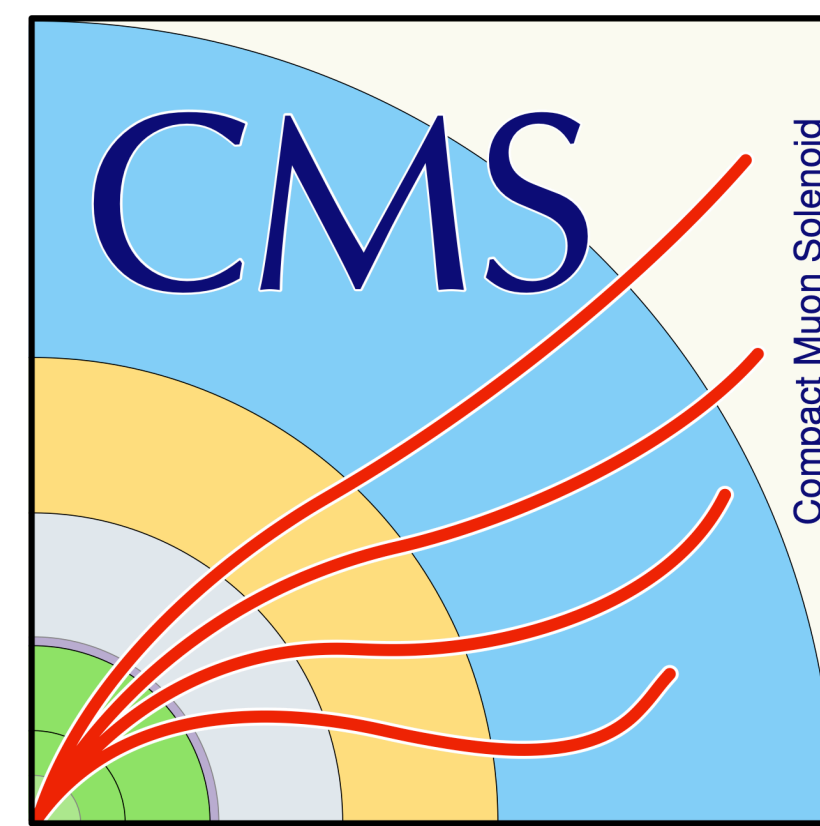




Alexander von
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Non-Relativistic Top Quark Pairs

(Based on 2412.16685, in collaboration with Garzelli, Moch, Steinhauser, Zenaiev)

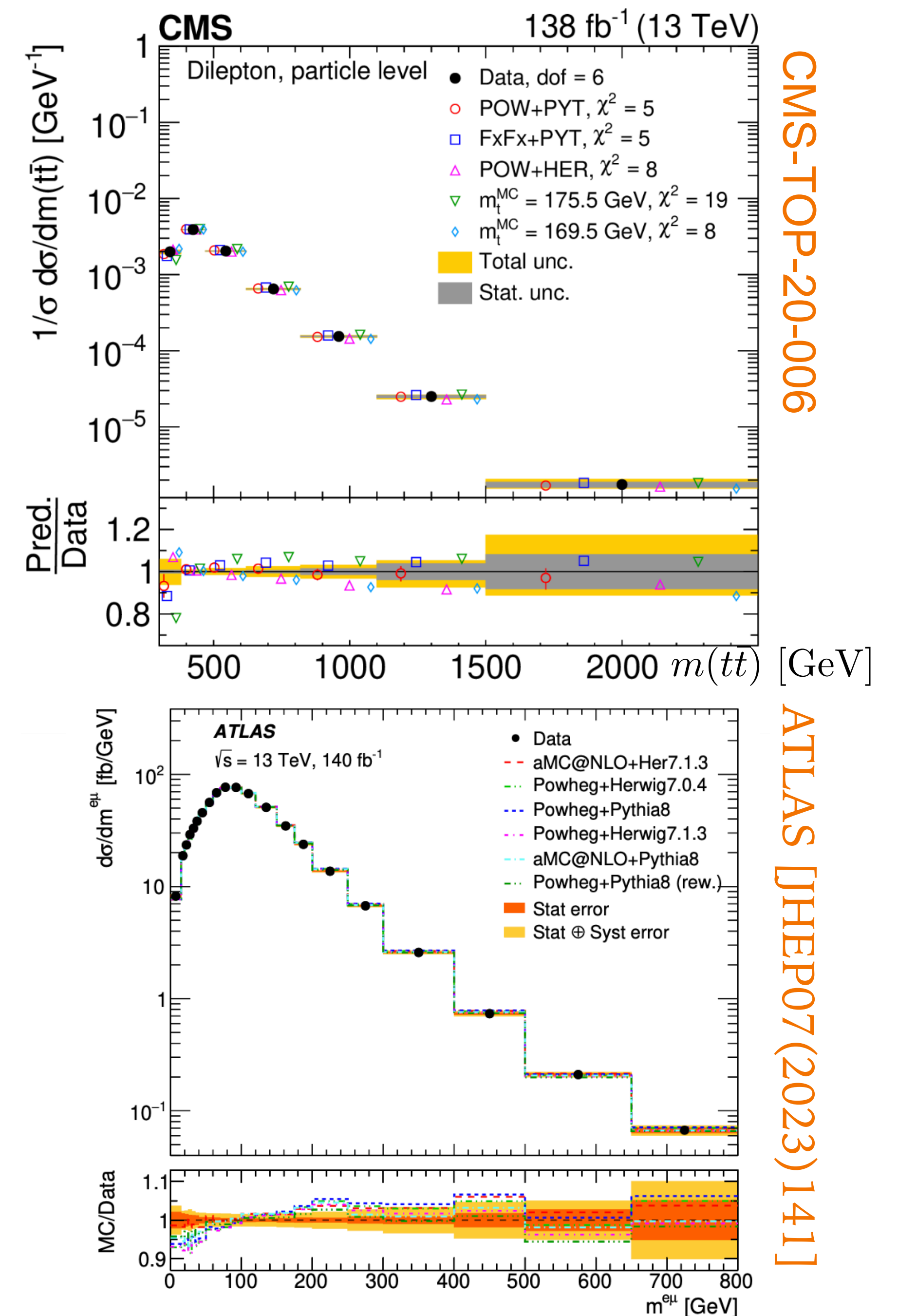
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Universität Hamburg & DESY

