

EuXFEL Operator Training

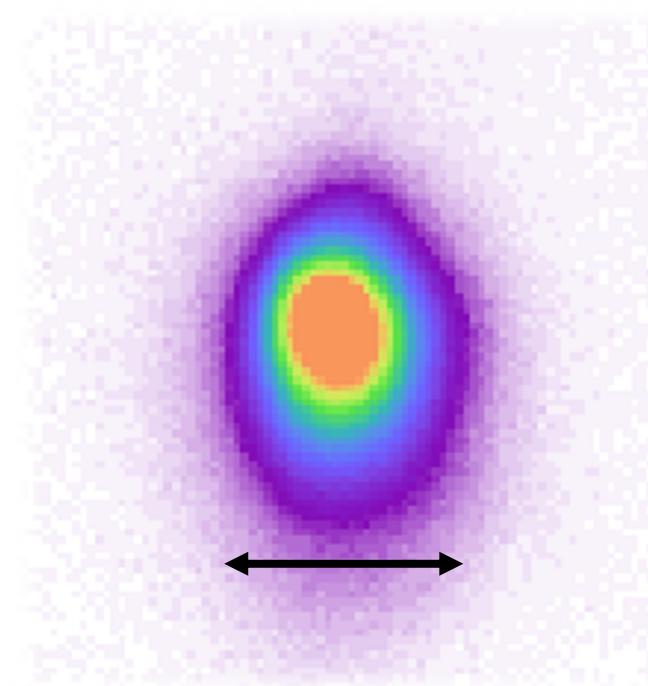
Injector beam optics measurements

Matthias Scholz
March 18, 2025



First things first

- The width of the beam (in horizontal or vertical plane) at a certain position in the beamline depends on two things: The so-called **beta function** at the position and the **emittance**.

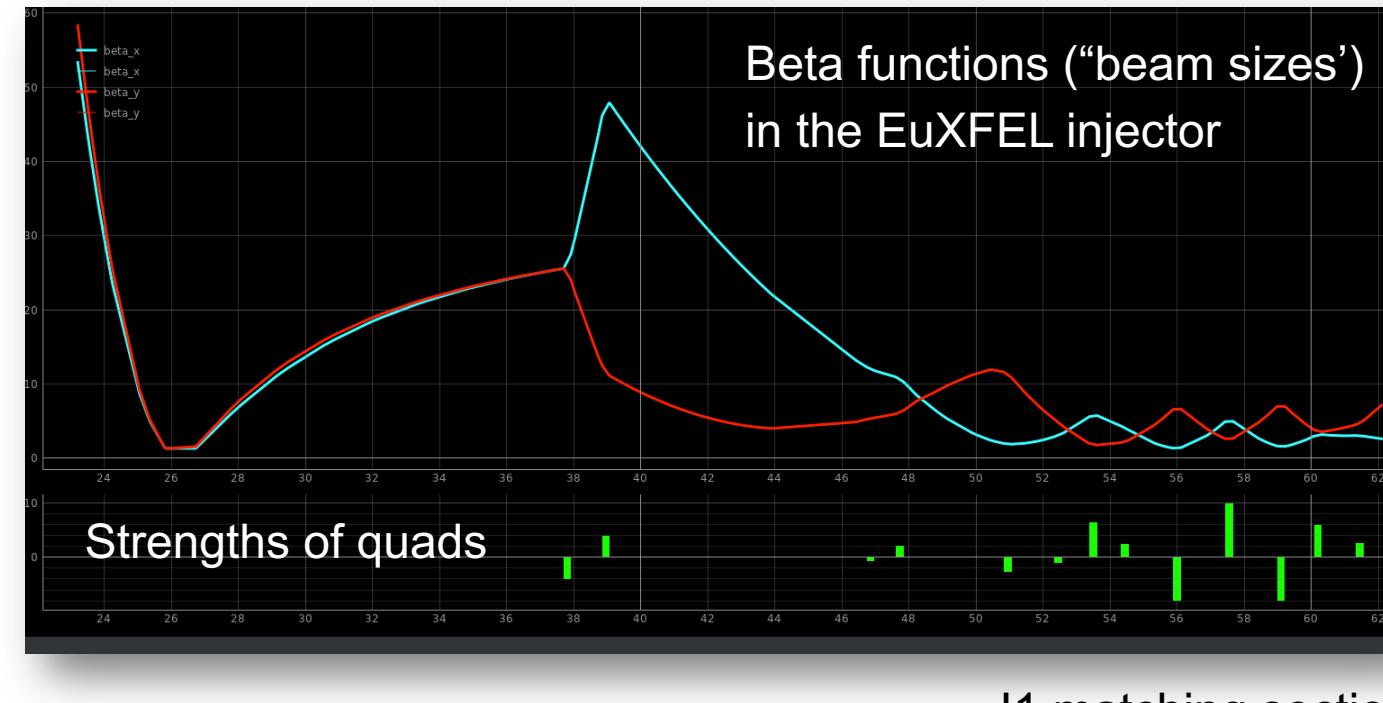


$$\sqrt{\epsilon_x \beta_x}$$

First things first

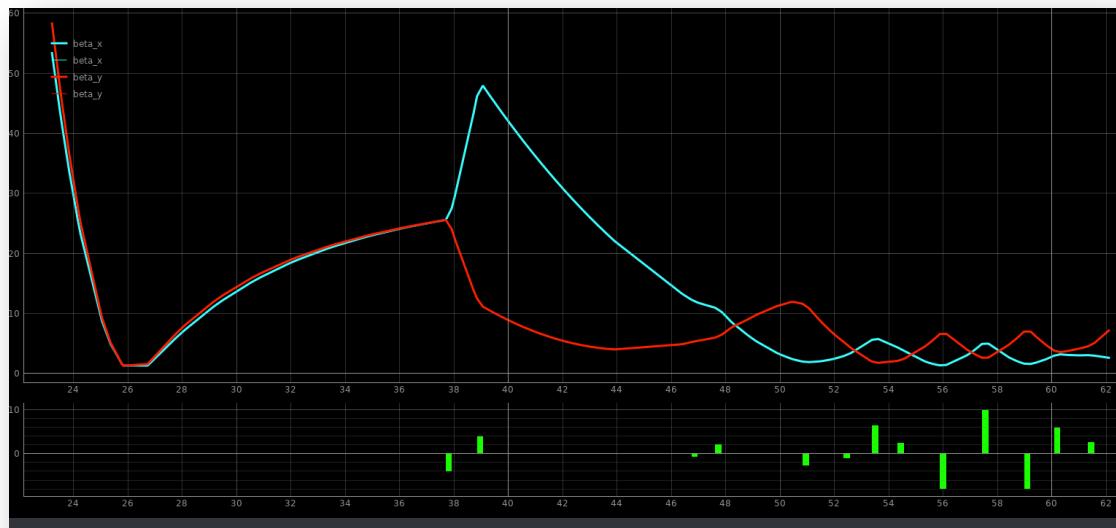
- Matching means, that the actual electron beam parameters fit to the design optics of the lattice (given by the position and strength of magnets). In other words, the beam's size at different positions in the accelerator is as designed.
- The lattice is designed such that the electron beam's quality in the undulator beamlines is as good as possible for lasing.

Position of
the cathode

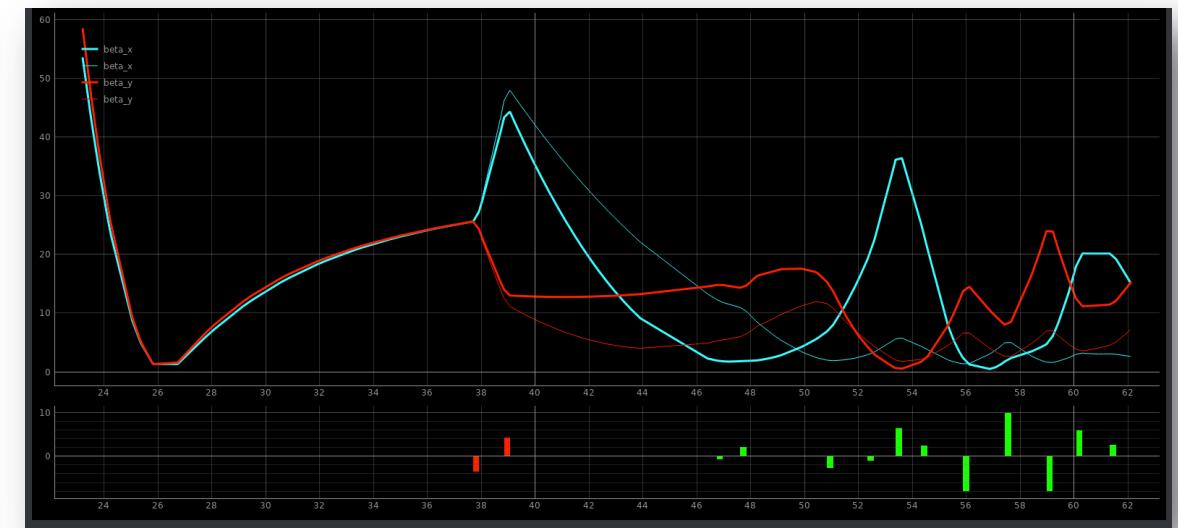


First things first

- Matched and mismatched beams in I1



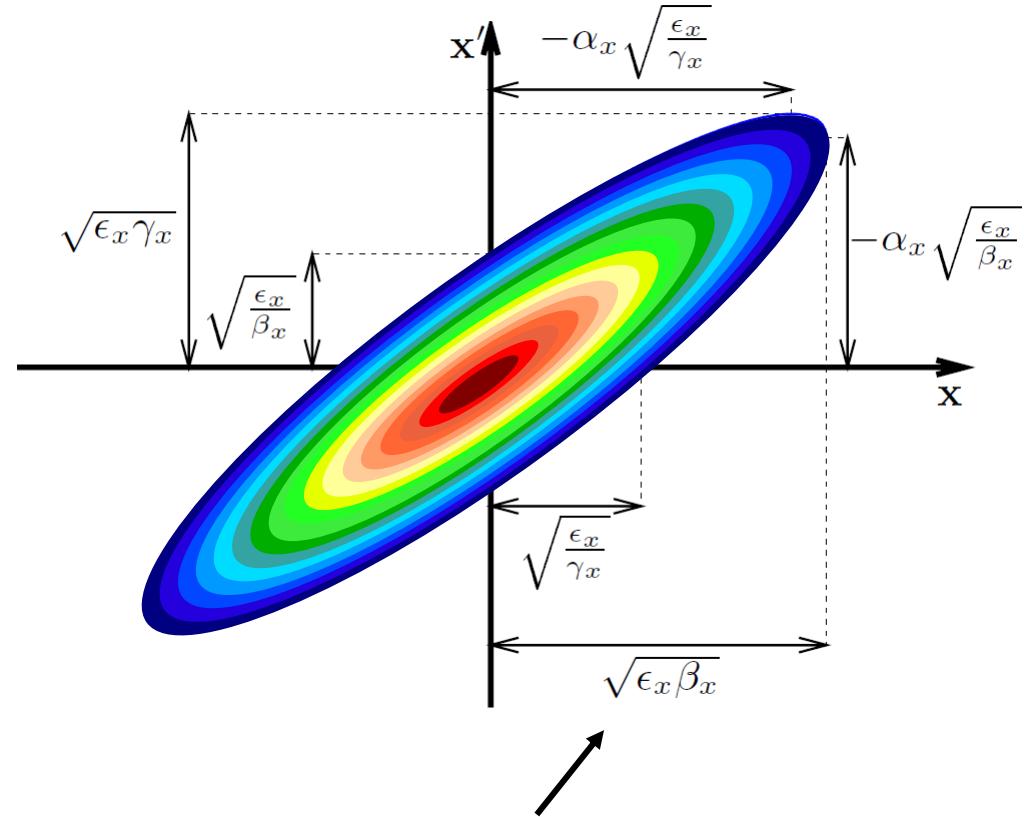
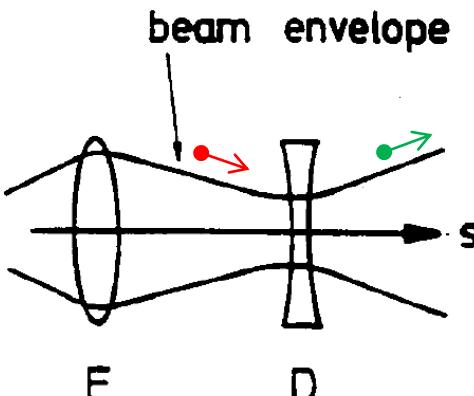
The beam sizes are different from what we need for successful operation



Changed the strengths of two quads in A1 and AH1

Emittance and Twiss-parameters

- The beam orientation is described with the Twiss-parameters (α, β, γ) .
- The “slope” of the ellipses are a signature of convergent or divergent beams.
- A beam which does not have the same orientations (with respect to design optics) is called “mismatched” even if the emittance is the same.



This, can actually be measured (transverse beam sizes) e.g. with a screen or wire!

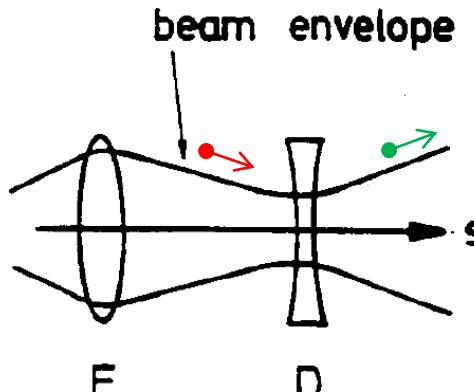
Emittance

- Area covered by particles in phase space is called emittance
- We can assume an elliptical distribution
- Emittance is conserved in linear optics (Liouville's theorem)
 - => beam behaves like an incompressible liquid
 - => focusing the beam will increase its divergence
- Small beams with little divergence as required for SASE lead to small emittance requirements.



