IMPROVING PREDICTIONS FOR SQUARK AND GLUINO PRODUCTION AT THE LHC WITH THE HELP OF SOFT GLUON RESUMMATION





AK and L. Motyka, Phys. Rev. Lett. 102, 111802 (2009), Phys. Rev. D 80 (2009) 095004
W. Beenakker, S. Brensing, M. Krämer, AK, E. Laenen and I. Niessen,
JHEP 12 (2009) 041, JHEP 08 (2010) 098, arXiv:1110.2446 [hep-ph]
W. Beenakker, S. Brensing, M. Krämer, AK, E. Laenen, L.Motyka and I. Niessen, IJMP A26 (2011) 2637
W. Beenakker et al., arXiv:1106.5647 [hep-ph]

5th Annual Workshop of the Helmholtz Alliance "Physics at the Terascale", Bonn, 7.12.2011

LHC SEARCHES



PARTONIC SUBPROCESSES

[Kane, Leveille'82][Harrison, Llewellyn Smith'84][Dawson, Eichten, Quigg'85]



Leading Order = $O(\alpha_s^2)$

LO vs NLO



Currently used for determining exclusion limits : NLO SUSY-QCD predictions

NLO AT THRESHOLD

- Large masses of SUSY particles \Rightarrow production close to threshold $\hat{s} \sim 4m^2$ 7
- General structure of the NLO correction in the threshold limit $\beta \rightarrow 0$, $\beta^2 = 1 4m^2/\hat{s}$ 7

$$\Delta \hat{\sigma_i}^{\text{NLO}} \sim \alpha_s \ \hat{\sigma_i}^{\text{LO}} \left\{ A^{(i)} \log^2(\beta^2) + B^{(i)} \log(\beta^2) + C^{(i)} \frac{1}{\beta} + D^{(i)} \right\}$$
Soft/collinear gluon emission
Coulomb gluons

Soft/collinear gluon emission





NLO AT THRESHOLD

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HIGHER ORDERS AT THRESHOLD

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Soft/collinear gluon emission

Coulomb gluons

At higher orders:

$$\sim \alpha_s^n \log^{2n}(\beta)$$

$$\sim \alpha_s^n / \beta^n$$

Both types of corrections can be resummed to all orders

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Here: N(N)LL resummation of soft gluon corrections → LO Coulomb corrections $(\alpha_s/\beta)^n$ resummed for $\tilde{q}\bar{\tilde{q}}$ and $\tilde{g}\tilde{g}$ [Kulesza, Motyka'09] → Subleading Coulomb corrections and bound state effects analysed in NRQCD @NLO for $\tilde{g}\tilde{g}$ and $\tilde{q}\tilde{g}$ [Hagiwara, Yokoya'09] [Kauth, Kühn, Marquard, Steinhauser'10-11] [Kauth, Kress, Kühn'11]

Resummation of soft and Coulomb corrections together [Beneke, Schwinn, Falgari'09], applied to $\tilde{q}\tilde{\tilde{q}}$ at NLL [Beneke, Schwinn, Falgari'10]

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RESUMMATION FOR SQUARK AND GLUINO PRODUCTION

Resummation performed in the space of Mellin moments taken wrt. $4m^2/S$ $\log(\beta^2) \leftrightarrow \log(N) \equiv L$



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Squark and gluino production: $2 \Rightarrow 2$ processes with non-trivial color structures:

$\begin{array}{rcl} \tilde{q}\bar{\tilde{q}} & 3\otimes\bar{3} & = & 1\oplus8\\ \tilde{q}\tilde{q} & 3\otimes3 & = & \bar{3}\oplus6\\ \tilde{q}\tilde{g} & 3\otimes8 & = & 3\oplus\bar{6}\oplus15 \end{array}$				
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	$ ilde q ar {ar q}$	$3\otimes \mathbf{ar{3}}$	=	${f 1}\oplus {f 8}$
$\widetilde{q}\widetilde{g}$ 3 \otimes 8 = 3 \oplus $\overline{6}$ \oplus 15	ilde q ilde q	${f 3}\otimes{f 3}$	=	$ar{f 3}\oplus{f 6}$
	ilde q ilde g	$3\otimes8$	=	$f 3 \oplus ar 6 \oplus f 15$
$\tilde{g}\tilde{g}$ 8 \otimes 8 = 1 \oplus 8 \oplus 8 \oplus 10 \oplus 1 $\bar{10}$ \oplus 27	$ ilde{g} ilde{g}$	$8\otimes8$	=	$1 \oplus 8 \oplus 8 \oplus 10 \oplus 10 \oplus 10 \oplus 27$

 soft wide-angle emission can change the colour structure of the underlying hard scattering; enters at NLL accuracy

NLL RESUMMATION FOR $2 \rightarrow 2$ PROCESSES WITH COLOUR AND MASSIVE FINAL STATES

[Kidonakis, Sterman'96-97][Bonciani, Catani, Mangano, Nason'98]

In appropriately chosen colour basis



- At NLL, need 1-loop anomalous dimensions matrices for all colour structures [AK, Motyka'09] [Beenakker, Brensing, Krämer, AK, Laenen, Niessen'09]
- Resummed expression matched with to the full NLO result ⇒ NLL+NLO