Theory-Experimental Top Quark Mass Workshop
DESY
29th January 2025

Introduction

- Significant excess in the invariant mass $M_{t\bar{t}} \simeq 2m_t$ from a recent CMS and ATLAS analysis
- New heavy Beyond Standard Model (BSM) Higgs boson decaying into $t\bar{t}$?
- Enhanced cross section $d\sigma/dM_{t\bar{t}}$ strictly related to bound states effects

Accurate SM theoretical predictions are crucial for reliable BSM searches



Theory Framework

$$d\sigma_{P_1 P_2 \rightarrow X} = \sum_{i,j} \int_0^1 dx_1 dx_2 f_{i,P_1}(x_1, \mu_f^2) f_{j,P_2}(x_2, \mu_f^2) d\hat{\sigma}_{ij} \left(1 + \text{NP Effects} \right)$$

- $d\hat{\sigma}_{ij}$ computable with perturbative QCD
- Factorization scale μ_f to separate the long distance effects from short distance dynamics
- Non-Perturbative inputs coming from Parton distribution functions $f_{i,j}$, quark masses, α_s (fit from experimental measurements, lattice computations...)

Theory Framework: $t\bar{t} + X$ @LHC

- Most of the $t\bar{t}$ pairs produced in the threshold region (non-relativistic effects play a crucial role)
- Invariant mass distribution is the choice at Hadron Colliders
- **QCD** factorization allows a simple expression

$$M_{t\bar{t}} \frac{d\sigma_{P_1 P_2 \rightarrow T}}{dM_{t\bar{t}}}(S, M_{t\bar{t}}^2) = \sum_{i,j} \int_{\rho}^1 d\tau \left[\frac{d\mathcal{L}_{ij}}{d\tau} \right](\tau, \mu_f^2) M_{t\bar{t}} \frac{d\hat{\sigma}_{ij \rightarrow T}}{dM_{t\bar{t}}}(\hat{s}, M_{t\bar{t}}^2, \mu_f^2)$$

Theory Framework: $t\bar{t} + X$ @LHC

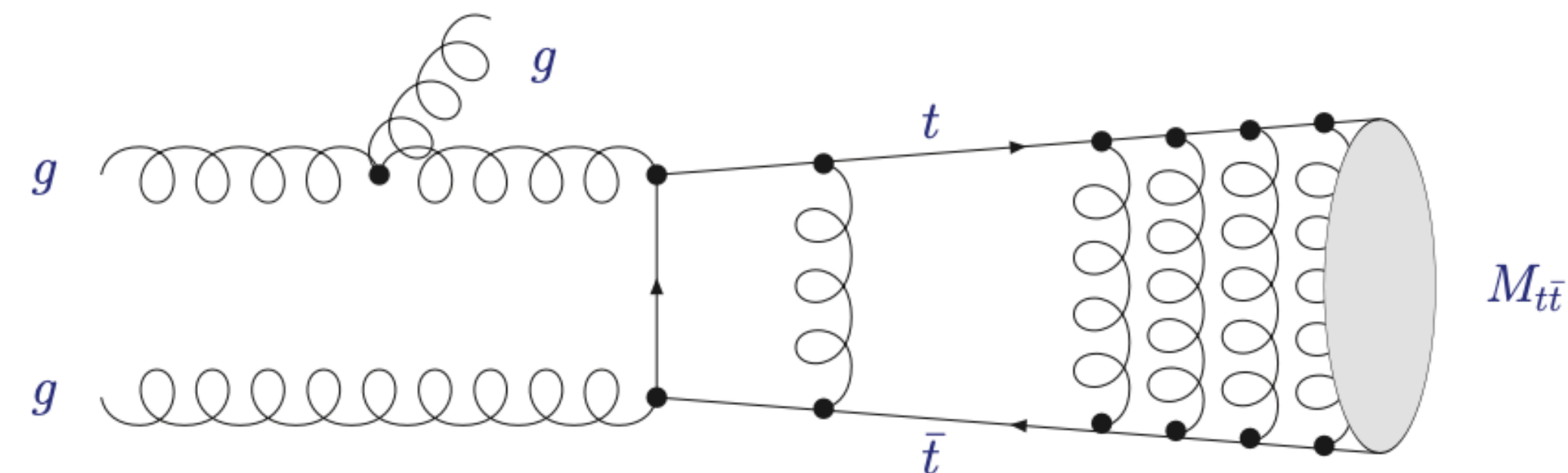
- How to describe bound state effects?
- **Non-Relativistic QCD** is the way

$$\beta_t = \sqrt{1 - 4m_t^2/M_{t\bar{t}}^2} \ll 1$$

- NR **QCD** allows a factorization of $d\hat{\sigma}_{ij}/dM_{t\bar{t}}$

Kiyo, Kuhn, Moch, Steinhauser, Uwer (EPJC 60 (2009) 375-286)

$$M_{t\bar{t}} \frac{d\hat{\sigma}_{ij \rightarrow T}}{dM_{t\bar{t}}}(\hat{s}, M_{t\bar{t}}^2, \mu_f^2) = F_{ij \rightarrow T}(\hat{s}, M_{t\bar{t}}^2, \mu_f^2) \frac{1}{m_t^2} \text{Im} G^{[1,8]}(M_{t\bar{t}} + i\Gamma_t)$$



