

# Searches for New Physics at the (HL-)LHC – Selected theory topics

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**HELMHOLTZ** RESEARCH FOR  
GRAND CHALLENGES

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# Outline and disclaimer

- Introduction
- Direct searches for New Physics
- BSM via precision Higgs measurements
- Di-Higgs production in BSM models

*Disclaimer: the selection of what I present is of course biased by my own research interests, and there are plenty more exciting directions that I can't mention because of time!*

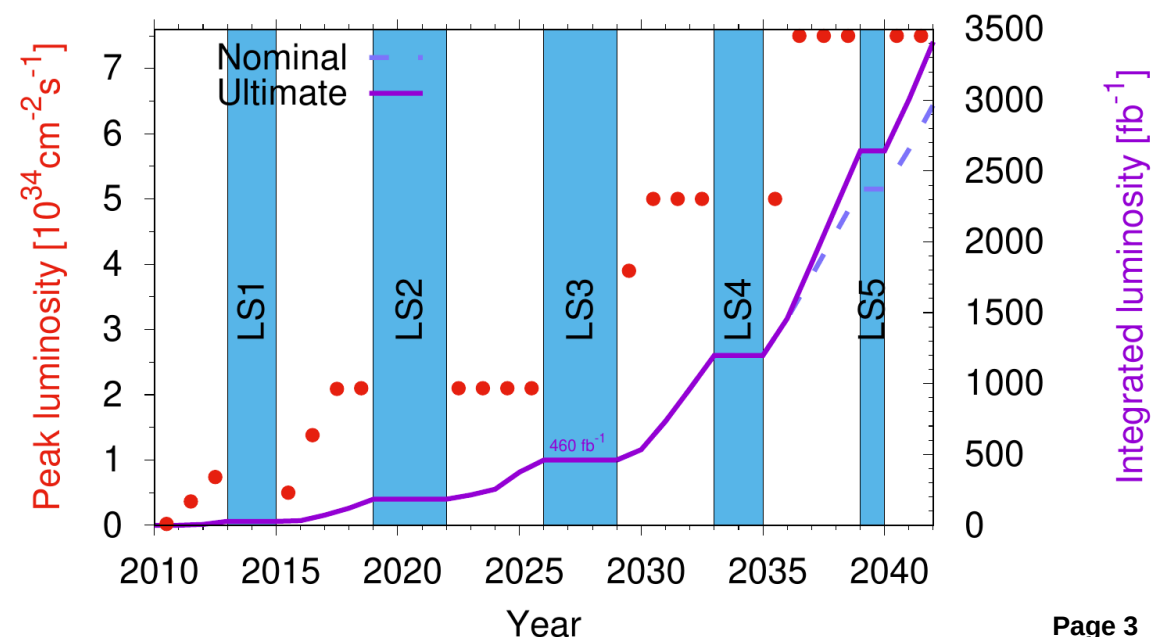
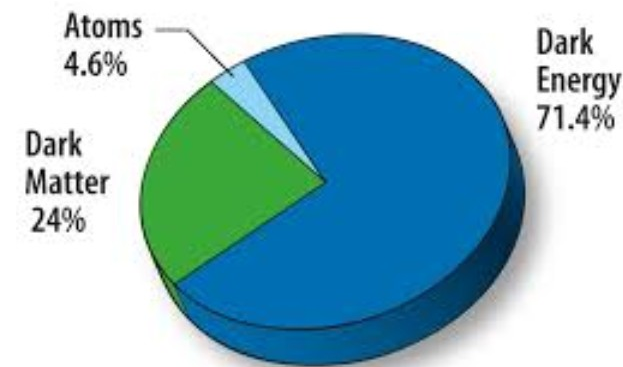
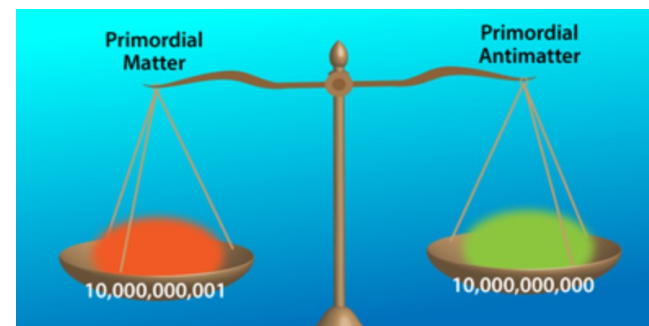
# BSM searches as of 2025

- No confirmed sign of Beyond-the-Standard-Model (BSM) Physics in LHC searches yet

- However, the **motivation for BSM remains intact**:

- matter-antimatter asymmetry  
(or baryon asymmetry of the Universe, BAU)
- dark matter
- origin of electroweak symmetry breaking
- naturalness and hierarchy problem(s)
- neutrino masses
- strong CP-problem
- ... and many more!

- **Only ~15% of total (HL-)LHC data collected so far!**



# Some avenues to search for New Physics at (HL-)LHC

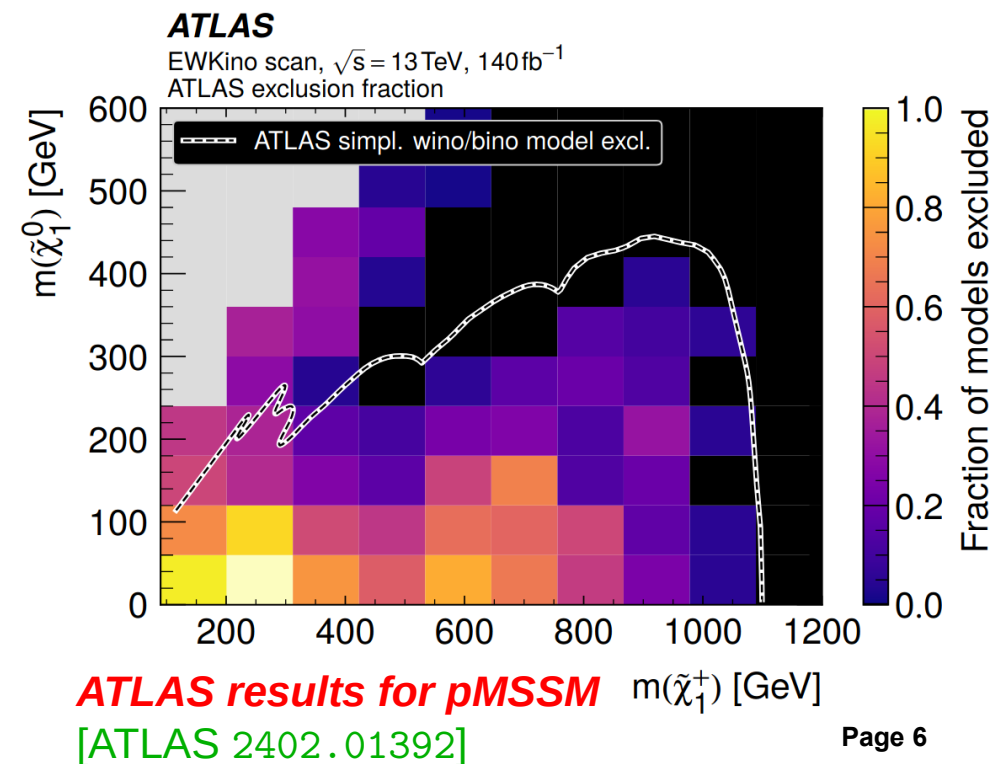
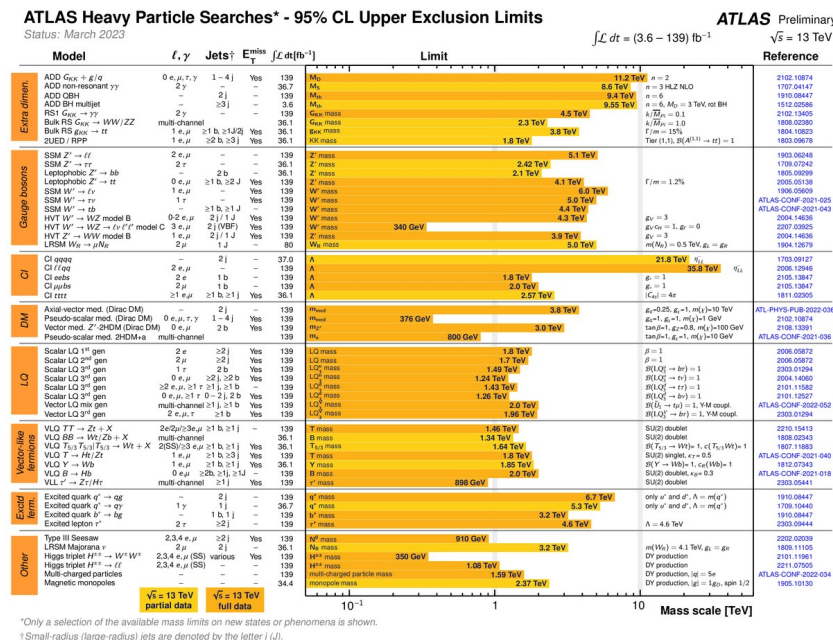
- **Increased luminosity**
  - search for rare processes (e.g. rare decays of top quark, or of Higgs boson; di-Higgs production, etc.)
- **New search ideas and strategies, and new analysis techniques**  
(c.f. also *talks of T. Vasquez Schröder and S. Lowette*)
  - consider new final states, new/forgotten channels, different regions of phase space
  - improved data analysis, e.g. with machine learning techniques
  - $\sqrt{\mathcal{L}}$  scaling is at best overly conservative [Belvedere, Englert, Kogler, Spannowsky '24]
- **Increased precision on properties of known particles**
  - precision measurements programme ongoing (more later on case of Higgs boson)
  - finding a deviation from SM would give us information about scale of BSM
- **More global analyses** (e.g. EFT) → *see e.g. talk of E. Vryonidou*



# Direct searches for New Physics

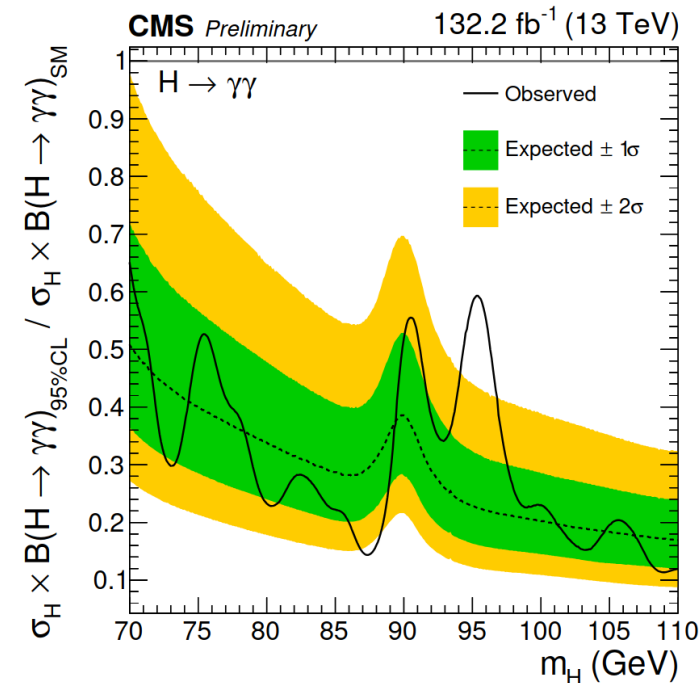
## Search limits and interpretations

- **Increasingly stringent limits on BSM states,**
  - e.g. → stops/sbottoms  $> 1.3$  TeV
  - gluinos and 1st/2nd family squarks  $> 2.4$  TeV
  - $Z'$   $> \sim 2$  TeV (at least)
  - scalar leptoquarks  $> 1.2$  TeV
- etc.
- Interpretation of searches often given in terms of simplified models/scenarios → **care is then needed to draw general conclusions!** (*c.f. pMSSM example*)
- **Different approaches for (re)interpretations:**
  - **recasting**, e.g. with MadAnalysis 5 [Conte et al. '12-'18], [Araz et al. '20, '21], CheckMATE [Drees et al. '13], [Dercks et al. '16], [Desai et al. '21], RIVET [Buckley et al. '10], [Bierlich et al. '19] with Contour [Buckley et al. '21], ColliderBit [Balázs et al. '17], [Athron et al '18] (from GAMBIT), or HackAnalysis [Goodsell '24]
  - **map BSM model/scenario onto simplified model search limits**
    - e.g. SModelS [Kraml et al. '13], [Alguero et al. '21]
  - **identify most sensitive BSM search channel to compare model to**
    - e.g. HiggsBounds [Bechtle et al '08-'20], [Bahl et al. '22]



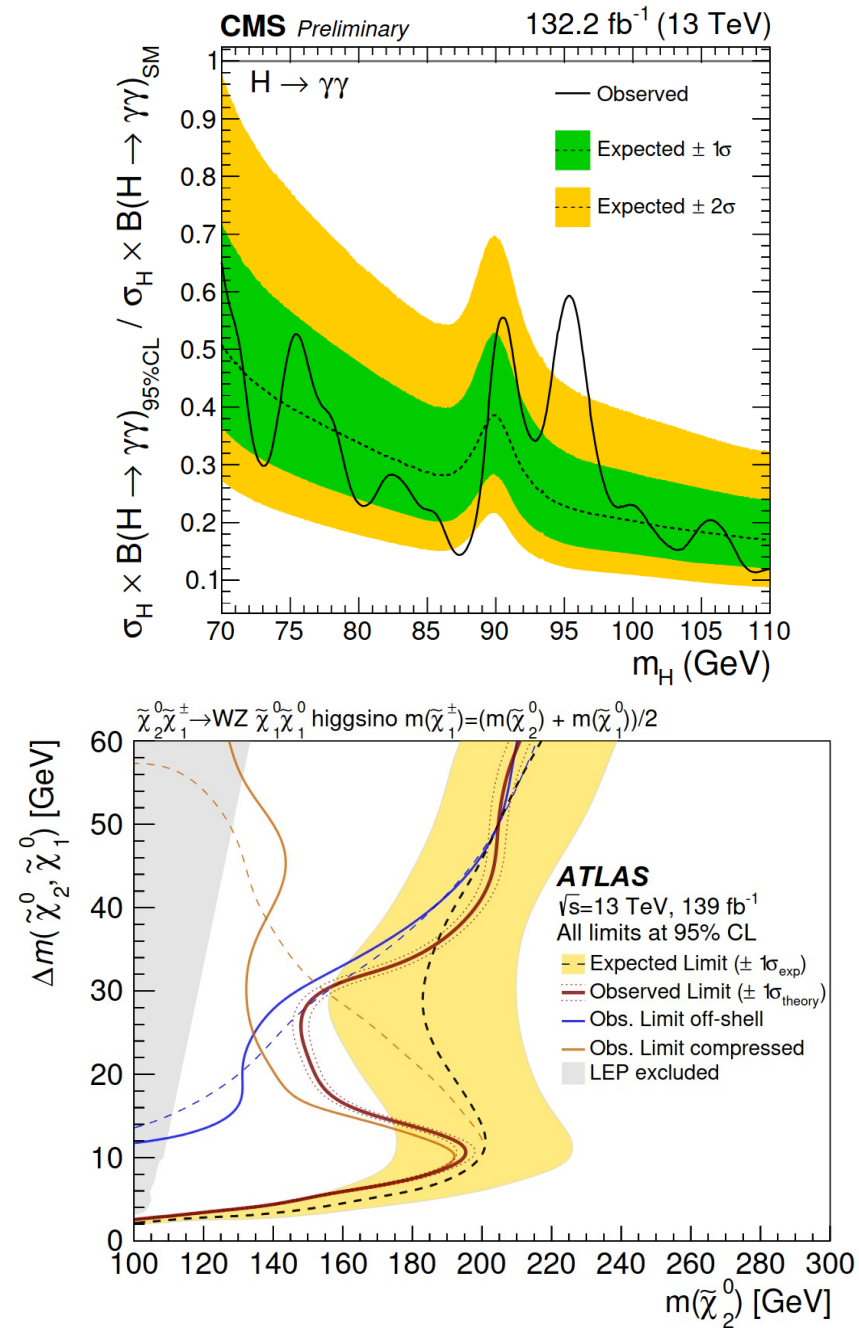
# Some reasons for excitement?

- Some tentatiling excesses worth mentioning:
- **A Higgs boson at 95 GeV?**
  - excesses seen by ATLAS and CMS in low mass  $\Phi \rightarrow \gamma\gamma$  searches
  - + CMS search for  $\Phi \rightarrow \tau^+\tau^-$  + LEP excess in  $\Phi \rightarrow b\bar{b}$  (debated)
  - numerous possible BSM interpretations (w. or w/o  $\tau^+\tau^-$  and  $b\bar{b}$ )  
(far too many references to fit on this slide)



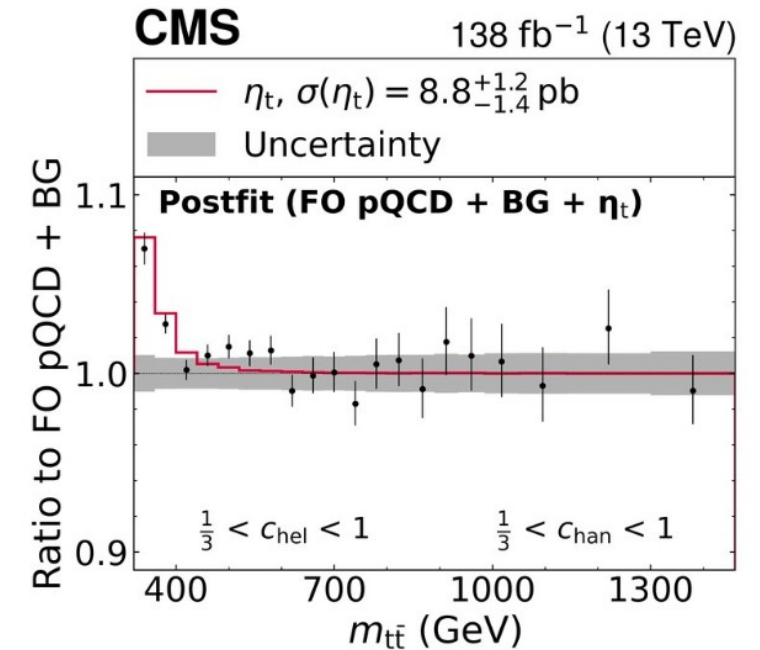
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  - Excesses in soft lepton and monojet searches**
    - excesses seen by ATLAS ([ATLAS-SUSY-2018-16], [ATLAS-SUSY-2019-09]) and CMS ([CMS-SUS-18-004]) in searches for 2 or 3 soft leptons + MET
    - recasting of ATLAS and CMS results ([ATLAS-EXOT-2018-06], [CMS-EXO-20-004]) finds corresponding excesses in searches for monojet + MET [Agin et al. '23]
    - interpretations possible in MSSM, NMSSM, Dirac gaugino models, with or without DM and/or  $h_{95}$ , see e.g. [Agin et al. '23, '24, '25], [Chakraborti et al. '24], [Ellwanger et al. '24], [Fuks et al. '25], [Araz et al. '25]

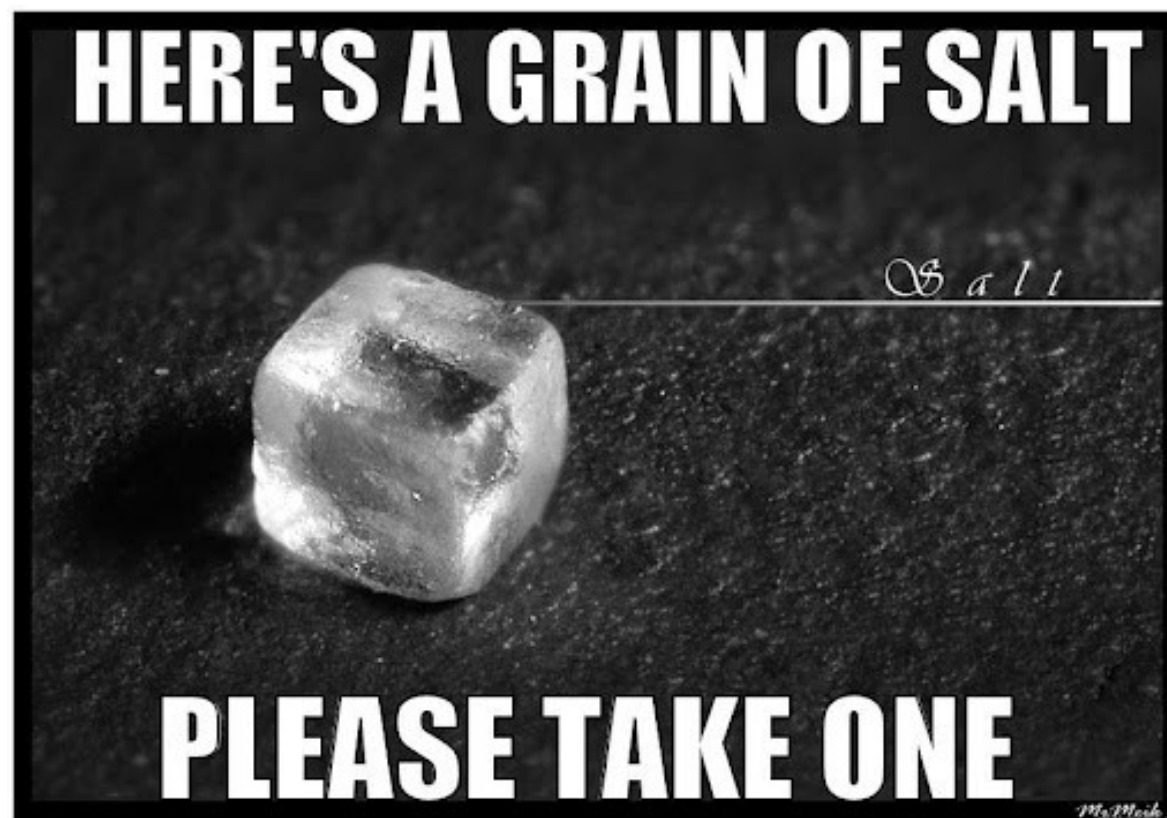


# Some reasons for excitement?

- Some tentatling excesses worth mentioning:
  - **A Higgs boson at 95 GeV?**
  - **Excesses in soft lepton and monojet searches**
  - **Excess at  $t\bar{t}$  threshold** → *see talk of S. Lowette yesterday*
    - *clear excess above SM prediction for non-resonant  $t\bar{t}$  production:* CMS  $\gg 5\sigma$  [CMS-TOP-24-007], confirmed by ATLAS [ATLAS-CONF-2025-008]
    - signal compatible with **toponium bound state** (predicted in SM) or(and?) with **BSM pseudoscalar**
    - only toponium (most likely, see e.g. [CMS-HIG-22-013] which uses NRQCD model from [Fuks et al. '21, '24]) or could it be both? (see [Djouadi, Ellis, Quevillon '24], [Bahl, Kumar, Weiglein '25])
    - inclusion of precise theory predictions (c.f. [Garzelli et al '24]) needed and underway
    - *see talk of M. Garzelli on Friday*



# Some reasons for excitement?



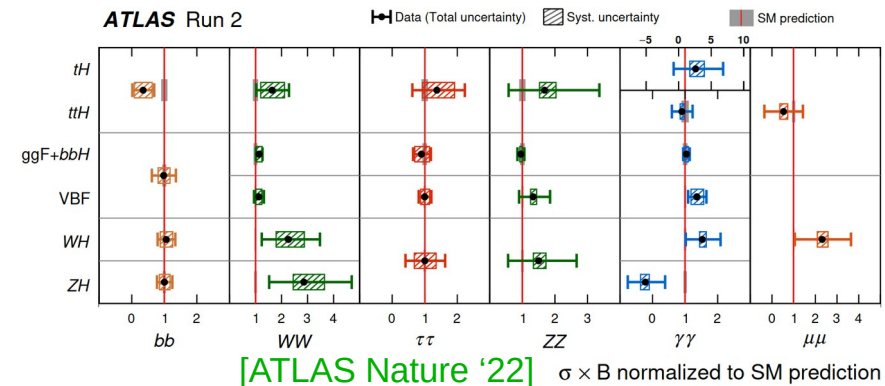
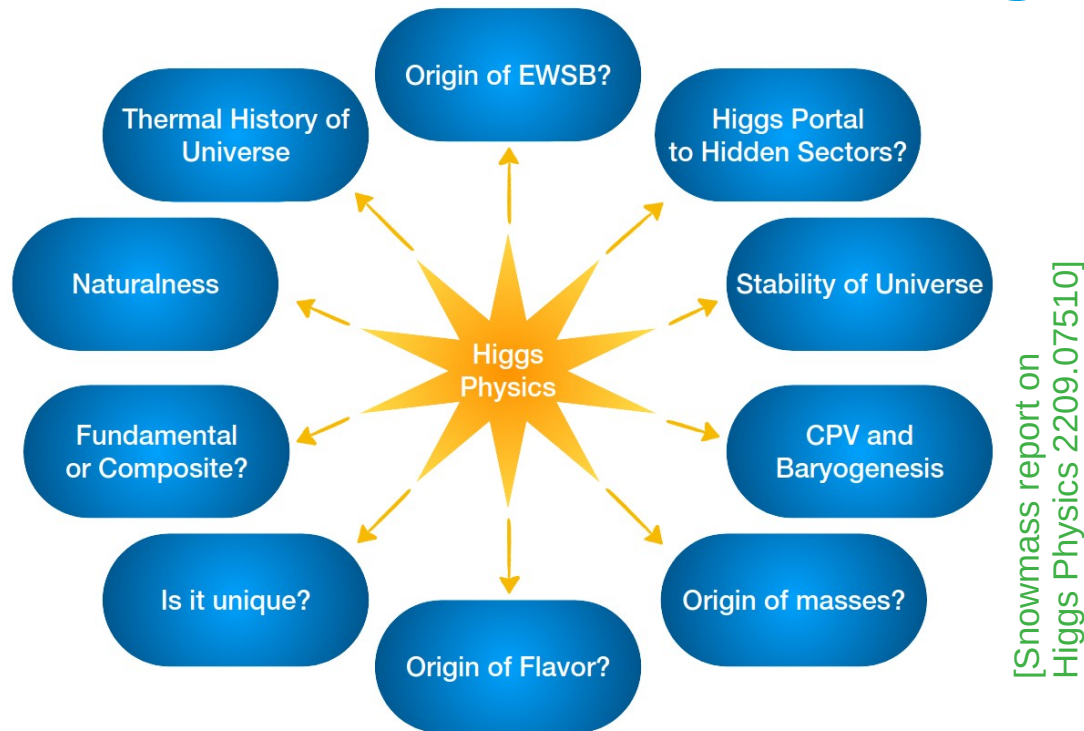
**NB: I am not claiming that any of the following are confirmed to be BSM yet, but:**

- **these examples show that there is still ample room for direct discoveries!**
- **while most of these will (likely) disappear or find an explanation within the SM, it suffices that one remain to have a discovery of New Physics!**

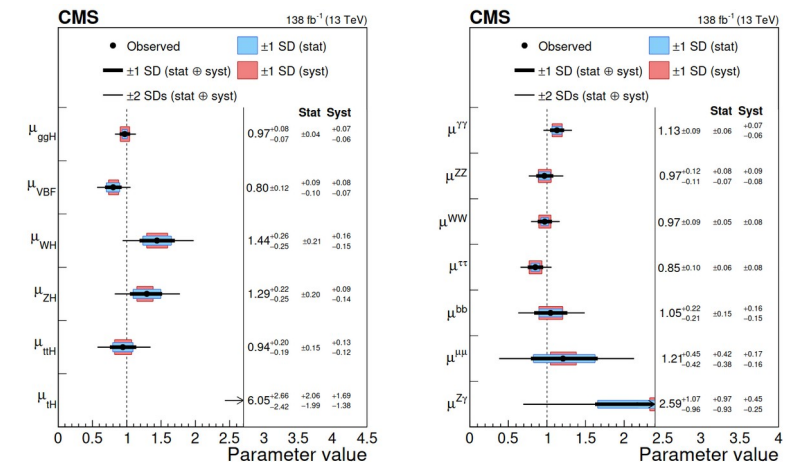
# BSM searches via Higgs precision measurements



# The central role of the Higgs to search for New Physics



[CMS Nature '22]

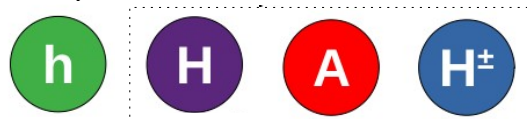


- The Higgs boson is **related to many of the open questions of HEP**
- BSM theories commonly feature extended Higgs/scalar sectors, or states that couple to the detected Higgs boson → **can modify properties of  $h_{125}$**
- Ongoing and future programme of precision measurements of Higgs properties at (HL-)LHC, see e.g. [ATLAS Nature '22], [CMS Nature '22]  
Results in terms of  $\kappa$ -framework, signal strengths, STXS, EFT operators, etc. (→ *c.f. talk of S. Lowette*)



# Example: dark matter in the Inert Doublet Model

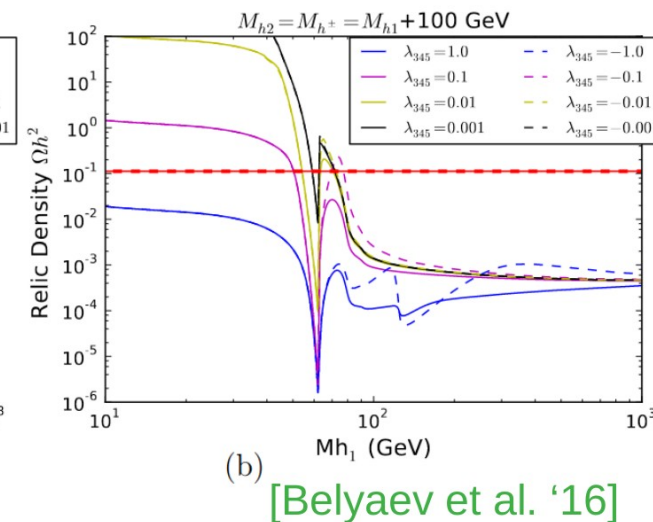
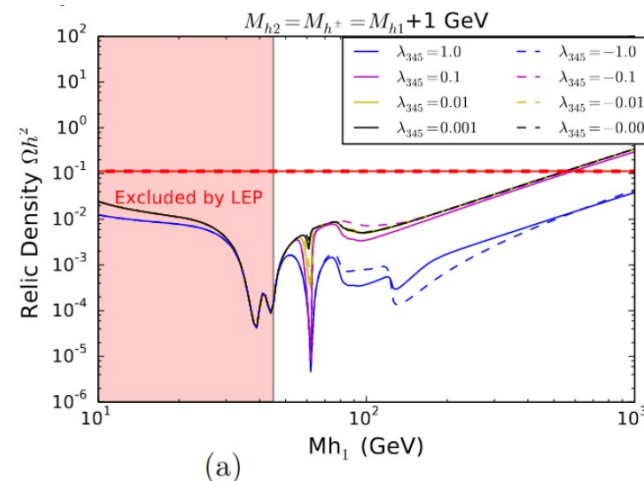
- **Inert Doublet Model (IDM):**  
add 2<sup>nd</sup> doublet to SM, charged under unbroken  $Z_\gamma$  symmetry



