# HIGGS MASS PREDICTIONS IN THE CP-VIOLATING HIGH-SCALE NMSSM

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Summary

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Calculating M<sub>h</sub> in the high-scale NMSSM Matching conditions: quartic-coupling matching, pole-mass matching Implementation in NMSSMCALC Uncertainties

3 Numerical analysis Comparison with previous works The case of a light singlet





#### Supersymmetry – out of reach?



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Numerical analysis

Summary

### The Next-to-Minimal Supersymmetric Standard Model





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## The Next-to-Minimal Supersymmetric Standard Model

Complex Next-to-Minimal Supersymmetric Standard Model

Superpotential of the  $\mathbb{Z}_3$ -symmetric NMSSM

$$\mathcal{W}_{\mathsf{NMSSM}} = \left[ y_e \hat{H}_d \cdot \hat{L} \hat{E}^c + y_d \hat{H}_d \cdot \hat{Q} \hat{D}^c - y_u \hat{H}_u \cdot \hat{Q} \hat{U}^c \right] - \lambda \hat{S} \hat{H}_d \cdot \hat{H}_u + \frac{1}{3} \kappa \hat{S}^3$$

• Complex scalar singlet extension of the MSSM ( $\lambda$ ,  $\kappa$  complex, e.g.  $\lambda = |\lambda|e^{i\varphi_{\lambda}}$ )



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- Complex scalar singlet extension of the MSSM ( $\lambda$ ,  $\kappa$  complex, e.g.  $\lambda = |\lambda|e^{i\varphi_{\lambda}}$ )
- $\blacktriangleright \ \mathbb{Z}_3$  symmetry forbids linear and bilinear terms
- $\Rightarrow$  Solves the  $\mu$  problem (no dimensionful couplings in the superpotential)



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- $\mu$  parameter is generated dynamically:

$$\mu_{\rm eff} = \frac{e^{i\boldsymbol{\varphi}_{\rm S}} v_{\rm S} \lambda}{\sqrt{2}}$$



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Higgs sector



#### Higgs mass calculations in the NMSSM

#### Constraining the NMSSM parameter space with the $m_h^{SM}$ measurement

#### **Fixed-order status:**

- Full 1L, 2L, in different renormalisation schemes (DR, mixed OS-DR) [Ellwanger et al. '93, '05][Elliot et al. '93][Pandita '93][King, White '95][Degrassi, Slavich '10][Staub et al. '10][Drechsel et al. '17][Ham et al. '01-'07][Funakubo, Tao '04][Cheung et al. '10][Goodsell, Staub '17][Domingo et al. '17][Goodsell et al. '15][Ender et al. '12][Graf et al. '12][Mühlleitner et al. '14][Dao et al. '19-'21]
- Tools: FlexibleSUSY [Athron et al.], NMSSMCALC [Baglio et al.], NMSSMTools [Ellwanger et al.], SOFTSUSY [Allanach et al.], SARAH/Spheno [Porod, Staub]

#### Status of effective field theory (EFT) approach:

- ▶ Pole-mass matching in FlexibleEFTHiggs [Athron et al. '17], SARAH/Spheno [Staub, Porod '17]
- Automated full 1L EFT matching in SARAH [Gabelmann et al. '18-'19]
- ► Full 1L + (NMSSM-specific) 2L EFT matching in the real NMSSM [Bagnaschi, Goodsell, Slavich '22]



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#### Higgs mass calculations at higher orders

#### Fixed-order calculations for the Higgs mass:

- Full perturbative series truncated at fixed order
- Reliable for not too high SUSY masses
   Dominant corrections from top/stop sector, e.g. at 1-loop: ΔM<sup>2</sup><sub>h</sub> ~ m<sup>4</sup><sub>t</sub> ln m<sup>2</sup><sub>t</sub>/m<sup>2</sup><sub>t</sub>



### Higgs mass calculations at higher orders

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- Full perturbative series truncated at fixed order Reliable for not too high SUSY masses Dominant corrections from top/stop sector, e.g. at 1-loop:  $\Delta M_h^2 \sim \frac{m_t^4}{v^2} \ln \frac{m_t^2}{m_t^2}$

If SUSY masses (e.g. stops) are heavy: large separation of scales

EW scale:  $m_t \sim v \ll$  SUSY scale:  $m_{\tilde{t}} \sim M_{SUSY}$ 

$$n \frac{M_{SUSY}^2}{v^2} \gg 1$$

Large logs  $\ln \frac{M_{SUSY}^2}{v^2}$  from higher orders are relevant and **need to be resummed**!



#### Summary

#### Effective field theory approach to calculating $M_h$

Assuming **all** SUSY particles are heavy:

Consider the SM as a (renormalisable) effective field theory (EFT) valid at the EW scale ~  $m_t$  ~ v, and the NMSSM as its UV completion at the high scale ~  $M_{SUSY}$ 





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$$\lambda^{\text{SM}}(Q_{\text{match}}) \stackrel{!}{=} \lambda^{\text{NMSSM}}(Q_{\text{match}}) \stackrel{\boldsymbol{\mu}_{R}}{\bullet} Q_{\text{match}} \sim M_{\text{SUSY}}$$



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#### Effective field theory calculations:

▶ Full SUSY theory matched to low-energy EFT at high matching scale Q<sub>match</sub>



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- ▶ RGE running from high down to EFT scale: resummation of large logarithms

$$\ln(M_{SUSY}^2/v^2) = \ln(\mu_R^2/v^2) + \ln(M_{SUSY}^2/\mu_R^2)$$
resummed by RGEs + 
$$\ln(M_{SUSY}^2/\mu_R^2)$$
part of matching condition at  $\mu_R \sim Q_{match} \sim M_{SUSY}$ 



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$$\ln(M_{SUSY}^2/v^2) = \underbrace{\ln(\mu_R^2/v^2)}_{\text{resummed by RGEs}} + \underbrace{\ln(M_{SUSY}^2/\mu_R^2)}_{\text{part of matching conditions}}$$