NLL+NLO RESULTS FOR 7 TEV

(for 14 TeV, see e.g. W. Beenakker, S. Brensing, M. Krämer, AK, E. Laenen, L.Motyka and I. Niessen, IJMP A26 (2011) 2637)

TOTAL NLL+NLO PRODUCTION RATES



Most precise predictions for squark and gluino production rates currently available

NLL CORRECTIONS

[W. Beenakker, S. Brensing, M. Krämer, AK, E. Laenen, L.Motyka and I. Niessen'11]



 $K_{\rm NLL} = \frac{\sigma^{\rm resummed, \rm NLL}}{\sigma^{\rm NLO}}$

- Soft-gluon resummation enhances the cross sections
- Highest corrections for the gluino-pair production: 20% correction to the NLO results for m_{al}= 1 TeV
- For the squark-gluino channel, NLL correction reaches 10% at m_{sq}=m_{gl}= 1 TeV

SCALE VARIATION

[W. Beenakker, S. Brensing, M. Krämer, AK, E. Laenen, L.Motyka and I. Niessen'11]



Significant reduction of the scale dependence for NLL+NLO compared to NLO, especially for gluino-pair production

THEORY ERROR

Gluino-pair production

[W. Beenakker, S. Brensing, M. Krämer, AK, E. Laenen, L.Motyka and I. Niessen'11]

7



Significant reduction of the FULL theory error due to reducing the scale variation!

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7

TEVATRON SEARCHES

- NLL+NLO analysis also performed for production of squarks and gluinos at the [Beenakker, Brensing, Krämer, AK, Laenen, Niessen'09]
- CDF mass limits revisited [Beenakker, Brensing, d'Onofrio, Krämer, AK, Laenen, Martinez, Niessen'11]



[ATLAS, PLB 701 (2011) 186]



 Auxiliary information publicly available, including signal acceptance times efficiency

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PUBLIC CODE: NLL-FAST

- All four processes of squark and gluino production at NLL+NLO
- Available at

http://web.physik.rwth-aachen.de/service/wiki/bin/view/Main/ BSMCrossSectionWorkingGroup

\rightarrow LPCC BSM Working group official recommendation

- For a given squark mass and a gluino mass the code returns:
 - ✓ LO and NLO central values (from PROSPINO)
 - ✓ NLL+NLO central value
 - ✓ upper and lower scale variation error on NLL+NLO
 - ✓ upper and lower pdf uncertainty
 - \checkmark upper and lower α_s uncertainty
- To speed up calculation, interpolation of the provided grids for squark and gluino masses in the range of 500-2000 GeV

NNLL+NLO SQUARK-ANTISQUARK PRODUCTION AT 7 TEV

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24

NNLL: How?



Exponentials at NNLL accuracy

$$\Delta_i^{(N)} \Delta_j^{(N)} \Delta_{ij \to kl,I}^{(\text{soft}),\text{N}} = \exp\left[Lg_1(\alpha_{\text{s}}L) + g_2(\alpha_{\text{s}}L) + \alpha_{\text{s}}g_3(\alpha_{\text{s}}L) + \dots\right]$$

- **Three-loop cusp anomalous dimension** [Moch,Vermaseren,Vogt'04]
- Two-loop soft anomalous dimensions [Contopanagos, Laenen, Sterman'96][Catani, de Florian, Grazzini'01][Beneke, Falgari, Schwinn'09][Czakon, Mitov, Sterman'09] [Ferroglia, Neubert, Pecjak, Yang'09]
- Matching coefficients

MATCHING COEFFICIENTS

Soft-Coulomb factorization [Bonciani, Catani, Mangano, Nason'98][Beneke, Falgari, Schwinn'09-10]

$$C_{ij \to kl,I}^{(N)} \stackrel{\text{NNLL}}{=} \left(1 + \frac{\alpha_{\text{s}}}{\pi} \, \mathcal{C}_{ij \to kl,I}^{\text{Coul},(1)}(N, \{m^2\}, \mu^2) \right) \, \left(1 + \frac{\alpha_{\text{s}}}{\pi} \, \mathcal{C}_{ij \to kl,I}^{(1)}(\{m^2\}, \mu^2) \right)$$

Form of the NLO Coulomb corrections known:

$$\sigma_{ij,I}^{\text{Coul},(1)} = -\frac{\alpha_{s}}{\pi} \frac{\pi^{2}}{2\beta} \kappa_{ij,I} \sigma_{ij,I}^{(0)}$$

$$\kappa_{q\bar{q},\mathbf{1}} = -\frac{4}{3}, \qquad \kappa_{q\bar{q},\mathbf{8}} = \frac{1}{6}, \qquad \kappa_{gg,\mathbf{1}} = -\frac{4}{3}, \qquad \kappa_{gg,\mathbf{8}_{\mathbf{A}}} = \frac{1}{6}, \qquad \kappa_{gg,\mathbf{8}_{\mathbf{S}}} = \frac{1}{6}$$

