



# Studies for a top quark mass measurement in the dilepton channel using the $m_{T2}$ variable

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# Method description

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- Select an observable which depends on the top mass
- Create a calibration curve from Monte-Carlo simulation samples with different top mass input
- Measure the chosen observable in data and obtain the top mass from the calibration curve
- Consider systematic uncertainties

# Standard dilepton events selection

## Standard dilepton events selection highlights

- Exactly two oppositely-charged leptons
- Electrons must satisfy  $p_T > 25$  GeV, while muons must satisfy  $p_T > 20$  GeV
- All leptons must satisfy  $|\eta| < 2.5$
- At least two jets with  $p_T > 25$  GeV and  $|\eta| < 2.5$
- For ee and  $\mu\mu$  channels:  $E_T^{miss} > 60$  GeV and  $|m_{\ell\ell} - m_Z| > 10$  GeV
- For  $e\mu$  channel:  $H_T > 130$  GeV

# The $m_{T2}$ variable

## $m_{T2}$ (stransverse mass)

- Formal definition<sup>1</sup>:

$$m_{T2} = \min_{\vec{p}_T^{(1)}, \vec{p}_T^{(2)}} \left[ \max \left[ m_T(m_i, \vec{p}_T^{(1)}), m_T(m_i, \vec{p}_T^{(2)}) \right] \right]$$

- with:

$$\vec{p}_T^{(1)} + \vec{p}_T^{(2)} = \vec{p}_T^{\text{miss}}$$

$$m_T(m_i, \vec{p}_T) = \sqrt{m_v^2 + m_i^2 + 2(E_T^v E_T^i - \vec{p}_T^v \cdot \vec{p}_T)}$$

- where the  $i$  subscript stands for invisible particles and the  $v$  subscript stands for visible particles.

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<sup>1</sup>C. Lester, D. Summers, Phys. Lett. B 463:99-103, 1999

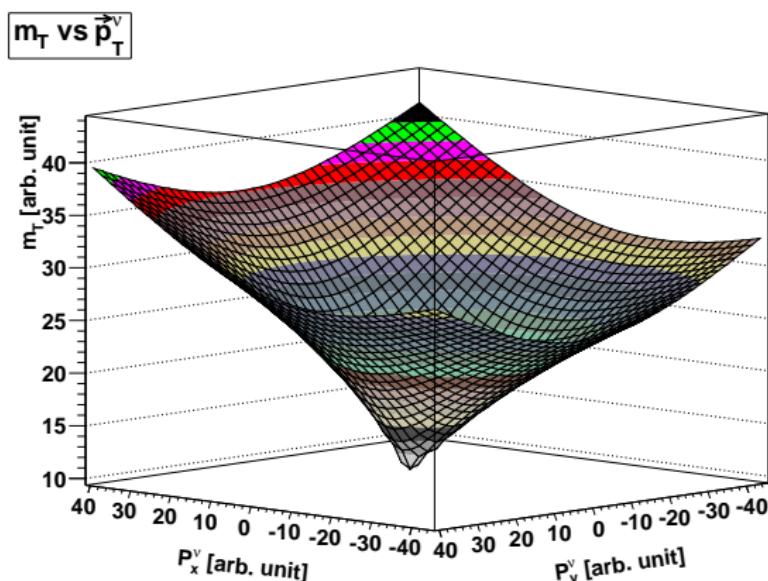
## $m_{T2}$ (stransverse mass)

- Used in events with two missing particles
- Represents a lower bound for the parent particle mass
- For top dilepton:

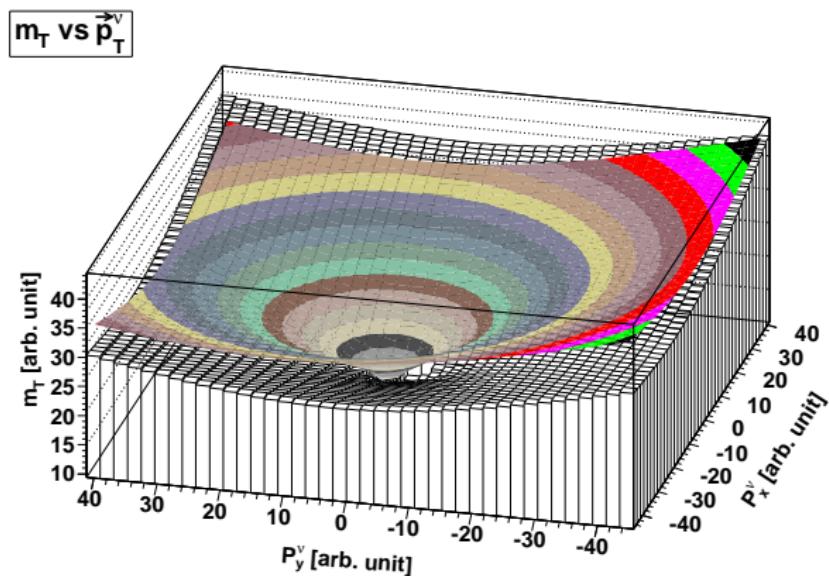
$$m_T(m_i, \vec{p}_T^{(i)}) \approx m_T(0, \vec{p}_T^{\nu_i}) = \sqrt{m_{b\ell}^2 + 2(E_T^{b\ell} \|\vec{p}_T^{\nu_i}\| - \vec{p}_T^{b\ell} \cdot \vec{p}_T^{\nu_i})}$$

└ The  $m_{T2}$  variable

$m_T$  dependence on  $\vec{p}_T^\nu$

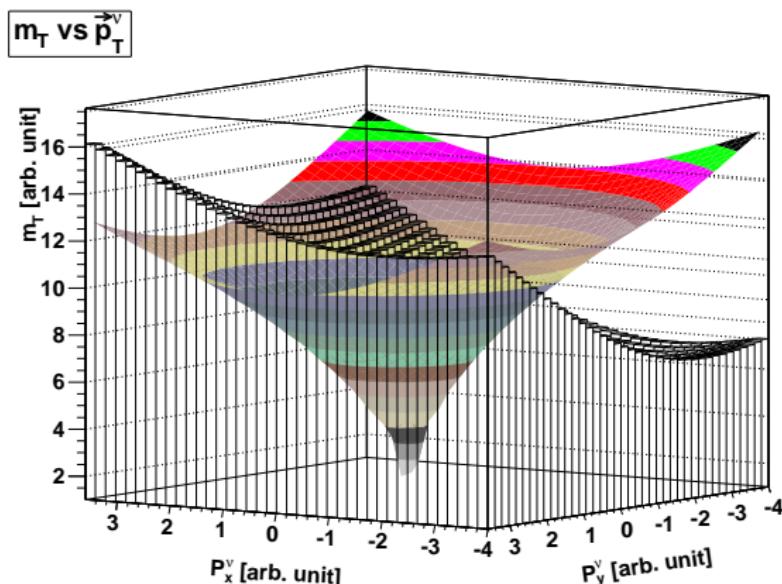


$$m_T(0, \vec{p}_T^\nu) = \sqrt{m_{bl}^2 + 2(E_T^{bl} \|\vec{p}_T^\nu\| - \vec{p}_T^{bl} \cdot \vec{p}_T^\nu)}$$

└ The  $m_{T2}$  variable $m_{T2}$  (no  $m_T$  intersection)

