

Probing magnetic field turbulence in supernova remnants & its importance for cosmic-ray acceleration

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- Yi-Jun Yang (Hong Kong)
- Luca Baldini (Pisa)
- Niccolo Buciantini (Arcetri)
- The IXPE team!

Some history



Victor Hess



Walter Baade



Fritz Zwicky



Iosif Shklovsky

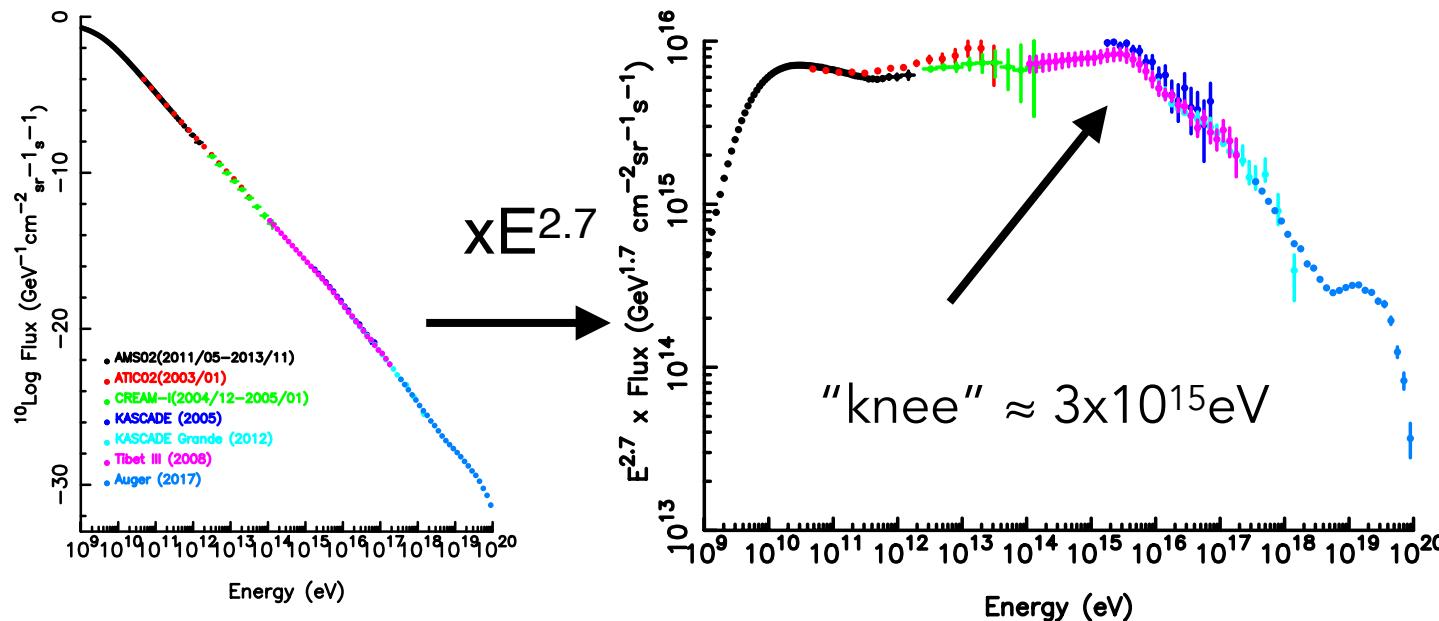
1911: Victor Hess discovers “cosmic rays”

1930s: cosmic rays are energetic particles!

1932: Baade & Zwicky: supernovae form neutron stars and are sources of cosmic rays

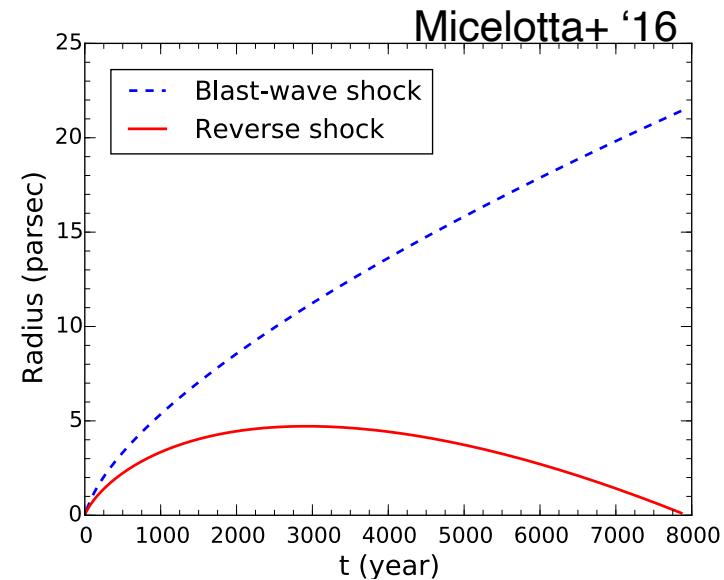
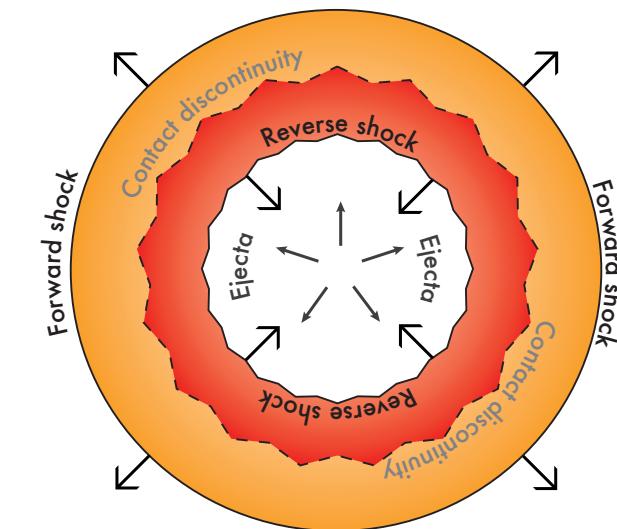
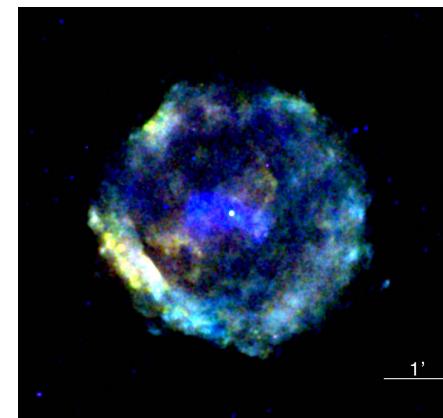
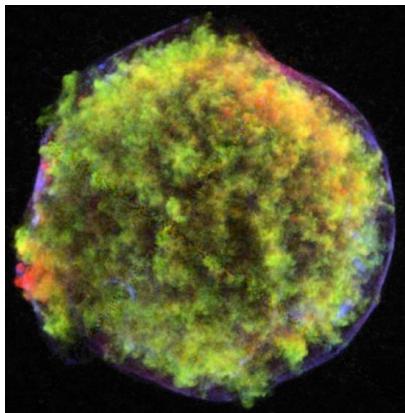
1950: Shklovsky suggests supernova radio emission is caused by relativistic electrons
(electron cosmic rays) → synchrotron radiation → predict polarization

Cosmic rays



- ISM energy density CRs $\approx 1 \text{ eV cm}^{-3}$, escape time $\tau \approx 15 \times 10^6 \text{ yr}$
- To fill Galaxy: need a power of $dE/dt \approx 6 \times 10^{40} \text{ erg/s}$
- SN power: $dE/dt \approx 6 \times 10^{41} \text{ erg/s}$ (10^{51} erg/SN , 2SNe/100yr)
 - SNRs considered primary sources of cosmic rays!
 - electron/positrons <1%; origin
- Problem: SNRs can explain CR power needed, but not the "knee"

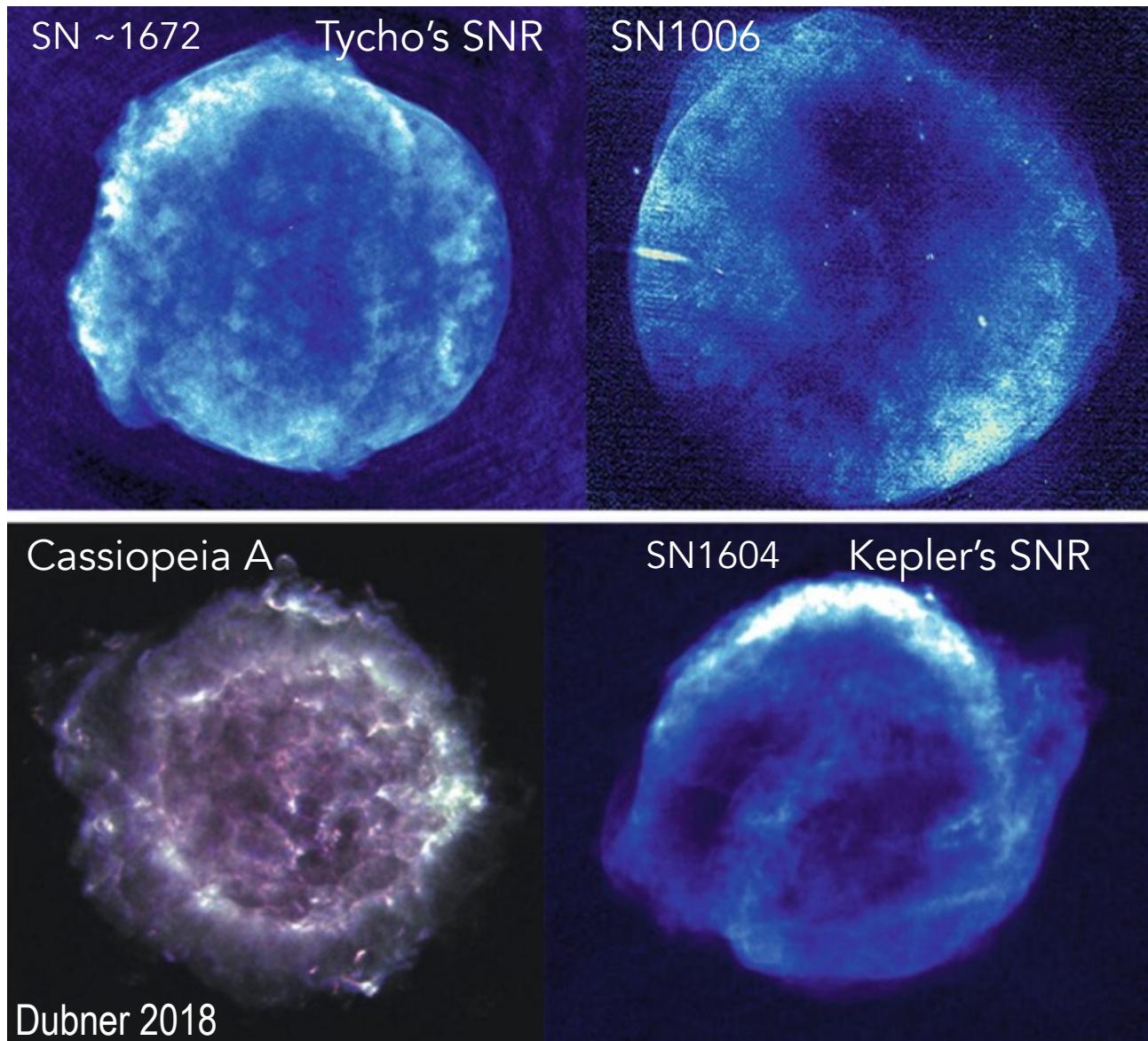
Supernova remnants (SNRs)



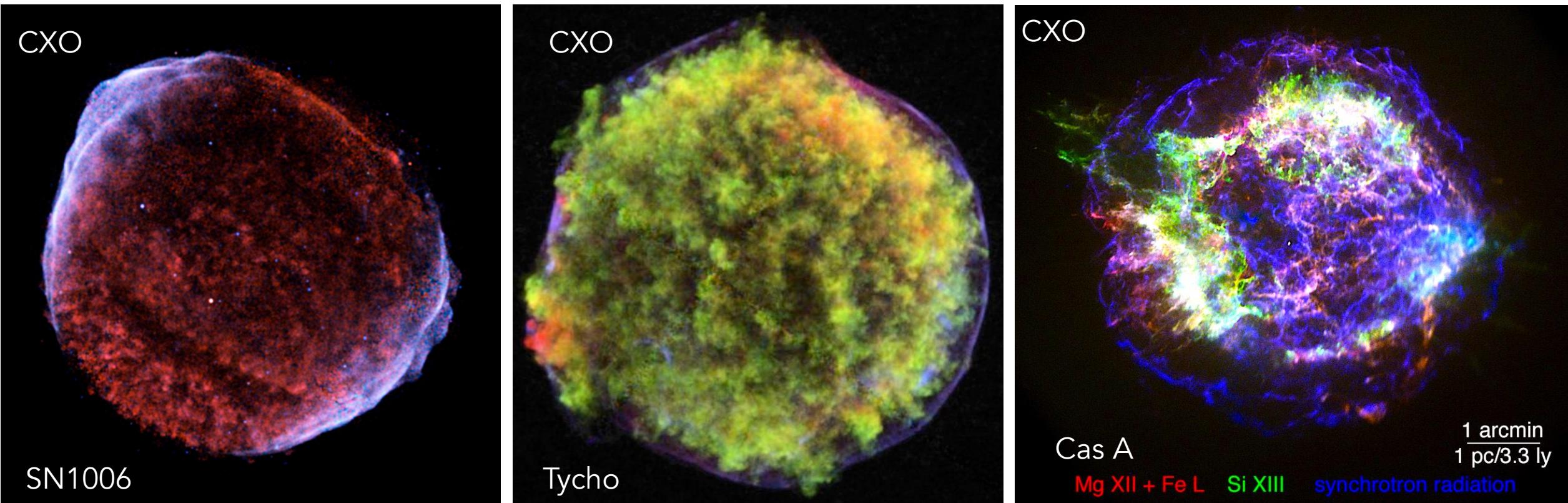
- Initiated by fast/energetic gas ejected by supernova explosion
- SNR shock are *collisionless* shocks:
 - shock transitions *not* due to atom-atom collisions
 - allows for (or results in?) cosmic-ray acceleration
- Young SNRs have two shocks:
 - forward shock (blast wave): shocks CSM/ISM
 - reverse shock: heats and compresses freely expanding SN ejecta!

Radio maps of young supernova remnants (VLA)

- Radio synchrotron emission
- Requires \sim GeV electrons
- Early evidence that SNRs accelerated particles (electrons) to relativistic energies



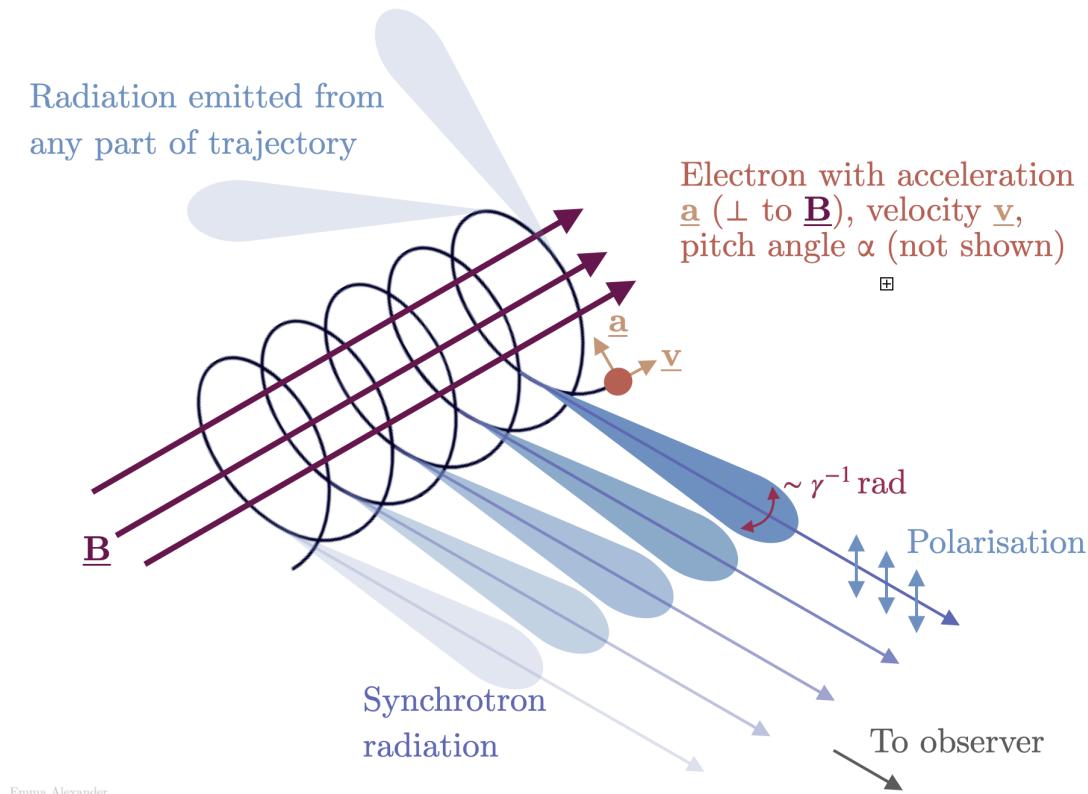
X-ray synchrotron emission from young SNRs



- Since 1995 (Koyama+ 95): young SNRs identified as X-ray synchrotron sources
- Requires 10-100 TeV electrons!

Polarization in astrophysics

- Polarization in general: geometric dependence
 - e.g. scattering geometry, or B-fields



- Synchrotron radiation: relativistic e^-/e^+ spiraling around B-field
- Instrinsically polarized: power law ($F_\nu \propto \nu^{-\alpha}$): pol. fraction = $\frac{\alpha + 1}{\alpha + 5/3} \approx 70\%$
- Polarization vector perpendicular to magnetic field

Diffusive shock acceleration (DSA): B-field turbulence needed!

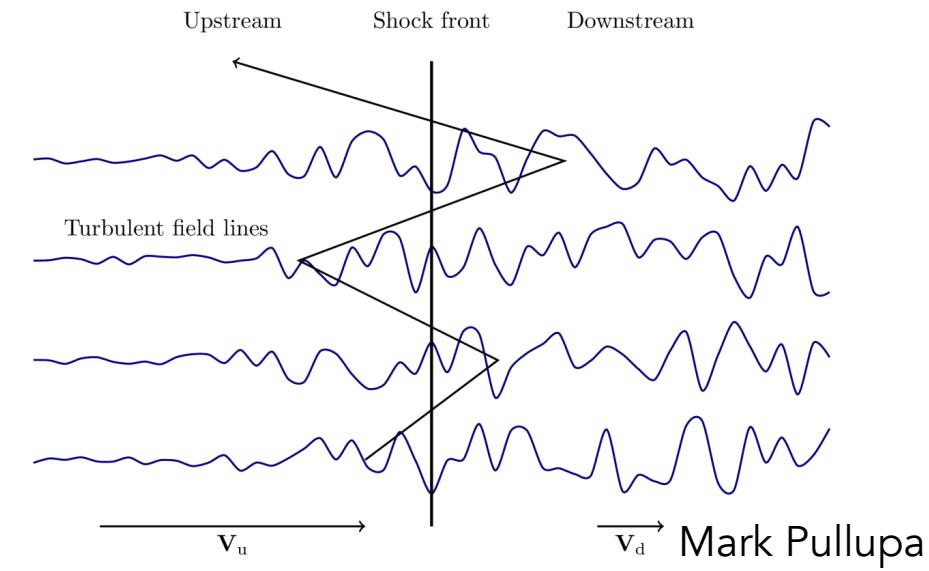
- Particles gain energy by crossing shock:

- $\Delta V_{\text{plasma}} \rightarrow$ Lorentz boost of $\frac{\Delta E}{E} \approx \frac{\Delta V}{c}$

- Diffusion: particle can cross shock $D = \frac{1}{3}c\lambda_{\text{mfp}} = \frac{1}{3}\eta r_g = \frac{1}{3}\eta \frac{E}{eB}$

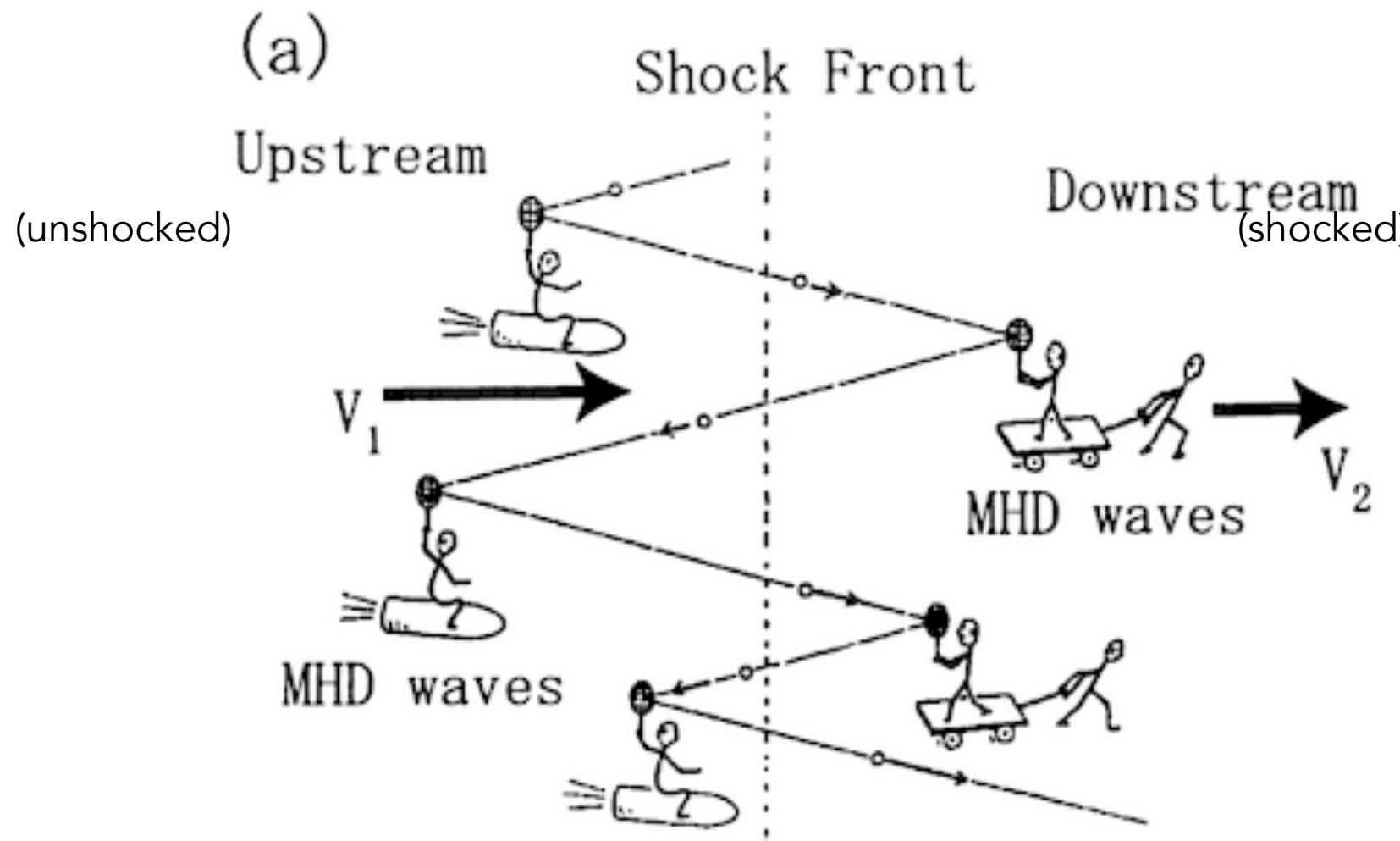
- Acceleration time: $\tau \approx \frac{8D_0}{V_s^2} \rightarrow E_{\text{max}} \propto \eta^{-1} B V_s^2 t$

- Higher energy: V_s high, B high and $\eta \approx \langle (\delta B/B)^2 \rangle^{-1} \approx 1$



turbulent fields!

