

Determination of γ with $B_s \rightarrow D_s K$

5th Annual Workshop of the Helmholtz Alliance
“Physics at the Terascale”

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Introduction

- Unitary CKM matrix

$$V_{\text{CKM}} \equiv V_L^u V_L^{d\dagger} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

- can be described by three mixing angles and one (CP-violating) phase
- Wolfenstein parametrization

$$V = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

Introduction

- Unitarity of the 3x3 CKM matrix implies e.g.

$$\sum_i V_{ij} V_{ik}^* = \delta_{jk}$$

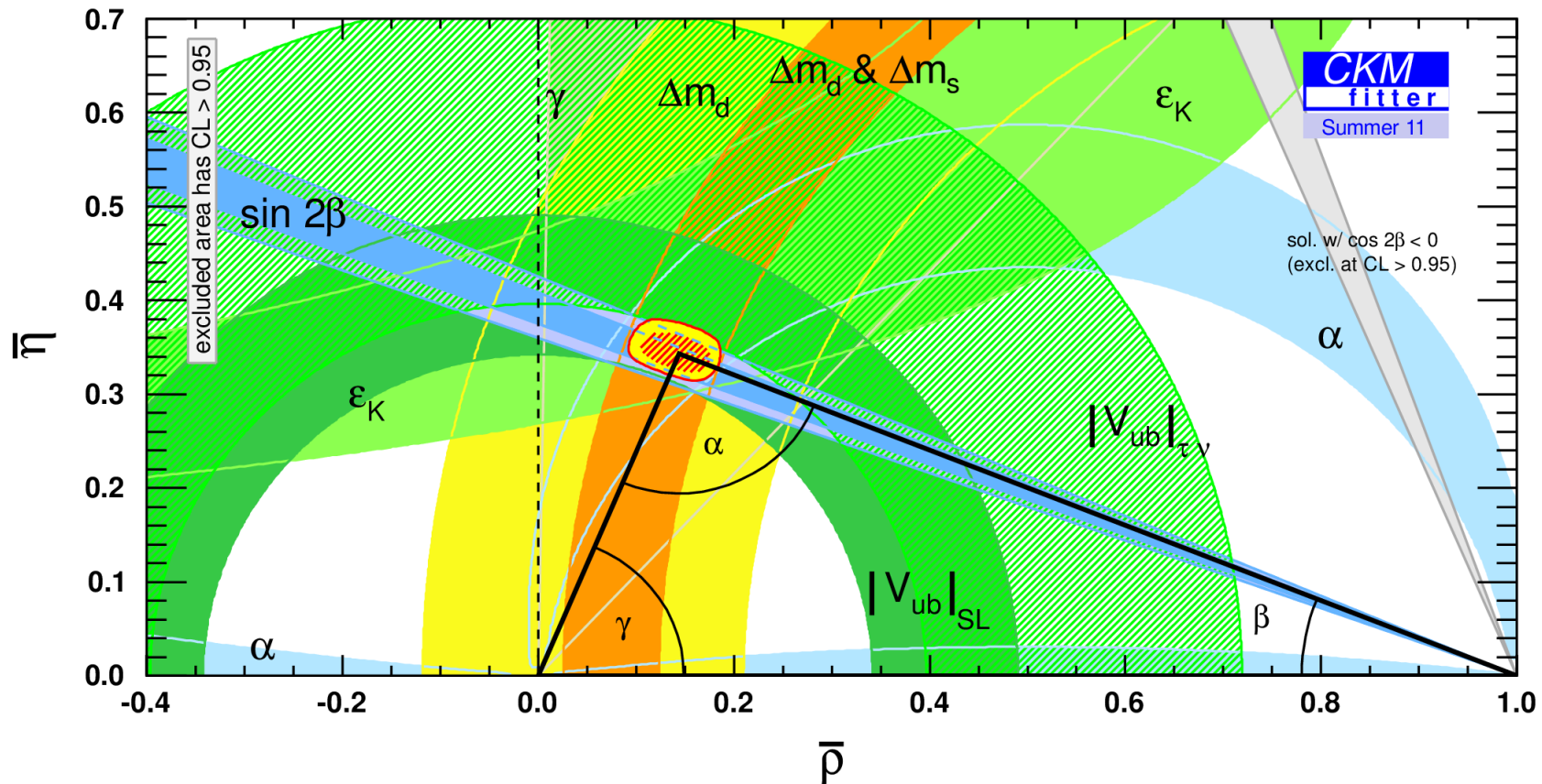
- This translates into several unitarity conditions; most commonly used