Theory Framework: $t\bar{t} + X$ @LHC

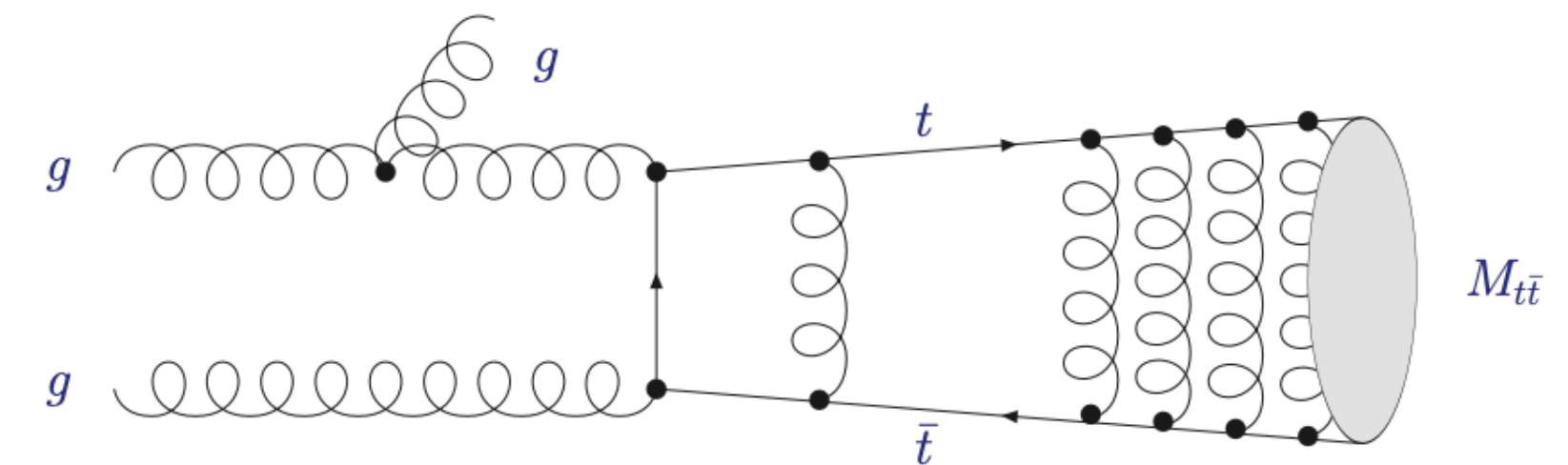
$$M_{t\bar{t}} \frac{d\hat{\sigma}_{ij \rightarrow T}}{dM_{t\bar{t}}}(\hat{s}, M_{t\bar{t}}^2, \mu_f^2) = F_{ij \rightarrow T}(\hat{s}, M_{t\bar{t}}^2, \mu_f^2) \frac{1}{m_t^2} \text{Im} G^{[1,8]}(M_{t\bar{t}} + i\Gamma_t)$$

- Hard function for production of a state

$$T = 2S+1 \quad L_J^{[1,8]} \longrightarrow \begin{array}{c} \text{Singlet (1), Octet (8)} \\ \text{Color State} \end{array}$$

Spin
Orbital angular momentum

- Non-Relativistic Green Function
Responsible for bound state formation



$$\left\{ 2m_t + \left[\frac{(-i\nabla)^2}{m_t} + V_C^{[1,8]}(\vec{r}) \right] - (M + i\Gamma_t) \right\} G^{[1,8]}(\vec{r}; M + i\Gamma_t) = \delta^{(3)}(\vec{r})$$

F_{ij} contribution

$$M_{t\bar{t}} \frac{d\hat{\sigma}_{ij \rightarrow T}}{dM_{t\bar{t}}}(\hat{s}, M_{t\bar{t}}^2, \mu_f^2) = \boxed{F_{ij \rightarrow T}(\hat{s}, M_{t\bar{t}}^2, \mu_f^2)} \frac{1}{m_t^2} \text{Im} G^{[1,8]}(M_{t\bar{t}} + i\Gamma_t)$$

- Evaluated with pQCD at NLO accuracy
- Threshold logarithms from soft regions $z = \rho/\tau \rightarrow 1$ dominating the contribution $\mathcal{L} \otimes F$
- **Resummation** up to NLL accuracy for $gg \rightarrow {}^1S_0^{[1]} ({}^1S_0^{[8]})$, $q\bar{q} \rightarrow {}^3S_1^{[8]}$ in the Mellin Space for $\mathcal{L} \otimes F$

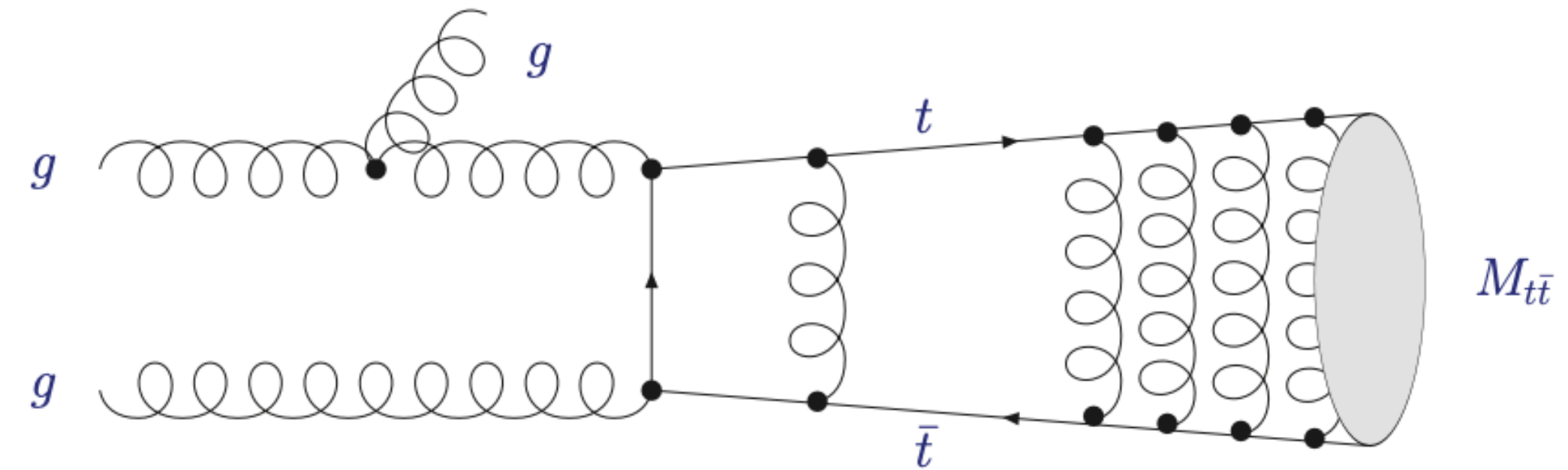
$$M_N[F_{ij}] = F_{ij \rightarrow T}^N(M_{t\bar{t}}^2, \mu_f^2) = \int_0^1 dz z^{N-1} F_{ij \rightarrow T}(\hat{s}, M_{t\bar{t}}^2, \mu_f^2)$$

$$M_N^{-1}[\mathcal{L} \otimes F] \longrightarrow \text{NLO+NLL accuracy}$$

Green Function Contribution

$$M_{t\bar{t}} \frac{d\hat{\sigma}_{ij \rightarrow T}}{dM_{t\bar{t}}}(\hat{s}, M_{t\bar{t}}^2, \mu_f^2) = F_{ij \rightarrow T}(\hat{s}, M_{t\bar{t}}^2, \mu_f^2) \frac{1}{m_t^2} \text{Im} G^{[1,8]}(M_{t\bar{t}} + i\Gamma_t)$$

