

# Simulating axion electrodynamics near pulsars

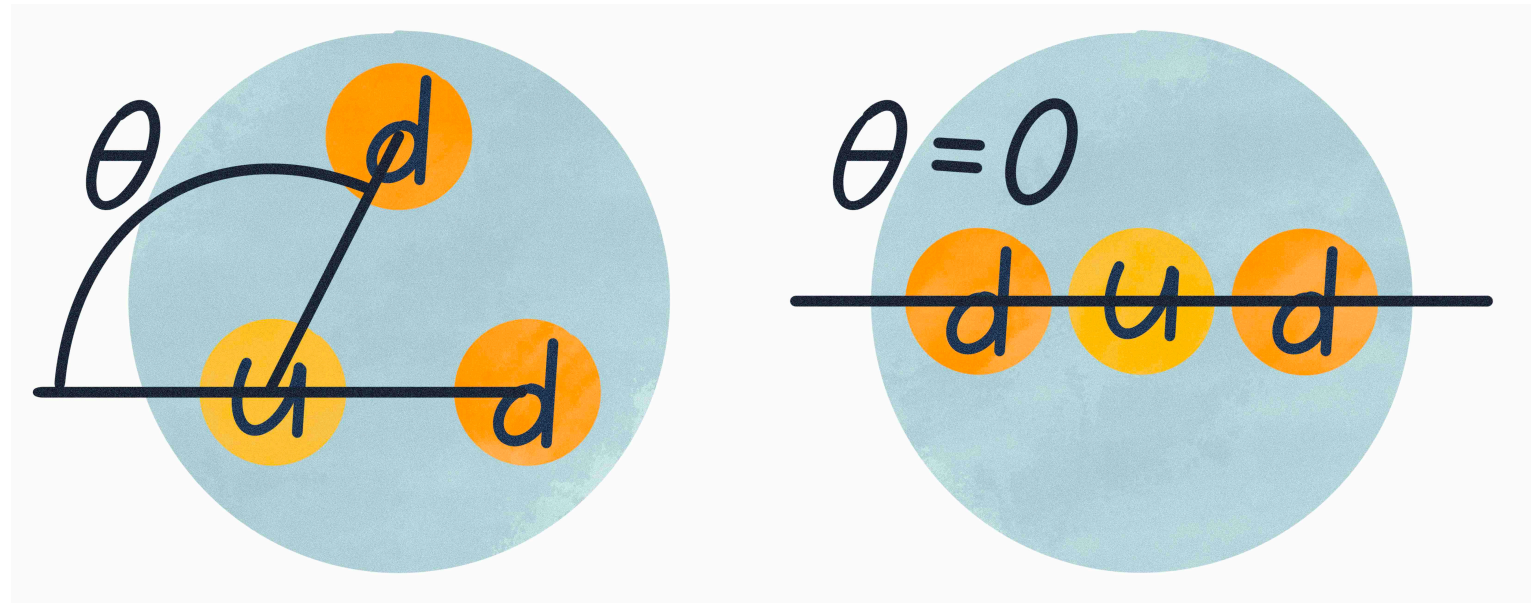
**DESY Theory Workshop**

Anne Freise



# Briefly: The axion

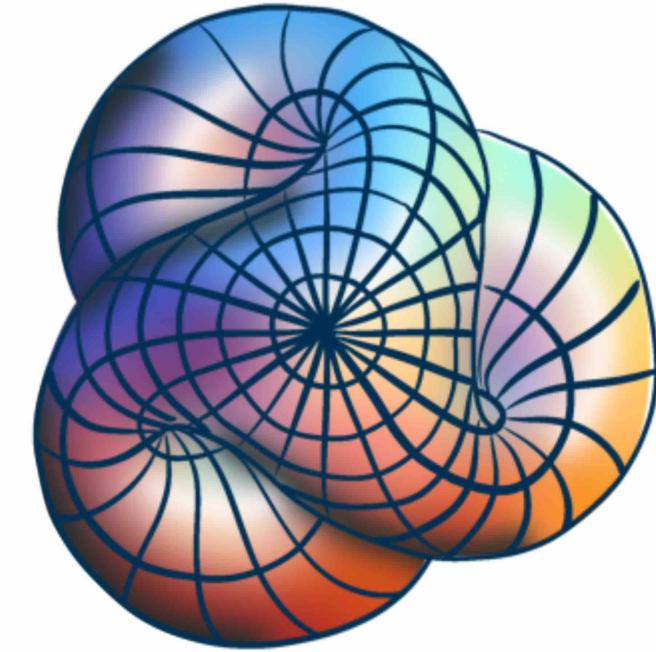
## Motivation for axions:



Strong CP-Problem



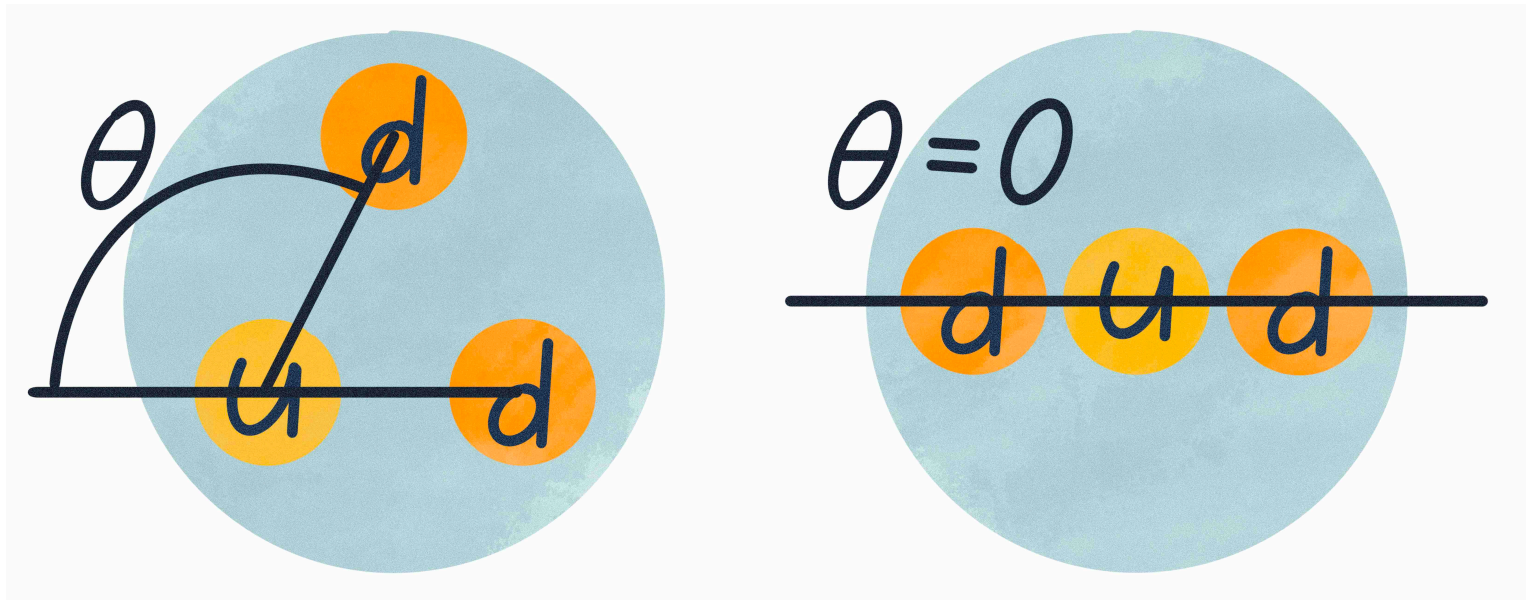
Dark matter



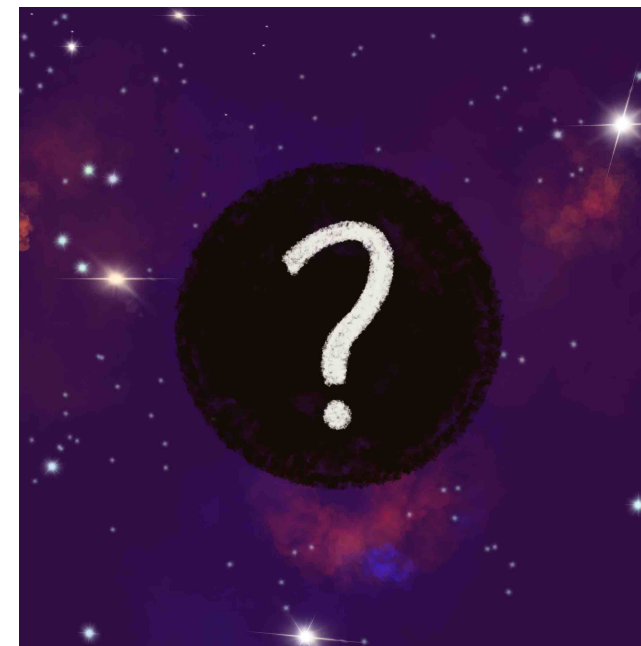
ALPs from UV theories

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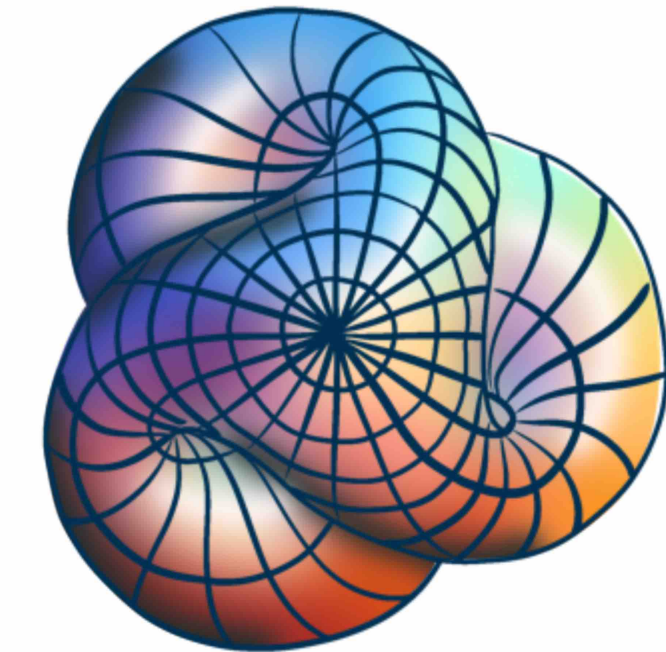
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ALPs from UV theories

## Axion couple to EM:

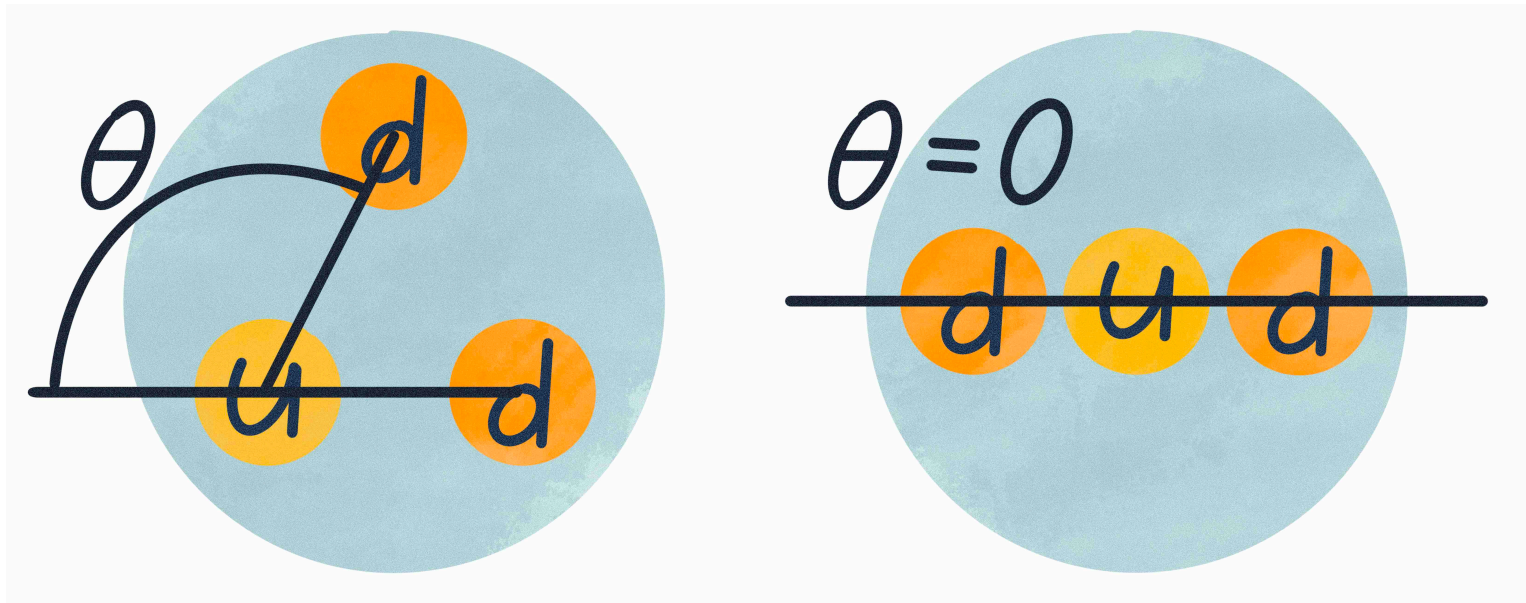
$$g_{a\gamma\gamma} a F_{\mu\nu} \tilde{F}^{\mu\nu}$$

$$\begin{aligned}\nabla \cdot \vec{E} &= \rho_e - g_{a\gamma\gamma} \nabla a \cdot \vec{B} \\ \nabla \times \vec{B} - \frac{\partial \vec{E}}{\partial t} &= \vec{J} + g_{a\gamma\gamma} \frac{\partial a}{\partial t} \vec{B} + g_{a\gamma\gamma} \nabla a \times \vec{E}\end{aligned}$$

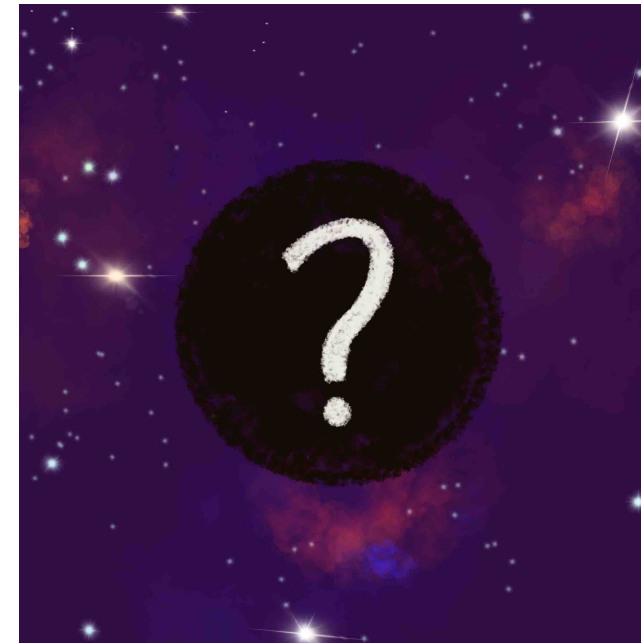


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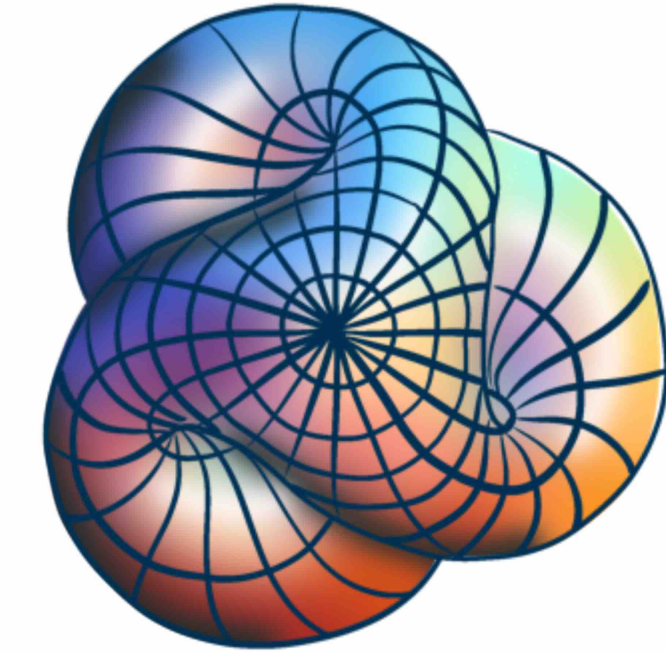
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## Axion couple to EM:

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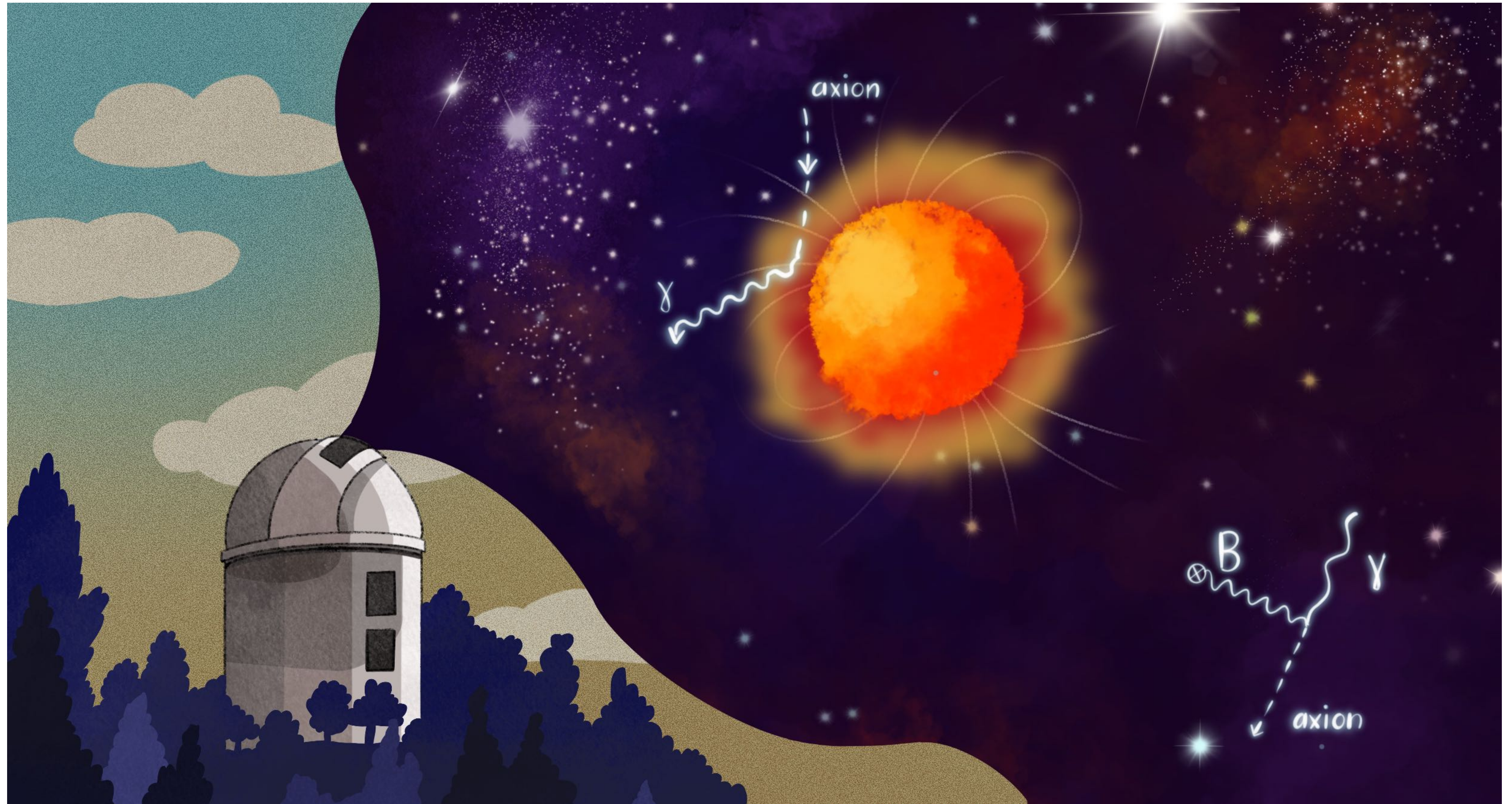
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Axon-induced charge density

Axon-induced current density



# Searches for axions via coupling to photons





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But what if the contribution to Maxwell's equations are non-perturbative?

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Large axion gradient

axion



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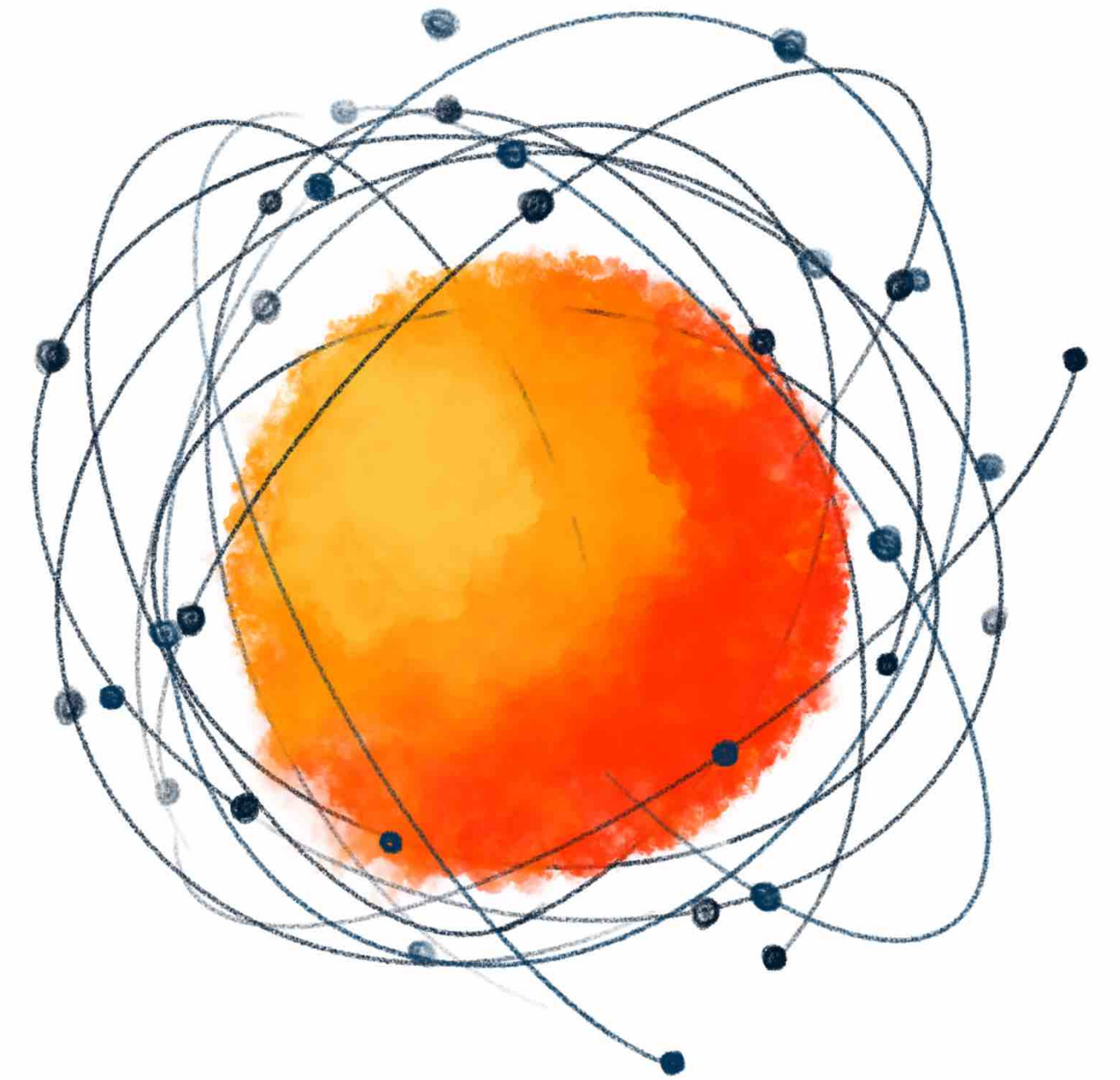
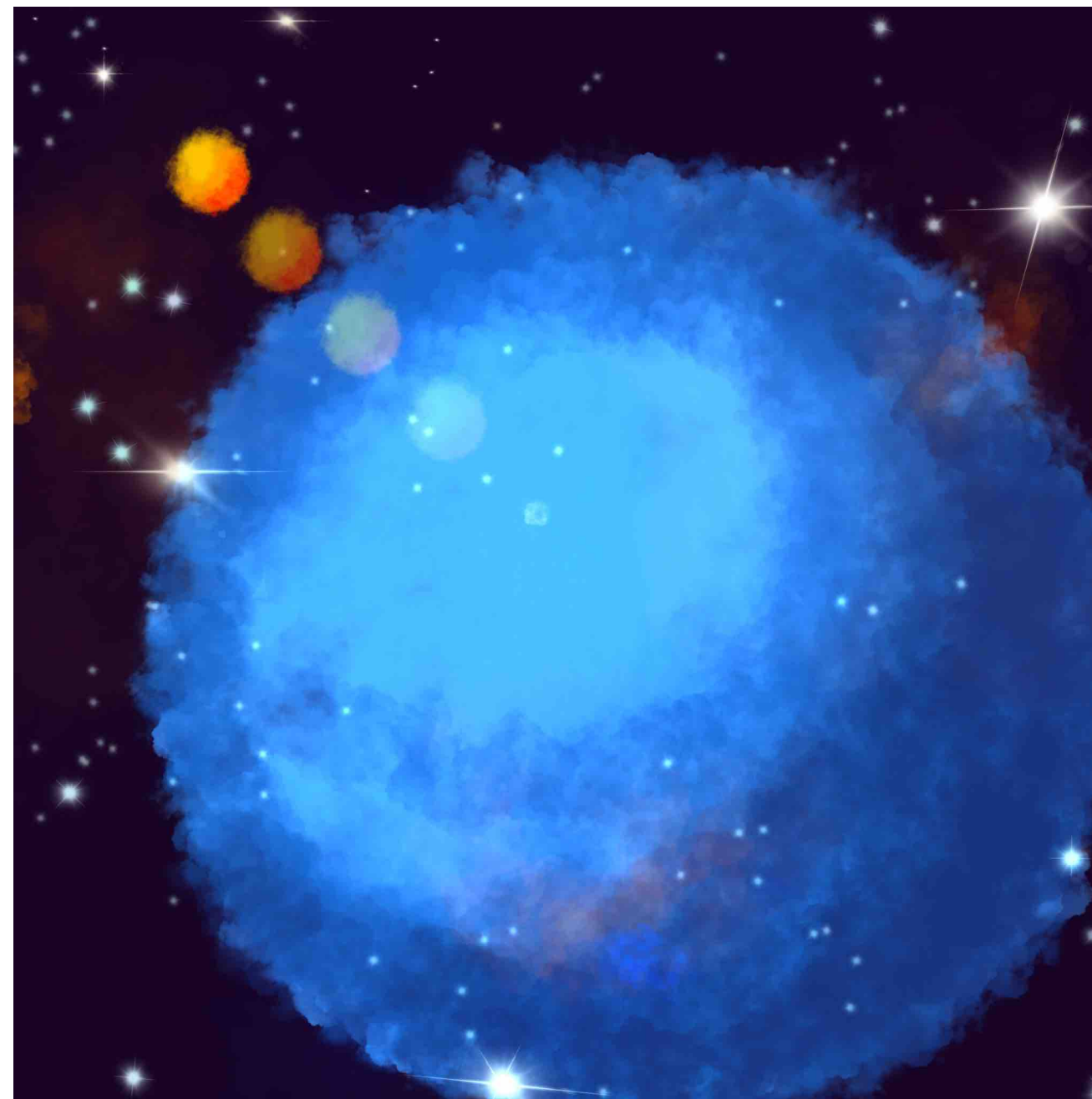
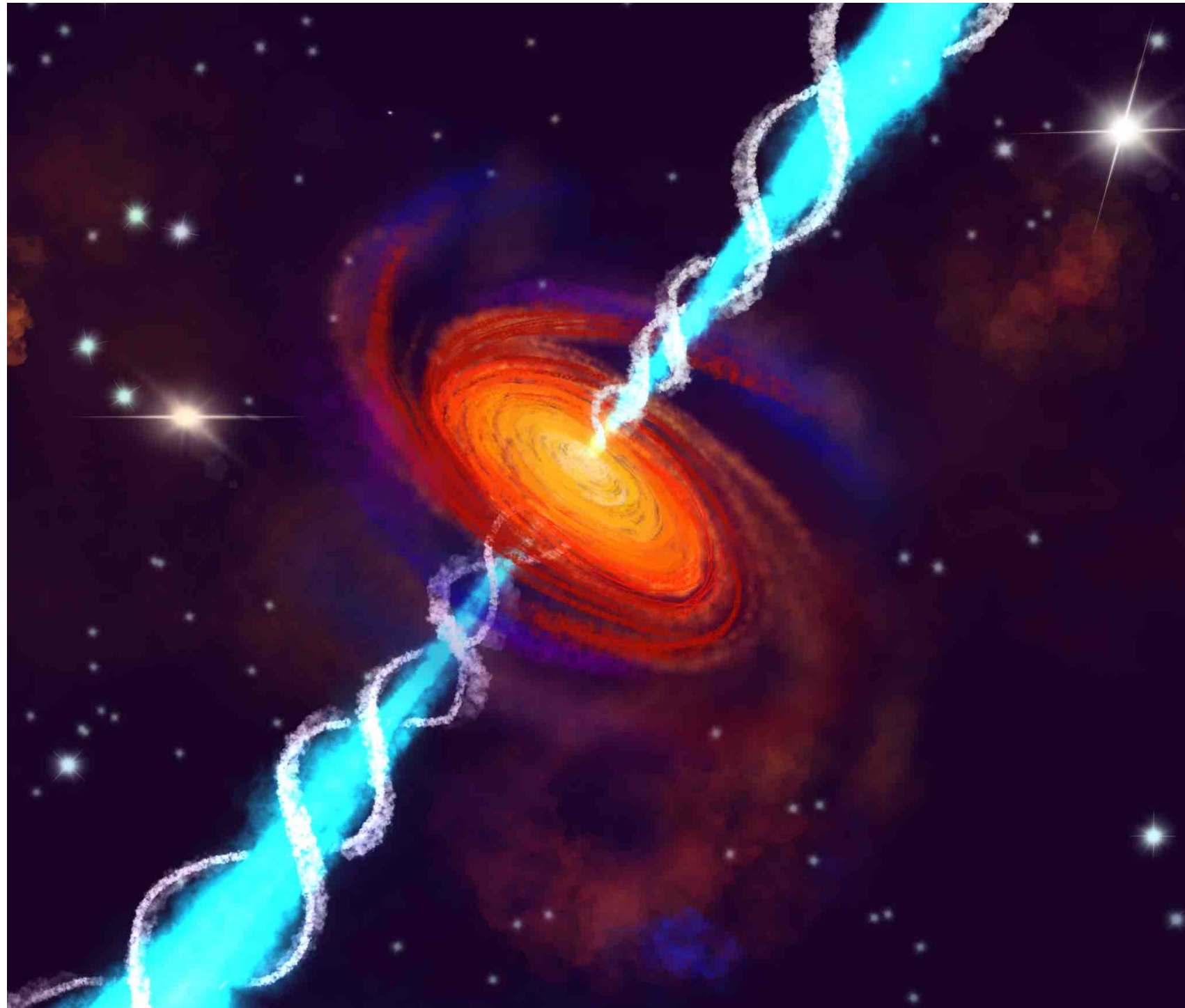
$E \ll B$