$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$

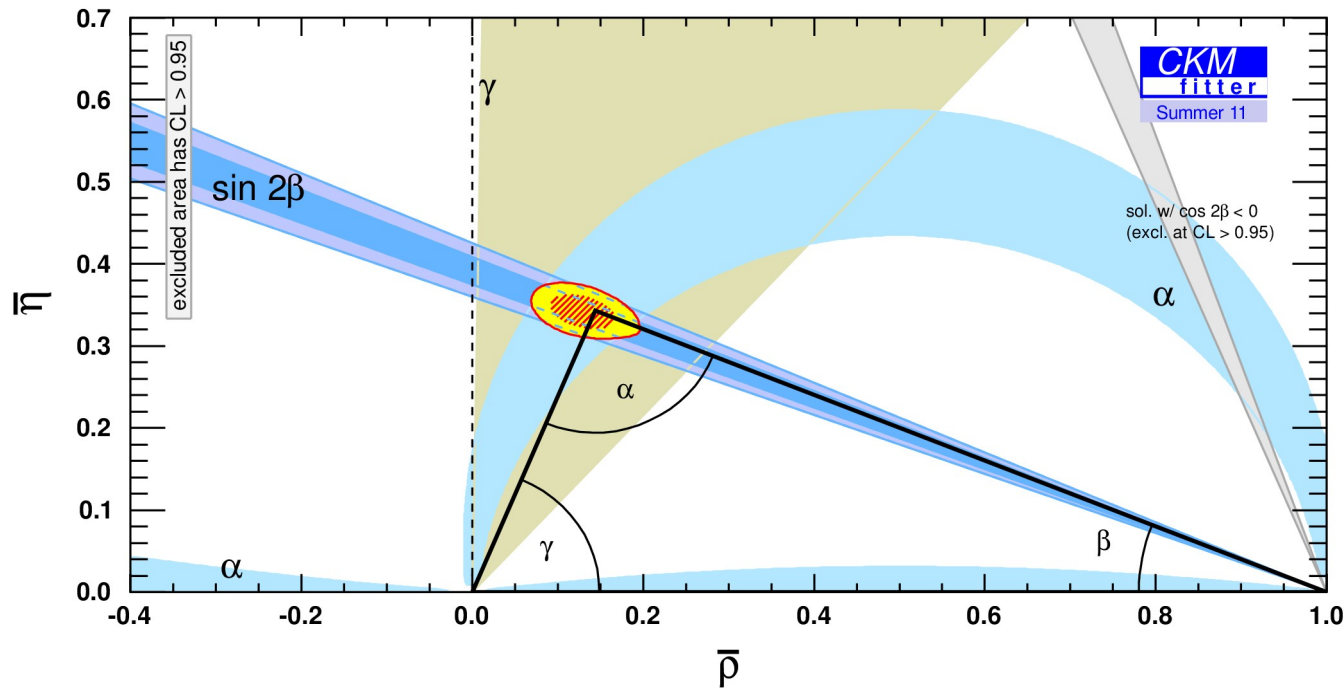
- Normalized to the best-known element

$$V_{cd} V_{cb}^*$$

Introduction



Introduction



$$\gamma = (67.3^{+4.2}_{-3.5})^\circ \text{ (CKM global fit)}$$

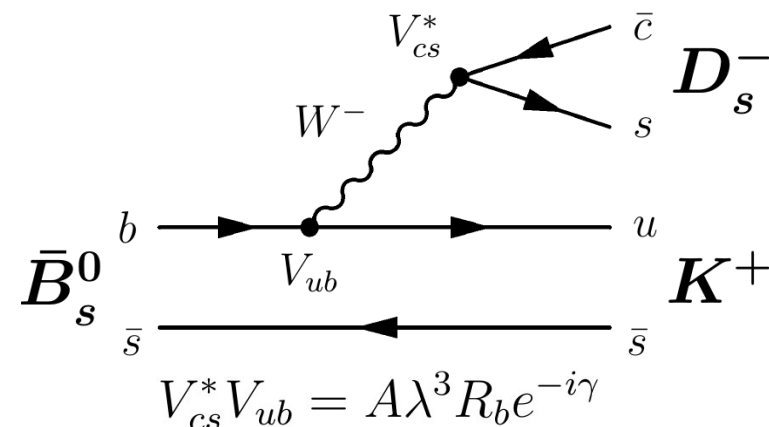
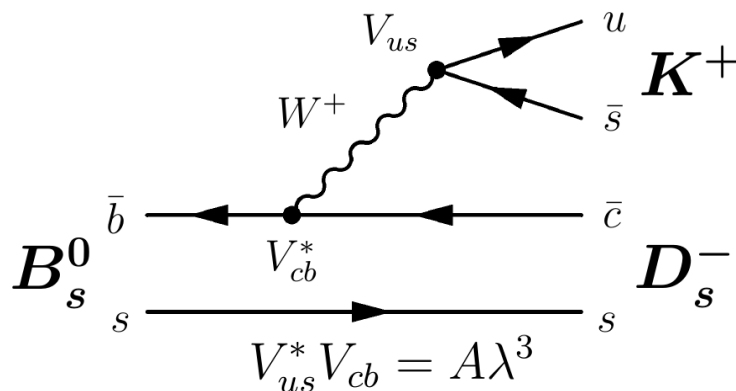
$$\gamma = (68^{+10}_{-11})^\circ \text{ (direct)}$$

Extracting γ from B_s decays

- In order to measure γ one needs decays containing V_{ub}

$$\gamma = \phi_3 = \arg \left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right)$$

- One possibility $B_s \rightarrow D_s K$



Extracting γ from B_s decays

- Why $B_s \rightarrow D_s K$?

- Theoretically clean

$$|B_{H,L}\rangle = p|B_s^0\rangle \mp q|\bar{B}_s^0\rangle$$

$$\lambda_{D_s^- K^+} = \left(\frac{q}{p}\right) \frac{\bar{A}_{D_s^- K^+}}{A_{D_s^- K^+}} = \left(\frac{V_{tb}^* V_{ts}}{V_{tb} V_{ts}^*}\right) \left(\frac{V_{ub} V_{cs}^*}{V_{cb}^* V_{us}}\right) \left|\frac{A_2}{A_1}\right| e^{i\Delta_{T1/T2}} = |\lambda_{D_s^- K^+}| e^{i(\Delta_{T1/T2} - (\gamma + \phi_s))}$$