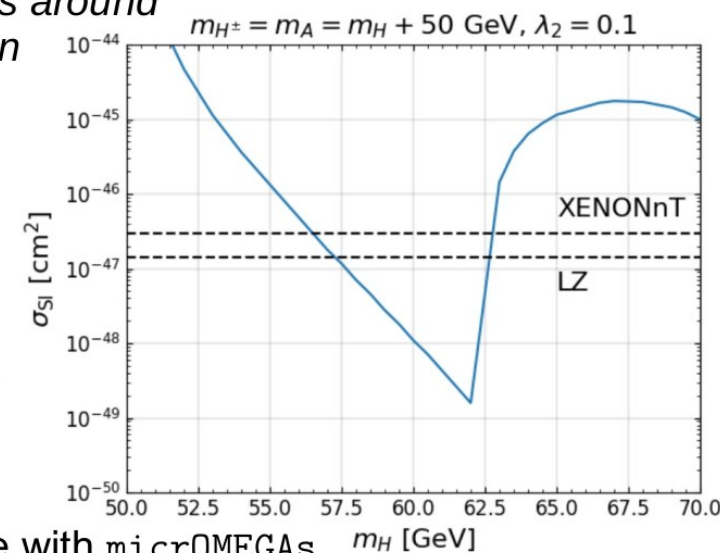
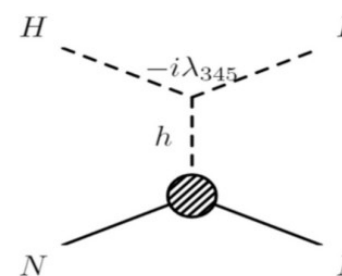
*Inert BSM scalars*

→ **lightest inert scalar  $H$  = DM candidate**

- DM relic density obtained via freeze-out, while evading current detection bounds
- **Higgs portal DM models like IDM testable via:**
  - DM direct and indirect searches
  - direct searches at colliders
  - precision/indirect tests, e.g. **properties of  $h_{125}$** 
    - **$h \rightarrow \text{invisible}$**   
(only if  $m_H < m_h/2$ ; can also be evaded by tuning portal coupling)
    - **$h \rightarrow \gamma\gamma$**



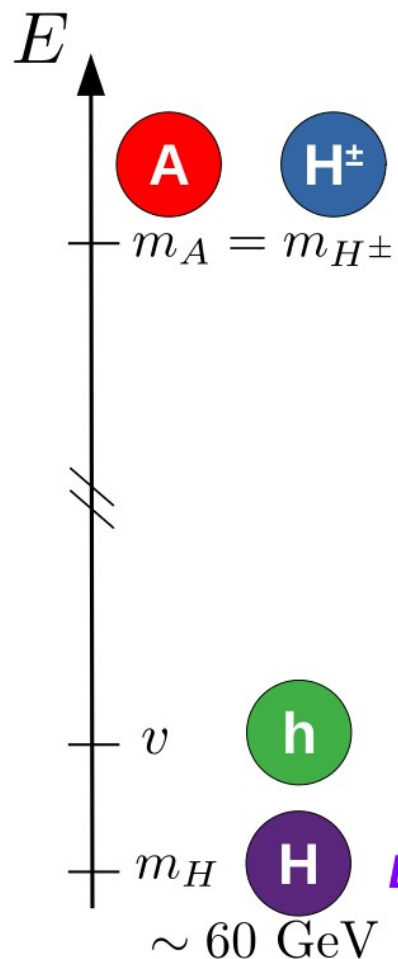
*Direct detection bounds around Higgs resonance region (i.e.  $m_H \sim m_h/2$ )*



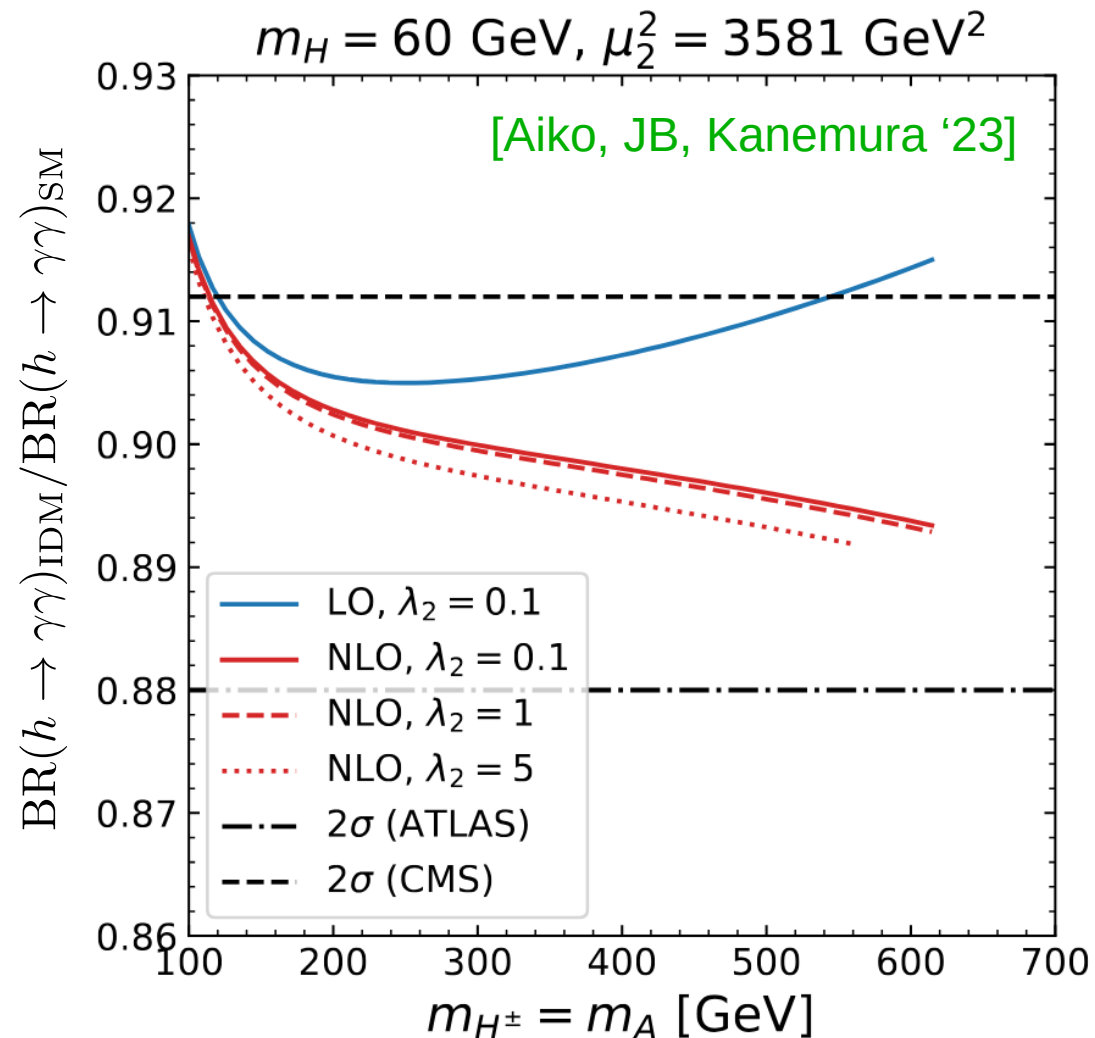
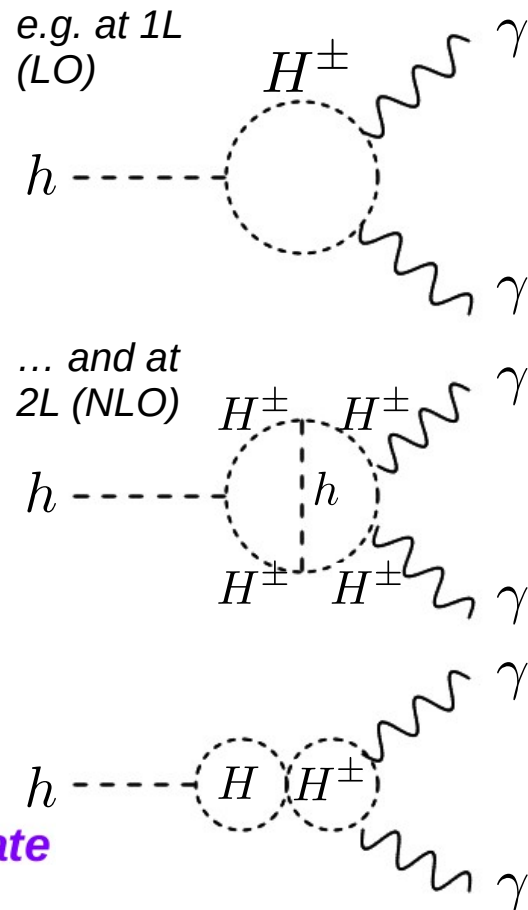
Plot made with micrOMEGAS  
[Bélanger et al. '18]

# Probing dark matter in the Inert Doublet Model with $h \rightarrow \gamma\gamma$

**“Higgs resonance”  
scenario of IDM:**  
DM candidate at  
 $\sim m_h/2$



**Charged Higgs boson  
gives a BSM  
contribution to  $h \rightarrow \gamma\gamma$**



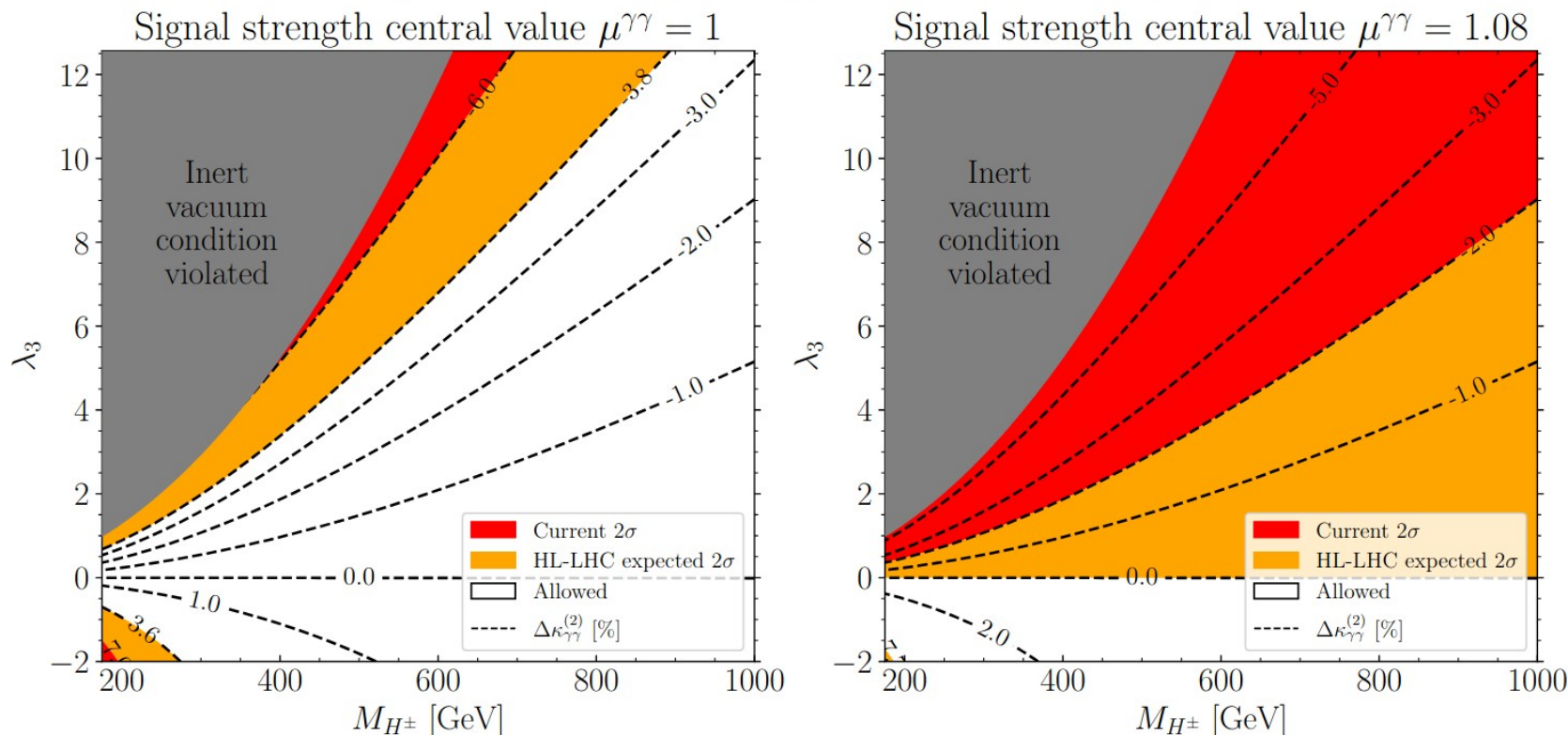
- **Almost entire “Higgs resonance” scenario ( $m_A = m_{H^\pm} > 120 \text{ GeV}$ ) could be excluded by  $h \rightarrow \gamma\gamma$ !**
- **Two-loop analysis crucial for this**

# Probing the Inert Doublet Model with $h \rightarrow \gamma\gamma$

- Significant constraints on IDM parameter space from  $\Gamma(h \rightarrow \gamma\gamma)$  at HL-LHC, especially if central value of signal strength remains  $> 1$  (now:  $\mu^{\gamma\gamma}=1.08$ )

$\Delta\kappa_{\gamma\gamma}^{(2)}$  in the IDM,  $M_{H^\pm} = M_A = M_H + 20$  GeV,  $\lambda_2 = 0.01$

[JB, Gabelmann, Robens, Stylianou '24]



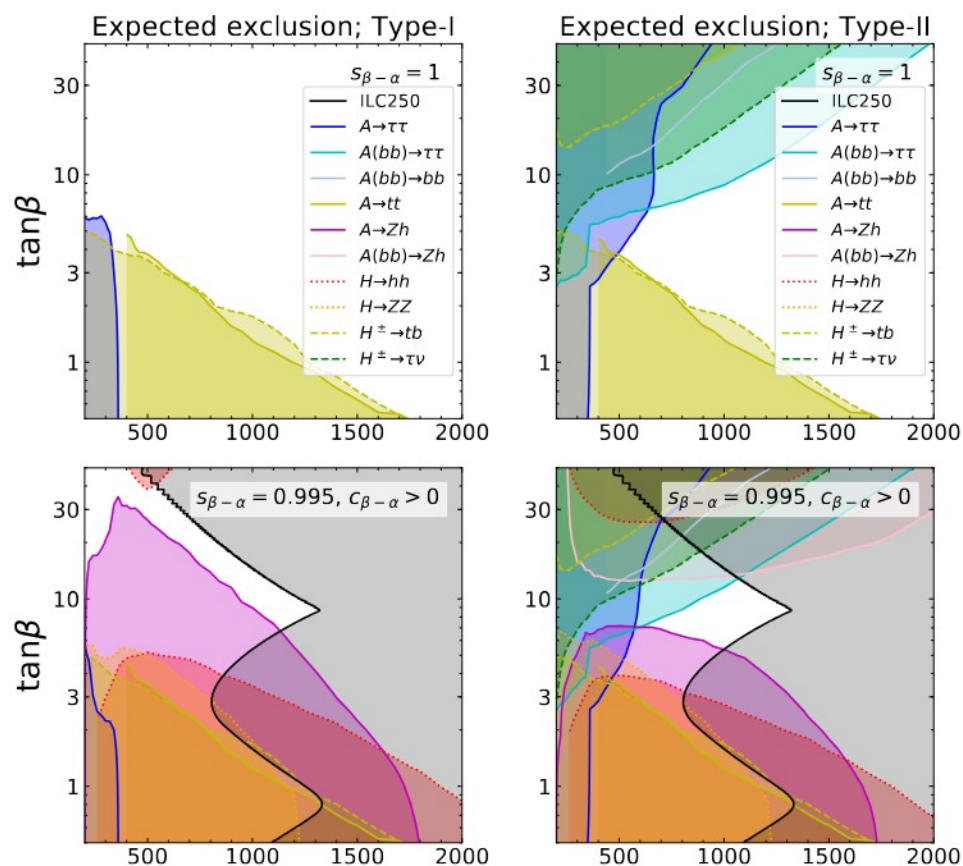
- Tension in a single measurement is of course **not enough**
  - **combined analysis of Higgs properties needed**, e.g. with HiggsSignals [Bechtle et al. '13, ;20], [Bahl et al. '22] or Lilith [Bernon, Dumont '15], [Kraml et al. '19]

# Precise predictions for Higgs properties in BSM models

- Public tools including NLO QCD and EW/BSM corrections for Higgs decays in specific models, e.g.:
  - HDecay [Djouadi et al., '98, '10] and variants like [Mühlleitner et al. '17], [Krause et al. '18], [Krause and Mühlleitner '19] (MSSM, 2HDM, N2HDM, composite Higgs, etc.)
  - Prophecy4f [Bredenstein et al. '06], [Altenkamp, Dittmaier, Rzehak '17], [Altenkamp, Boggia, Dittmaier '18], [Denner, Dittmaier, Mück '19] (2HDM, HSM)
  - H-COUP [Kanemura et al., '17, '19], [Aiko et al., '23] (HSM, 2HDM, IDM)
- Public tools for Higgs/scalar decays beyond LO, in general renormalisable theories
  - SARAH/SPheno [Staub '08-'15], [Porod '03], [Staub, Porod '11] based on [Goodsell, Liebler, Staub '17]
  - FlexibleDecay [Athron et al., '21] (part of FlexibleSUSY [Athron et al., '14, '17]; see also NPointFunctions [Khasianevich et al., '24])
- Inclusion of known higher-order SM contributions is **crucial for reliable comparisons with experimental data**
- Higgs production at LHC dominantly via gluon fusion, less affected by BSM if not charged under  $SU(3)_c$ , but other production channels can also be affected

# Interplay of Higgs measurements with other BSM searches

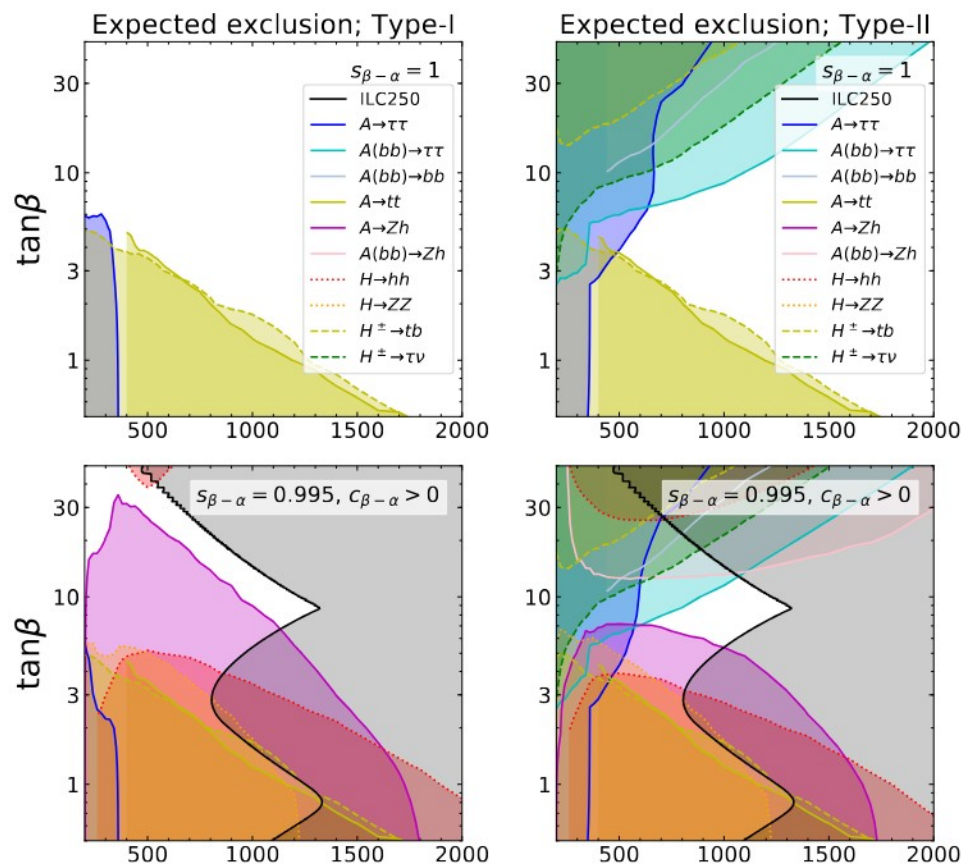
- **Example 1:** Complementary cover of BSM parameter space (here for 2HDM [Aiko et al. '20]) from direct searches and indirect constraints from precision measurements of Higgs properties (finding a deviation sets upper bound on BSM mass scale)



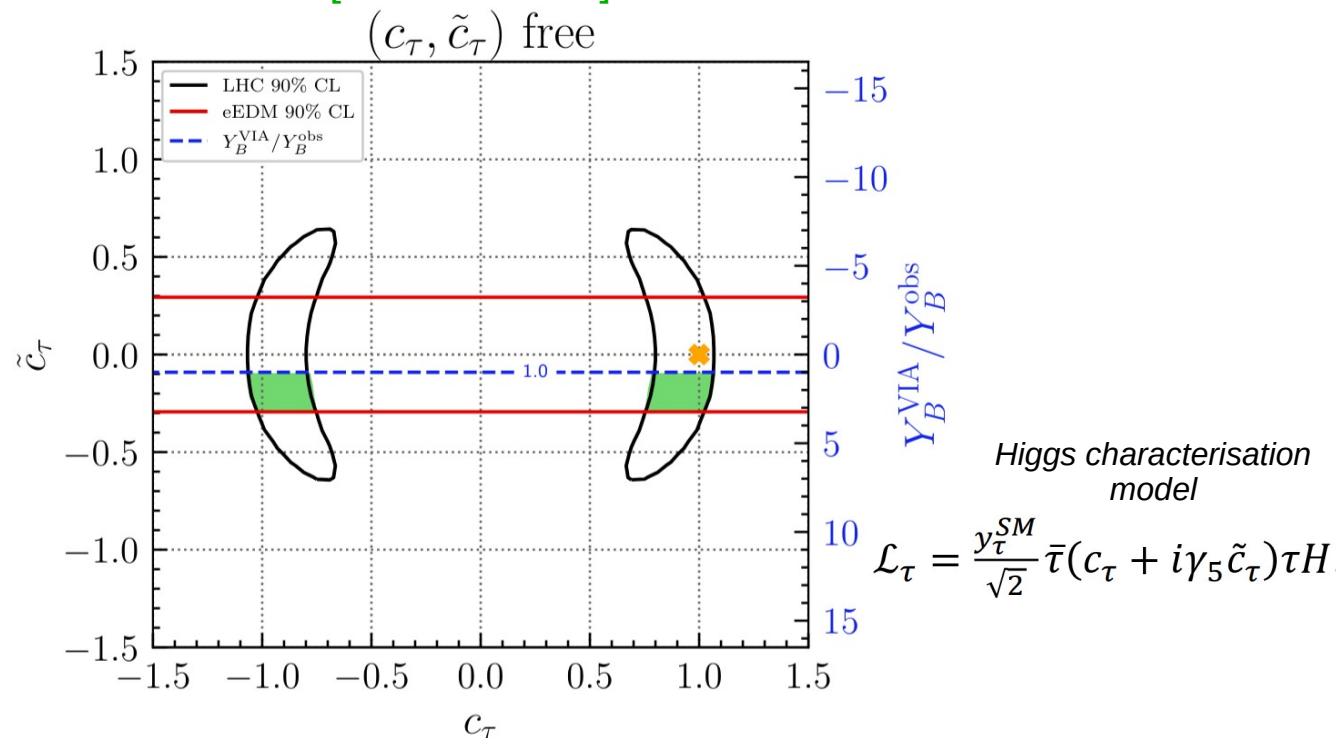


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- **Example 2:** CP violation (needed for baryogenesis, c.f. [Sakharov '67]) in Higgs-fermion interactions so far not very constrained (unlike in Higgs-gauge-boson interactions) → probed via **angular distributions of Higgs processes at colliders**, via **electric dipole moments**, and related to **prediction of BAU**, e.g. here global analysis of CPV in Higgs-tau sector [Bahl et al. '22]



See also [Miralles et al. '24] for CPV in top/Higgs sector (studied within SMEFT)

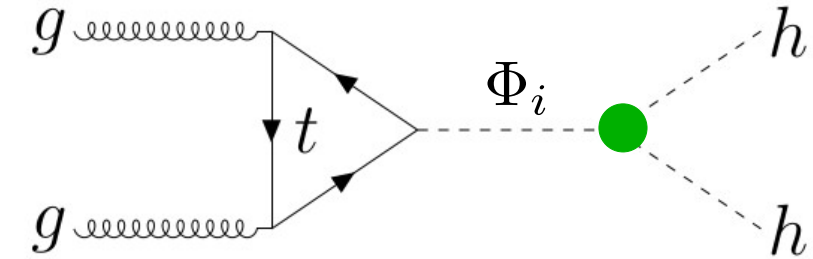
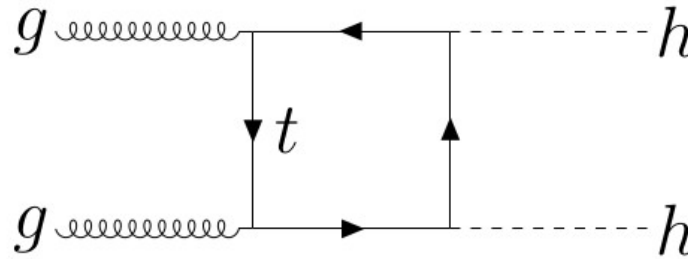
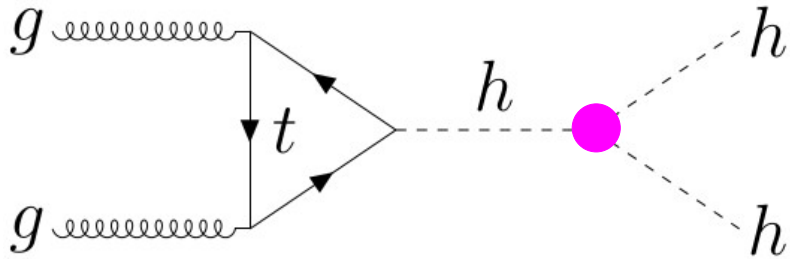
# Di-Higgs production

# Di-Higgs production

➤ Dominant channel for di-Higgs production at (HL-)LHC: **gluon fusion**

Here, leading order (LO) diagrams, involving top quark (dominant contribution among quark loops)

$h \equiv h_{125}$   
[discovered Higgs boson]



## “Non-resonant contributions”

- Standard Model (SM)-like diagrams
- Involves the trilinear self-coupling of  $h_{125}$  —  $\lambda_{hhh}$ 
  - **probe of the Higgs potential**
- Large destructive interference between triangle and box diagram
  - **suppression of cross-section in SM**
  - **large changes in di-Higgs cross-section possible from BSM effects in  $\lambda_{hhh}$**

## “Resonant contributions”

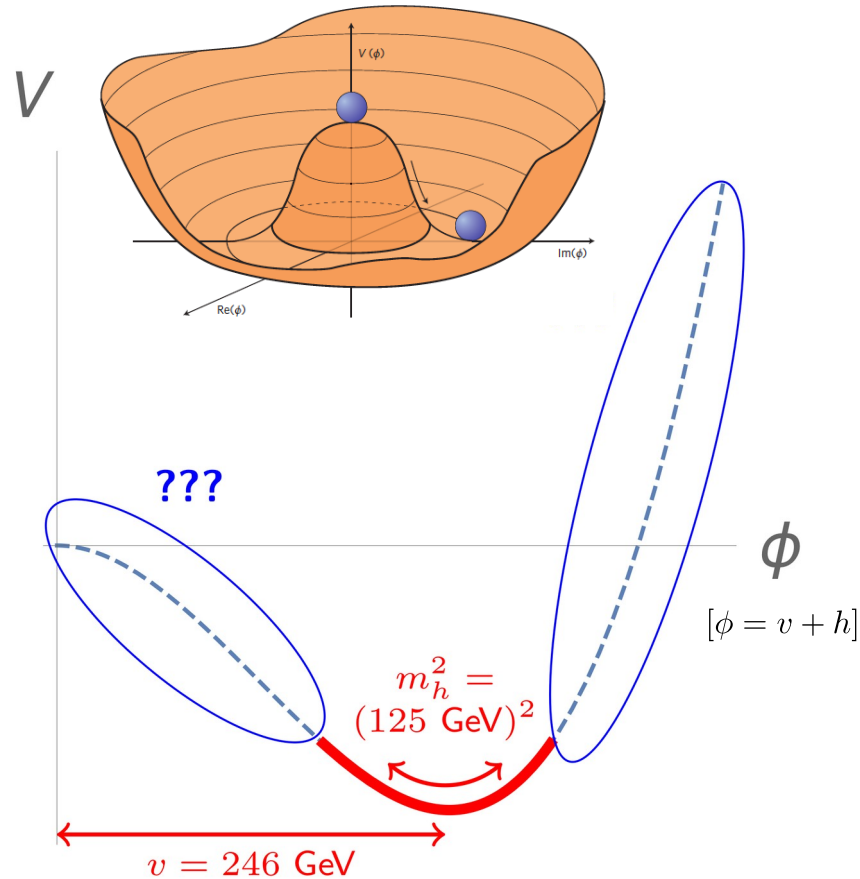
- Diagrams involving BSM scalars in s-channel
  - (here generically denoted  $\Phi_i$ )
  - **collider searches for BSM scalars**
- Involve BSM trilinear scalar couplings  $\lambda_{ijk}$  → **probe of Higgs potential in extended scalar sectors**

*NB: in the following, I focus on **higher-order BSM corrections to  $gg \rightarrow h_i h_j$***

*Higher-order QCD/EW corrections to  $ggF$  and other channels are of course crucial → see talk of S. Jones!*