Large axion gradient

axion



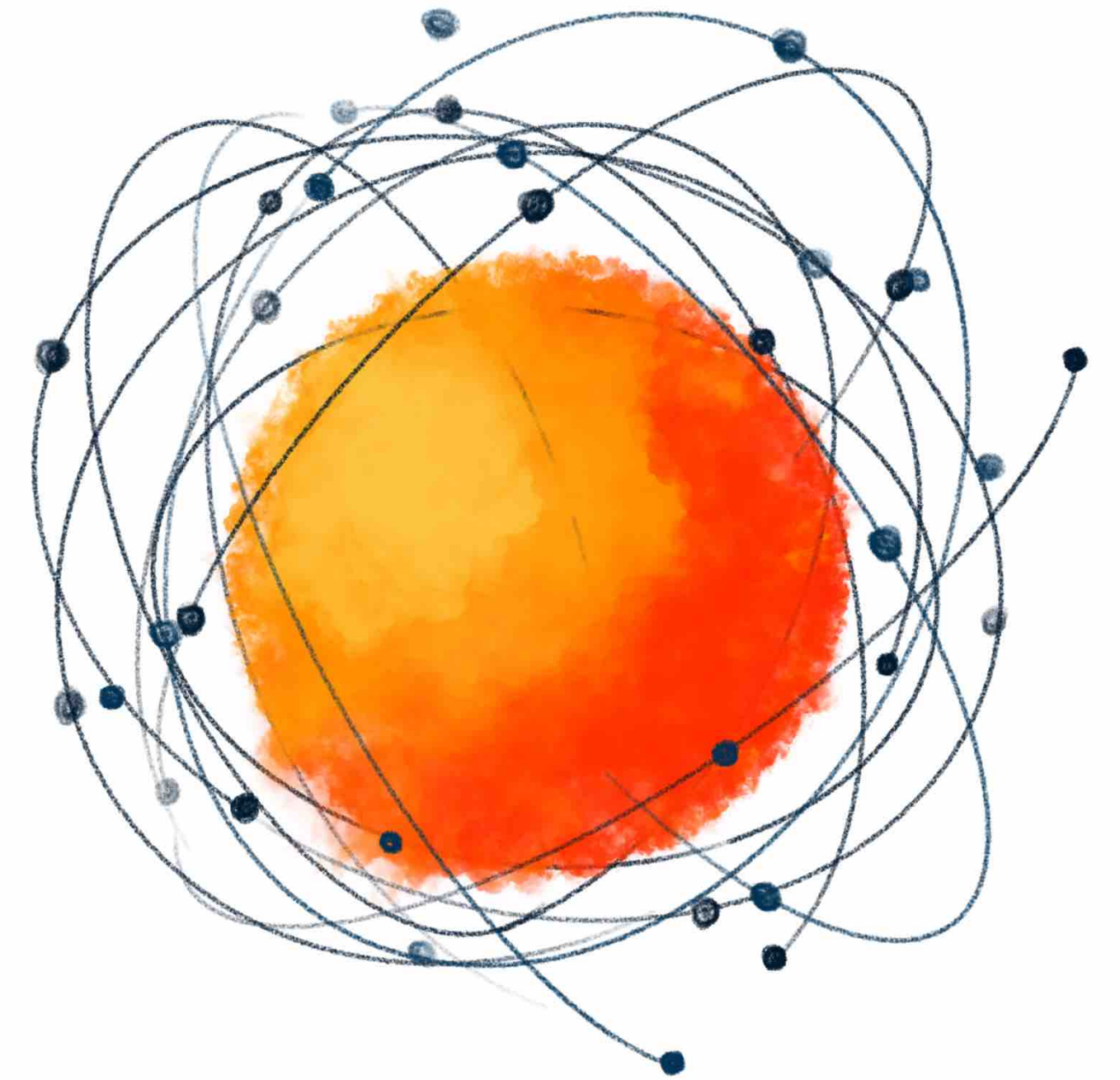
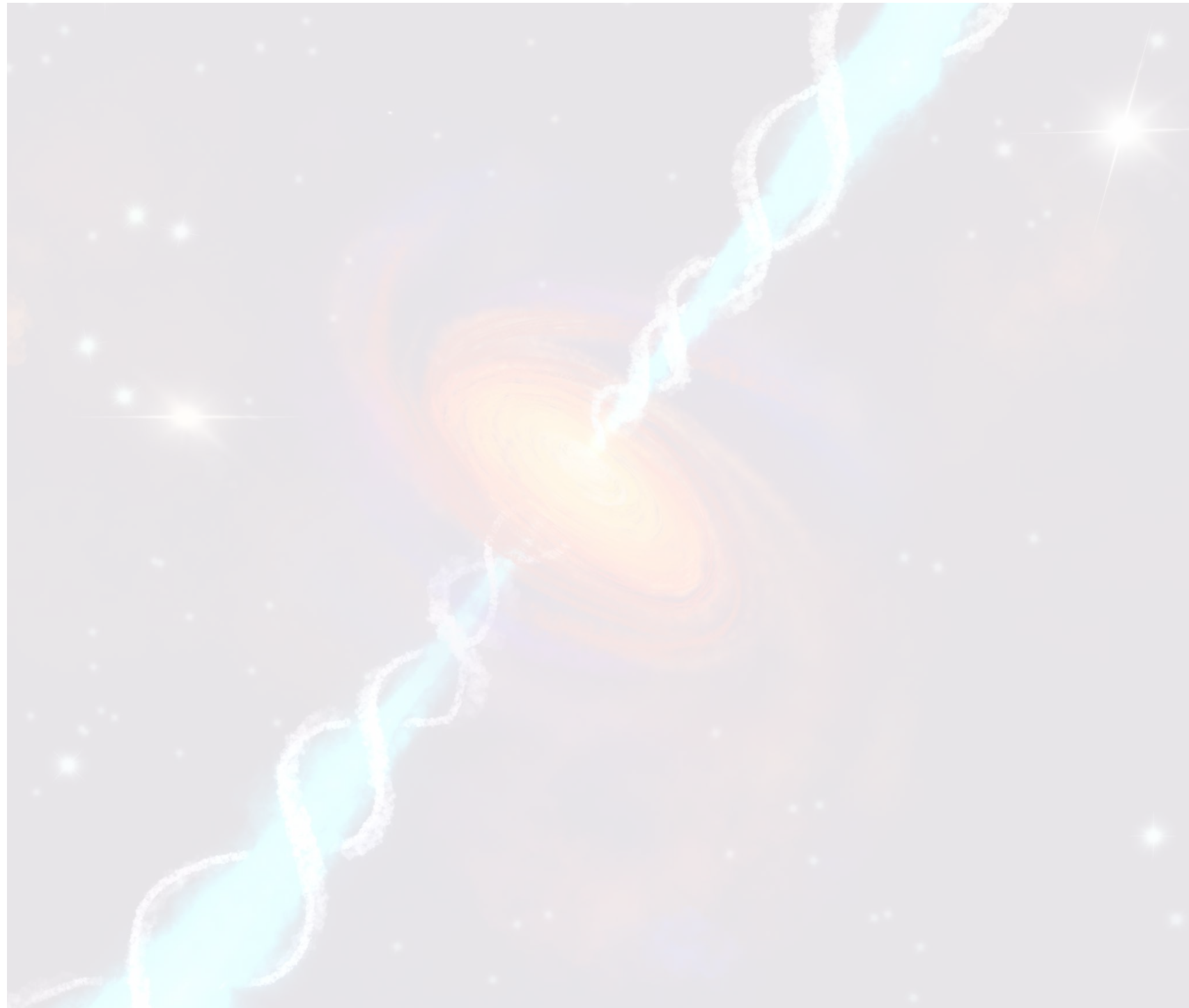
# Non-perturbative axion electrodynamics: Black holes, axion stars and axion clouds





# Non-perturbative axion electrodynamics:

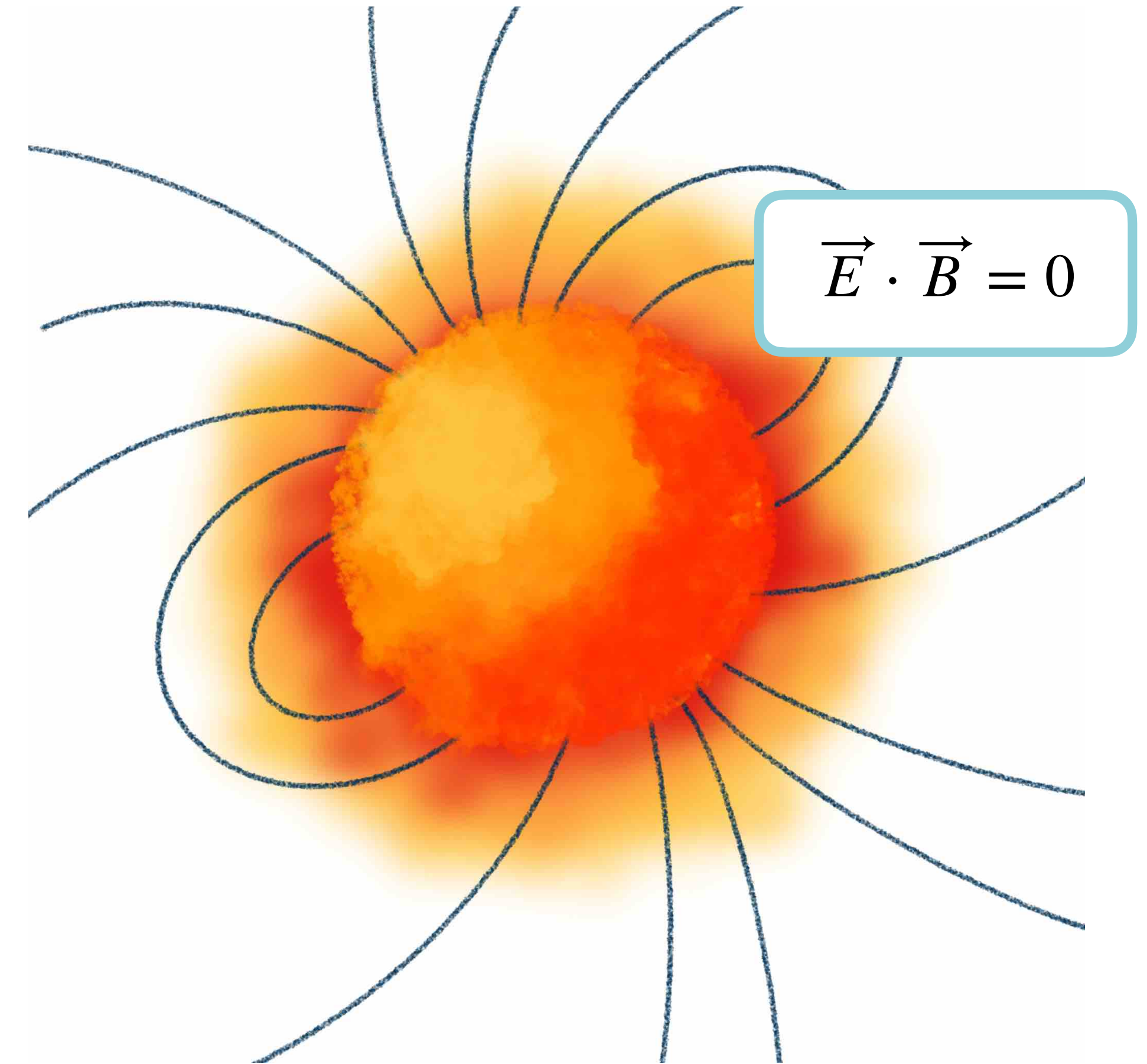
## Black holes, axion stars and **axion clouds**





# Briefly: Neutron stars

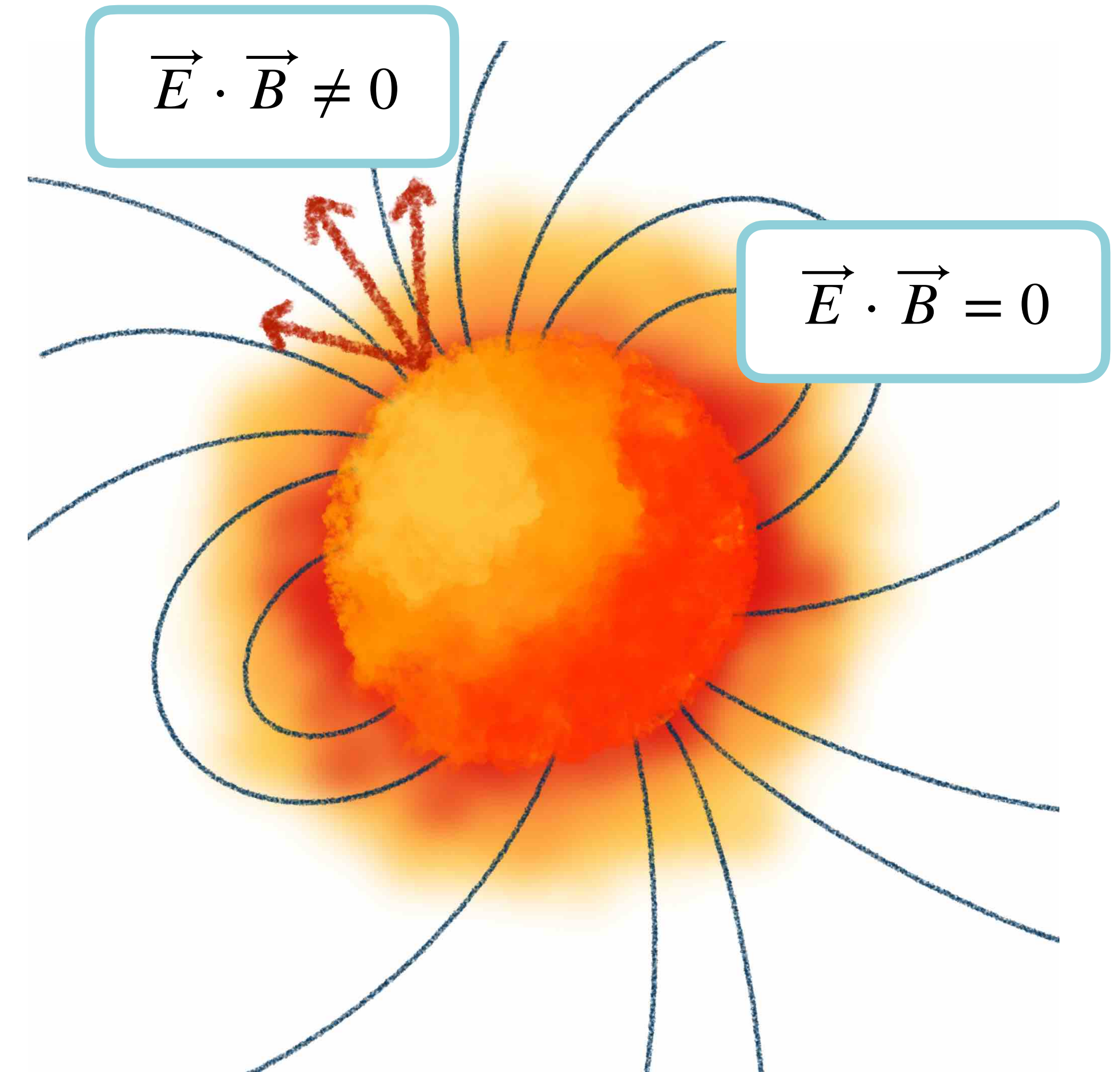
- **Neutron star** = rotating ideal conductor
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- Equilibrium configuration with  $\vec{E} \cdot \vec{B} = 0$





# Briefly: Neutron stars

- **Neutron star** = rotating ideal conductor
  - Dipolar magnetic field and plasma-filled magnetosphere
  - Equilibrium configuration with  $\vec{E} \cdot \vec{B} = 0$
- But we observe pulsar emission
- Have localised region with **unscreened electromagnetic** fields (responsible for emission)





# Axion production in vacuum gaps

Polar cap

Parallel E-field  $E_{\parallel}$

200

0

-200

Neutron star

Fluctuations in  $(\vec{E} \cdot \vec{B})$  produce axions

Figure credit: Ashley Bransgrove



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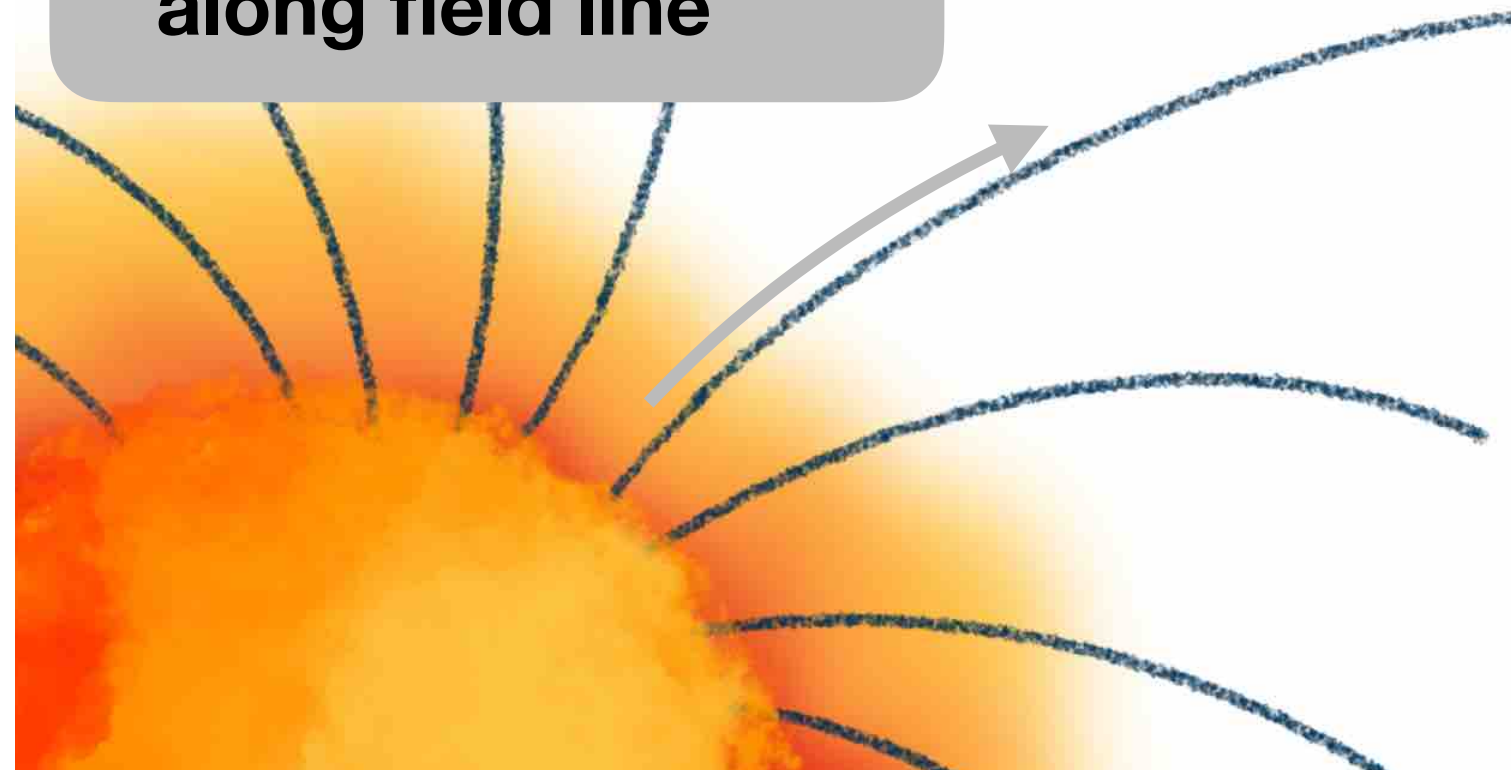
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Figure credit: Ashley Bransgrove



