

The Seiberg-Witten Axion

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מכון רקה
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of Physics



Axion-Photon Coupling

Peccei-Quinn Mechanism



- Quantized anomaly generated coupling

$$\mathcal{L} \supset -\frac{a}{f} \left(\sum_i Q_{PQ} q_i^2 \right) \frac{e^2}{16\pi^2} F \tilde{F} \propto \sum_i \dots \dots \dots \otimes \begin{array}{c} q_i \\ \nearrow Q_{PQ} \\ \downarrow \\ q_i \end{array}$$

- **Heuristic:** magnetically charged PQ fermions $\alpha^{-2} \sim 10^4$ enhancement

$$e \rightarrow \frac{4\pi}{e}, \quad \mathcal{L} \sim \frac{1}{e^2} \frac{a}{f} F \tilde{F}$$

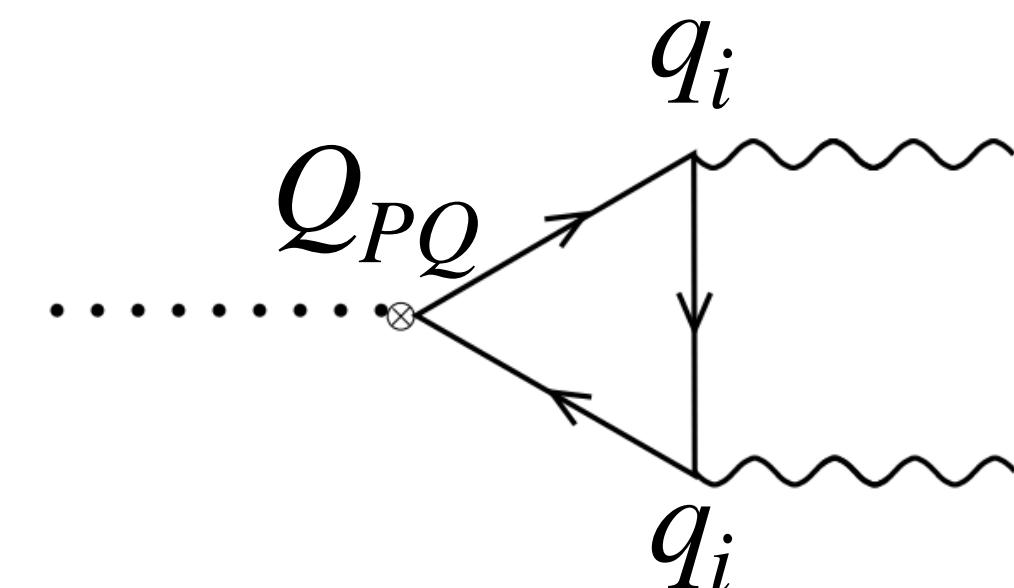
Can the axion coupling be large?

Example: Instantons



$$\begin{aligned}\mathcal{L} &\supset -\frac{e^2}{16\pi^2} F_{\mu\nu} \widetilde{F}^{\mu\nu} \left\{ N \frac{a}{f} - \sum_{k=1}^{\infty} \left[b_k \sin\left(\frac{ka}{f}\right) + c_k \cos\left(\frac{ka}{f}\right) \right] \right\} \\ &\simeq -\frac{e^2}{16\pi^2} F_{\mu\nu} \widetilde{F}^{\mu\nu} \frac{a}{f} \left\{ \boxed{N} - \boxed{\sum_k k b_k} \right\} + O\left(\frac{a^2}{f^2}\right)\end{aligned}$$

Usual anomaly



Instanton corrections

Linear coefficient not quantized
and can be large!

Is axion QED duality covariant? Can we keep Bianchi? (Answer: Yes!)



- Maxwell equations + axion

[Sikivie '83]

$$\partial_\mu F^{\mu\nu} = -g_{a\gamma}(\partial_\mu a) \widetilde{F}^{\mu\nu}, \quad \partial_\mu \widetilde{F}^{\mu\nu} = 0$$

EOM

Bianchi identity

- Seems **inconsistent** w/S-duality ($F^{\mu\nu} \rightarrow \widetilde{F}^{\mu\nu}$, $\widetilde{F}^{\mu\nu} \rightarrow -F^{\mu\nu}$)

- Naive fix

$$\partial_\mu F^{\mu\nu} = -g_{a\gamma}(\partial_\mu a) \widetilde{F}^{\mu\nu}, \quad \partial_\mu \widetilde{F}^{\mu\nu} = g_{a\gamma} \partial_\mu F^{\mu\nu}$$