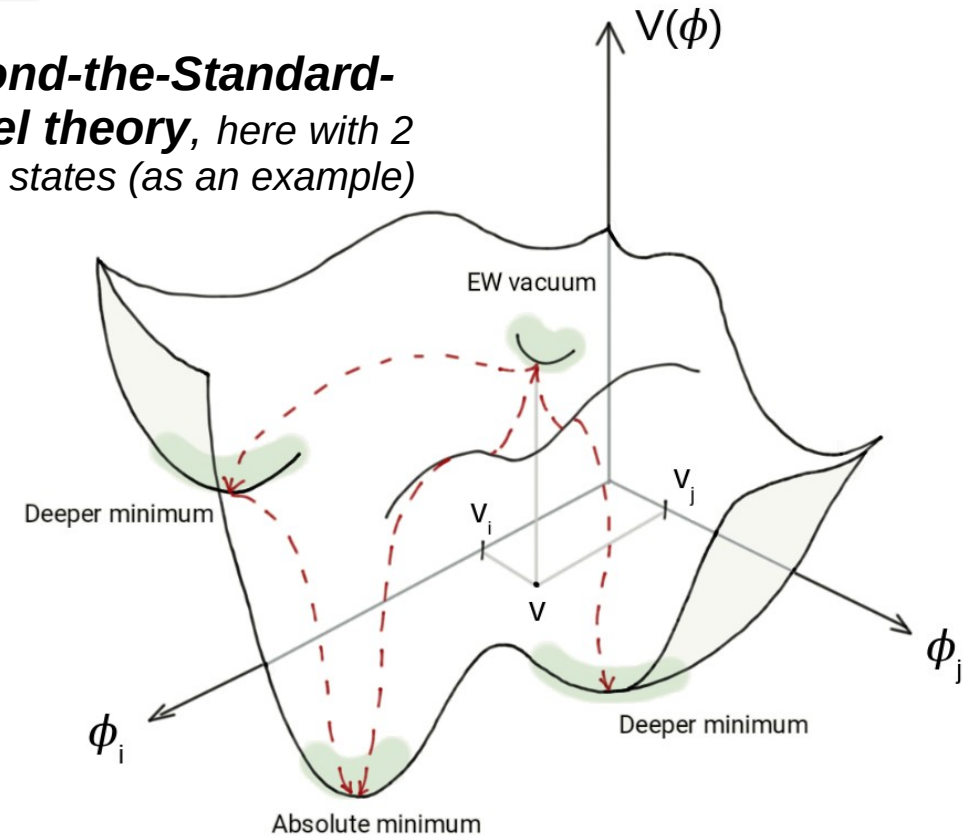
# Form of the Higgs potential and trilinear scalar couplings



## One field direction

↔ shape of potential away from EW minimum is related to  $\lambda_{hhh}$

**Beyond-the-Standard-Model theory**, here with 2 scalar states (as an example)



## Extended scalar sectors

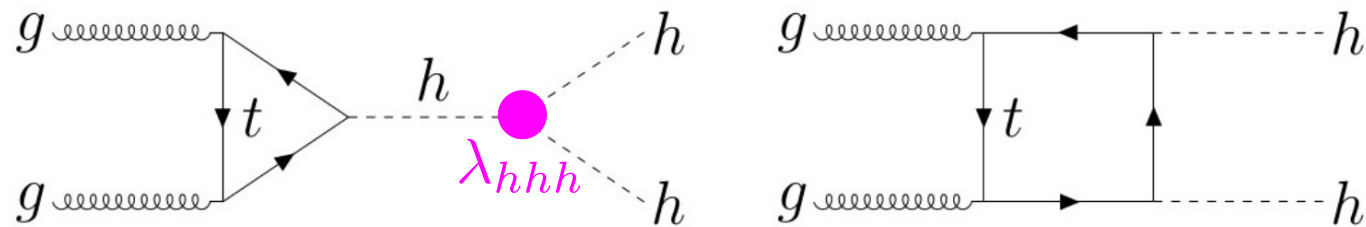
→ more complex Higgs potentials  
→ more trilinear scalar couplings needed to reconstruct potential

➤ **Form of Higgs potential related to how EWPT took place in early Universe**

# Interference in non-resonant di-Higgs production

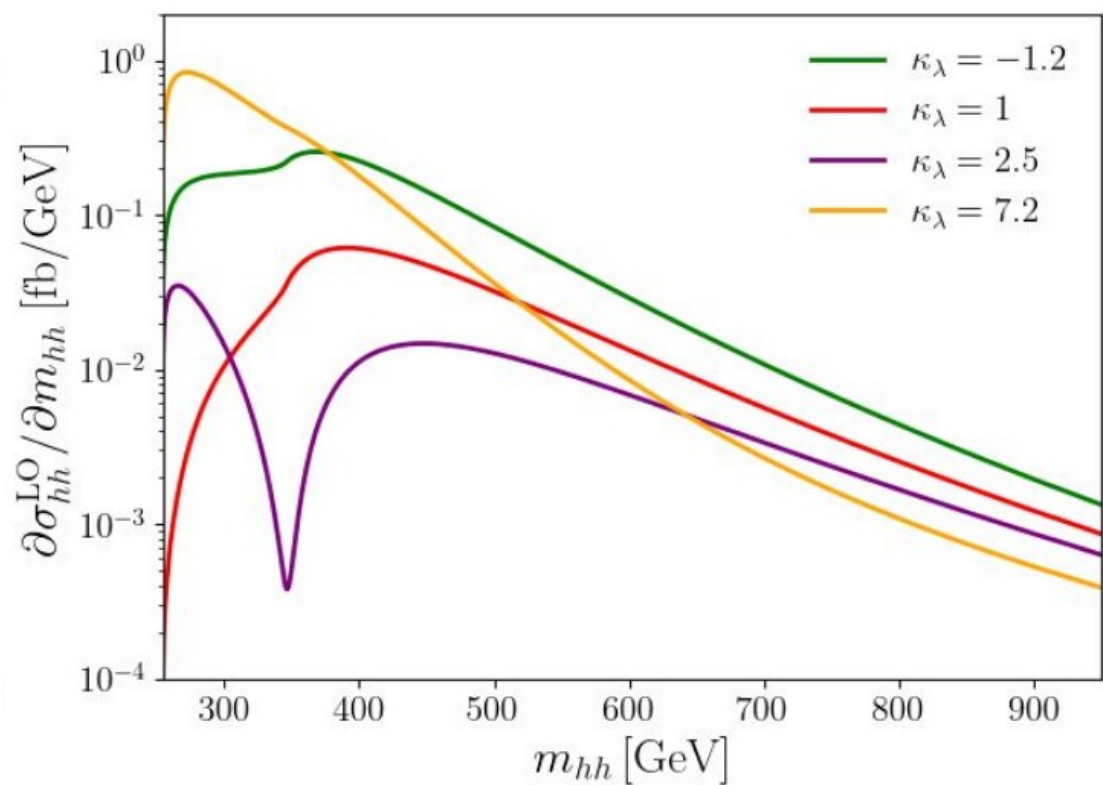
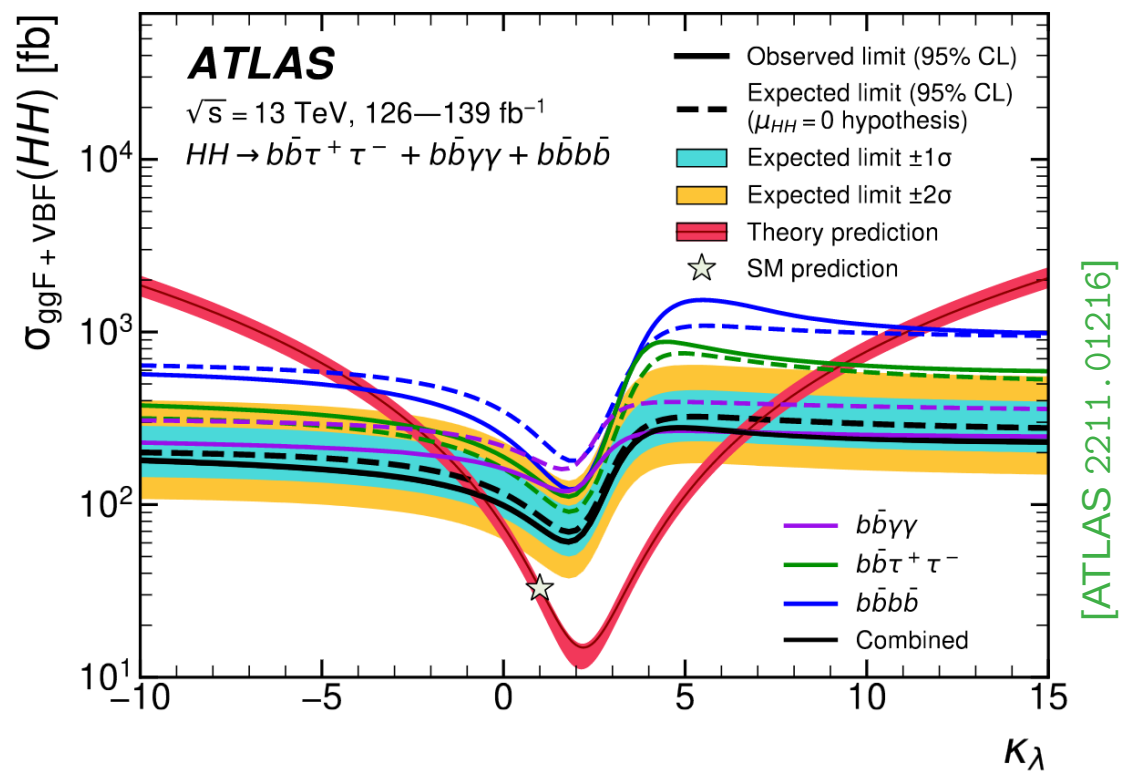
Coupling modifier:

$$\kappa_\lambda \equiv \frac{\lambda_{hhh}}{(\lambda_{hhh}^{(0)})^{\text{SM}}}$$



Relative change in total cross-section for varying  $\kappa_\lambda$

Differential  $m_{hh}$  distributions for varied  $\kappa_\lambda$



Plot by [K. Radchenko Serdula '24]

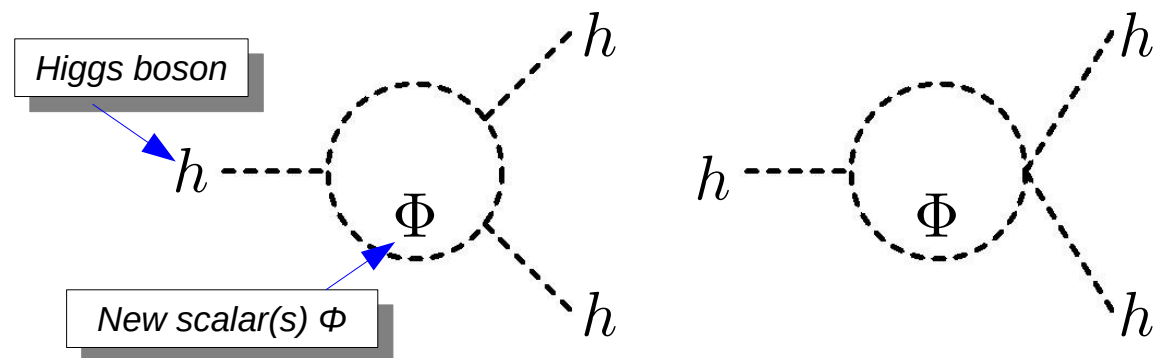
Note: impact of change in top Yukawa → overall shift (up/down) of distribution

# Mass-splitting effects in the trilinear Higgs coupling

- Latest bounds on  $\lambda_{hhh}$  [ATLAS PRL '24]

$$-1.2 < \kappa_\lambda = \frac{\lambda_{hhh}}{(\lambda_{hhh}^{(0)})^{\text{SM}}} < 7.2$$

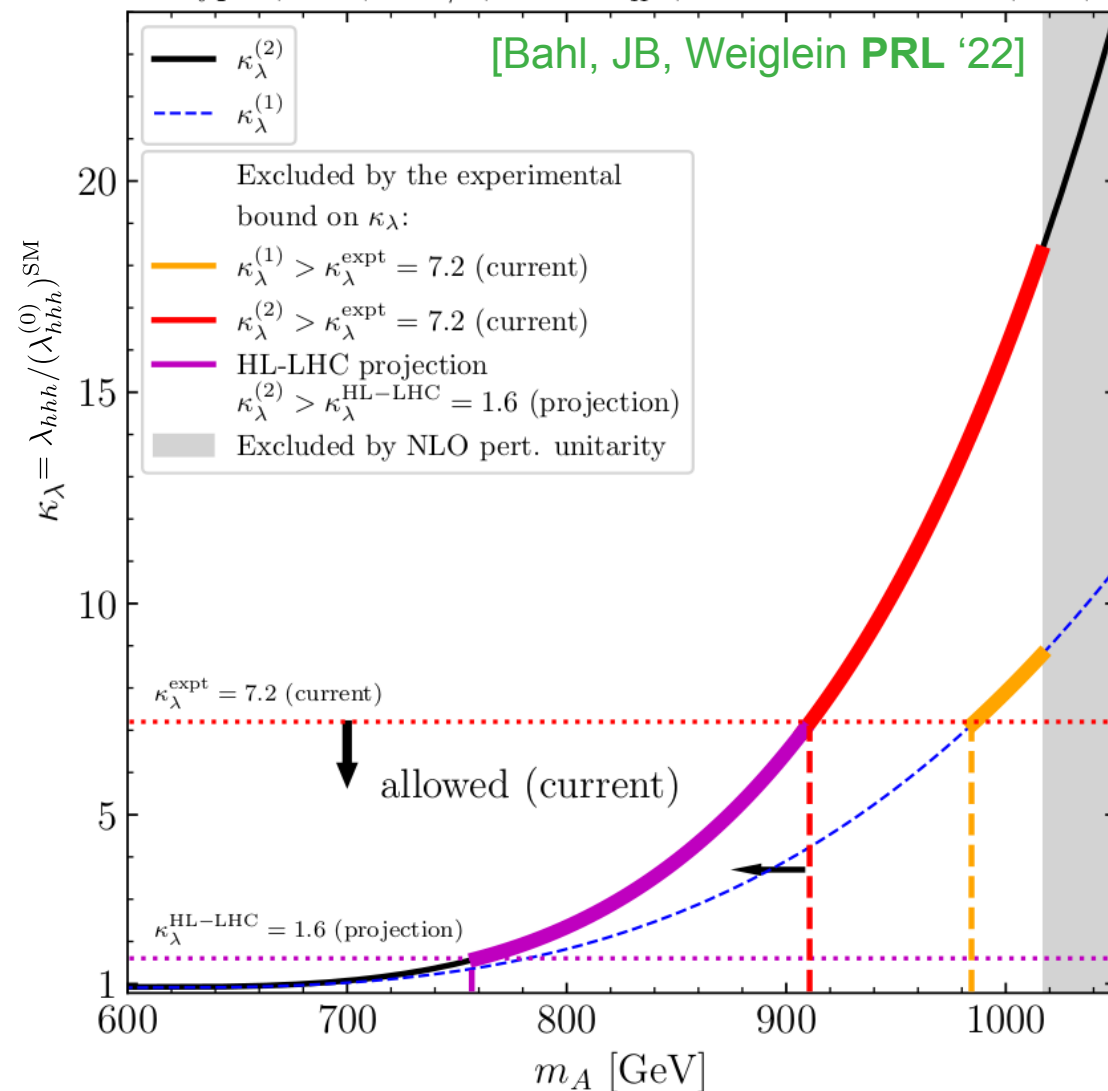
- **Large effects from New Physics possible in  $\lambda_{hhh}$ ,**  
due to radiative corrections from extra scalars,  
e.g. at leading order (one loop)



Physical nature of these large BSM effects **confirmed by explicit two-loop calculations**, e.g. [JB, Kanemura '19]

- BSM deviations in  $\kappa_\lambda$  **can** also be **motivated from the point of view of early-Universe evolution**, e.g. **strong first-order EW phase transition** (*more in a few slides*)

2HDM type I,  $\alpha = \beta - \pi/2$ ,  $m_A = m_{H^\pm}$ ,  $M = m_H = 600$  GeV,  $\tan \beta = 2$

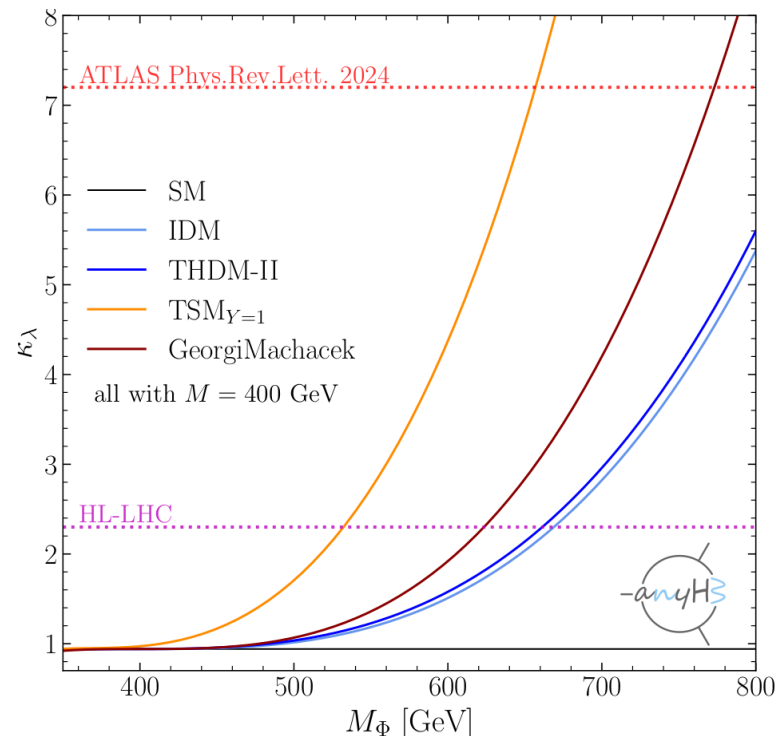


# Large corrections to trilinear scalar couplings

## Mass-splitting effects in various BSM models:

anyH3 v1 [Bahl, JB, Gabelmann, Weiglein '23]

public tool for full one-loop calculation of  $\lambda_{hhh}$  in arbitrary renormalisable models, using UFO inputs



## Many more examples with model-specific calculations:

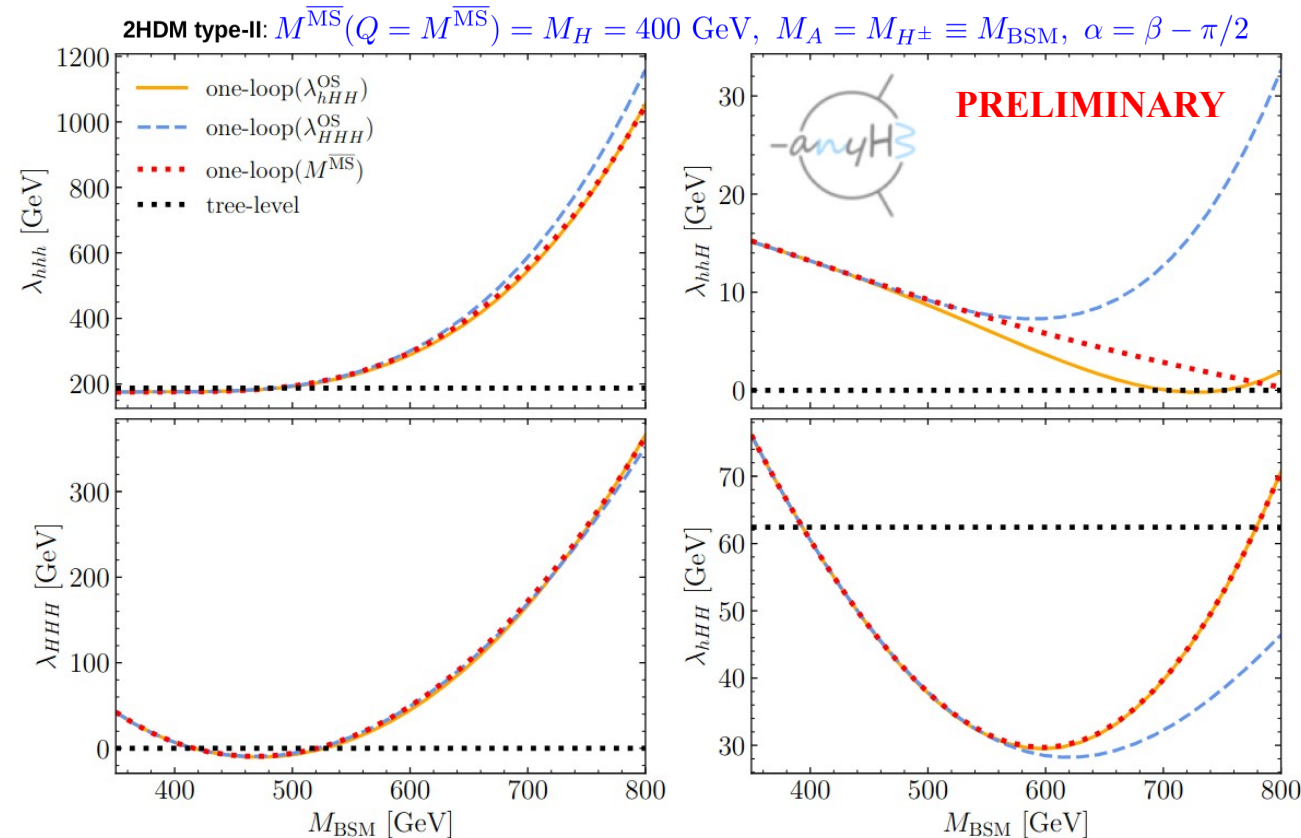
at 1L: [Kanemura et al. '04, '16], [Hollik, Penaranda '04], [Aoki et al. '12], [Dao et al. '13], [Hashino, Kanemura, Orikasa '16], [Basler et al. '17, '19], [Chiang et al. '18];

... and at 2L: [Brucherseifer et al. '13], [Dao et al. '15], [Senaha '18], [JB, Kanemura '19], [JB, Kanemura, Shimoda '20], [Borschensky et al '22], etc.

## Mass-splitting effects in trilinear scalar couplings:

anyH3 v2 [Bahl, JB, Gabelmann, Radchenko Serdula, Weiglein WIP] → calculation extended to generic  $\lambda_{ijk}$

Here for a benchmark example in an aligned 2HDM and with different renormalisation schemes

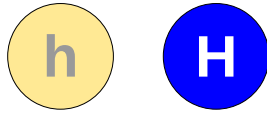


See also e.g. [Arco, Heinemeyer, Mühlleitner, '25]

# Two example models to investigate di-Higgs production

- **RxSM: general singlet extension of the SM**  
(without a  $Z_2$  symmetry)

- add a real singlet to SM
- 2 CP-even Higgs bosons



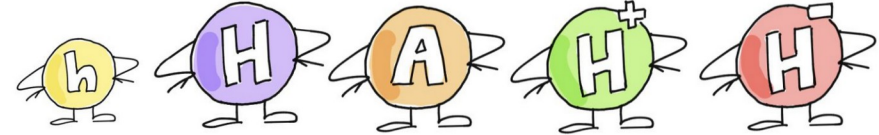
- Scalar sector parametrised in terms of:

$$\underbrace{m_h^2, v}_{\text{known}}, \underbrace{m_H^2, \alpha, v_S, \kappa_S, \kappa_{SH}}_{\text{free}}$$

with

$m_h, m_H$  : masses of detected and BSM Higgs bosons  
 $\alpha$  : CP-even mixing angle  
 $v, v_S$  : EW and singlet VEVs  
 $\kappa_S, \kappa_{SH}$  : Lagrangian trilinear couplings

- **2HDM: Two-Higgs-Doublet Model**  
(here CP-conserving variant)



Drawing by  
[K. Radchenko  
Serdula]

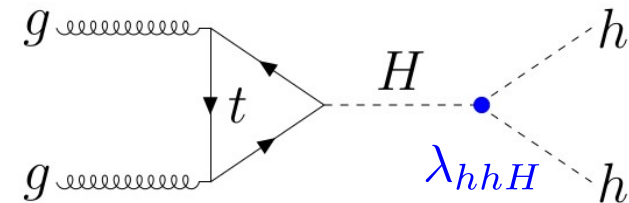
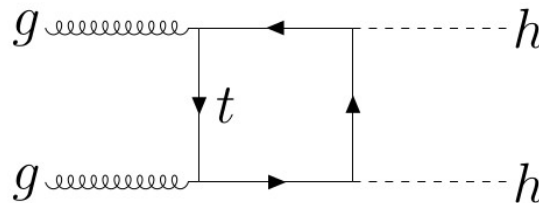
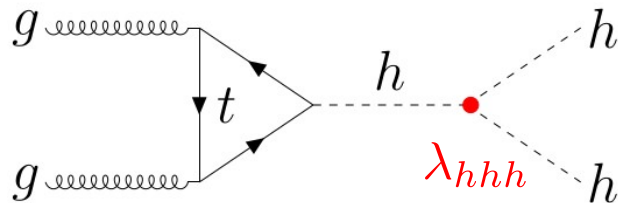
- Scalar sector parametrised in terms of:

$$\underbrace{m_h^2, v}_{\text{known}}, \underbrace{m_H^2, m_A^2, m_{H^\pm}^2, M, \alpha, \tan \beta}_{\text{free}}$$

with

$m_{h,H,A,H^\pm}$  : masses of detected and BSM Higgs bosons  
 $\alpha$  : CP-even mixing angle  
 $\tan \beta \equiv v_2/v_1$  : ratio of VEV of 2 doublets  
 $v$  : EW VEV  
 $M$  : BSM mass scale (controls decoupling)

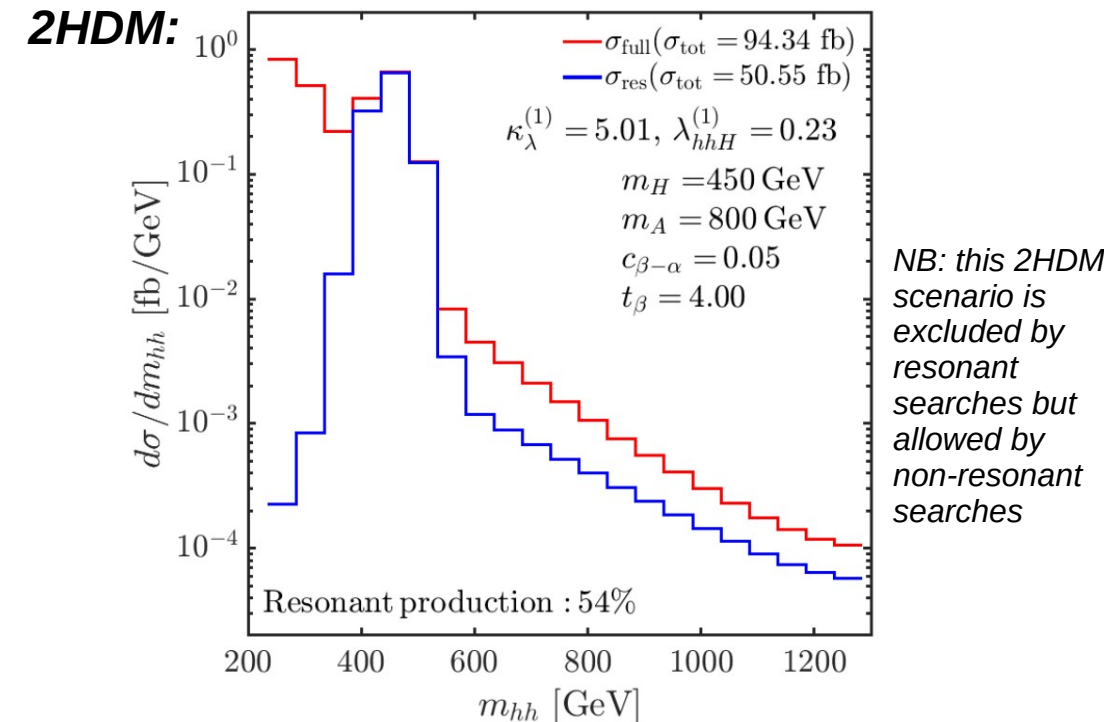
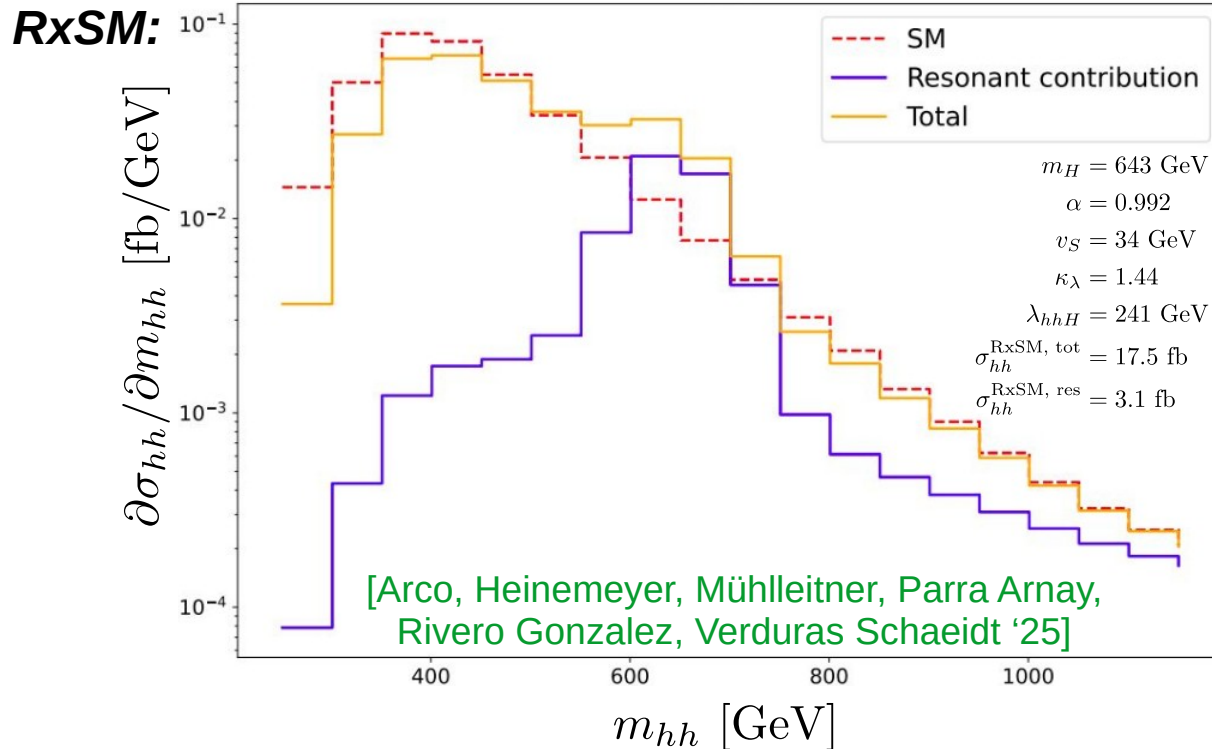
- Three **leading diagrams** in di-Higgs production, with **significant dependence on 2 relevant trilinears:**  
 $\lambda_{hhh}$  and  $\lambda_{hhH}$