# Unscreened region: 1d example

Charges travelling  
along field line



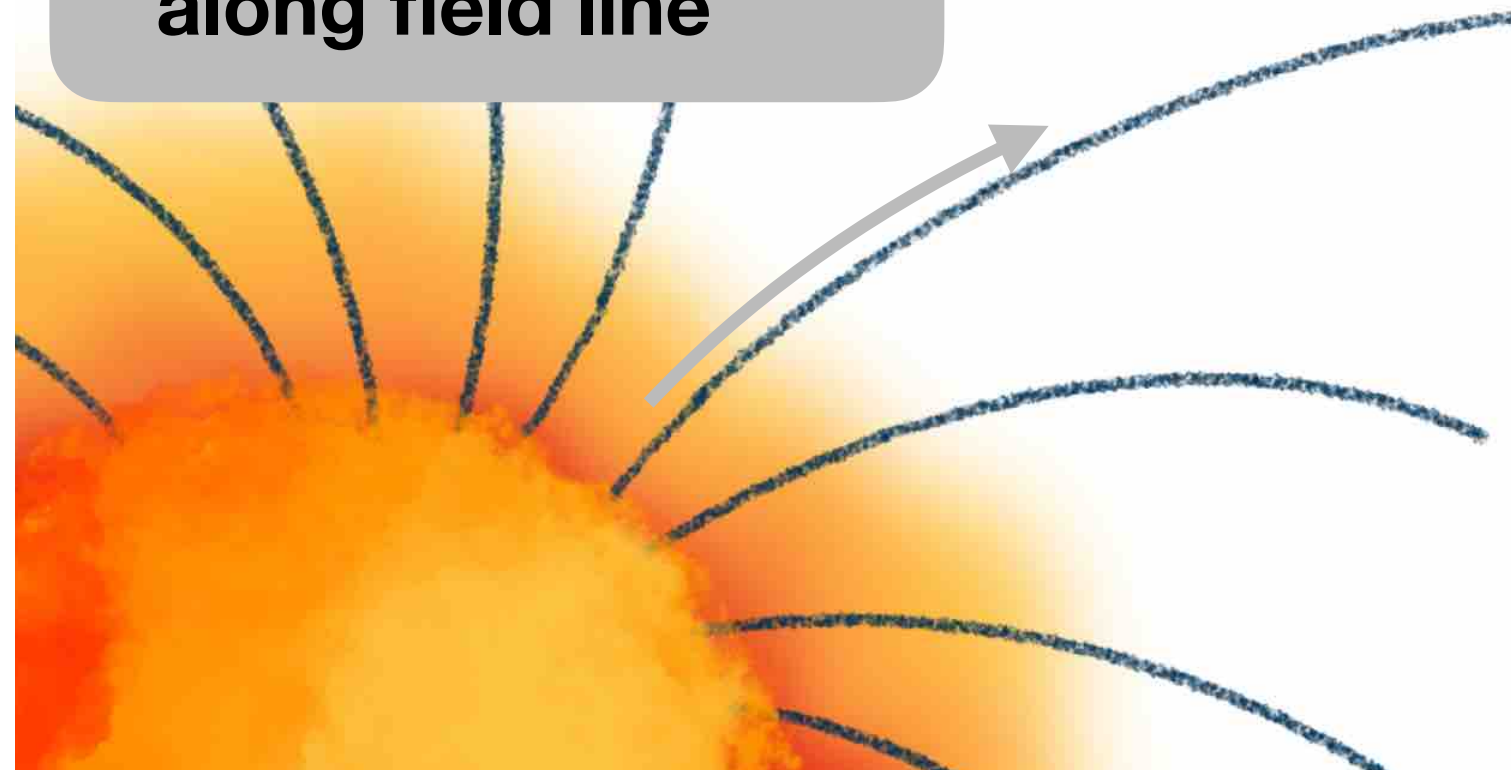
Evolution of charges:  $\frac{dE}{dx} = -(\rho - \rho_{GJ})$

- **Current supplied** to sustain twist in the magnetic field lines  $j_m = \nabla \times B$



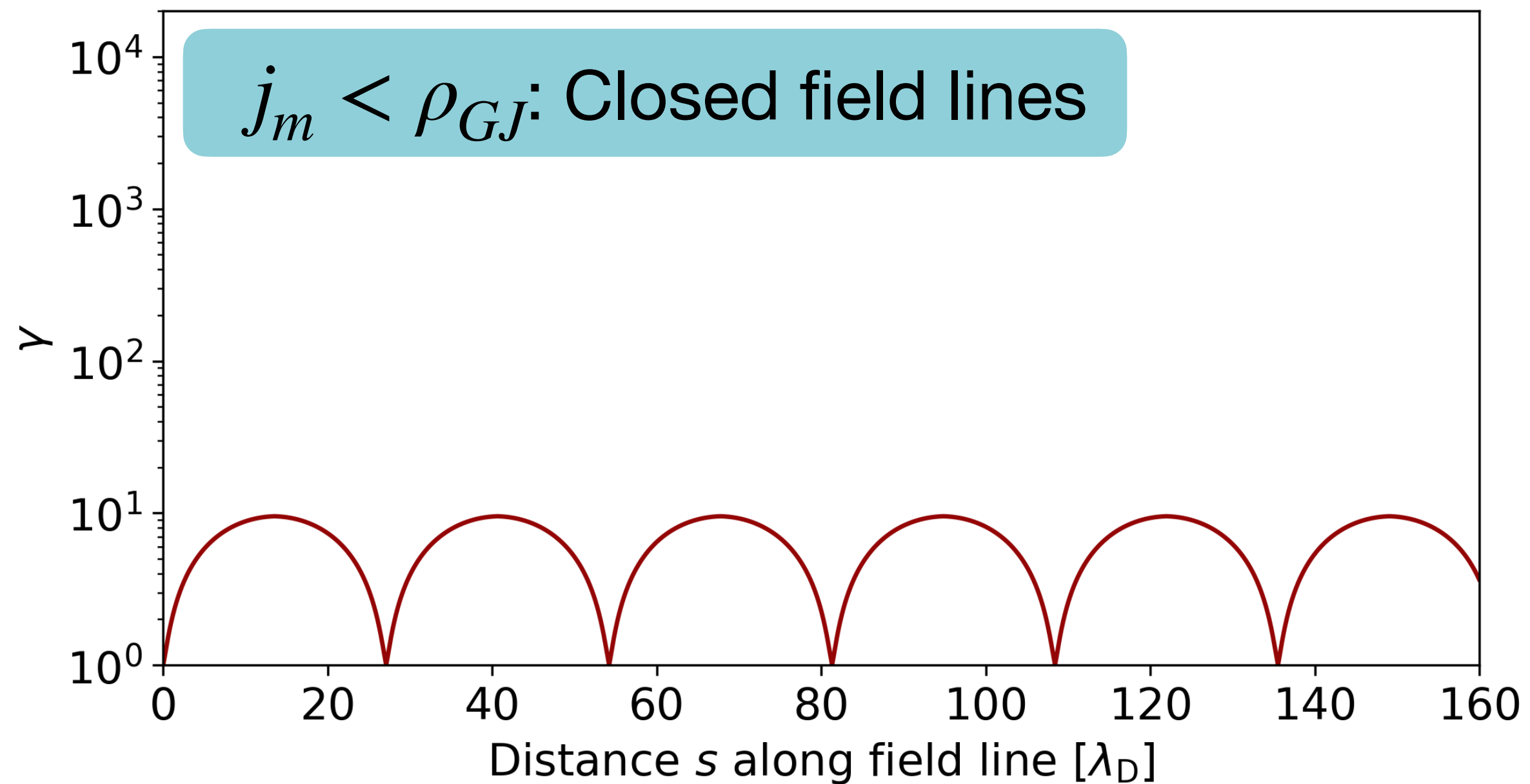
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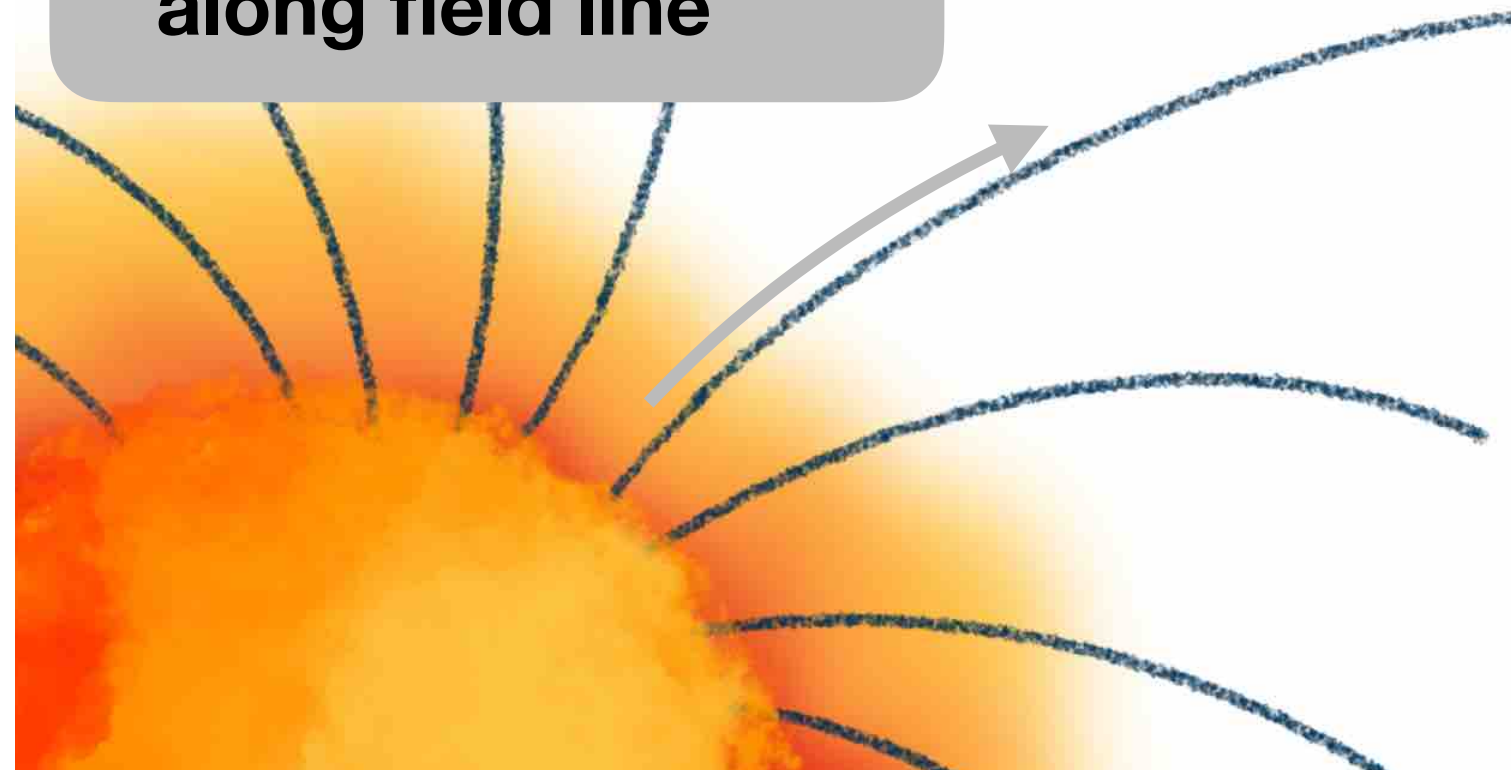
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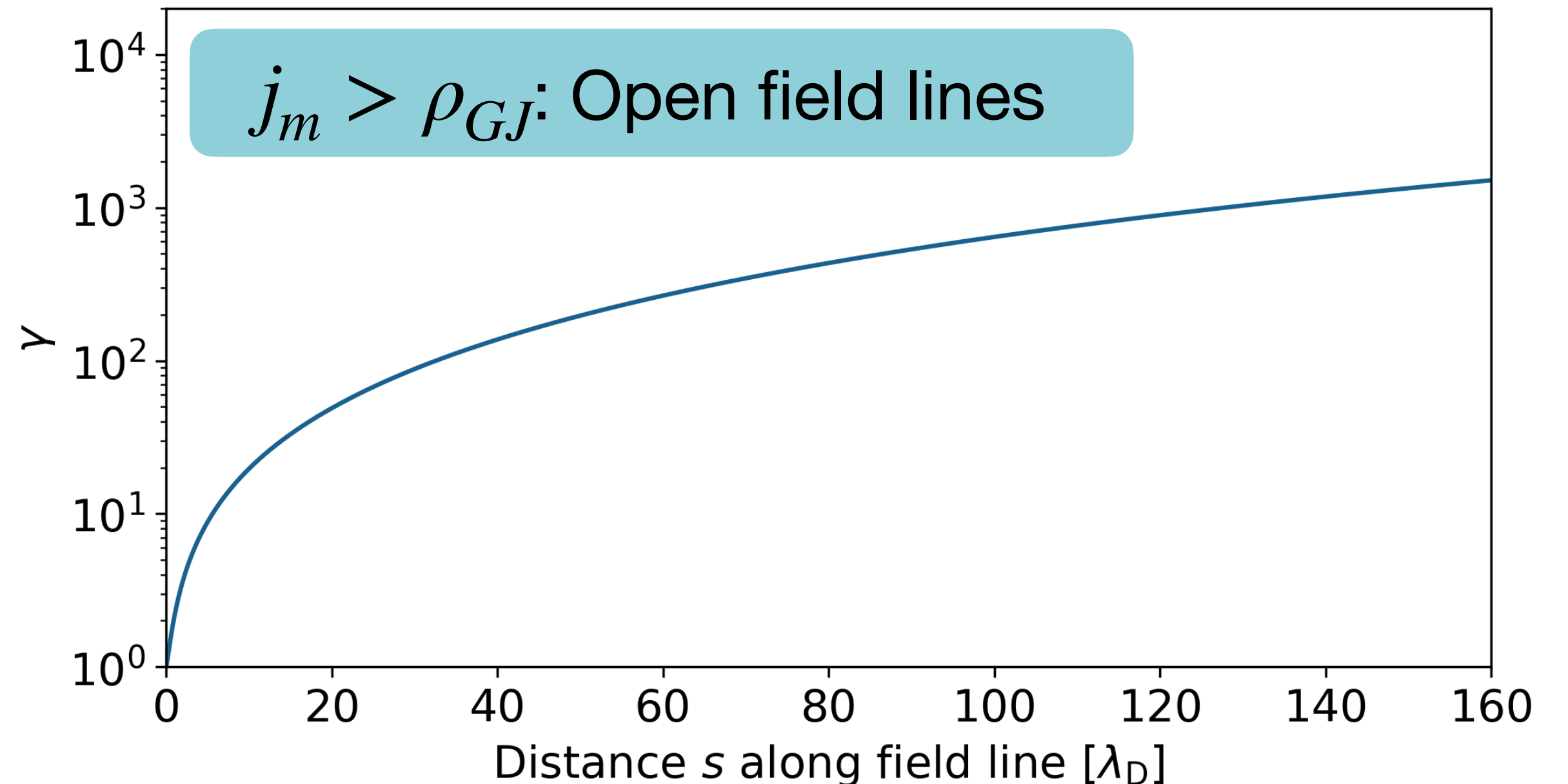
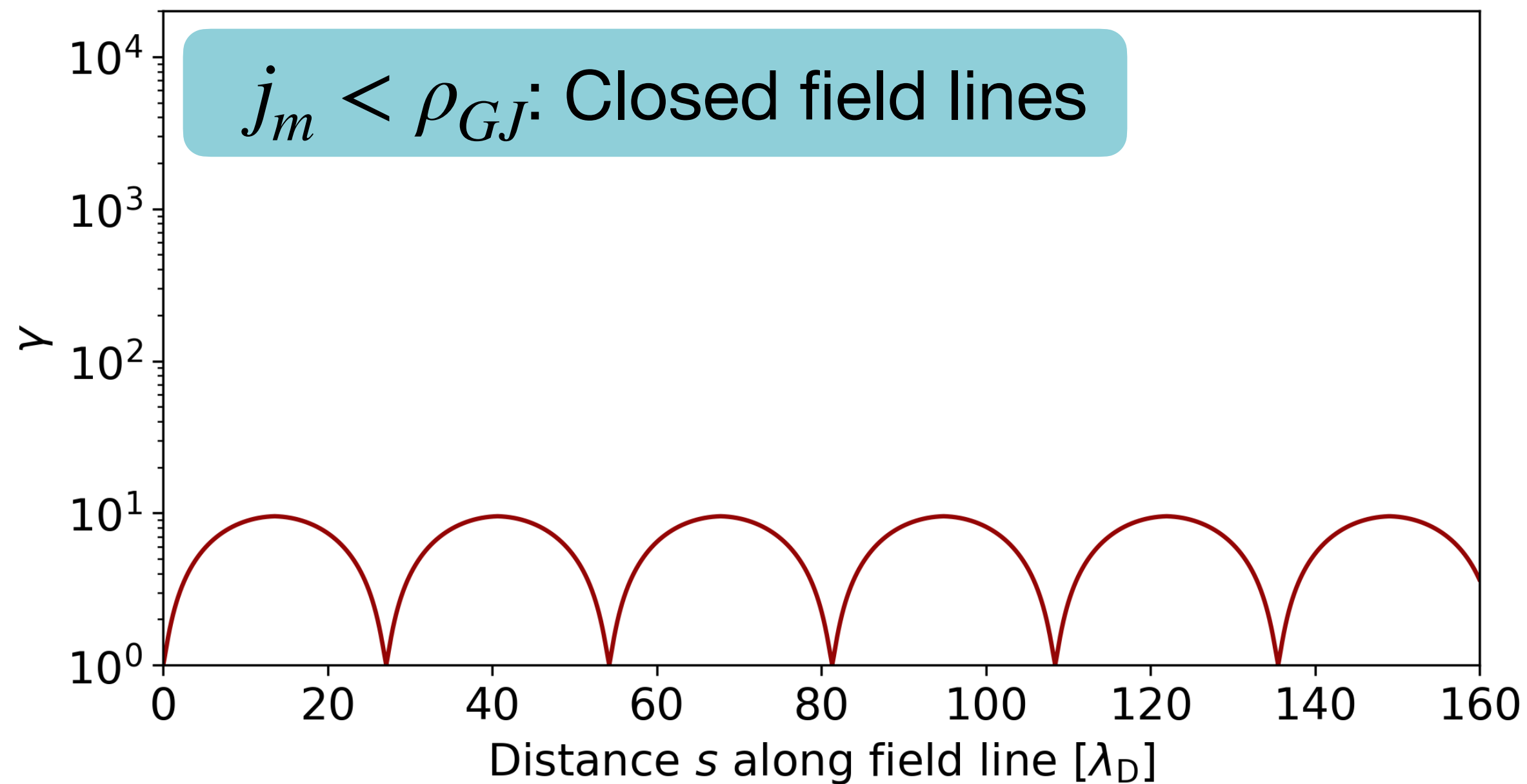
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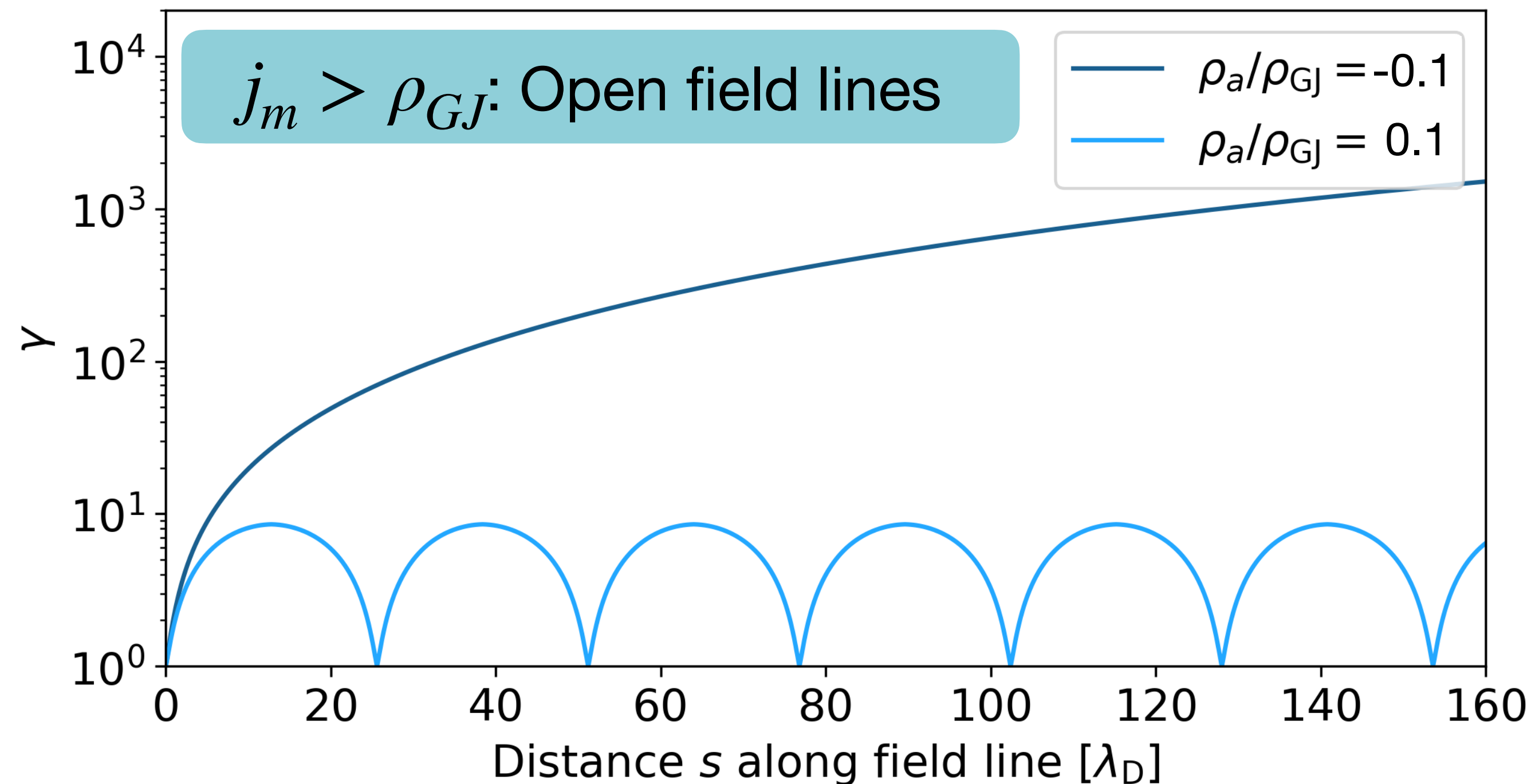




