



Broken Weyl Gravity

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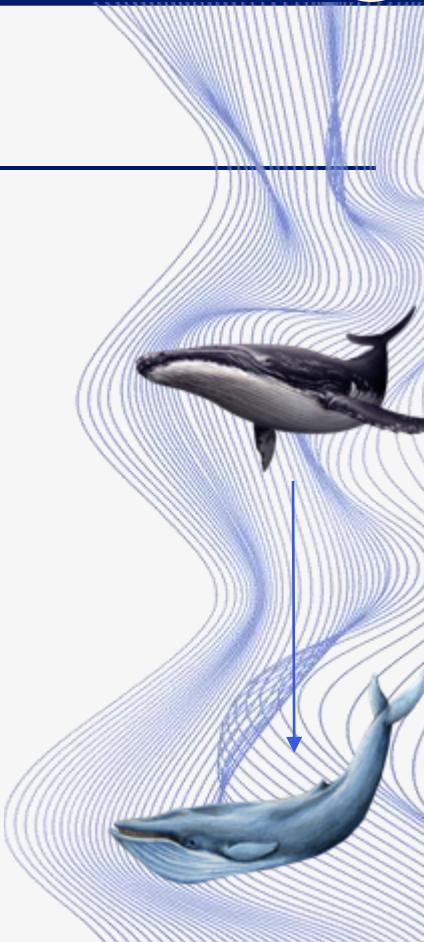
Work with Irvin Martinez [2509.xxxxx]



Weyl Transformations

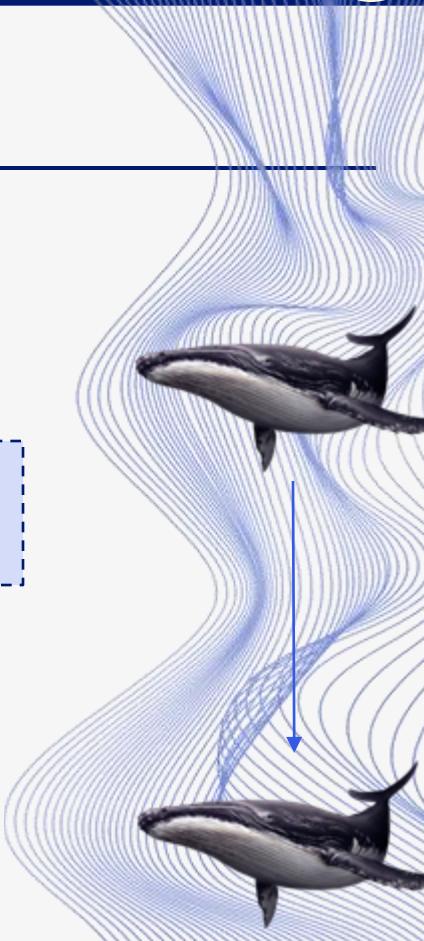
$$g_{\mu\nu}(x) \rightarrow \Omega^2(x) g_{\mu\nu}(x)$$

$$\phi(x) \rightarrow \Omega^{-\Delta}(x) \phi(x)$$



Route to Weyl invariance

Iorio et. al. [9607110]





CCWZ Coset construction

Callan, Coleman, Wess & Zumino (1969)

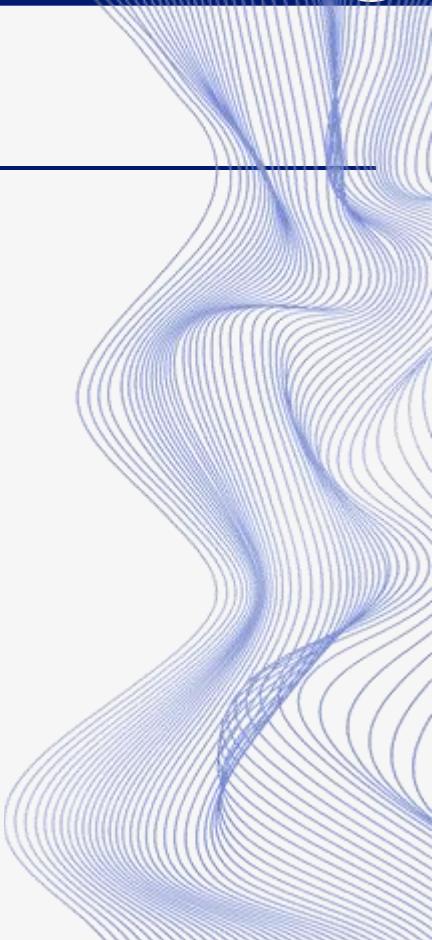
$$g = e^{ix_a P^a} e^{i\pi_\alpha(x) Z^\alpha}$$