→ Non-log terms  $O(v^2/M_{SUSY}^2)$  not included: EFT only valid for  $v/M_{SUSY} \ll 1!$ 



**Matching conditions** relate the SM and NMSSM couplings such that both theories describe the same physics at the high scale  $Q = Q_{match}$ 

 $\underbrace{V^{\text{SM}} \supset \lambda^{\text{SM}}[H]^{4}}_{\lambda^{\text{SM}}(Q) \leftrightarrow \lambda^{\text{NMSSM}}(Q), Y^{\text{SM}}_{i}(Q) \leftrightarrow Y^{\text{NMSSM}}_{i}(Q), g^{\text{SM}}_{j}(Q) \leftrightarrow g^{\text{NMSSM}}_{j}(Q), \dots$ 





Summary

#### Matching the NMSSM parameters to the SM



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#### Quartic-coupling matching

" $\lambda^{\text{SM}} = \lambda^{\text{NMSSM}}$ "

- Matching of 4-point functions
- Evaluate directly in  $\mathbf{v} \rightarrow 0$  limit
- → Analytical expressions



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Quartic-coupling matching	Pole-mass matching
" $\lambda^{SM} = \lambda^{NMSSM}$ "	$"M_h^{\rm SM} = M_h^{\rm NMSSM}"$
Matching of 4-point functions	<ul> <li>Matching of 2-point functions</li> </ul>
• Evaluate directly in $v \rightarrow 0$ limit	<ul> <li>Partial O(v<sup>2</sup> / M<sup>2</sup><sub>SUSY</sub>) terms included</li> </ul>
→ Analytical expressions	$\rightarrow$ Numerical expressions



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$\rightarrow$ Analytical expressions	$\rightarrow$ Numerical expressions

 $\Rightarrow$  Compare both approaches, estimate size of  $O(v^2/M_{SUSY}^2)$  terms





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Yukawa couplings only appear starting from one-loop corrections

 $\Rightarrow$  For one-loop matching of  $\lambda^{SM}$ , match Yukawa couplings at tree level, e.g.:

$$Y_t^{\text{NMSSM},\overline{\text{DR}}} = Y_t^{\text{SM},\overline{\text{MS}}} / \sin\beta$$





VSW

#### Matching the NMSSM parameters to the SM

**Matching conditions** relate the SM and NMSSM couplings such that both theories describe the same physics at the high scale  $Q = Q_{match}$ 

$$\xrightarrow{\sim} \lambda^{\text{SM}}[H]^{4}}{\lambda^{\text{SM}}(Q)} \leftrightarrow \lambda^{\text{NMSSM}}(Q), \quad Y_{i}^{\text{SM}}(Q) \leftrightarrow Y_{i}^{\text{NMSSM}}(Q), \quad g_{j}^{\text{SM}}(Q) \leftrightarrow g_{j}^{\text{NMSSM}}(Q), \quad \dots$$

#### Gauge couplings already appear at tree level

⇒ For one-loop matching of  $\lambda^{SM}$ , match gauge couplings at one loop:

$$g_i^{\text{NMSSM},\overline{\text{DR}}} = g_i^{\text{SM},\overline{\text{MS}}} + \delta g_i^{\text{reg}} + \delta g_i^{\text{thr}}$$

- ►  $\delta g_i^{\text{reg}}$ : one-loop regularisation scheme shifts ( $\overline{\text{DR}} \rightarrow \overline{\text{MS}}$ )
- $\delta g_i^{\text{thr}}$ : one-loop gauge threshold corrections



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## Quartic-coupling matching

Evaluated in limit of unbroken EW symmetry (i.e.  $v_u, v_d \rightarrow 0$ ) and vanishing ext. momentum, but keeping tan  $\beta$  = const.,  $v_s \neq 0$ :



**Note:**  $\Delta \lambda_h^{MSSM,2l}$ : 2L QCD and mixed QCD-EW corrections in the limit of the CP-conserving MSSM (not sensitive to the CPV phases in  $\lambda_h^{MMSSM,tree}$  and  $\Delta \lambda_h^{MMSSM,1l}$ )



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#### Quartic-coupling matching: tree-level contribution

 $\lambda^{\text{NMSSM},\overline{\text{MS}}}(Q_{\text{match}}) = \lambda_h^{\text{NMSSM},\text{tree}} + \Delta\lambda_h^{\text{NMSSM},1l} + \Delta\lambda_h^{\text{MSSM},2l}$ 





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#### Quartic-coupling matching: tree-level contribution

$$\lambda^{\text{NMSSM},\overline{\text{MS}}}(Q_{\text{match}}) = \lambda_h^{\text{NMSSM},\text{tree}} + \Delta\lambda_h^{\text{NMSSM},11} + \Delta\lambda_h^{\text{MSSM},21}$$





Numerical analysis

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### Quartic-coupling matching: tree-level contribution

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### Quartic-coupling matching: tree-level contribution

$$\lambda_{h}^{\text{NMSSM,MS}}(Q_{\text{match}}) = \lambda_{h}^{\text{NMSSM,tree}} + \Delta\lambda_{h}^{\text{NMSSM,1l}} + \Delta\lambda_{h}^{\text{MSSM,2l}}$$

$$\lambda_{h}^{\text{NMSSM,tree}} = \frac{1}{8}(g_{1}^{2} + g_{2}^{2})\cos^{2}2\beta + \frac{1}{4}|\lambda|^{2}\sin^{2}2\beta}{}_{\text{MSSM-like terms}} + \frac{1}{48}|\lambda|^{2}\sin^{2}\beta} \left(3|\kappa|^{2}M_{H^{\pm}}^{2}(1 - \cos 4\beta) + \frac{1}{48}|\kappa|^{2}M_{S}^{2}(3M_{S}^{2} + M_{A_{S}}^{2})} \left(3|\kappa|^{2}M_{H^{\pm}}^{2}(1 - \cos 4\beta) + \frac{1}{48}|\kappa|^{2}M_{S}^{2}(3M_{S}^{2} + M_{A_{S}}^{2}) \left(|\kappa||\lambda||\cos \varphi_{Y}\sin 2\beta - 2|\lambda|^{2}\right)\right)^{2}$$

