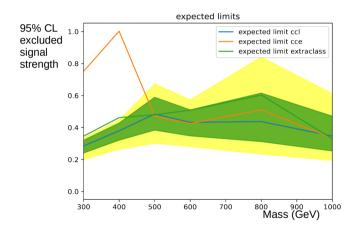




What about an analysis benchmark scenario?



- We also encountered the issue where the network evaluation produces some bins that have a negative net weight
- This is unphysical as far as DNN output bins hold physical value
- So far: worked with absolute value of bins for fit
- Currently implementing an algebra trick for yield to avoid negatively weighted events in the evaluation
- (very much WIP) results:



Conclusion



 We found a way to train DNNs in a stable manner when samples in the training distribution are negatively weighted

It can be used in a full on DNN based LHC style analysis