DSA cartoon



M. Scholer

X-ray synchrotron radiation

- Requires >10 TeV electrons:

- $$h\nu \approx 19 \left(\frac{B}{100 \text{ }\mu\text{G}} \right) \left(\frac{E}{100 \text{ TeV}} \right)^2 \text{ keV}$$

- Electrons cool fast:

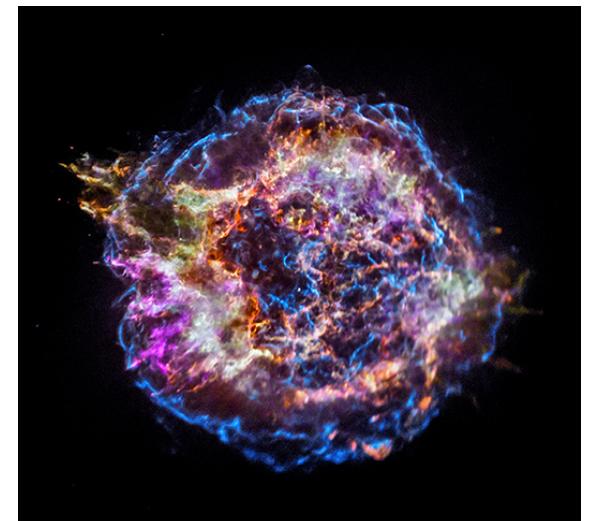
- $$\tau_{\text{cool}} \approx 12.5 \left(\frac{B}{100 \text{ }\mu\text{G}} \right)^{-2} \left(\frac{E}{100 \text{ teV}} \right)^{-1} \text{ yr}$$

- → Acceleration needs to be fast
- → Electrons “out of contact with shock” will not emit X-rays
- → Narrow X-ray filaments

- Combination of acceleration and cooling:
$$h\nu_{\text{cutoff}} \approx 1.4\eta^{-1} \left(\frac{V_{\text{sh}}}{5000 \text{ km/s}} \right)^2 \text{ keV}$$

- $$\eta \approx \langle (\delta B/B)^2 \rangle^{-1} \approx 1$$
 turbulence parameter

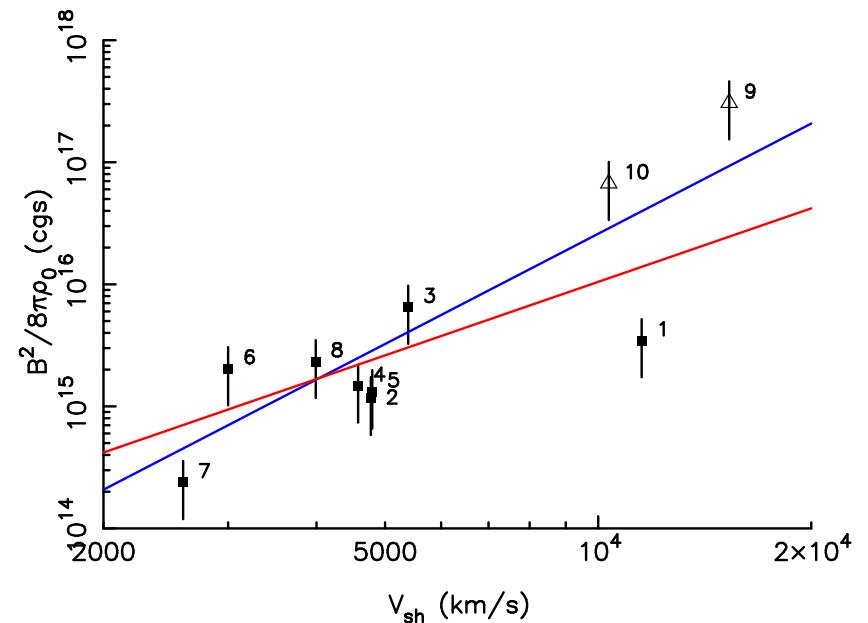
- Electrons have cooled when far from shock:
$$B \approx 110 \left(\frac{l}{10^{17} \text{ cm}} \right)^{-2/3} \mu\text{G}$$



Magnetic -field amplification

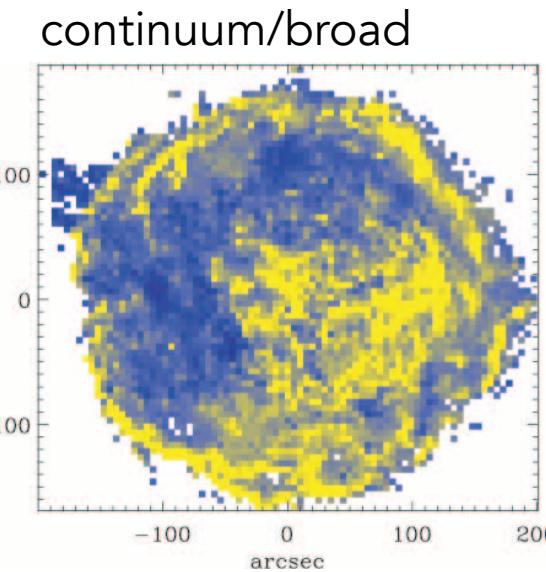
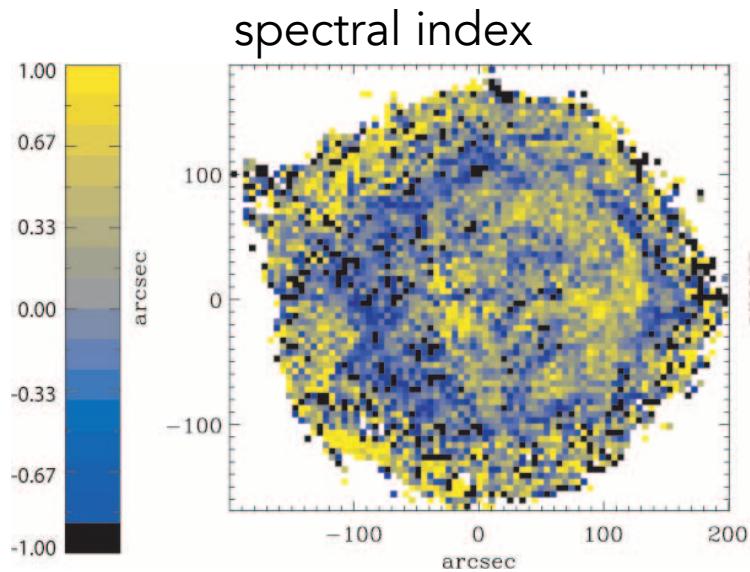
Helder, JV, + 2012

ID	SNR	Dist (kpc)	$n_{\text{H},0}$ (cm^{-3})	V_s (km/s)	ΔR ($''$)	l_{diff} (10^{17} cm)	B_2 (μG)	E_{el} (TeV)	τ_{syn} (yr)
1	G1.9+0.3 (SW)	8.5	0.022	11520	3.1	2.8	66.6	33	86
2	Cas A (NE)	3.4	0.9	4773	1.1	0.4	246.5	17	12
3	Kepler (SE)	5.0	0.05	5390	1.8	0.9	137.8	23	29
4	Tycho (W)	3.0	0.5	4579	1.6	0.5	207.0	19	16
5	SN1006 (E)	2.2	0.085	4795	9.1	2.1	81.1	30	64
6	RCW 86 (NE)	2.5	0.01	3000	28.6	7.6	34.5	46	232
7	RX J1713.7-3946	1.0	0.1	2592	63.5	6.7	37.3	44	206
8	RX J0852.0-4622	1.0	0.03	3990	28.4	3.0	63.9	34	92

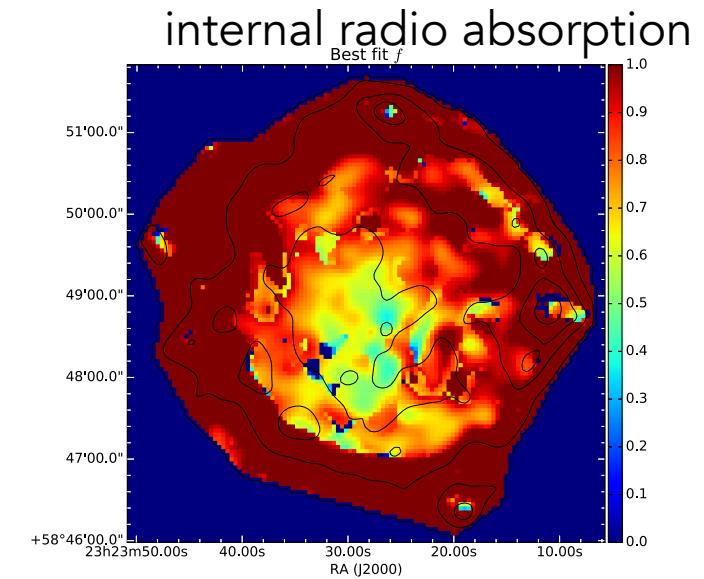


- Magnetic fields much larger than ISM: $B \approx 30 - 300 \mu\text{G}$
- Likely mechanism: Bell (2004) instability
- Bell (2004): $B^2 \propto \rho V_s^3$
 - Indeed: higher densities associated with larger B

Cassiopeia A: X-ray synchrotron from western reverse shock



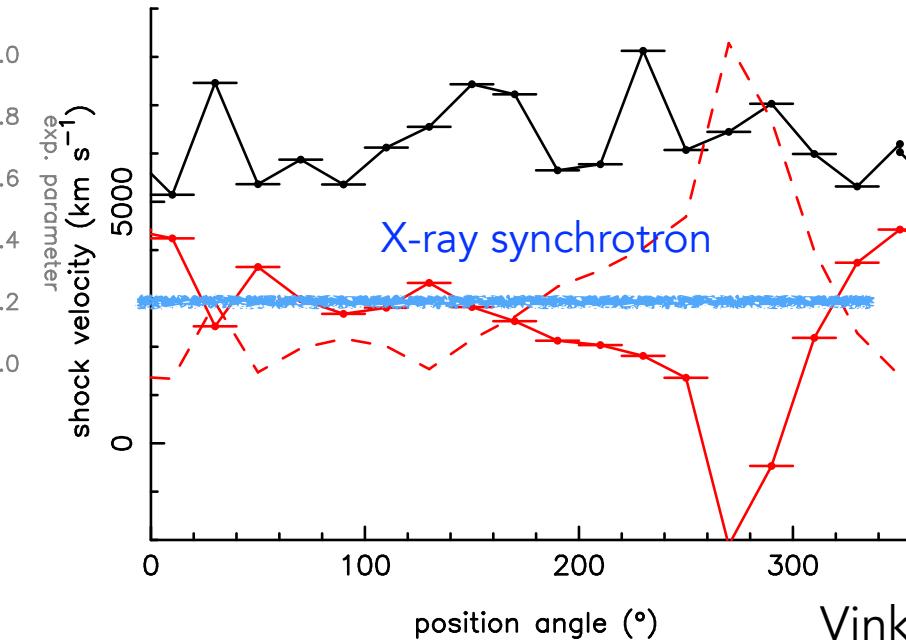
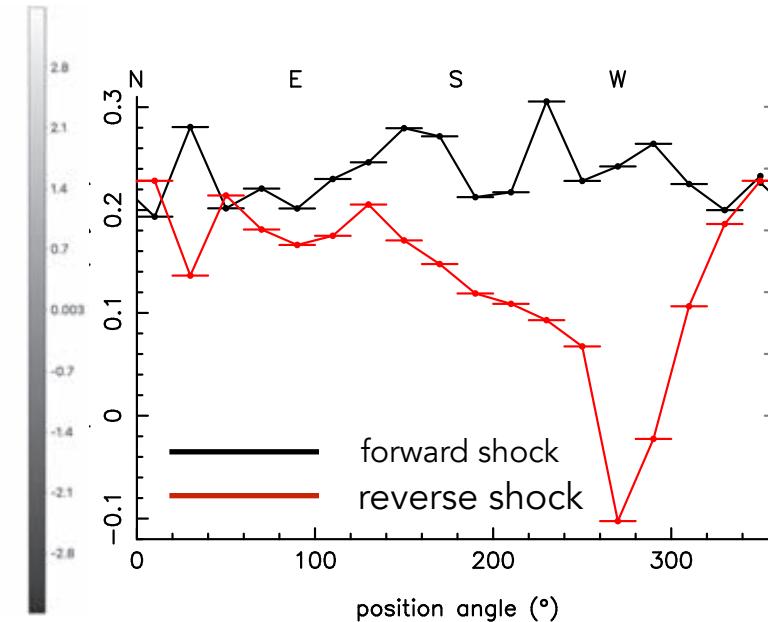
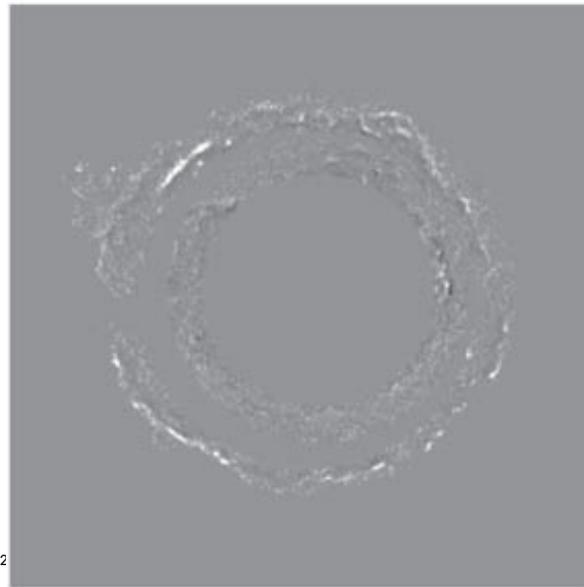
Helder & Vink 2008



Arias, Vink, et al 2018

- X-ray synchrotron radiation: requirese $V_s > 3000$ km/s
- Narrow filaments: $B \sim 200 \mu\text{G}$
 - Apperently B-field amplification even with low seed fields (ejecta)!

Expansion rates

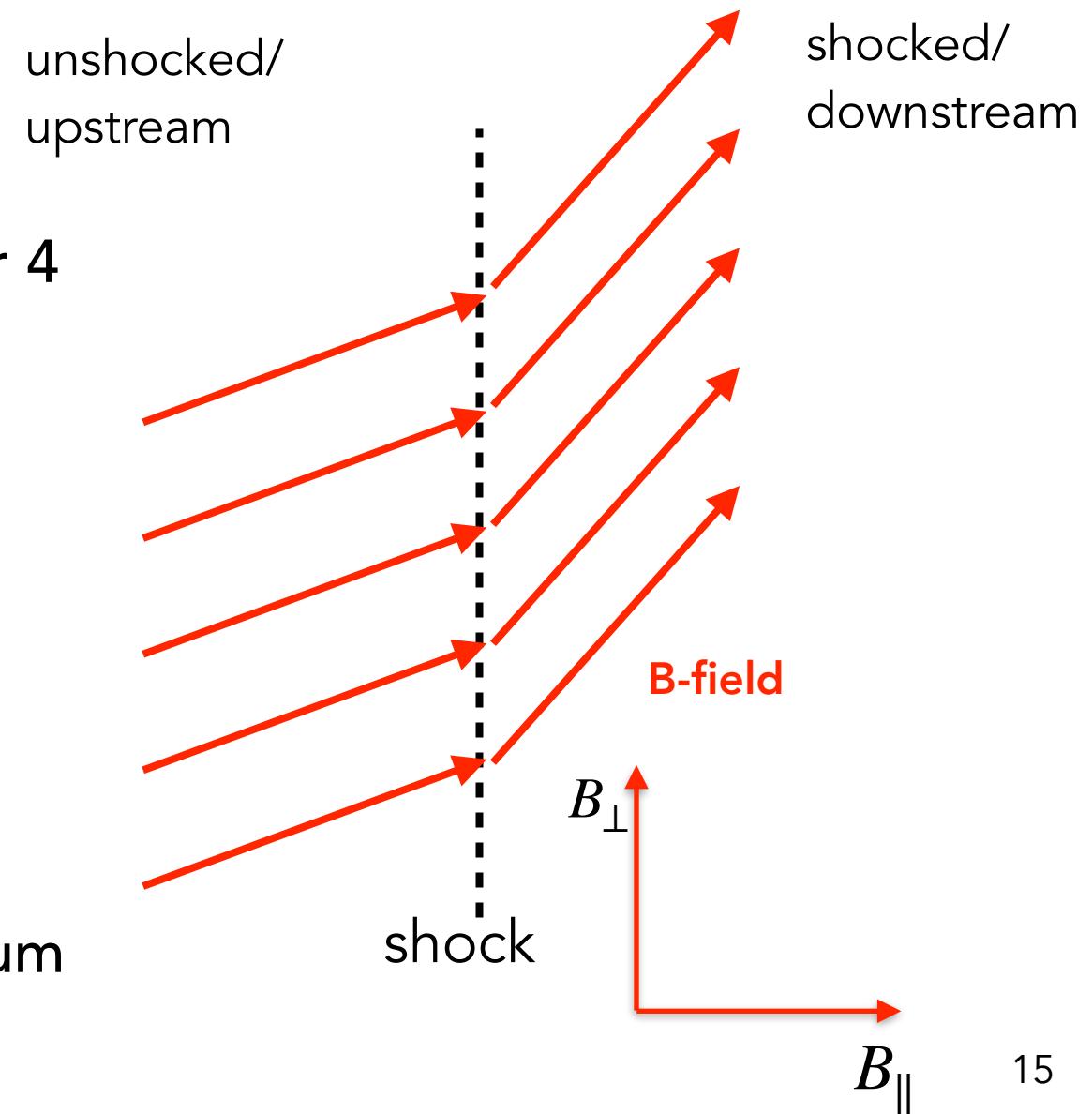


Vink+ '22a

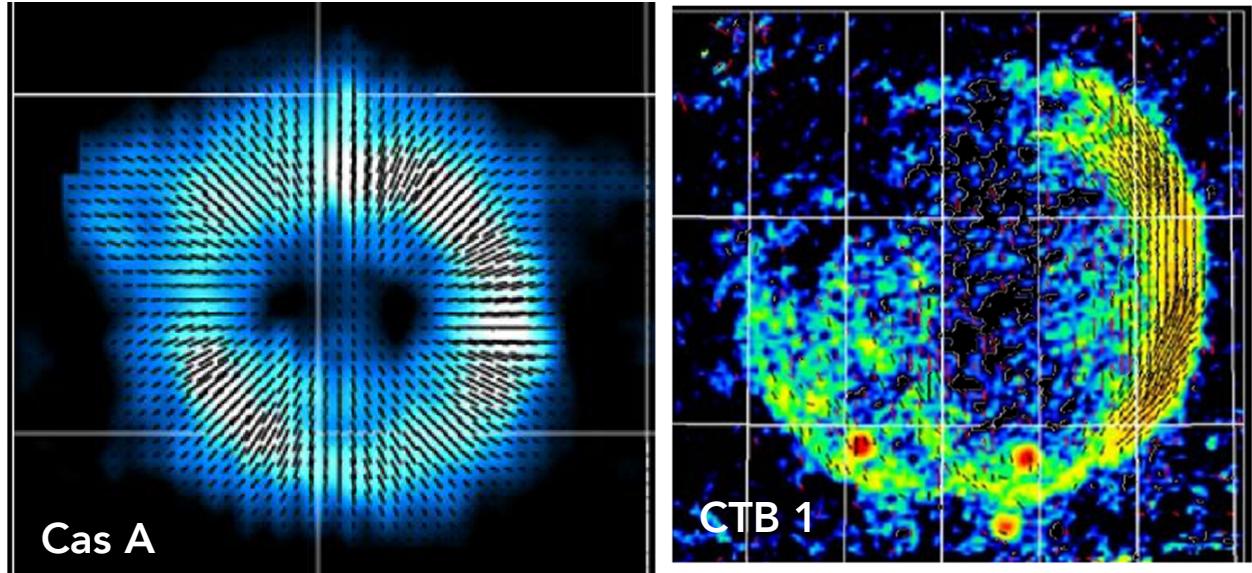
- Forward shock: rate 0.2 - 0.3 %/yr (times scale 350-550 yr)
- Expansion parameter: $R \propto t^m \rightarrow m = \frac{V_{\text{sh}}}{R_{\text{sh}}/\text{age}}$ $m=0.6-0.95$
 - bit larger than older measurements
- Reverse shock is moving inward in the West!

Shock aligns B-fields

- Strong shock: plasma compressed by factor 4
- B_{\perp} compressed by 4
- B_{\parallel} uncompressed
- B-field turbulence for DSA:
 - self-generated by cosmic rays!
 - resonant (wavelength \approx gyroradius)
 - non-resonant (Bell '04)
- Theories consider mostly upstream medium



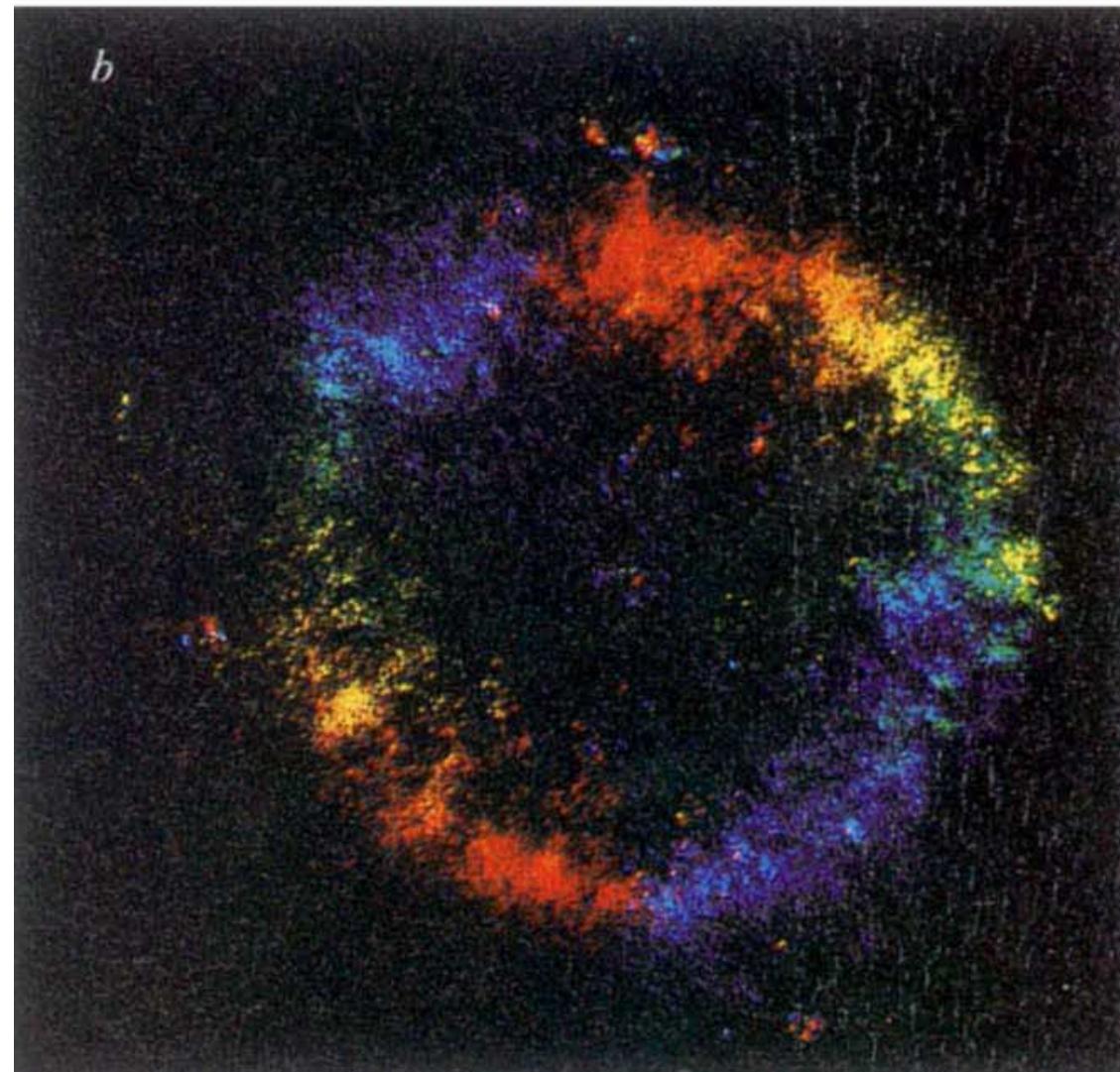
Radio synchrotron polarization from SNRs