# Interference effects: resonant contributions vs full distributions

- Including interference between non-resonant and resonant contributions can **drastically change di-Higgs invariant mass distributions**
- Distributions computed with HPAIR ([Plehn, Spira, Zerwas '96], [Dawson, Dittmaier, Spira '98], [Abouabid et al. '22], [Arco et al., '25]), shown here after experimental effects taken into account (15% smearing and 50 GeV binning)
- Relatively good agreement between peak of resonant and total distributions, but **away from peak they can differ by up to 2 orders of magnitude**
  - large impact of interference effects **warrants analysis of these scenarios with full predictions**
  - possible with **codes for di-Higgs predictions** (e.g. HPAIR, anyHH), or **reweighting tools**, e.g. HHReweighter [Feuerstake et al '24]



NB: this 2HDM scenario is excluded by resonant searches but allowed by non-resonant searches

[Heinemeyer, Mühlleitner, Radchenko, Serdula, Weiglein '24]

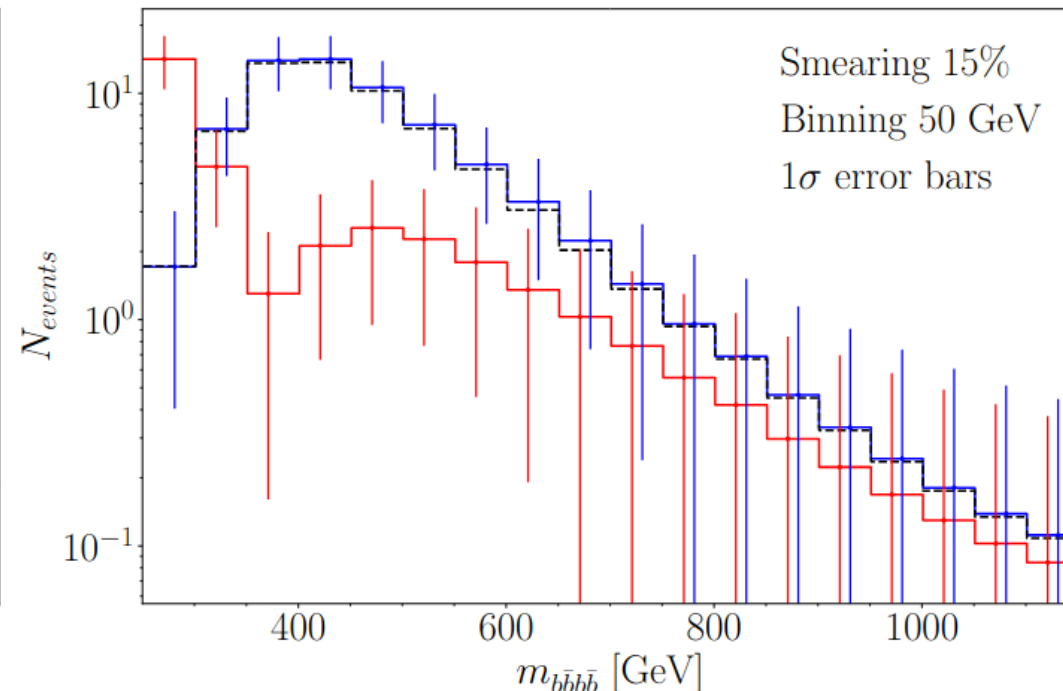
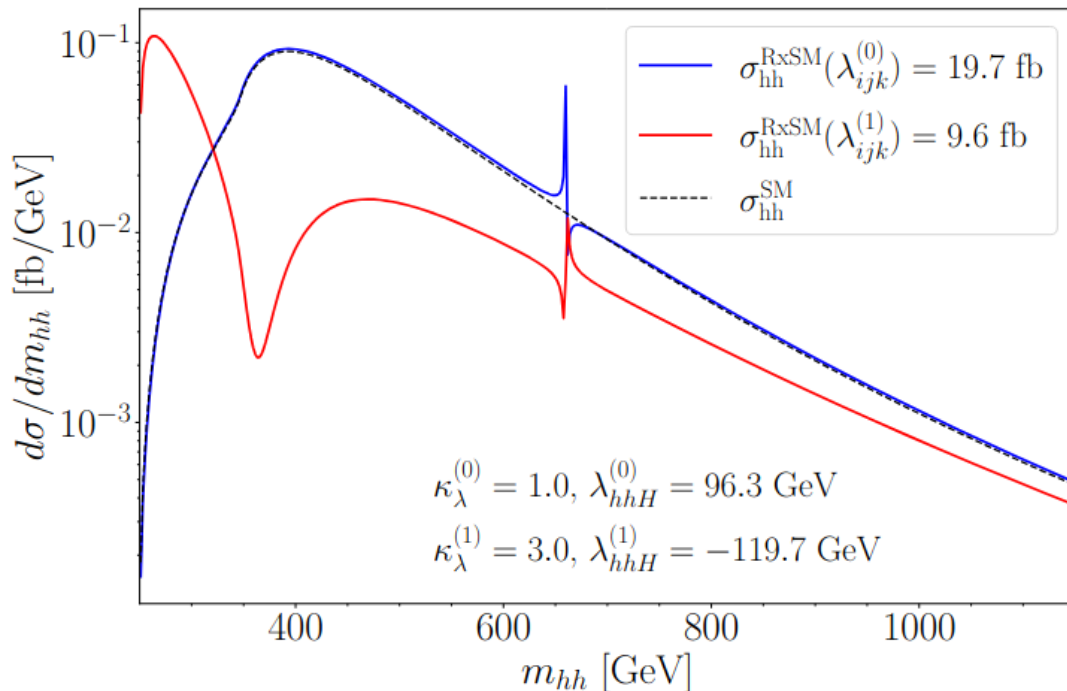
# Impact of NLO corrections in the RxSM

[JB, Heinemeyer, Parra Araya, Verduras Schaeidt '25]

## Impact on di-Higgs invariant mass distributions

BP1:  $m_H = 659.4$  GeV,  $\cos \alpha = 0.99$ ,  $v_S = 56.1$  GeV,  $\kappa_S = -880$  GeV,  $\kappa_{SH} = -880$  GeV,  $Z^{(0)} = 0.3$ ,  $Z^{(1)} = 9.3$

NB: total cross-section is SM-like!

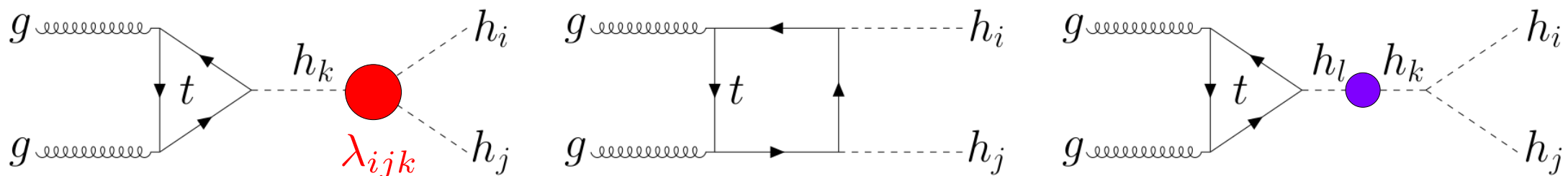


- Cross-sections computed with RxSM-specific version of HPAIR [Arco et al. '25]; results shown at LO in QCD
- Large radiative corrections to both trilinear couplings,  $\lambda_{hhh}$  and  $\lambda_{hhH}$ , modify the interference pattern and shift the dip from  $m_{hh} \sim 250$  GeV to 350 GeV + change the peak-dip structure at  $m_H$  into dip-peak
- After taking into account experimental effects (with smearing and binning), an analysis with tree-level trilinears ( $Z^{(0)}=0.3$ ) would not be able to find a deviation from the SM, but an analysis with one-loop ones would ( $Z^{(1)}=9.3$ )

# Di-Higgs production in arbitrary models: anyHH

[Bahl, JB, Gabelmann,  
Radchenko Serdula,  
Weiglein *WIP*]

- **anyHH: Total and differential cross-sections** (so far, at LO in QCD) for  $gg \rightarrow h_i h_j$  including:
  - **1L corrections to  $\lambda_{ijk}$**  (computed by anyH3)
  - **BSM contributions in s-channel diagrams**
  - **momentum-dependence** both in vertex corrections and in propagators



- Takes UFO model files as inputs, as anyH3. So far limited to models without additional coloured particles.
- Good agreement found with existing results in the literature – e.g. HPAIR (*details in backup*)

*See also parallel talk of M. Gabelmann tomorrow!*



# Impact of NLO corrections in the 2HDM

[Bahl, JB, Gabelmann,  
Radchenko Serdula,  
Weiglein WIP]

Example in **aligned 2HDM**, with di-Higgs cross-section and  $m_{hh}$  distributions computed with anyHH

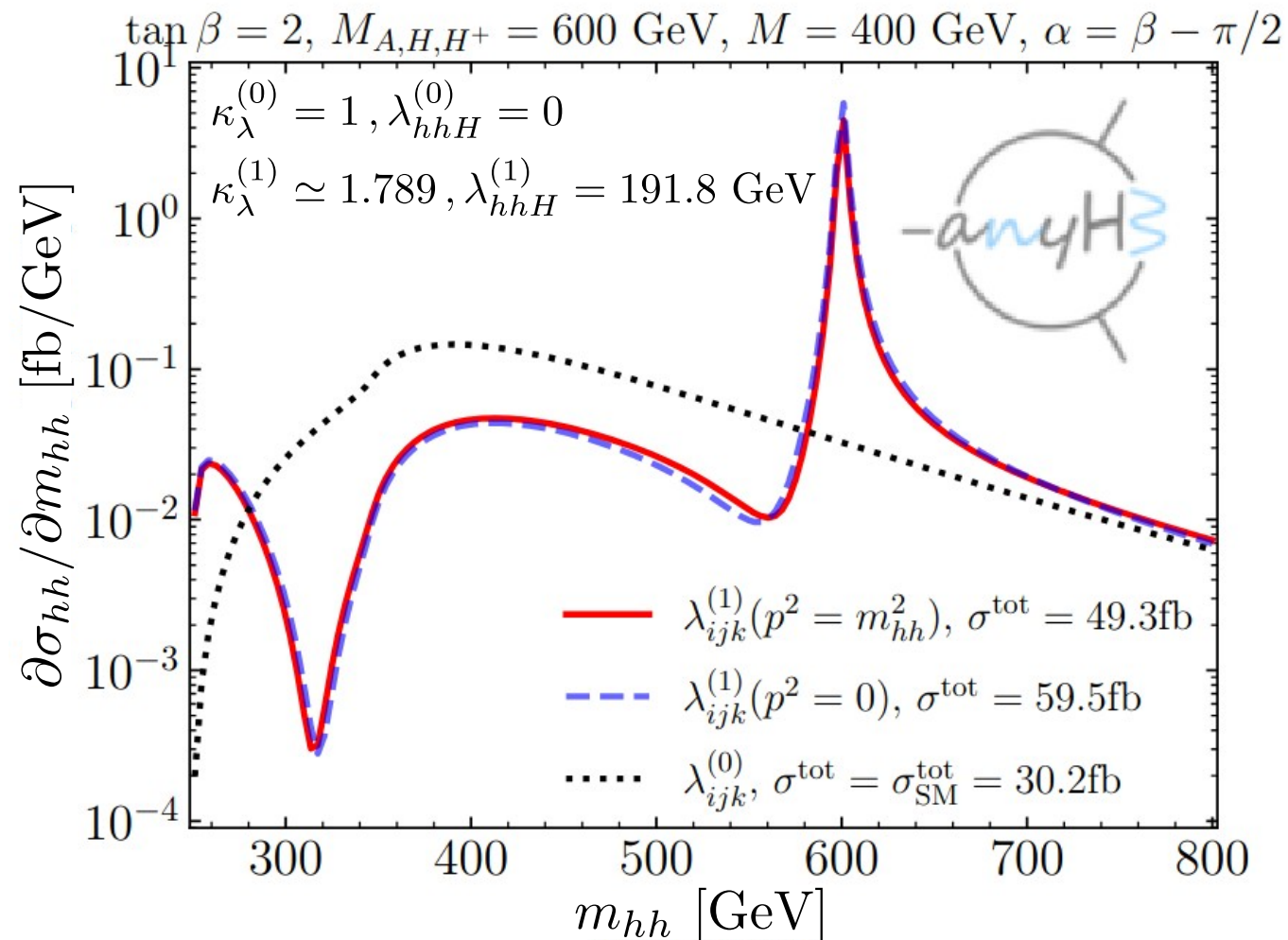
→  $\kappa_\lambda^{(0)} = 1$ ;  $\lambda_{hhH}^{(0)} = 0$  (due to alignment limit)

## Impact of loop corrections to trilinear couplings

Black vs red curves → huge impact of loop corrections to  $\lambda_{ijk}$  on both cross-section and distributions

## Impact of momentum in s-channel diagrams

Blue vs red curves → O(20%) impact of momentum in  $\lambda_{ijk}$

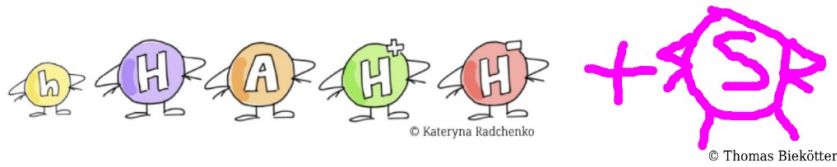


Note: similar results for impact of loop corrections also found [Heinemeyer, Mühlleitner, Radchenko Serdula, Weiglein '24]

# Results in the N2HDM with anyHH

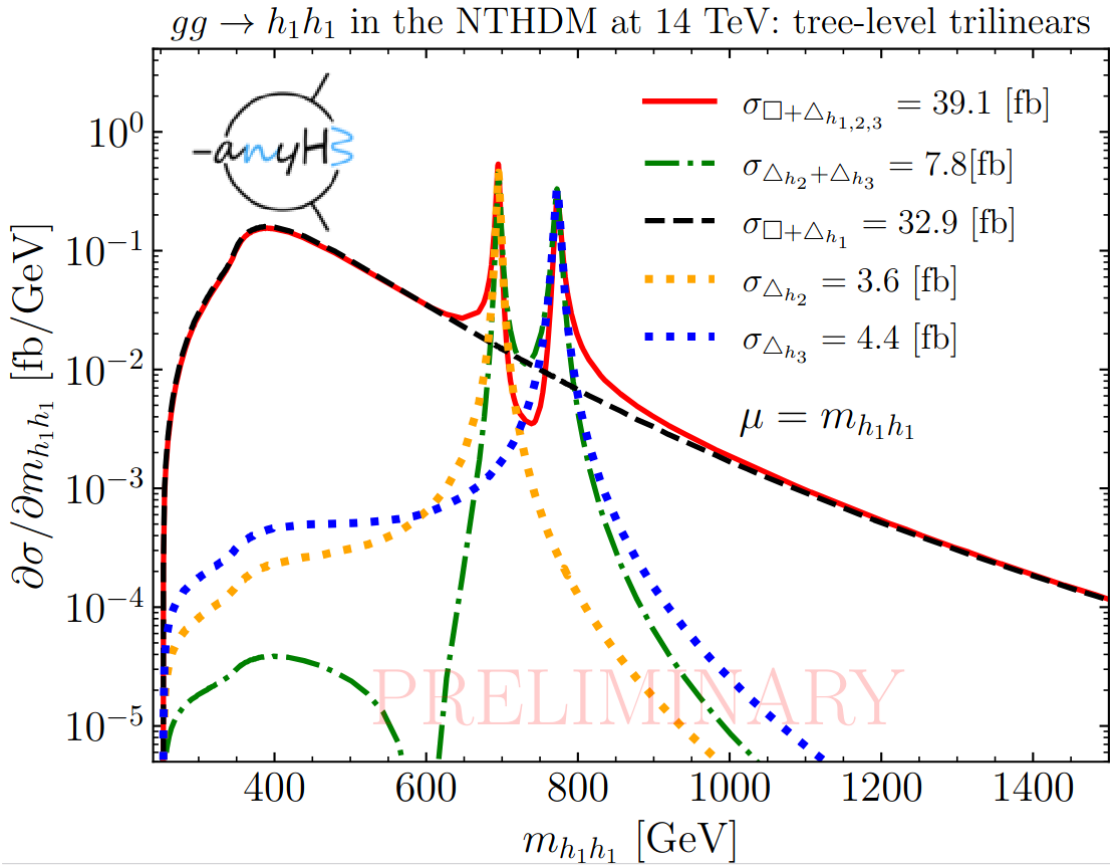
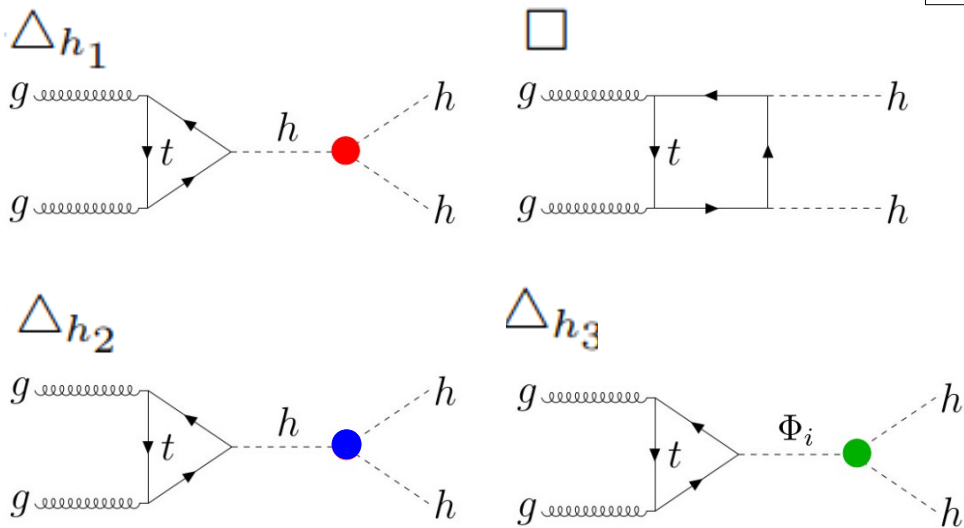
[Bahl, JB, Gabelmann, Radchenko Serdula, Weiglein WIP]

- N2HDM = 2HDM + real singlet
  - 3 CP-even mass eigenstates  $h_1, h_2, h_3$



- anyHH allows computing contributions to di-Higgs production together or separately
  - *find impact of interference*
- Here first with **tree-level trilinear scalar couplings**

$\kappa_\lambda^{(0)}$	0.97
$\kappa_\lambda^{(1)}$	2.18
$\lambda_{h_1 h_1 h_2}^{(0)}$ [GeV]	93.5
$\lambda_{h_1 h_1 h_2}^{(1)}$ [GeV]	40.3
$\lambda_{h_1 h_1 h_3}^{(0)}$ [GeV]	160.5
$\lambda_{h_1 h_1 h_3}^{(1)}$ [GeV]	342.8



## N2HDM benchmark definition:

$\alpha_1 = 1.019,$   
 $M_{h_1} = 125 \text{ GeV},$   
 $M_A = 673 \text{ GeV},$

$\alpha_2 = -0.076,$   
 $M_{h_2} = 695 \text{ GeV},$   
 $M_{H^\pm} = 762 \text{ GeV},$   
 $v_S = 415.4 \text{ GeV}.$

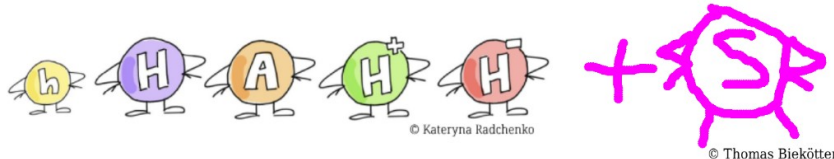
$\alpha_3 = 0.960,$   
 $M_{h_3} = 773 \text{ GeV},$   
 $M_{12} = 367 \text{ GeV},$

Allowed by flavour,  
Higgs phys. EWPO,  
vacuum stability,  
perturbative unitarity

# Results in the N2HDM with anyHH

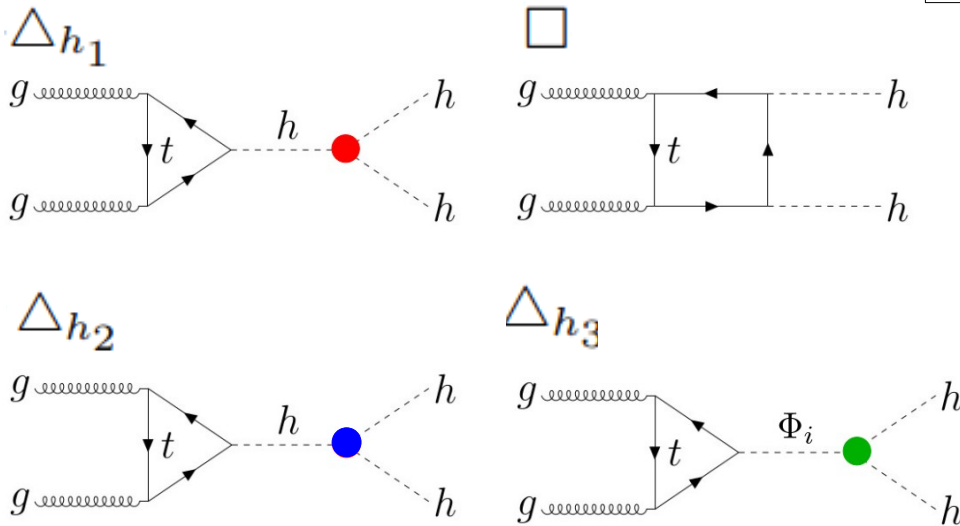
[Bahl, JB, Gabelmann,  
Radchenko Serdula,  
Weiglein WIP]

- **N2HDM = 2HDM + real singlet**  
→ 3 CP-even mass eigenstates  
 $h_1, h_2, h_3$

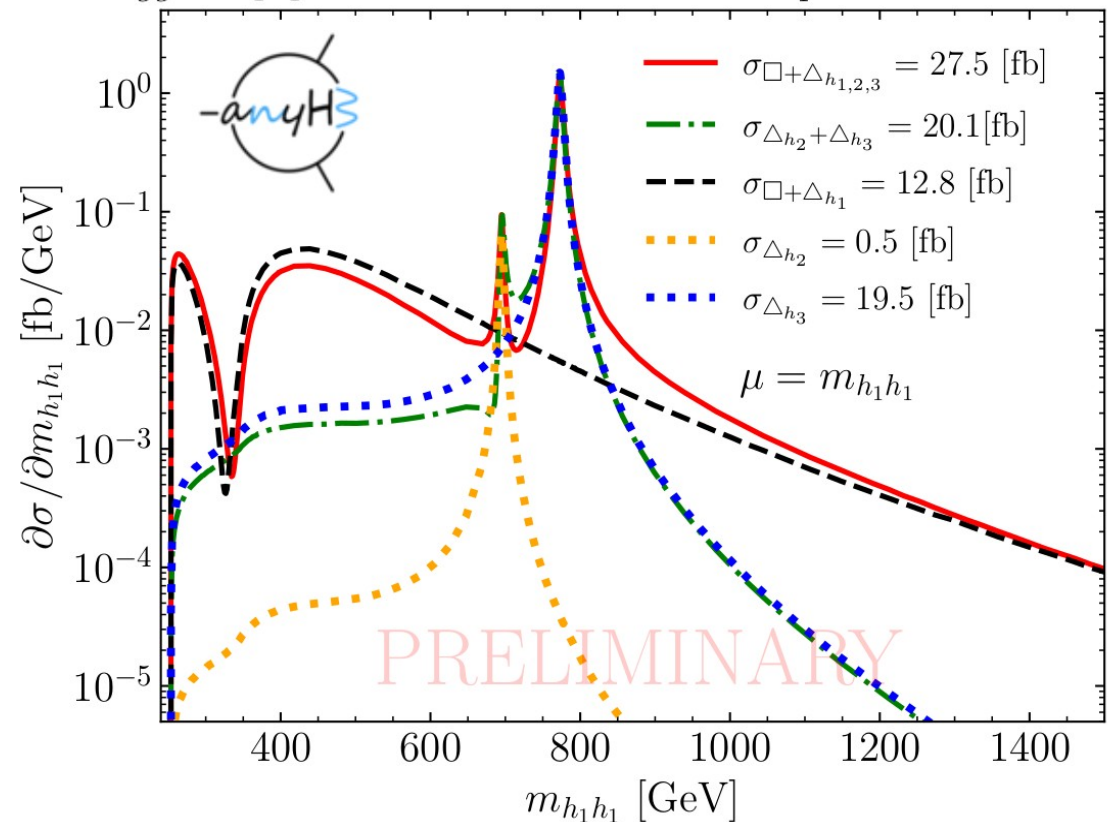


- anyHH allows computing contributions to di-Higgs production together or separately  
→ *find impact of interference*
- Here first with **loop-corrected trilinear scalar couplings**

$\kappa_\lambda^{(0)}$	0.97
$\kappa_\lambda^{(1)}$	2.18
$\lambda_{h_1 h_1 h_2}^{(0)}$ [GeV]	93.5
$\lambda_{h_1 h_1 h_2}^{(1)}$ [GeV]	40.3
$\lambda_{h_1 h_1 h_3}^{(0)}$ [GeV]	160.5
$\lambda_{h_1 h_1 h_3}^{(1)}$ [GeV]	342.8



$gg \rightarrow h_1 h_1$  in the NTHDM at 14 TeV: loop-corrected trilinears



N2HDM benchmark definition:

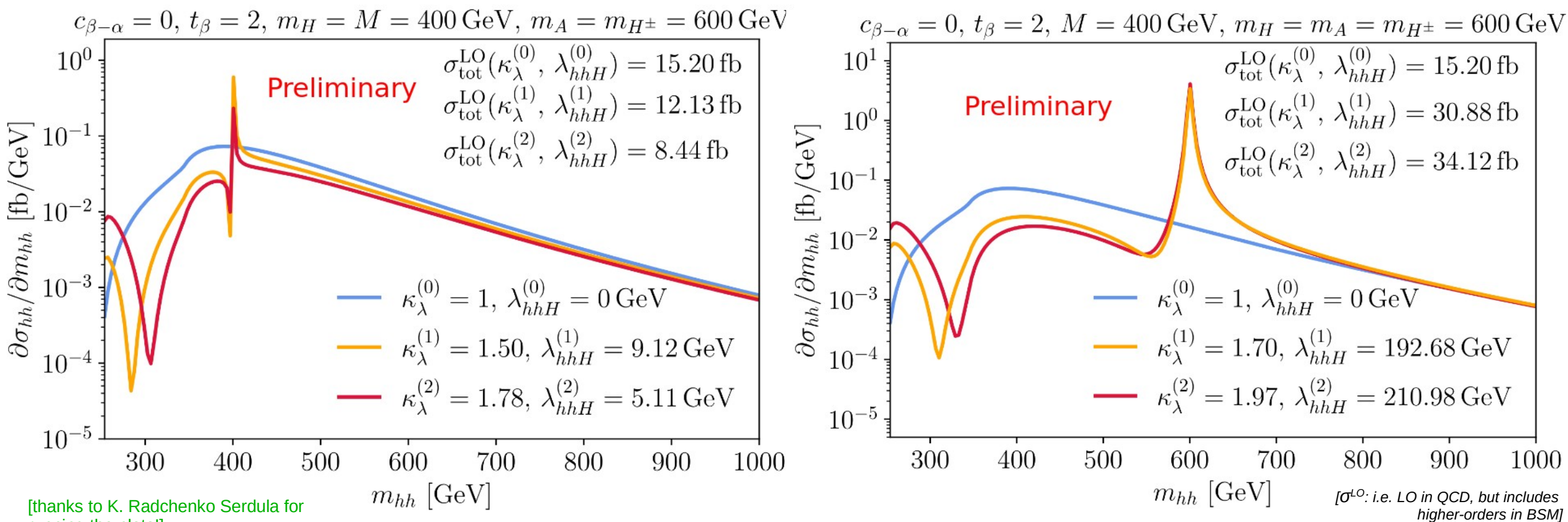
$\alpha_1 = 1.019,$	$\alpha_2 = -0.076,$	$\alpha_3 = 0.960,$
$M_{h_1} = 125 \text{ GeV},$	$M_{h_2} = 695 \text{ GeV},$	$M_{h_3} = 773 \text{ GeV},$
$M_A = 673 \text{ GeV},$	$M_{H^\pm} = 762 \text{ GeV},$	$M_{12} = 367 \text{ GeV},$
$\tan \beta = 1.53,$	$v_S = 415.4 \text{ GeV}.$	

Allowed by flavour,  
Higgs phys. EWPO,  
vacuum stability,  
perturbative unitarity

# Impact of NNLO BSM corrections in the 2HDM

## What about higher orders?

Here: example in **aligned 2HDM**, with di-Higgs cross-section and  $m_{hh}$  distributions computed with anyHH and with 2L corrections to  $\lambda_{hhh}$  and  $\lambda_{hhH}$  from [JB, Egle, Verduras Schaeidt WIP]

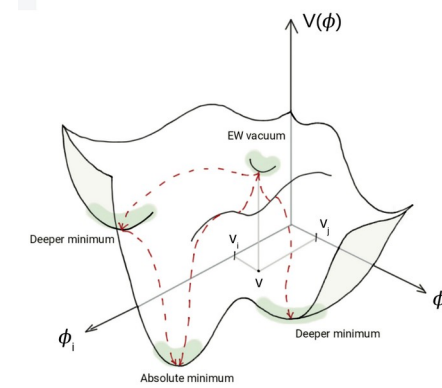


Note: see also [Degrassi, Gröber, Slavich '25] for NNLO BSM corrections to  $\lambda_{hhh}$ ,  $\lambda_{hhH}$  and total di-Higgs cross-section