$$g^{-1}dg = e^a P_a + \omega^\alpha Z_\alpha + \omega^A T_A$$



Algebra

$$[P_\mu, D] = -i P_\mu$$

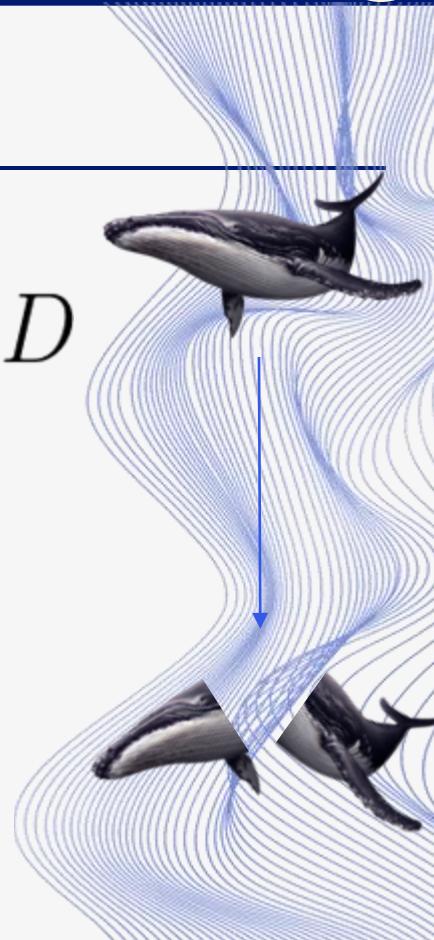


Weyl breaking

$$g^{-1}Dg = d + ie^a P_a + \frac{i}{2}\omega^{ab}J_{ab} + i\nabla\varphi D$$

$$\mathcal{T}^a = de^a - e^b \wedge \omega^a{}_b + e^a \wedge A$$

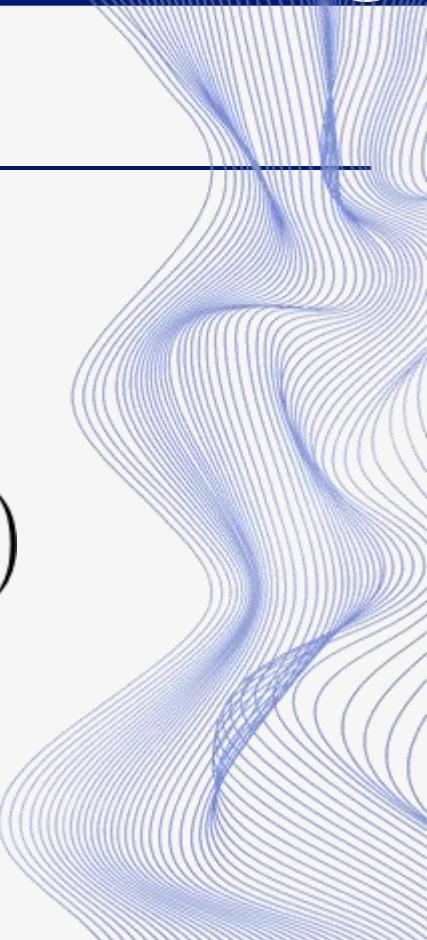
$$\mathcal{R}^{ab} = d\omega^{ab} + \omega^{ac} \wedge \omega_c{}^b \quad \mathcal{F} = dA$$





Results 1: Mass

$$R = \det(e) (\bar{R} + 6\nabla_\mu A^\mu - 6A_\mu A^\mu)$$





2: Torsion

Barker, Zell, [2306.14953]

$$T^{(1)\lambda}_{\mu\nu} \equiv \frac{1}{2}T^{\lambda}_{\mu\nu} + \frac{1}{2}T^{\lambda}_{\nu\mu} + \frac{1}{6}g_{\mu\nu}T^{(2)\lambda} - \frac{1}{6}\delta^{\lambda}_{\nu}T^{(2)}_{\mu} + \frac{1}{3}\delta^{\lambda}_{\mu}T^{(2)}_{\nu}$$