Dubner&Giacani (2015)
(Magnetic-field vectors)

- *Mature* SNRs ($\gtrsim 2500$ yr): tangentially oriented fields
 - Makes sense: shock compresses tangential B-field components only
- *Young* SNRs ($\lesssim 2500$ yr): radially oriented B-fields and low pol. frac (Cas A: ~5%)
 - Poorly understood

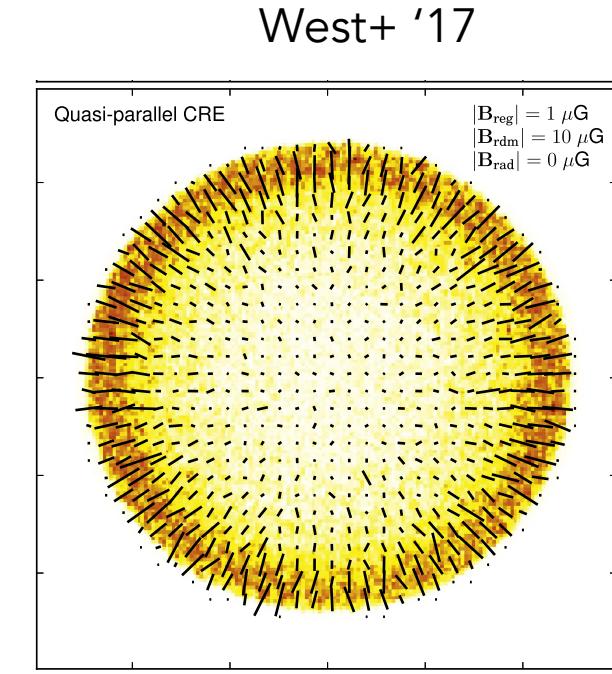
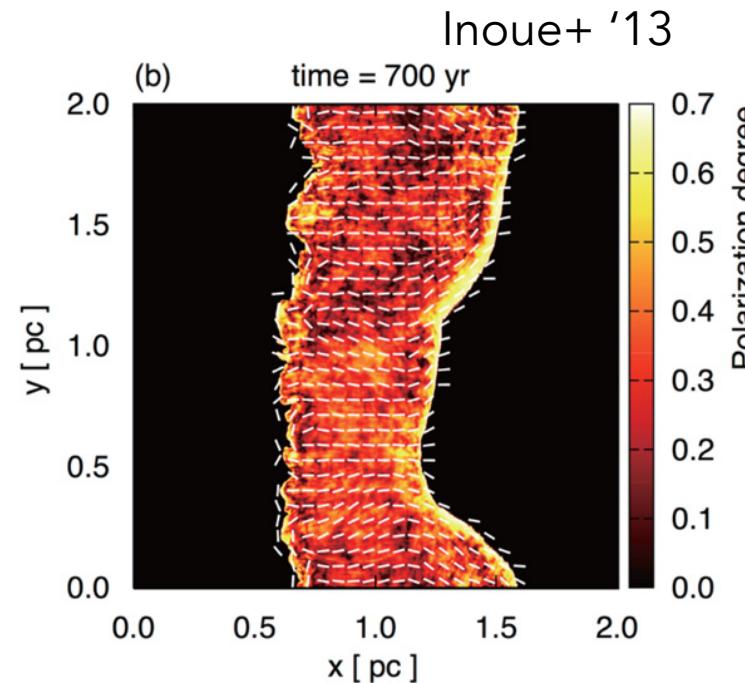
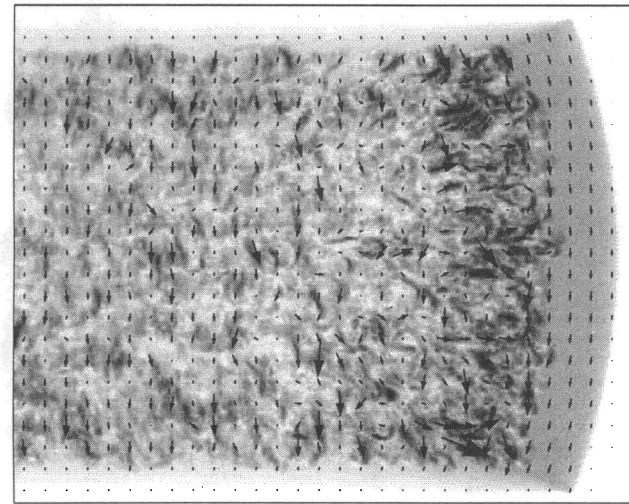
POLARIZATION AND MAGNETIC FIELDS



Braun+ '87

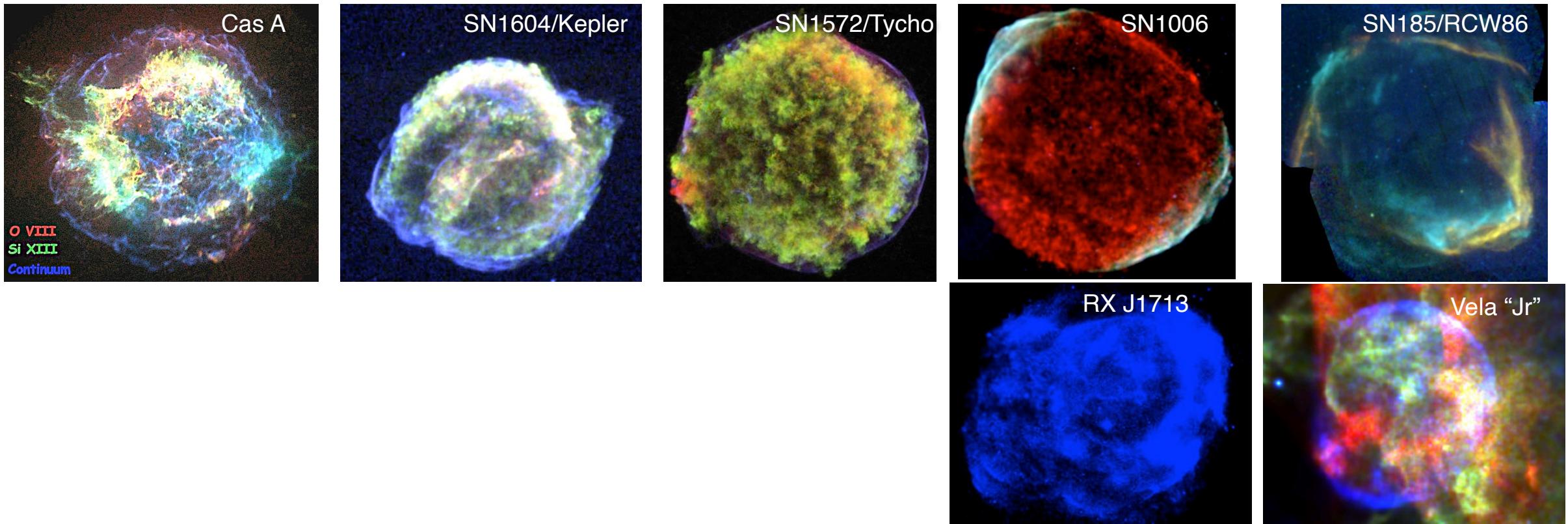
Explanations for radial B-fields in young SNRs

Jun&Norman '96



- Two schools of thoughts:
 1. Hydrodynamical filamentation, due to Rayleigh-Taylor or other instabilities
 - Assumes tangential magnetic field at shock, and radial further downstream
 2. Acceleration happens where B-field is parallel (i.e. radial): only emission from these regions

Why X-ray polarization if we have radio polarization?



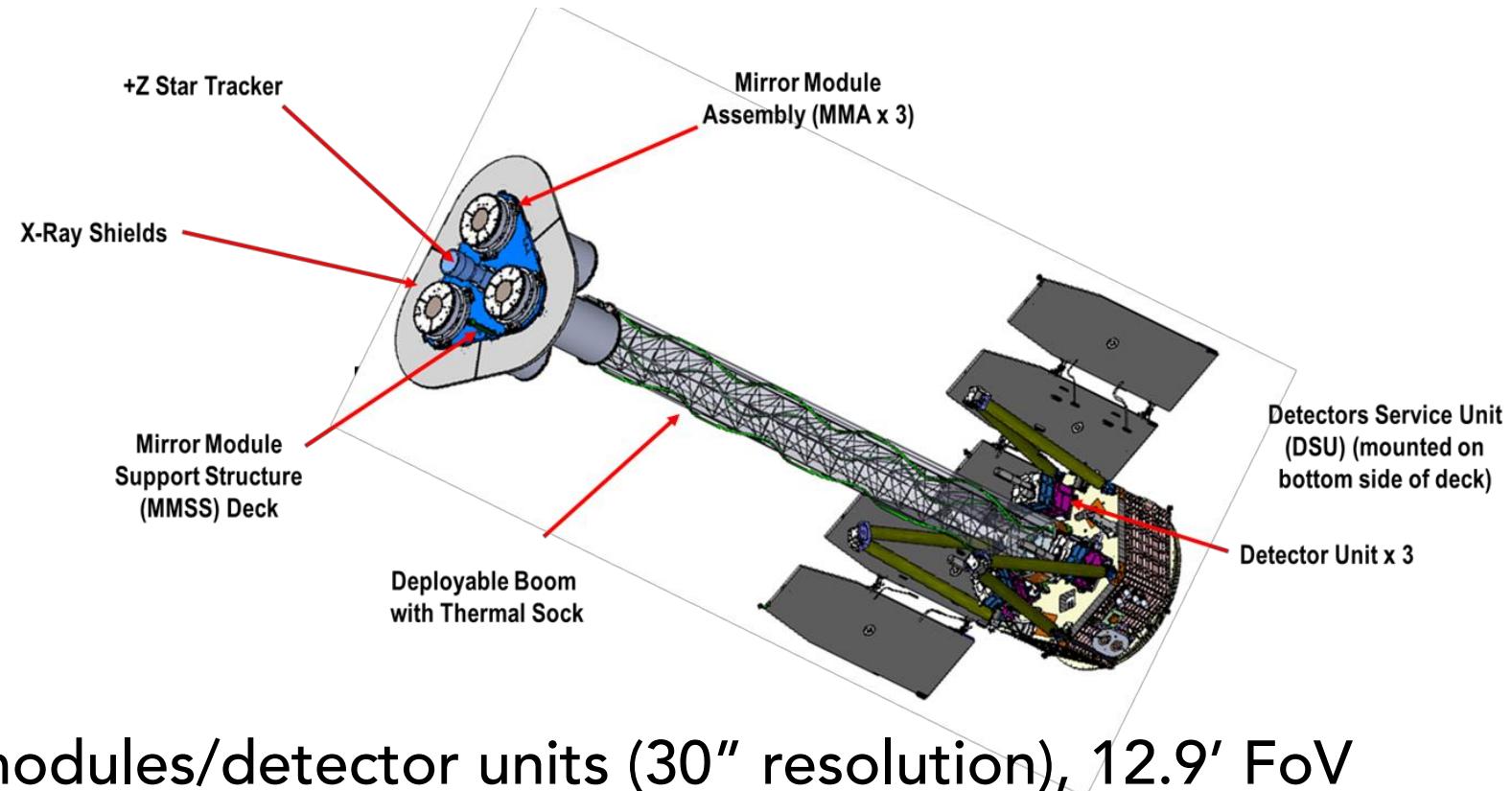
- X-ray synchrotron radiation → only near shocks (not contact discontinuity!)
 - Turbulence expected to be high here (at least upstream)
- Only young (<3000 yr) SNRs show X-ray synchrotron radiation
- Complication: also thermal X-rays (except Vela Jr, RXJ1713)

Imaging X-ray Polarimetry Explorer (IXPE)



- NASA/ASI small explorer mission: launched Dec. 9 2021
- US: spacecraft + X-ray mirrors; Italy: detectors

Imaging X-ray Polarimetry Explorer (IXPE)



- 3 X-ray mirror modules/detector units (30" resolution), 12.9' FoV
- Gas-pixel detectors

Measuring X-ray polarization with IXPE

Weisskopf+ '22

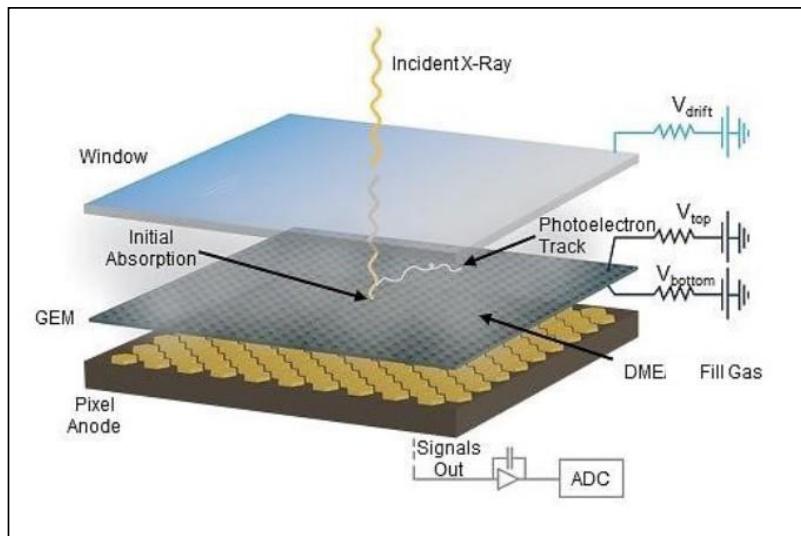
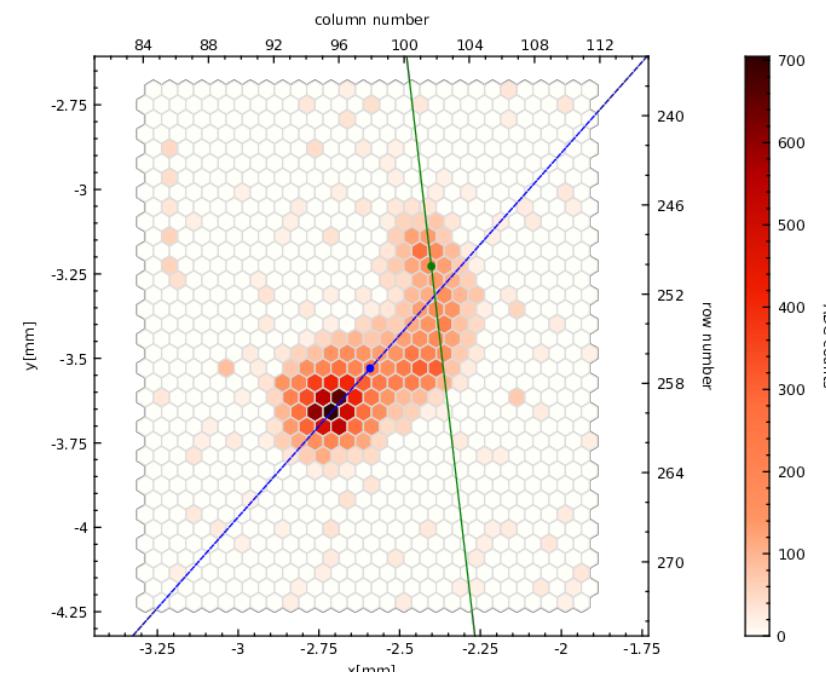
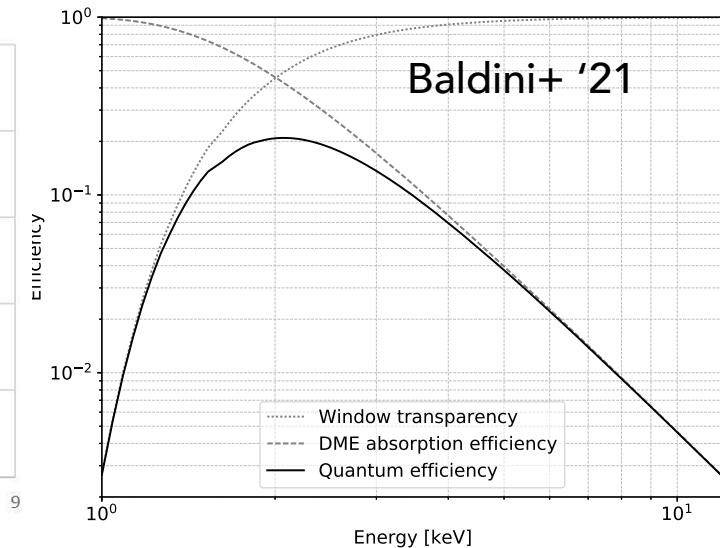
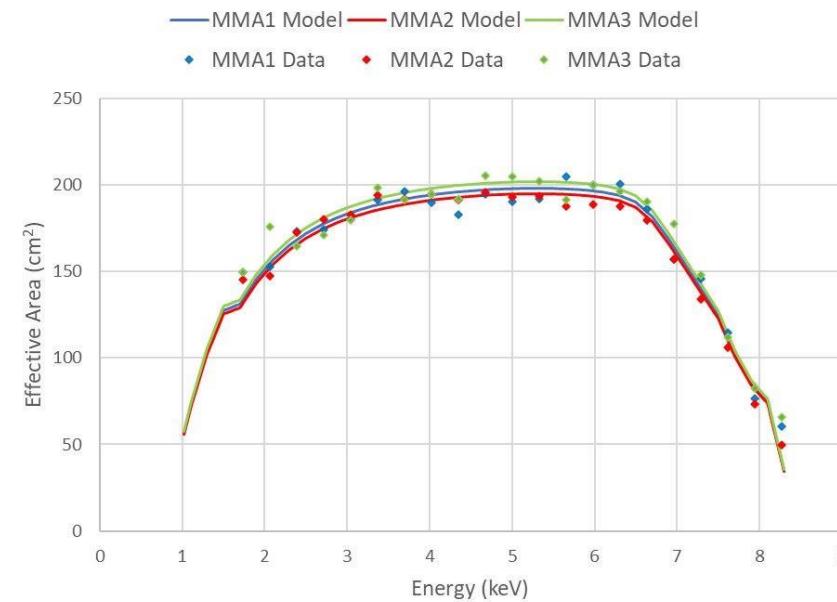
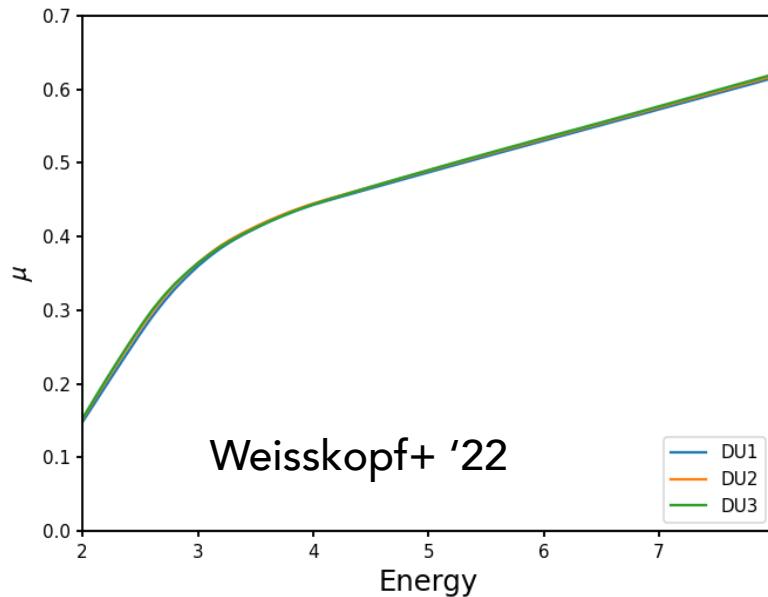


Figure 9: Schematic of the Gas Pixel Detector (GPD)



- Gas Pixel Detector: photo-electron (pe) angle $\phi \propto \cos^2 \psi$
 - pe creates secondary electron cloud: shape used to determine Φ
- Φ determined from shape of secondary electron clouds

Modulation curve and efficiency

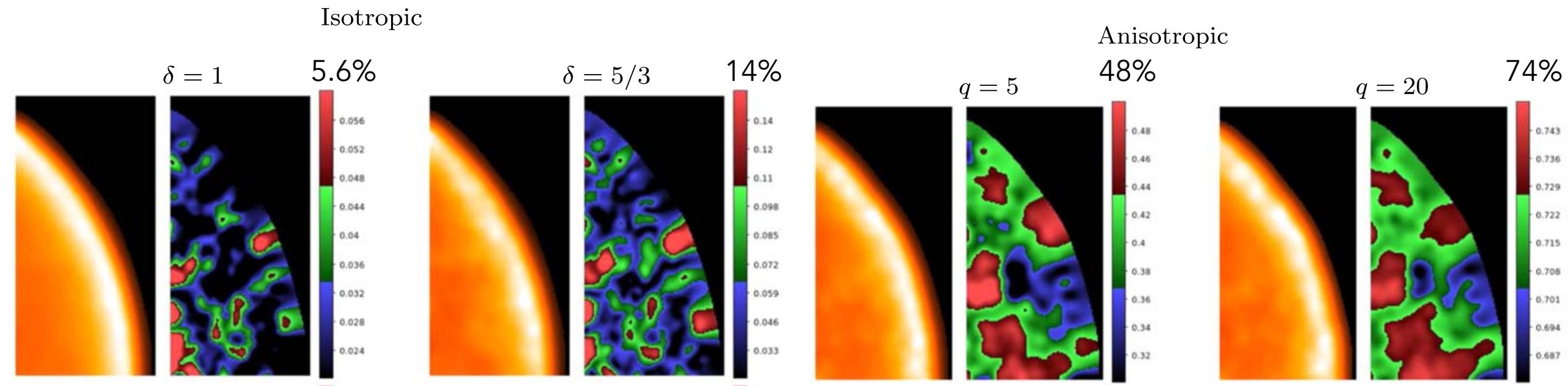


- For ideal detector estimator for Q and U :
 - $Q = \sum_i q_i = \sum_i 2 \cos(2\phi_i)$, $U = \sum_i q_i = \sum_i 2 \sin(2\phi_i)$
 - factor 2: needed as response $\propto \cos^2 \psi$ (not $\propto \cos \psi$)
- GPD detector: errors in measuring $\Phi \rightarrow$ degradation of polarization signal
- Degradation captured by “modulation curve” (μ): response to 100% polarized source
- IXPE optimum: ~ 3 keV (large μ , reasonable eff. area)

Naive expectations for IXPE observations young SNRs

- From radio observation: expect radial B-field!
 - *But:* at shock perpendicular field compressed: tangential B-field near shock?
 - Could radial magnetic field establish further away from shock?
- We need turbulence for DSA: polarization fraction low?
 - *But:*
 - B-field compressed: impinges a preferred B-field direction
 - Steep synchrotron spectrum in X-rays: intrinsically more highly polarized
 - Small filaments: less line of sight effects than in the radio
 - Turbulent field theories (e.g. Bell instability): apply to *upstream* magnetic field