- Responsible for bound state formation due to multiple gluons exchange
- Only dependent on $M_{t\bar{t}}$ and $\Gamma_t \gg \Lambda_{\text{QCD}}$
- Evaluated at NLO in **QCD**
- The nature of **QCD** potential strictly depends on the colour structure of T



Impact of soft gluon resummation

- Run2@LHC

$$\sqrt{S} = 13 \text{ TeV}$$

$$m_t = 172.5 \text{ GeV (pole mass scheme)}$$

$$\Gamma_t = 1.4 \text{ GeV}$$

$$\text{NNPDF_3.1_NNLO_as_0118}$$

$$\alpha_s(M_Z) = 0.1180$$

$$\mu_r = \mu_f \in \{m_t, 2m_t, 4m_t\}$$

	NLO			resummed		
$gg \rightarrow {}^1S_0^{[1]}$	18.2	18.7	18.3	19.4	20.5	21.1
$gg \rightarrow {}^1S_0^{[8]}$	55.8	55.2	52.8	60.0	61.5	62.0
$q\bar{q} \rightarrow {}^3S_1^{[8]}$	21.7	22.3	22.0	22.4	22.4	22.0

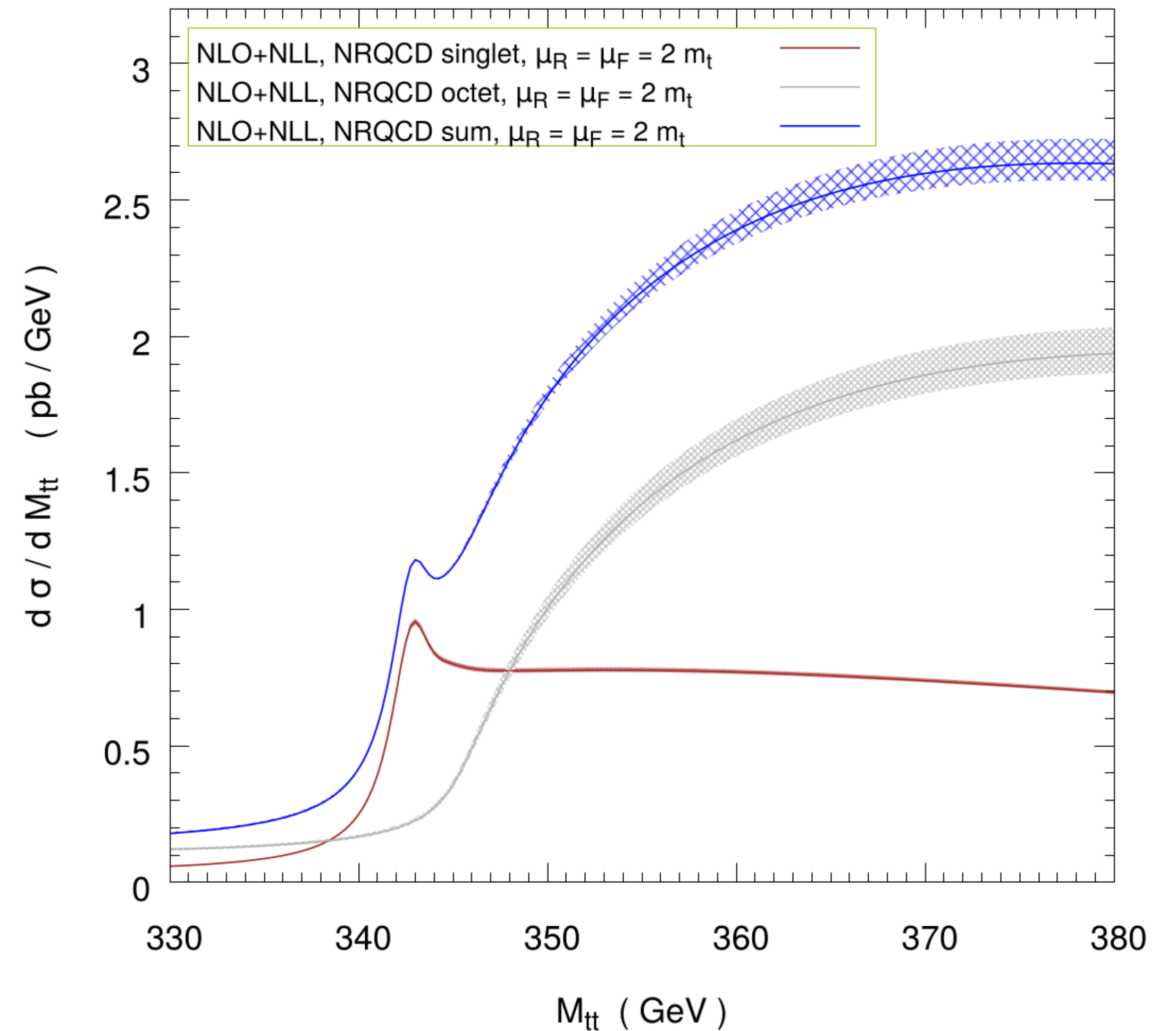
Up to 10% from soft gluon resummation
for the considered channels

No large threshold logarithms from the S -wave channels

$$gg \rightarrow {}^3S_1^{[1,8]} + q\bar{q} \rightarrow {}^1S_0^{[1,8]} + gq \rightarrow {}^1S_0^{[1,8]} + gq \rightarrow {}^3S_1^{[8]} = \mathcal{O}(5\%)$$