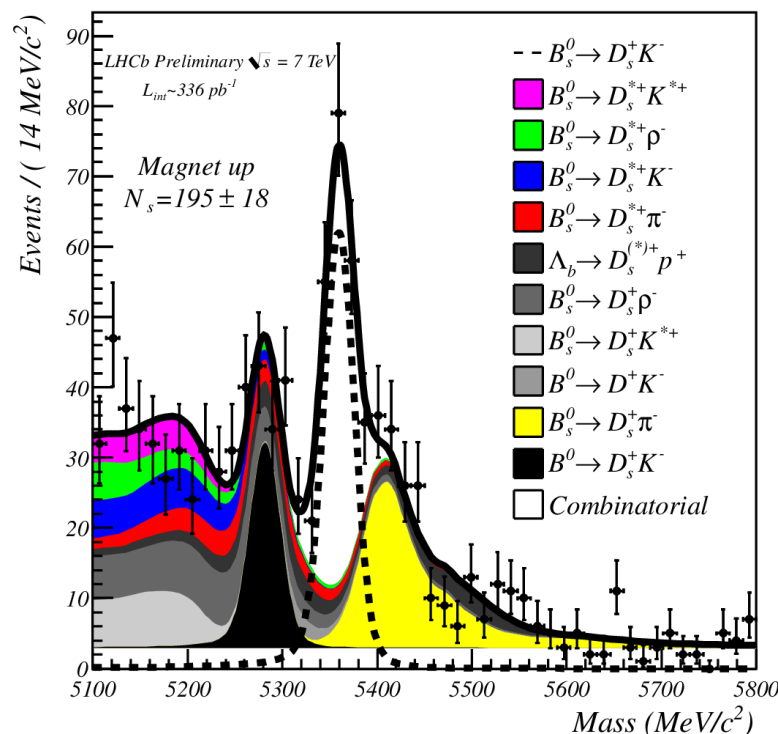
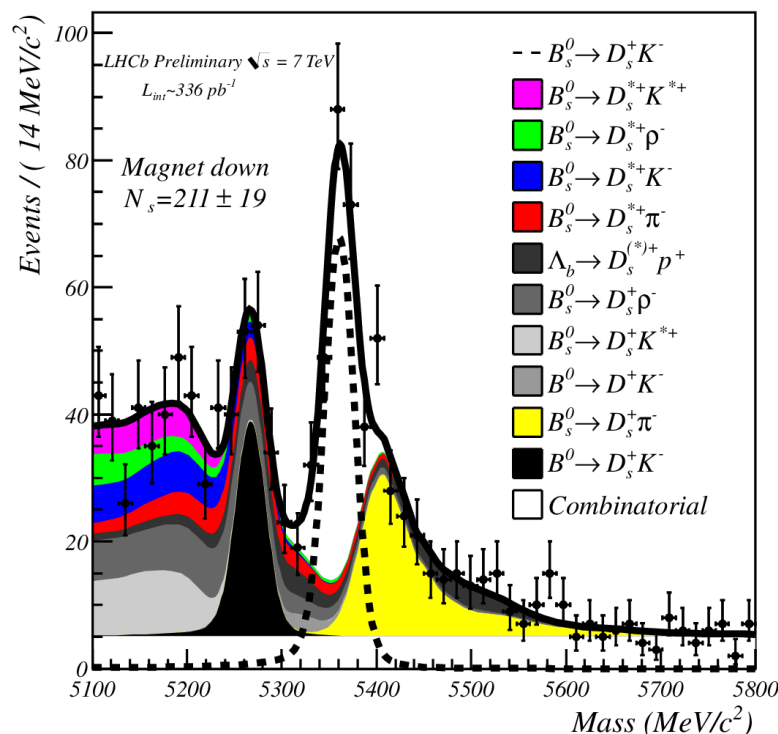
$$\bar{\lambda}_{D_s^+ K^-} = \left(\frac{p}{q}\right) \frac{A_{D_s^+ K^-}}{\bar{A}_{D_s^+ K^-}} = \left(\frac{V_{tb} V_{ts}^*}{V_{tb}^* V_{ts}}\right) \left(\frac{V_{ub}^* V_{cs}}{V_{cb} V_{us}^*}\right) \left|\frac{A_2}{A_1}\right| e^{i\Delta_{T1/T2}} = |\lambda_{D_s^- K^+}| e^{i(\Delta_{T1/T2} + (\gamma + \phi_s))}$$

$$\longrightarrow \gamma + \phi_s = \frac{1}{2} [\arg(\bar{\lambda}_{\bar{f}}) - \arg(\lambda_f)]$$

- Tree-level diagrams
- Very important SM benchmark measurement (LHCb exclusive)