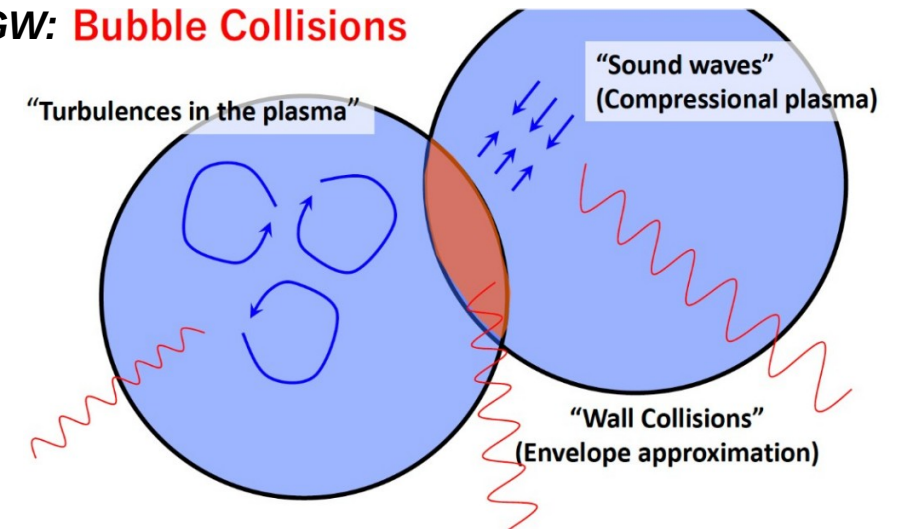


# Complementary probes of SFOEWPT

- SFOEWPT motivated by scenario of **electroweak baryogenesis**, as a possible solution to BAU,
  - needed fulfill 3<sup>rd</sup> Sakharov condition [Sakharov '67] (departure from thermal equilibrium)
  - c.f. talk by L. Biermann tomorrow*
- **Probes of SFOEWPT:**
  - *reconstruct form of Higgs potential realised in Nature*
    - access **trilinear Higgs/scalar coupling(s)**, e.g. at (HL-)LHC via di-Higgs production processes
  - *search for **cosmological relics** of a strong first-order phase transition*
    - stochastic background of **gravitational waves** (GW)
      - probed with space-based GW interferometers like LISA
    - **primordial black holes** (PBHs) → densities of PBHs constrained by micro-lensing observations (e.g. OGLE)
    - **primordial magnetic fields** (PMFs) → lower bounds on PMFs from X-ray observations (e.g. MAGIC or Fermi/LAT)



## GW: Bubble Collisions



## PBH production:

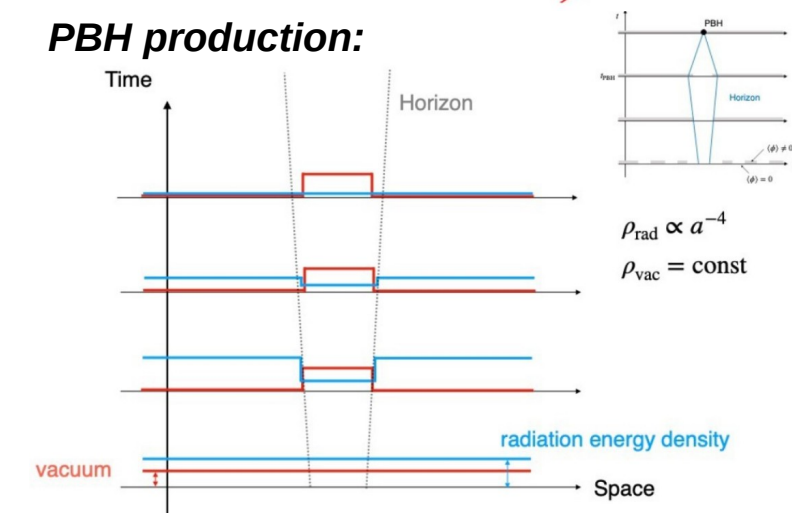
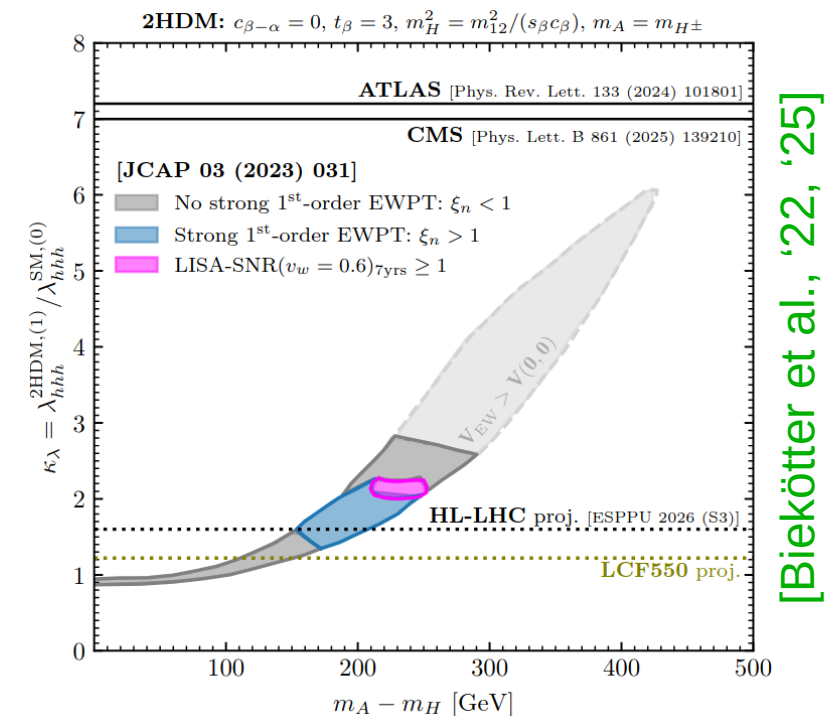


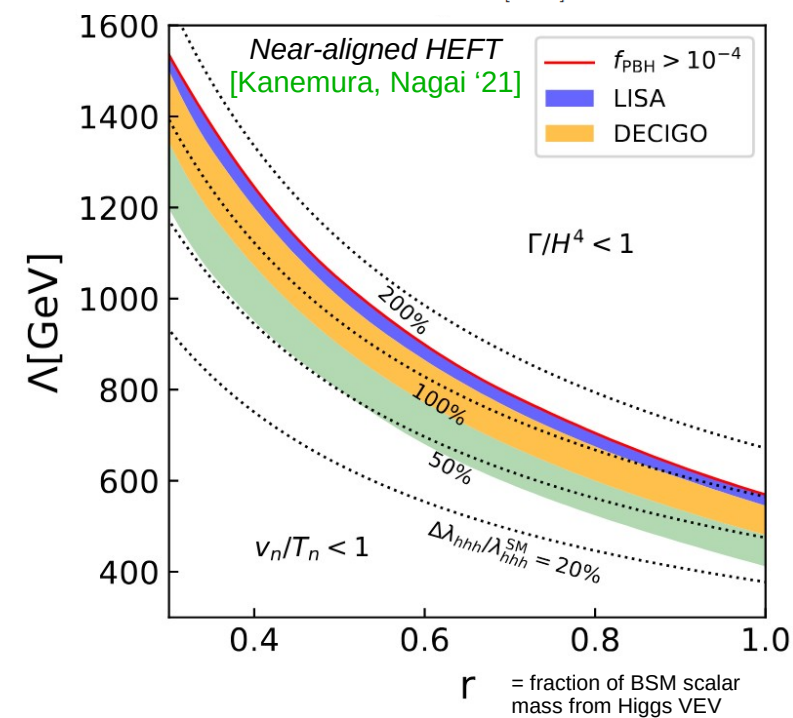
Figure from  
[Kanemura '23]

# Complementary probes of SFOEWPT

- **Probes of SFOEWPT:**
  - *reconstruct form of Higgs potential realised in Nature*
  - *search for **cosmological relics** of a strong first-order phase transition*
- Many examples, e.g. for
  - **models with extended scalar sectors** (singlet model variants, 2HDMs, classical scale invariant models, etc.) [Hashino et al., '16, '18, '19], [Huang, Long, Wang, '16], [Artymowski et al. '17], [Chala, Ramos, Spannowsky '18], [Alves et al. '19, '20], [Chen, Li, Wu, Bian '19], [Biekötter et al. '22]
  - **composite Higgs models** [Bruggisser et al., '18]
  - **EFTs** (SMEFT/HEFT/naHEFT) [Hashino et al. '22, '25]
  - **Warped extra-dimensions** [Ghoshal et al. '25]
- ... and many more
- See also review [Athron et al '23]



[Biekötter et al., '22, '25]



[Hashino et al., '22]

# Synergies between di-Higgs and gravitational waves in RxSM

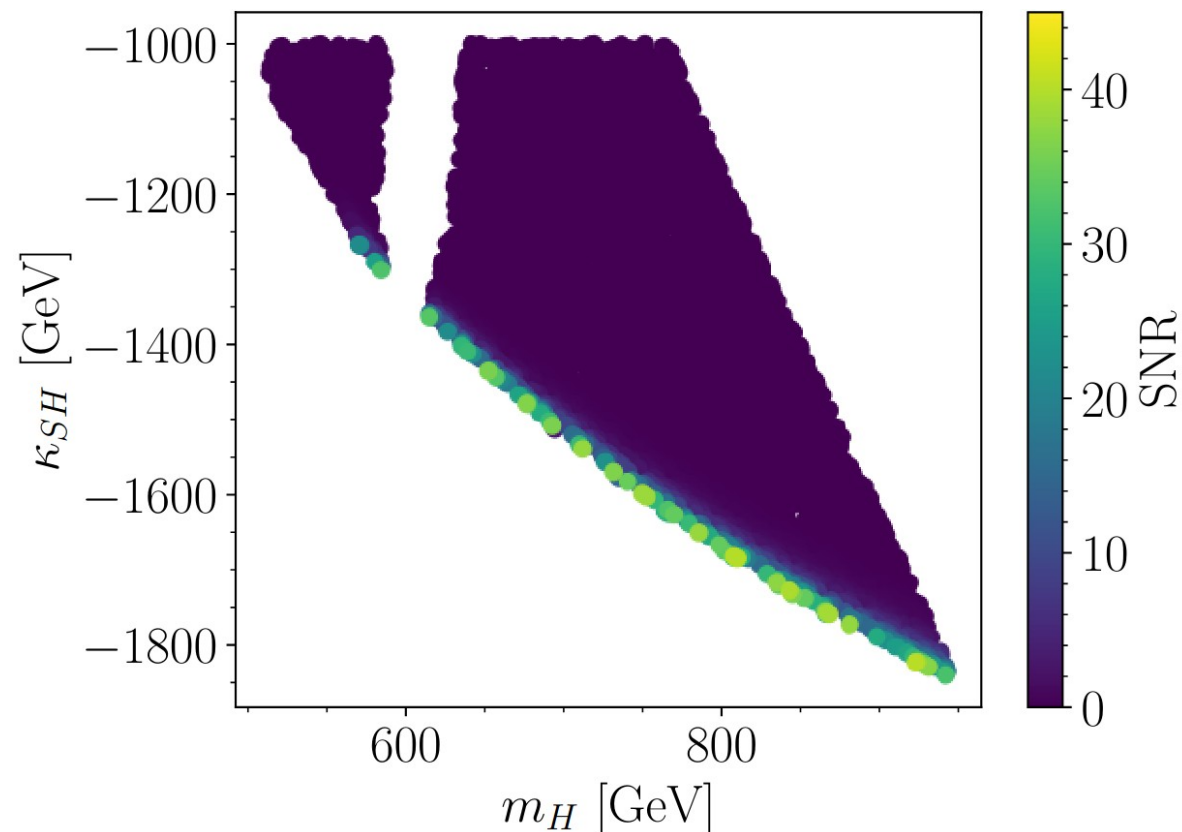
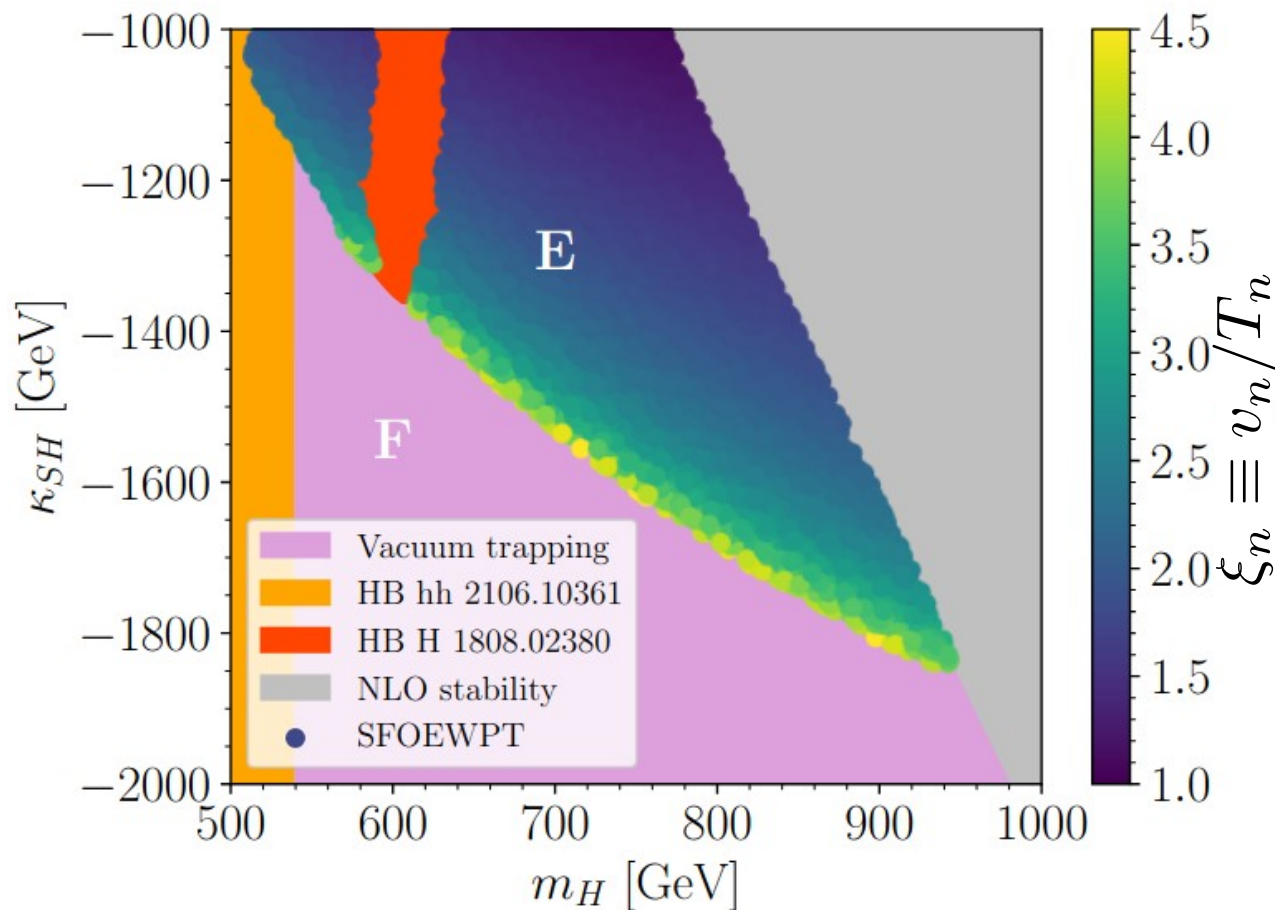
[JB, Heinemeyer, Pulido Boatella,  
Verduras Schaeidt *WIP*]

## Thermal histories in RxSM

Here: benchmark plane with:

$$c_\alpha = 0.98, \kappa_S = -300 \text{ GeV}, v_S = 280 \text{ GeV}$$

## Region E → SFOEWPT

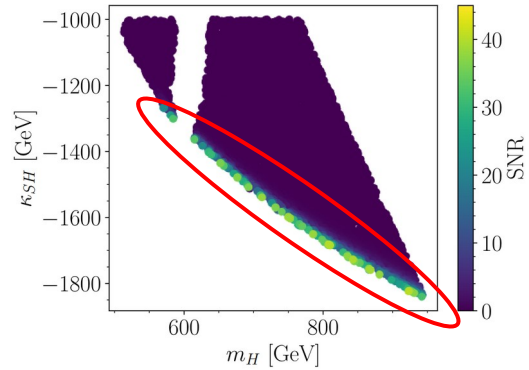


For a band in this plane, one finds a **stochastic background of gravitational waves (GW) detectable with LISA** (w. 3 yrs. data taking,  $v_w = 0.6$ )

→ *could we probe this region at (HL-)LHC?*

# Synergies between di-Higgs and gravitational waves in RxSM

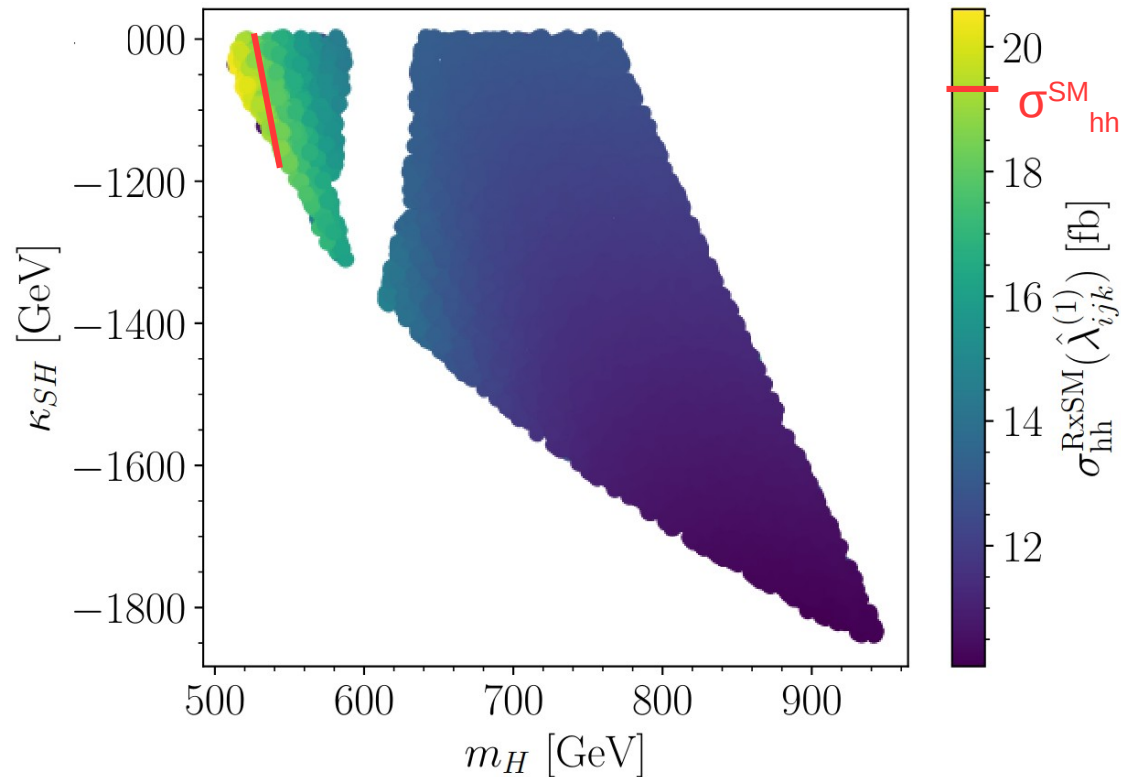
[JB, Heinemeyer, Pulido Boatella,  
Verduras Schaeidt *WIP*]



Region with observable GW signal at LISA:

- di-Higgs cross-section below SM prediction

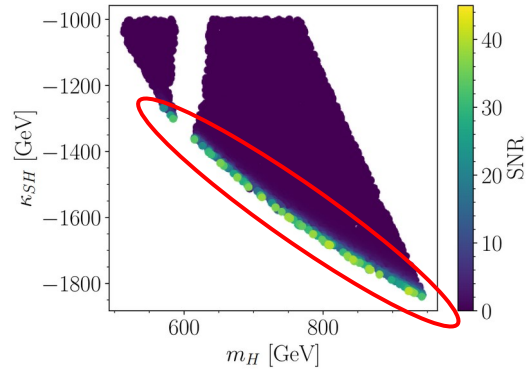
→ difficult to probe this region using total cross-section





# Synergies between di-Higgs and gravitational waves in RxSM

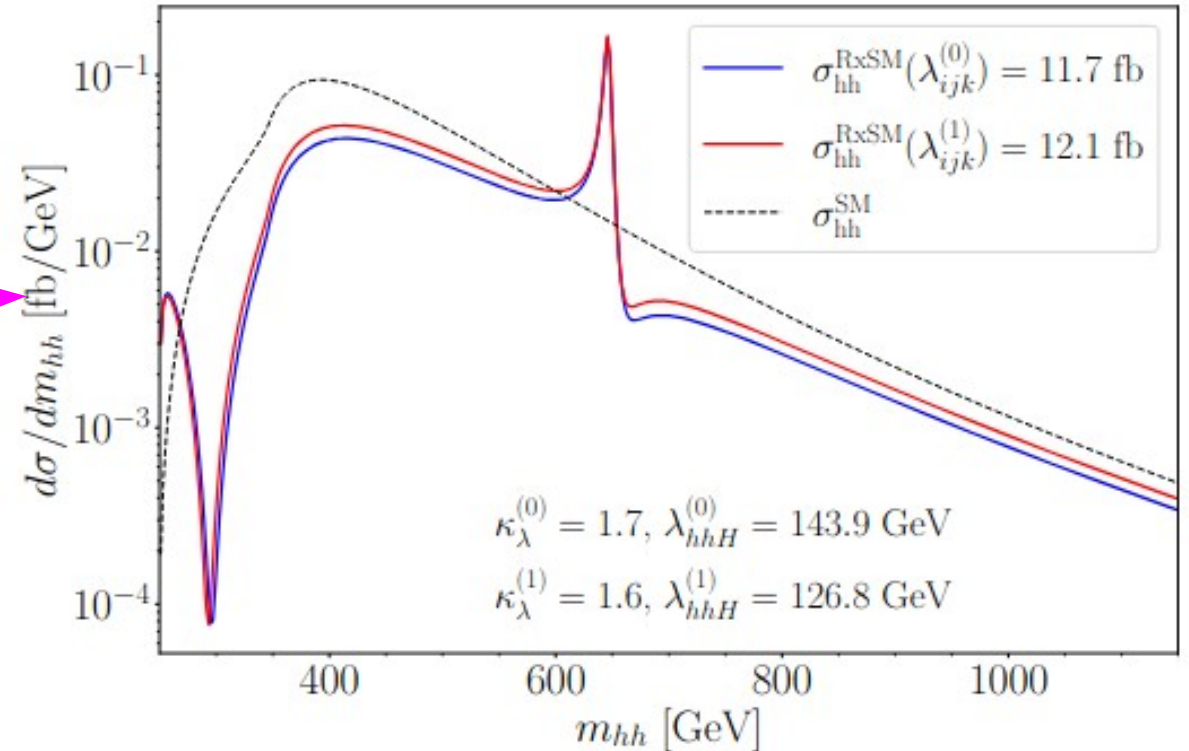
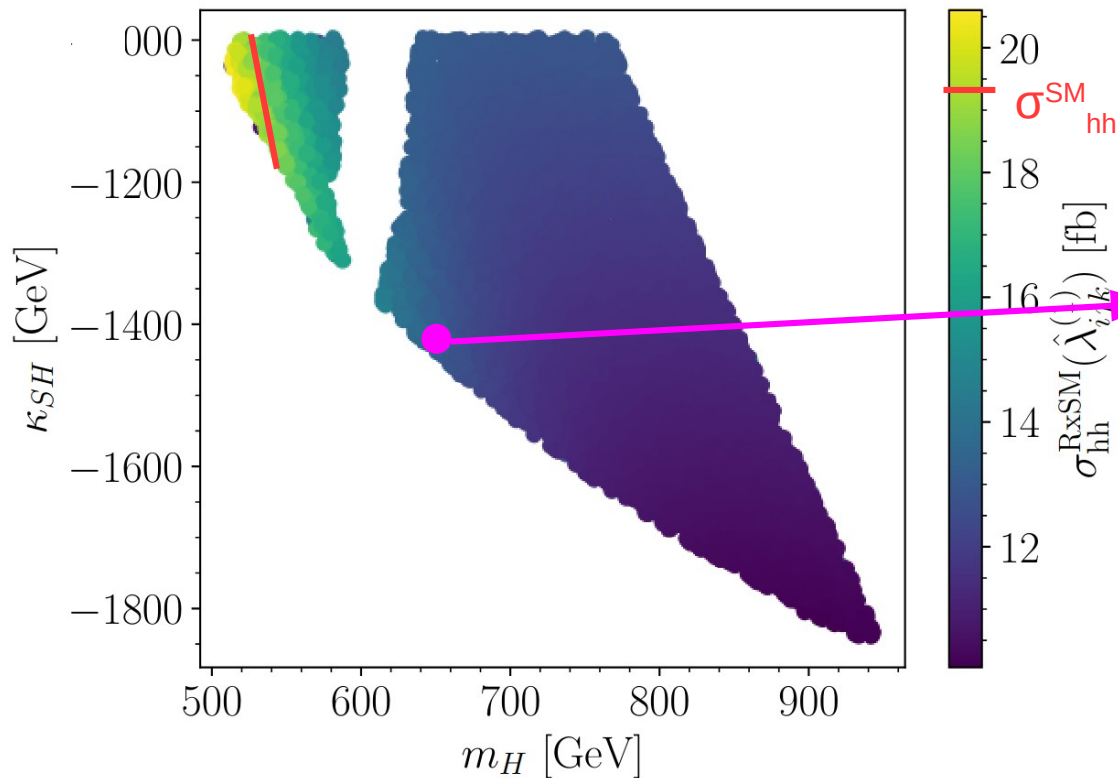
[JB, Heinemeyer, Pulido Boatella, Verduras Schaeidt *WIP*]



Region with observable GW signal at LISA:

- di-Higgs cross-section below SM prediction  
→ difficult to probe this region using total cross-section

... but  $m_{hh}$  distribution can be distinguished from SM!