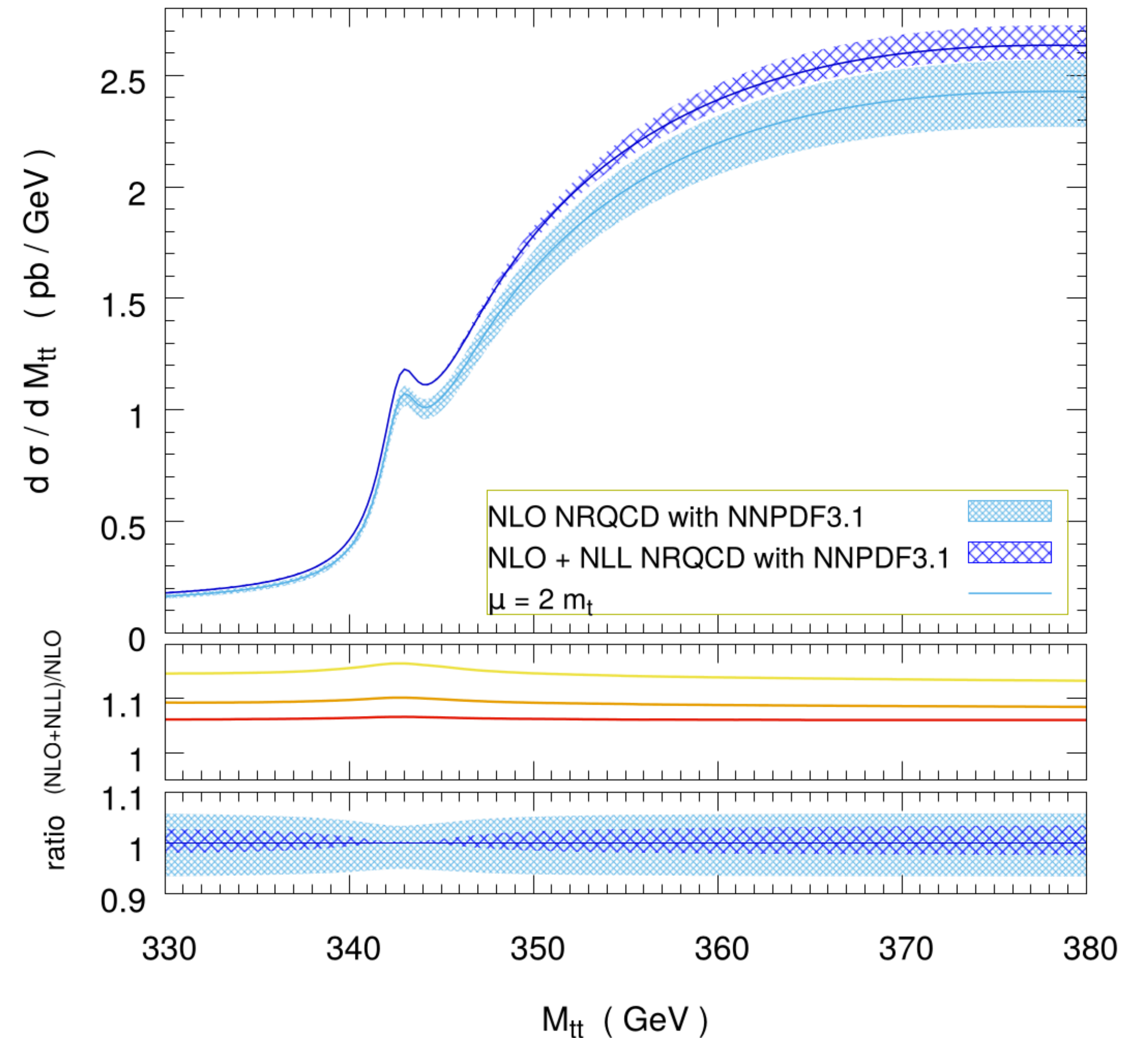
Theoretical Predictions at $\sqrt{S} = 13$ TeV

- $gg \rightarrow {}^1S_0^{[1]}$ shows a resonance peak for *toponium* formation
- $gg \rightarrow {}^1S_0^{[8]} + q\bar{q} \rightarrow {}^3S_1^{[8]}$ shows the repulsive effect at the threshold $M_{t\bar{t}} \simeq 2m_t$
- Strong impact on the shape coming from Γ_t below the threshold



Theoretical Predictions at $\sqrt{S} = 13$ TeV

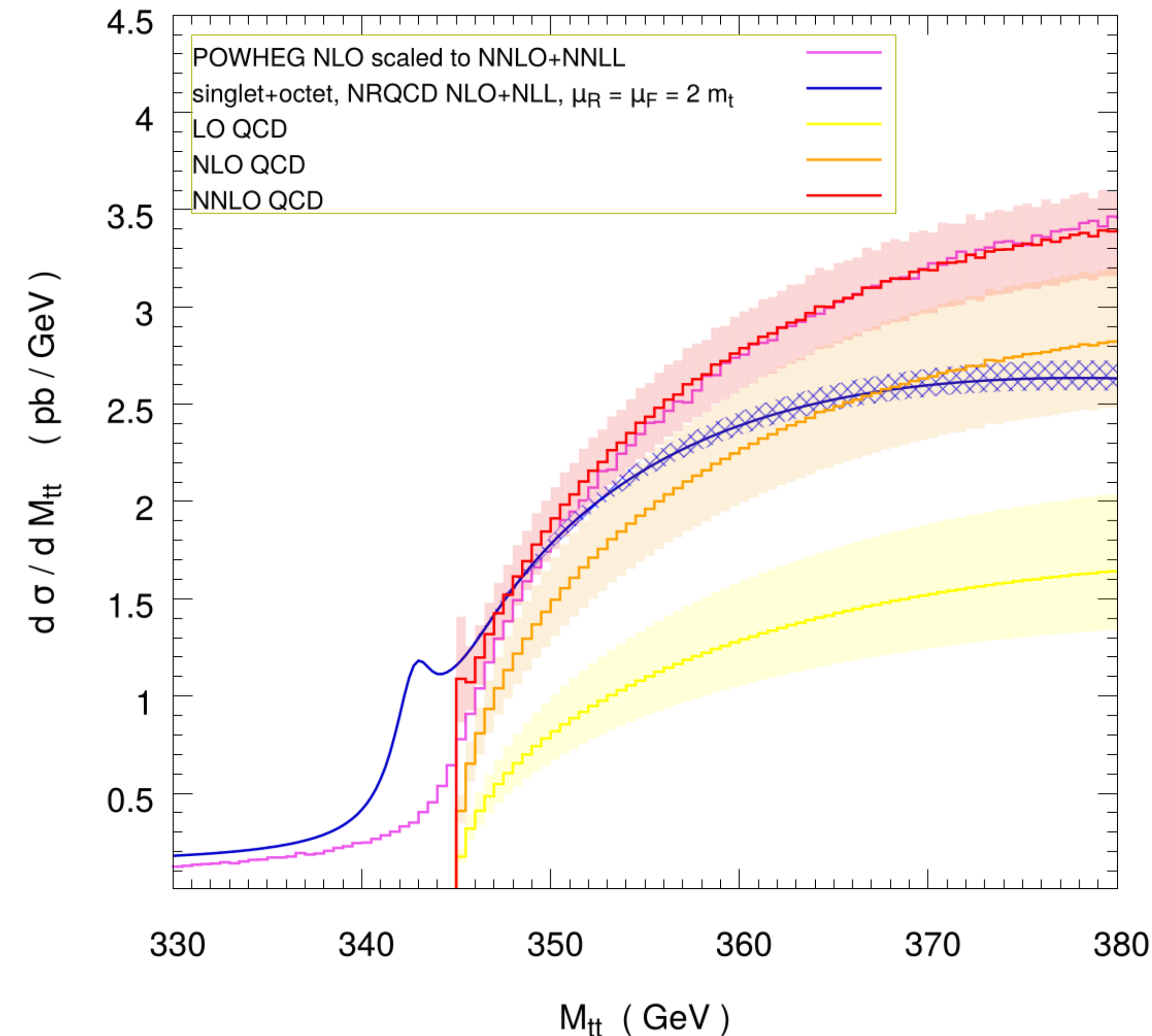
- Approximately **+10%** from soft gluon resummation in the whole $M_{t\bar{t}}$ range
- Reduction of scale dependence, in particular in the peak region
- Scale stability improved