$$T^{(2)}_{\mu} \equiv T^{\lambda}_{\lambda\mu}$$

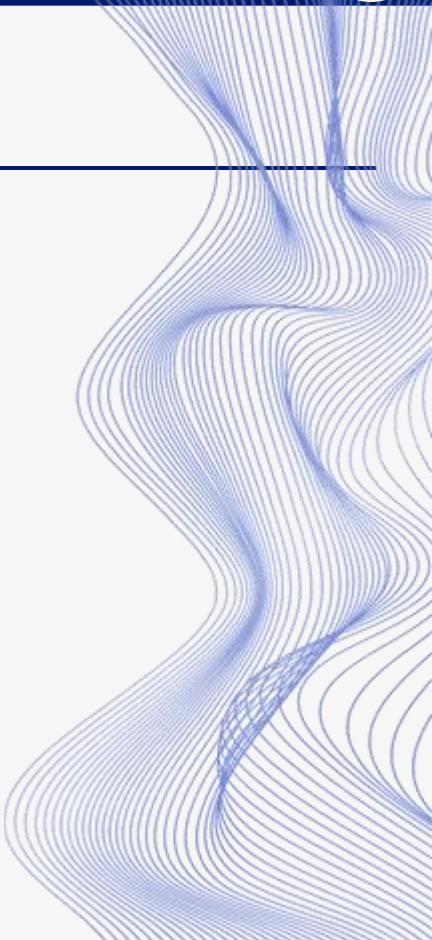
$$T^{(3)}_{\mu} \equiv \frac{1}{6}\varepsilon_{\mu\nu\sigma\lambda}T^{\nu\sigma\lambda}$$





Torsion

$$\mathcal{T}^a = 0 \leftrightarrow T_\mu^{(2)} \sim A_\mu$$





3: Generalized Proca

L. Heisenberg [1402.7026]

- Interacting massive vector theory
- Interactions tuned so EOMs are second order in derivatives
- No Ostrogradsky ghosts





$$\mathcal{L}_2 = G_2(A_\mu, F_{\mu\nu}, \tilde{F}_{\mu\nu})$$

$$\mathcal{L}_3 = G_3(X) \nabla_\mu A^\mu$$

$$\mathcal{L}_4 = G_4(X) \bar{R} + G_{4,X} [(\nabla_\mu A^\mu)^2 - \nabla_\rho A_\sigma \nabla^\sigma A^\rho]$$

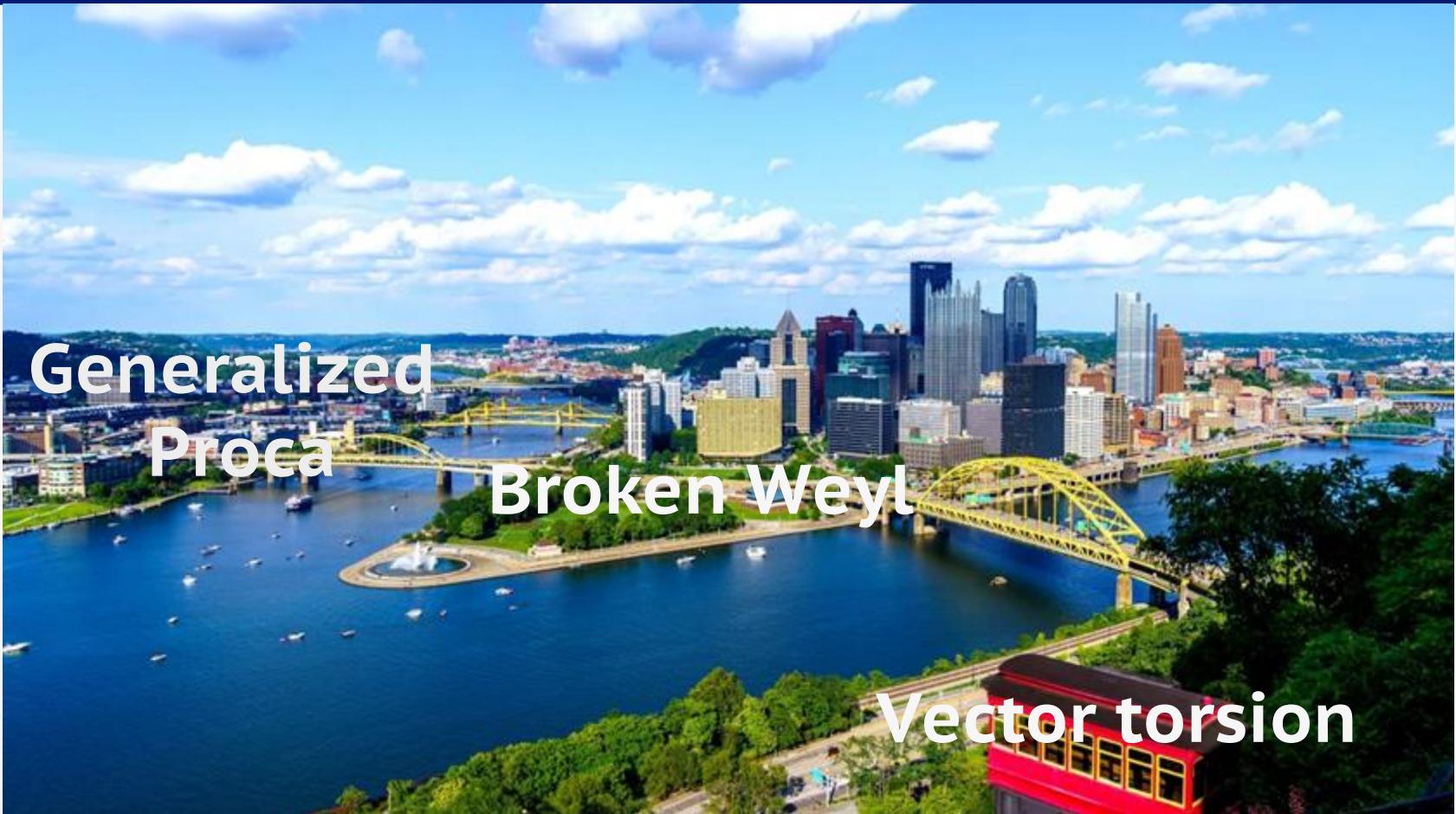
$$\begin{aligned} \mathcal{L}_5 = & G_5(X) \bar{G}_{\mu\nu} \nabla^\mu A^\nu - \frac{1}{6} G_{5,X} [(\nabla \cdot A)^3 \\ & + 2 \nabla_\rho A_\sigma \nabla^\gamma A^\rho \nabla^\sigma A_\gamma - 3 (\nabla \cdot A) \nabla_\rho A_\sigma \nabla^\sigma A^\rho] \end{aligned}$$