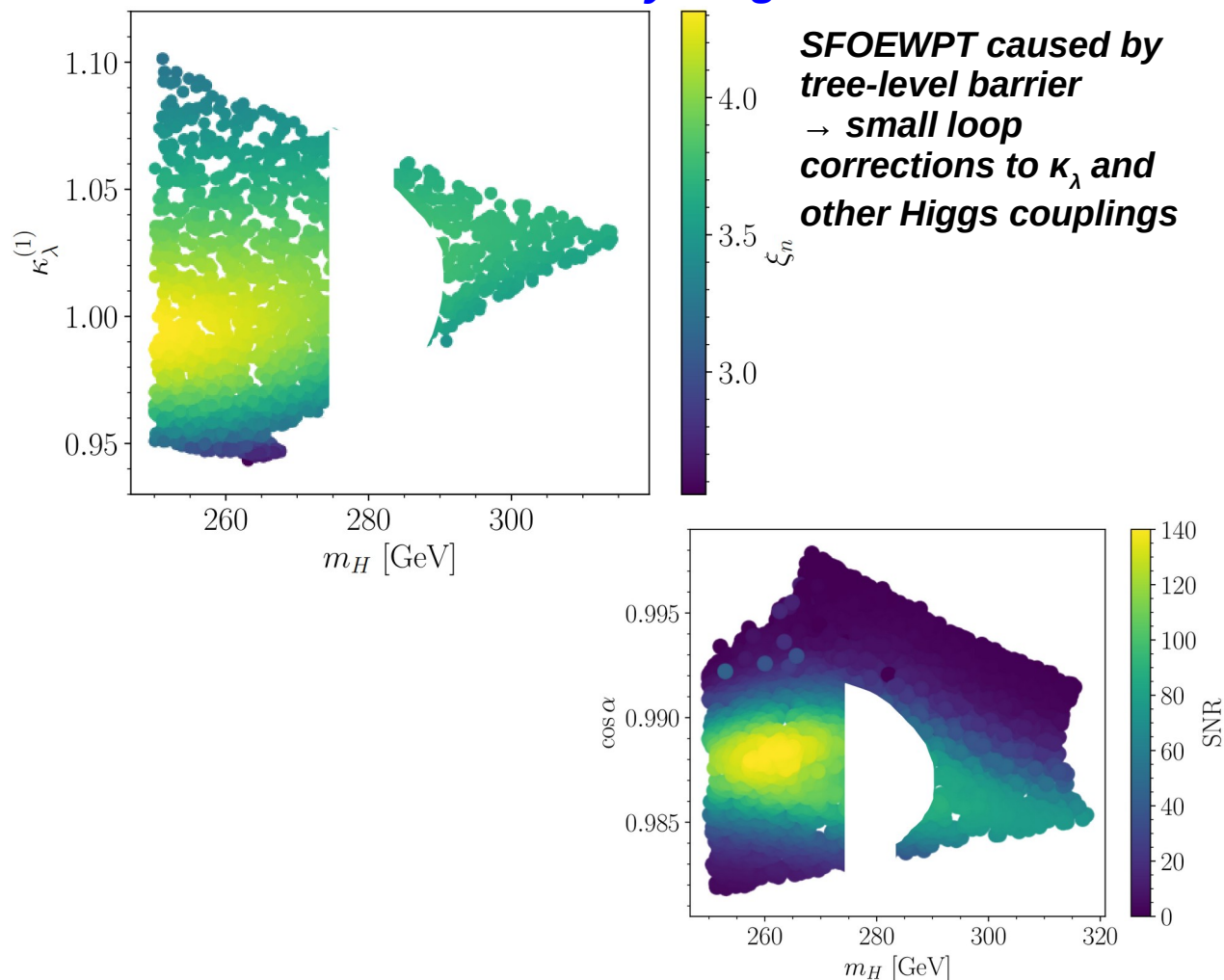


# Complementary probes of SFOEWPT in RxSM

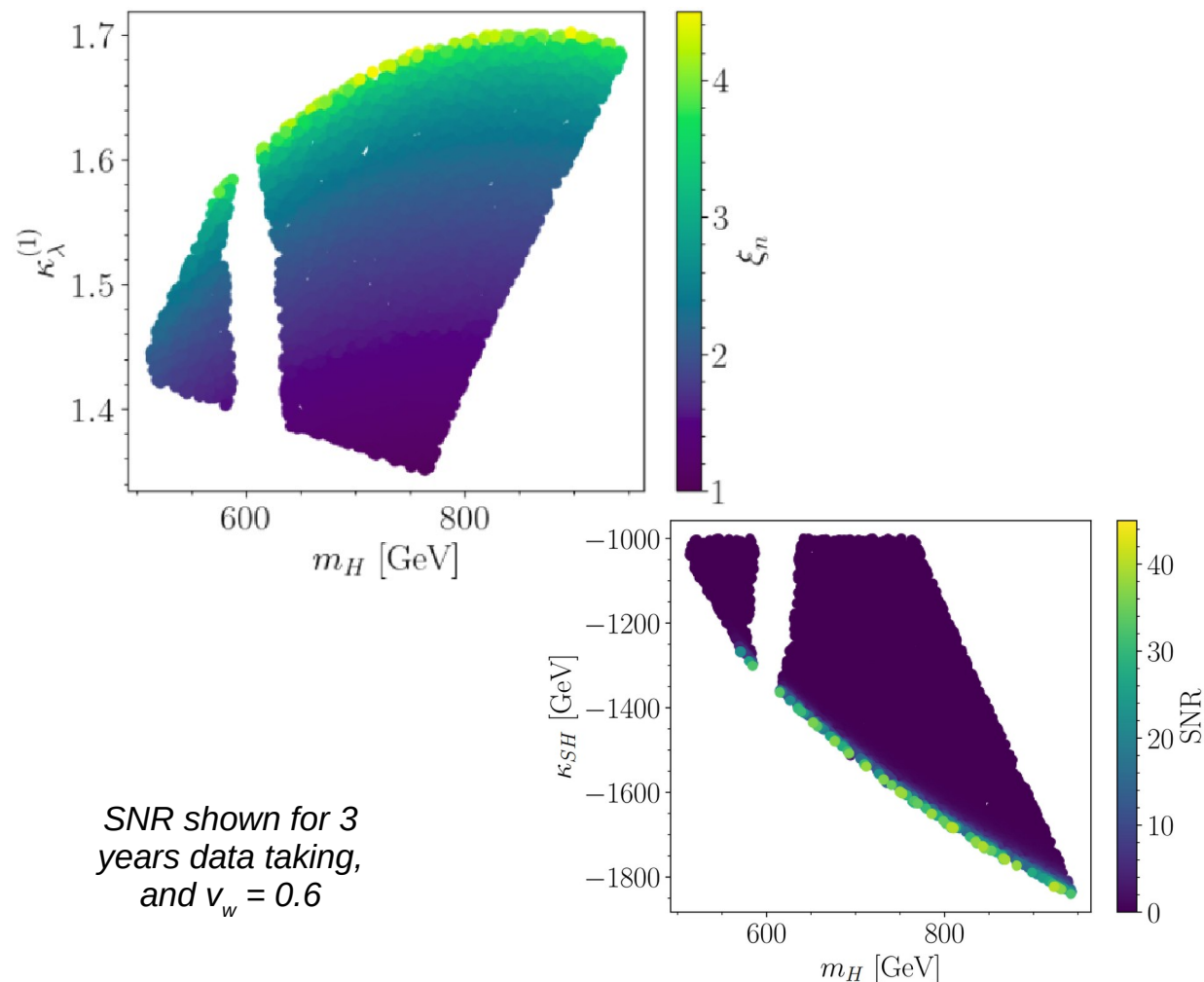
[JB, Heinemeyer, Pulido Boatella, Verduras Schaeidt *WIP*]

- No guarantee that SFOEWPT scenarios in RxSM can all be probed with  $gg \rightarrow hh$  or GW  
→ complementarity needed to cover as much as possible of the RxSM parameter space

## BP with SFOEWPT driven by singlet field



## BP for SFOEWPT driven by doublet field



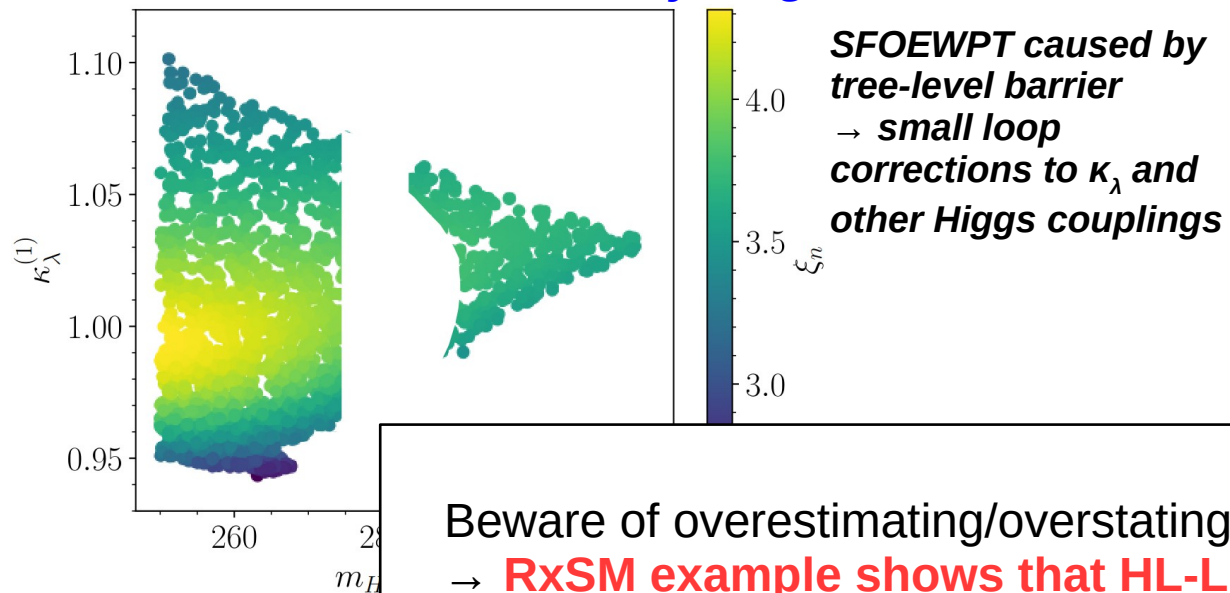
*SNR shown for 3 years data taking, and  $v_w = 0.6$*

# Complementary probes of SFOEWPT in RxSM

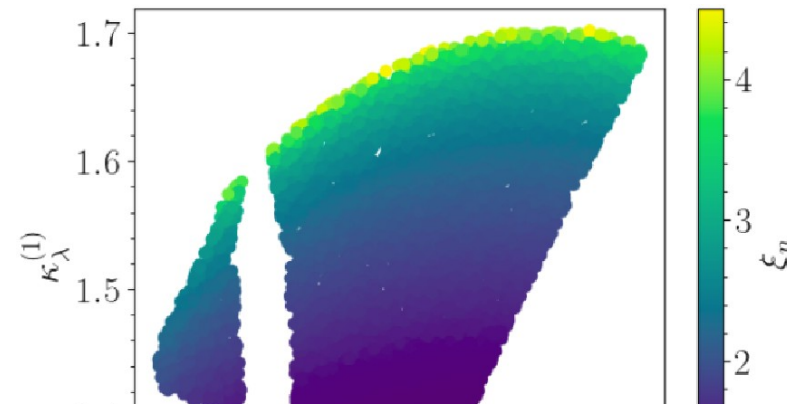
[JB, Heinemeyer, Pulido Boatella, Verduras Schaeidt WIP]

- No guarantee that SFOEWPT scenarios in RxSM can all be probed with  $gg \rightarrow hh$  or GW  
→ complementarity needed to cover as much as possible of the RxSM parameter space

## BP with SFOEWPT driven by singlet field

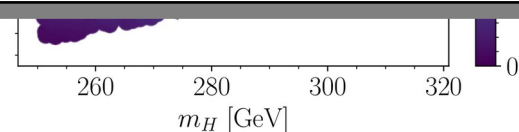


## BP for SFOEWPT driven by doublet field

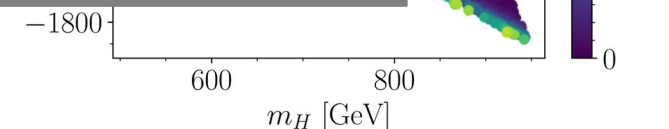


Beware of overestimating/overstating reach of single measurement/single process  
→ RxSM example shows that HL-LHC will not be able to completely exclude the possibility of a SFOEWPT

Note: EFT treatments cannot be applied if EWPT occurs (partly) along BSM field direction(s) that is(are) integrated out



years data taking,  
and  $v_w = 0.6$



# Summary

- 85% of (HL-)LHC data remains to be taken → **plenty of room left for BSM discoveries!**
- **Significant progress to come in direct searches**, thanks to ingenuity in terms of new search strategies, analysis techniques, etc.
- Some tentatizing excesses
  - more data from Run 3 and beyond might clarify this
  - **it suffices that one of them materialises to have a BSM discovery!**
- **Precision measurements of properties of Higgs boson** (or of other known particles) have strong potential to probe or constrain BSM
  - **high precision theory predictions (QCD/EW/BSM) are needed**
  - combined/global analyses
- Intense theory efforts to prepare for di-Higgs production searches, one of the flagship measurements at HL-LHC
  - **BSM higher-order effects could be very significant**

# Thank you very much for your attention!

## Contact

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Elektronen-Synchrotron

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[johannes.braathen@desy.de](mailto:johannes.braathen@desy.de)

# Backup slides



# RxSM

# The RxSM

## General singlet extension of the SM (no $Z_2$ symmetry)

### ➤ Potential

$$V(\Phi, S) = \mu^2(\Phi^\dagger\Phi) + \frac{\lambda}{2}(\Phi^\dagger\Phi)^2 + \kappa_{SH}(\Phi^\dagger\Phi)S + \frac{\lambda_{SH}}{2}(\Phi^\dagger\Phi)S^2 + \frac{M_S^2}{2}S^2 + \frac{\kappa_S}{3}S^3 + \frac{\lambda_S}{2}S^4.$$

➤ Field content (after EWSB)

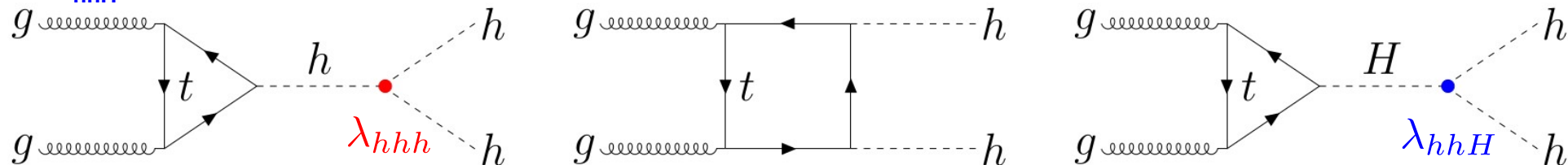
$$\Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}G^+ \\ v + \phi + iG^0 \end{pmatrix}, \quad S = s + v_S$$

➤ Mixing among 2 CP-even Higgs bosons: Gauge basis:  $\phi, s \xrightarrow{\text{mixing angle } \alpha}$  Mass basis:  $h, H$

➤ RxSM scalar sector parametrised in terms of  $\underbrace{m_h^2, v}_{\text{known}}, \underbrace{m_H^2, \alpha, v_S, \kappa_S, \kappa_{SH}}_{\text{free}}$

➤ Three leading diagrams in di-Higgs production, with significant dependence on 2 relevant trilinears:

$\lambda_{hhh}$  and  $\lambda_{hhH}$



# Full on-shell renormalisation of the RxSM

[JB, Heinemeyer, Parra Arnay,  
Verduras Schaeidt *WIP*]

- Masses:  $m_h^2, m_H^2$

Renormalization of two-point functions

- EW VEV:  $v$

SM-like electroweak sector

- Singlet VEV:  $v_S$

No divergences

- Mixing angle:  $\alpha$

Rotation matrix: [Kanemura, Kikuchi, Yagyu, '15]

- Tadpoles:  $t_\phi, t_s$

OS/Standard scheme

- Kappas:  $\kappa_S, \kappa_{SH}$

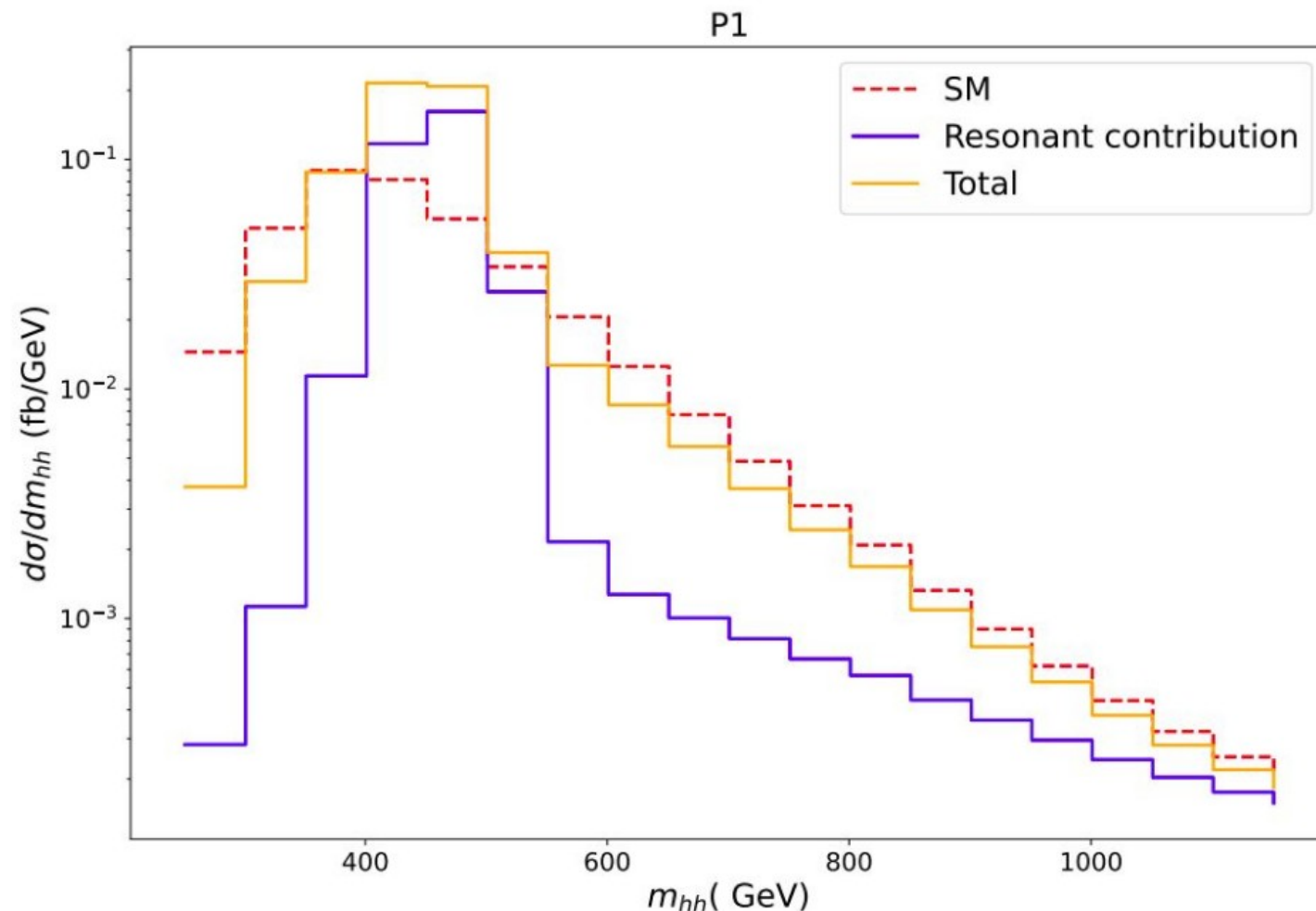
$$\hat{\lambda}_{hHH}^{(1)} \stackrel{!}{=} \lambda_{hHH}^{(0)} \quad \hat{\lambda}_{HHH}^{(1)} \stackrel{!}{=} \lambda_{HHH}^{(0)}$$

*Slide by A. Verduras Schaeidt*

# Interference effects in the RxSM

Di-Higgs production differential distributions: total result vs resonant only

[Arco, Heinemeyer, Mühlleitner,  
Parra Aray, Rivero Gonzalez,  
Verduras Schaeidt '25]



## Benchmark P1

$$m_H = 459 \text{ GeV}$$

$$\alpha = 0.984$$

$$v_S = 46 \text{ GeV}$$

$$\kappa_\lambda = 1.47$$

$$\lambda_{hhH} = 177 \text{ GeV}$$

$$\sigma_{hh}^{\text{RxSM, tot}} = 31.1 \text{ fb}$$

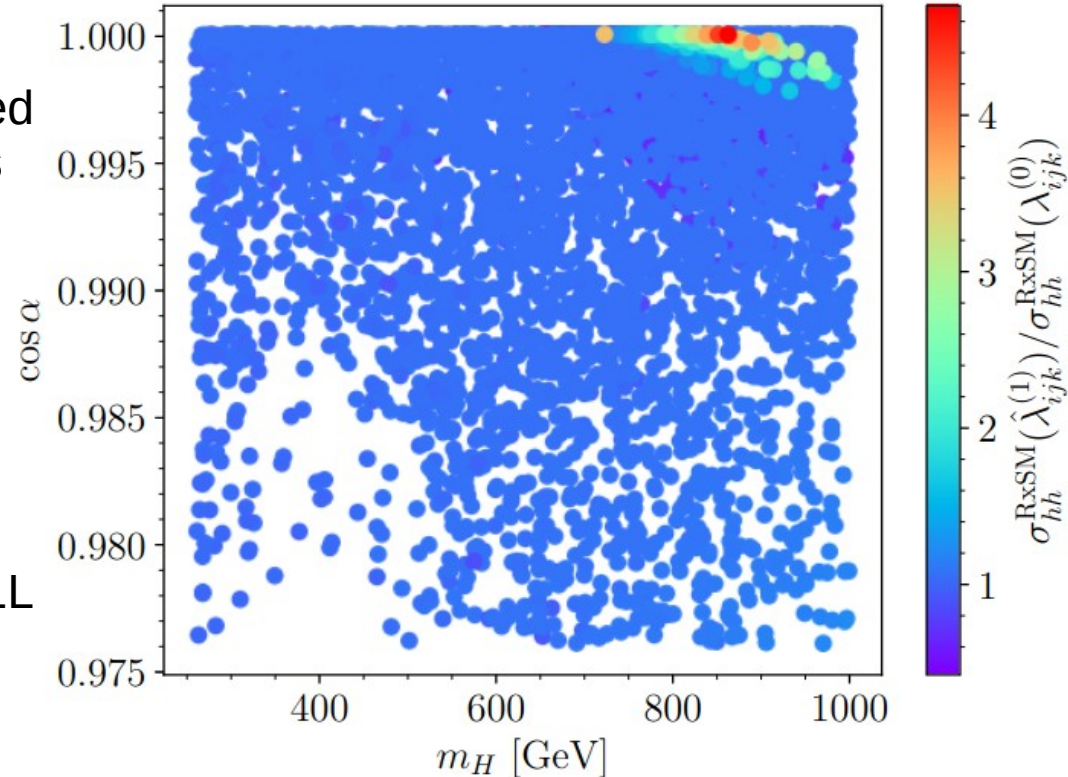
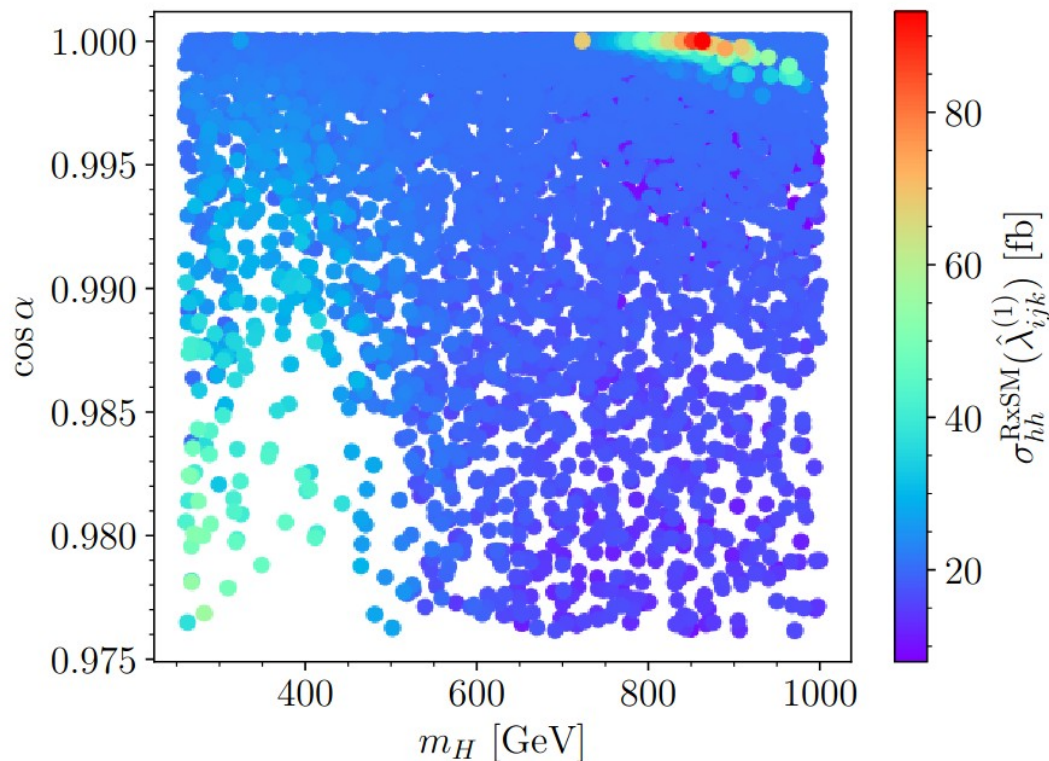
$$\sigma_{hh}^{\text{RxSM, res}} = 16.3 \text{ fb}$$

- Distributions shown here after **experimental effects** are taken into account (**15% smearing and 50 GeV binning**)
- **Relatively good agreement between peak of resonant and total distributions, but tails are far apart**

# Impact of NLO corrections in the RxSM

[JB, Heinemeyer, Parra Aray, Verduras Schaeidt '25]

## Parameter scans



- Largest increases in  $\sigma_{hh}^{\text{RxSM}}$  w.r.t. SM for  $m_H > 750$  GeV,  $v_S < 50$  GeV and small mixing → **loop induced effects**
- Points with smaller increases in  $\sigma_{hh}^{\text{RxSM}}$  (up to  $\sim 2.5 \sigma_{hh}^{\text{SM}}$ ) for low  $m_H$  → **effect from resonant H contribution (already at tree level)**

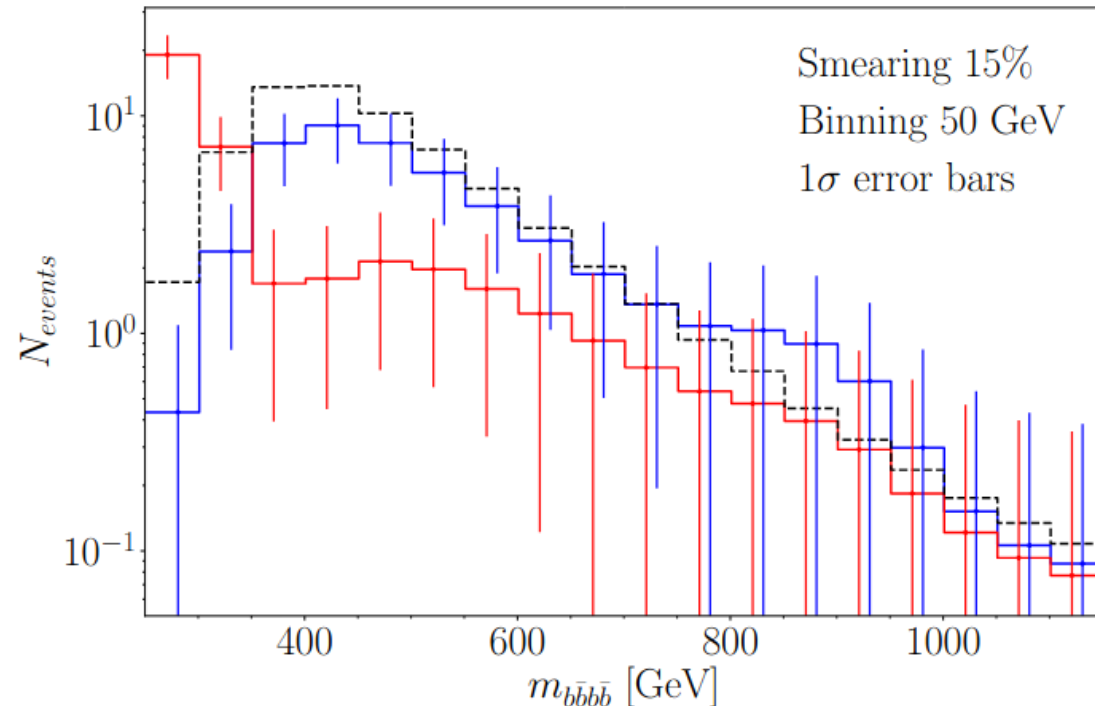
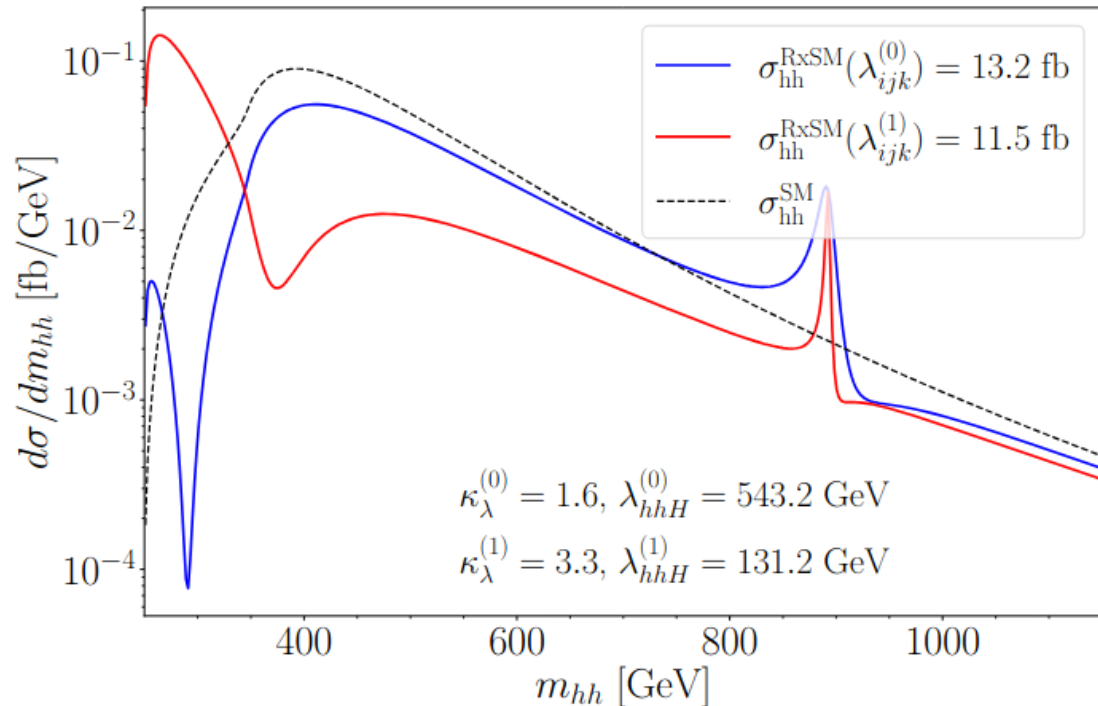


# Impact of NLO corrections in the RxSM

[JB, Heinemeyer, Parra Aray,  
Verduras Schaeidt '25]

## Impact on di-Higgs invariant mass distributions

BP4:  $m_H = 891.1$  GeV,  $\cos \alpha = 0.99$ ,  $v_S = 37.0$  GeV,  $\kappa_S = -993$  GeV,  $\kappa_{SH} = -933$  GeV,  $Z^{(0)} = 3.5$ ,  $Z^{(1)} = 10.5$



- Total cross-section is not modified very significantly
- Large (positive) correction to  $\lambda_{hhh}$  changes the distribution drastically for low  $m_{hh}$ , while large negative correction to  $\lambda_{hhH}$  makes the peak at  $m_H$  narrower
- Change at low  $m_{hh}$  is substantial enough to allow distinguishing the RxSM from the SM with an analysis using one-loop trilinear scalar couplings