Next-to-Minimal Supersymmetric Standard Model

Calculating M<sub>h</sub> in the high-scale NMSSM

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### Quartic-coupling matching: one-loop contribution

$$\lambda^{\text{NMSSM},\overline{\text{MS}}}(Q_{\text{match}}) = \lambda_h^{\text{NMSSM},\text{tree}} + \Delta\lambda_h^{\text{NMSSM},11} + \Delta\lambda_h^{\text{MSSM},21}$$

with

$$\Delta \lambda_{h}^{\text{NMSSM,1l}} = \Delta \lambda_{\Box} + \Delta \lambda_{\Delta} + \Delta \lambda_{\text{SE}} + \Delta \lambda_{\text{CT}} + \Delta \lambda_{\text{reg}} + \Delta \lambda_{\text{gauge-thr}}$$

► 
$$\overline{\text{DR}} \rightarrow \overline{\text{MS}}$$
 shifts:  $\Delta\lambda_{\text{reg}} = \frac{1}{64\pi^2} \left[ \frac{g_2^4}{3} \cos^2 2\beta - \frac{1}{2} \left( g_1^4 + 2g_1^2 g_2^2 + 3g_2^4 \right) \right]$   
► 1L gauge thresholds:  $\Delta\lambda_{\text{gauge-thr}} = \frac{1}{4} \left( g_1 \delta g_1^{\text{thr}} + g_2 \delta g_2^{\text{thr}} \right) \cos^2 2\beta + \mathcal{O} \left( (\delta g_i)^2 \right)$ 

(same as in the MSSM)


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with



• box contributions:  $\Delta \lambda_{\Box}$ 

• vertex contributions:  $\Delta \lambda_{\triangle} = -\frac{1}{2} \frac{g_{hhs}}{M_s^2} \Delta g_{hhs} - \frac{1}{2} \frac{g_{hhA_s}}{M_A^2} \Delta g_{hhA_s}$ 

1L amplitudes from SARAH with SM part already subtracted [Gabelmann et al. '18]

► self-energy contributions: 
$$\Delta\lambda_{SE} = \frac{1}{2} \left(\frac{g_{hhS}}{M_S^2}\right)^2 \Sigma_{SS}(0) + \frac{1}{2} \left(\frac{g_{hhA_s}}{M_{A_s}^2}\right)^2 \Sigma_{A_sA_s}(0) + \frac{g_{hhA_s}g_{hhS}}{M_{A_s}^2 M_S^2} \Sigma_{SA_s}(0)$$



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## Quartic-coupling matching: one-loop contribution

with  

$$\Delta\lambda_{h}^{\text{NMSSM,\overline{MS}}}(Q_{\text{match}}) = \lambda_{h}^{\text{NMSSM,tree}} + \Delta\lambda_{h}^{\text{NMSSM,11}} + \Delta\lambda_{h}^{\text{MSSM,21}}$$
with  

$$\Delta\lambda_{h}^{\text{NMSSM,11}} = \Delta\lambda_{\Box} + \Delta\lambda_{\Delta} + \Delta\lambda_{SE} + \Delta\lambda_{CT} + \Delta\lambda_{reg} + \Delta\lambda_{gauge-thr}$$

$$\delta^{(1)}Z_{h} = -\frac{d\Sigma_{hh}}{dp^{2}}\Big|_{p^{2}=0}$$

$$\Delta\lambda_{CT} = 2\lambda_{h}^{\text{NMSSM,tree}}\delta^{(1)}Z_{h} - \frac{\delta^{(1)}t_{h_{s}}}{2v_{s}}\left(\frac{g_{hhs}^{2}}{M_{s}^{2}} + \frac{g_{hhs}^{2}}{M_{s}^{2}}\right) + \frac{\delta^{(1)}t_{a_{s}}}{2v_{s}}\left(3\frac{g_{hha_{s}}^{2}}{M_{a_{s}}^{2}} \tan \varphi_{\omega} - 2\frac{g_{hha_{s}}g_{hhs}}{M_{a_{s}}^{2}M_{s}^{2}} - \frac{g_{hhs}^{2}}{M_{s}^{2}} \tan \varphi_{\omega}\right)$$

$$+ \delta^{(1)} \text{Im} A_{\lambda}\left(\frac{g_{hha_{s}}}{M_{a_{s}}^{2}}\frac{\partial g_{hha_{s}}}{\partial \text{Im} A_{\lambda}} + \frac{g_{hhs}}{M_{s}^{2}}\frac{\partial g_{hhs}}{\partial \text{Im} A_{\lambda}}\right)\Big|_{\text{min}}$$
evaluated at the minimum of the potential



Next-to-Minimal Supersymmetric Standard Model

Calculating M<sub>h</sub> in the high-scale NMSSM

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## Quartic-coupling matching: one-loop contribution



#### Intermezzo: treatment of tadpoles and counterterms

Work in  $\overline{DR}$  or  $\overline{MS}$  scheme  $\rightarrow$  no finite counterterm (CT) contributions Exception: tadpoles are calculated in a "tadpole-on-shell scheme":

$$- - \frac{t_i^{(1)}}{2} - \frac{1}{2} + - \frac{\delta^{(1)}t_i}{2} - \otimes = 0$$

such that  $\delta^{(1)}t_i = -t_i^{(1)}$ 





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such that  $\delta^{(1)}t_i = -t_i^{(1)}$ 

- ► Minimum of V<sub>H</sub> does not move: tree-level VEV corresponds to the true VEV
- ► No explicit tadpoles in loop diagrams (exactly cancelled by the tadpole CTs)
- However: tadpole CTs  $\delta^{(1)}t_i$  appearing in mass and vertex CTs