- Hard-matching coefficients $C^{(1)}_{ij,l}$: Analytical results \checkmark
 - obtained from NLO corrections considered in the threshold limit

SQUARK-ANTISQUARK PRODUCTION AT NNLL

[W. Beenakker, S. Brensing, M. Krämer, AK, E. Laenen, L.Motyka and I. Niessen'11]



NNLL +NLO: \rightarrow up to 30% increase of the total cross section wrt NLO for squarks with mass of 1.5 TeV

SQUARK-ANTISQUARK PRODUCTION AT NNLL

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NNLL +NLO: → up to 30% increase of the total cross section wrt NLO for squarks with mass of 1.5 TeV → significant reduction of the scale dependence



- Results for the threshold-resummed total cross section at NLL+NLO available for all four processes of squark and gluino pair-production, as well as stop-pair production
 - **7** Significant reduction of the theory error due to scale variation
- NNLL+NLO: squark-antisquark production
- NLL+NLO results are the most accurate predictions currently available for all channels of squark and gluino production, should be used for determination of mass limits at the LHC



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CMS search for stopped HSCPs, CMS-EXO-11020



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SCALE VARIATION CTND.

Gluino-pair production

[W. Beenakker, S. Brensing, M. Krämer, AK, E. Laenen, L.Motyka and I. Niessen, IJMP A26 (2011) 2637]

7

Squark-gluino production



Theory error due to scale variation below 10% for NLL+NLO down by a factor of 2 (squark-gluino) or a factor of 4 (gluino-pair) for masses > 1 TeV

Corrections to $\mathcal{O}(\alpha_s^2)$ processes

■ NLO SUSY-QCD corrections → $O(\alpha_s^3)$ [Beenakker, Höpker, Spira, Zerwas'96] [Beenakker, Krämer, Plehn, Spira, Zerwas'97]



Sum.

e.g.

- For squark-antisquark and stopantistop production:approximate NNLO contributions $\rightarrow O(\alpha_s^4)$ [Langenfeld, Moch'09] [Langenfeld'10]
- **7** EW corrections $\rightarrow O(\alpha_s^2 \alpha)$ [Hollik, Kollar, Trenkel'07][Hollik, Mirabella'08] [Hollik, Mirabella, Trenkel'08] [Beccaria et al.'08] [Mirabella'09] [Germer, Hollik, Mirabella, Trenkel'10]] [Germer, Hollik, Mirabella'11]

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e.g.

Tree-level EW effects $\mathcal{O}(\alpha_s \alpha)$ and $\mathcal{O}(\alpha^2)$

Sun.

QCD-EW interference and photon-induced contributions, tree-level EW [Bornhauser et al.'07][Alan, Cankocak, Demir'07] [Hollik, Kollar, Trenkel'07][Hollik, Mirabella'08] [Hollik, Mirabella, Trenkel'08] [Bozzi, Fuks, Klasen'05] [Germer, Hollik, Mirabella, Trenkel'10] [Germer, Hollik, Mirabella'11]







RESUMMATION-IMPROVED NLL+NLO TOTAL CROSS SECTION

NLL resummed expression has to be matched with the full NLO result

$$\begin{split} \sigma_{h_{1}h_{2}\rightarrow kl}^{(\mathrm{match})}(\rho,\{m^{2}\},\mu^{2}) &= \sum_{i,j=q,\bar{q},g} \int_{C_{\mathrm{MP}}-i\infty}^{C_{\mathrm{MP}}+i\infty} \frac{dN}{2\pi i} \; \rho^{-N} \; f_{i/h_{1}}^{(N+1)}(\mu^{2}) \; f_{j/h_{2}}^{(N+1)}(\mu^{2}) \\ &\times \left[\left. \hat{\sigma}_{ij\rightarrow kl}^{(\mathrm{res},N)}(\{m^{2}\},\mu^{2}) \; - \; \hat{\sigma}_{ij\rightarrow kl}^{(\mathrm{res},N)}(\{m^{2}\},\mu^{2}) \right|_{_{NLO}} \right] \\ &+ \left. \sigma_{h_{1}h_{2}\rightarrow kl}^{\mathrm{NLO}}(\rho,\{m^{2}\},\mu^{2}), \right. \end{split}$$

- Inverse Mellin transform evaluated using a contour in the complex N space according to 'Minimal Prescription' [Catani, Mangano, Nason Trentadue'96]
- NLO cross sections evaluated with publicly available code PROSPINO [Beenakker, Hoepker, Krämer, Plehn, Spira, Zerwas] [http://people.web.psi.ch/spira/prospino/] [http://www.thphys.uni-heildelberg.de/plehn/prospino/]

NNLL: WHY?

NNLL contributions important for $t\bar{t}$ production [Bonciani, Catani, Mangano, Nason'98]





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7

GLUINO-PAIR PRODUCTION AT THE LHC

Currently used for determining exclusion limits : NLO SUSY-QCD predictions



 $pp \rightarrow \tilde{g}\tilde{g} + X$ LHC @ 7 TeV

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REMINDER: TEVATRON SEARCHES



Essential to know total production cross sections for squarks and gluinos well