# So what if we add axions?

Evolution of charges in 1d:  $\frac{dE}{dx} = -(\rho - \rho_{GJ} - \rho_a)$

- Axions can **change evolution** dramatically:



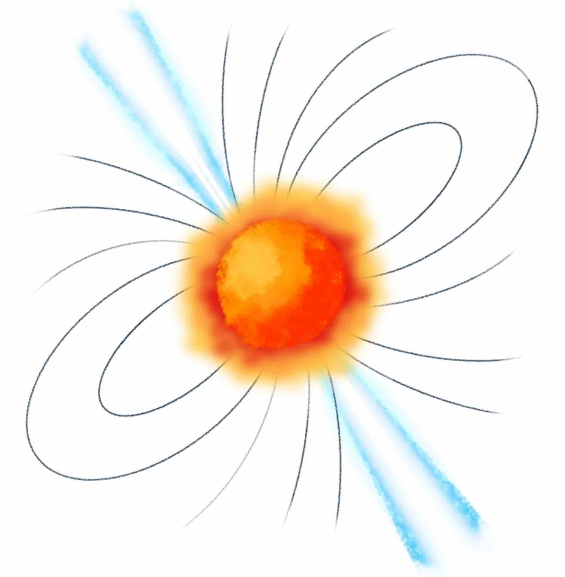
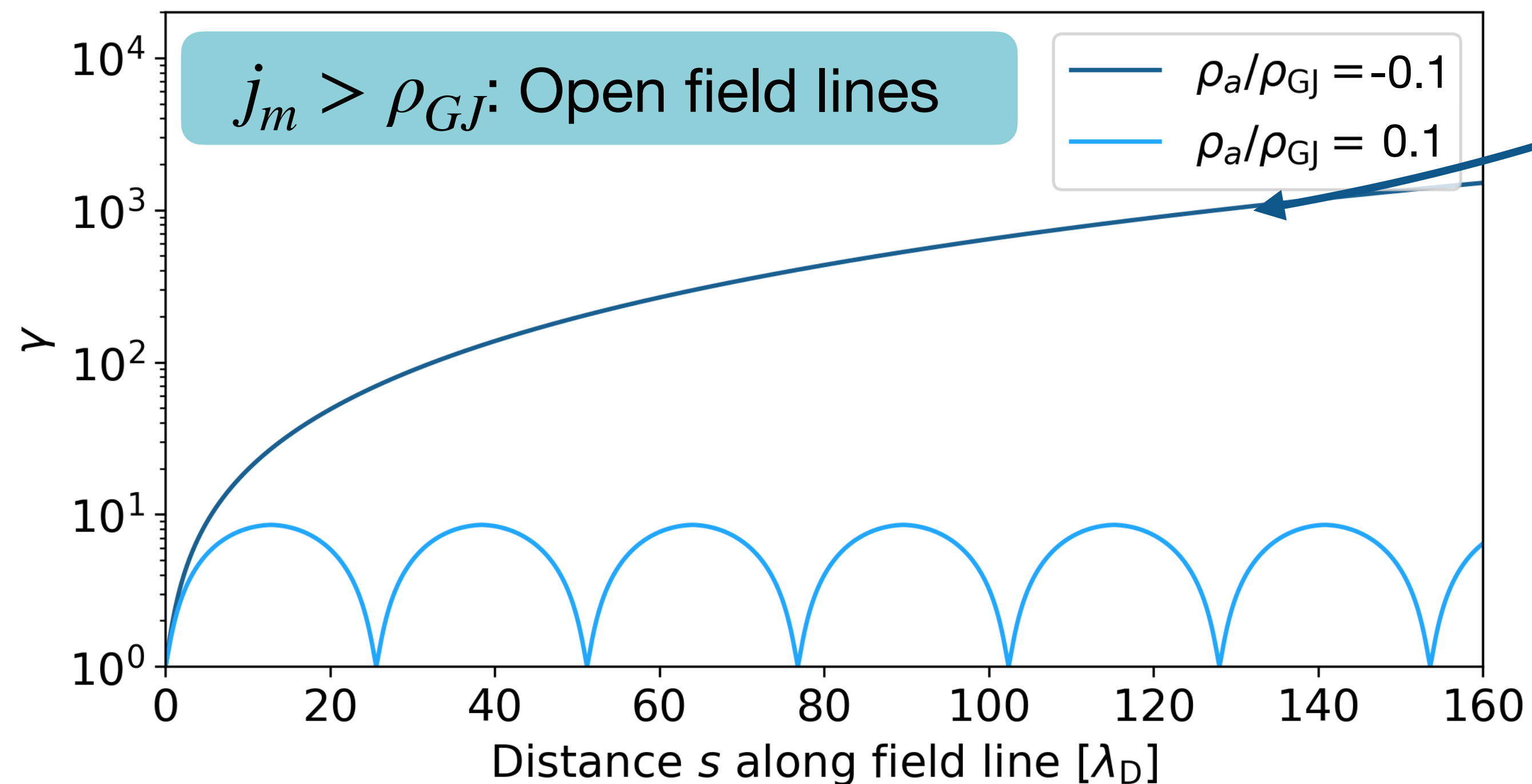


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→ Pulsar **produces emission**

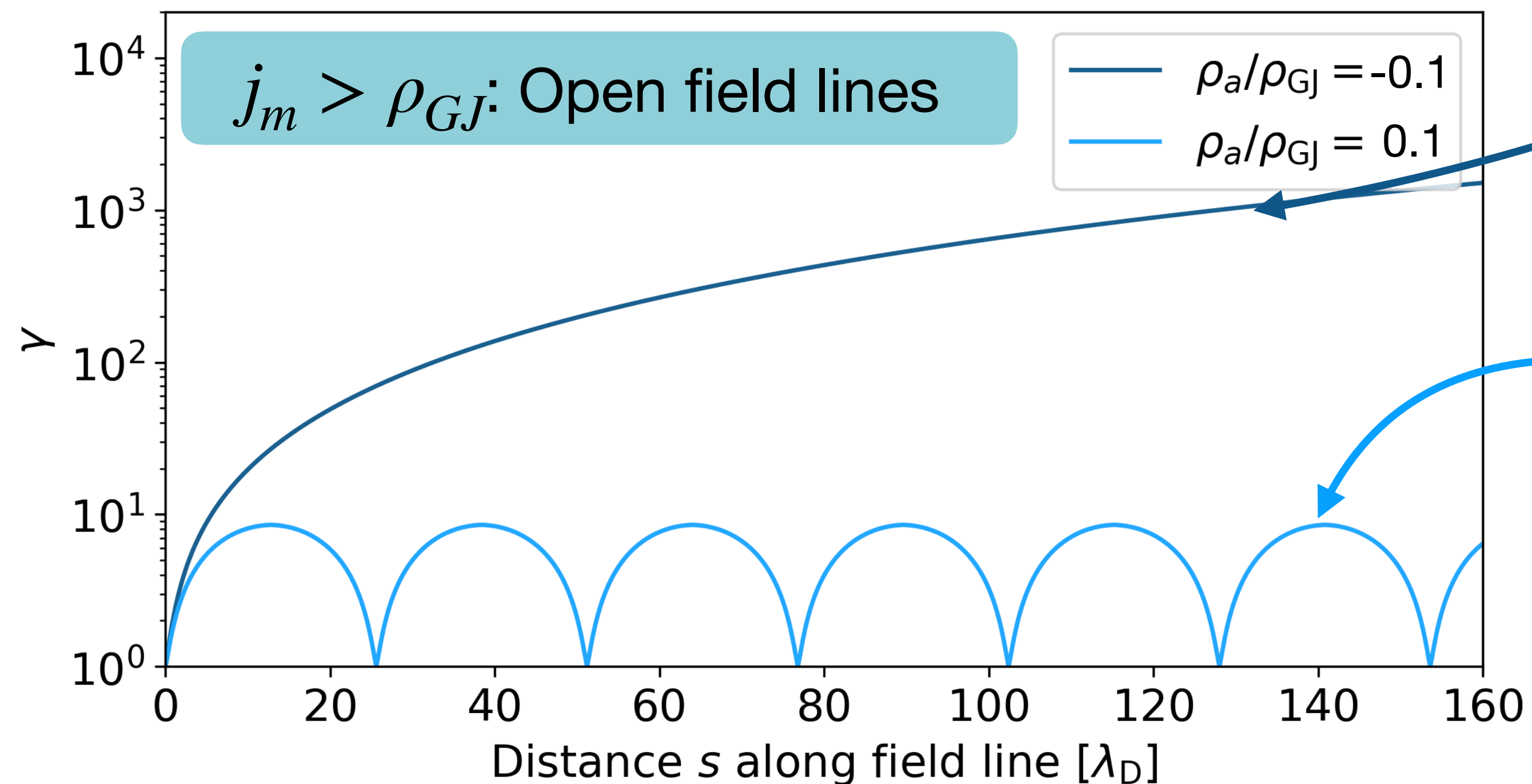




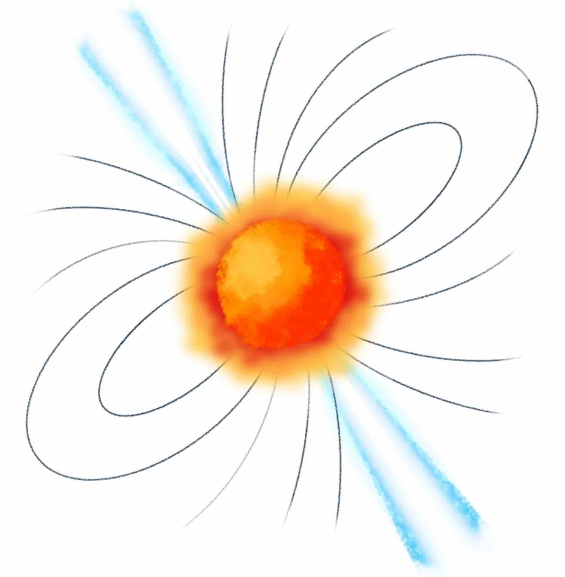
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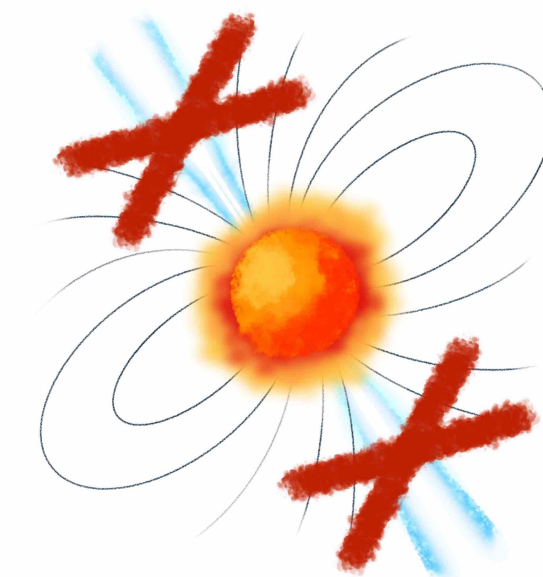
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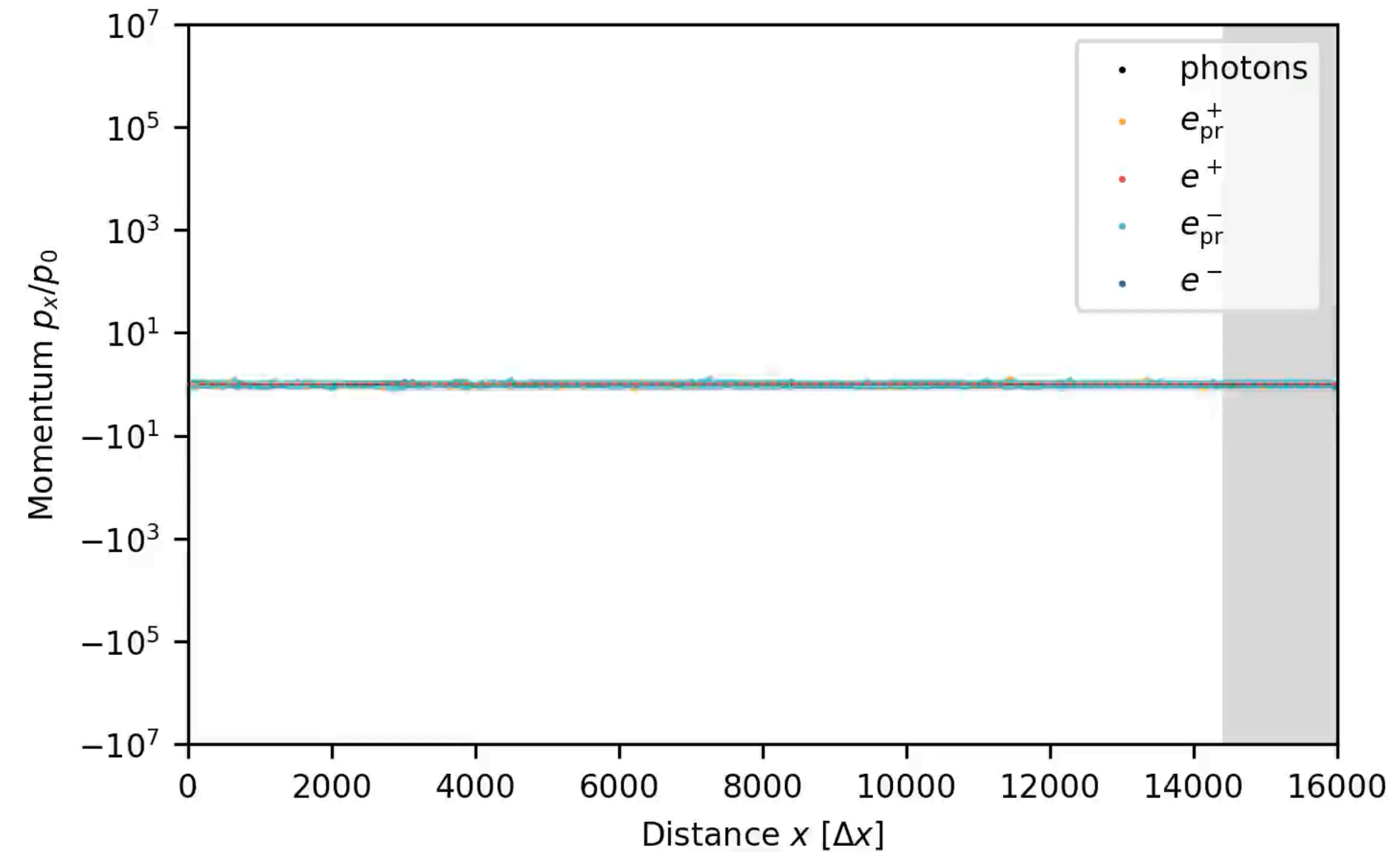
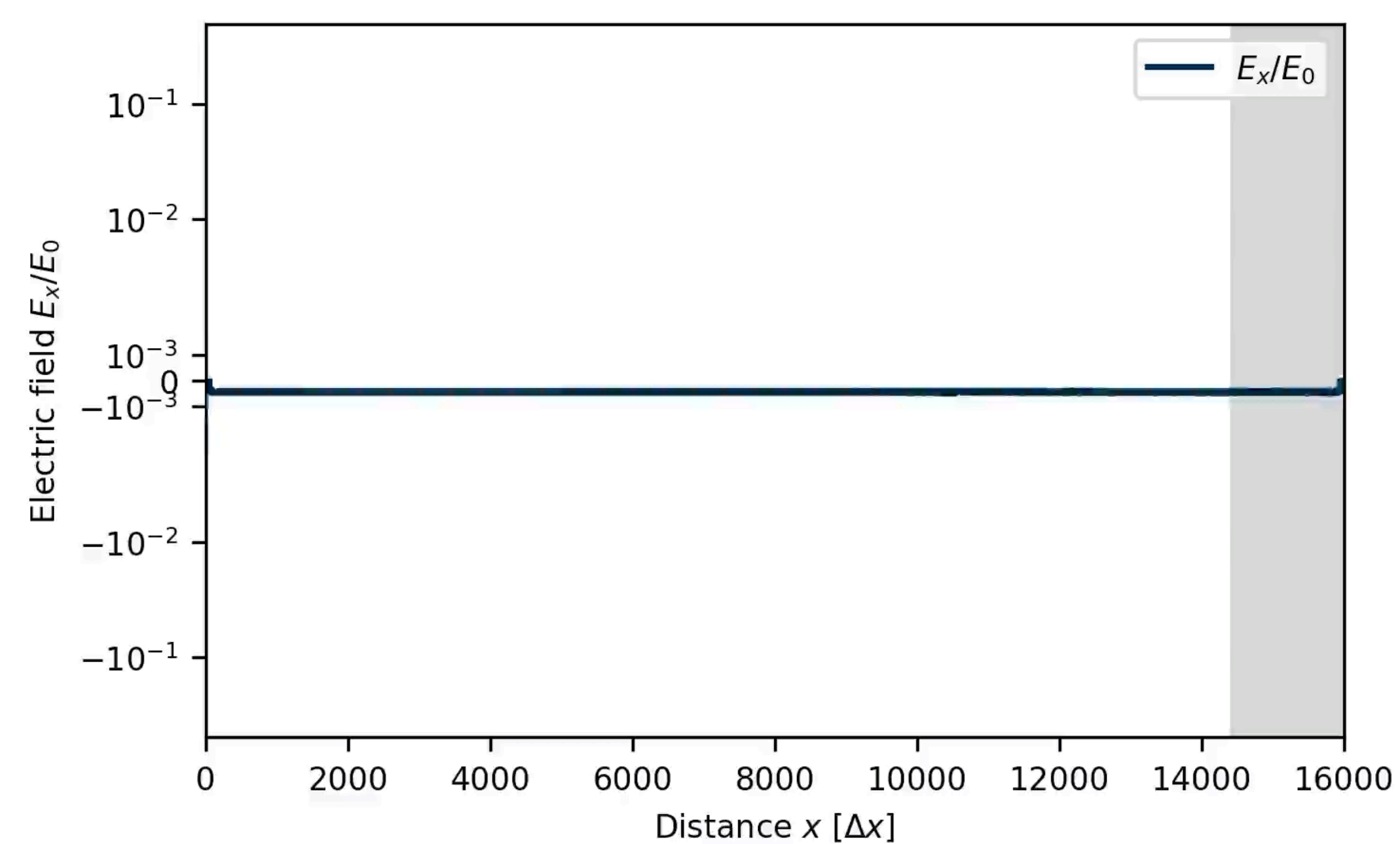
No pair production!  
→ No emission = **pulsar nulling**