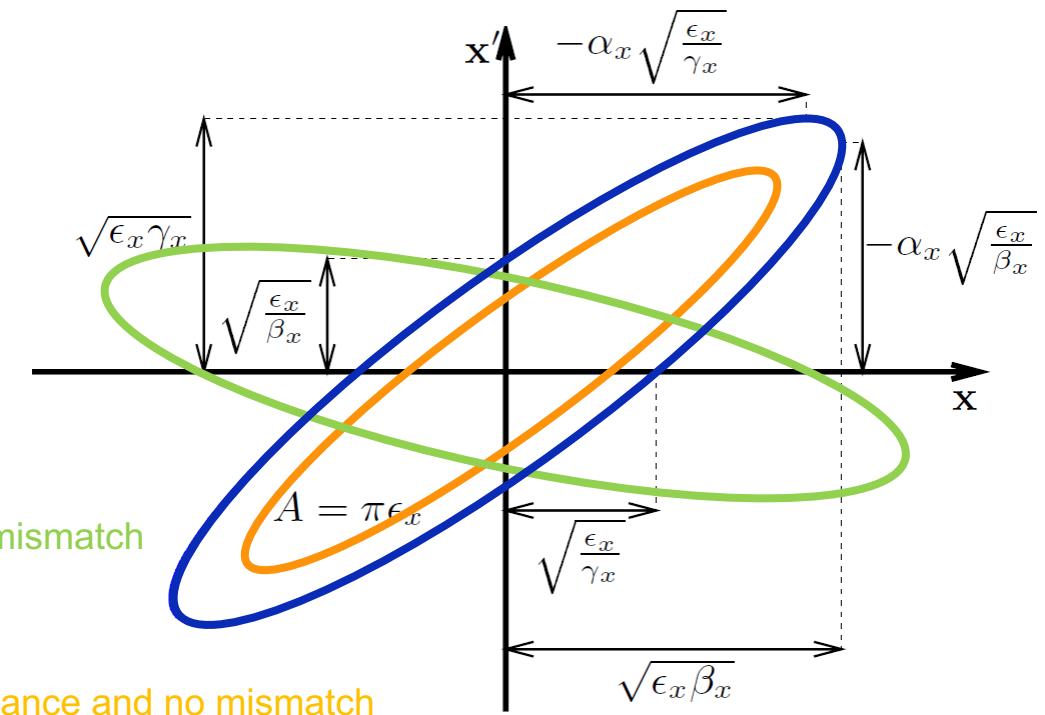
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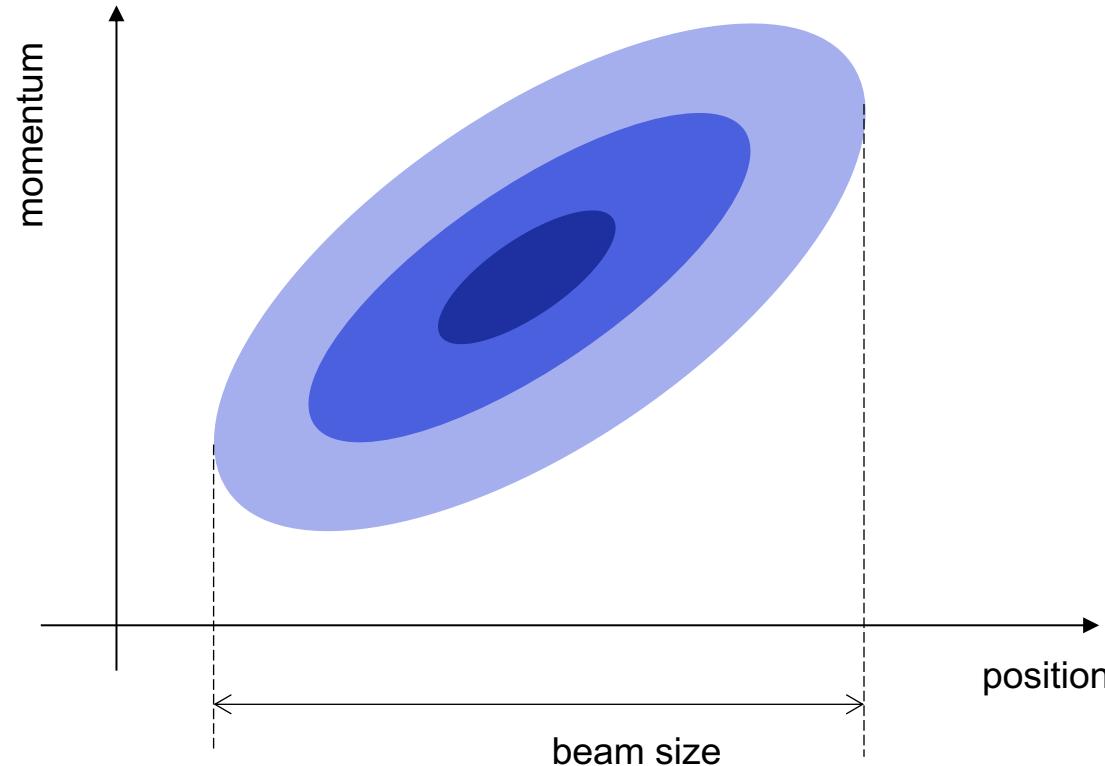


same emittance with mismatch

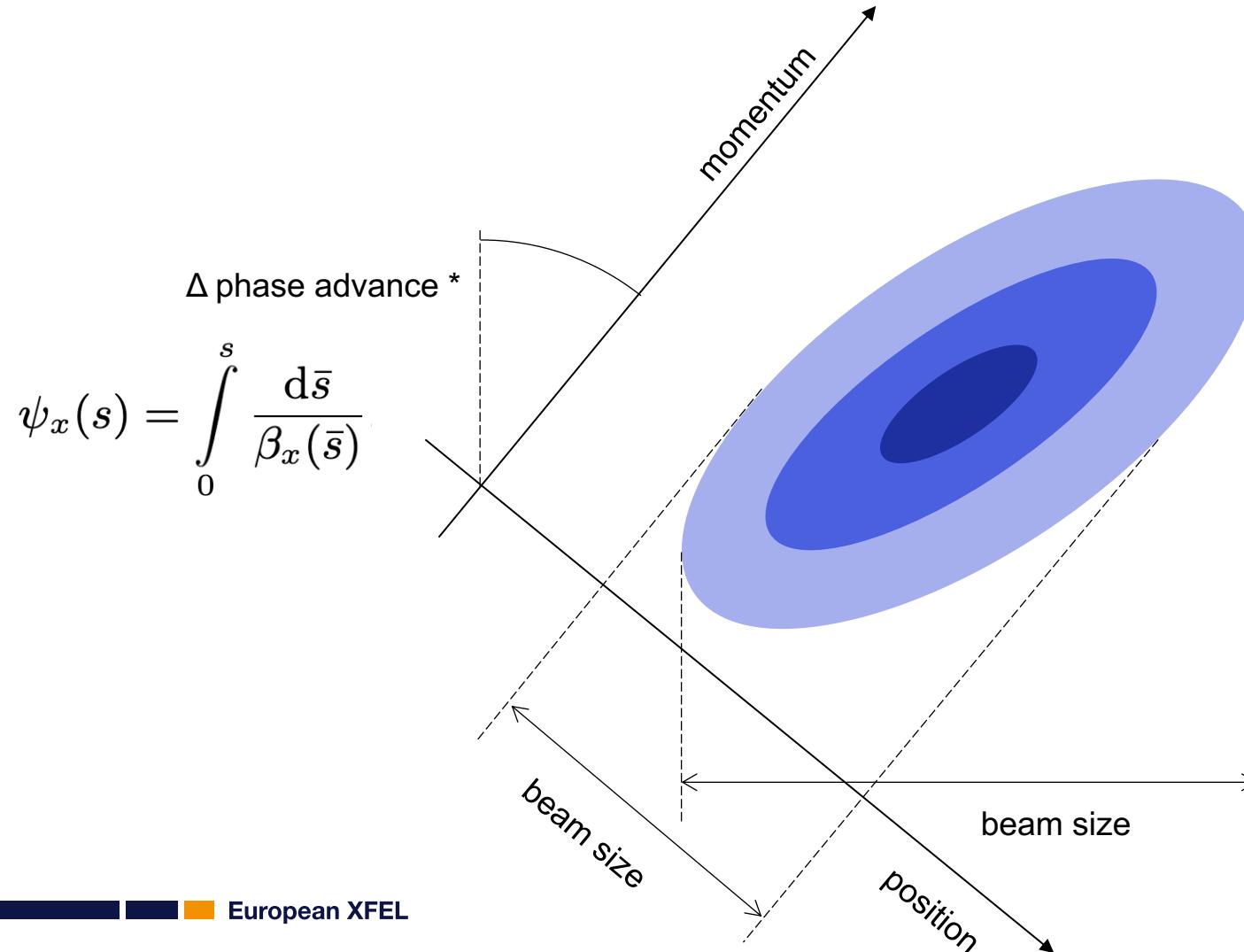
smaller emittance and no mismatch



Emittance and beam size measurements

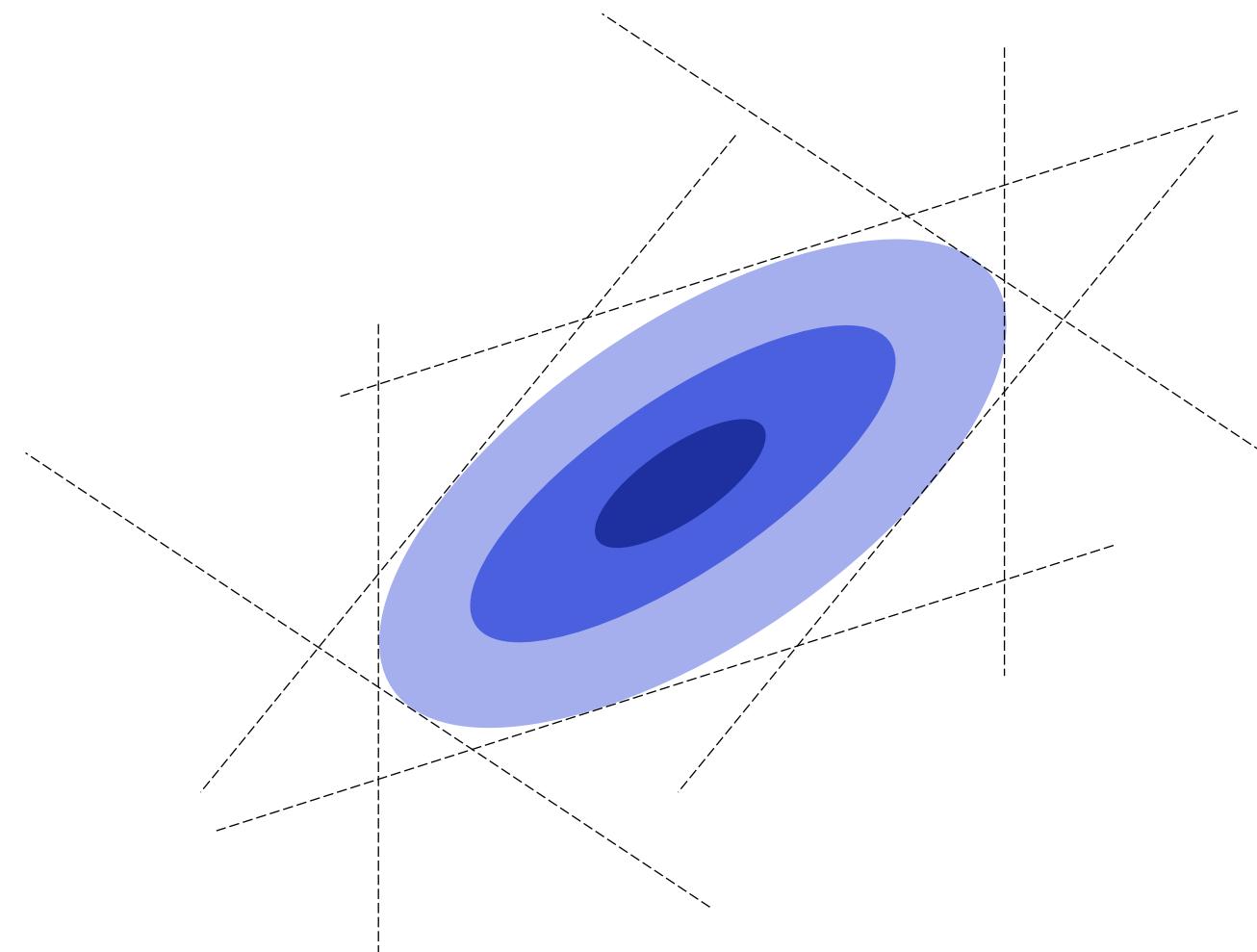


Emittance and beam size measurements



* This is only true in the so called normalized phase space, but for simplicity's sake, let's keep it that way.

Emittance and beam size measurements



How to determine emittance and Twiss parameters

The definition of the emittance and the Twiss parameters at position 0 using the second beam moments.

$$\varepsilon_x = \sqrt{\langle x_0^2 \rangle \langle x_0'^2 \rangle - \langle x_0 x_0' \rangle^2} \quad \text{and} \quad \begin{pmatrix} \beta_{x_0} \\ \alpha_{x_0} \\ \gamma_{x_0} \end{pmatrix} = \begin{pmatrix} \langle x_0^2 \rangle / \varepsilon_x \\ -\langle x_0 x_0' \rangle / \varepsilon_x \\ \langle x_0'^2 \rangle / \varepsilon_x \end{pmatrix}$$

We can only measure $\langle X^2 \rangle$, the squared rms beam size σ^2 .

-> not enough...

However, we know how $\langle X^2 \rangle$ is transformed from 0 to i using the transfer matrix elements R_{kl}

$$\langle x_i^2 \rangle = R_{11}^{(i)2} \langle x_0^2 \rangle + R_{12}^{(i)2} \langle x_0'^2 \rangle + 2R_{11}^{(i)} R_{12}^{(i)} \langle x_0 x_0' \rangle + 2R_{11}^{(i)} R_{16}^{(i)} \langle x_0 s_0 \rangle + 2R_{12}^{(i)} R_{16}^{(i)} \langle x_0' s_0 \rangle + R_{16}^{(i)2} \langle s_0^2 \rangle$$

We do the measurements in section with no bending magnets and assume that the transfer matrix elements R_{16} and R_{26} are zero.

How to determine emittance and Twiss parameters

The definition of the emittance and the Twiss parameters at position 0 using the second beam moments.

$$\varepsilon_x = \sqrt{\langle x_0^2 \rangle \langle x_0'^2 \rangle - \langle x_0 x_0' \rangle^2} \quad \text{and} \quad \begin{pmatrix} \beta_{x_0} \\ \alpha_{x_0} \\ \gamma_{x_0} \end{pmatrix} = \begin{pmatrix} \langle x_0^2 \rangle / \varepsilon_x \\ -\langle x_0 x_0' \rangle / \varepsilon_x \\ \langle x_0'^2 \rangle / \varepsilon_x \end{pmatrix}$$

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can be measured

three unknowns

Transfer matrix elements -> well known

Calculation of beam moments

Lets make 3 measurements with different transfer matrices!

$$\begin{aligned}\sigma_{x,1}^2 &= \langle x_1^2 \rangle = R_{11}^{1,2} \langle x_0^2 \rangle + R_{12}^{1,2} \langle x_0'^2 \rangle + 2R_{11}^1 R_{12}^1 \langle x_0 x_0' \rangle \\ \sigma_{x,2}^2 &= \langle x_2^2 \rangle = R_{11}^{2,2} \langle x_0^2 \rangle + R_{12}^{2,2} \langle x_0'^2 \rangle + 2R_{11}^2 R_{12}^2 \langle x_0 x_0' \rangle \\ \sigma_{x,3}^2 &= \langle x_3^2 \rangle = R_{11}^{3,2} \langle x_0^2 \rangle + R_{12}^{3,2} \langle x_0'^2 \rangle + 2R_{11}^3 R_{12}^3 \langle x_0 x_0' \rangle\end{aligned}$$

can be measured

Transfer matrix elements -> well known

three unknowns and 3 equations

$$\begin{pmatrix} \langle x_0^2 \rangle \\ \langle x_0 x_0' \rangle \\ \langle x_0'^2 \rangle \end{pmatrix} = \begin{pmatrix} R_{11}^{(1)^2} & 2R_{11}^{(1)} R_{12}^{(1)} & R_{12}^{(1)^2} \\ R_{11}^{(2)^2} & 2R_{11}^{(2)} R_{12}^{(2)} & R_{12}^{(2)^2} \\ R_{11}^{(3)^2} & 2R_{11}^{(3)} R_{12}^{(3)} & R_{12}^{(3)^2} \end{pmatrix}^{-1} \begin{pmatrix} \sigma_{x,1}^2 \\ \sigma_{x,2}^2 \\ \sigma_{x,3}^2 \end{pmatrix}$$

Done. All 3 required beam moments can be calculated.