Comparison with CMS analysis

- **NLO+NLL** with NRQCD
- Fixed-Order terms at **LO**, **NLO** and **NNLO**
(Garzelli, Mazzitelli, Moch, Zenaiev [2311.05509])
- **NLO POWHEG** rescaled to NNLO+NNLL
(Thanks to Anuar, Grohsjean, Jeppe, Schwanenberger)
- NRQCD only valid for $|M_{t\bar{t}} - 2m_t| \lesssim 5 \text{ GeV}$

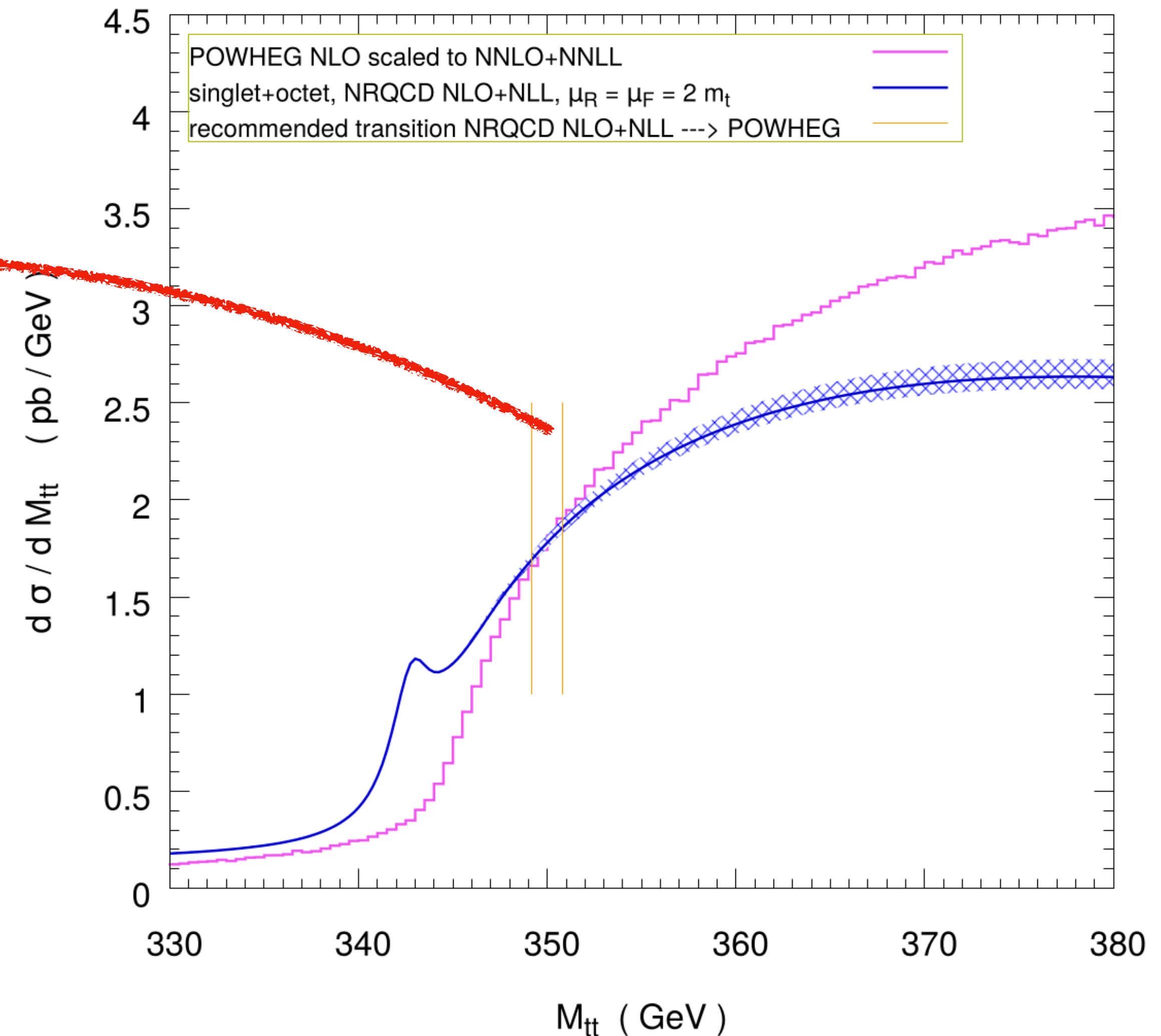
A matching is required!



From NRQCD to NNLO

Additive matching for
 $M_{t\bar{t}} \gtrsim 350 \text{ GeV}$
where NRQCD stops to be valid