# So ... how do we add axions?

- Take PIC (Particle-In-Cell) simulation ...

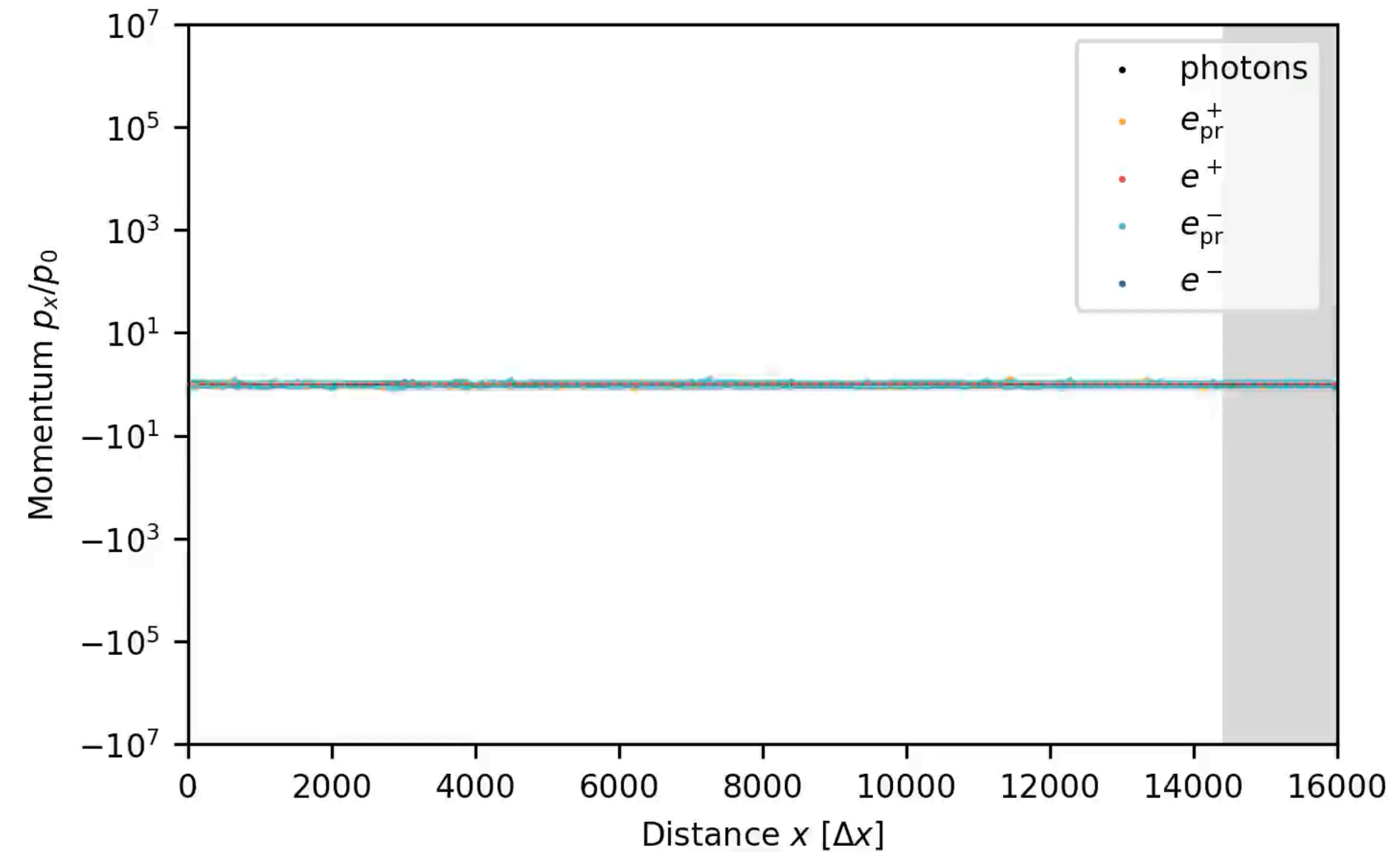
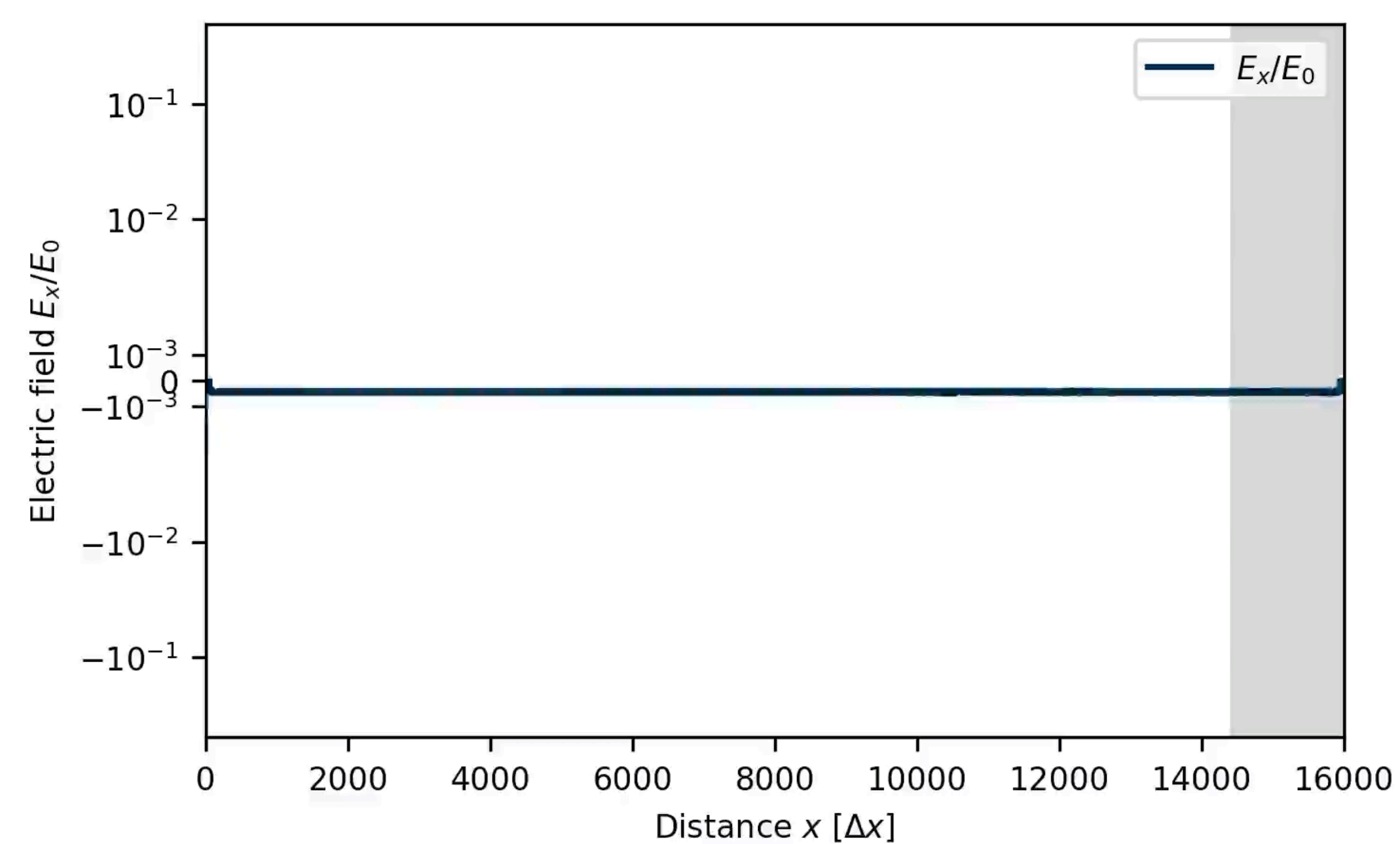


... and add the axion field!



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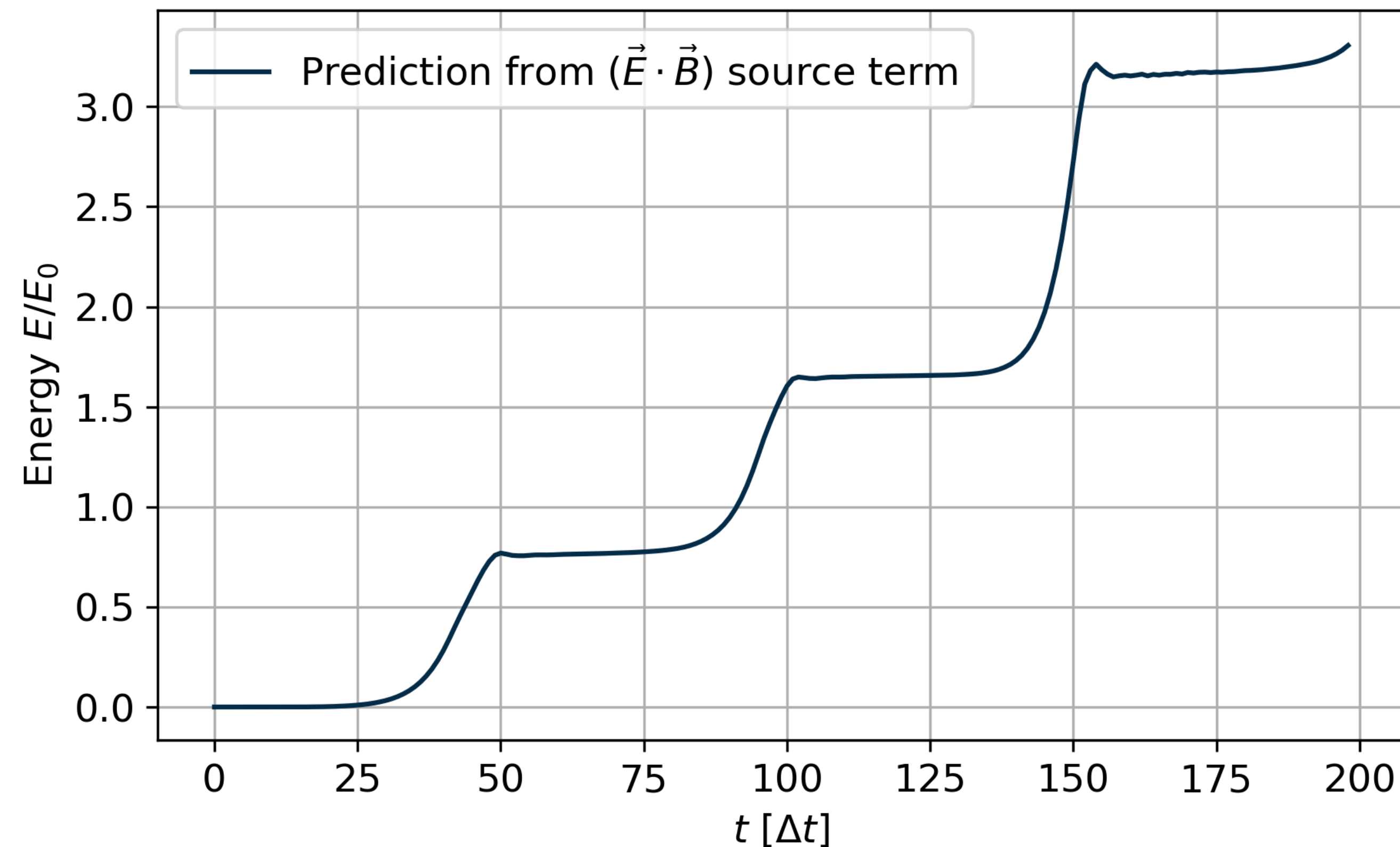