On the way to the first direct measurement of γ in $B_s \rightarrow D_s K$

- First observation of $B_s \rightarrow D_s K$ in 2008 (CDF)
- Establish the signal at LHCb
- Measure the branching ratio of $B_s \rightarrow D_s K$



Branching Ratio measurement of $B_s \rightarrow D_s K$

- Get yields of the different floating components from the mass-fit

Parameter	Fit value	
	Magn. Down	Magn. Up
Num. $B^0 \rightarrow D_s^- K^+$	105 ± 18	91 ± 17
Num. $B_s^0 \rightarrow D_s^- \pi^+$ and $B^0 \rightarrow D^- \pi^+$	161 ± 22	158 ± 21
Num. $B_s^0 \rightarrow D_s^\mp K^\pm$	211 ± 19	195 ± 18
$B_s^0 \rightarrow D_s^\mp K^\pm$ mass mean (MeV/c ²)	5360.8 ± 1.8	5359.7 ± 1.8

336 pb⁻¹

Branching Ratio measurement of $B_s \rightarrow D_s K$

- Calculate the Branching Ratio

$$\frac{\mathcal{B}(B_s^0 \rightarrow D_s^\mp K^\pm)}{\mathcal{B}(B_s^0 \rightarrow D_s^- \pi^+)} = \frac{N_{B_s^0 \rightarrow D_s^\mp K^\pm}}{N_{B_s^0 \rightarrow D_s^- \pi^+}} \frac{\epsilon_{B_s^0 \rightarrow D_s^- \pi^+}^{\text{PID}}}{\epsilon_{B_s^0 \rightarrow D_s^\mp K^\pm}^{\text{PID}}} \frac{\epsilon_{B_s^0 \rightarrow D_s^- \pi^+}^{\text{Sel}}}{\epsilon_{B_s^0 \rightarrow D_s^\mp K^\pm}^{\text{Sel}}}$$

$$\frac{\mathcal{B}(B_s^0 \rightarrow D_s^\mp K^\pm)}{\mathcal{B}(B_s^0 \rightarrow D_s^- \pi^+)} = 0.0647 \pm 0.0044 \text{ (stat.) } {}^{+0.0039}_{-0.0043} \text{ (syst.)}$$

World's most precise

CDF result: $0.097 \pm 0.018(\text{stat}) \pm 0.009(\text{sys})$

Branching Ratio measurement of $B_s \rightarrow D_s K$

- Together with the a former LHCb measurement of f_s/f_d and the relative yields of several B/B_s modes one can calculate $B_s \rightarrow D_s \pi$

$$\mathcal{B}(B_s^0 \rightarrow D_s^- \pi^+) = \mathcal{B}(B^0 \rightarrow D^- \pi^+) \frac{\epsilon_{B^0 \rightarrow D^- \pi^+}}{\epsilon_{B_s^0 \rightarrow D_s^- \pi^+}} \frac{N_{B_s^0 \rightarrow D_s^- \pi^+} \mathcal{B}(D^+ \rightarrow K^- \pi^+ \pi^+)}{\frac{f_s}{f_d} N_{B^0 \rightarrow D^- \pi^+} \mathcal{B}(D_s^+ \rightarrow K^+ K^- \pi^+)}$$

$$\mathcal{B}(B_s^0 \rightarrow D_s^- \pi^+) = (3.04 \pm 0.19 \text{ (stat.)} \pm 0.23 \text{ (syst.)} {}^{+0.18}_{-0.16} (f_s/f_d)) \times 10^{-3}$$

Branching ratio measurement of $B_s \rightarrow D_s K$

- Finally one can use the result from $B_s \rightarrow D_s \pi$ to calculate the absolute Branching Ratio for $B_s \rightarrow D_s K$