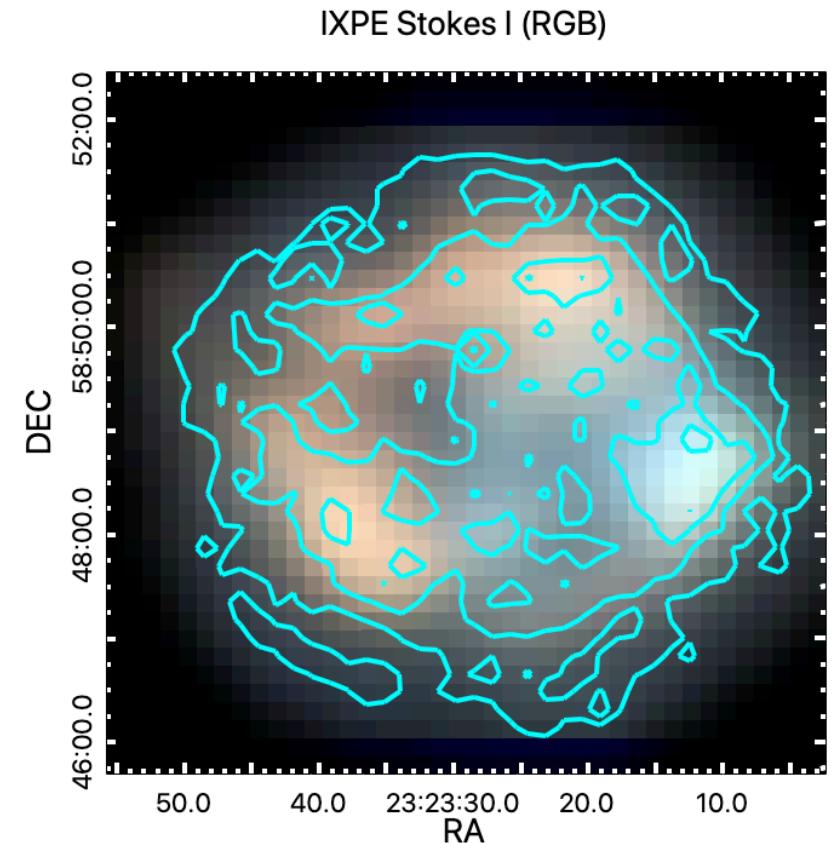
IXPE -like simulations Bykov et al. 2020



- Aimed at predictions for IXPE Tycho's observations
- Simulations assume either shock-compressed or isotropic B-field fluctuations
- Assumes turbulent spectrum $\delta B^2(k) \sim k^\delta$ ($\delta=1, 5/3$), with cutoff for $k^{-1} \sim 10^{18} \text{cm}$
 - For Cas A/Tycho $10^{18} \text{cm}: 20''$

Analysis of IXPE data

- Main SW tool: *ixpeobsim* (Baldini+ '21)
- Additional method: spectral polarimetry
 - Cas A, Tycho: account for thermal emission
 - Use of chi-square statistics:
 - $Q = \bar{\mu}^{-1} \sum_k q_k, \quad U = \bar{\mu}^{-1} \sum_k u_k$
 - Expectation values $E[Q]=0, E[U]=0$
 - Hence $S \equiv \frac{Q^2}{\text{Var}(Q)} + \frac{U^2}{\text{Var}(U)}$ has χ^2_2 distribution
 - Significances: $2\sigma: \chi^2 = 6.18, 3\sigma: \chi^2 = 11.8, 4\sigma: \chi^2 = 19.3$



X-ray spectroscopic analysis

- Per energy bin:

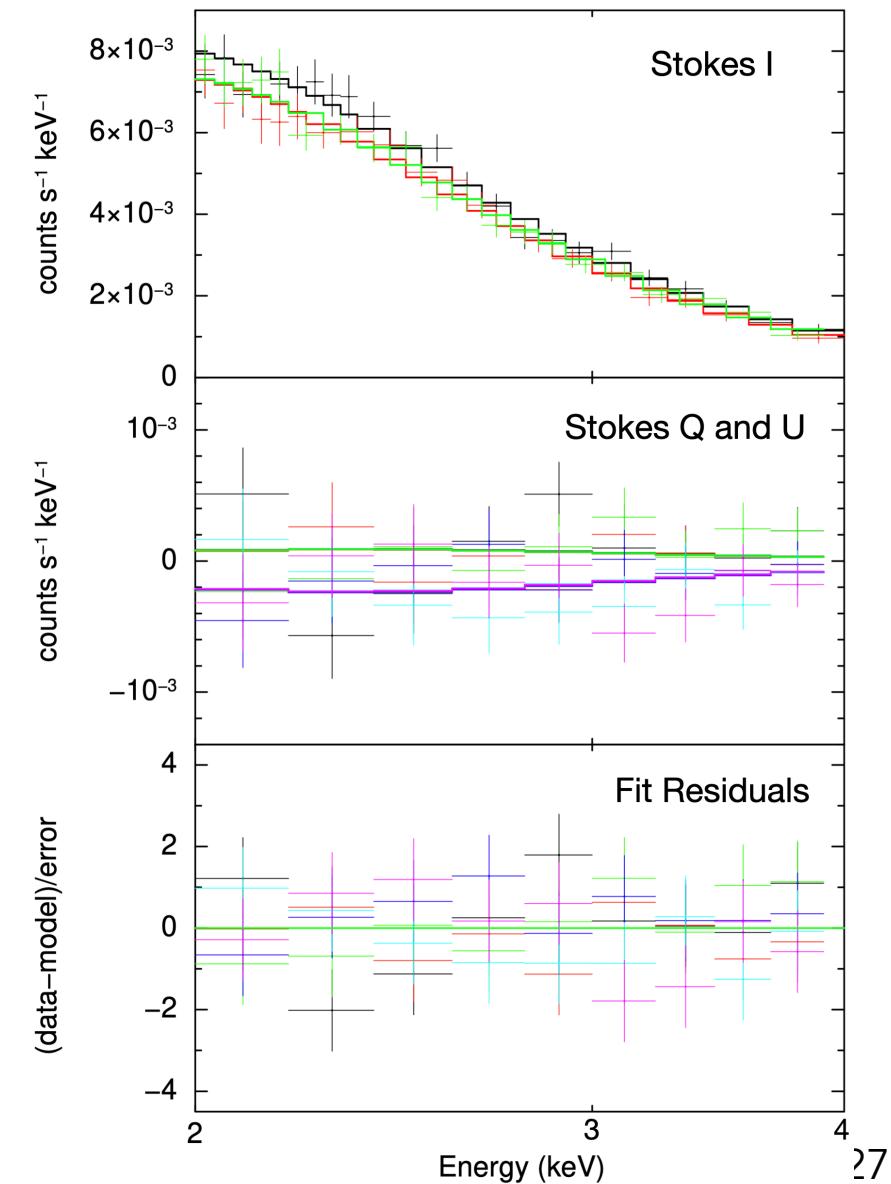
- $$Q(E_j) = \frac{1}{\sum_i w_i} \sum_i w_i q_i(E_j), \quad U(E_j) = \frac{1}{\sum_i w_i} \sum_i w_i u_i(E_j)$$

- Fit simultaneously I, Q, and U spectrum

- Forward folding:

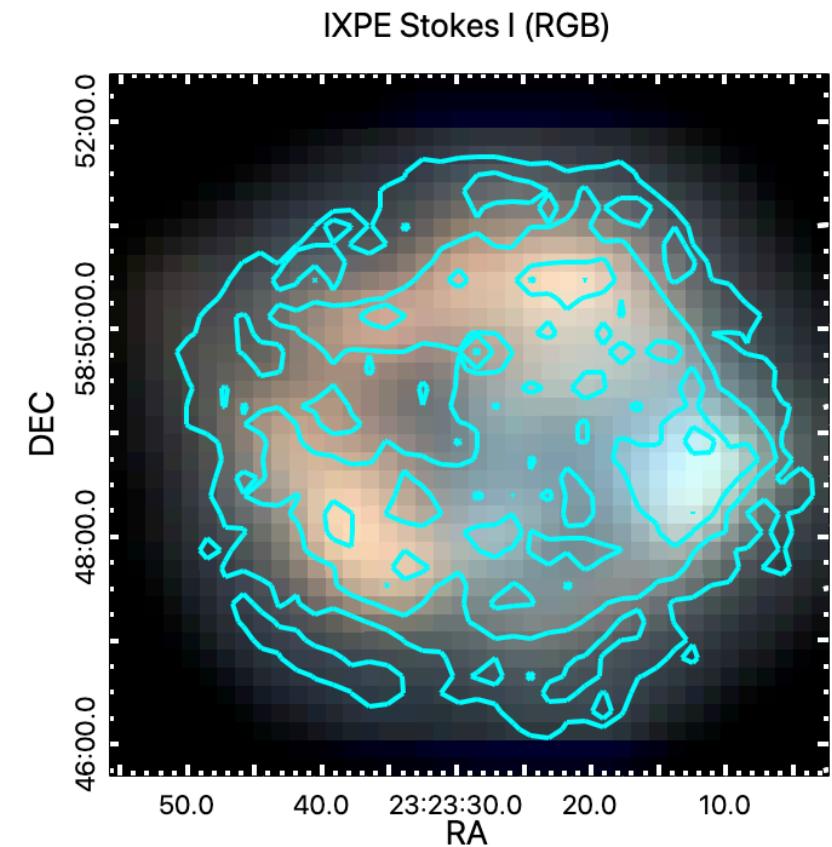
- instrumental modulation factor prescribed
- Polarization degree and angle: predict signal in Q, U spectra

- Big advantage over imaging technique:
 - Take care of thermal components and background

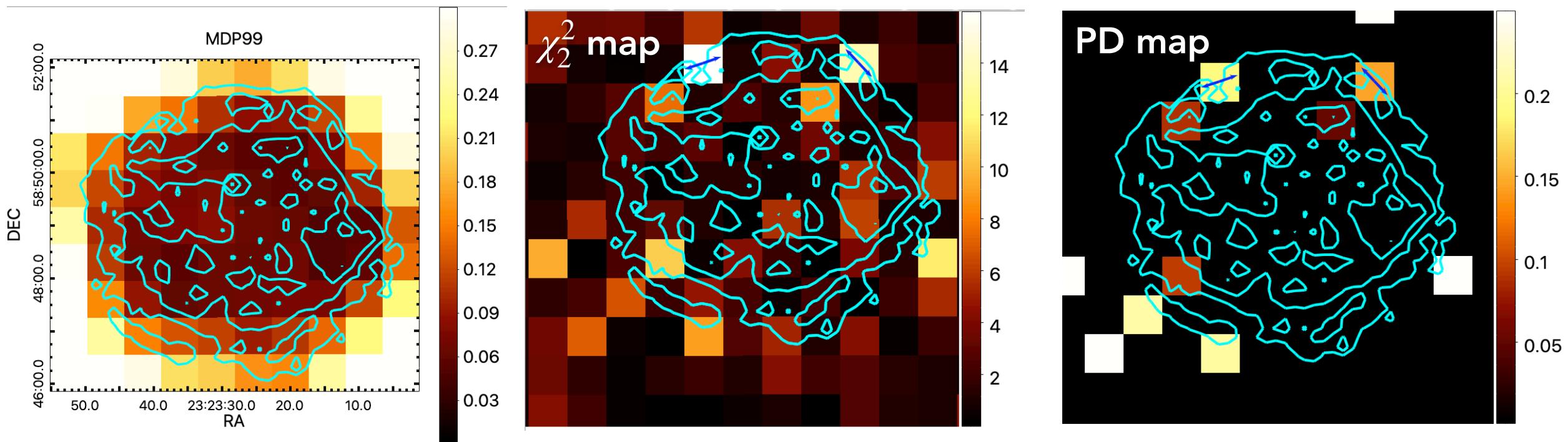


The IXPE observations of Cas A

- Youngest core collapse SNR (350 yr)
- Brightest radio source in sky
- Observations: January 11-29, 2022 (~900 ks)
- Initially some calibration/SW issues:
 - bending boom on orbital phase
 - corrected in released event list
 - remaining spurious offsets (removed by team)
 - 2.5' remaining WCS error (corrected for by team)
 - uncertainties about correctness u and q columns
 - PI/energy reconstruction imperfect (charge buildup) and det. unit dependent
- Effective exposure: 819 ks



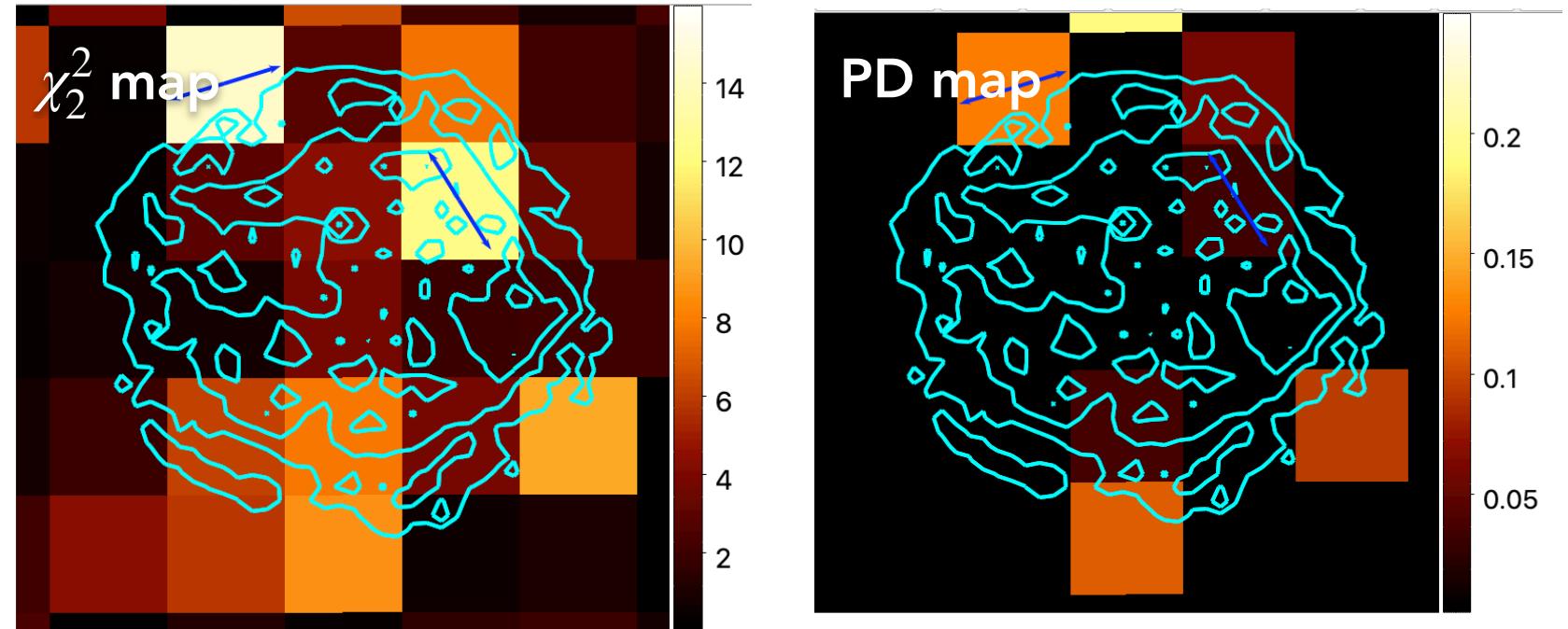
Pixel-by-pixel analysis



Vink+ 2022

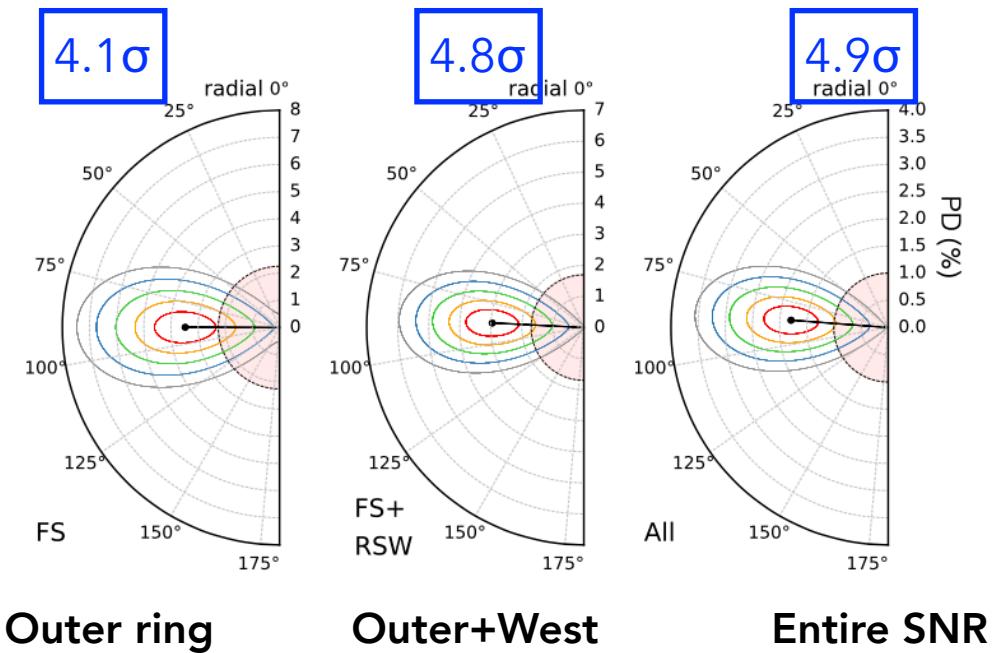
- MDP99 for Cas A (42" pixels): ~6—18% (3-6 keV)
- Typically two pixels at $>3\sigma$ ($\chi^2 > 11.8$) found, but position shifts for different binnings
- Cas A covered by ~200 resolution elements:
 - ~0.5 spurious signals at 3σ level expected \rightarrow hints for pol., no solid detections

Pixel-by-pixel analysis



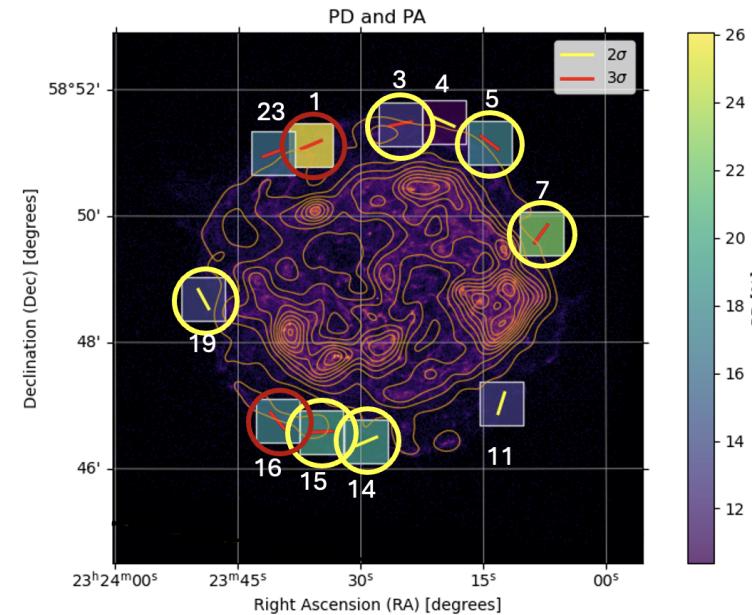
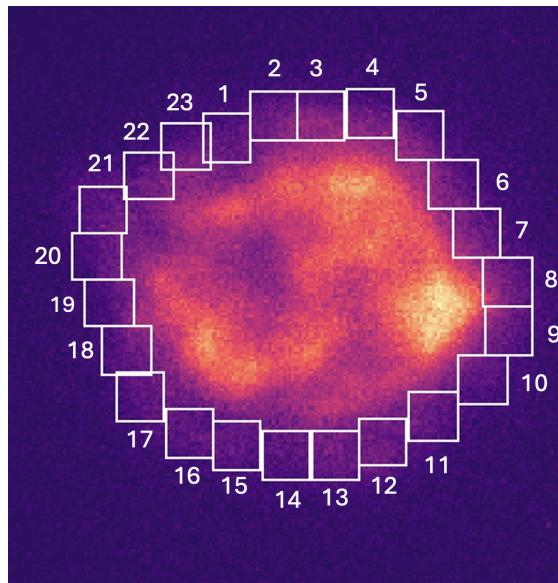
- Peaks in confidence: $\chi^2 \lesssim 15.9$ ($\lesssim 3.5\sigma$)
- Polarization degrees just above MDP99 levels: 4% to 19%
- Conclusion:
 - No solid detections
 - pol. fraction must be low: <4% for inner regions; <15—20% outskirts

Results assuming circular symmetry



- For the outer shock region and FS+W and All: detections at the $4\text{--}5\sigma$ level!
- The polarization degree is low: 2—3.5%
 - After correction for *thermal contamination*: 2.4—5%
- The polarization vectors indicate a tangential direction: radial magnetic field!
 - Similar/lower pol. frac than radio
 - *Radial magnetic fields already at 10^{17} cm from shock!*

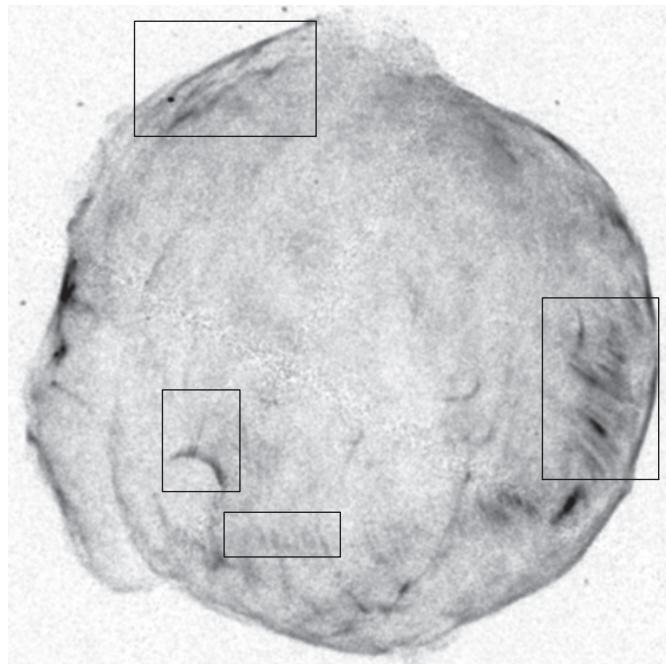
Reanalysis Cas A data using spectroscopic polarization



Mercuri, Greco, Vink, Ferrazzoli, Perri, 202

- Uses spectroscopy with I, Q & U spectra
- Automatically corrects for thermal emission (but with poor spectral resolution)
- Finds 3-4sigma detections at outskirts with PD \sim 11-26%

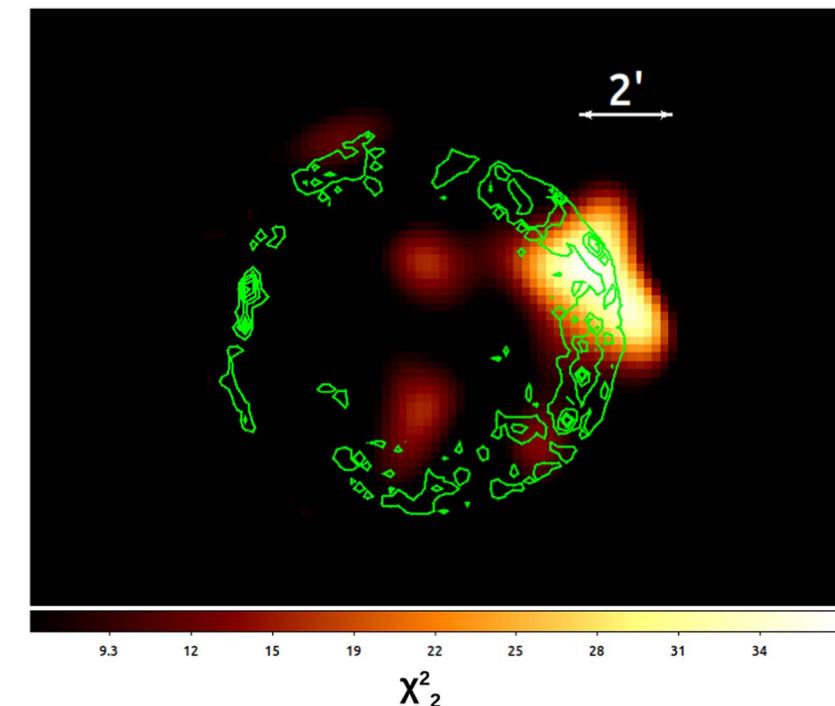
Tycho's SNR/SN1572



Eriksen+ 2011



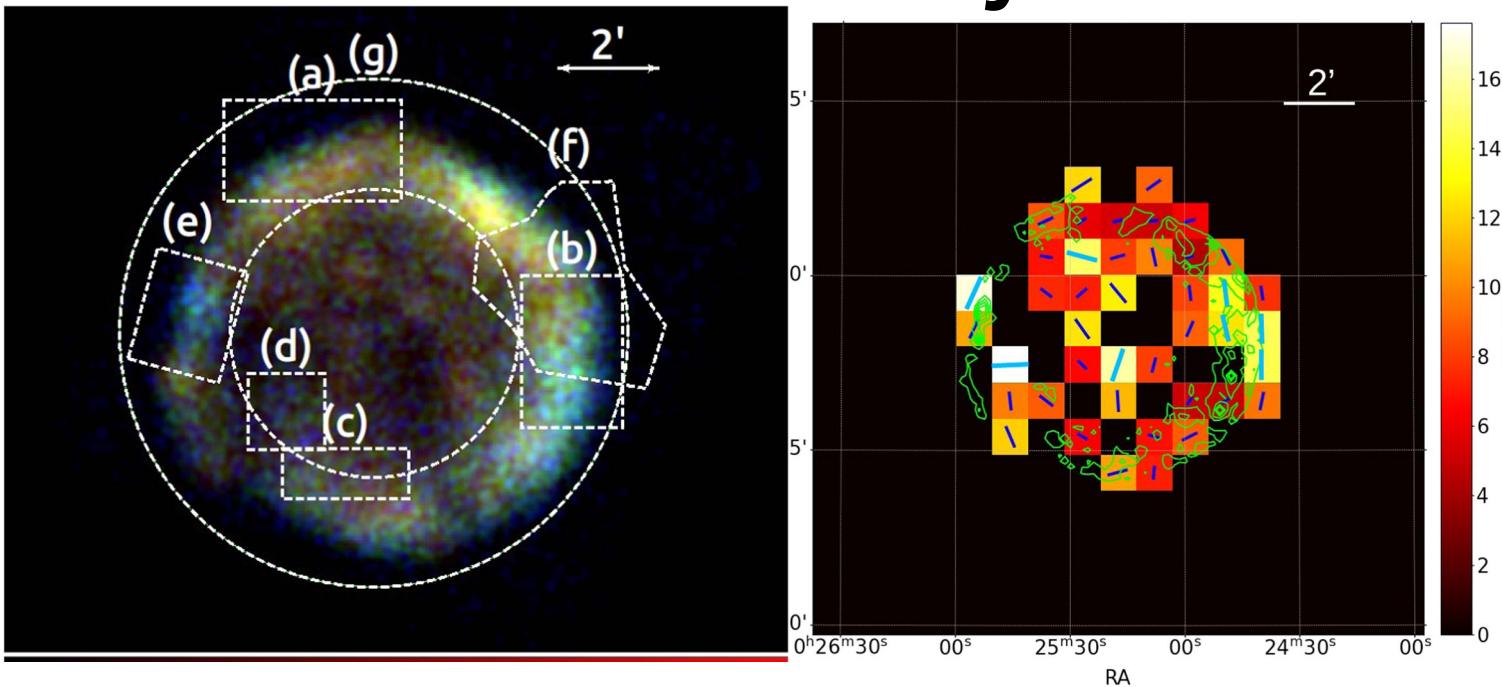
Tycho's stripes!