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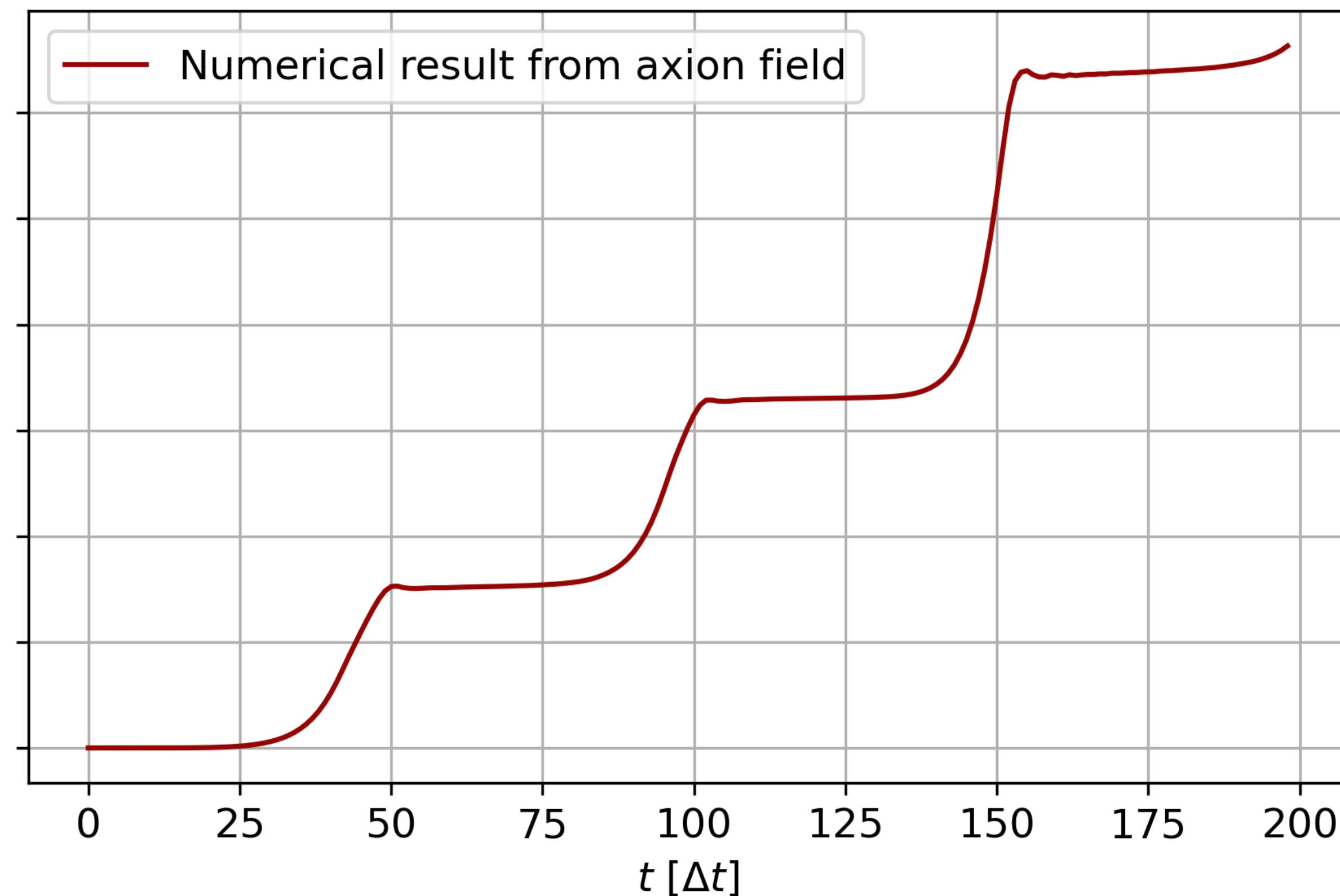


# Axions-PLC: Sanity check 1

- Axion production: **Energy distribution** over time



$$\frac{dE}{dk} \sim \text{FT}[g_{a\gamma\gamma} \vec{E} \cdot \vec{B}]$$

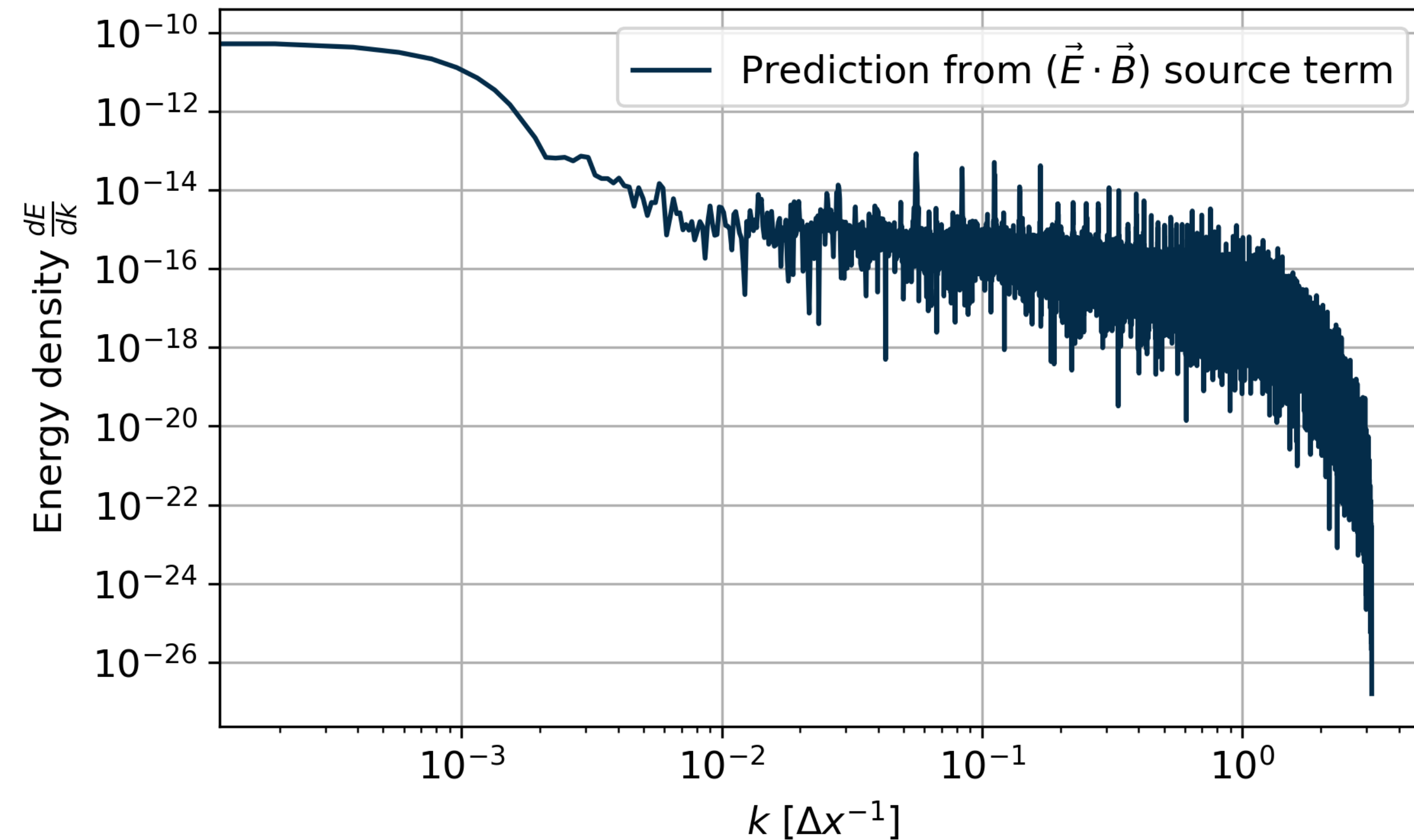


$$\frac{dE}{dk} \sim \text{FT}[(\nabla a)^2 + \dot{a}^2 + m_a^2 a^2]$$

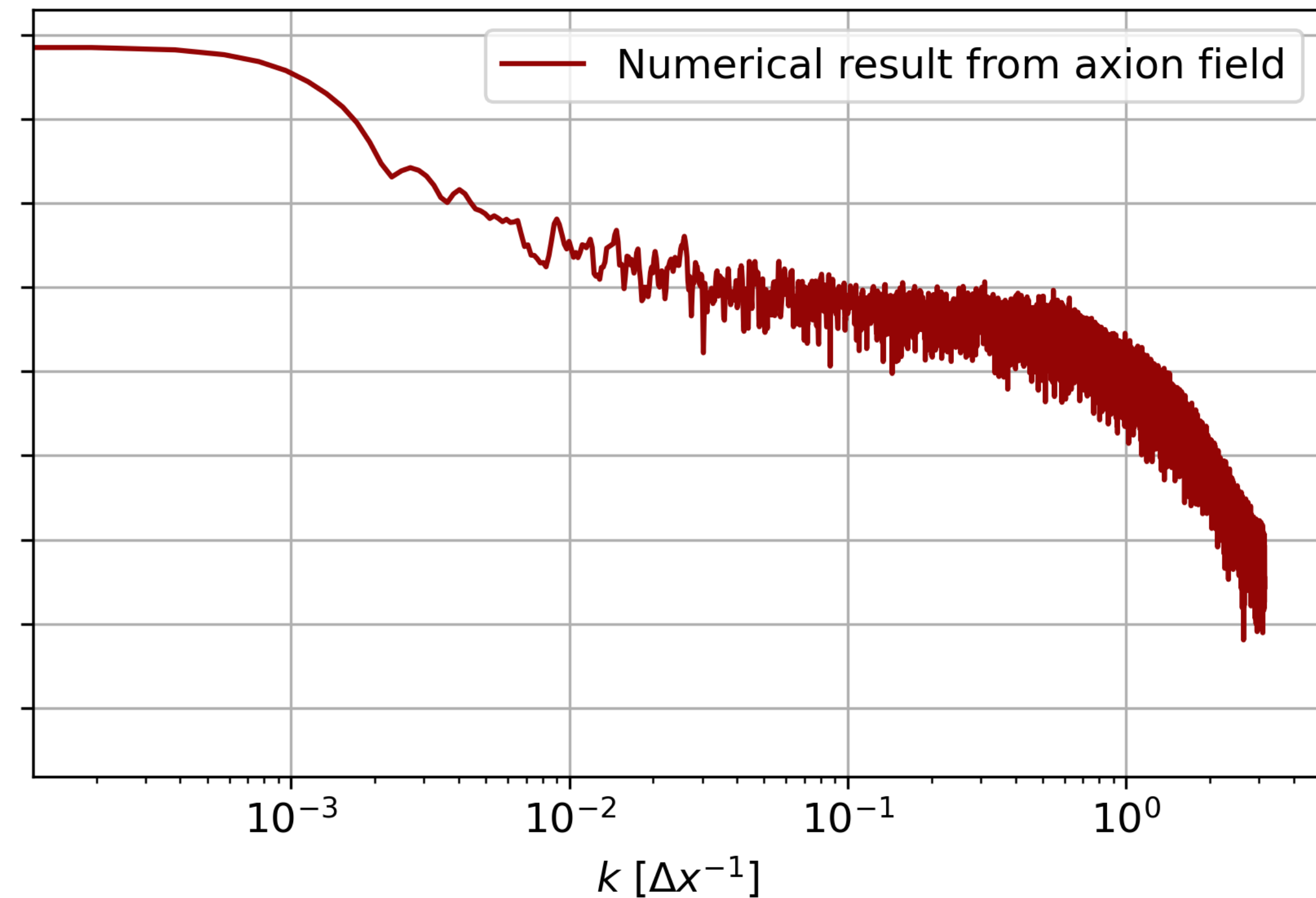


# Axions-PLC: Sanity check 2

- Axion production: **Energy distribution** in k-space



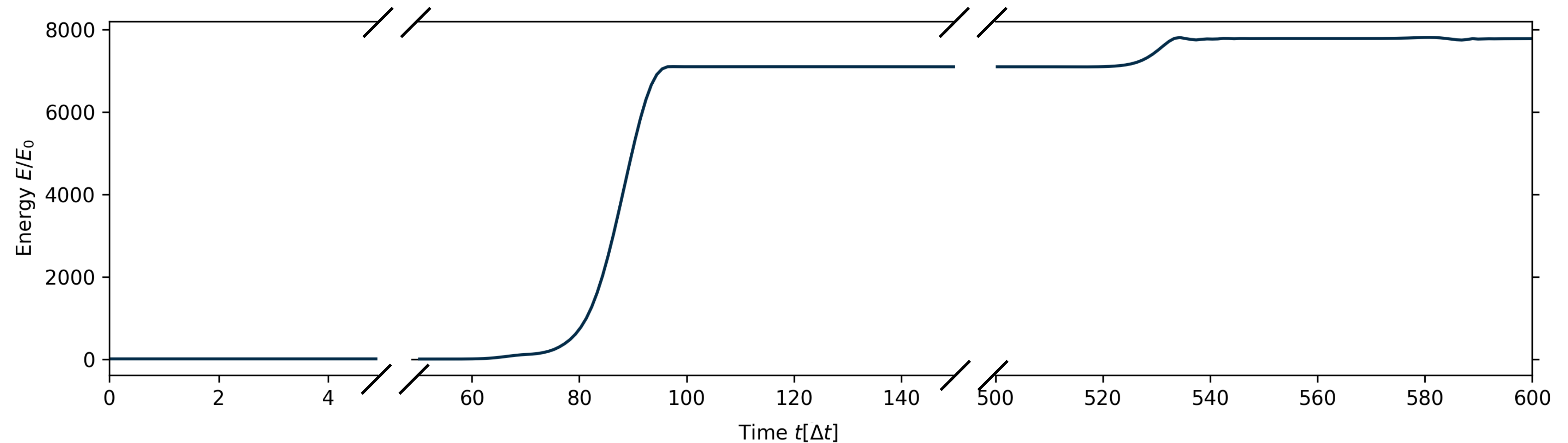
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# Back-reaction: Effect on pair cascade

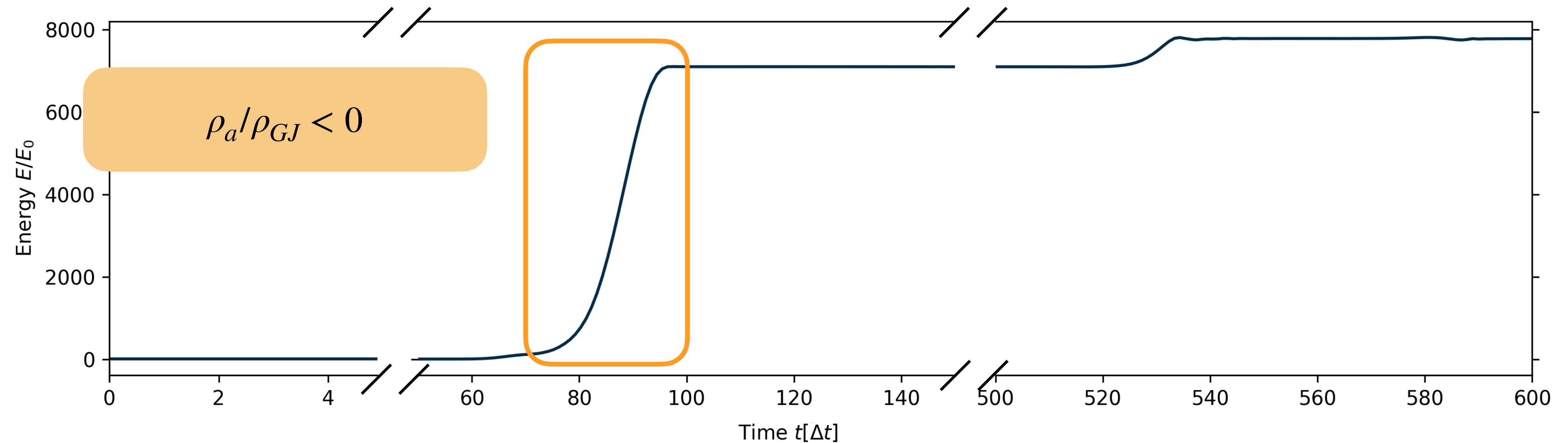
- Consider regime where axion charge density  $\rho_a$  becomes dominant:





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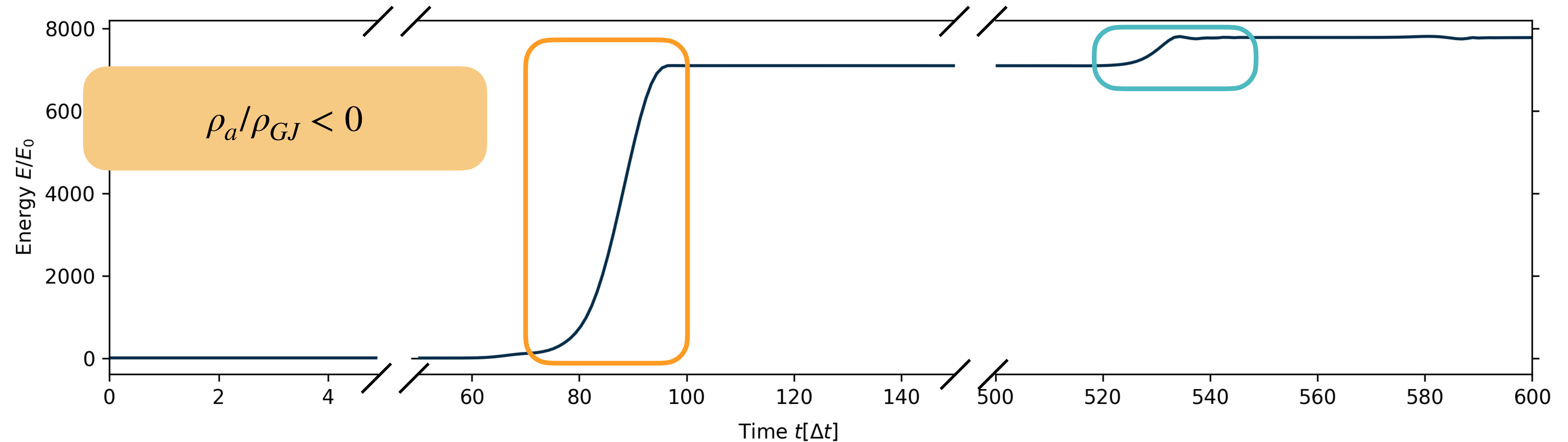
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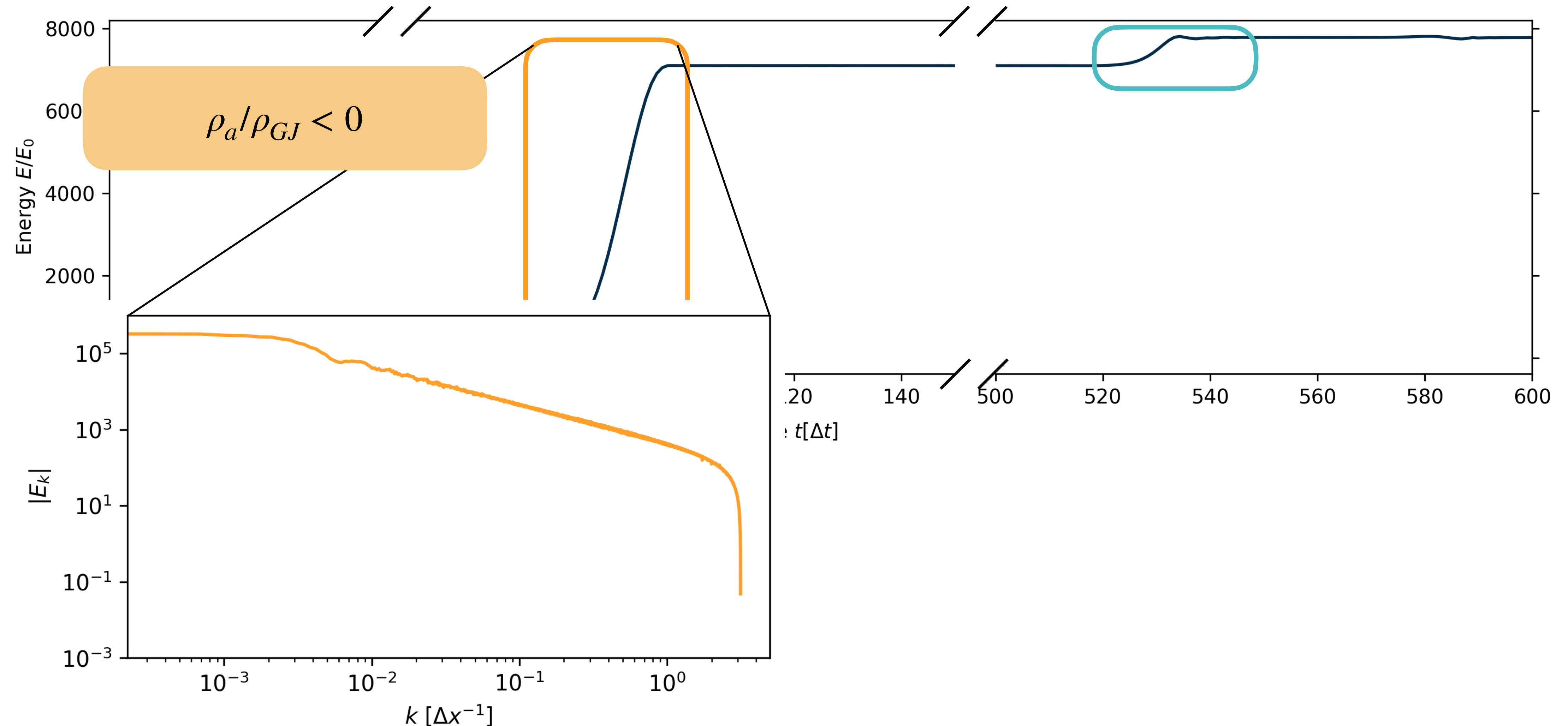