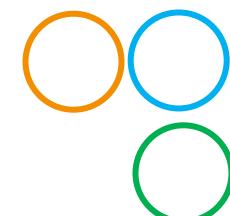
Fit of beam moments

- Calculating the beam moments with 3 measurements does not result in any error estimations!
- -> Preferably more than 3 measurements should be made.
- The beam moments can be determined by a least square fit:

$$\chi^2 = \sum_i \left[\frac{\langle x_i^2 \rangle - \left(R_{11}^i \langle x_0^2 \rangle + R_{12}^i \langle x_0'^2 \rangle + 2R_{11}^i R_{12}^i \langle x_0 x_0' \rangle \right)}{\sigma \langle x_i^2 \rangle} \right]^2$$

↑

minimize



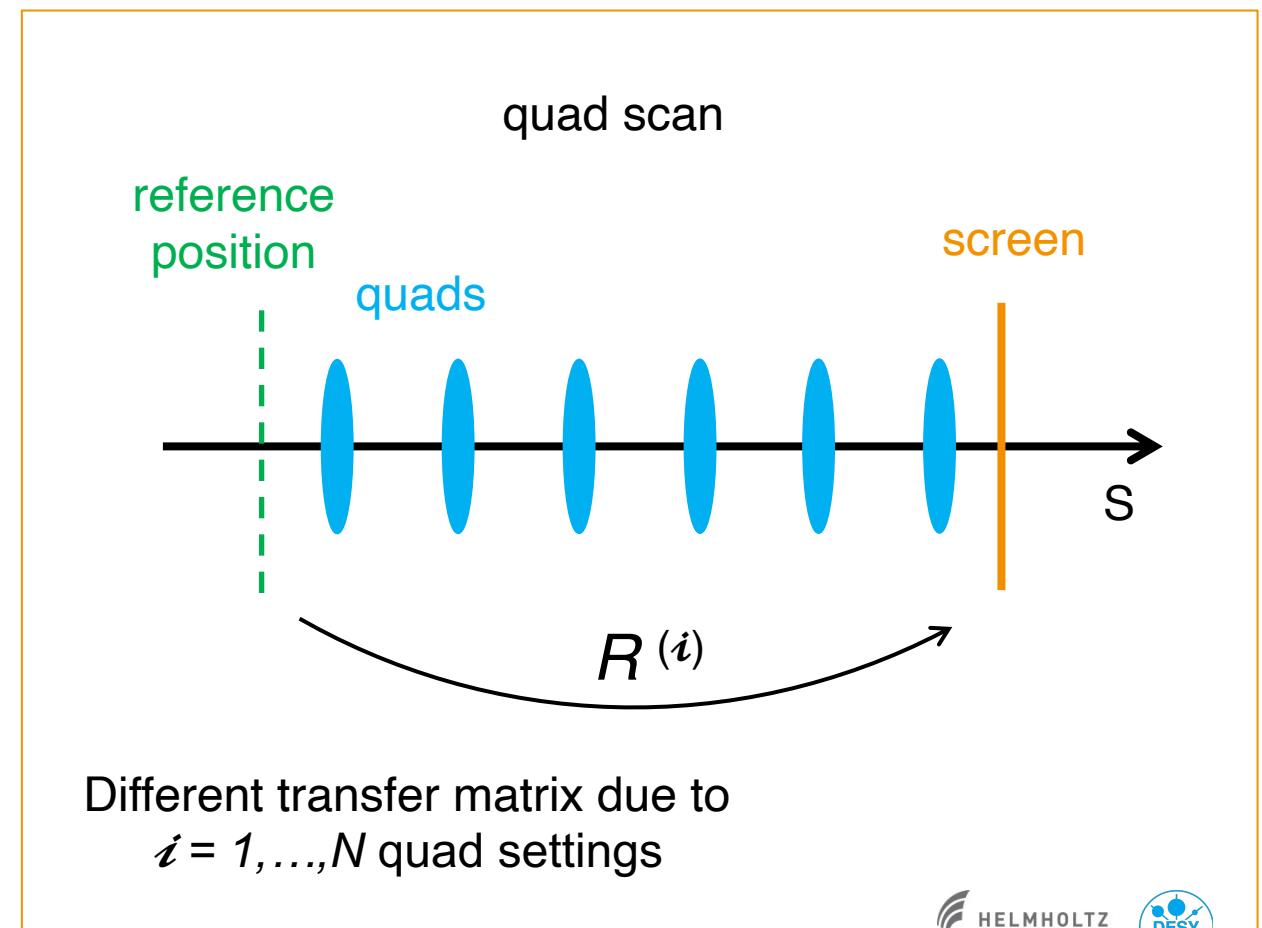
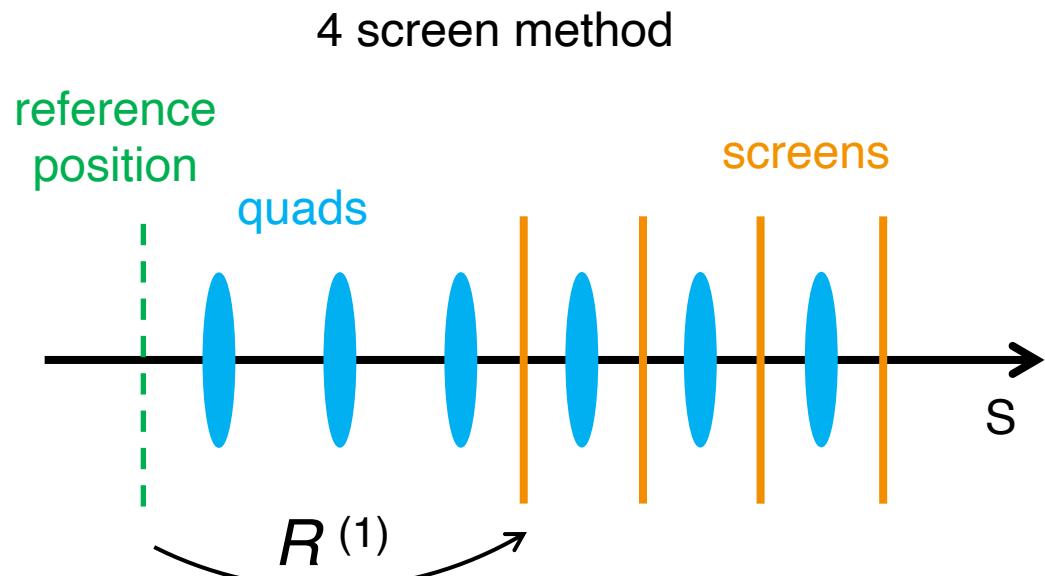
known
fit parameters

Measurements of the Transverse Emittance at the VUV-FEL

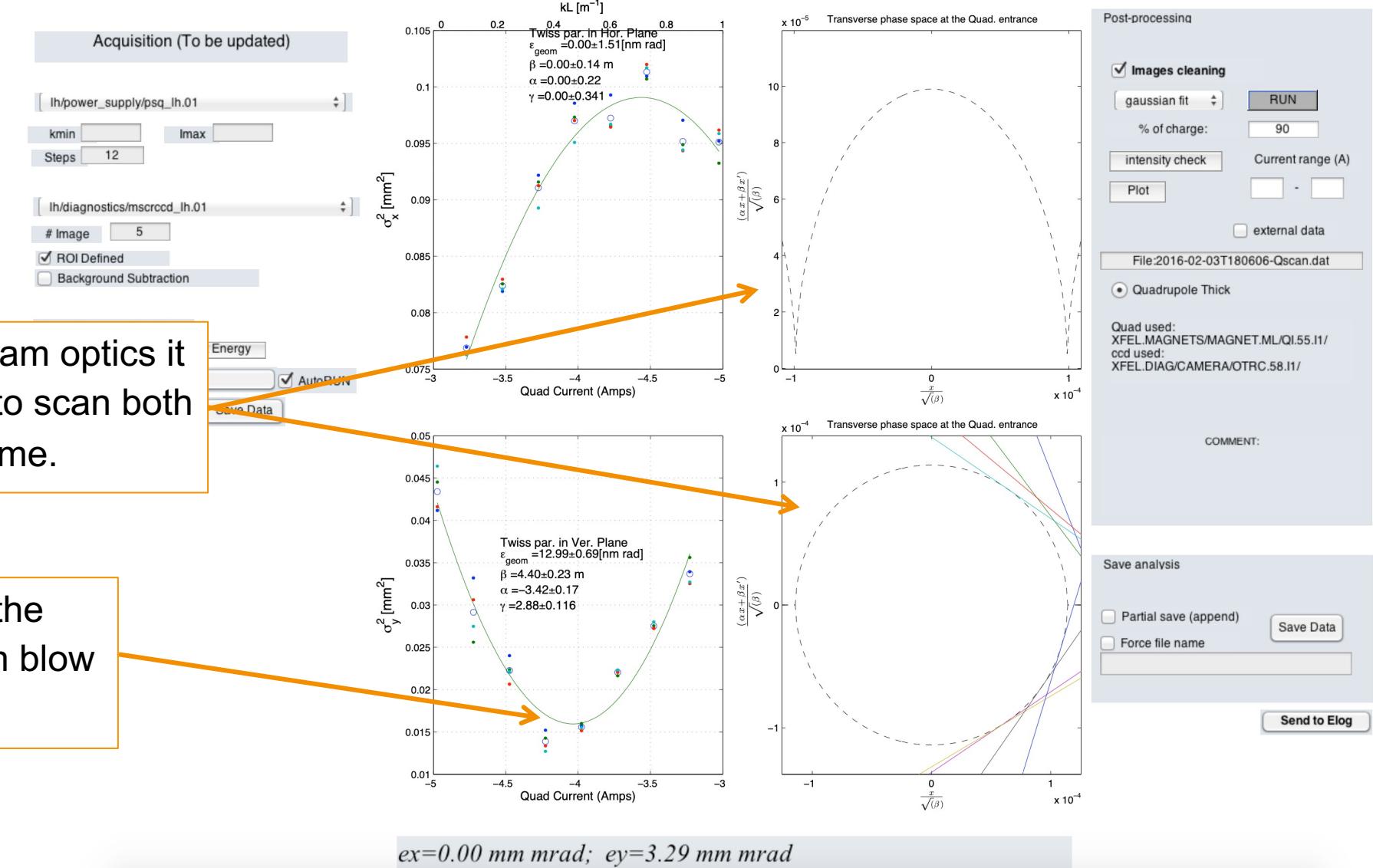
Diploma Thesis
by
Florian Löhl

Measurement methods

How to make at least 3 different measurements with different transfer matrices between a reference position and the measurement position.



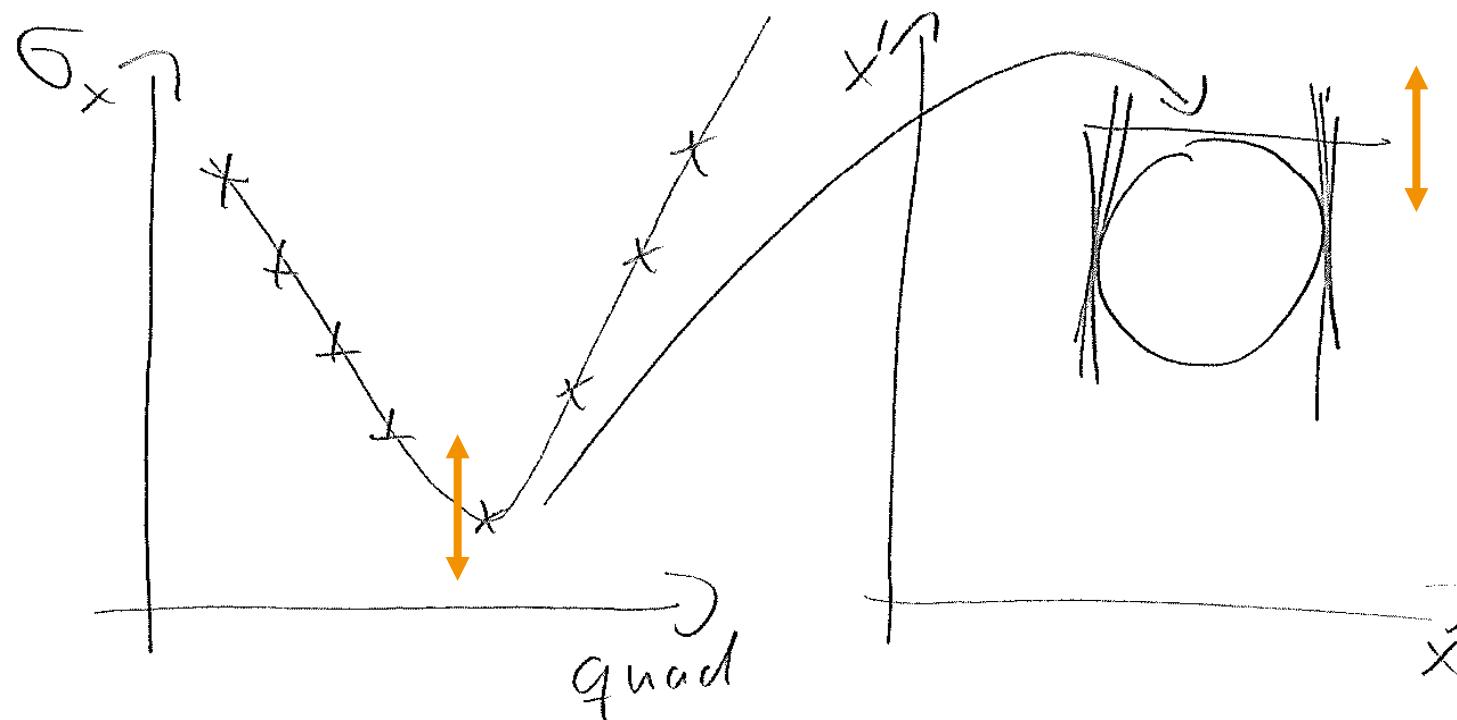
Single quad scan



A very small beam size in the injector can lead to a beam blow up due to space charge.

Depending on the beam optics it is often not possible to scan both planes at the same time.

Single quad scan and scan step sizes



- If equally large steps are selected for the magnetic strength, this can potentially lead to doubtful measurement results.
- The measurement result of the emittance in the example on the right hand side is absolutely dominated by the one measurement taken in the beam waist.

Many thanks to Bolko for the nice and explanatory drawing 😊

Multi quad scans

- Using more than one quadrupole has the advantage that:
 - The beam size at the screen can be kept constant for all measurement steps. No small beams are necessary that might be blown up by space charge.
 - Both transverse planes can be scanned over a wide range in the same measurement (advantage over most single quad scans).
 - Many measurement steps are possible thus measurement errors in single measurements can be found and neglected (advantage over multi-screen method).

PHYSICAL REVIEW SPECIAL TOPICS - ACCELERATORS AND BEAMS 17, 052801 (2014)

Four-dimensional transverse beam matrix measurement using the multiple-quadrupole scan technique

Eduard Prat* and Masamitsu Aiba
Paul Scherrer Institut, CH-5232 Villigen PSI, Switzerland
(Received 10 July 2013; published 19 May 2014)

Accurate measurements of the transverse beam properties are essential to understand and optimize particle beams. We present an optimized method that uses three quadrupole magnets and one profile monitor to measure the full 4D transverse matrix of the beam. The method has been applied to the SwissFEL Injector Test Facility (SITF) at the Paul Scherrer Institute (Villigen). The SITF is the principal test bed and demonstration plant for the SwissFEL project, which aims at realizing a hard-x-ray free-electron laser in 2017. Simulations, measurements, and results of cross-plane coupling correction are presented.