#### Intermezzo: tadpole equation for $a_d$

Tree-level tadpole equation for the  $a_d$  component (CP-odd doublet):

$$\frac{t_{a_d}}{v\sin\beta} = \frac{1}{2} |\lambda| v_s \left( -|\kappa| v_s \sin\varphi_y + \sqrt{2} \operatorname{Im} A_\lambda \cos(\varphi_\omega - \varphi_y) + \sqrt{2} \operatorname{Re} A_\lambda \sin(\varphi_\omega - \varphi_y) \right)$$
  
$$\Rightarrow \operatorname{Im} A_\lambda = \frac{\sqrt{2}}{|\lambda| v_s \cos(\varphi_\omega - \varphi_y) \sin\beta} \frac{t_{a_d}}{v} + \frac{|\kappa| v_s}{\sqrt{2}} \frac{\sin\varphi_y}{\cos(\varphi_\omega - \varphi_y)} - \operatorname{Re} A_\lambda \tan(\varphi_\omega - \varphi_y)$$

with the tree-level tadpole  $t_{a_d} = t_{a_d}^{(0)} = 0$  at the minimum.



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Tree-level tadpole equation for the  $a_d$  component (CP-odd doublet):

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$$\Rightarrow \operatorname{Im} A_{\lambda} = \frac{\sqrt{2}}{|\lambda| v_{\rm S} \cos(\varphi_{\omega} - \varphi_{\rm y}) \sin\beta} \frac{t_{a_d}}{v} + \frac{|\kappa| v_{\rm S}}{\sqrt{2}} \frac{\sin\varphi_{\rm y}}{\cos(\varphi_{\omega} - \varphi_{\rm y})} - \operatorname{Re} A_{\lambda} \tan(\varphi_{\omega} - \varphi_{\rm y})$$

with the tree-level tadpole  $t_{a_d} = t_{a_d}^{(0)} = 0$  at the minimum.

→ Finite CT contribution from  $t_{a_d} \rightarrow t_{a_d}^{(0)} + \delta^{(1)} t_{a_d}$  (all other pars. renormalised DR):

$$\delta^{(1)} \operatorname{Im} A_{\lambda} = \frac{\sqrt{2}}{|\lambda| v_{S} \cos(\varphi_{\omega} - \varphi_{y}) \sin \beta} \frac{\delta^{(1)} t_{a_{d}}}{v} \longrightarrow$$



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Tree-level tadpole equation for the  $a_d$  component (CP-odd doublet):

$$\frac{t_{a_d}}{v\sin\beta} = \frac{1}{2} |\lambda| v_S \left( -|\kappa| v_S \sin\varphi_y + \sqrt{2} \operatorname{Im} A_\lambda \cos(\varphi_\omega - \varphi_y) + \sqrt{2} \operatorname{Re} A_\lambda \sin(\varphi_\omega - \varphi_y) \right)$$
  
$$\Rightarrow \operatorname{Im} A_\lambda = \frac{\sqrt{2}}{|\lambda| v_S \cos(\varphi_\omega - \varphi_y) \sin\beta} \frac{t_{a_d}}{v} + \frac{|\kappa| v_S}{\sqrt{2}} \frac{\sin\varphi_y}{\cos(\varphi_\omega - \varphi_y)} - \operatorname{Re} A_\lambda \tan(\varphi_\omega - \varphi_y)$$

with the tree-level tadpole  $t_{a_d} = t_{a_d}^{(0)} = 0$  at the minimum.

→ Finite CT contribution from  $t_{a_d} \rightarrow t_{a_d}^{(0)} + \delta^{(1)} t_{a_d}$  (all other pars. renormalised DR):

 $δ<sup>(1)</sup> Non-vanishing contribution from <math>δ<sup>(1)</sup>t_{a_d}/v$  for  $v \to 0!$ 



Demand that the pole masses  $M_h^{\chi}$  (X = SM, NMSSM) of the SM-like Higgs states are the same:

$$(M_h^{\text{SM}})^2 \stackrel{!}{=} (M_h^{\text{NMSSM}})^2$$

e.g. [Athron et al. '16], [Braathen et al. '18]

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with  $(M_h^X)^2 = (m_h^X)^2 - \text{Re}\,\hat{\Sigma}_h^X (p^2 = (M_h^X)^2)$ 

- $m_h^{\chi}$ : SM(-like)  $\overline{\text{MS}}$  ( $\overline{\text{DR}}$ ) Higgs mass in the SM (NMSSM)
- $\hat{\Sigma}_{h}^{X}$ :  $\overline{MS}$  ( $\overline{DR}$ ) renormalised self energies in the SM (NMSSM)



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Expansion of self energy around small external momenta:

 $\operatorname{Re} \hat{\Sigma}_h^{\boldsymbol{X}} \big( (\boldsymbol{m}_h^{\boldsymbol{X}})^2 \big) = \hat{\Sigma}_h^{\boldsymbol{X}}(0) + (\boldsymbol{m}_h^{\boldsymbol{X}})^2 \, \hat{\Sigma}_h^{\boldsymbol{X}'}(0) + \mathcal{O} \big( (\boldsymbol{m}_h^{\boldsymbol{X}})^4 \big)$ 



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Gauge thresholds at one loop:

$$\begin{pmatrix} m_h^{\text{NMSSM}} \end{pmatrix}^2 \equiv \begin{pmatrix} m_h^{\text{NMSSM}}(g_i^{\text{NMSSM},\overline{\text{DR}}} \to g_i^{\text{SM},\overline{\text{MS}}} + \delta g_i) \end{pmatrix}^2$$
$$= \begin{pmatrix} m_h^{\text{NMSSM}}(g_i^{\text{SM},\overline{\text{MS}}}) \end{pmatrix}^2 + \frac{\delta^{\text{gauge}}m_h^2}{\delta^{\text{gauge}}m_h^2} + \mathcal{O}((\delta g_i)^2)$$