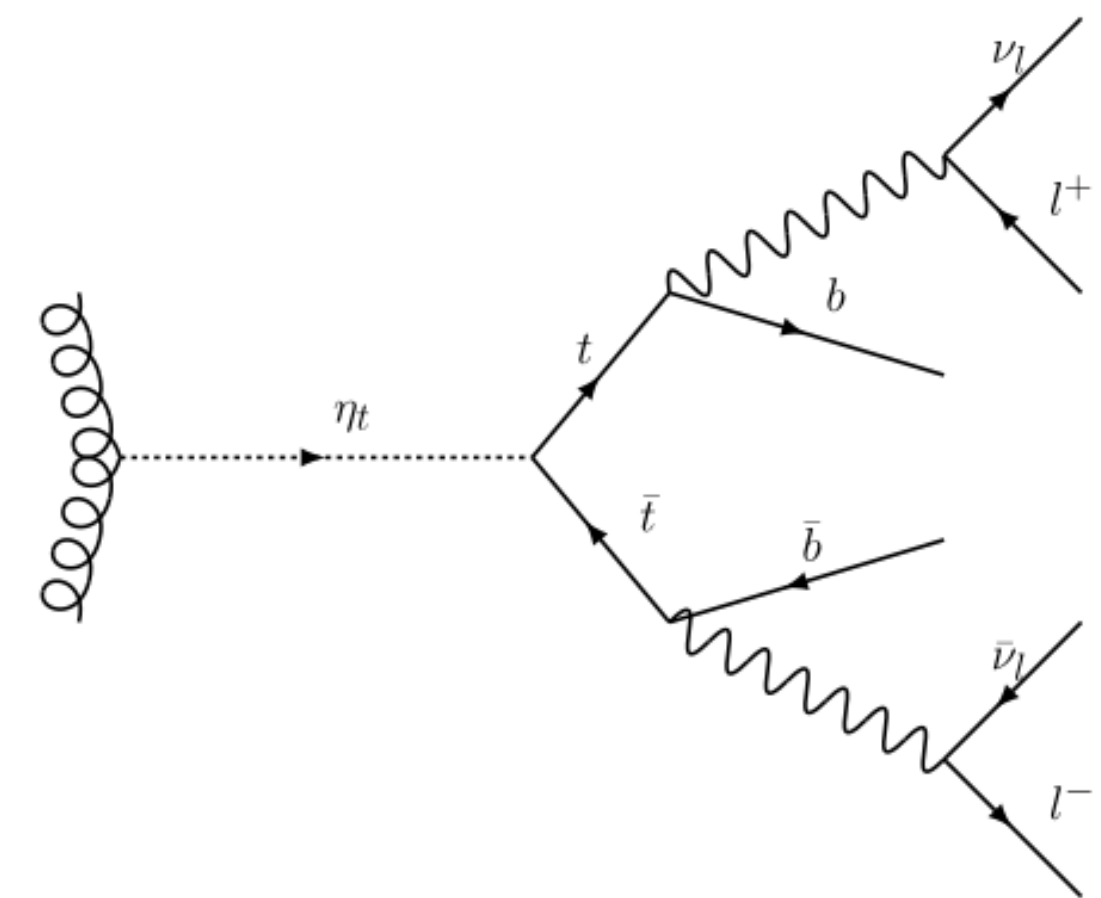
POWHEG predictions only applicable for
 $M_{t\bar{t}} \gg 2m_t$



Modelling $t\bar{t}$ resonances

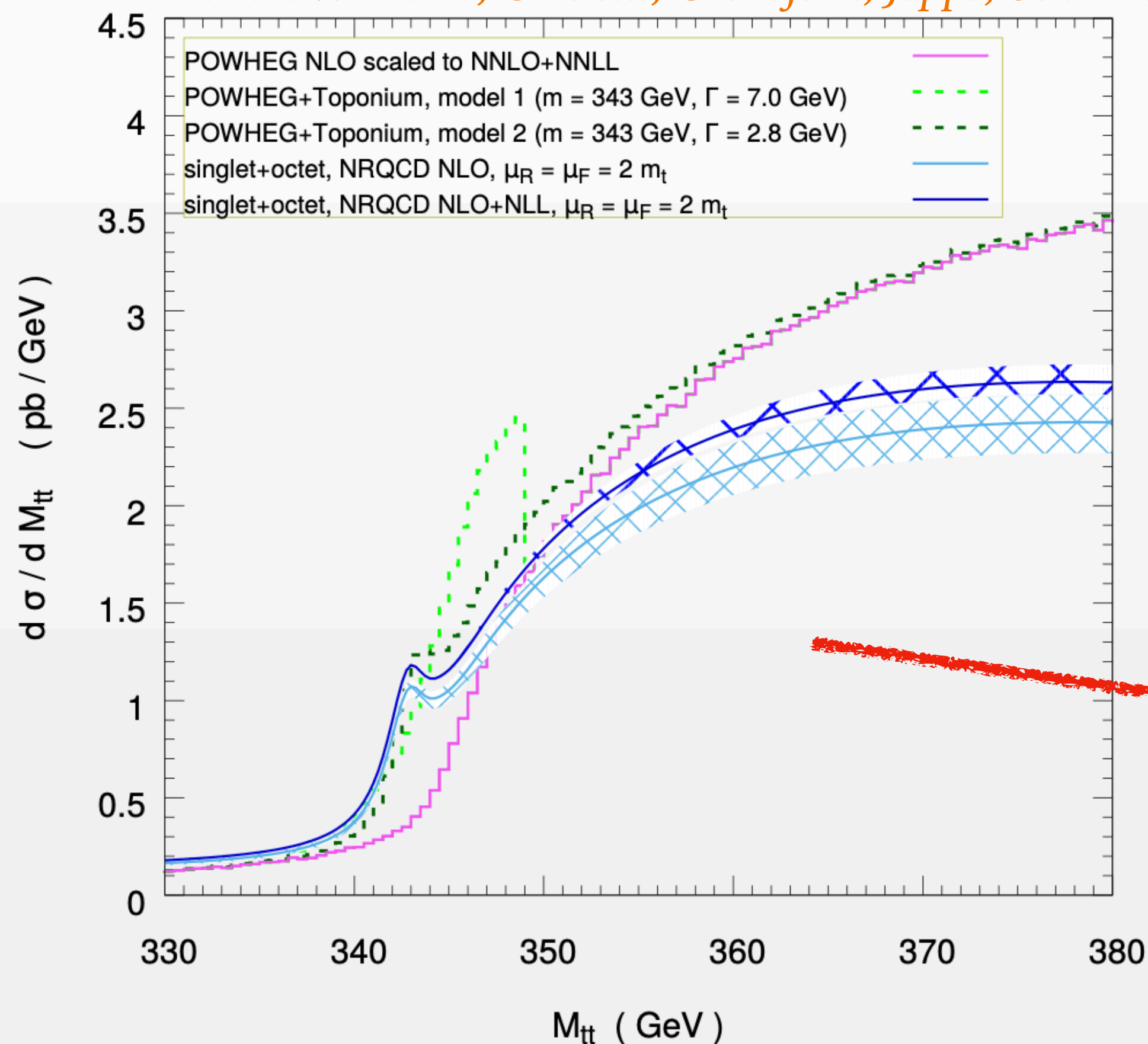
- CMS analysis based on NLO POWHEG predictions rescaled at NNLO+NNLL
- Bound states simulated by introducing a new particle η_t with mass and decay fitted for $M_{t\bar{t}} \in [337, 349]$ GeV (Fuks, Hagiwara, Ma, Zheng [2102.11281])
- Matrix element re-weighting with NRQCD Green Function (Fuks, Hagiwara, Ma, Zheng [2411.18962]) not yet implemented for analysis

$$\mathcal{L}_{\eta_t} = \frac{1}{2} \partial_\mu \phi_{\eta_t} \partial^\mu \phi_{\eta_t} - \frac{1}{2} m_{\eta_t} \phi_{\eta_t}^2 - \frac{1}{4} g_{gg\eta_t} \phi_{\eta_t} G_{\mu\nu}^a \tilde{G}^{a\mu\nu} - i g_{tt\eta_t} \phi_{\eta_t} \bar{t} \gamma_5 t$$