DOI: 10.1103/PhysRevSTAB.17.052801

PACS numbers: 29.20.Ej, 41.60.Cr, 41.85.-p, 29.27.Fh

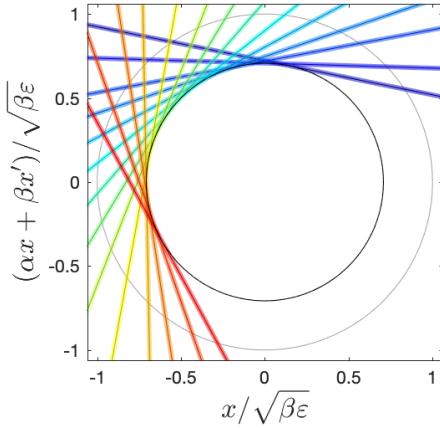
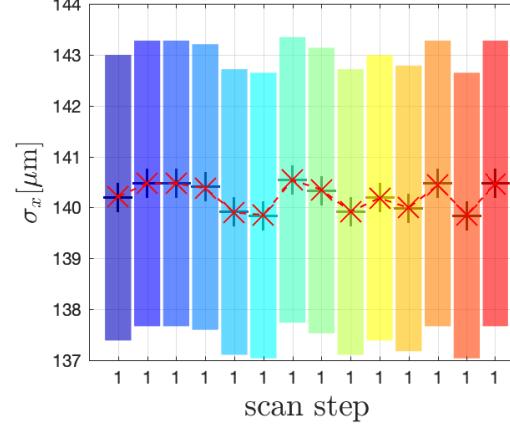
I. INTRODUCTION

Precise knowledge of the transverse beam parameters is essential in all types of charged particle accelerators. In this study we focus on the transverse properties of the electron

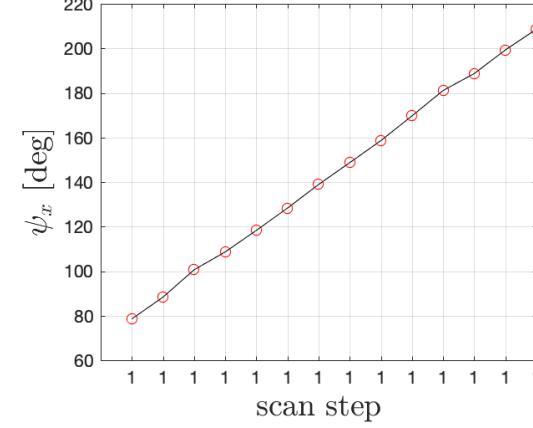
beam parameters (beam sizes and coupling correlation) are measured at a single position and quadrupole strengths are changed to generate the required optics for the 4D measurement. Four-dimensional measurements by means of quadrupole scans have already been reported in the past

Prepared quad scan for the EuXFEL injector

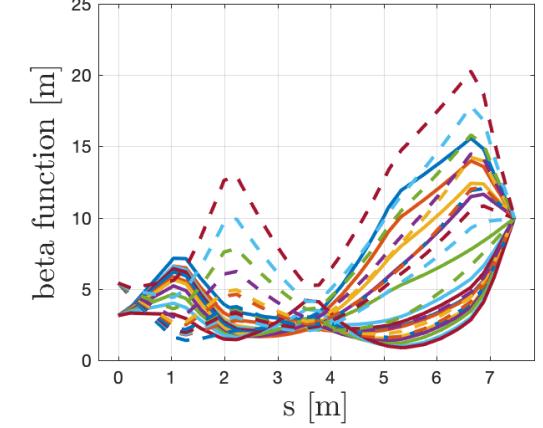
(Gaussian) normalised horizontal phase space

(Gaussian) $\chi^2/N = 3.7091e - 05$ 

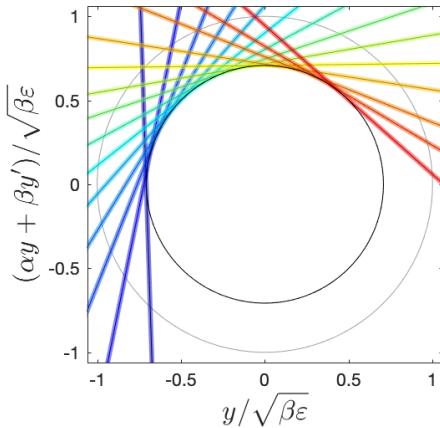
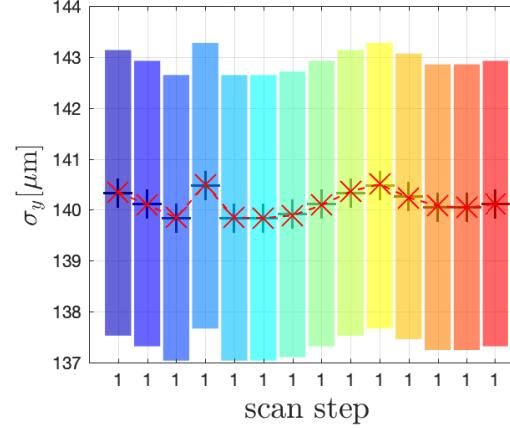
horizontal phase advances



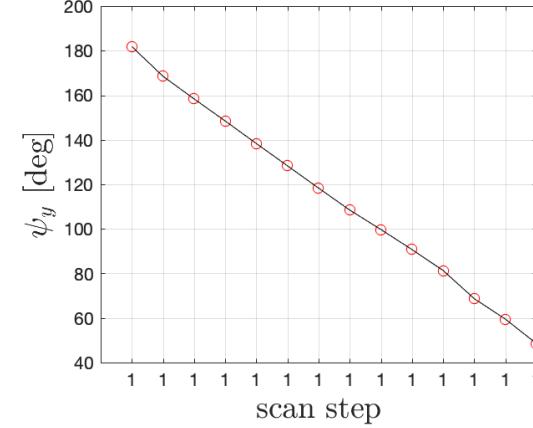
beta functions for all scan steps



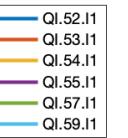
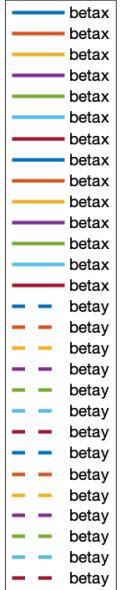
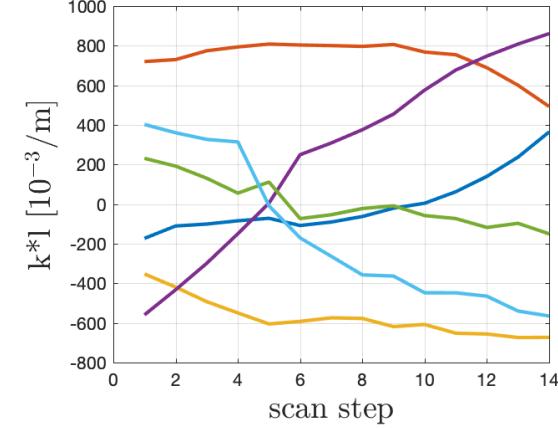
(Gaussian) normalised vertical phase space

(Gaussian) $\chi^2/N = 7.3187e - 05$ 

vertical phase advances



quad strengths



Optics matching in the injector using screen stations and multi knob quad scans

quad_scan_GUI

Quad scan GUI

Measurement

Injector (OTRC.59.I1)

Screens

Cycle only at the end of the measurement (default)

Scan increment (leave empty for default value)

Safe full resolution pictures (only screen measurement)

Use the following quad settings after the scan:

Design (default) previous setup

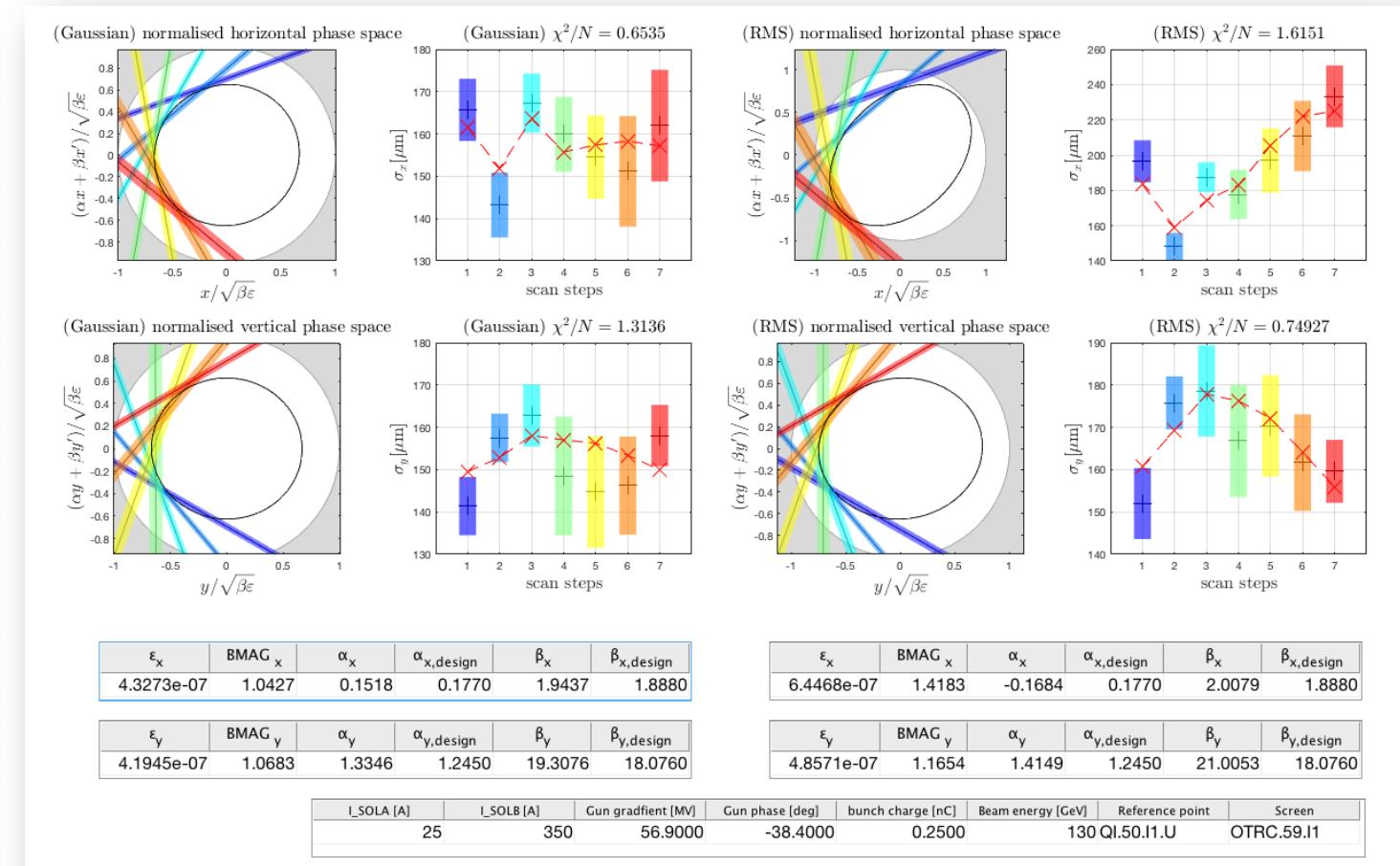
Start the scan **Load data**

Re-evaluation

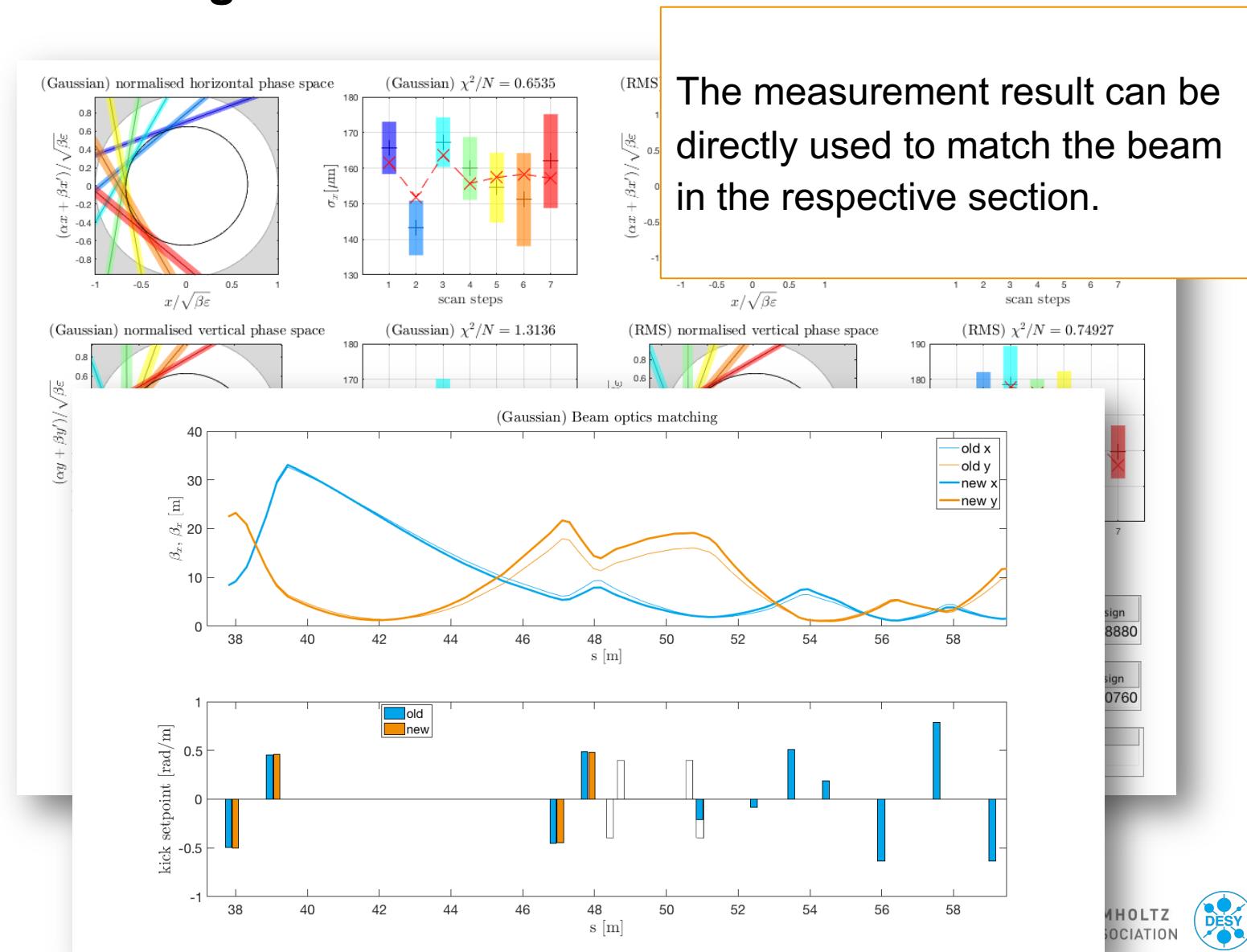
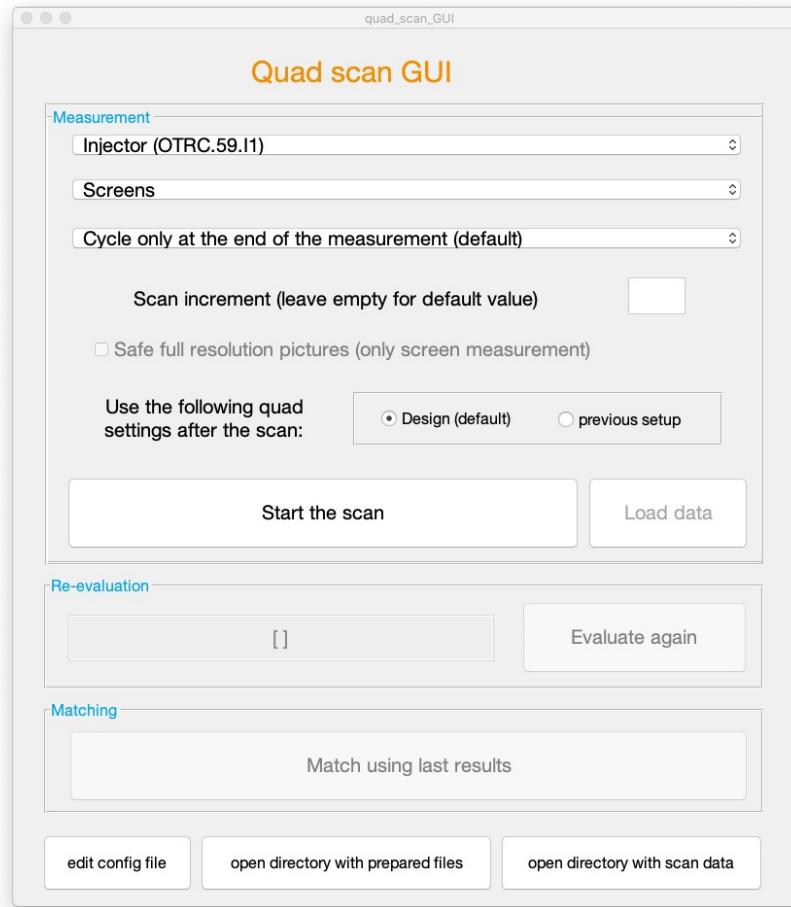
Matching