Summary

# Pole-mass matching: tree-level contribution

At tree level, pole masses = tree-level masses:

$$(M_h^{\text{SM}})^2 \stackrel{!}{=} (M_h^{\text{NMSSM}})^2 \Rightarrow (m_h^{\text{SM}})^2 \stackrel{!}{=} (m_h^{\text{NMSSM}})^2$$

Use  $\overline{\text{MS}}$  relation  $(m_h^{\text{SM}})^2 = 2(v^{\text{SM}})^2 \lambda_h^{\text{SM}}$  and solve for  $\lambda_h^{\text{SM}}$ :

$$\lambda_h^{\rm SM} = \frac{(m_h^{\rm NMSSM})^2}{2(v^{\rm NMSSM})^2}$$

where  $v^{\text{NMSSM}} = v^{\text{SM}}$  and  $\delta g_i = 0$  (tree-level matching of the VEV and the  $g_i$ )



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where  $v^{\text{NMSSM}} = v^{\text{SM}}$  and  $\delta g_i = 0$  (tree-level matching of the VEV and the  $g_i$ )

Analytical diagonalisation of tree-level mass matrix & expansion in  $v/M_{SUSY}$ : obtained same expression as for tree-level quartic-coupling matching!



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# Pole-mass matching: one-loop contribution

At one loop, take into account 1L self energies (reuse from implementation for fixed-order calculations in NMSSMCALC):

$$(M_h^{\text{SM}})^2 \stackrel{!}{=} (M_h^{\text{NMSSM}})^2 \implies (m_h^{\text{SM}})^2 - \text{Re}\,\hat{\Sigma}_h^{\text{SM}}\big((m_h^{\text{SM}})^2\big) \stackrel{!}{=} (m_h^{\text{NMSSM}})^2 - \text{Re}\,\hat{\Sigma}_h^{\text{NMSSM}}\big((m_h^{\text{NMSSM}})^2\big)$$



At one loop, take into account 1L self energies (reuse from implementation for fixed-order calculations in NMSSMCALC):

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At one loop, take into account 1L self energies (reuse from implementation for fixed-order calculations in NMSSMCALC):

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Expand for small ext. moms., again use  $(m_h^{SM})^2 = 2(v^{SM})^2 \lambda_h^{SM}$ , and solve for  $\lambda_h^{SM}$ :

$$\lambda_h^{\rm SM} = \frac{1}{2(v^{\rm NMSSM})^2} \left[ (m_h^{\rm NMSSM})^2 \left( 1 - 2\Delta \hat{\Sigma}_h' \right) - \Delta \hat{\Sigma}_h \right]$$



with  $\Delta \hat{\Sigma}_{h}^{(\prime)} \equiv \hat{\Sigma}_{h}^{\text{NMSSM}(\prime)}(0) - \hat{\Sigma}_{h}^{\text{SM}(\prime)}(0)$ 

 $\Rightarrow$  Consistent expansion at 1L, get  $v/M_{SUSY}$  corrections for free!



At one loop, take into account 1L self energies (reuse from implementation for fixed-order calculations in NMSSMCALC):

$$(M_h^{\text{SM}})^2 \stackrel{!}{=} (M_h^{\text{NMSSM}})^2 \implies (m_h^{\text{SM}})^2 \stackrel{!}{=} (m_h^{\text{NMSSM}})^2 - \text{Re}\,\hat{\Sigma}_h^{\text{NMSSM}}\big((m_h^{\text{NMSSM}})^2\big) + \text{Re}\,\hat{\Sigma}_h^{\text{SM}}\big((m_h^{\text{SM}})^2\big)$$

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with  $\Delta \hat{\Sigma}_{h}^{(\prime)} \equiv \hat{\Sigma}_{h}^{\text{NMSSM}(\prime)}(0) - \hat{\Sigma}_{h}^{\text{SM}(\prime)}(0)$  $\Rightarrow \text{ Consi} \text{ Large cancellations! } 1L, get v/M_{\text{SUSY}} \text{ corrections for free!}$ 



At one loop, take into account 1L self energies (reuse from implementation for fixed-order calculations in NMSSMCALC):

$$(M_{h}^{\text{SM}})^{2} \stackrel{!}{=} (M_{h}^{\text{NMSSM}})^{2} \Rightarrow (m_{h}^{\text{SM}})^{2} \stackrel{!}{=} (m_{h}^{\text{NMSSM}})^{2} - \operatorname{Re} \hat{\Sigma}_{h}^{\text{NMSSM}} ((m_{h}^{\text{NMSSM}})^{2}) + \operatorname{Re} \hat{\Sigma}_{h}^{\text{SM}} ((m_{h}^{\text{SM}})^{2})$$
  
Expand for small ext. moms., again use  $(m_{h}^{\text{SM}})^{2} = 2(v^{\text{SM}})^{2}\lambda_{h}^{\text{SM}}$ , and solve for  $\lambda_{h}^{\text{SM}}$ :  
$$\lambda_{h}^{\text{SM}} = \frac{1}{2(v^{\text{NMSSM}})^{2}} \left[ (m_{h}^{\text{NMSSM}})^{2} (1 - 2\Delta \hat{\Sigma}_{h}) - \Delta \hat{\Sigma}_{h} \right]$$

with 
$$\Delta \hat{\Sigma}_{h}^{(\prime)} \equiv \hat{\Sigma}_{h}^{\text{NMSSM}(\prime)}(0) - \hat{\Sigma}_{h}^{\text{SM}(\prime)}(0)$$
  
 $\Rightarrow \text{ Consi}$ 
Large cancellations! 1L, get v
(One-loop matching of the VEV, e.g. [Braathen et al. '18])





At one loop, take into account 1L self energies (reuse from implementation for fixed-order calculations in NMSSMCALC):