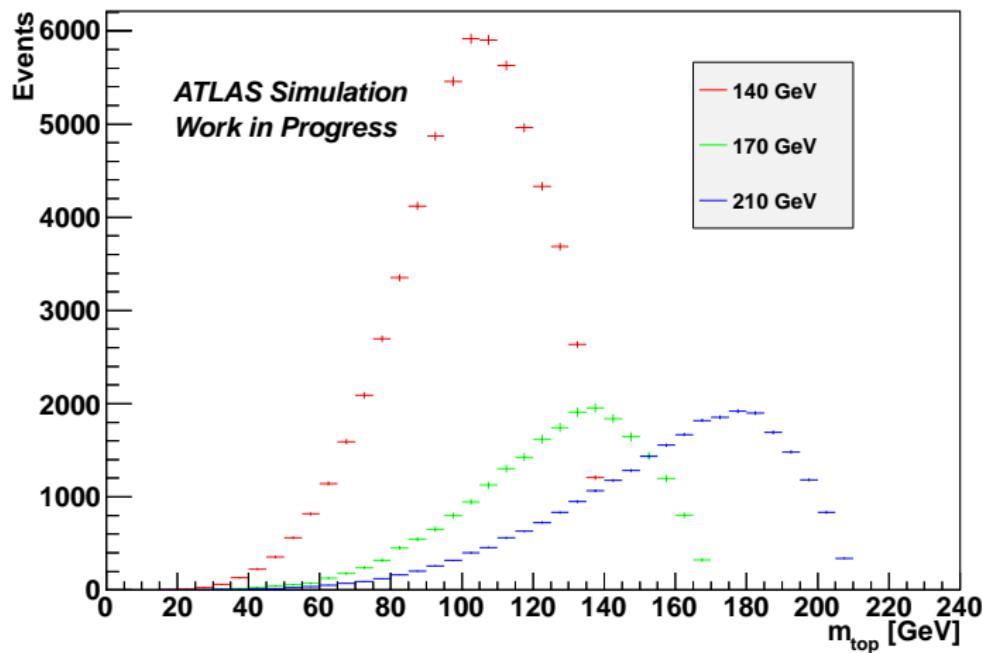
$$m_{T2} = \min_{\vec{p}_T^{\nu 1}, \vec{p}_T^{\nu 2}} \left[ \max \left[ m_T(0, \vec{p}_T^{\nu 1}), m_T(0, \vec{p}_T^{\nu 2}) \right] \right]$$

## $m_{T2}$ (with $m_T$ intersection)

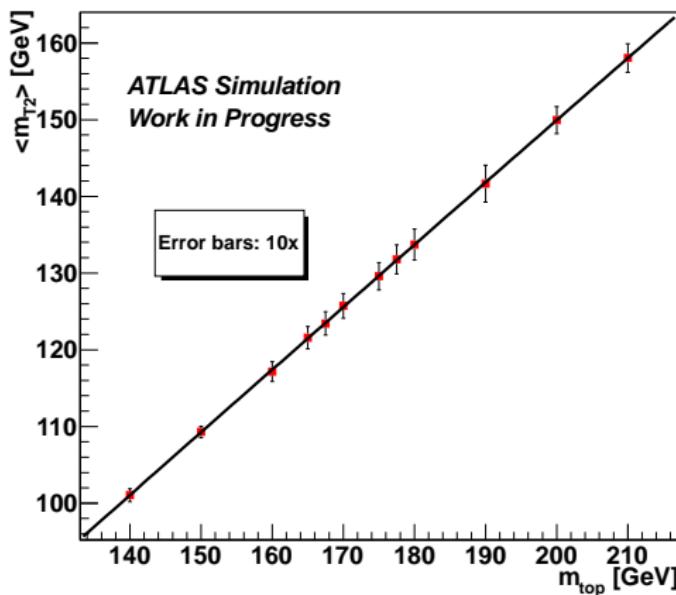


$$m_{T2} = \min_{\vec{p}_T^{\nu 1}, \vec{p}_T^{\nu 2}} \left[ \max \left[ m_T(0, \vec{p}_T^{\nu 1}), m_T(0, \vec{p}_T^{\nu 2}) \right] \right]$$

# $m_{T2}$ distributions for different input masses (Truth)



# Calibration curve<sup>2</sup> (Truth)



<sup>2</sup>Second order polynomial fit

# Systematic uncertainty

# Systematic uncertainties

- Based on ATLAS top reconstruction group's final recommendations for release 16
- Main contributions to systematic uncertainties (More than 0.5 GeV):
  - Jet energy scale, b-jet energy scale, and pileup
  - Initial and final state radiation
  - Fake leptons estimation
  - MC generator (MC@NLO vs POWHEG) + HERWIG