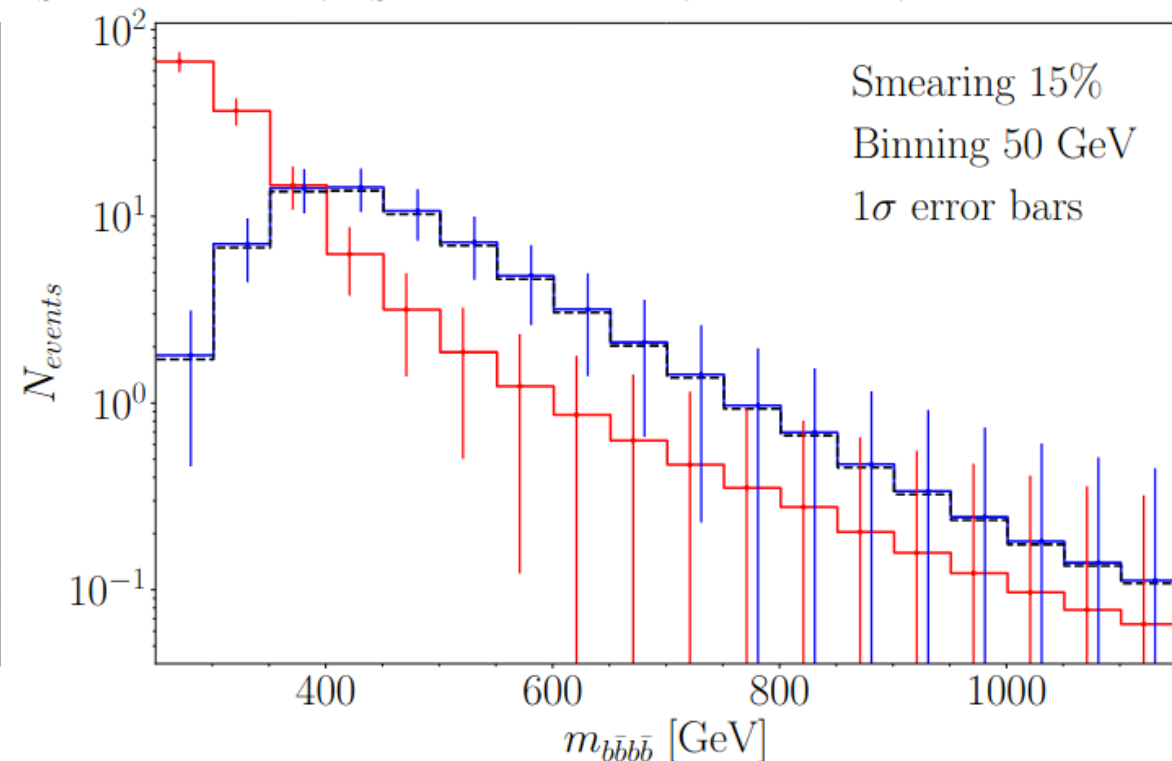
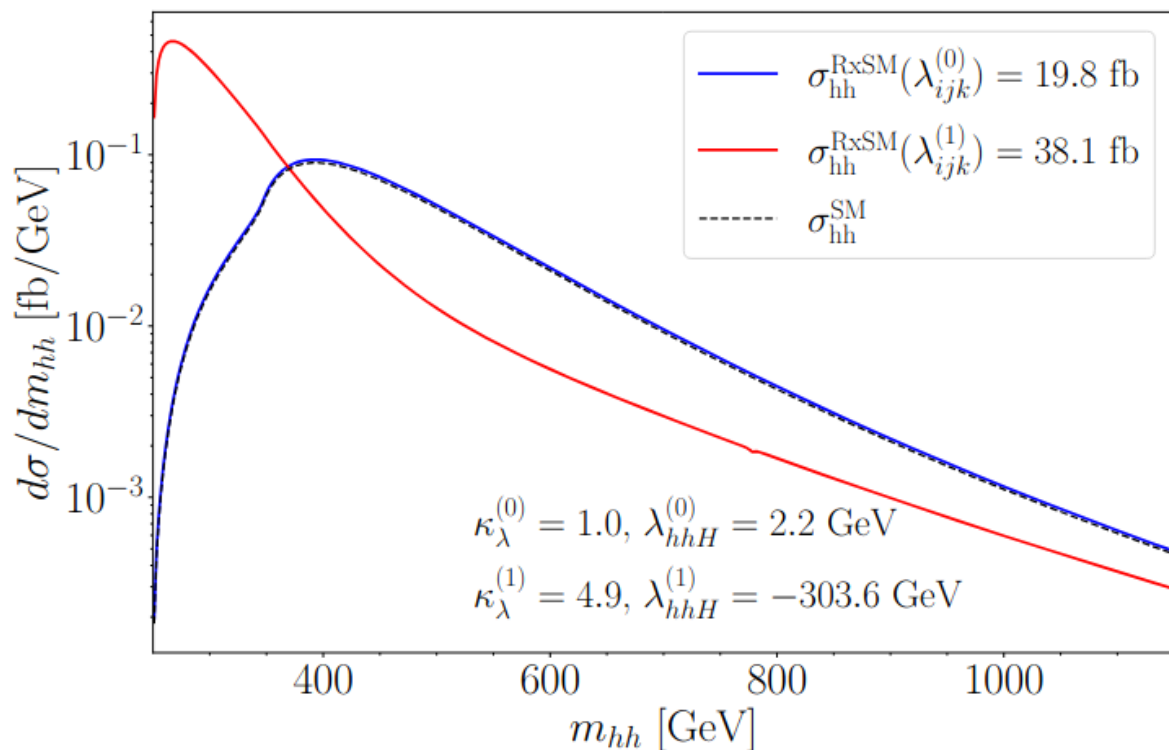


# Impact of NLO corrections in the RxSM

[JB, Heinemeyer, Parra Aray,  
Verduras Schaeidt *WIP*]

## Impact on di-Higgs invariant mass distributions

BP2:  $m_H = 777.6$  GeV,  $\cos \alpha = 1.0$ ,  $v_S = 44.7$  GeV,  $\kappa_S = -931$  GeV,  $\kappa_{SH} = -931$  GeV,  $Z^{(0)} = 0.3$ ,  $Z^{(1)} = 21.3$



- Similar to BP1, main effect from loop correction to  $\kappa_\lambda$  (resonant peak suppressed by high  $m_H$ )
- As for BP1, for BP2, an analysis with tree-level trilinears ( $Z^{(0)}=0.3$ ) would not be able to show a deviation from the SM, but an analysis with one-loop ones would ( $Z^{(1)}=21.3$ )

# 2HDM

# The Two-Higgs-Doublet Model

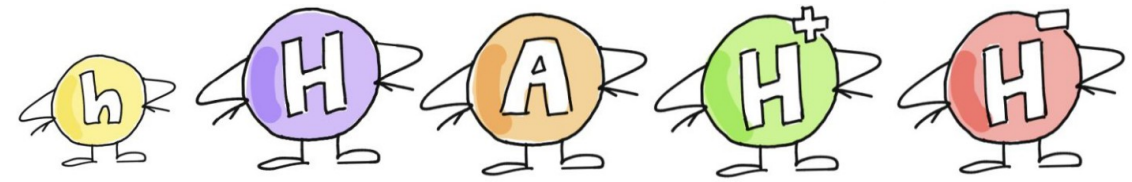


Figure by [K. Radchenko Serdula '24]

- 2  $SU(2)_L$  doublets  $\Phi_{1,2}$  of hypercharge  $1/2$
- CP-conserving 2HDM, with softly-broken  $Z_2$  symmetry ( $\Phi_1 \rightarrow \Phi_1$ ,  $\Phi_2 \rightarrow -\Phi_2$ ) to avoid tree-level FCNCs

$$V_{2\text{HDM}}^{(0)} = m_1^2 |\Phi_1|^2 + m_2^2 |\Phi_2|^2 - m_3^2 (\Phi_2^\dagger \Phi_1 + \Phi_1^\dagger \Phi_2) \\ + \frac{\lambda_1}{2} |\Phi_1|^4 + \frac{\lambda_2}{2} |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_2^\dagger \Phi_1|^2 + \frac{\lambda_5}{2} \left( (\Phi_2^\dagger \Phi_1)^2 + \text{h.c.} \right) \\ v_1^2 + v_2^2 = v^2 = (246 \text{ GeV})^2$$

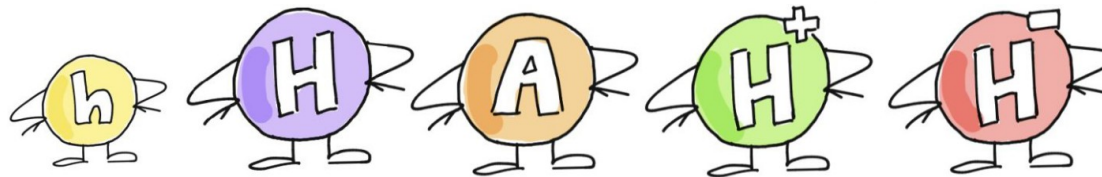
- **Mass eigenstates:**  
 $h, H$ : CP-even Higgs bosons ( $h \rightarrow 125\text{-GeV SM-like state}$ );  $A$ : CP-odd Higgs boson;  
 $H^\pm$ : charged Higgs boson
- **BSM parameters:** 3 BSM masses  $m_H, m_A, m_{H^\pm}$ , BSM mass scale  $M$  (defined by  $M^2 \equiv 2m_3^2/s_{2\beta}$ ), angles  $\alpha$  (CP-even Higgs mixing angle) and  $\beta$  (defined by  $\tan\beta = v_2/v_1$ )
- **BSM-scalar masses** take form  $m_\Phi^2 = M^2 + \tilde{\lambda}_\Phi v^2$ ,  $\Phi \in \{H, A, H^\pm\}$
- We take the **alignment limit**  $\alpha = \beta - \pi/2 \rightarrow$  all Higgs couplings are SM-like at tree level  
 $\rightarrow$  compatible with current experimental data

# Interference effects in the 2HDM

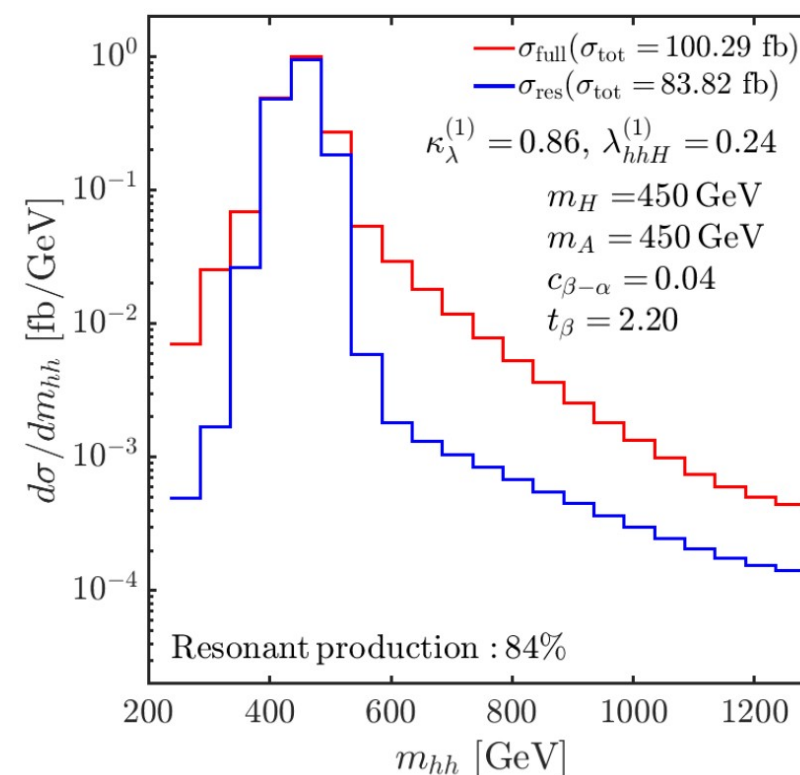
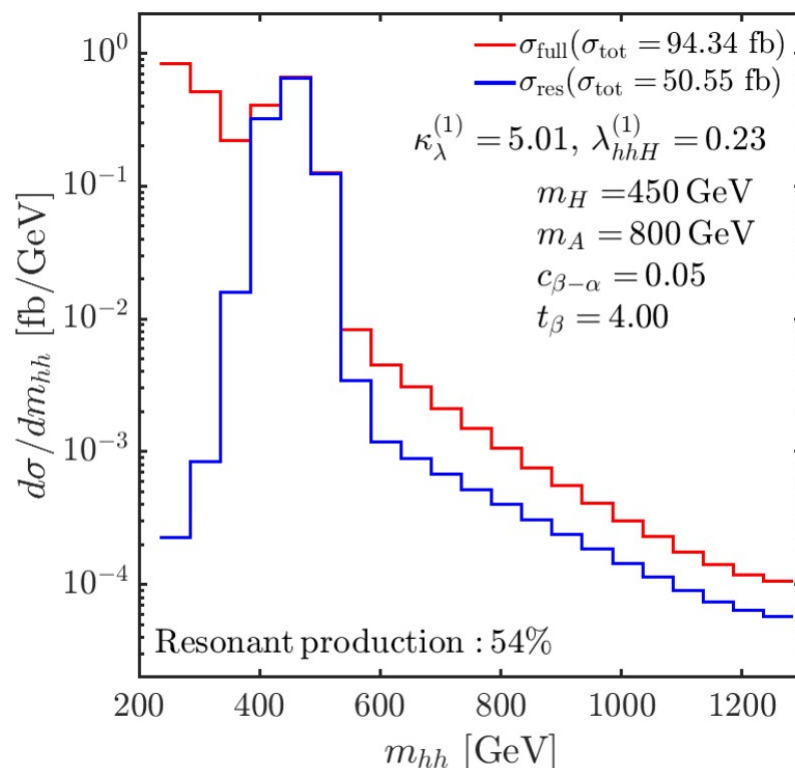
[Heinemeyer, Mühlleitner,  
Radchenko Serdula, Weiglein '24]

## Resonant only vs total distributions

- 2HDM adds second doublet to SM
- Interference between non-resonant and resonant contributions as well as loop corrections to trilinear scalar couplings can again drastically change di-Higgs invariant mass distributions
- 2 benchmark scenarios *excluded by resonant searches but allowed by non-resonant searches* [ATLAS '22]  
→ large impact of interference effects **warrants analysis of these scenarios with full calculation**



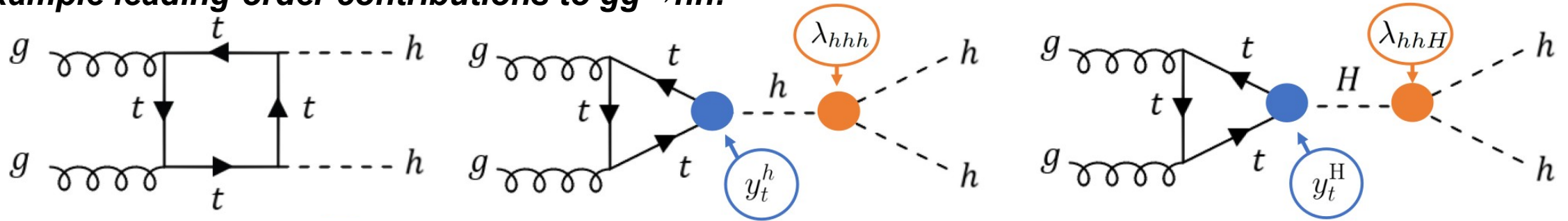
Drawing by  
[K. Radchenko  
Serdula '24]



anyH3 (v2) / anyHH

# Ongoing developments in anyBSM: anyLambdaijk and anyHH

**Example leading-order contributions to  $gg \rightarrow hh$ :**

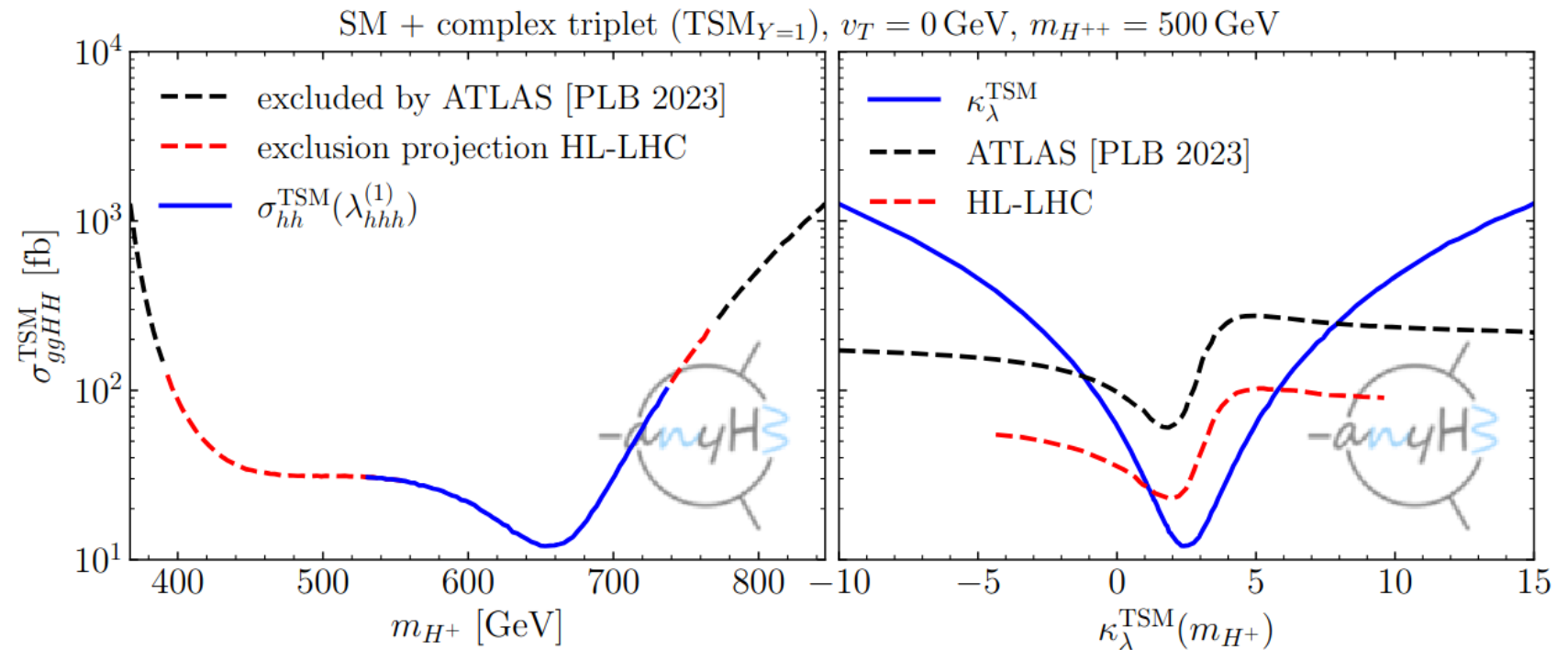


[Diagrams by A. Verduras Schaeidt]

Having predictions for di-Higgs production, including **all (i.e. resonant + non-resonant) contributions + 1L corrections to trilinear scalar couplings in arbitrary models** would be highly desirable

→ new modules anyLambdaijk and anyHH

[Bahl, Braathen, Gabelmann, Radchenko Serdula, GW WIP]

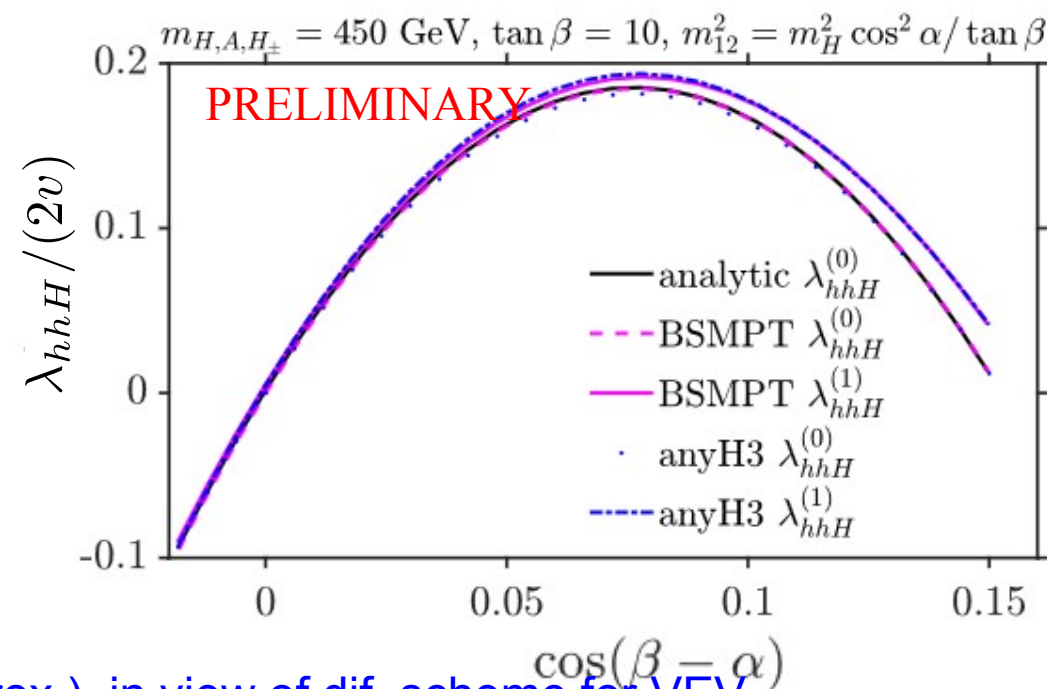
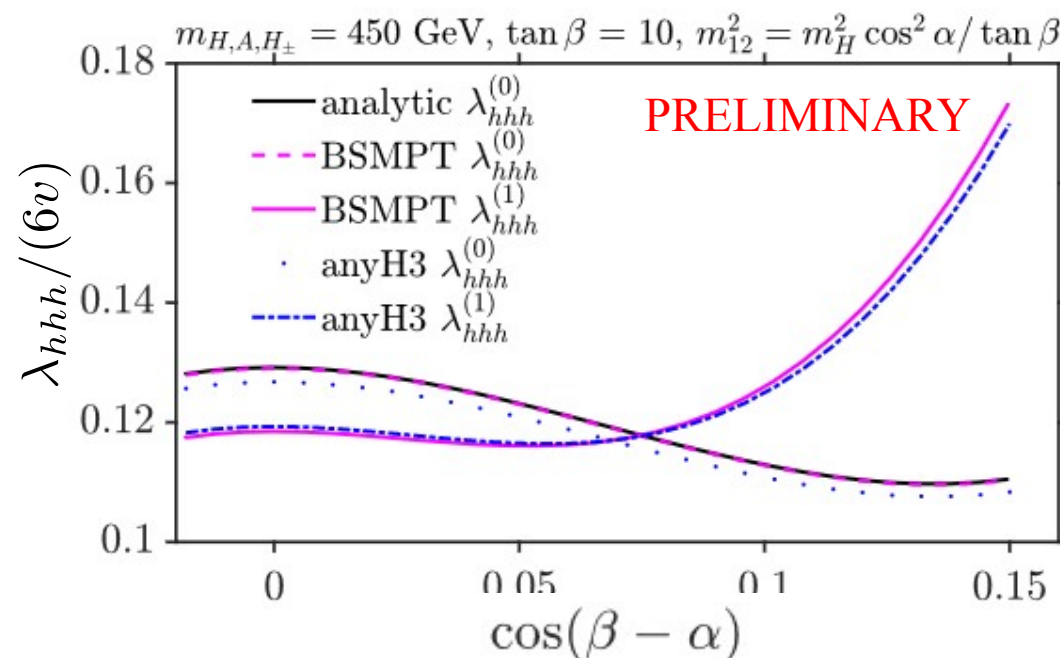
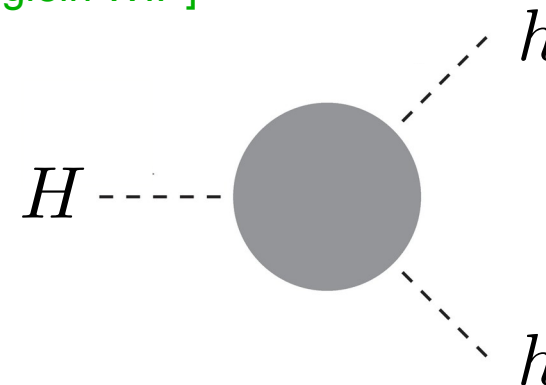
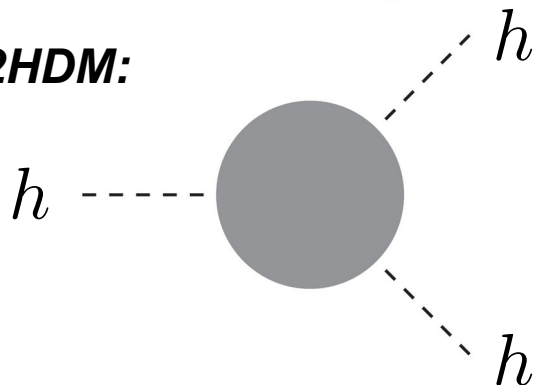




# Ongoing developments: anyLamijk

[Bahl, JB, Gabelmann, Radchenko  
Serdula, Weiglein *WIP*]

Example in a 2HDM:

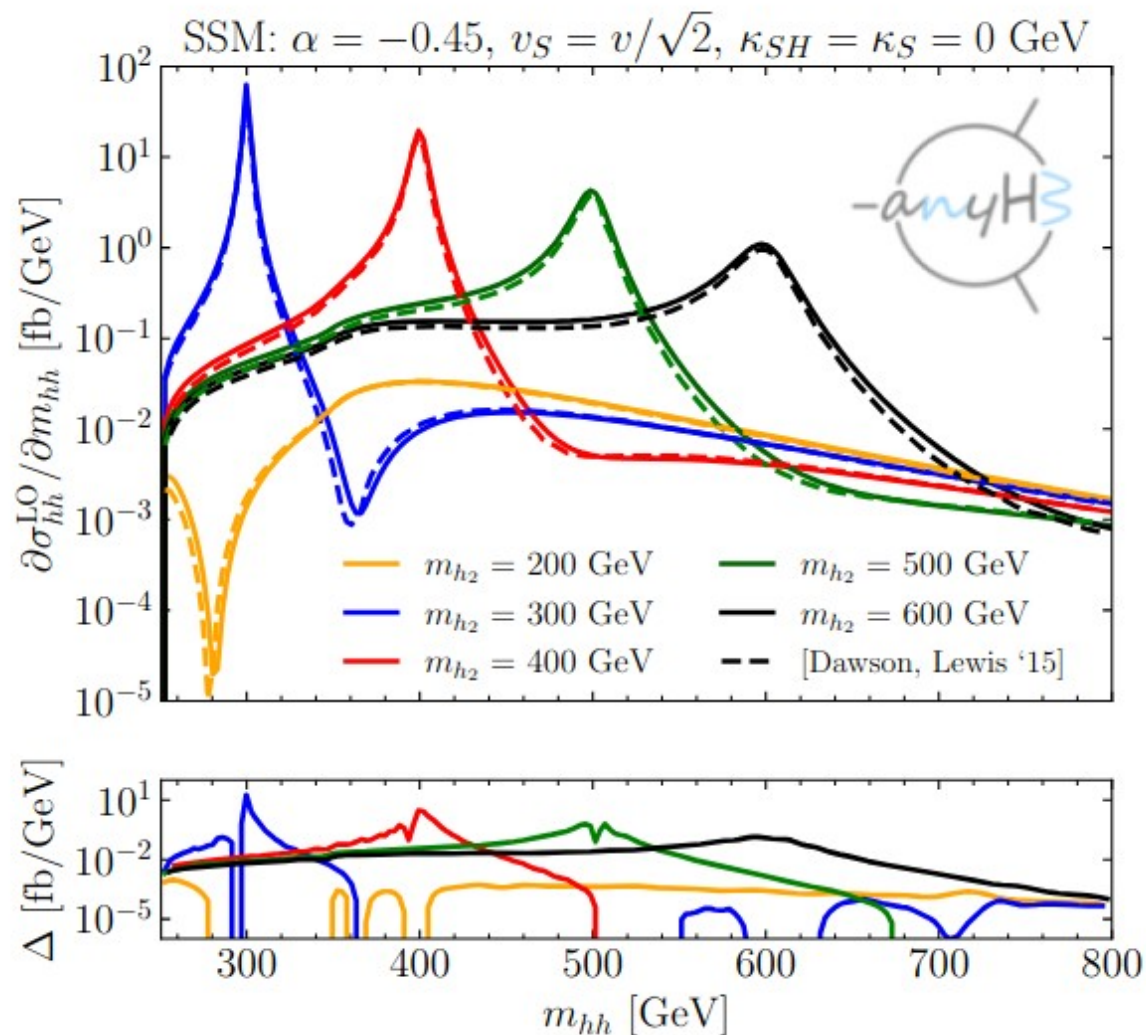
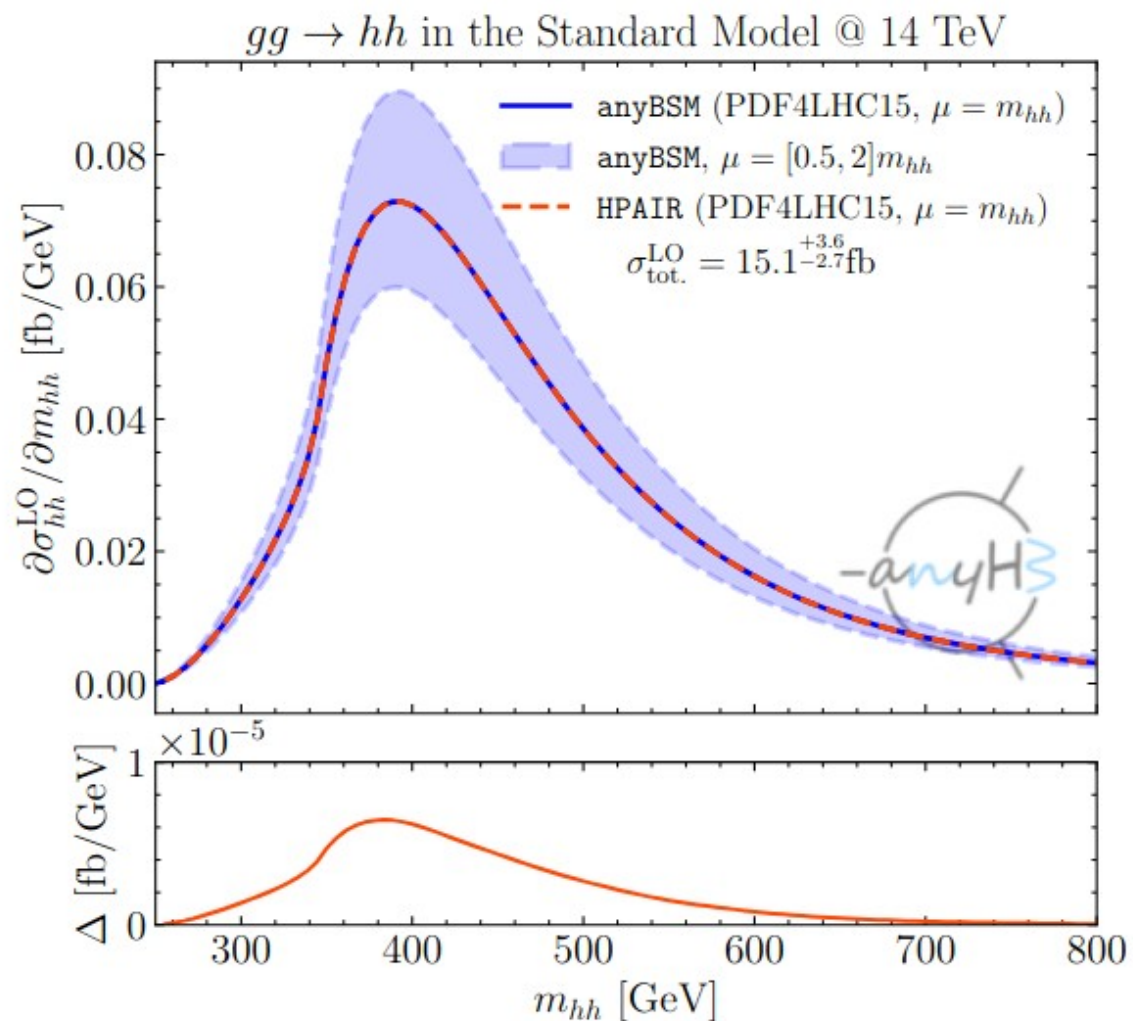


→ excellent agreement with BSMPT results (in eff. pot. approx.), in view of dif. scheme for VEV

→ full OS schemes for  $\lambda_{hhh}$  and  $\lambda_{hhH}$  couplings worked out in 2HDM [Bahl, JB, Gabelmann, Radchenko Serdula, Weiglein], RxSM [JB, Heinemeyer, Verduras Schaeidt], and more [Bosse, JB, Gabelmann, Hannig, Weiglein]!