 $(M^{\text{SM}})^2 \stackrel{!}{=} (M^{\text{SMSSM}})^2 \xrightarrow{} (m^{\text{SM}})^2 \stackrel{!}{=} (m^{\text{SMSSM}})^2 - \text{Re} \hat{\Sigma}_h^{\text{SMSSM}}((m^{\text{SMSSM}}_h)^2) + \text{Re} \hat{\Sigma}_h^{\text{SM}}((m^{\text{SM}}_h)^2)$ **Numerical limit of**  $v \rightarrow 0$ : excellent agreement with  $\lambda_{h}^{SM}$  from quartic-coupling matching! =  $2(v^{SM})^2 \lambda_b^{SM}$ , and solve for  $\lambda_b^{SM}$ :  $\rightarrow \lambda_h^{\text{SM}} = \frac{1}{2(v^{\text{NMSSM}})^2} \left[ (m_h^{\text{NMSSM}})^2 (1 - 2\Delta \hat{\Sigma}_h') - \Delta \hat{\Sigma}_h \right]$ with  $\Delta \hat{\Sigma}_{h}^{(\prime)} \equiv \hat{\Sigma}_{h}^{\text{NMSSM}(\prime)}(0) - \hat{\Sigma}_{h}^{\text{SM}(\prime)}(0)$   $\Rightarrow \text{ Consi}$ Large cancellations! 1L, get v (One-loop matching of the VEV, e.g. [Braathen et al. '18])





Summary

### NMSSMCALC algorithm to determine SM Higgs mass prediction $M_h$





## NMSSMCALC algorithm to determine SM Higgs mass prediction M<sub>h</sub>



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### NMSSMCALC algorithm to determine SM Higgs mass prediction M<sub>h</sub>





Summary

### NMSSMCALC algorithm to determine SM Higgs mass prediction $M_h$





## Uncertainty estimate (I)

- SM uncertainties:
  - ► missing EW corrections (from choice of input scheme):  $\Delta_{G_F/\alpha_{M_2}}^{SM} = |M_h^{G_F} M_h^{\alpha_{M_2}}|$
  - missing h.o. terms in  $\overline{\text{MS}}$ -OS conversion between  $\lambda_h^{\text{SM},\text{MS}}$  and  $M_h$ :

$$0 \stackrel{!}{=} p^2 - 2\lambda_h^{\text{SM},\overline{\text{MS}}}(Q_{\text{EW}}) v^2(Q_{\text{EW}}) + \text{Re}\,\hat{\Sigma}_h^{\text{SM},\overline{\text{MS}}}(p^2,Q_{\text{EW}})$$

Solve iteratively for  $p^2 = M_h^{\overline{\text{MS}},\text{pole}}(Q_{\text{EW}})$ , vary  $Q_{\text{EW}}$ :

$$\Delta^{\text{SM}}_{Q_{\text{EW}}} = \max\left\{|M^{\text{OS}}_h - M^{\overline{\text{MS}},\text{pole}}_h(2M_t)|, |M^{\text{OS}}_h - M^{\overline{\text{MS}},\text{pole}}_h(M_t/2)|\right\}$$

• missing 3L top corrections: 
$$\Delta_{Y_t}^{SM} = M_h(Y_t^{\odot(\alpha_s^2)}) - M_h(Y_t^{\odot(\alpha_s^3)})$$



## Uncertainty estimate (II)

- SUSY uncertainties:
  - variation of the matching scale Q<sub>match</sub> with respect to the SUSY input scale M<sub>SUSY</sub>:

$$\Delta_{Q_{\text{match}}}^{\text{SUSY}} = \max\left\{ |M_h^{M_{\text{SUSY}}/2} - M_h^{M_{\text{SUSY}}}|, |M_h^{2M_{\text{SUSY}}} - M_h^{M_{\text{SUSY}}}| \right\}$$



## Uncertainty estimate (II)

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#### **Combined uncertainty:**

For pole-mass  
matching 
$$M_h^{\text{II}}$$
: 
$$\Delta M_h^{\text{II}} = \left[ \left( \Delta_{G_F}^{\text{SM}} \right)^2 + \left( \Delta_{Q_{\text{EW}}}^{\text{SM}} \right)^2 + \left( \Delta_{Y_t}^{\text{SM}} \right)^2 + \left( \Delta_{Q_{\text{match}}}^{\text{SUSY}} \right)^2 \right]^{\frac{1}{2}}$$
  
For quartic-coupling  
matching  $M_h^{\text{IV}}$ : 
$$\Delta M_h^{\text{IV}} = \left[ \left( \Delta M_h^{\text{II}} \right)^2 + \left( \underbrace{M_h^{\text{II}} - M_h^{\text{IV}}}_{V^2/M_{\text{SUSY}}^2} \right)^2 \right]^{\frac{1}{2}}$$
  
"EFT uncertainty"



## Comparison with previous works







## Comparison with previous works



Summary

## The case of a light singlet







## The case of a light singlet





# v/M<sub>SUSY</sub> effects



[CB, Dao, Gabelmann, Mühlleitner, Rzehak '24]

#### **Parameter scan:**

$$\begin{split} &100 \, \text{GeV} \leq M_1, M_2 \leq 1.5 \, \text{TeV}, \quad 100 \, \text{GeV} \leq \mu_{\text{eff}} \leq 1.5 \, \text{TeV}, \\ &1 \, \text{TeV} \leq m_{\tilde{Q}_{L_3}}, m_{\tilde{t}_{R_3}} \leq 2.5 \, \text{TeV}, \quad M_{\text{SUSY}} = \sqrt{m_{\tilde{Q}_{L_3}}} m_{\tilde{t}_{R_3}}, \\ &M_3 = \max\{M_{\text{SUSY}}, 2.3 \, \text{TeV}\}, \quad -2.5 \, \text{TeV} \leq A_{\kappa} \leq 100 \, \text{GeV}, \\ &-2.5 \, \text{TeV} \leq A_{\lambda} \leq 2.5 \, \text{TeV}, \quad -\sqrt{6} \leq \hat{X}_t \leq \sqrt{6}, \\ &1 \leq \tan\beta \leq 20, \quad 0.05 \leq \lambda, \kappa \leq 1.0 \end{split}$$