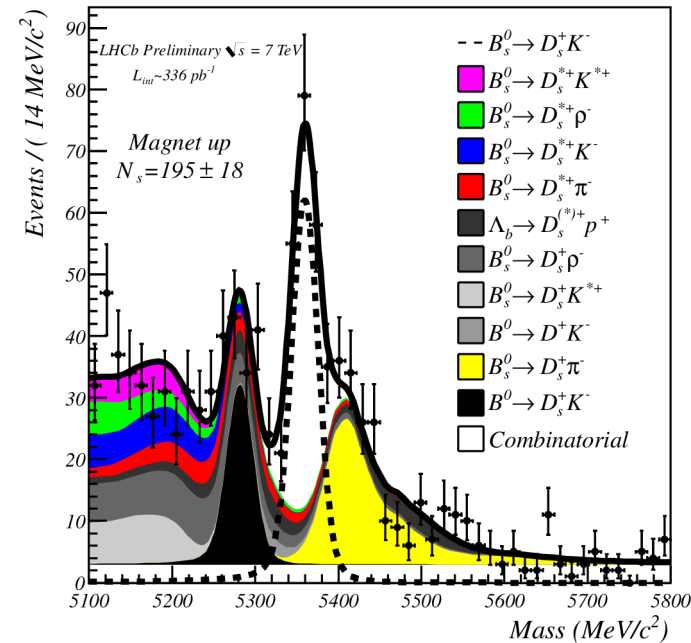
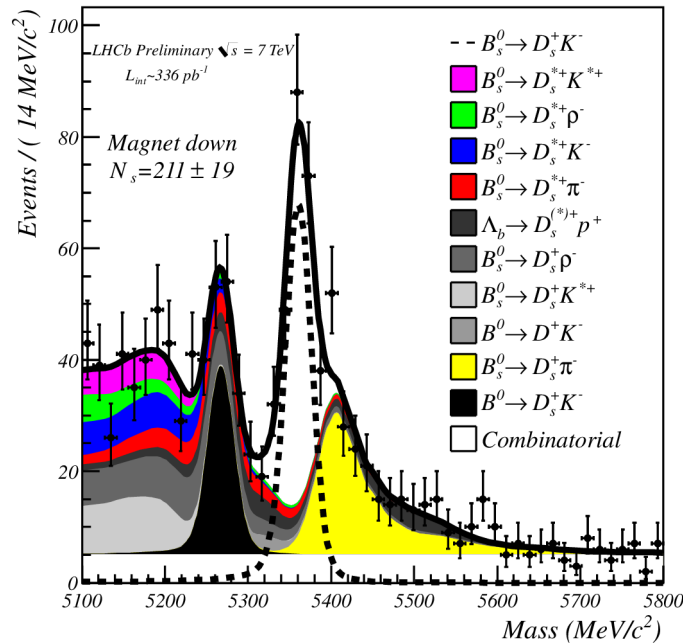
$$\mathcal{B}(B_s^0 \rightarrow D_s^\mp K^\pm) = (1.97 \pm 0.18 \text{ (stat.) } {}^{+0.19}_{-0.20} \text{ (syst.) } {}^{+0.11}_{-0.10} (f_s/f_d)) \times 10^{-4}$$

World's most precise

- Details on the analysis can be found in LHCb-CONF-2011-057
- Paper in preparation

On the way towards γ

- Develop and validate a 2D fitter in mass and time



On the way towards γ

- Possibly many background components are leaking into the signal region
- Study time structure of these components
- Time acceptance and resolution has to be known
- Expected sensitivity $\sigma(\gamma+\phi_s)=10-12^\circ$ with $1-2 \text{ fb}^{-1}$ (2007)
- First result winter-conferences 2012(?)