# Optimization cuts

- $m_{T2}$ :

- The leading lepton must satisfy  $p_T > 40$  GeV
- The sub-leading lepton must satisfy  $p_T > 25$  GeV
- The event must satisfy  $U_T < 60$  GeV
- The event must satisfy  $m_{T2} < 220$  GeV

where:

$$U_T = \|\vec{p}_T^{(lep1)} + \vec{p}_T^{(lep2)} + \vec{p}_T^{(jet1)} + \vec{p}_T^{(jet2)} + \vec{p}_T^{miss}\|$$

## Additional measurement

- Problem: The optimization cuts have little effect in the jet energy scale systematic uncertainty
  - Solution: Make an additional measurement with  $\langle p_T^{(leptons)} \rangle$ :

$$p_T^{(leptons)} = \|\vec{p}_T^{(lep1)} + \vec{p}_T^{(lep2)}\|$$

## Measurement combination

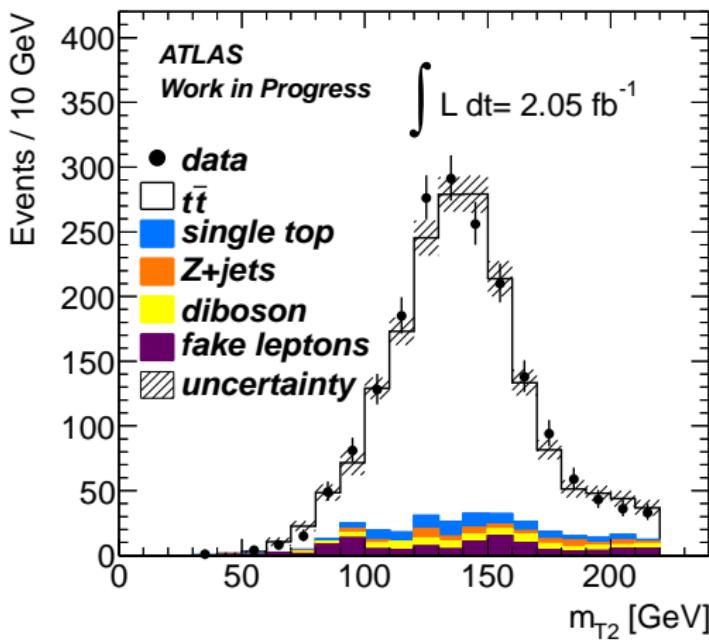
The measurements are merged using the least squares method:

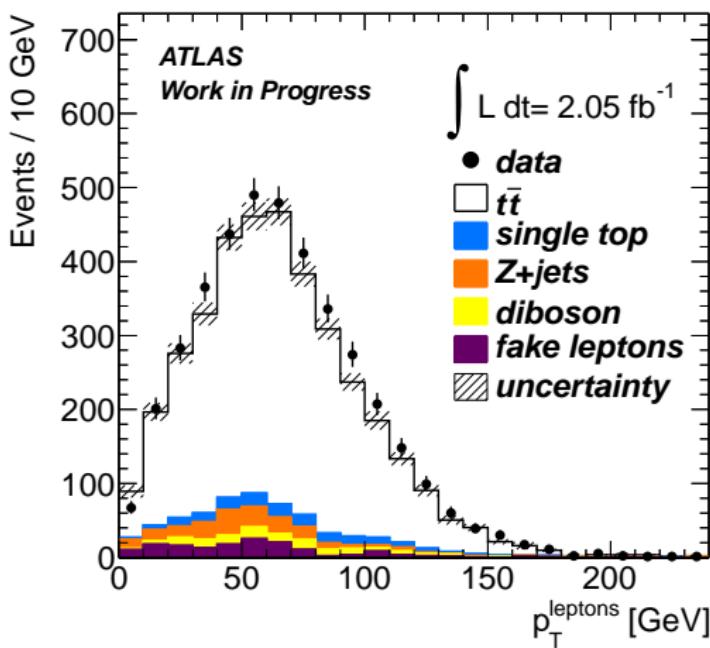
$$m_{comb} = w m_1 + (1 - w) m_2$$

$$w = \frac{\sigma_2^2 - \rho \sigma_1 \sigma_2}{\sigma_1^2 + \sigma_2^2 - 2\rho \sigma_1 \sigma_2}$$

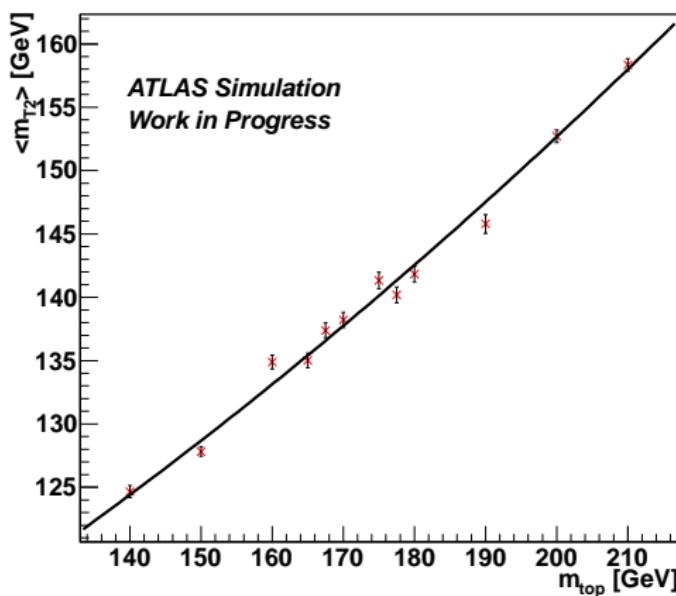
$$\sigma_{comb} = \sqrt{\frac{(1 - \rho) \sigma_1^2 \sigma_2^2}{\sigma_1^2 + \sigma_2^2 - 2\rho \sigma_1 \sigma_2}}$$

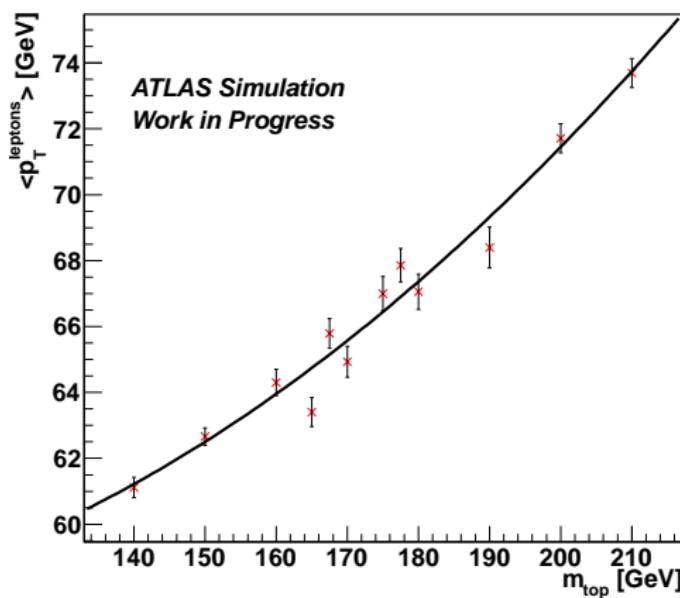
# Preliminary results

Agreement between MC and data  $2 \text{ fb}^{-1}$  ( $m_{T2}$ )