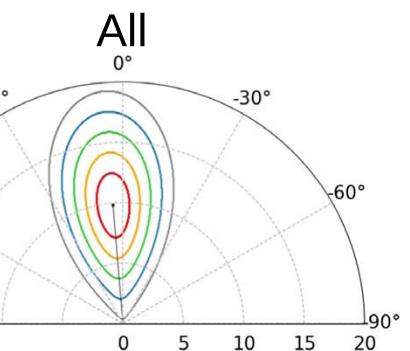
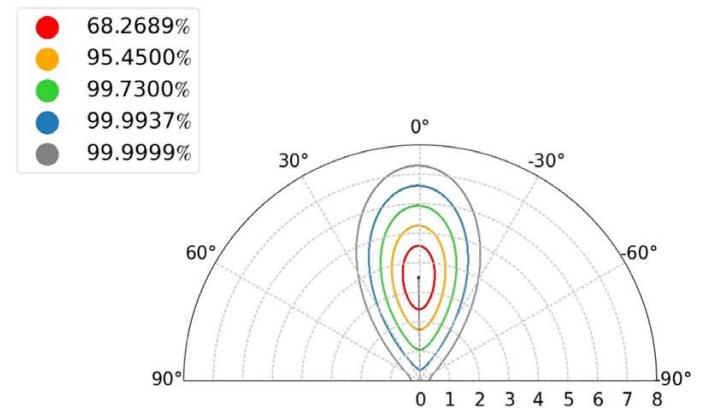
Ferrazzoli+ 2023

- Like Cas A: narrow rims, indicating $B \sim 200 \mu G$
- Special mysterious structures: Tycho's stripes!
 - Is it a magnetic-field pattern → expect high polarization fraction!

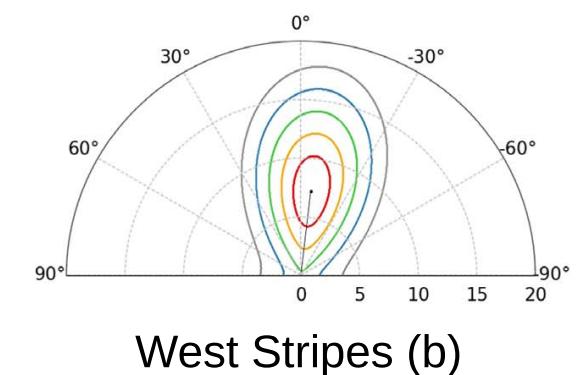
Tycho's SNR/SN1572 IXPE results



Ferrazzoli+ 2023



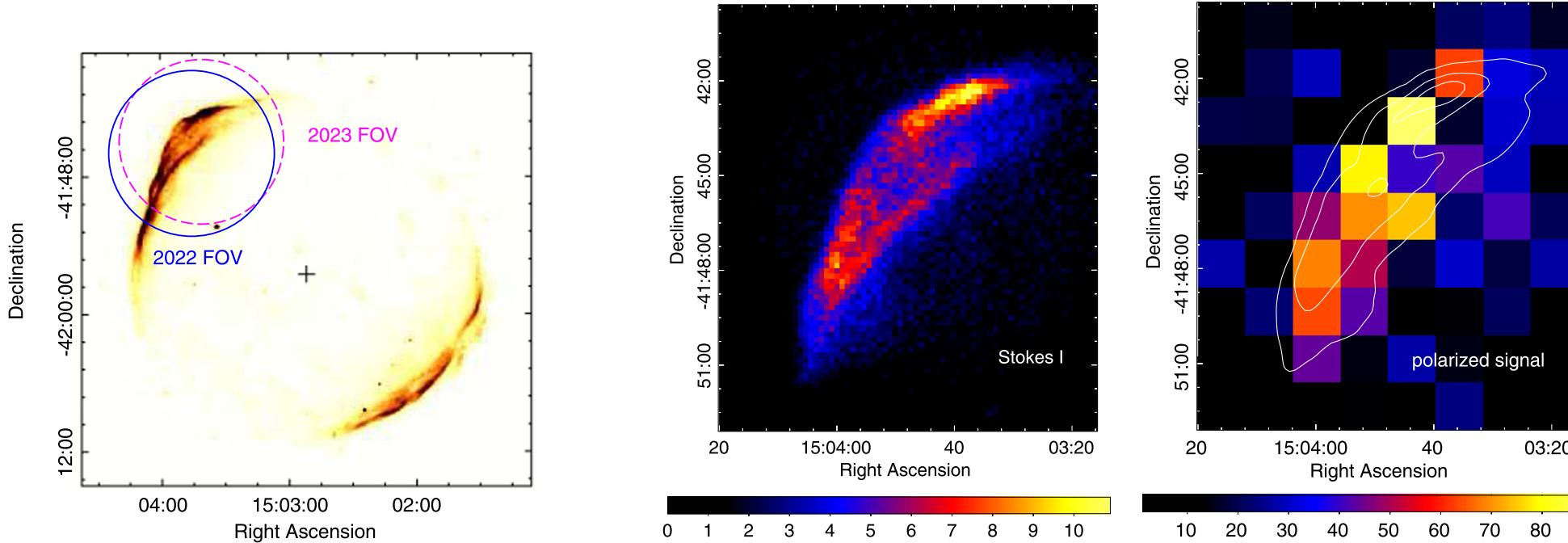
Stripes, Chi2 (f)



West Stripes (b)

- PD corrected:
 - All: 9%; rim: 12%; f: 10% (all $>5\sigma$); b: 7.3% (3.7 σ)
- B-field orientation: *radial!*
- *Stripes, don't stand out: PD=7%, 3.7 σ , radial B-field*

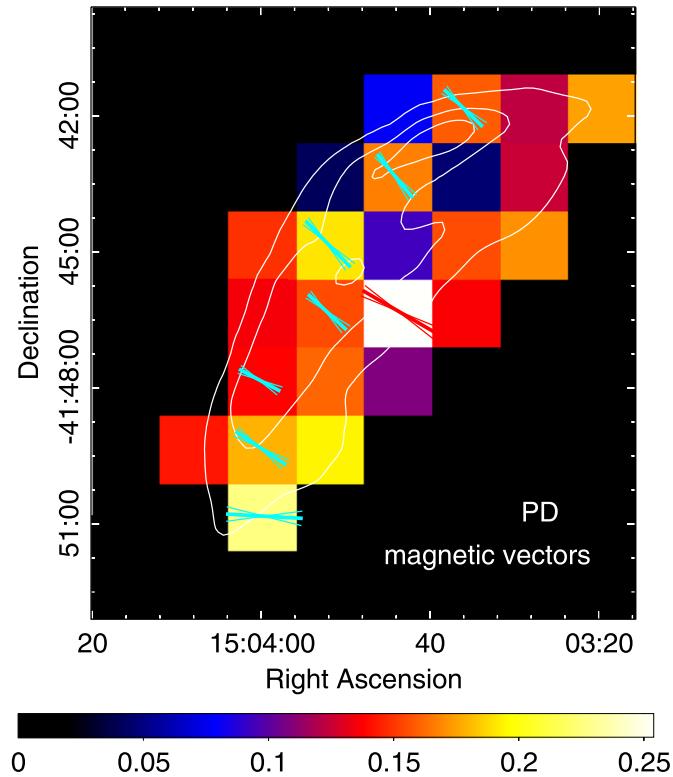
SN1006



Zhou+ 2023

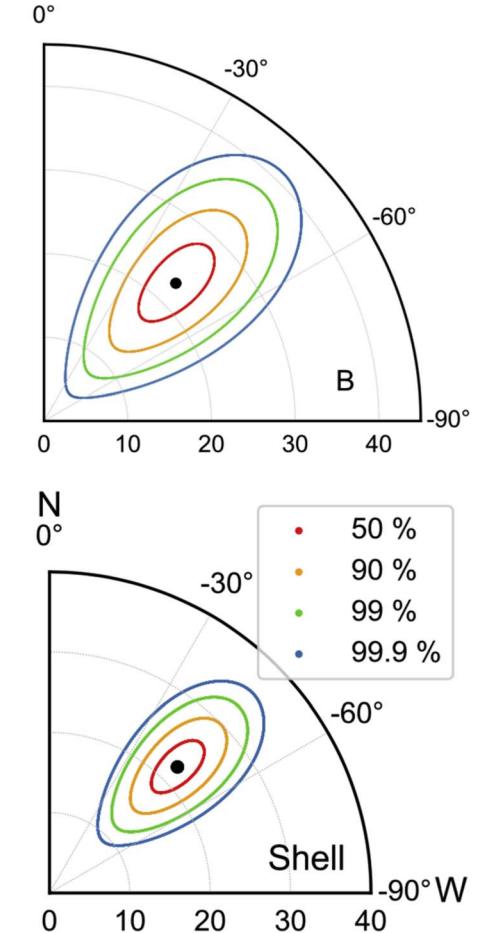
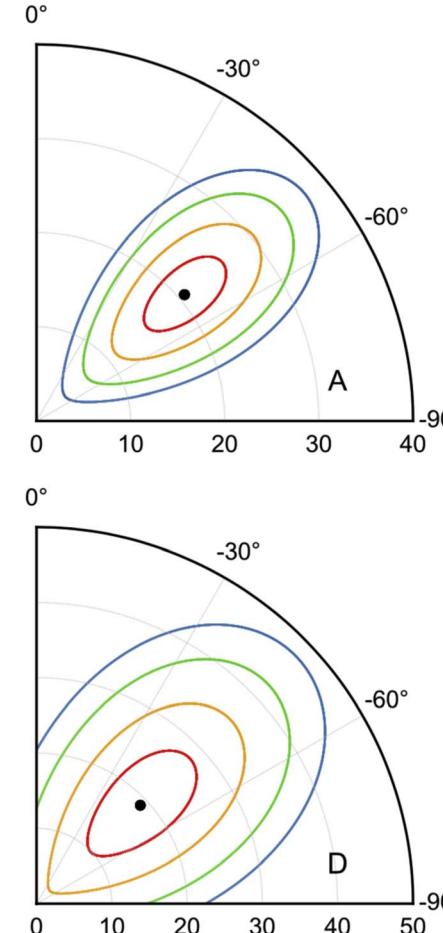
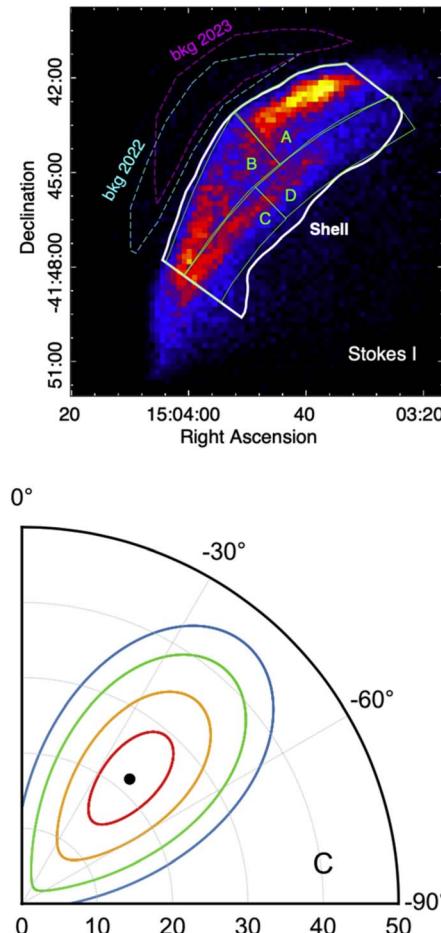
- SN1006 is first SNR for which X-ray synchrotron was discovered (Koyama+ 95)
- Large shell (30'): targetted NE rim
- NE rim: synchrotron dominated (no thermal emission)
- Synchrotron width relatively large: $B \sim 80 \mu G$

SN1006 IXPE results

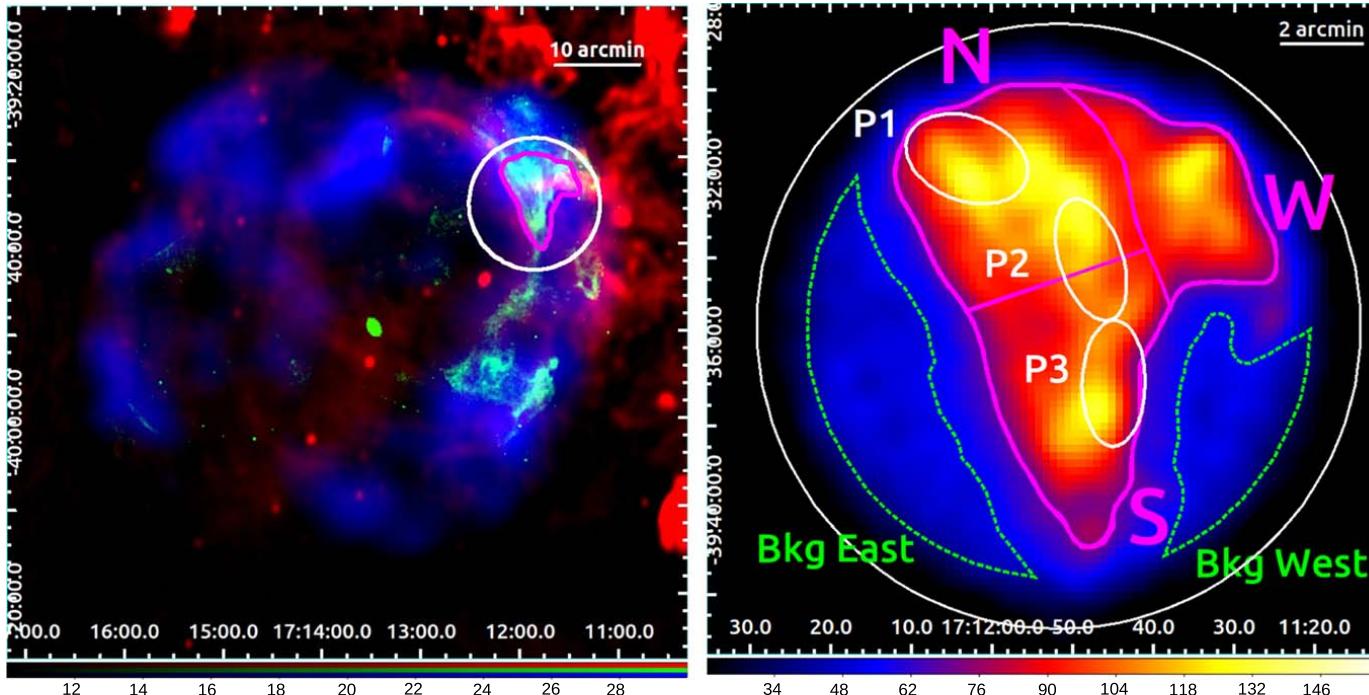


Zhou+ 2023

- Pol. degree: $\sim 22\%$
- B-field orientation: radial
- PD larger than in the radio ($\sim 13\%$)!



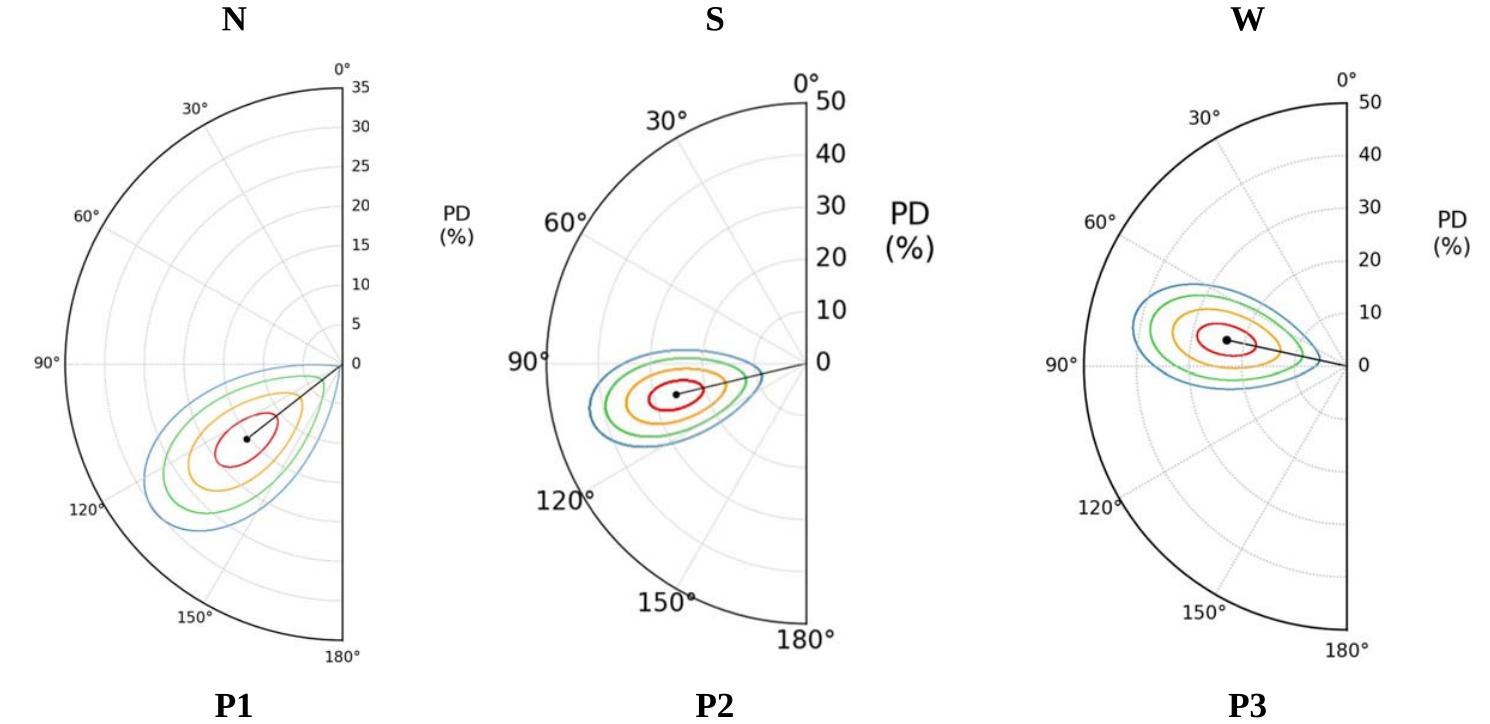
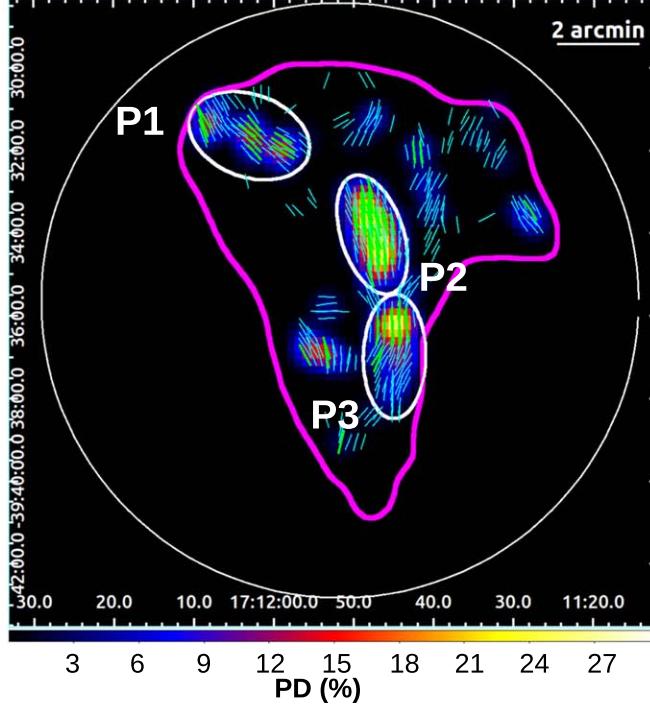
RX J1713.7–3946



Ferrazzoli+ 2024

- Very large shell: 1 degree
- Nearby: 1 kpc
- No or very weak thermal X-rays
- Wide X-ray synchrotron region: $B \sim 10 - 30 \mu G$
- Faint in radio -> *no reliable radio polarization!*

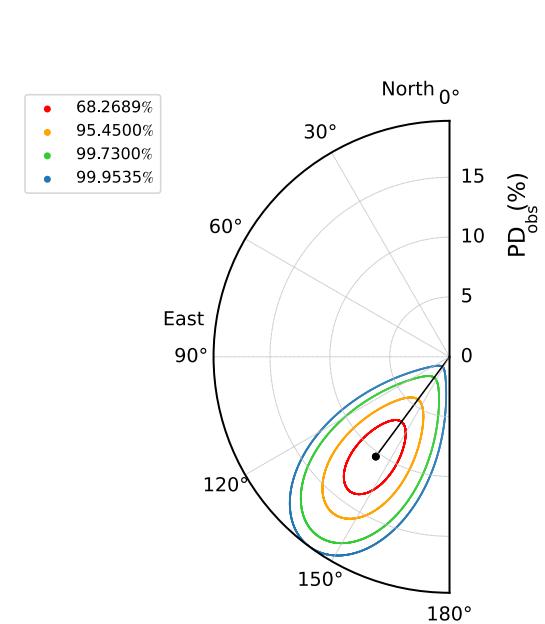
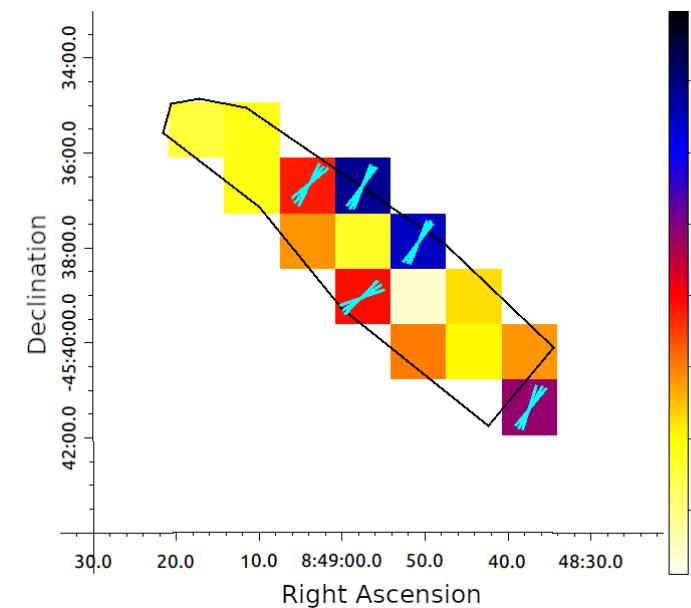
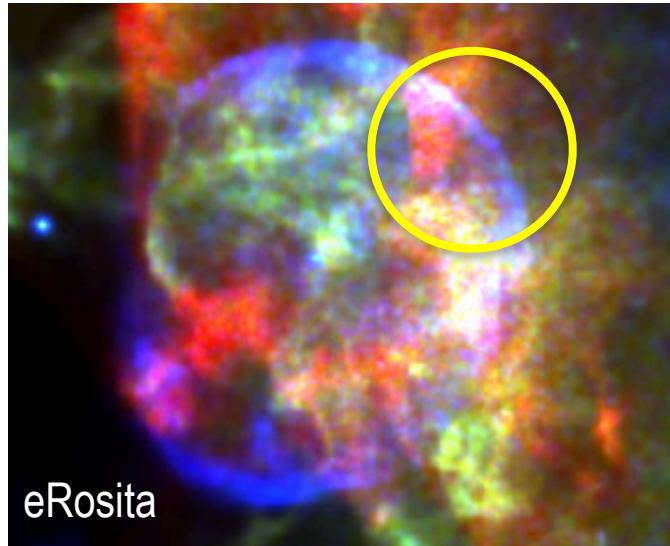
Surprising result RX J1713.7–3946: tangential field!