Match using last results

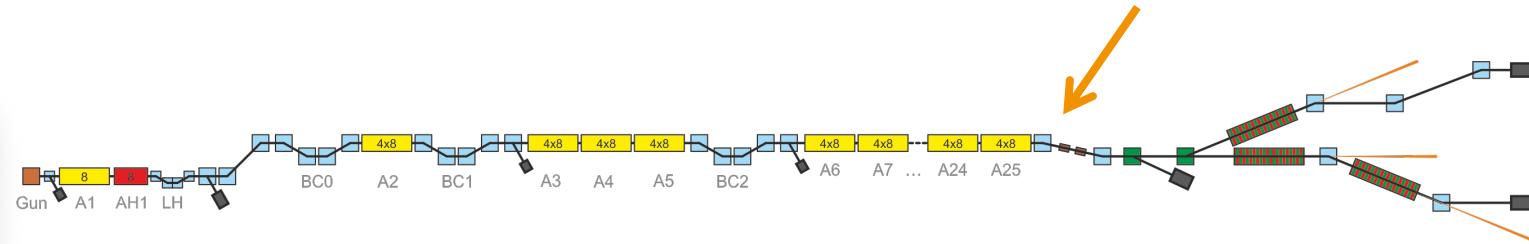
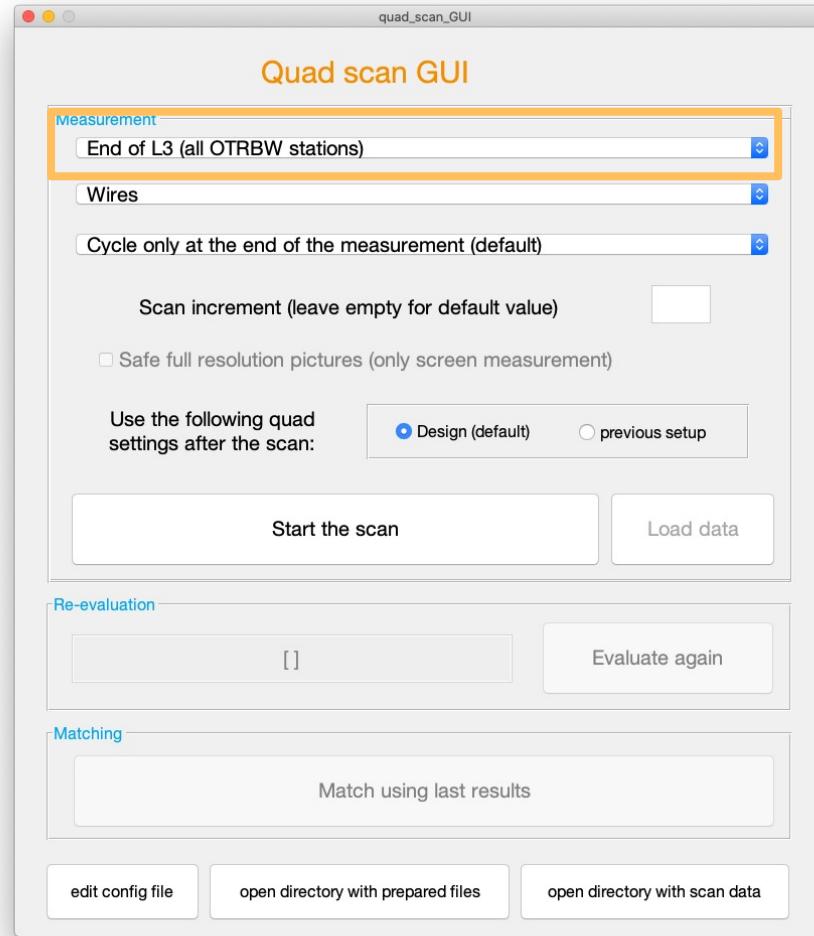
edit config file **open directory with prepared files** **open directory with scan data**



Optics matching in the injector using screen stations



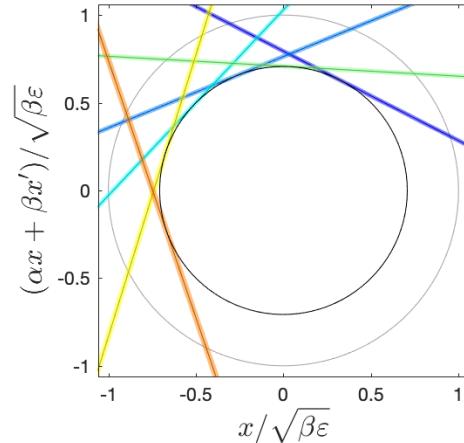
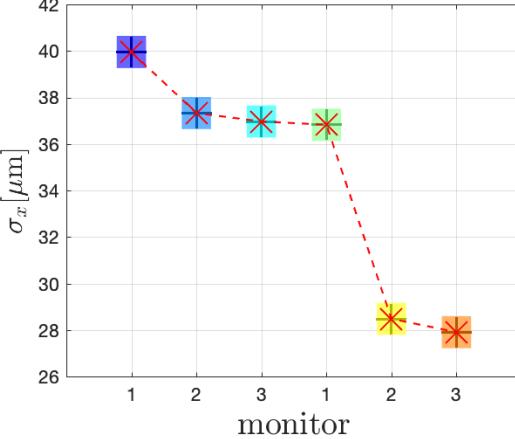
Beam optics measurements downstream L3



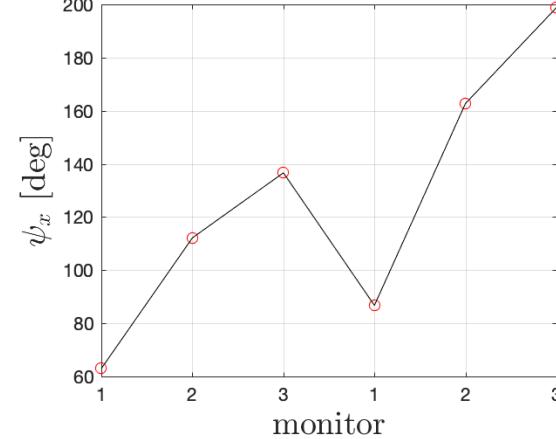
- Final beam optics measurements and corrections at the end of the main linac.
- This measurement can be carried out using either screens or wire scanners.
- It ensures, *inter alia*, an effective collimation in the following section.

Prepared quad scan for L3

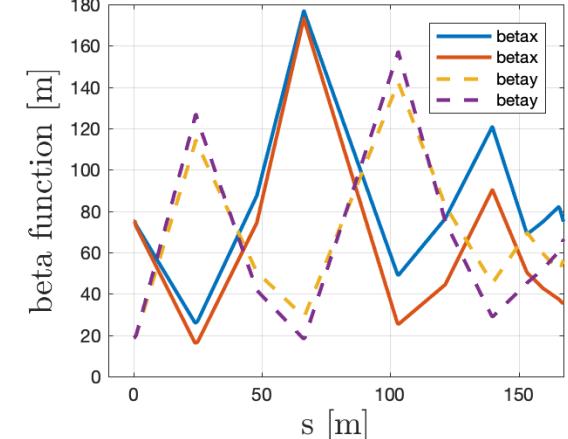
(Gaussian) normalised horizontal phase space

(Gaussian) $\chi^2/N = 8.2081e - 08$ 

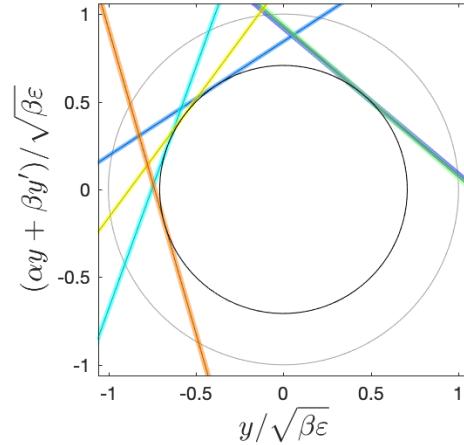
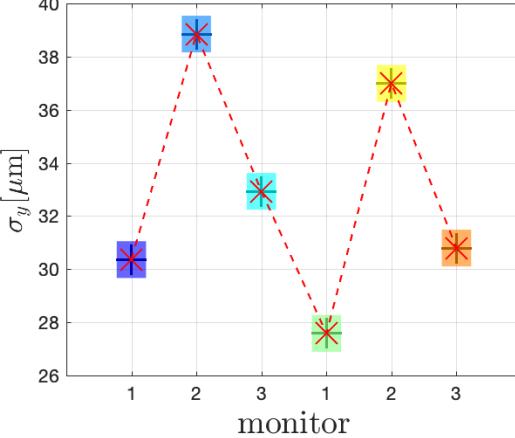
horizontal phase advances



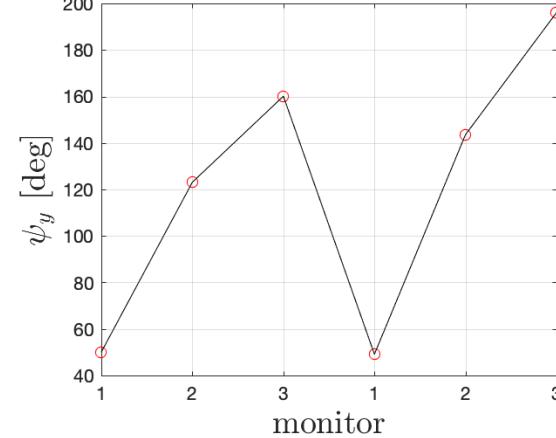
beta functions for all scan steps



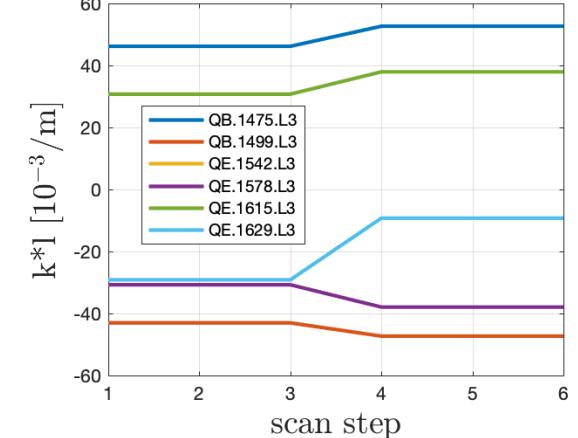
(Gaussian) normalised vertical phase space

(Gaussian) $\chi^2/N = 3.1762e - 06$ 

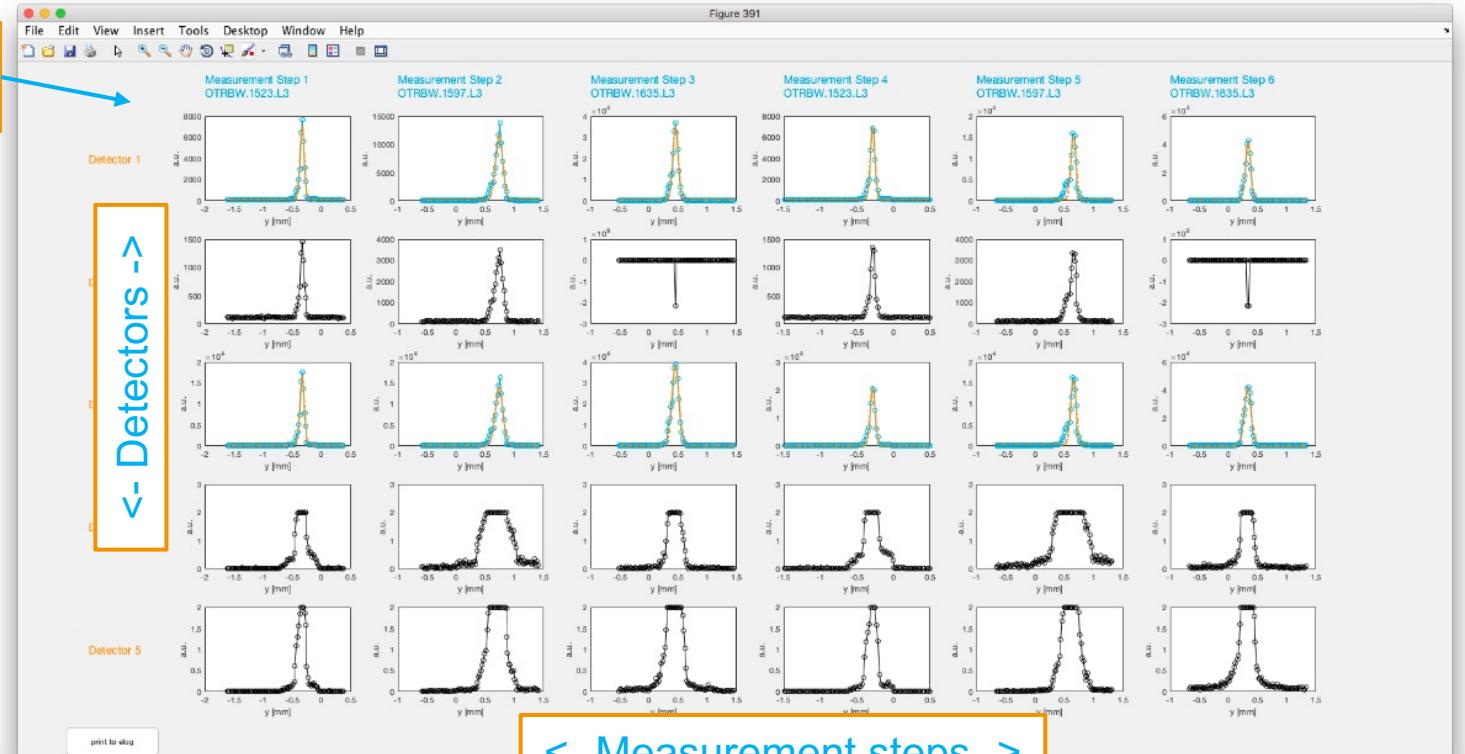
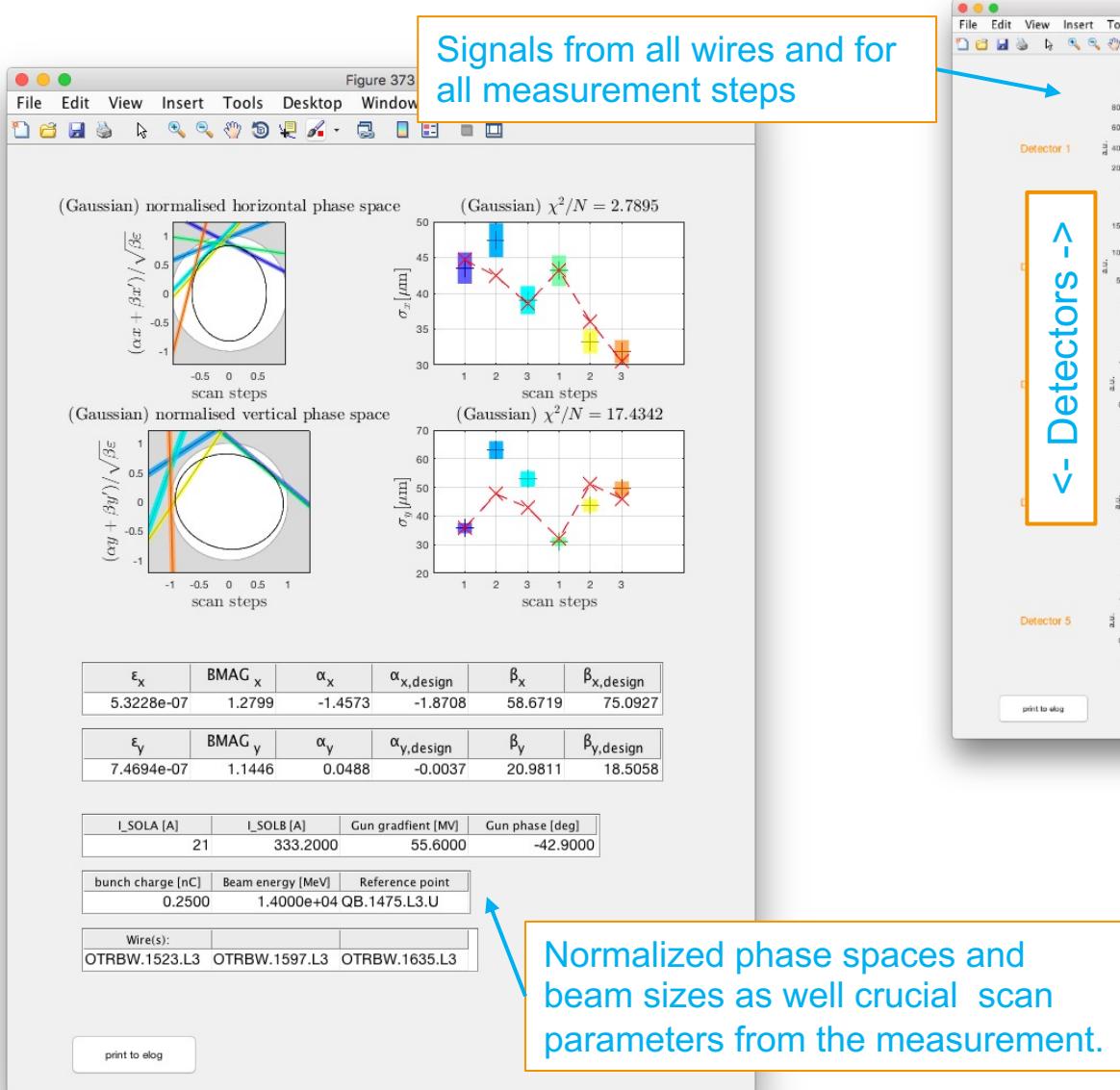
vertical phase advances