Modelling $t\bar{t}$ resonances

Thanks to Anuar, Garzelli, Grohsjean, Jeppe, Schwanenberger



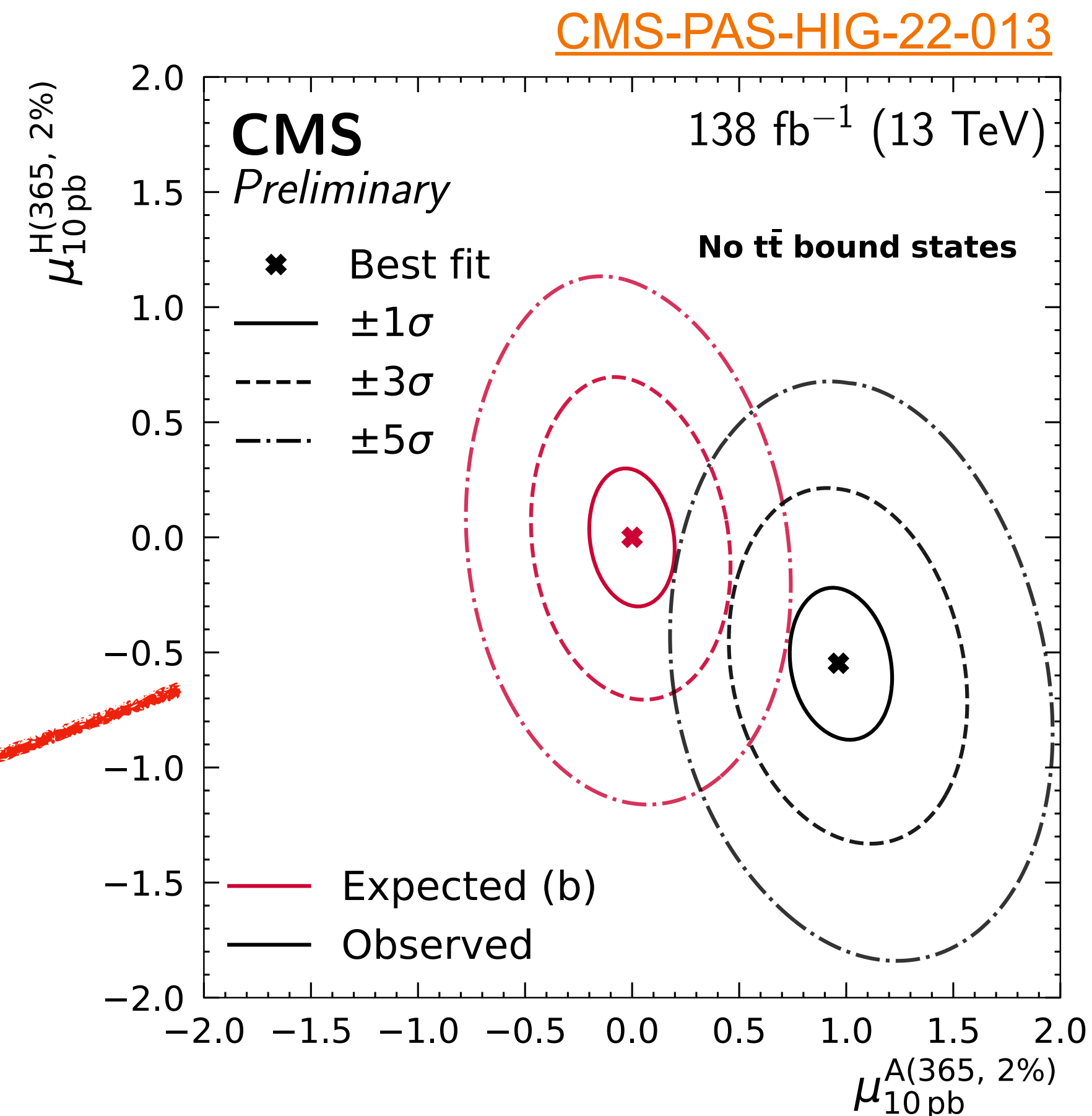
- No accounting for QCD higher orders effects
- Repulsive interaction for color octet states, other S - and P - wave singlet states are not considered
- NRQCD with Coulomb and threshold resummation to fill this gap in $M_{t\bar{t}} \in [340, 350]$ GeV

- CMS Fuks model implementation ($\Gamma_{\eta_t} = 7$ GeV) does not match with NRQCD
- Improved agreement moving from $\Gamma_{\eta_t} = 7$ GeV to $\Gamma_{\eta_t} = 2\Gamma_t = 2.8$ GeV (*Maltoni et al. [JHEP 03, 2024, 099]*)

Modelling $t\bar{t}$ resonances

- Is the excess in the data related to a scalar or a pseudoscalar?
- 2D fit with arbitrary signal strength
- Scalar term compatible with zero

Data point towards a pure pseudoscalar!



Conclusions and Outlooks

- NRQCD methods highly useful to provide reliable theoretical inputs for the experimental analysis
- Pseudoscalar particle to model “toponium” formation below the threshold
- NNLO corrections to Green Function ($\mathcal{O}(10\%)$) in the peak region
- NNLO corrections to hard function F_{ij} ($\mathcal{O}(10\%)$) at the threshold
- Lower bound estimate on $d\sigma/dM_{t\bar{t}}$ for $M_{t\bar{t}} \simeq 2m_t$
- Forthcoming refined study about the impact of parameters settings (m_t , $\alpha_s(M_Z)$, μ_r , μ_f , PDFs sets)
- More accurate matching prescription
- Other observables to be considered, kinematic cuts...

Thank you for the attention!!!