Ferrazzoli+ 2024

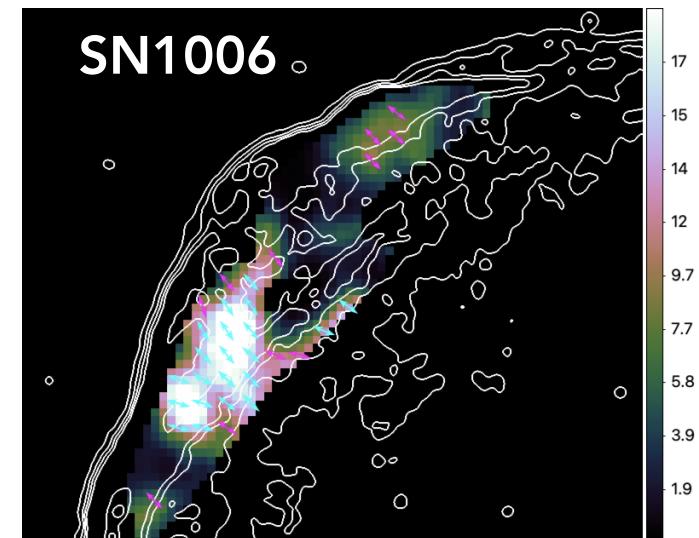
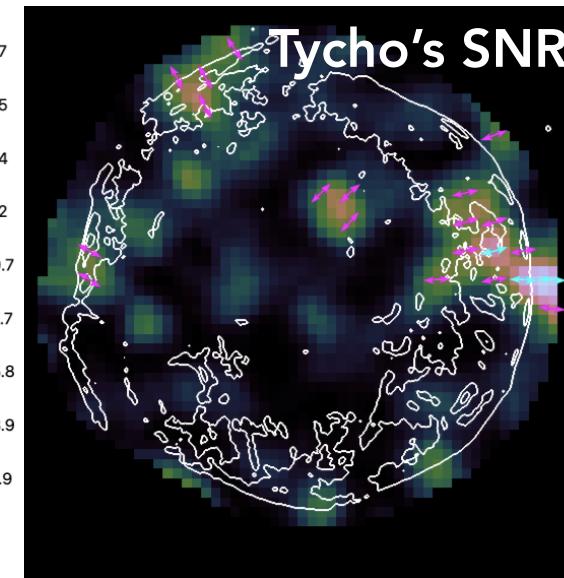
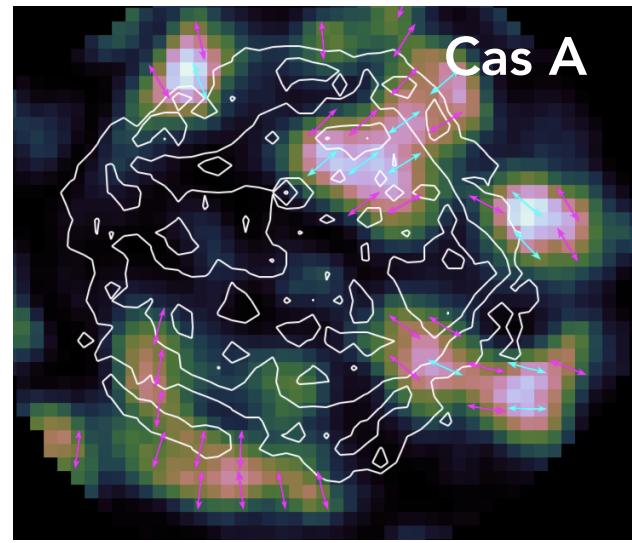
- Pol. fraction (spectral fits): 26-37%
- B-field orientation: *tangential!*
- Highest pol. fraction: very close to shock
 - reorientation/turbulence further downstream?

Vela Jr/RXJ0852.0–4622 (G266.2–1.2)

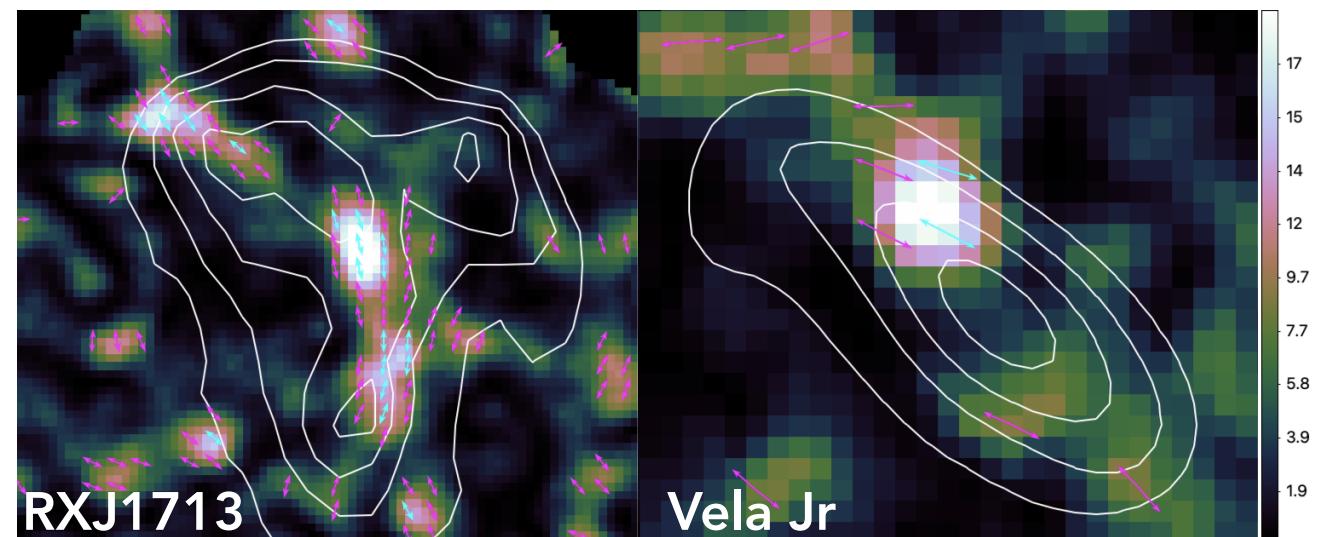


- Large shell: 2 degree, on top of Vela SNR
- B-field estimate (H.E.S.S.): $B_2 \approx 10 \mu\text{G}$
- Probably oldest SNR (~ 3000 yr) with X-ray synchrotron:
 - requires evolution in low density bubble
- IXPE:
 - B- field is *tangential* (like RXJ1713)!
 - $\text{PD} \approx 16 \pm 5\%$

IXPE Statistical maps (χ^2_2)



- $\sim 4\text{-}5\sigma$ detection of polarization
- correct for thermal contributions
- Cas A: only after some tricks:
 - entire SNR only
 - 5% pol. degree
 - high downstream turbulence



Summary PD and orientations

	Age (yr)	B field	P.D.	Orientation B-field	Ref.
Cas A	~350	~250 μ G	~5%	radial	Vink+ '22
Tycho	452	~200 μ G	~10%	radial	Ferrazzoli+ '23
SN1006	1018	~30-80 μ G	~20%	radial	Zhou+ '23
RX J1713	~1500	~20 μ G	26%—30%	tangential	Ferrazzoli+ '24
Vela Jr	~3000	~10 μ G	10%—20%	tangential	Prokhorov+ '24

- Radial vs tangential: age (or B-field?) dependence in X-rays
- PD low (5-30%)/high B turbulence
- Note: turbulence must be high enough to allow X-ray synchrotron (i.e. $\eta \approx 1$)
 - But: low B \rightarrow long cooling time
 - for RX J1713/Vela jr turbulence for acceleration may be in the past

Turbulence & geometry

- B-field turbulence generated by cosmic rays not resolved by IXPE
 - $\sim 10^{16} - 10^{17}$ cm for Bell instability
 - $\sim 10^{15}$ cm for resonant instability (=gyroradius 10 TeV particles, $B=100 \mu\text{G}$)
 - Turbulence at these scales needed for X-ray synchrotron → but not resolved!
 - Bykov+ '20 simulations assumed spectrum up to 10^{18} cm → (barely) resolvable
 - Shock compression: imposes preferential, tangential, B-field direction
 - Need to stretch and possibly renew turbulence downstream
- Geometry:
 - Most likely B-field stretching: clumps + Richtmeyer-Meshkov (Innoue+ 13)
 - Competing model by West+ 17 unlikely for X-rays!
 - Bykov+ '24: clumping associated with upstream Bell instability!
 - Bell scales with density and shock velocity

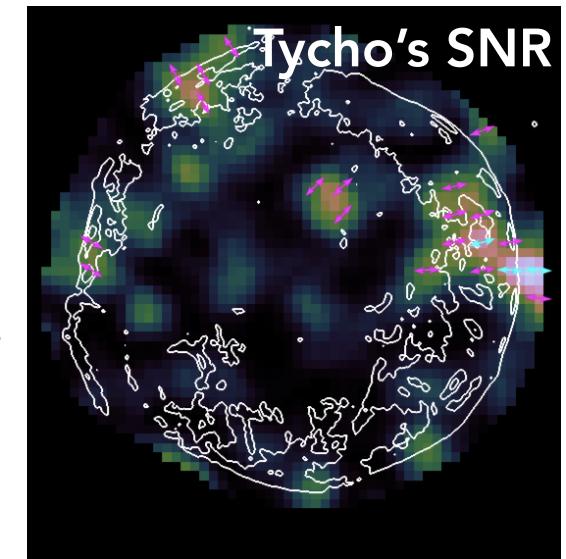
Final suggestion

- X-ray synchrotron provide evidence for Bell magnetic-field amplification
 - Suggests turbulent magnetic field
 - And $B^2 = K\rho V_s^2$ or $K\rho V_s^3$
 - But for low density, lower shock velocities $B_{\text{Bell}} \approx B_0$
 - Largest polarisation fraction: RXJ1713 and SN 1006 → lowest ρ and B
 - Normalizing to Cas A ($n_H \sim 2 \text{ cm}^{-3}$, $V_s = 6000 \text{ km/s}$): $K=0.15\%$
 - For what density and $V_s = 3000 \text{ km/s}$ is $B_{\text{Bell}} \approx B_0 \approx 20 \mu\text{G}$?
 - Answer: $n_H \sim 0.05 \text{ cm}^{-3}$ comparable to RX J1713, Vela jr!
 - *But still need sufficient turbulence for acceleration!*

Possibility: magnetic fields become tangential when Bell amplification (B_{Bell}) is subdominant compared to pre-existing magnetic-field strength (B_0)!

Summary

- A new window on SNRs has opened: X-ray polarimetry with IXPE
- Target young SNRs:
 - X-ray synchrotron emission associated with the shock regions
 - X-ray synchrotron → requires $V_s > 3000$ km/s and turbulent (*upstream?*) fields
 - Evidence for magnetic-field amplification (Bell 2004)
- IXPE results:
 - Low pol. fraction: 5-30% → requires *downstream* turbulence
 - Radial magnetic fields → stretching field lines starts at shock front
 - Exceptions: RXJ1713 and Vela Jr, both have relatively low B-fields
- Not yet fully understood:
 - Why sometimes radial B-fields close to shock?
 - What generates downstream turbulence? -> theory mostly concentrates on upstream mechanisms (Bell instability)
 - RXJ1713/Vela jr: low B-fields, more CSM/Galactic fields?
 - but X-ray synchrotron requires turbulence!

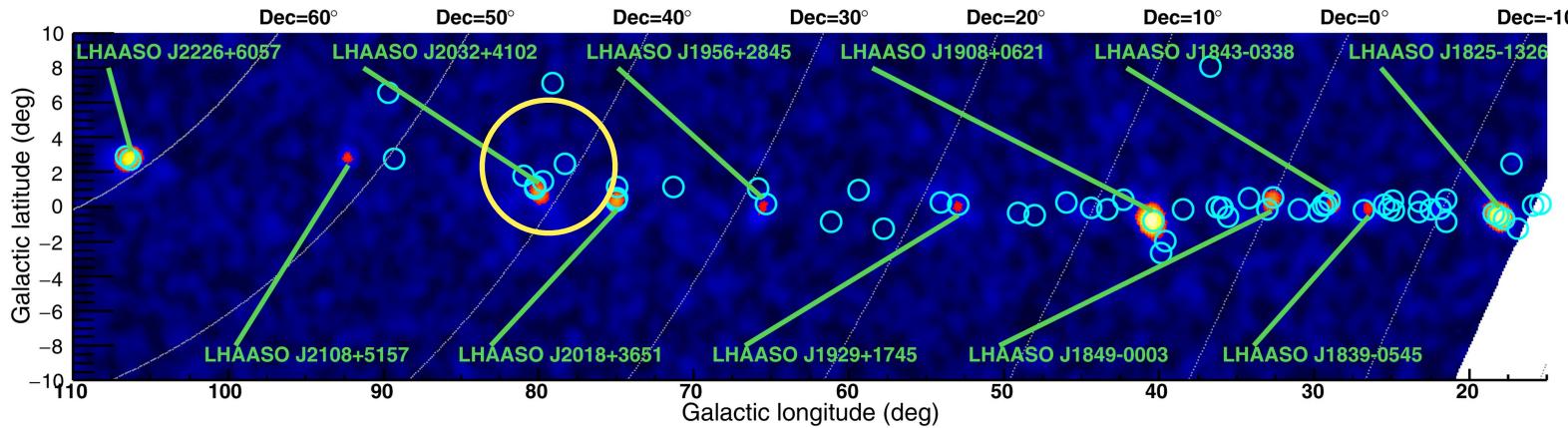


Ferrazzoli+ 2023

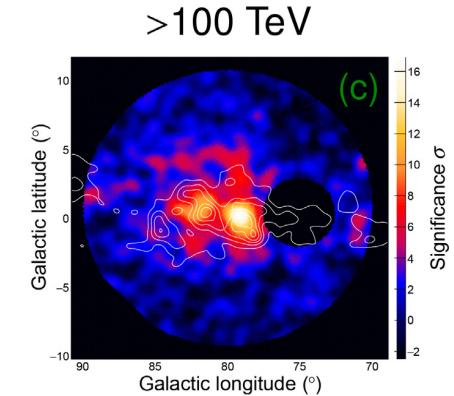


Part II: Can stochastic acceleration create PeVatrons

LHAASO PeVatrons: 100-1400 TeV sources



LHAASO coll, Nat. '21

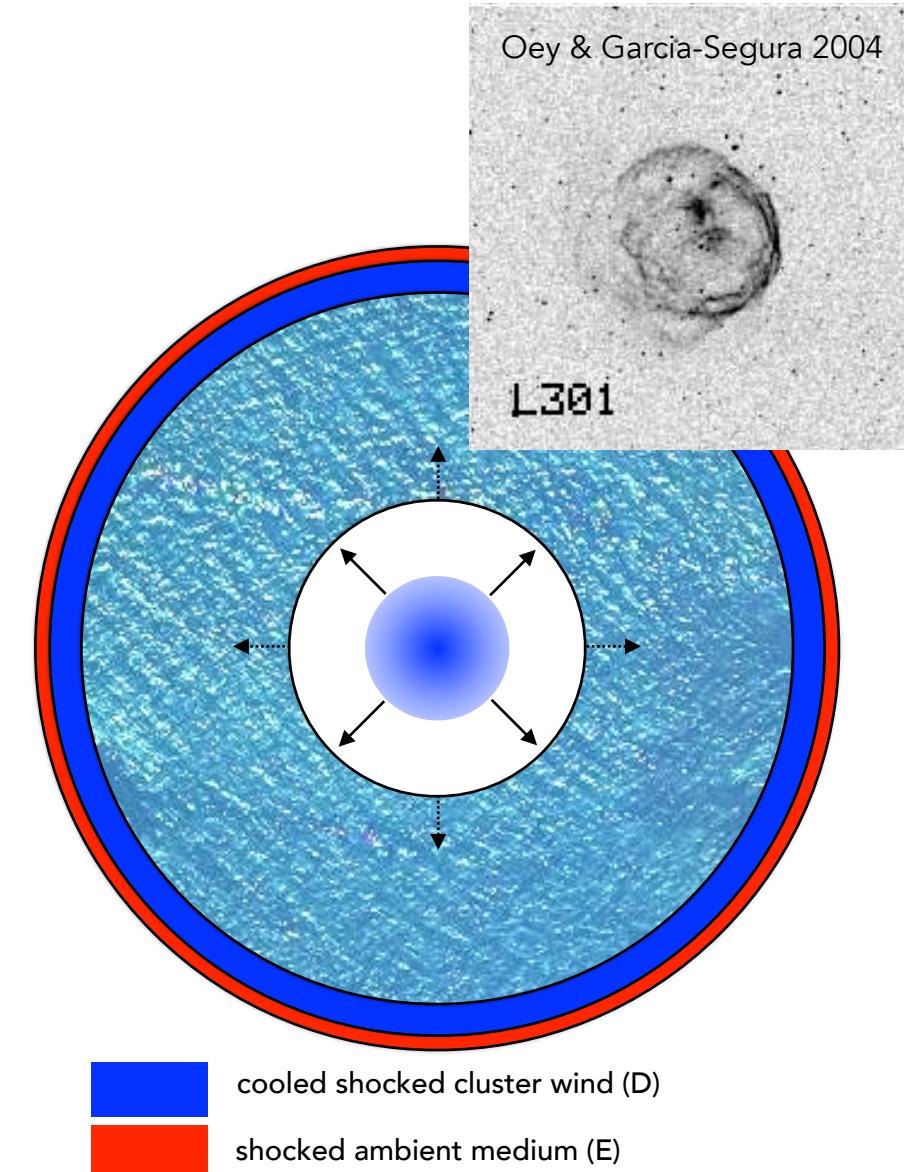


Cygnus Bubble: LHAASO coll, Sc. Bull. '24

- SNe can explain CR power, but not the CR "knee"! -> Where/what are the PeVatrons?
- LHAASO detected PeV photons! -> PeVatron case solved?
- The situation is still complicated:
 - Many sources are pulsars → do not (?) accelerate protons, but leptons
 - LHAASO PSF is poor: multiple source within PSF → which (if any) is the true PeVatron?
- One source may provide a hint: the Cygnus OB2 association/Cygnus Bubble
 - Combined effects SNe & Stellar winds? (Bykov & Toptygin '92, Parizot+ '04, Vieu+ '22-24)

Could superbubbles be the major sites of Galactic Cosmic Rays?

- Superbubbles are the giant bubbles (>40—200 pc) created by young massive clusters
- Bubble energized by
 - stellar winds (up to 3000 km/s)
 - main power for $t \leq 4$ Myr
 - supernovae (dominates lifetime budget)
- Long history of being considered important for CR acceleration (Montmerle c.s., Bykov, Parizot c.s.)
- Questions:
 - Are there collective effects?
 - And if so: can they be PeVatrons? And how?



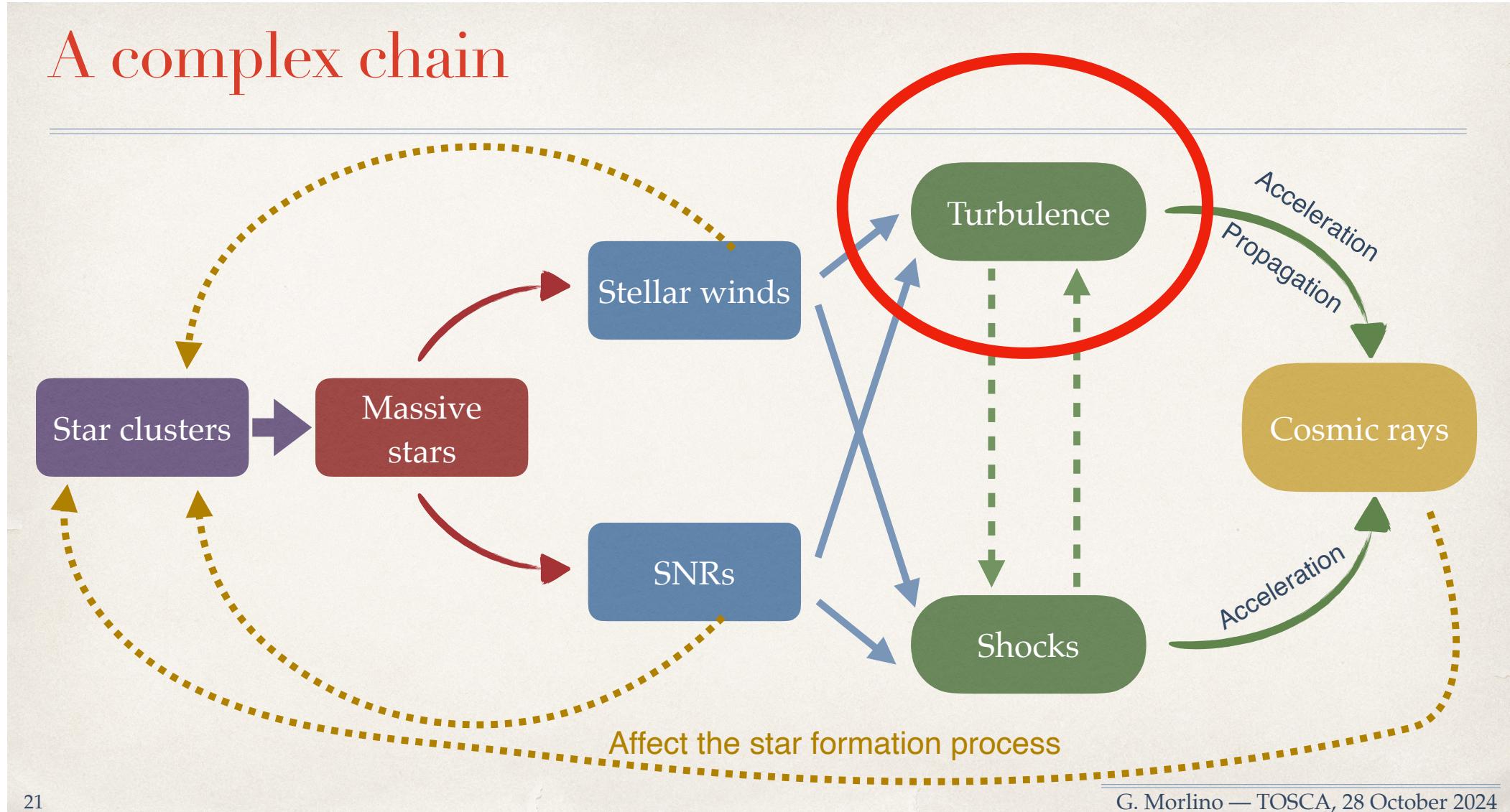
Superbubbles as (PeV) sources of cosmic rays

- SNRs appear *not* to be PeVatrons
 - Observationally/theoretically $E_{\max} \lesssim 10^{14}$ eV
 - But: SNe/SNRs perhaps PeVatrons early on? (if dense winds)
 - Or in special environments (*superbubbles*?!)
- Details in cosmic ray composition favor a wind-enriched environment
- SBs: Just many individual sources or collective phenomena?
 - *Is the whole more than the sum of the individual parts?*
- Collective SB phenomena:
 - Multiple shocks (winds/snrs) keep interacting and accelerating particles (e.g. Bykov)
 - Long-lived and fast (2000 km/s) cluster wind termination shock
 - This talk: second order Fermi acceleration by magnetic field turbulence

Superbubbles: are they more than the sum of their parts?