$$\mathcal{L}_6 = G_6(X) \mathcal{L}^{\mu\nu\alpha\beta} \nabla_\mu A_\nu \nabla_\alpha A_\beta + \frac{G_{6,X}}{2} \tilde{F}^{\alpha\beta} \tilde{F}^{\mu\nu} \nabla_\alpha A_\mu \nabla_\beta A_\nu$$



Broken Weyl \subset Generalized Proca*

*Ask me about the caveat if interested



Generalized
Proca

Broken Weyl

Vector torsion



Thank you for listening !

XXX

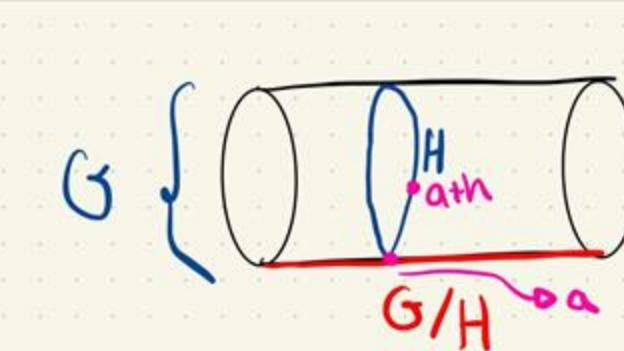


Effective theory

$$\begin{aligned} \mathcal{S} = & \int \epsilon_{abcd} \left(\Lambda e^a \wedge e^b \wedge e^c \wedge e^d + \frac{M_{Pl}^2}{2} R^{ab} \wedge e^c \wedge e^d \right) - \frac{1}{4} F \wedge \star F - m^2 A \wedge \star A \\ & + \mathcal{L}_{RR} + G_2(X) + R_{ab} \wedge F \wedge \star (F \wedge e^a \wedge e^b) + \dots \end{aligned}$$



Relative Lie Algebra cohomology



CE cohomology
 $a \sim a + h$
 $a \in G/H, h \in H$

$$H_{CE}^k(g, h, \mu) = \frac{\ker(d : C^k \rightarrow C^{k+1})}{\text{Im}(d : C^{k-1} \rightarrow C^k)}$$

↓
 # WZ terms $\Leftrightarrow \dim H_{CE}^{d+1}$