quad strengths

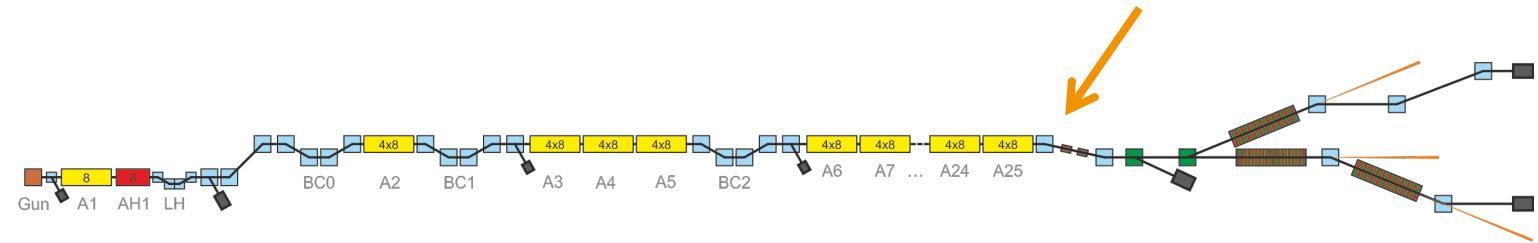


Measurement results for quad scans with wires

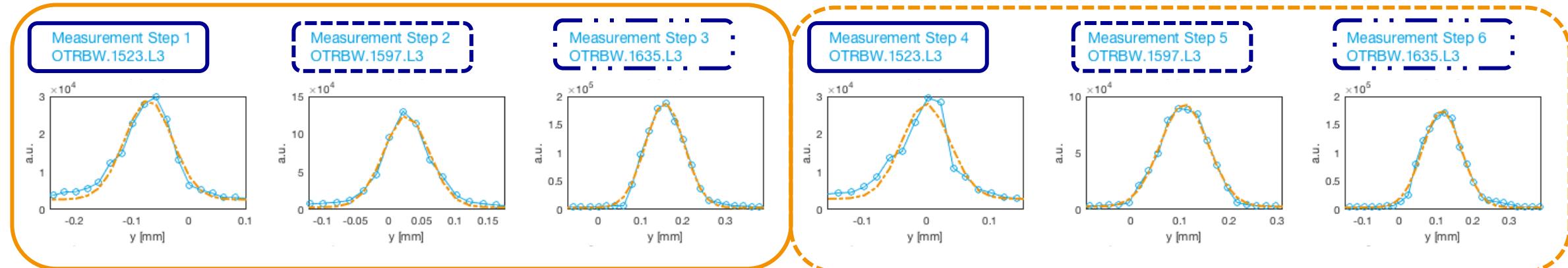


- Blue intensity traces indicate that the data from the respective detector is used for the evaluation.
- Thus, saturated signals should be presented in black, which means they are not considered in the evaluation.
- The upper plot is shown twice, one plot for each plane.

Beam optics measurements downstream L3



Electron beam profiles

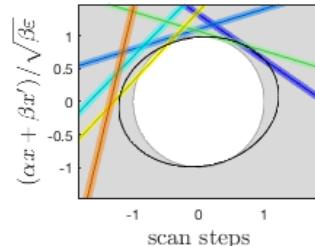
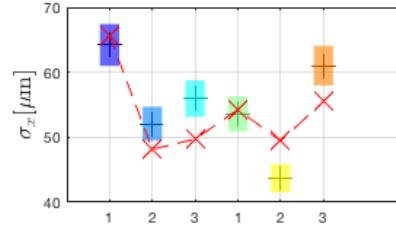


A quadrupole scan using :

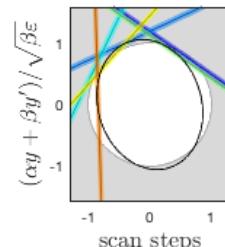
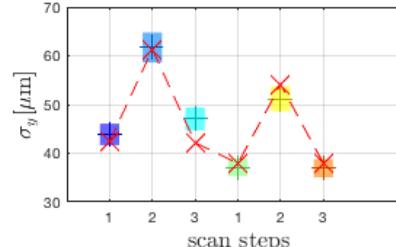
- Two different beam optics
- Three different wire scanners (or screen stations)

Optics matching in L3

(Gaussian) normalised horizontal phase space

(Gaussian) $\chi^2/N = 5.9099$ 

(Gaussian) normalised vertical phase space

(Gaussian) $\chi^2/N = 2.182$ 

ϵ_x	BMAG x	α_x	$\alpha_{x,design}$	β_x	$\beta_{x,design}$
1.2071e-06	1.2549	-2.7815	-2.1766	101.1636	81.8567

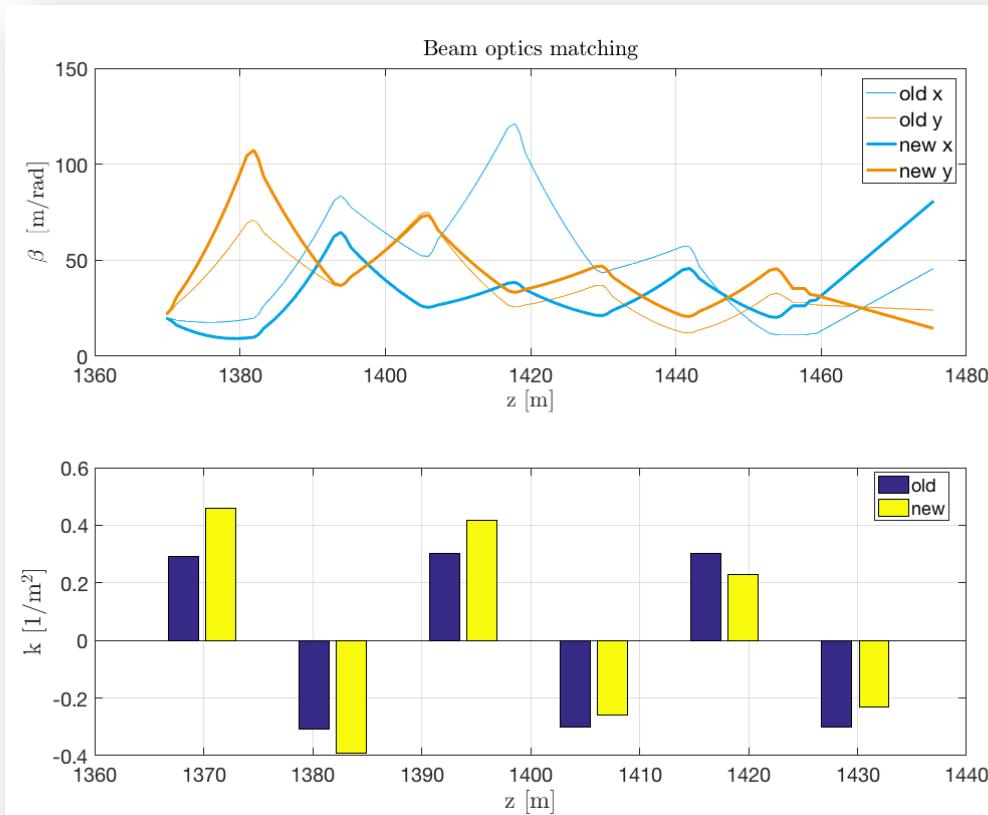
ϵ_y	BMAG y	α_y	$\alpha_{y,design}$	β_y	$\beta_{y,design}$
8.9710e-07	1.2806	0.1023	-0.0437	11.9247	14.4968

I_SOLA [A]	I_SOLB [A]	Gun gradfient [MV]	Gun phase [deg]
25.4000	349	56.9000	-39

bunch charge [nC]	Beam energy [MeV]	Reference point
0.2500	1.4001e+04	QB.1475.L3.U

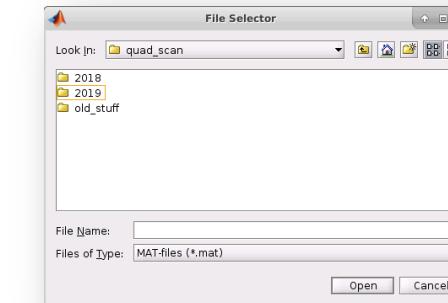
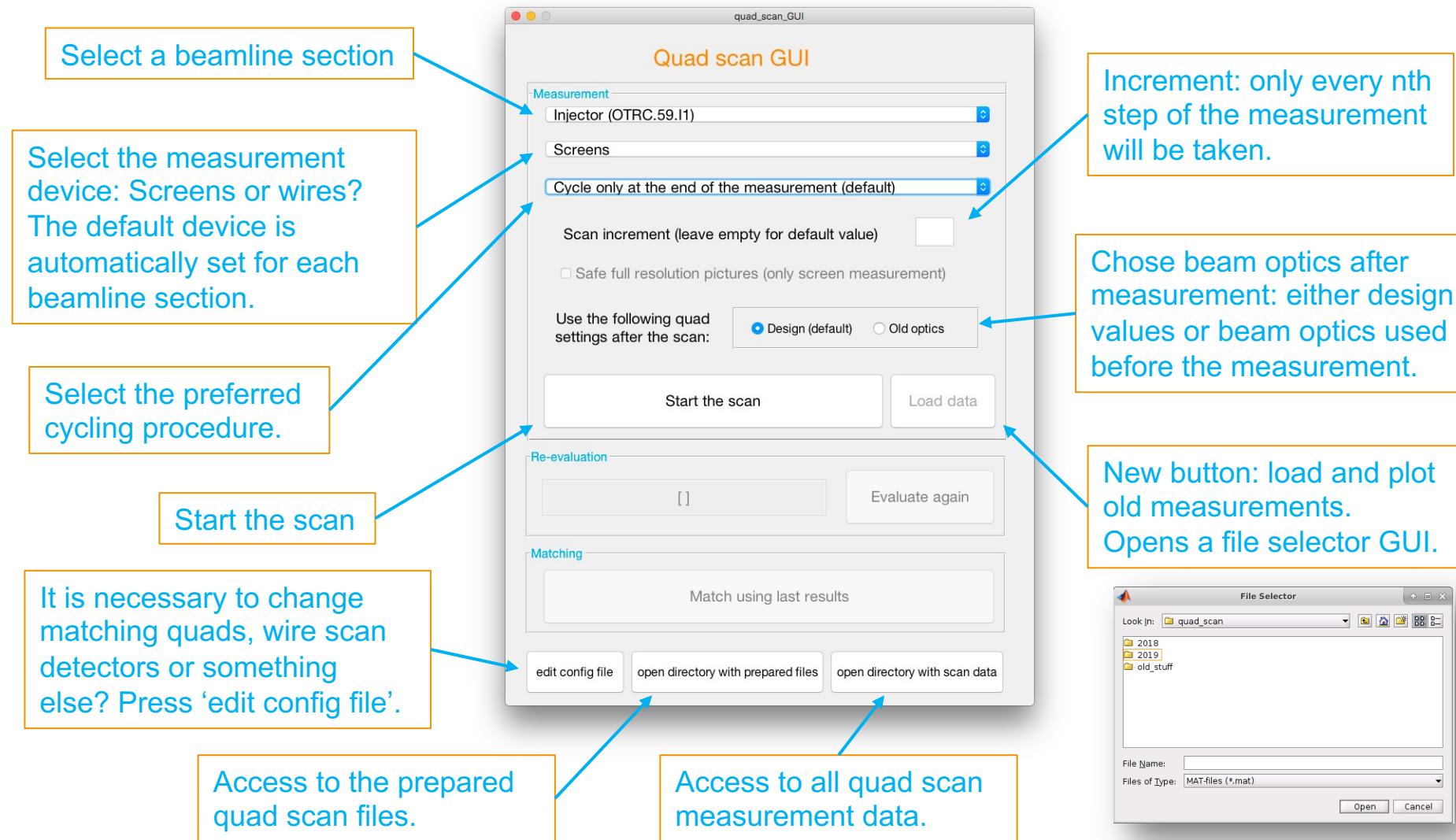
Wire(s):	OTRBW.1523.L3	OTRBW.1597.L3	OTRBW.1635.L3

- The beam optics measurement presentation is the same as for the screen measurements.
- The measurement result can be used to match the beam in L3.