Sketch courtesy of G. Morlino

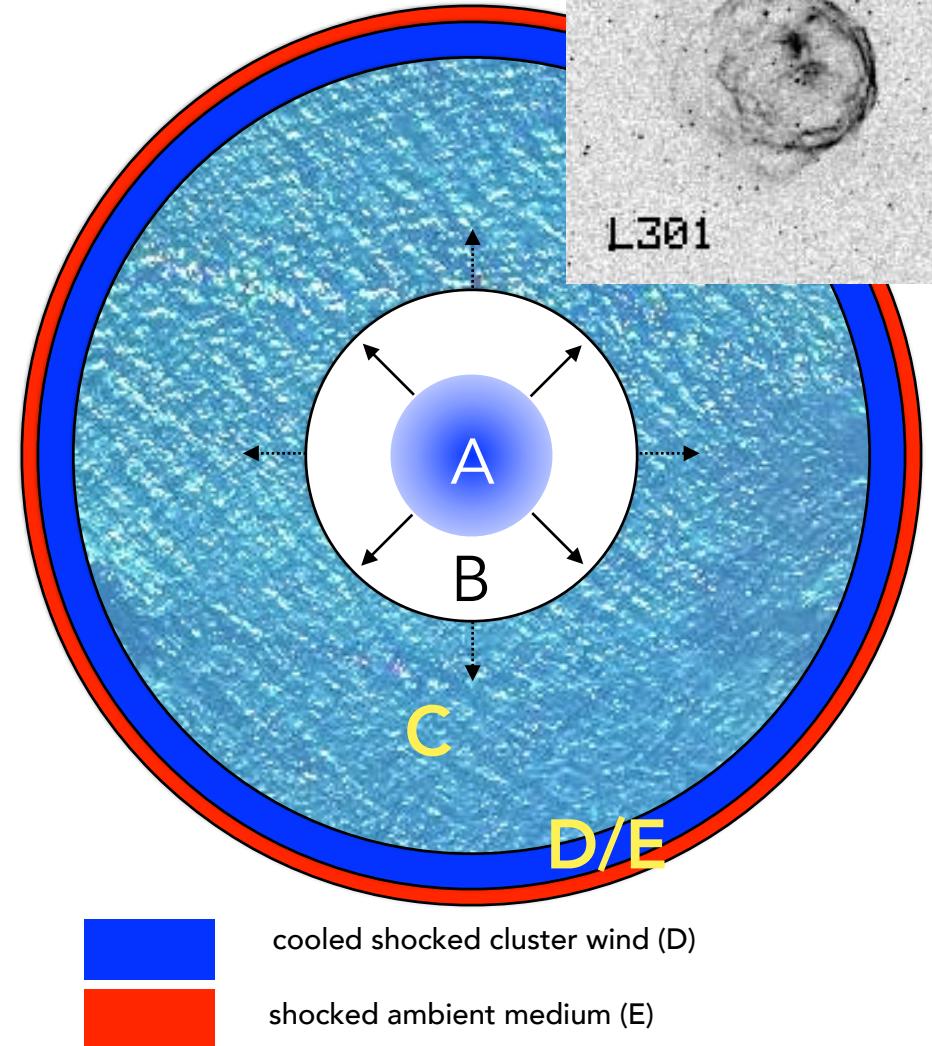
A complex chain



Superbubbles

Oey & Garcia-Segura 2004

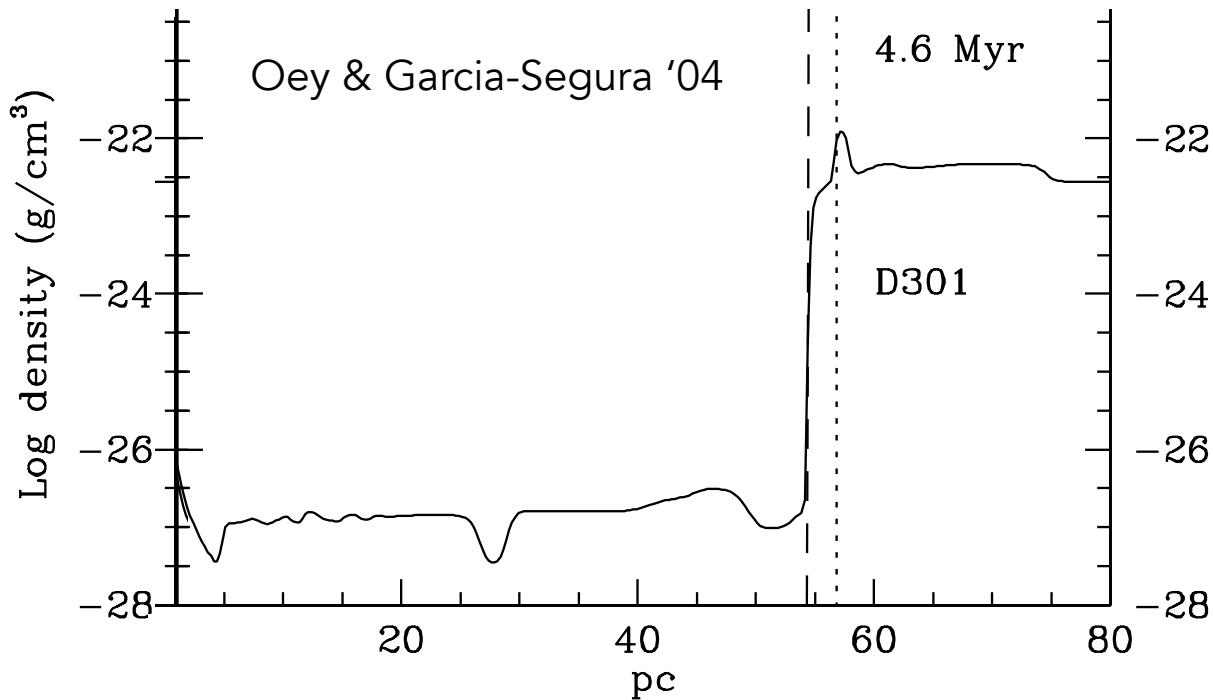
- Several options for CR acceleration:
 - Cluster itself: colliding winds (A)
 - DSA
 - Termination shock cluster wind (boundary B/C)
 - DSA
 - Inside tenuous superbubble ©
 - Stochastic/2nd order Fermi
 - Occasional supernova remnant in (mostly in C)
 - e.g. 30DorC (H.E.S.S. '15, Kavanagh+ '19)
- All may contribute!
 - But which is responsible for PeV CRs?
- Region D/E could be site of (hadronic) gamma-rays
 - (bombarded by CRs from A,B,C)



cooled shocked cluster wind (D)
shocked ambient medium (E)

Superbubble

- Models predict 100-200 pc (Weaver+ '77)
- But typical sizes LMC: 50 pc
 - Likely cause: ISM pressure locally high (Oey & Garcia Segura '04)
- Superbubble itself: could be very low density!
 - $\rho \approx 10^{-27} - 10^{-26} \text{ g cm}^{-3}$ ($n_{\text{H}} \sim 0.0005 - 0.005 \text{ cm}^{-3}$)
 - expected Alfvén speed: $V_{\text{A}} = \frac{B}{\sqrt{4\pi\rho}} \approx 585 \left(\frac{B}{10 \text{ }\mu\text{G}} \right) \left(\frac{n_{\text{H}}}{0.001 \text{ cm}^{-3}} \right)^{-1/2} \text{ km/s}$
- SB surrounding shell: $n_{\text{H}} \sim 1 - 100 \text{ cm}^{-3}$



Second-order shock acceleration inside SB

- Fermi's (1948) original idea
 - Particles scatter off moving magnetic irregularities (Alfvén waves) → gain or lose energy
 - On average gain: $\frac{\Delta E}{E} = \xi \left(\frac{V_A}{c} \right)^2$ ($\xi \sim 1$)
 - Space diffusion also based on scattering: $D = \frac{1}{3} \lambda_{\text{mfp}} c \rightarrow \Delta t = \frac{\lambda_{\text{mfp}}}{c} = \frac{3D}{c^2}$
 - Assume $D = D_0 \left(\frac{E}{E_0} \right)^\delta$ (ISM $\delta \approx 0.3-0.7$; Bohm diffusion $\delta \approx 1$)
 - Rate of energy gain: $\frac{1}{E} \frac{dE}{dt} \approx \frac{1}{E} \frac{\Delta E}{\Delta t} = \xi \frac{1}{3D_0} \left(\frac{E}{E_0} \right)^{-\delta} V_A^2$

NB connection acceleration-diffusion often expressed as

$$D_{xx} D_{pp} = \frac{1}{9} p^2 V_A^2 \text{ (e.g. Thornbury & Drury, 2014)}$$

Remarkable: Fermi-2 as efficient as Fermi-1?

- Expression for maximum energy: $E_{\max} = \left[E_{\text{inj}}^\delta + \frac{\delta\xi}{3D_0} V_A^2 E_0^\delta t \right]^{1/\delta}$
- 2nd order Fermi acceleration time scale: $\tau_{\text{acc,2nd}} \approx \frac{3D_0}{\delta\xi V_A^2} \left(\frac{E_{\max}}{E_0} \right)^\delta = \frac{3D(E_{\max})}{\delta\xi V_A^2}$
- 1st order Fermi acceleration time scale: $\tau_{\text{acc,1st}} \approx \frac{8D_0}{\delta V_s^2} \left(\frac{E_{\max}}{E_0} \right)^\delta = \frac{8D(E_{\max})}{\delta V_s^2}$
- For relevant velocities 1st and 2nd order Fermi have similar timescales!
- In reality: SNRs can have $V \sim 5000$ km/s, Alfvén speed is rarely that high!
- NB: a similar equation was derived by Thornbury&Drury (2014)
- Their conclusion: Fermi-2 not important for ISM ($V_A \sim 10 - 30$ km/s)

Maximum energy taking into account escape

- High energies particles leak away due to diffusion, limits E_{\max} :

- $R = \sqrt{6Dt} \rightarrow \tau_{\text{esc}} = \frac{R^2}{6D}$

- $\tau_{\text{acc}} \approx \tau_{\text{esc}}$, $D = \frac{1}{3}\lambda_{\text{mfp}}c = \frac{1}{3}\eta \frac{cE}{eB}$:

$$E_{\max} = 5.5 \times 10^{14} \eta^{-1} \sqrt{\delta\xi} \left(\frac{B}{10 \text{ }\mu\text{G}} \right) \left(\frac{R}{50 \text{ pc}} \right) \left(\frac{V_A}{500 \text{ km s}^{-1}} \right) \text{ eV}$$

- or using $V_A = \frac{B}{\sqrt{4\pi\rho}}$:

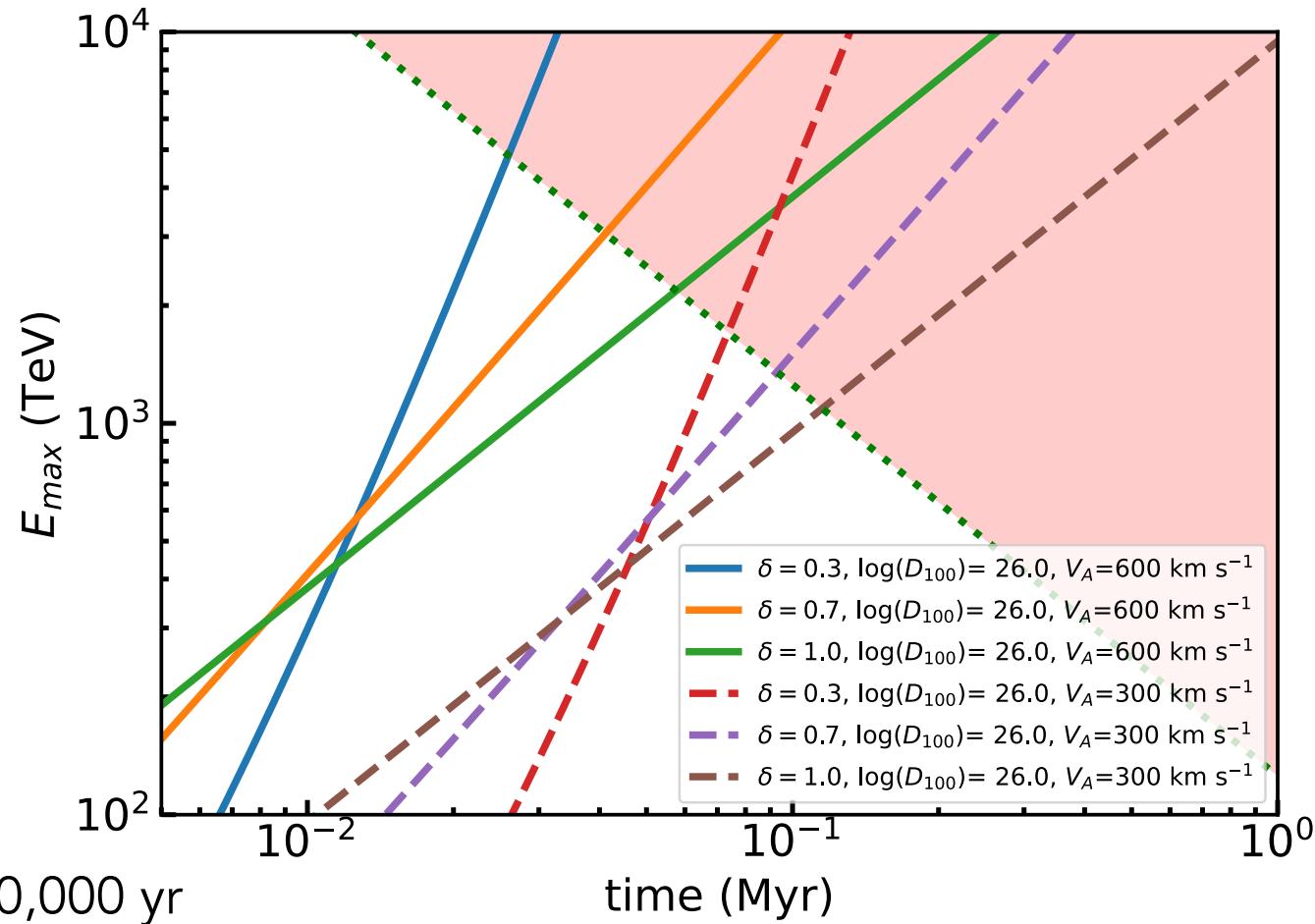
$$E_{\max} = 6.4 \times 10^{14} \eta^{-1} \sqrt{\delta\xi} \left(\frac{B}{10 \text{ }\mu\text{G}} \right)^2 \left(\frac{R}{50 \text{ pc}} \right) \left(\frac{n_H}{0.001 \text{ cm}^{-3}} \right)^{-1/2} \text{ eV}$$

- For multi-PeV protons: high B and $\eta \sim 1$ (Bohm diffusion):

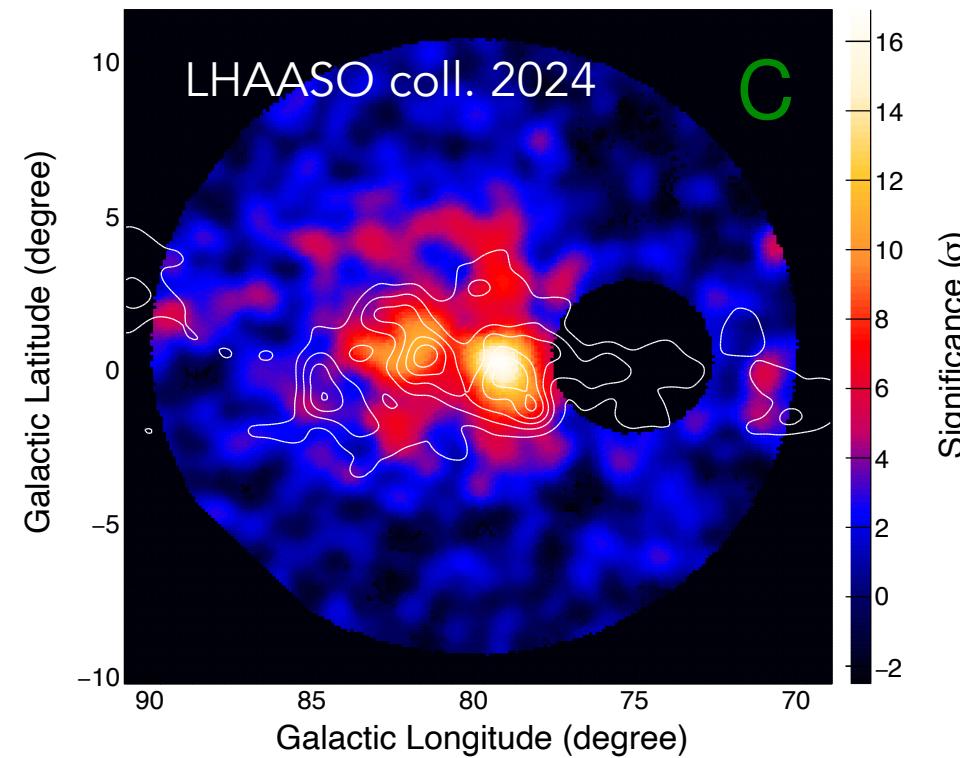
- E.g. $B=30 \text{ }\mu\text{G}$ gives $E_{\max} \approx 6.8 \times 10^{15} \text{ eV}$

Conditions needed for Fermi-2 PeVatrons?

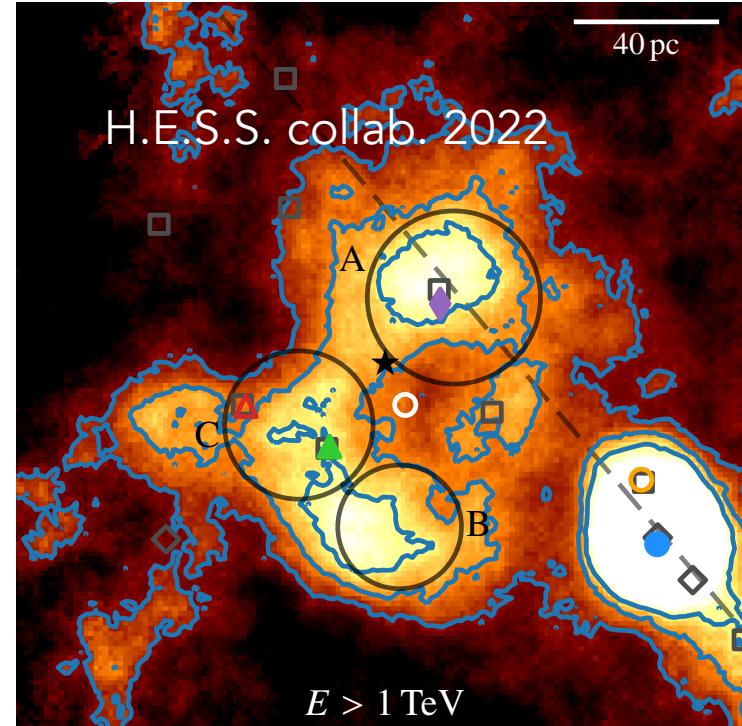
- Need fast Alfvén speeds:
 - $V_A \gtrsim 500 \text{ km/s}$
 - $n_H \approx 0.001 \text{ cm}^{-3}, B \approx 10 - 50 \mu\text{G}$
 - Need very slow diffusion:
 - $D(100 \text{ TeV}) \approx 10^{26} \text{ cm}^3\text{s}^{-1}$
 - likely Bohm diffusion
 - Mechanism can be quite fast, 20,000-100,000 yr
- Injection: CRs pre-accelerated by wind shocks, termination shocks, SNRs



Cygnus Cocoon & Westerlund 1

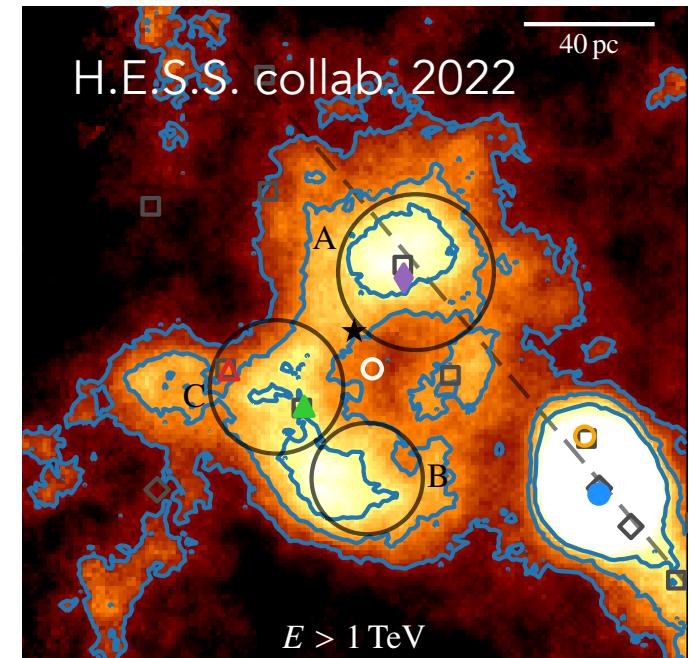
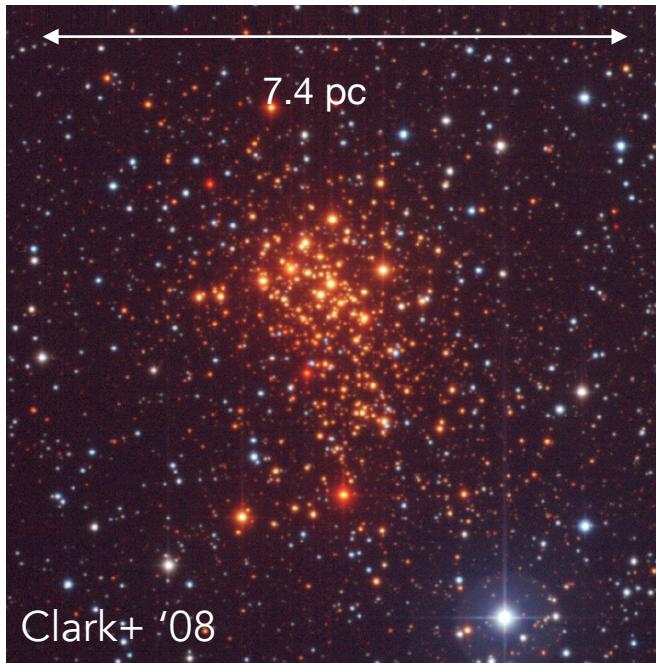