#### **Bounds and constraints:**

- ▶  $M_{\tilde{t}_1} > 1310 \text{ GeV}, M_{\tilde{g}} > 2.3 \text{ GeV}, M_{H^+} > 500 \text{ GeV}$
- ▶ 122 GeV  $\leq M_h^{\text{II}} \leq 128 \text{ GeV}$
- Using HiggsTools [Bahl et al. '22] to check for compatibility with data from LEP, Tevatron, LHC



### Effects of CP-violating phases

[CB, Dao, Gabelmann, Mühlleitner, Rzehak '24]





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## Effects of CP-violating phases



[CB, Dao, Gabelmann, Mühlleitner, Rzehak '24]







#### Summary

#### Calculation of the SM-like Higgs mass in the EFT approach for the CPV NMSSM

- Applicable for heavy SUSY masses  $(v/M_{susy} \ll 1)$ , resums large logarithms
- Implementation at full 1L (+2L MSSM) via quartic-coupling & pole-mass matching
  - $\rightarrow$  Excellent agreement found for CPC and CPV case in v  $\rightarrow$  0 limit  $\checkmark$ arXiv:2406.17635
  - $\rightarrow$  Estimate of v/M<sub>susy</sub> contributions for EFT uncertainty

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Implementation in our code NMSSMCALC (https://itp.kit.edu/~maggie/NMSSMCALC)

[Baalio, CB, Dao, Gabelmann, Gröber, Krause, Mühlleitner, Le, Rzehak, Spira, Streicher, Walz]

- Spectrum calculator of 1L & 2L Higgs masses, self couplings, decay widths New: EFT implementation for M<sub>h</sub>!
- For the CP-conserving and CP-violating NMSSM
- ...and more: electron EDMs, muon q 2,  $\rho$  parameter,  $M_{\mu\nu}$


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### THANK YOU FOR YOUR ATTENTION! 🙂





# Backup

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## NMSSM tree-level Higgs masses in the unbroken phase limit

Higgs mass matrix  $\mathcal{M}_{ij}$  becomes block-diagonal for  $v \rightarrow 0$ , easy to diagonalise analytically (<u>after</u> applying tadpole equations):

$$\begin{split} h_{1} \sim h_{u} : & m_{h_{1}}^{2} \equiv m_{h_{SM}}^{2} = 0 \quad (\text{since it is } \propto v^{2}) \\ h_{2} \sim a_{s} : & m_{h_{2}}^{2} \equiv M_{A_{s}}^{2} = -\frac{3|\kappa| \operatorname{Re} A_{\kappa} v_{S}}{\sqrt{2} \cos \varphi_{w}} \\ h_{3} \sim a_{d} : & m_{h_{3}}^{2} = M_{H^{\pm}}^{2} = \frac{|\lambda| v_{s} \left(\sqrt{2} \operatorname{Re} A_{\lambda} + |\kappa| v_{s} \cos \varphi_{w}\right)}{\sin \beta \cos \beta \cos(\varphi_{w} - \varphi_{y})} \\ h_{4} \sim h_{d} : & m_{h_{4}}^{2} = m_{h_{3}}^{2} \\ h_{5} \sim h_{s} : & m_{h_{5}}^{2} \equiv M_{S}^{2} = \frac{|\kappa| v_{s} \left(4|\kappa| v_{s} + \sqrt{2} \frac{\operatorname{Re} A_{\kappa}}{\cos \varphi_{w}}\right)}{2} \end{split}$$



## Backup Quartic-coupling matching: couplings

$$\begin{split} g_{hhS} &= \frac{1}{2v_s} \left( |\kappa| |\lambda| v_s^2 \sin(2\beta) \cos \varphi_y - 2|\lambda|^2 v_s^2 + M_{H^{\pm}}^2 \sin^2(2\beta) \right), \\ g_{hhA_s} &= -\frac{3}{2} |\kappa| |\lambda| v_s \sin(2\beta) \sin \varphi_y, \\ \frac{\partial g_{hhS}}{\partial \operatorname{Im} A_{\lambda}} &= -|\lambda| \sin(2\beta) \sin(\varphi_{\omega} - \varphi_y), \\ \frac{\partial g_{hhA_s}}{\partial \operatorname{Im} A_{\lambda}} &= -|\lambda| \sin(2\beta) \cos(\varphi_{\omega} - \varphi_y) \end{split}$$



# Contribution of $a_d$ tadpole for $v \rightarrow 0$

Backup

One-loop contribution from stops (after expanding stop mixing matrices to O(v)):

$$\delta^{(1)}t_{a_d} = v \frac{3|\lambda||A_t|v_S Y_t^2}{16\pi^2 \sqrt{2}\sin\beta} B(m_{\tilde{Q}_3}, m_{\tilde{U}_{R,3}}) \sin(\varphi_\omega - \varphi_y + \varphi_{A_t})$$

with  $B(x, y) = (A(x) - A(y))/(x^2 - y^2)$  and  $A(x) = x^2(1 + \ln(\mu^2/x^2))$ 

General way of computing the contributions: one-loop effective potential:

$$\begin{split} \delta^{(1)}t_{a_d} &= v \cdot \left. \frac{\partial t_{a_d}}{\partial v} \right|_{v=0} + \mathcal{O}(v^2) = v \cdot \left. \frac{\partial^2 V(h, a_d, \dots)}{\partial a_d \partial h} \right|_{h=a_d=0; v=0} + \mathcal{O}(v^2) \\ &= v \cdot \Sigma_{h \to a_d} (p^2 = 0) \Big|_{v=0} + \mathcal{O}(v^2) \\ &= v \cdot \left( \sin \beta \Sigma_{h \to G} (p^2 = 0) - \cos \beta \Sigma_{h \to A} (p^2 = 0) \right) \Big|_{v=0} + \mathcal{O}(v^2) \end{split}$$