Conclusion & Outlook

- Short introduction (& motivation) to the determination of γ from $B_s \rightarrow D_s K$
 - Theoretically clean
 - Very important SM benchmark measurement
- Observation of $B_s \rightarrow D_s K$ at LHCb
- Most precise measurement of $B_s \rightarrow D_s K / B_s \rightarrow D_s \pi$

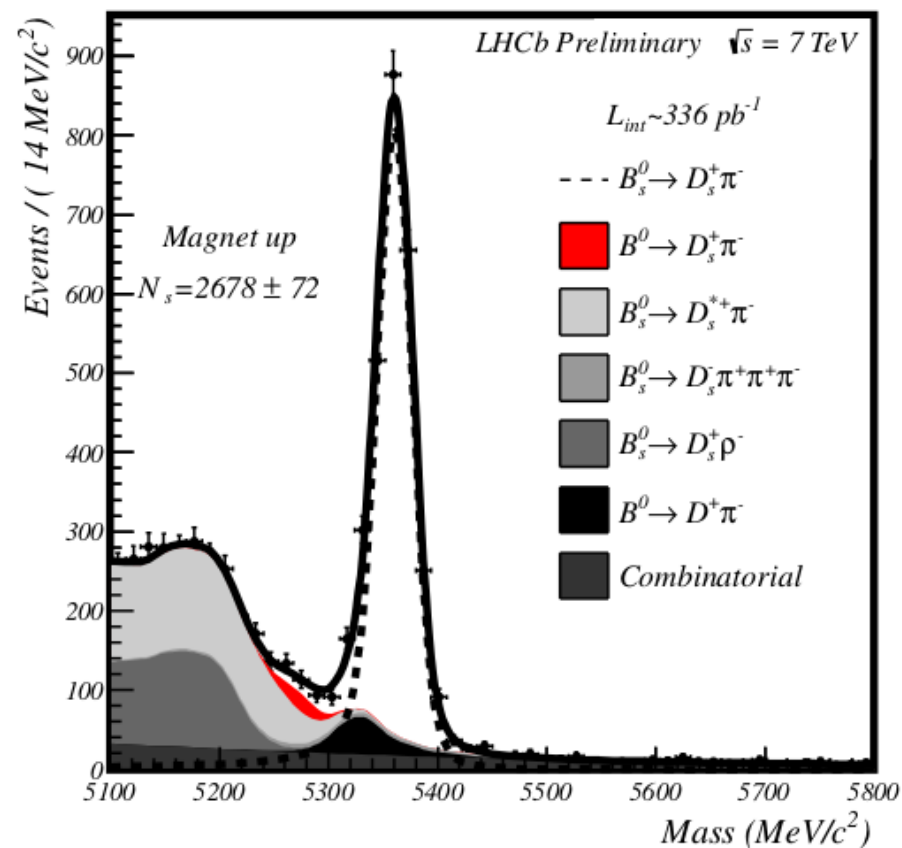
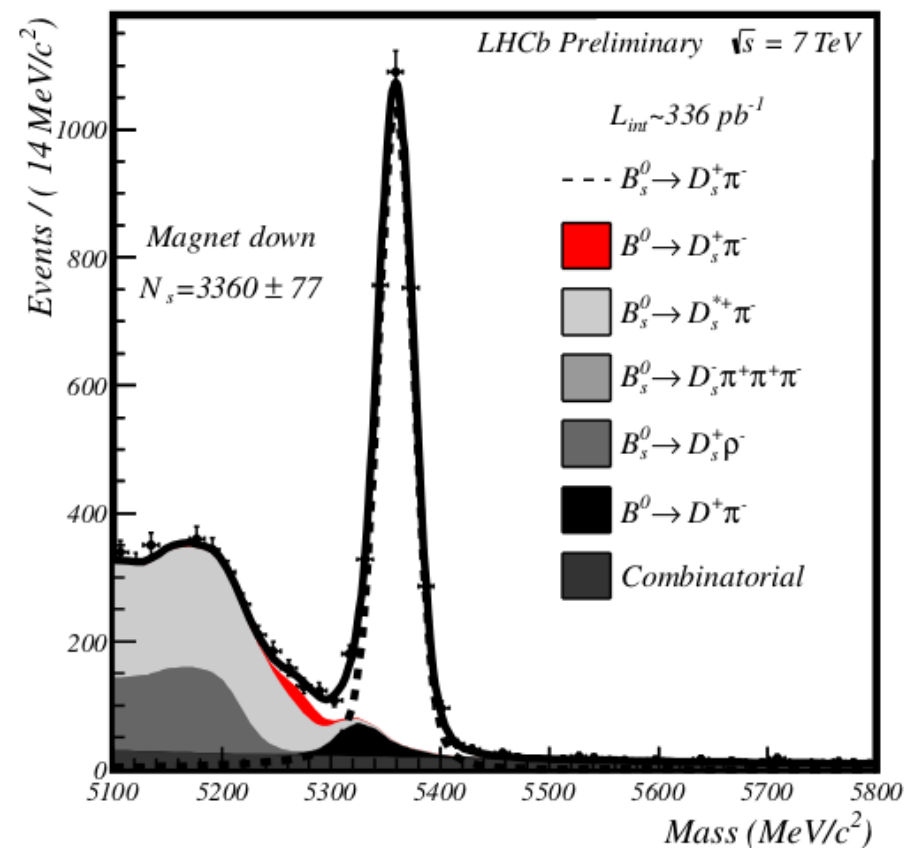
- Next steps
 - Study background in more detail
 - Develop 2D fitter in mass and time
 - Time acceptance and resolution
 - Aim for winter-conferences (?)