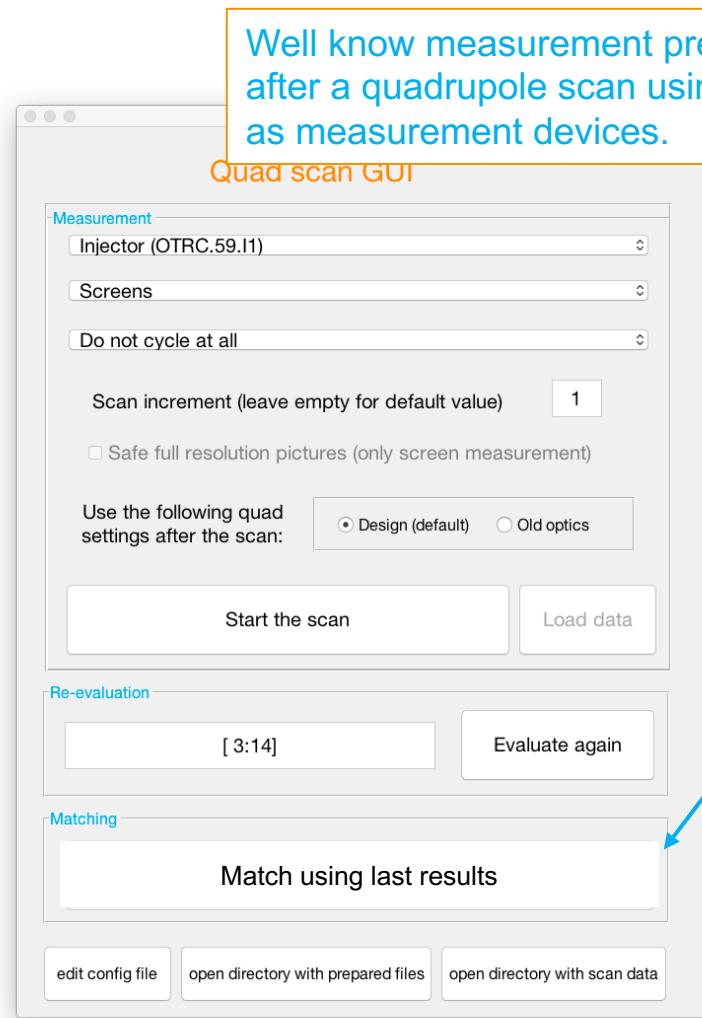
Multi quad scan GUI

Tools Advertising

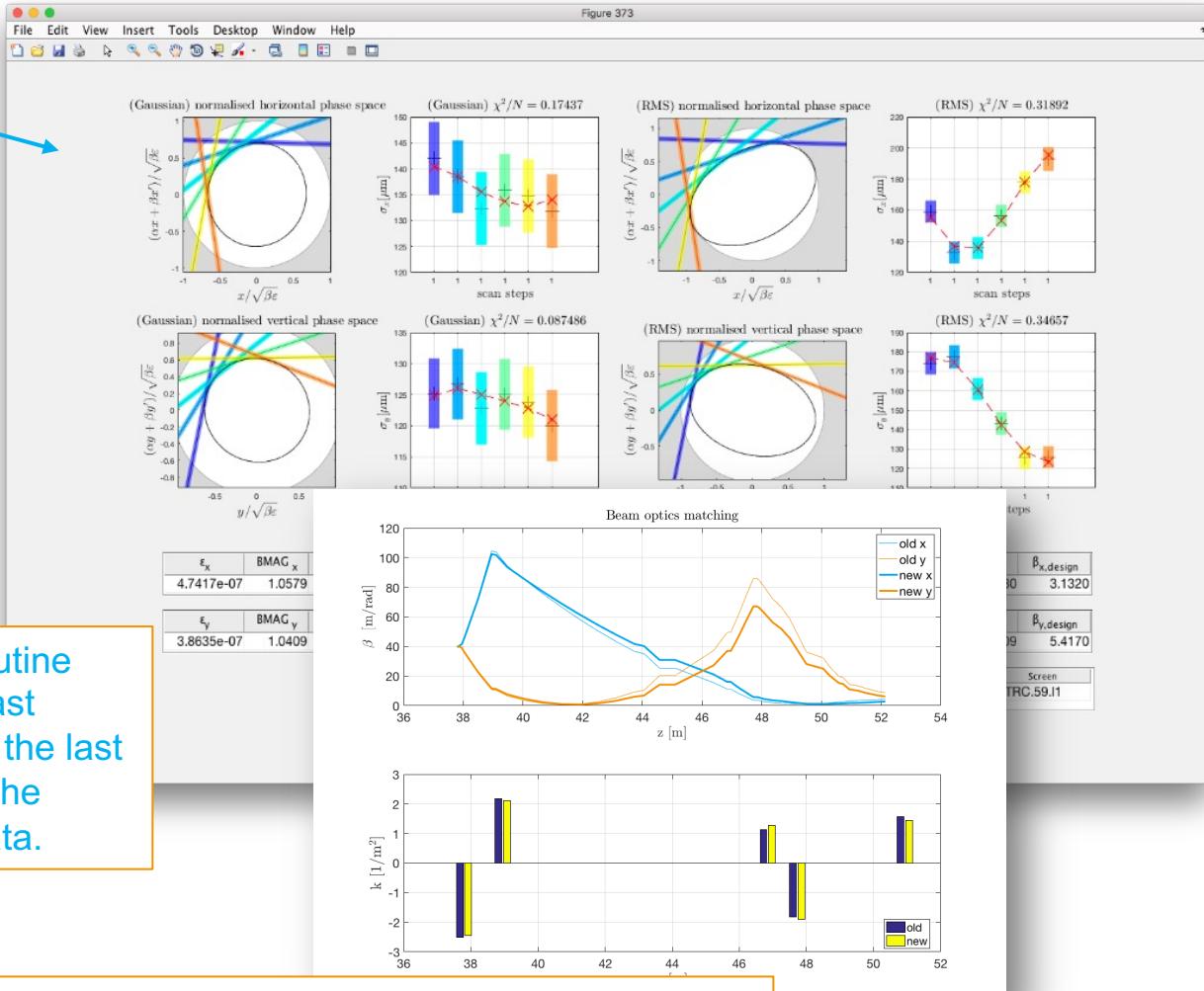


Measurement results for quad scans with screens

Tools Advertising



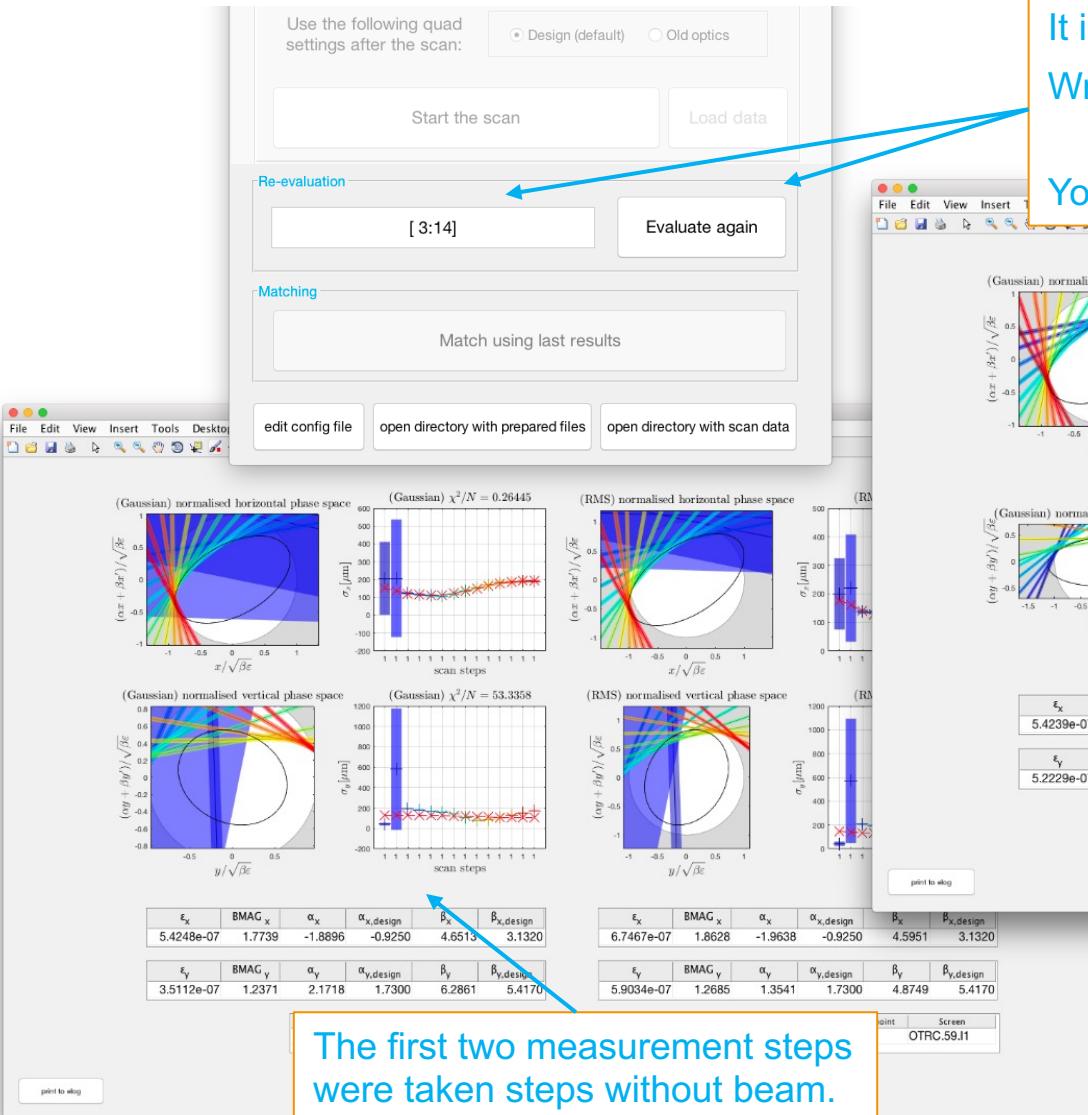
Well known measurement presentation after a quadrupole scan using screen as measurement devices.



The matching routine uses either the last measurement or the last re-evaluation of the measurement data.

Typical result after matching calculation. This plot is only shown if the algorithm found a solution.

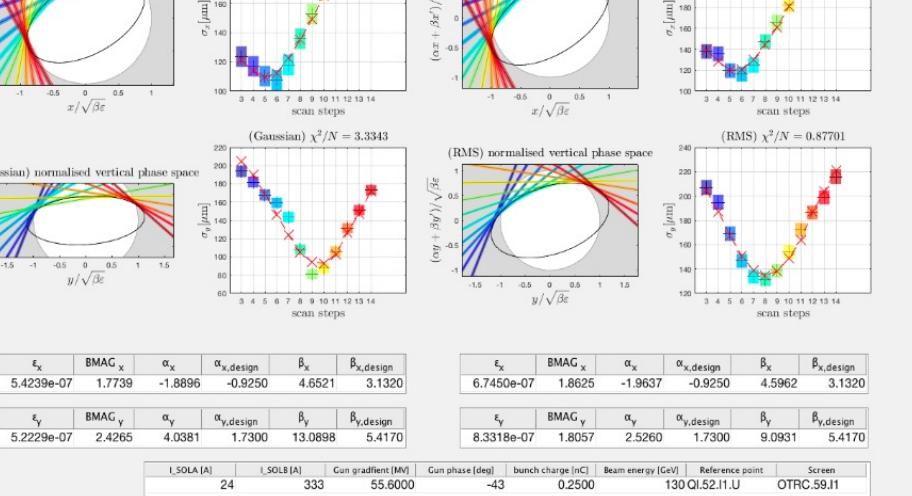
Deselecting single measurements



The first two measurement steps were taken steps without beam.

Tools Advertising

It is possible to evaluate only a selection of the taken data steps. Write all step numbers that should into that field and press 'Evaluate again'. You can use MATLAB type vector definitions like [3:7] = [3 4 5 6 7].



After deselecting the first two measurement steps

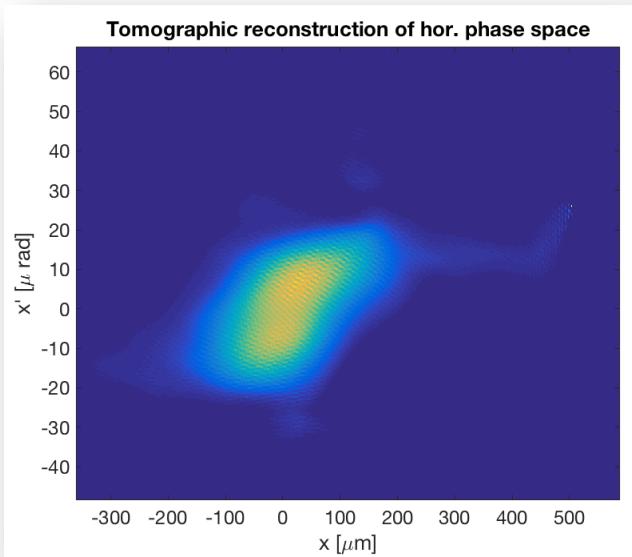
Be careful with the deselection of measurement steps and with the following evaluation of the data!

This functionality must only be used to deselect measurements steps that went clearly wrong (e.g. no beam).

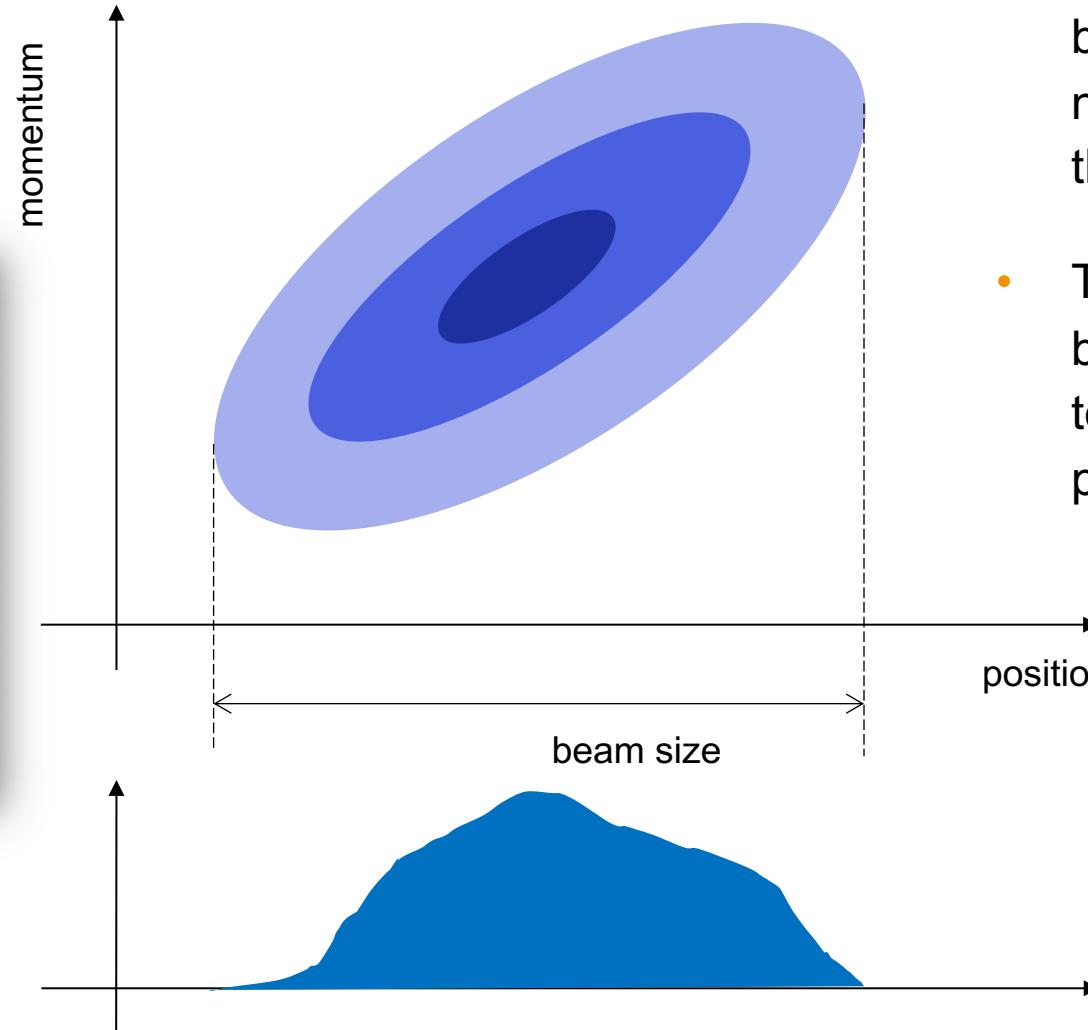
It must not be used to deselect 'unwanted' measurement steps to improve e.g. emittance size or beam optics matching!