[Ringwald & Sokolov '22]

Violates Bianchi identity

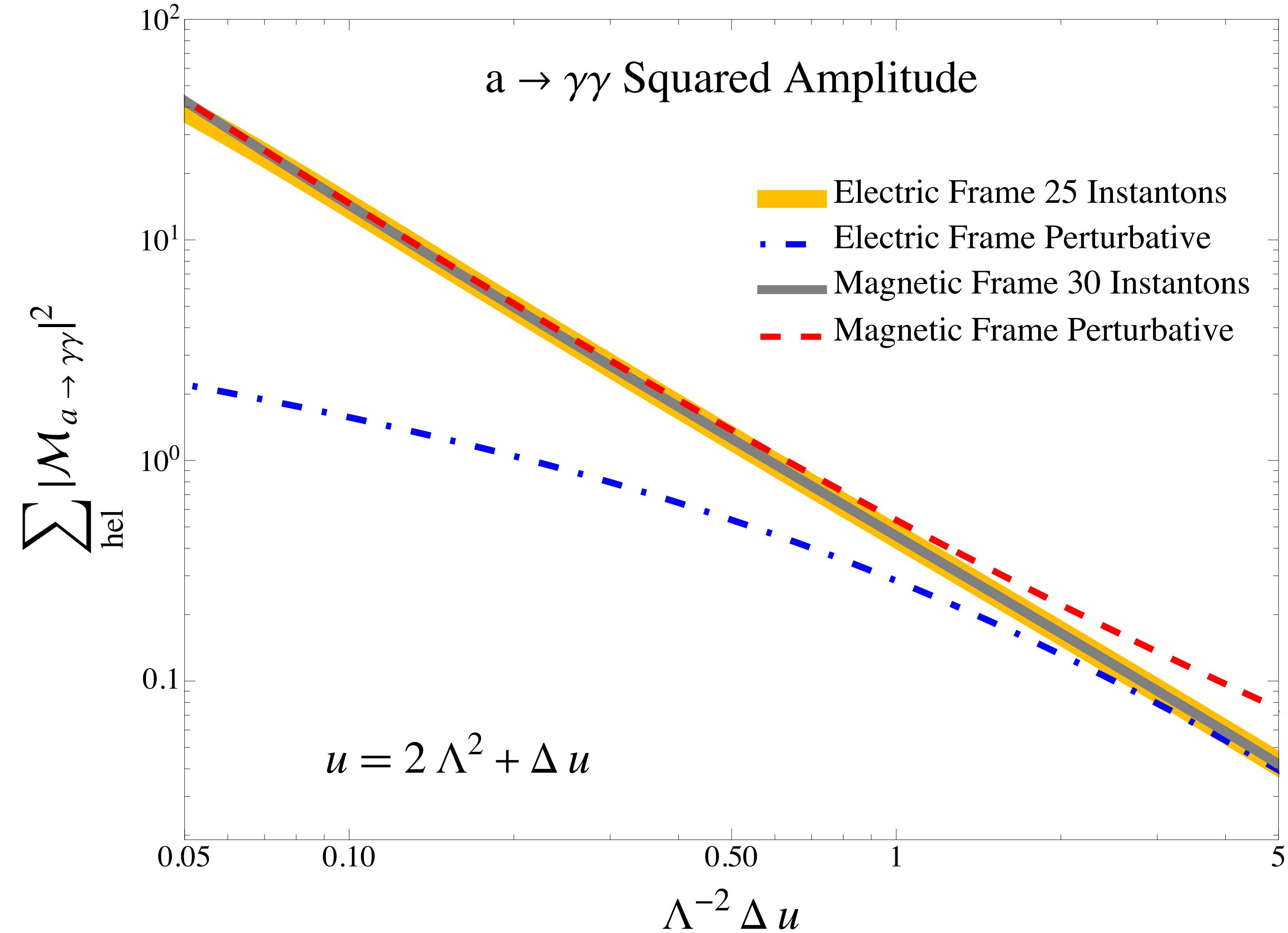
Why Seiberg-Witten theory?

It has all the ingredients.



- We need a toy model that has:
 - IR axion electrodynamics [our contribution]
 - Weak and strongly coupled regimes
 - EM duality
 - Charges and monopoles
 - Analytic control over instantons (SUSY)

$\mathcal{N} = 2$, **SU(2) Super
Yang-Mills has them all**
[Seiberg & Witten '94]



- Generalization + string theory axion EFT [arXiv: 2509.XXXXX]