# One-loop gauge thresholds

Backup

e.g. [Bagnaschi, Giudice, Slavich, Strumia '14]

$$\begin{split} \delta g_{1}^{\mathrm{thr}} &= -\frac{g_{1}^{3}}{512\pi^{2}} \left[ 12 \ln \frac{\mu_{\mathrm{eff}}^{2}}{Q^{2}} + 3 \ln \frac{M_{H^{\pm}}^{2}}{Q^{2}} + \sum_{i=3}^{2} \left( 3 \ln \frac{m_{\tilde{L}_{i}}^{2}}{Q^{2}} + 6 \ln \frac{m_{\tilde{e}_{R,i}}^{2}}{Q^{2}} \right) \right. \\ &\quad + \left. \sum_{i=1}^{3} \left( \ln \frac{m_{\tilde{Q}_{i}}^{2}}{Q^{2}} + 8 \ln \frac{m_{\tilde{u}_{R,i}}^{2}}{Q^{2}} + 2 \ln \frac{m_{\tilde{d}_{R,i}}^{2}}{Q^{2}} \right) \right], \\ \delta g_{2}^{\mathrm{thr}} &= -\frac{g_{2}^{3}}{192\pi^{2}} \left[ 8 \ln \frac{M_{2}^{2}}{Q^{2}} + 4 \ln \frac{\mu_{\mathrm{eff}}^{2}}{Q^{2}} + \ln \frac{M_{H^{\pm}}^{2}}{Q^{2}} + \sum_{i=3}^{2} \left( \ln \frac{m_{\tilde{L}_{i}}^{2}}{Q^{2}} + 3 \ln \frac{m_{\tilde{Q}_{i}}^{2}}{Q^{2}} \right) \right], \\ \delta g_{3}^{\mathrm{thr}} &= -\frac{g_{3}^{3}}{192\pi^{2}} \left[ 12 \ln \frac{M_{3}^{2}}{Q^{2}} + \sum_{i=1}^{3} \left( 2 \ln \frac{m_{\tilde{Q}_{i}}^{2}}{Q^{2}} + \ln \frac{m_{\tilde{u}_{R,i}}^{2}}{Q^{2}} + \ln \frac{m_{\tilde{d}_{R,i}}^{2}}{Q^{2}} \right) \right] \end{split}$$





# Benchmark points (I)

BP1: [Bagnaschi et al. '22] BP2: [Slavich et al. '20] BP3: our own scan

	tan β	λ	к	<b>M</b> 1	M <sub>2</sub>	M <sub>3</sub>	A <sub>t</sub>	$A_{\lambda}$	$A_{\kappa}$	$\mu_{eff.}$	$m_{\tilde{Q}_{L_3}}$	$m_{\tilde{t}_{R_3}}$
BP1	3.0	0.6	0.6	1.0	2.0	2.5	12.75	0.3	-2.0	1.5	5.0	5.0
BP2	20.0	0.05	0.05	3.0	3.0	3.0	-7.20	-2.85	-1.0	3.0	3.0	3.0
BP3	1.27	0.73	0.62	0.24	1.18	2.3	-0.39	0.06	-1.44	0.49	1.79	1.51

	$M_h^{\mathrm{II}}$	M <sup>™</sup> <sub>h</sub>	$m_{h_2}$	<i>m</i> <sub><i>h</i><sub>3</sub></sub>	m <sub>A1</sub>	m <sub>A2</sub>	m <sub>H⁺</sub>
BP1	124.29 (h <sub>u</sub> )	124.31 (h <sub>u</sub> )	2407.6 (h <sub>s</sub> )	2971.8 (h <sub>d</sub> )	2905.7 (a)	3000.2 (a <sub>s</sub> )	2967.1
BP2	125.26 (h <sub>u</sub> )	125.28 (h <sub>u</sub> )	2996.4 (h <sub>d</sub> )	5744.4 (h <sub>s</sub> )	2985.3 (a <sub>s</sub> )	3010.5 (a)	2997.8
BP3	127.18 (h <sub>u</sub> )	129.47 (h <sub>u</sub> )	305.5 (h <sub>s</sub> )	659.5 (h <sub>d</sub> )	663.8 (a)	1308.7 (a <sub>s</sub> )	658.4





## Benchmark points (II)

### Other SUSY masses:

	$m_{\tilde{t}_1}$	$m_{\tilde{t}_2}$	$m_{\chi_1^0}$	$m_{\chi^0_2}$	$m_{\chi^0_3}$	$m_{\chi_{4}^{0}}$	$m_{\chi_5^0}$	$m_{\chi_1^+}$	$m_{\chi_2^*}$
BP1	4829.6	5168.2	997.2	1491.5	1502.4	2010.5	3003.3	1490.2	2010.5
BP2	2831.6	3164.7	2932.7	3000.0	3000.0	3067.9	6000.0	2940.9	3060.0
BP3	1514.2	1799.1	232.8	484.1	498.2	835.4	1192.7	477.3	1192.6

### Uncertainties:

	$\Delta_{Y_t}^{SM}$	$\Delta_{Q_{EW}}^{SM}$	$\Delta^{SM}_{G_F/\alpha_{M_Z}}$	$\Delta_{Q_{match}}^{SUSY}$	$\Delta_{v^2/M_{SUSY}^2}^{SUSY}$	$\Delta M_h^{II}$	∆M <sup>™</sup> <sub>h</sub>
BP1	-738	208	-19	376	-21	854	836
BP1	-679	212	-69	403	-12	819	820
BP1	-401	197	21	834	-2294	947	2452



## Quartic-coupling vs. pole-mass matching for $v \rightarrow 0$



Christoph Borschensky – Higgs Mass Predictions in the CPV High-Scale NMSSM

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## Comparison between EFT and fixed-order results