Tomographic reconstruction of transverse phase spaces

Tomographic reconstruction of the horizontal phase space for the center slice.

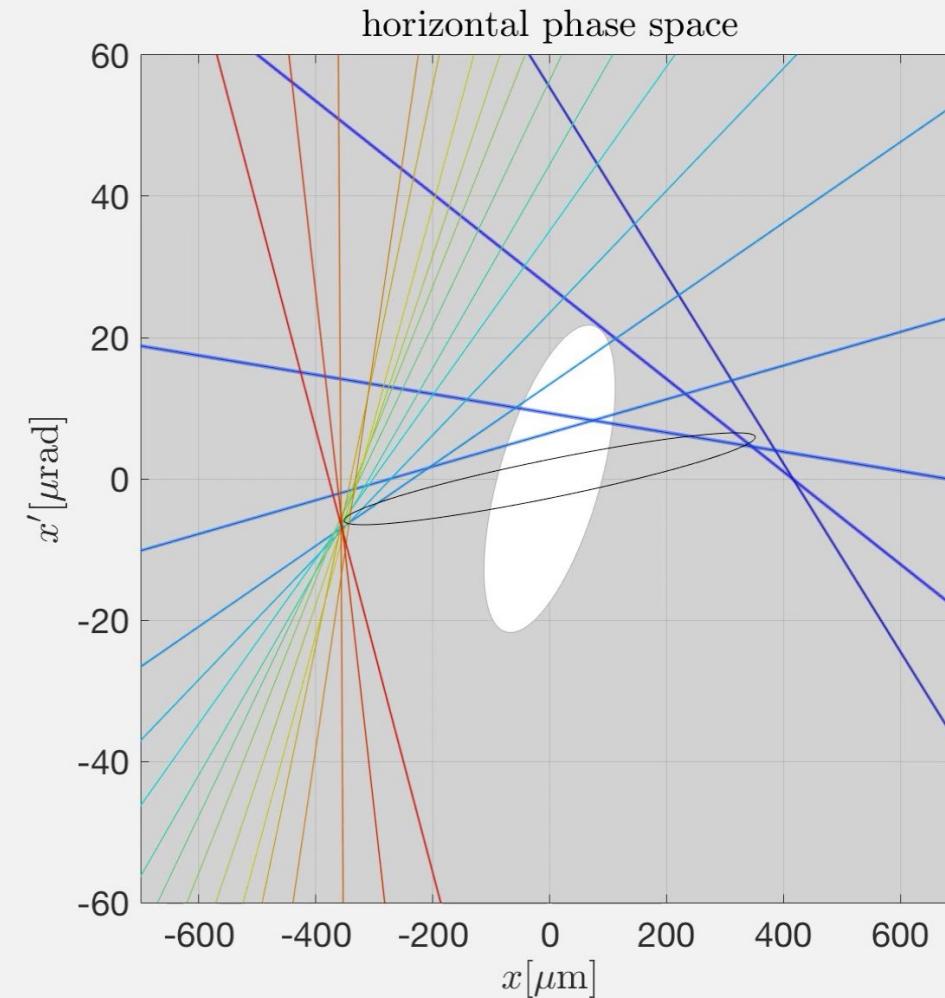
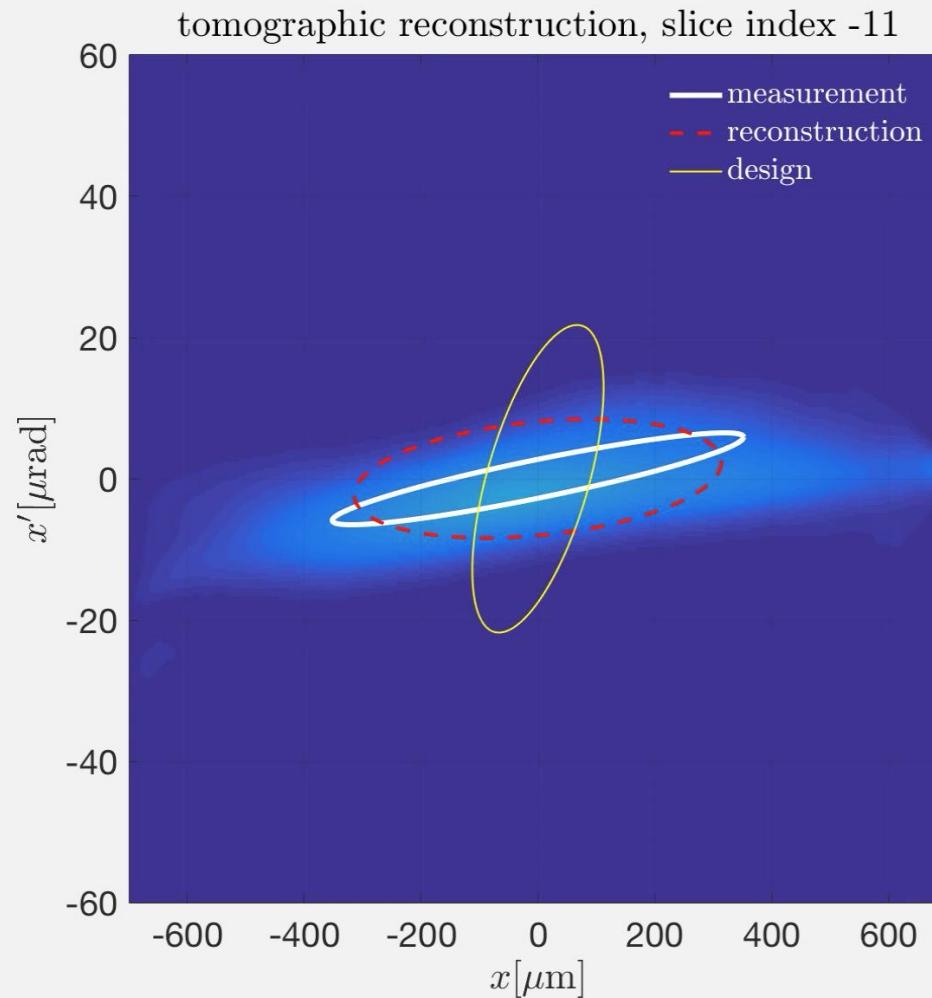


European XFEL

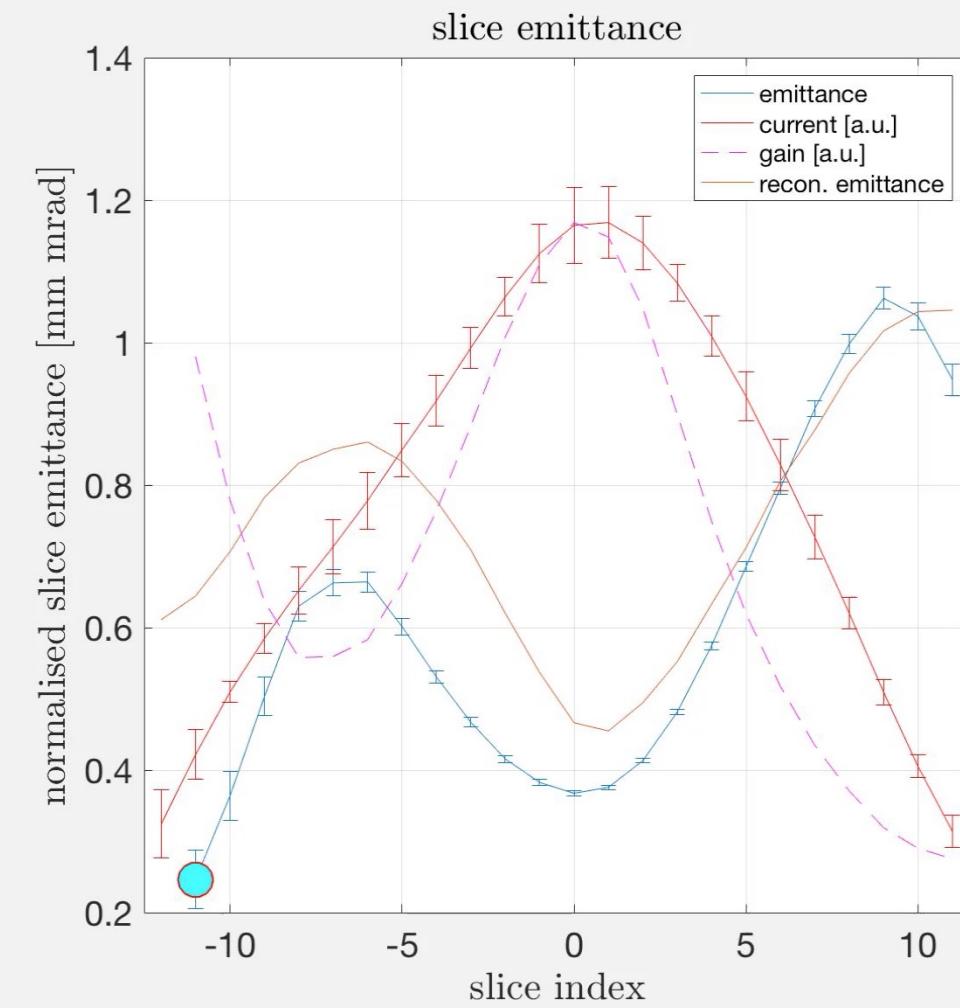
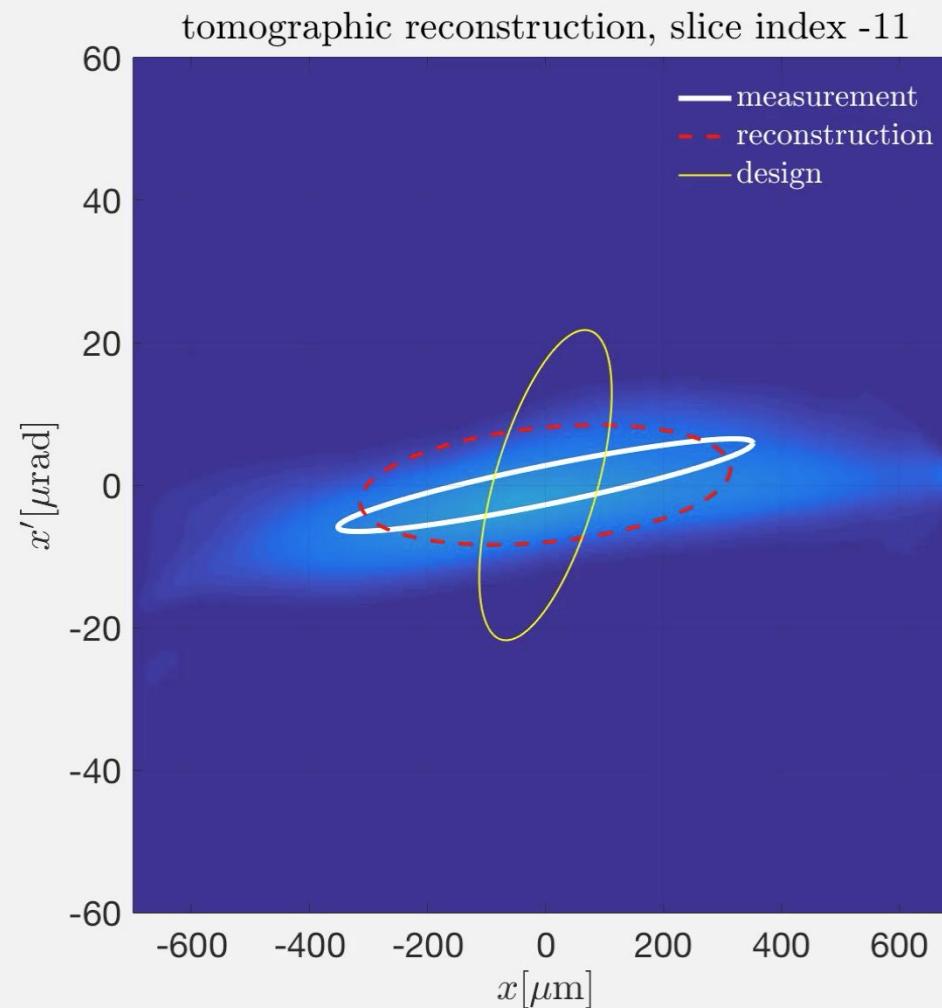


- Even more information about the beam can be obtained by using not only the beam sizes but also the profiles.
- The transverse phase spaces can be reconstructed using a tomographic algorithm and the profiles from different 'angles'.

Tomographic reconstruction of the hor. phase space using a quad scan



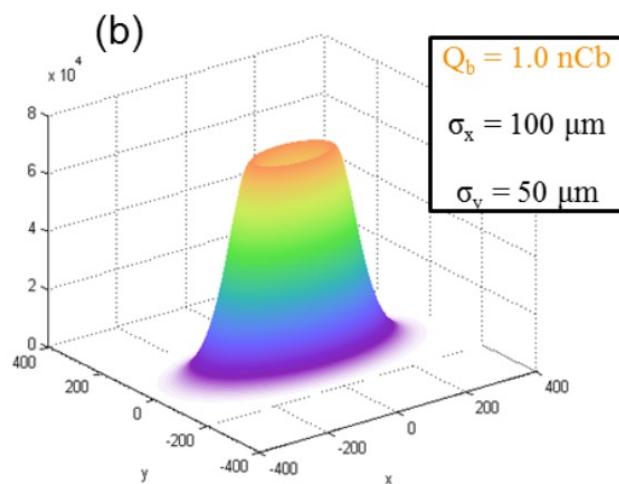
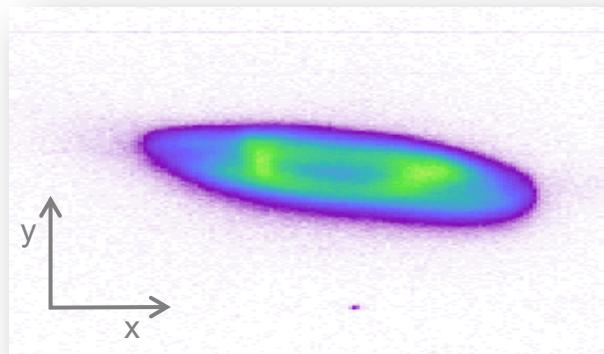
Tomographic reconstruction of the hor. phase space using a quad scan



EuXFEL

Lyo screens

- It turned out that measured emittances sizes depended on the beam size on the screens.
- In addition, the beam spots one the screens were not gaussian shaped but looked like smoke rings.



- It was not clear if the beam looks like that or if the LYSO screens can not display the bunches correctly.
- No other screens were available in the machine.

- It turned out that it was a quenching effect of the scintillators.
- That effect could be reproduced in simulations.
- Most of the screens have been or will be replaced with YAP or GGAG.