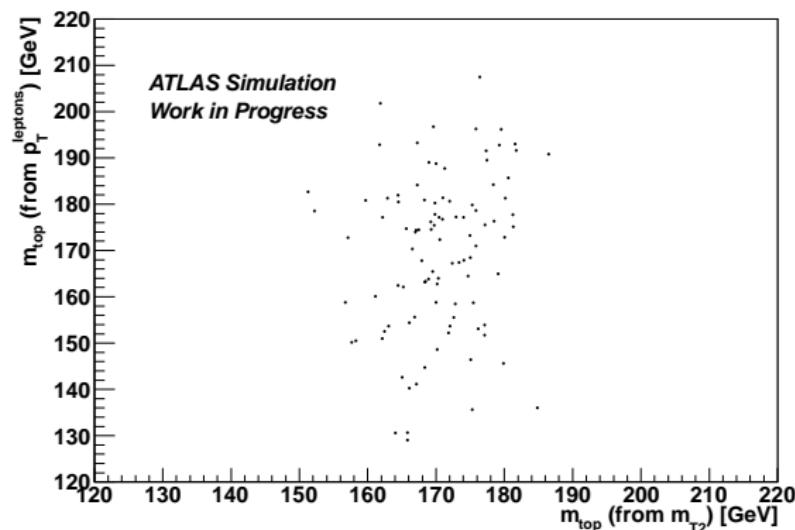
Agreement between MC and data  $2 \text{ fb}^{-1}$  ( $p_T^{(\text{leptons})}$ )

# $m_{T2}$ calibration curve (Reco)



$p_T^{(\text{leptons})}$  calibration curve (Reco)

# Correlation between the two measurements



Correlation coefficient: 0.17

# Results on $2.05 \text{ fb}^{-1}$ data<sup>3</sup>

<i>All measurements in GeV</i>	$m_{T2}$	$p_T^{(\text{leptons})}$	Combined
Top mass	172.7	174.1	172.9
Stat. uncertainty	$\pm 1.4$	$\pm 3.0$	$\pm 1.2$
Total systematic uncertainty	$+4.1$ $-4.6$	$+3.4$ $-4.3$	$+3.6$ $-4.2$
JES <sup>Up</sup> Down	$+3.6$ $-3.6$	$-2.2$ $+2.2$	$\pm 2.8$
ISR and FSR	$+1.4$ $-2.5$	$+1.5$ $-3.1$	$+1.1$ $-2.6$
Fake leptons estimation	$+0.7$ $-0.1$	$+1.0$ $-0.0$	$+0.7$ $-0.0$
MC Generator	$\pm 1.2$	$\pm 0.4$	$\pm 1.1$

# Outlook

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- Perform optimization separately in each dilepton mode.
- Improve the calibration curve using mass variation samples with higher statistics.
- Use b-tagging
- Use stronger cuts.

# Thank you!

# Backup

## Measurement combination

- The measurements are merged using the least squares method

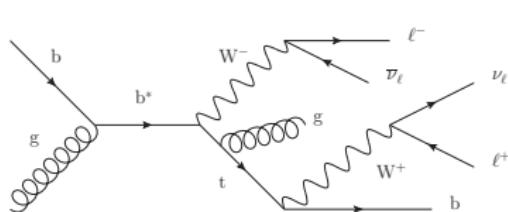
$$\chi^2(m_{comb}) = \sum_{i,j} (m_i - m_{comb})(V^{-1})_{ij}(m_j - m_{comb})$$

- For two measurements:

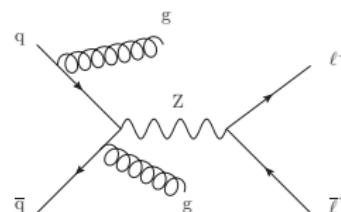
$$V = \begin{pmatrix} \sigma_1^2 & \rho\sigma_1\sigma_2 \\ \rho\sigma_1\sigma_2 & \sigma_2^2 \end{pmatrix}$$

# Main background

- The main background sources are the following:
  - Single top quarks produced in electroweak interactions
  - Z-bosons with additional jets
  - Dibosons (WW, WZ, ZZ)
  - Events with fake leptons



Single top



Z+jets