- >0.6 PeV photons
- $R \sim 55$ pc
- $D(100 \text{ TeV}) \approx \frac{R^2}{6t} \approx 1.4 \times 10^{26} \left(\frac{t}{\text{Myr}} \right)^{-1}$
- Absence of termination shock?
(Vieu+ '24)



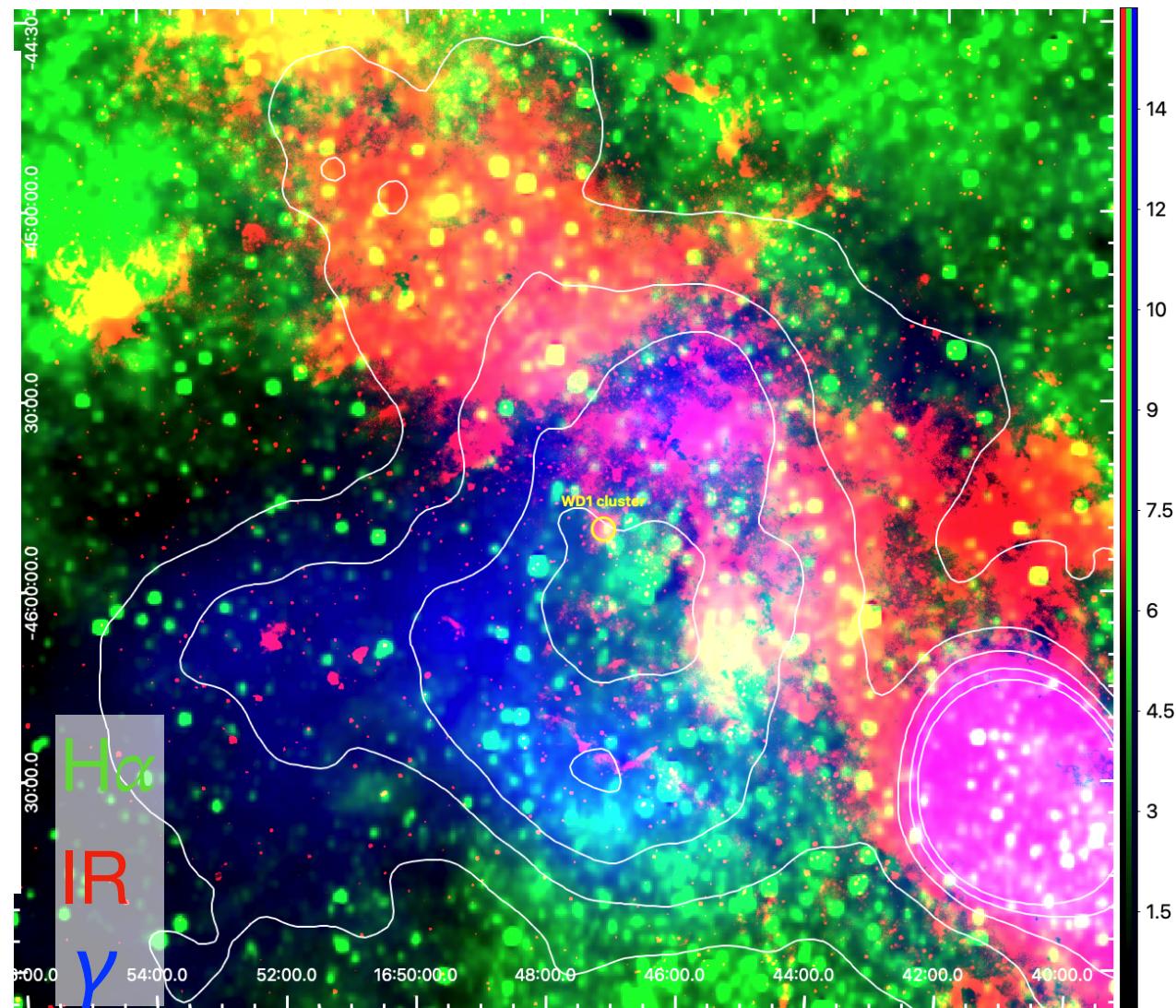
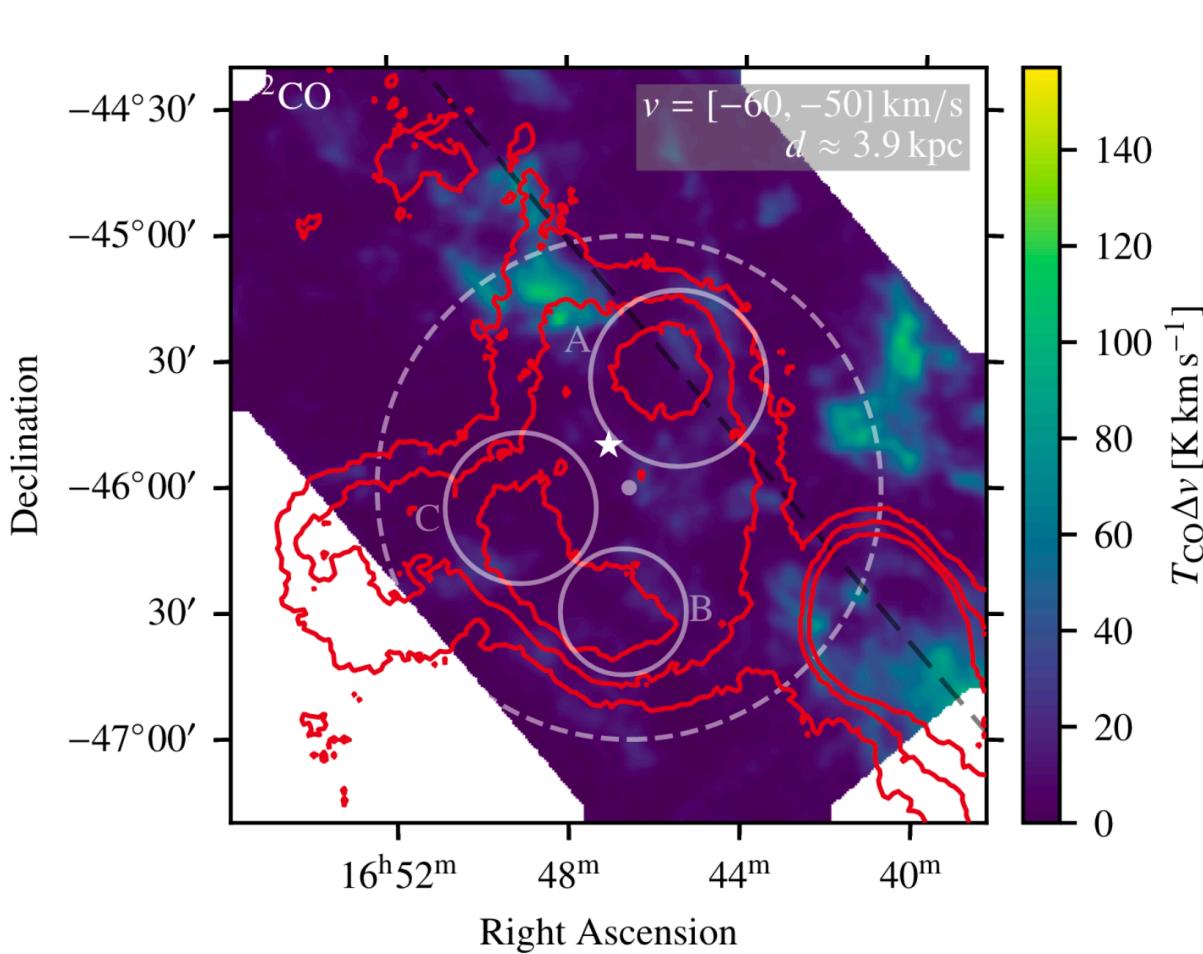
- proton break > 200 TeV
- $R \sim 50$ pc
- $D(100 \text{ TeV}) \approx \frac{R^2}{6t} \approx 1.2 \times 10^{26} \left(\frac{t}{\text{Myr}} \right)^{-1}$
- H.E.S.S. coll. '22: $B \gtrsim 50 \mu\text{G}$
(Bohm diffusion, 200 TeV particles and $t=1$ Myr)

Starforming region Westerlund 1

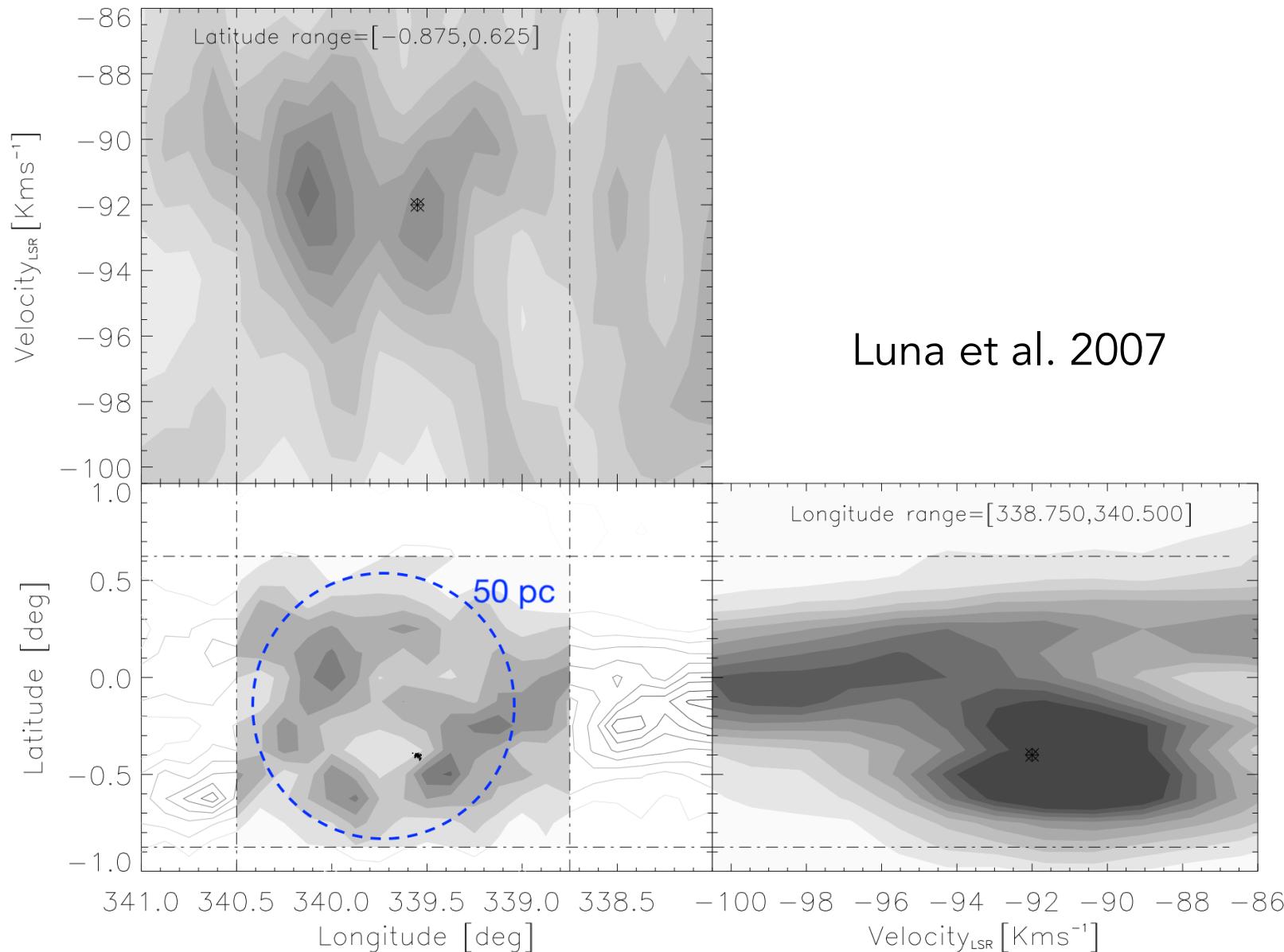


- Very rich massive cluster (27 Wolf-Rayet stars!): $L_w \approx 10^{39} \text{ erg/s}$
- About 4 Myr old
- Associated with TeV gamma-ray source: HESS J1646–458
- Gamma-ray emission up to 200 TeV:
- Total CR energy: $W_p \approx 6 \times 10^{51} d_{4.9 \text{kpc}}^2 n_{\text{H}} \text{ erg}$ ($\sim 20\%$ of $E_w = L_w t$)

Westerlund 1 multiwavelength picture: an ISM hole

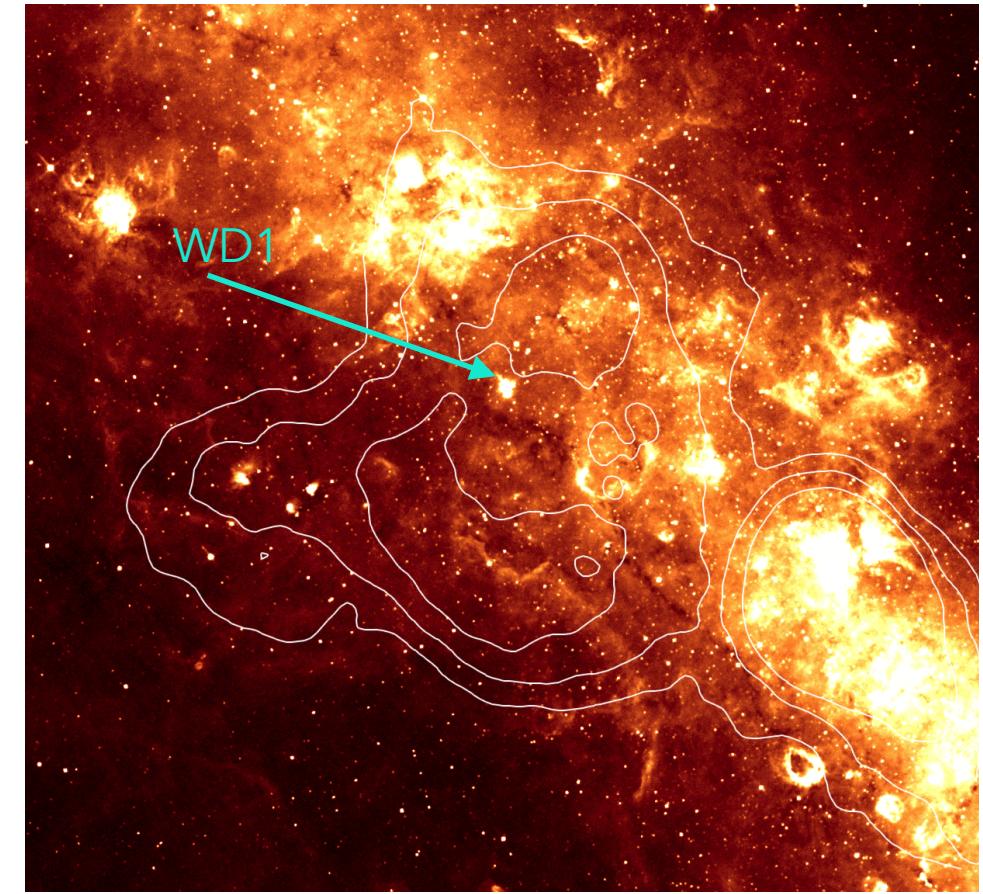


Is WD1 TeV source inside a cavity of 50~pc?



TeV source WD 1: termination shock or shell?

- **Termination shock model:**
 - size TeV source << size superbubble
 - termination shock in low density: emission likely leptonic (Härrer+ '23)
 - Requires $V_{ts}=2500$ km/s
 - Problem 1: average stellar wind $\sqrt{v_w^2} \approx 1350$ km/s (Fenech+ '18)
 - problem 2: why is starcluster so close to gamma-ray shell in NE? and why not brighter there?
- **Shell model:**
 - TeV emission hadronic (shell $n_{\text{H}} \approx 1 - 10 \text{ cm}^{-3}$)
 - Most TeV CRs in SB do not produce radiation
 - shell size small: $\sim 50 \text{ pc}$
 - Gamma-ray shell fits within gap of ISM
 - Why is dense shell not visible in IR/CO/optical?



IR map (8micron) with H.E.S.S. contours

Energetic constraints Westerlund 1

- Very rich massive cluster: $L_w \approx 10^{39}$ erg/s
- Age: 5~Myr (but active for ~Myr?)
- Total energy: $E_w = L_w t \approx 3 \times 10^{52} L_{w,39} t_{\text{Myr}}$ erg
- H.E.S.S.: $W_p \approx 6 \times 10^{51} d_{4.9kpc}^2 n_H$ erg ($\sim 20\%$ E_w)
- Magnetic field: $E_B \approx \frac{B^2}{8\pi} V \approx \frac{1}{6} B^2 R^3 \approx 6 \times 10^{49} (B/10 \mu\text{G})^2$ erg (0.2% E_w)
 - For Fermi-2: turbulent field needs to be continuously replenished
- What about CR energy in bubble vs shell?
 - $\langle n \rangle = \frac{V_{\text{shell}} n_{\text{shell}} + V_{\text{bubble}} n_{\text{bubble}}}{V_{\text{tot}}}$
 - $\Delta R/R \approx 10\% : \langle n \rangle \approx 30\% n_{\text{shell}} \approx 0.3 - 3 \text{ cm}^{-3}$
 - So W_p estimate H.E.S.S. approximately valid, but may be off by factor ~ 3

Pros and Cons Fermi-2 in superbubbles

- DSA/Fermi-1:
 - Pros: DSA proven to be important in many environments to work
 - spectral slope more or less right ($\sim E^{-2.3}$)
 - Cons:
 - Individual stellar winds not powerful enough, but maybe CR encounter multiple shocks
 - Cluster termination shock: is it always there? and is it fast enough?
 - density is low -> no direct source of hadronic emission
- Fermi-2:
 - Requires extreme circumstances: $D(100 \text{ TeV}) \sim 10^{26} \text{ cm}^2/\text{s}$, $V_A > 500 \text{ km/s}$
 - But evidence for low D, and high B and low n!
 - Works even if termination shock is weak/absent, provided enough turbulence
 - Cons: *Fermi-2 spectrum intrinsically hard* (no built-in escape mechanism)
 - PIC simulations Fermi-2: softer spectra due to backreaction on B-turbulence
 - Feeds off turbulent field: needs continuous generation of Alfvén waves

Could supernovae inside SBs PeVatrons?

- We concentrated on either DS by termination shock, or Fermi-2 inside tenuous bubble
- Both have their pros and cons
- What if it is just supernovae?
 - Both Cygnus Cocoon & WD1 are old enough for a few SNe!
- What is special about supernovae inside superbubbles?
 - Low density ($<0.001 \text{ cm}^{-3}$)
 - may never really reach radiation phase
 - takes much longer time to slow down
 - expected total energy in CRs generated should be similar ($\sim 10\%$ of E_{sn})
 - but more time allows particle to reach PeV domain!
 - But: hot plasma \rightarrow low Mach number!

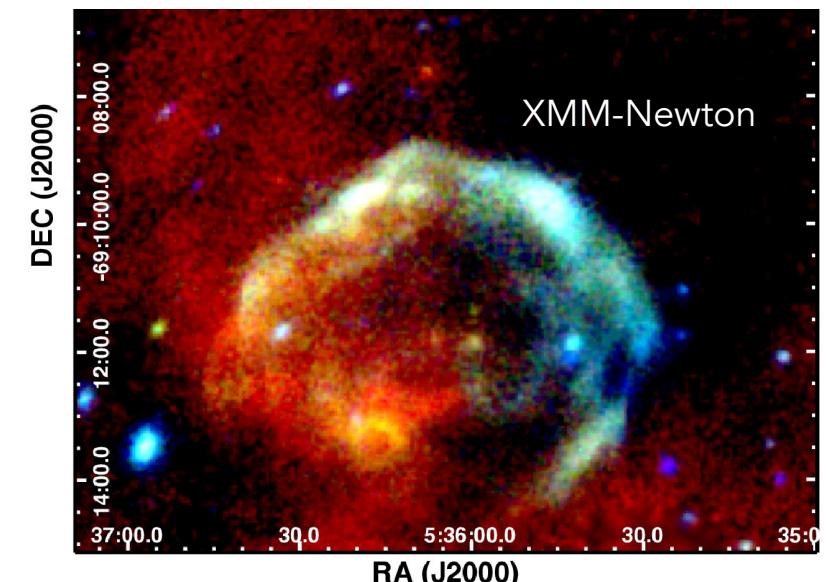
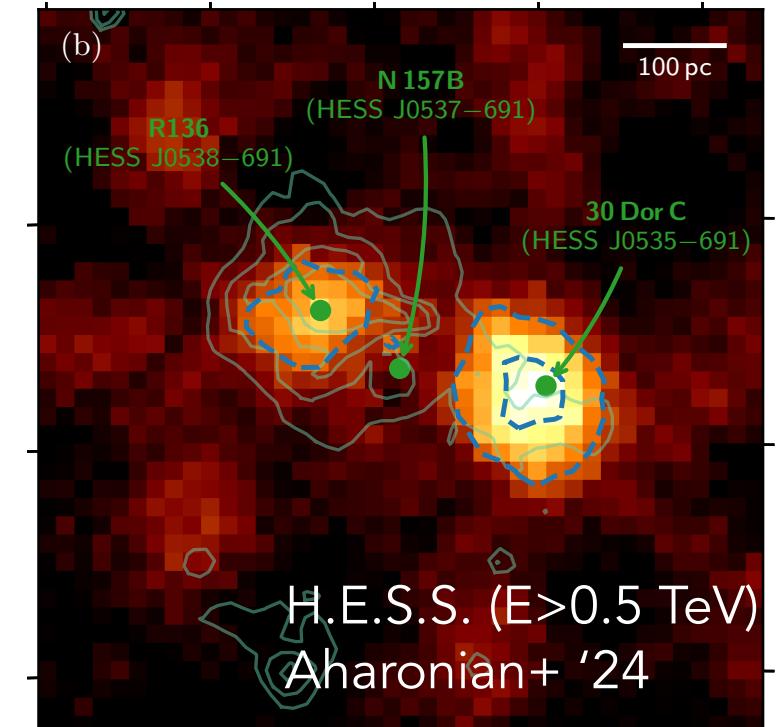
30 Dor C

- Radius $\sim 45\text{-}50$ pc
- Non-thermal X-ray and VHE gamma-ray
- X-ray synchrotron: $V_{\text{sh}} > 3000$ km/s
- Optical HII: $V < 100$ km/s (Kavanagh+ '19)
- Most likely explanation X-ray synchrotron:
 - Single SNR, $t \sim 6000$ yr
 - X-ray width & leptonic model: $B \sim 10\text{-}20 \mu\text{G}$
 - gamma-rays: leptonic

(Bamba+ '04, H.E.S.S. coll+ '15, Kavanagh+ '19, Aharonian+ '24)

- Single SNR, $R \sim 50$ pc, $V > 3000$ km/s: $n_{\text{H}} \sim 0.0005 \text{ cm}^{-3}$

$$\bullet R \approx (Et^2/\rho)^{1/5}, V_s = \frac{2}{5} \frac{R}{t}$$



Summary

- Despite textbook case: Fermi-2 can be very efficient provided V_A is high and D is small
 - Physics: 2nd order in (V/c) , but boost per scattering
 - DSA: multiple scatterings needed before boost
- In superbubbles environment for Fermi-2 potentially ideal:
 - If $n \sim 0.001 \text{ cm}^{-3}$: $V_A > 500 \text{ km/s}$
 - Observational evidence for $D(100 \text{ TeV}) \sim 10^{26} \text{ cm}^{-3}\text{s}$
 - PeV energies can be reached in those circumstances!
- What needs to be done:
 - realistic calculations of spectrum
 - does Fermi2 predict too hard spectra or will it be softened by transport?
 - does it drain the magnetic-field turbulence too quickly?
 - and if so: what will happen? quenching acceleration? are we sometimes lucky?
- Supernovae inside SBs may be an alternative (or additional?) scenario