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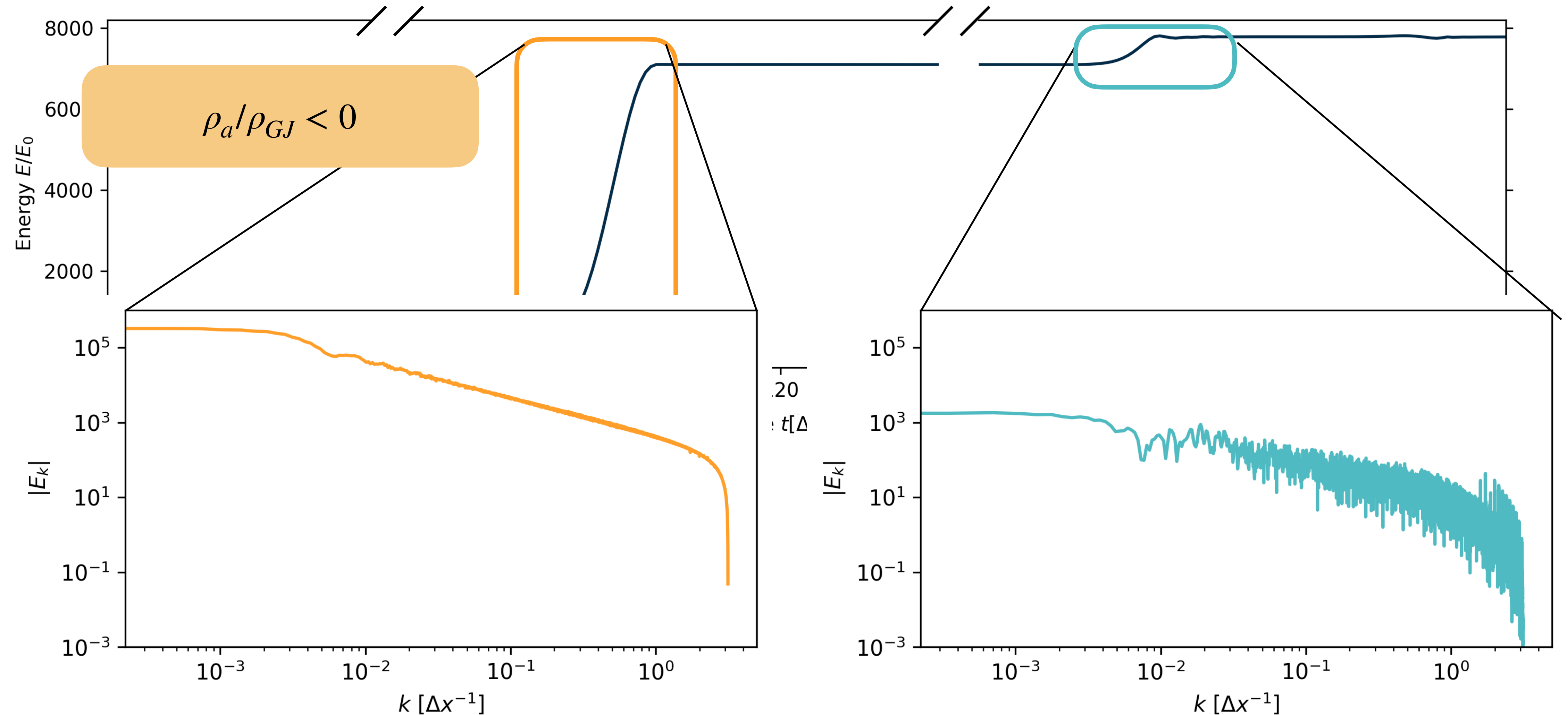
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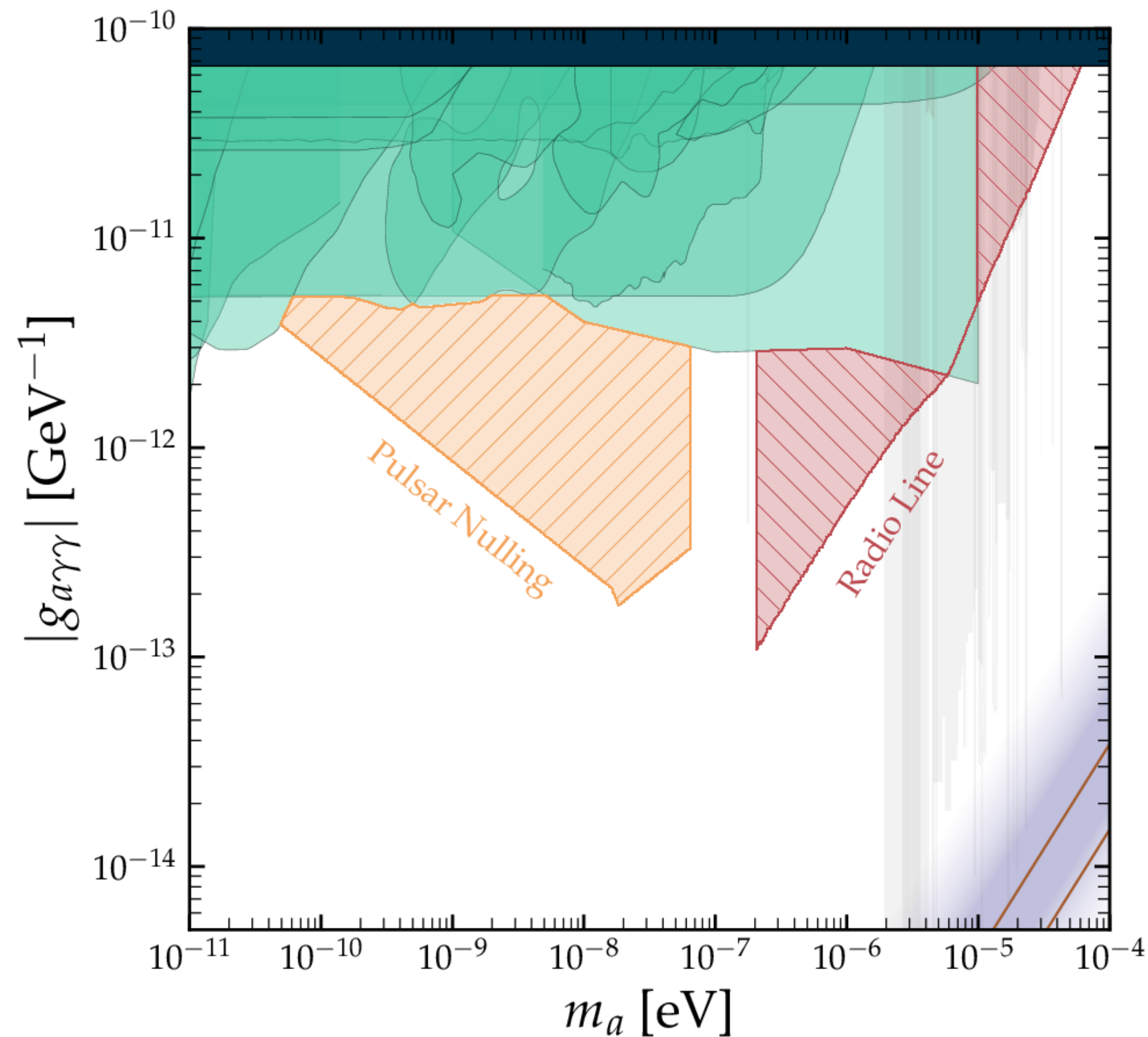
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# Outlook:

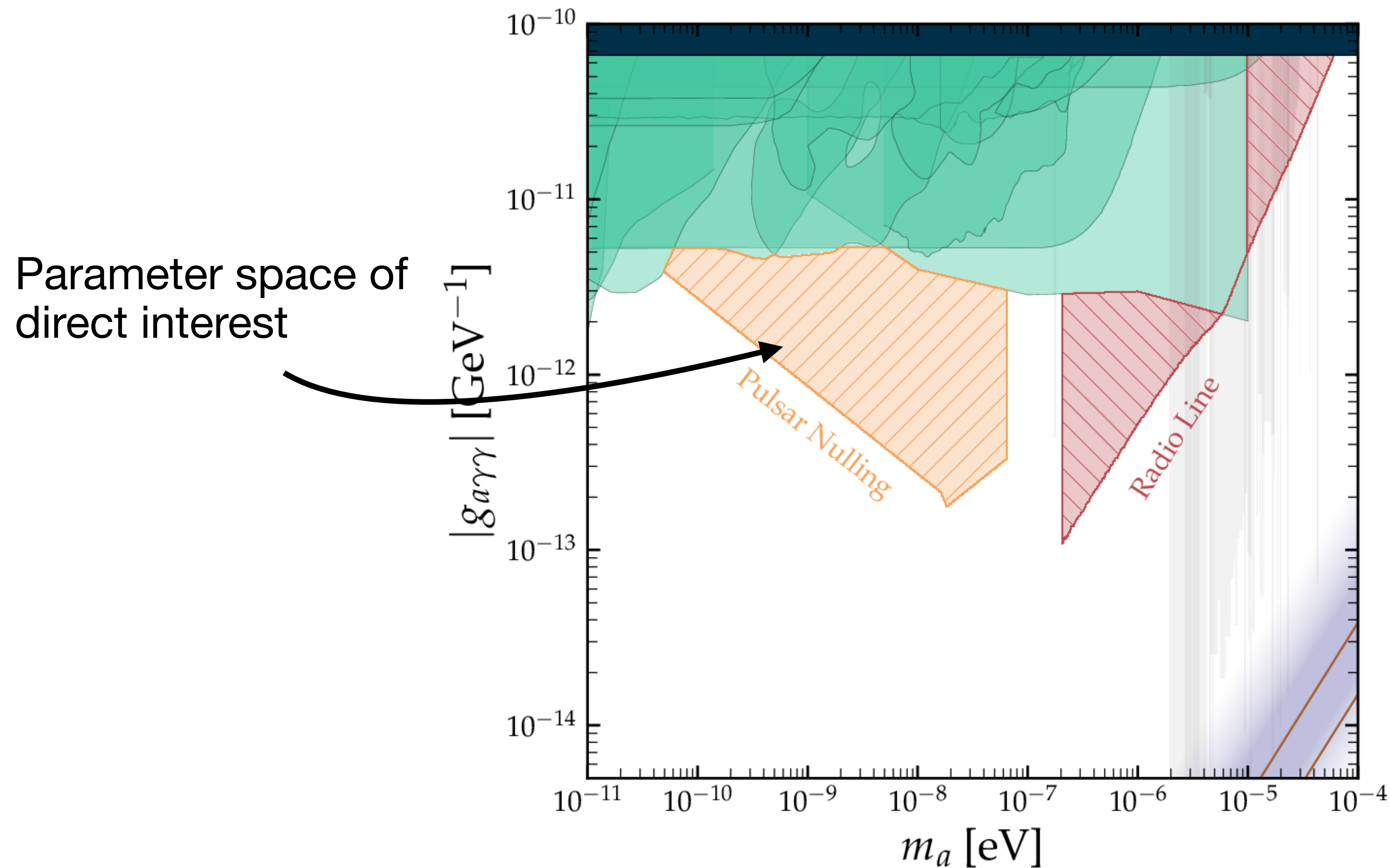
## Region of interest in parameter space



Caputo et al, [2311.14795]

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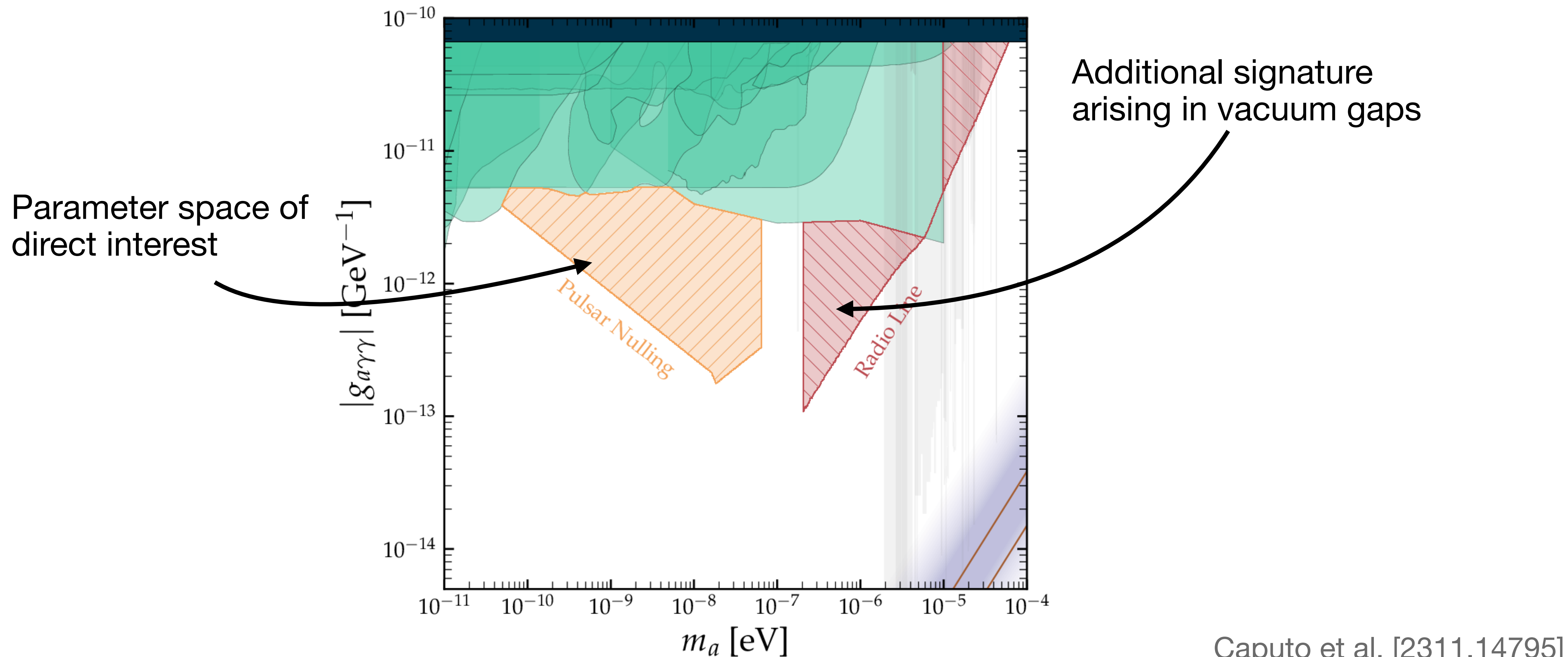


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# Outlook:

## Region of interest in parameter space



# Summary and outlook

- Dense axion cloud around pulsars can lead to **dramatic experimental signatures**
- Build first PIC axion electrodynamic simulation to explore non-perturbative effects
- More results to come soon!
- Extend simulation to **2+1 dimension** to model coherent radio emission
- Can we show that a similar effect occurs in **black holes**?