Backup Slides

Backup

	$B_s^0 \rightarrow D_s^\mp K^\pm$		$B_s^0 \rightarrow D_s^- \pi^+$		$\epsilon_{B_s^0 \rightarrow D_s^\mp K^\pm} / \epsilon_{B_s^0 \rightarrow D_s^- \pi^+}$	
	$\epsilon_{\text{cum}} (\%)$	$\epsilon_{\text{rel}}(\%)$	$\epsilon_{\text{cum}} (\%)$	$\epsilon_{\text{rel}}(\%)$	$\epsilon_{\text{cum}} (\%)$	$\epsilon_{\text{rel}}(\%)$
Generator		16.56 ± 0.04		16.13 ± 0.15	1.03 ± 0.01	1.027 ± 0.01
Recon.+Strip.	9.06 ± 0.04	9.06 ± 0.04	9.02 ± 0.02	9.02 ± 0.02	1.00 ± 0.01	1.00 ± 0.01
BDTG>0.1	8.15 ± 0.04	90.0 ± 0.1	8.14 ± 0.02	90.3 ± 0.1	1.00 ± 0.01	1.00 ± 0.01
L0	3.96 ± 0.03	48.6 ± 0.3	3.89 ± 0.02	47.8 ± 0.1	1.02 ± 0.01	1.02 ± 0.01
Hlt	2.57 ± 0.02	64.8 ± 0.4	2.50 ± 0.01	64.2 ± 0.2	1.03 ± 0.01	1.01 ± 0.01
$p_{\text{bach}} < 100 \text{ GeV}$	2.21 ± 0.02	86.1 ± 0.3	2.15 ± 0.01	86.0 ± 0.2	1.03 ± 0.01	1.00 ± 0.01
Total					1.058 ± 0.014	

Backup



Backup

Background type	Magn. Down	Magn. Up
$B_s^0 \rightarrow D_s^{*-} \pi^+$	70 ± 23	63 ± 21
$B_s^0 \rightarrow D_s^{*-} K^+$	80 ± 27	72 ± 34
$B_s^0 \rightarrow D_s^- \rho^+$	150 ± 50	135 ± 45
$B_s^0 \rightarrow D_s^- K^{*+}$	150 ± 50	135 ± 45
$B_s^0 \rightarrow D_s^{*-} \rho^+$	50 ± 17	45 ± 15
$B_s^0 \rightarrow D_s^{*-} K^{*+}$	50 ± 17	45 ± 15
$\Lambda_b \rightarrow D_s^- p + \Lambda_b \rightarrow D_s^{*-} p$	80 ± 27	72 ± 34