# Ongoing developments: tests of anyHH with leading order trilinear couplings

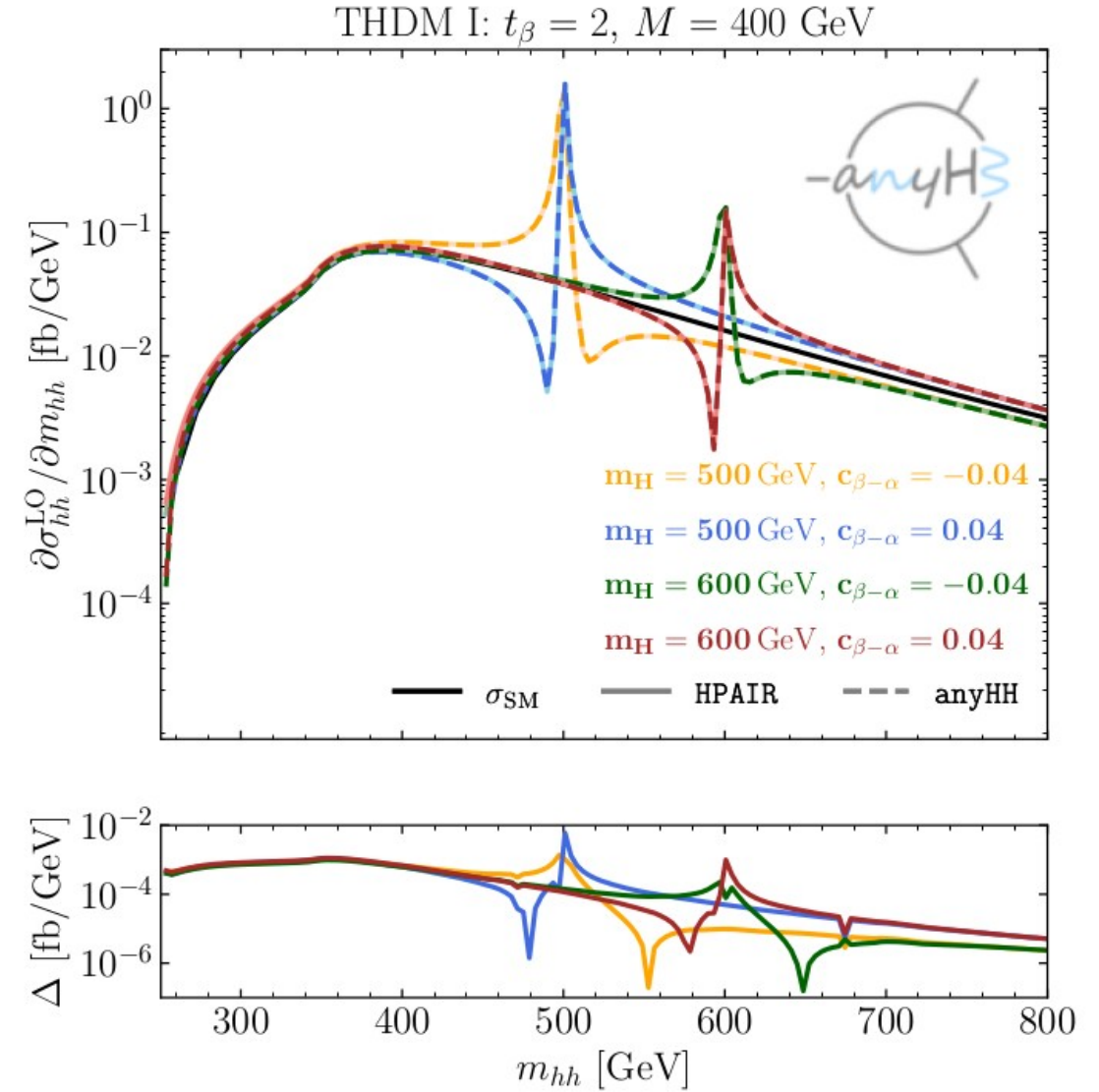
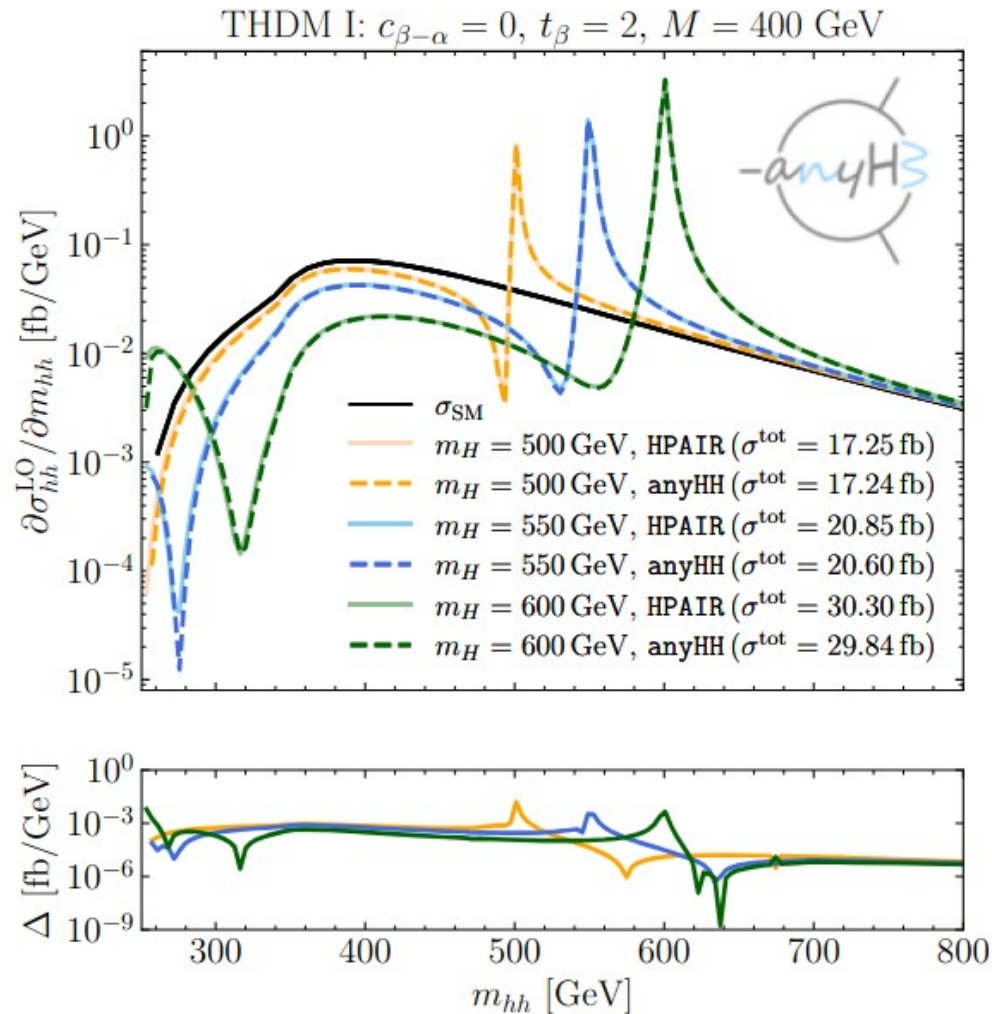
$$\Delta \equiv |\partial\sigma_{hh}^{\text{LO}}/\partial m_{hh}(\text{HPAIR}) - \partial\sigma_{hh}^{\text{LO}}/\partial m_{hh}(\text{anyHH})|$$



- Excellent agreement with LO HPAIR result, once one ensures that running of  $\alpha_s$  + choice of PDFs are same

- Very good agreement results of [Dawson, Lewis '15] for singlet extension of SM (remaining difference because PDF sets can't be taken to be the same)

# Ongoing developments: comparisons with HPAIR in the 2HDM

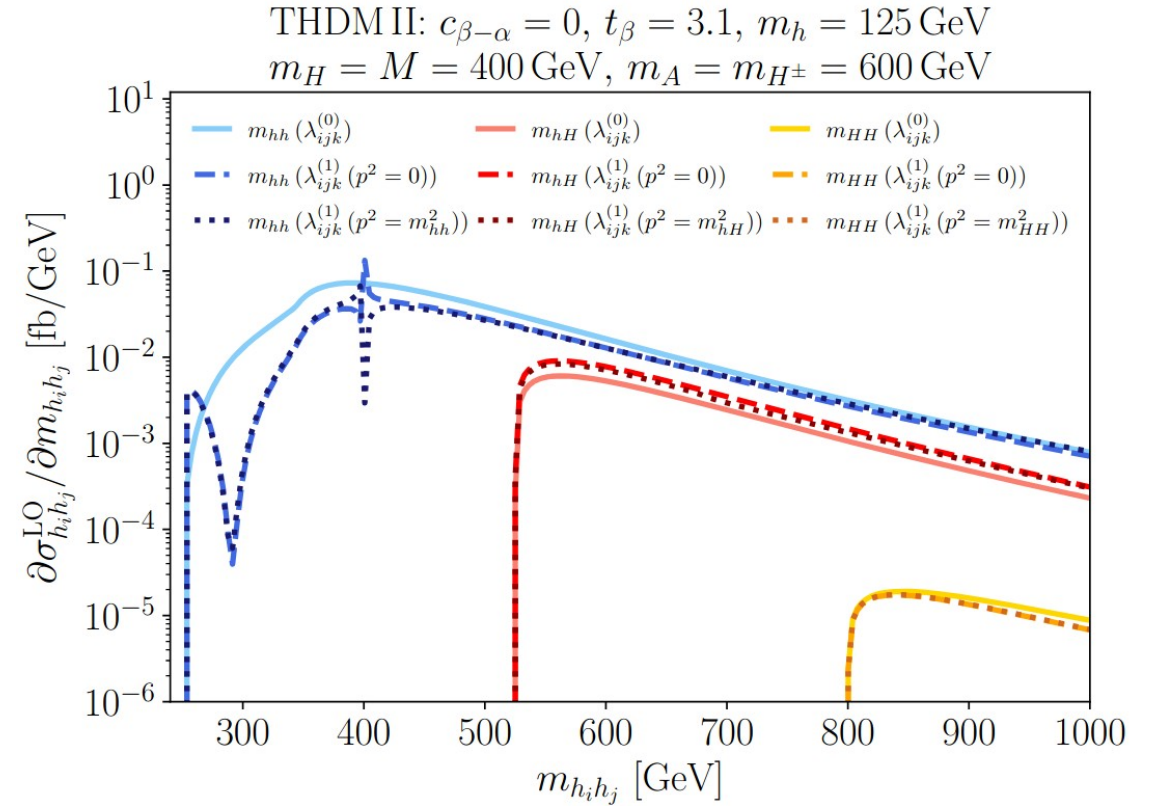
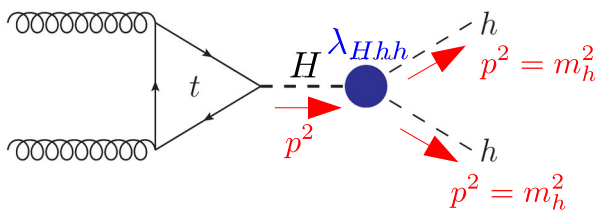
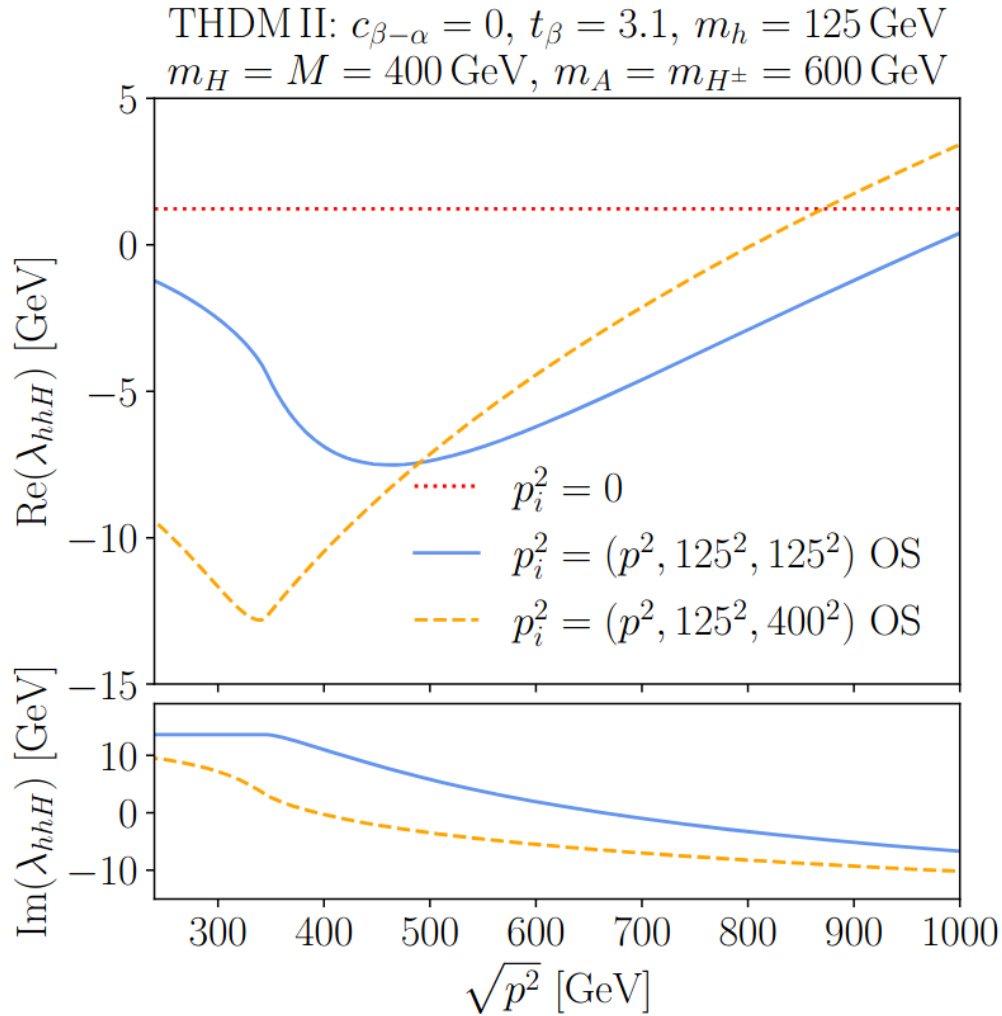


Very good agreement with HPAIR, using one-loop trilinear scalar couplings computed by anyH3/anyLambdaijk, for 2HDM benchmarks (here in alignment limit)



# Momentum effects

[Bahl, JB, Gabelmann,  
Radchenko Serdula,  
Weiglein WIP]



Peak around  $m_{hh} = m_H$  depends on  $\lambda_{hhH}$  and  $\Gamma_{\text{tot.}}^H$   
 • Here: alignment limit, so at tree level:  $\lambda_{hhH}^{(0)} = 0$

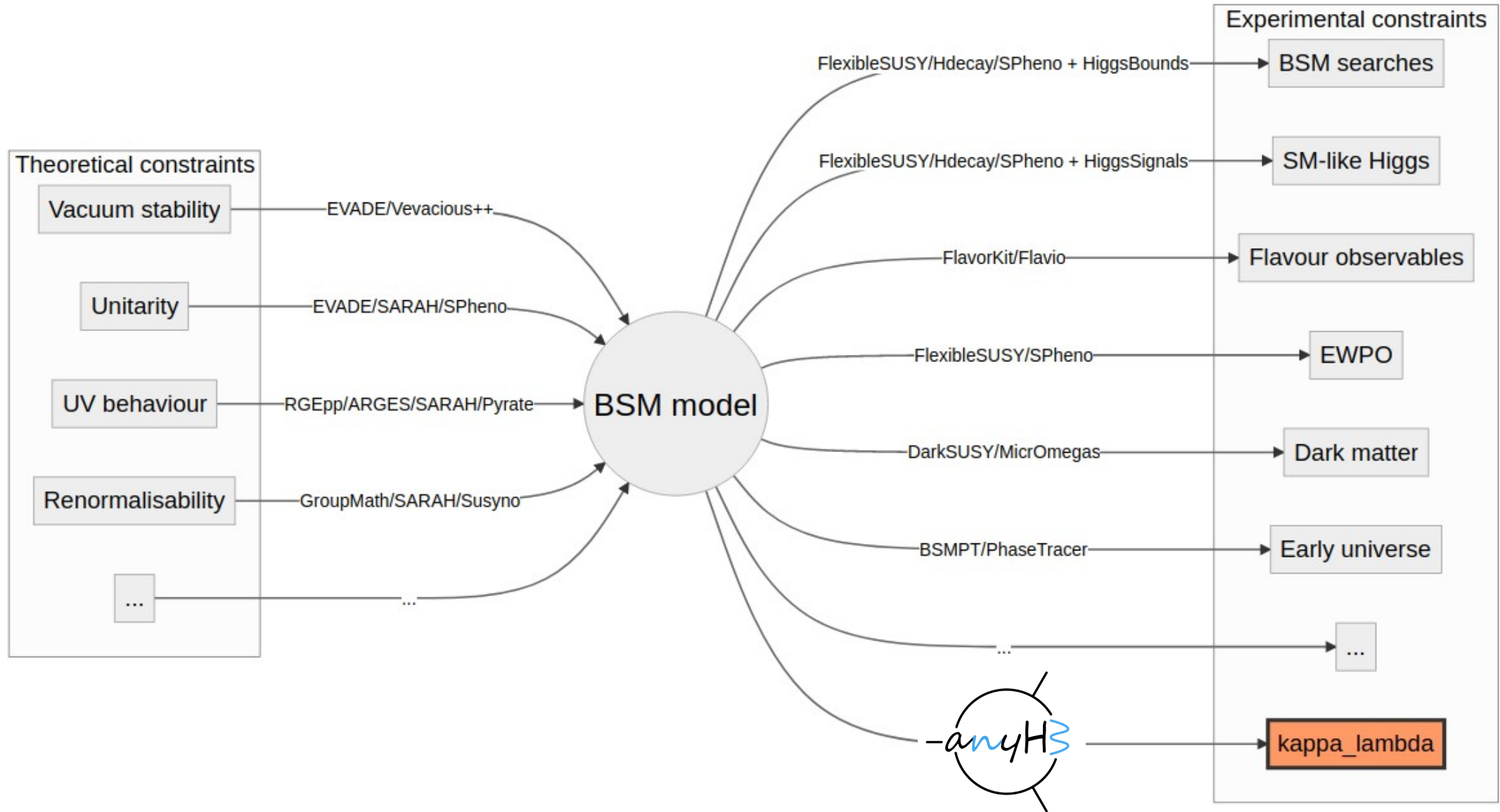
• However at loop level:  $\lambda_{hhH}^{(1)}(0, 0, 0) \sim 1 \text{ GeV} > 0$   
 but  $\lambda_{hhH}^{(1)}(m_{hh}^2, m_h^2, m_h^2) < 0$

**Consequence: ‘dip-peak’ → ‘peak-dip’ structure**

# anyH3 (v1)

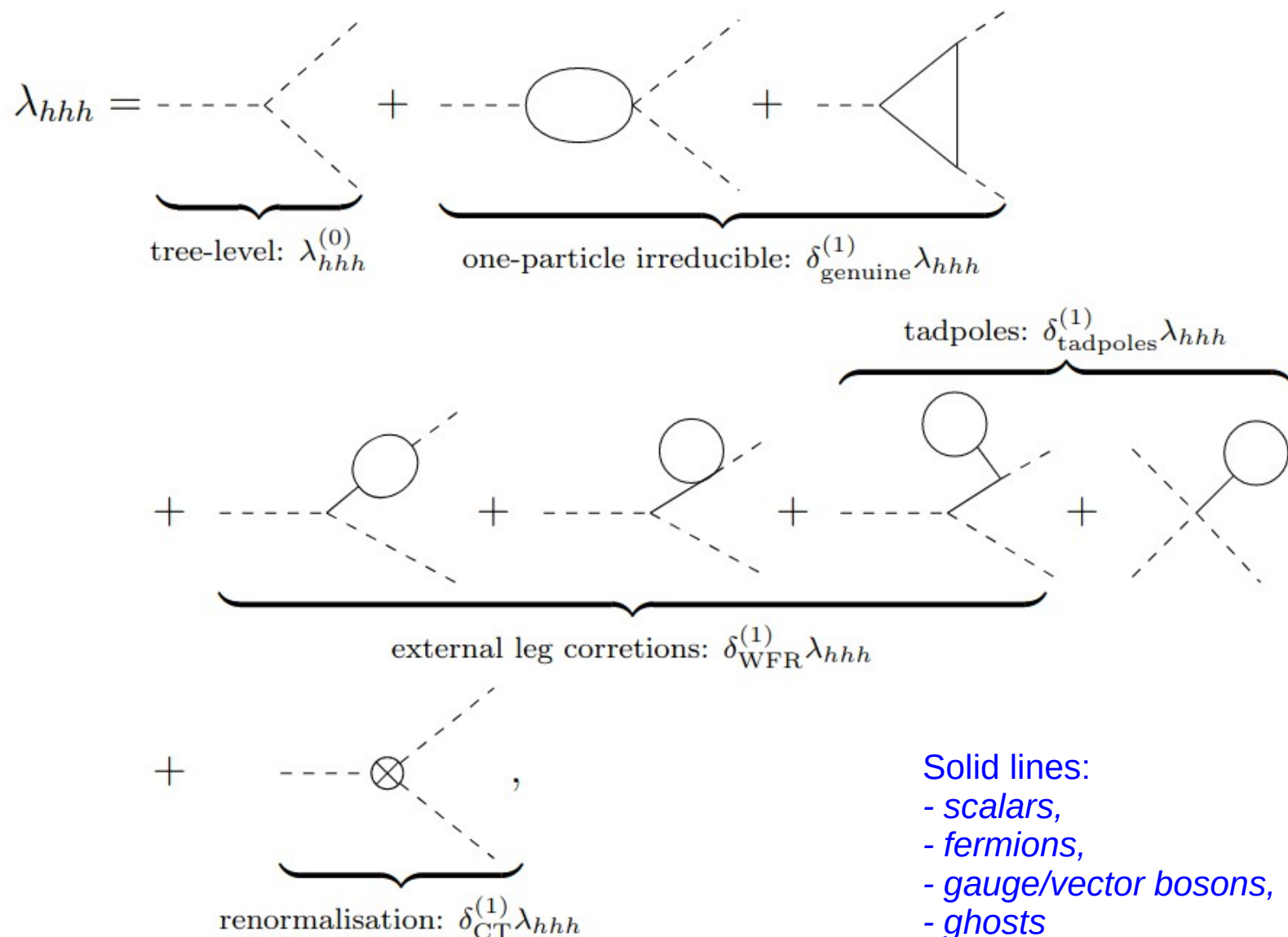


# $\lambda_{hhh}$ within the landscape of automated tools



# Full one-loop calculation of $\lambda_{hhh}$ with anyH3: how does it work?

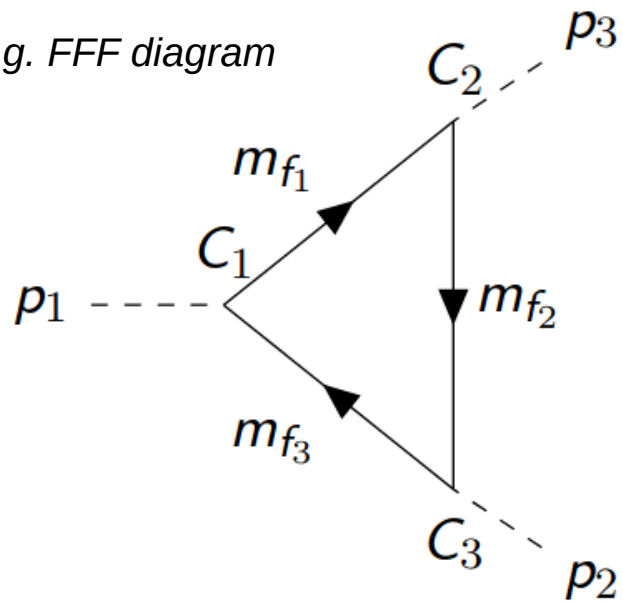
- Generic results applied to concrete (B)SM model, using inputs in UFO format  
[Degrande et al., '11], [Darmé et al. '23]
- Loop functions evaluated via COLLIER [Denner et al '16] interface, pyCollier
- Restrictions on **particles** and/or **topologies** possible
- Renormalisation performed automatically** (*more in backup*)



# Computing $\lambda_{hhh}$ in general renormalisable theories: method

Our method: we derive and implement analytic results for **generic diagrams**, i.e. assuming generic

e.g. FFF diagram



For evaluation:

- Apply to concrete (B)SM model, using inputs in UFO format [Degrande et al., '11], [Darmé et al. '23]
- Evaluate loop functions via COLLIER [Denner et al '16] interface, pyCollier
- All included in public tool anyH3 [Bahl, JB, Gabelmann, Weiglein '23]

➤ Couplings  $C_i = C_i^L P_L + C_i^R P_R$ , where  $P_{L,R} \equiv \frac{1}{2}(1 \mp \gamma_5)$

➤ Masses on the internal lines  $m_{fi}$ ,  $i=1,2,3$

➤ External momenta  $p_i$ ,  $i=1,2,3$

$$= 2\mathbf{B0}(p_3^2, m_2^2, m_3^2)(C_1^L(C_2^L C_3^R m_{f1} + C_2^R C_3^R m_{f2} + C_2^R C_3^L m_{f3}) + C_1^R(C_2^R C_3^L m_{f1} + C_2^L C_3^L m_{f2} + C_2^L C_3^R m_{f3})) + m_{f1} \mathbf{C0}(p_2^2, p_3^2, p_1^2, m_1^2, m_3^2, m_2^2)((C_1^L C_2^L C_3^R + C_1^R C_2^R C_3^L)(p_1^2 + p_2^2 - p_3^2) + 2(C_1^L C_2^L C_3^L + C_1^R C_2^R C_3^R)m_{f2} m_{f3} + 2m_{f1}(C_1^L(C_2^L C_3^R m_{f1} + C_2^R C_3^R m_{f2} + C_2^R C_3^L m_{f3}) + C_1^R(C_2^R C_3^L m_{f1} + C_2^L C_3^L m_{f2} + C_2^L C_3^R m_{f3}))) + \mathbf{C1}(p_2^2, p_3^2, p_1^2, m_1^2, m_3^2, m_2^2)(2p_2^2(C_1^L C_3^R(C_2^L m_{f1} + C_2^R m_{f2}) + C_1^R C_3^L(C_2^R m_{f1} + C_2^L m_{f2})) + (p_1^2 + p_2^2 - p_3^2)((C_1^L C_2^L C_3^R + C_1^R C_2^R C_3^L)m_{f1} + (C_1^L C_2^R C_3^L + C_1^R C_2^L C_3^R)m_{f3})) + \mathbf{C2}(p_2^2, p_3^2, p_1^2, m_1^2, m_3^2, m_2^2)((p_1^2 + p_2^2 - p_3^2)(C_1^L C_3^R(C_2^L m_{f1} + C_2^R m_{f2}) + C_1^R C_3^L(C_2^R m_{f1} + C_2^L m_{f2})) + 2p_1^2((C_1^L C_2^L C_3^R + C_1^R C_2^R C_3^L)m_{f1} + (C_1^L C_2^R C_3^L + C_1^R C_2^L C_3^R)m_{f3}))$$

(B0, C0, C1, C2: loop functions)

# Flexible choice of renormalisation schemes

$$\delta_{\text{CT}}^{(1)} \lambda_{hhh} = \text{---} \bigotimes \text{---} = ?$$

➤ **1L calculation** → renormalisation of all parameters entering  $\lambda_{hhh}$  at tree-level

➤ In general:

$$(\lambda_{hhh}^{(0)})^{\text{BSM}} = (\lambda_{hhh}^{(0)})^{\text{BSM}} \left( \underbrace{m_h \simeq 125 \text{ GeV}, v \simeq 246 \text{ GeV}}_{\text{SM sector}}, \underbrace{m_{\Phi_i}}_{\text{BSM masses}}, \underbrace{\alpha_i}_{\text{BSM mixing angles}}, \underbrace{v_i}_{\text{BSM VEVs}}, \underbrace{g_i}_{\text{indep. BSM coups.}} \right)$$

➤ Most automated codes:  $\overline{\text{MS}}/\overline{\text{DR}}$  only

➤ **anyH3**: much more flexibility, following **user choice**:

- **SM sector** ( $m_h, v$ ): fully OS or  $\overline{\text{MS}}/\overline{\text{DR}}$
- **BSM masses**: OS or  $\overline{\text{MS}}/\overline{\text{DR}}$
- **Additional couplings/vevs/mixings**: by default  $\overline{\text{MS}}$ , but **user-defined ren. conditions** also possible!

$$\delta_{\text{CT}}^{(1)} \lambda_{hhh} = \sum_x \left( \frac{\partial}{\partial x} (\lambda_{hhh}^{(0)})^{\text{BSM}} \right) \delta^{\text{CT}} x, \quad \text{with } x \in \{m_h, v, m_{\Phi_i}, v_i, \alpha_i, g_i, \text{etc.}\}$$

*Renormalised in  $\overline{\text{MS}}$ , OS, in custom schemes, etc.*

## (Default) Renormalization choice of $(v^{\text{SM}})^{\text{OS}}$ and $(m_i^2)^{\text{OS}}$

- >  $v^{\text{OS}} \equiv \frac{2M_W^{\text{OS}}}{e} \sqrt{1 - \frac{M_W^{2\text{OS}}}{M_Z^{2\text{OS}}}}$  with
  - $\delta^{(1)} M_V^{2\text{OS}} = \frac{\Pi_V^{(1),T}}{M_V^{2\text{OS}}} (p^2 = M_V^{2\text{OS}}), V = W, Z$
  - $\delta^{(1)} e^{\text{OS}} = \frac{1}{2} \dot{\Pi}_\gamma(p^2 = 0) + \text{sign}(\sin \theta_W) \frac{\sin \theta_W}{M_Z^2 \cos \theta_W} \Pi_{\gamma Z}(p^2 = 0)$
- > attention (i):  $\rho^{\text{tree-level}} \neq 1 \rightarrow$  further CTs needed (depends on the model)  
 $\rightarrow$  ability to define *custom* renormalisation conditions
- > scalar masses:  $m_i^{\text{OS}} = m_i^{\text{pole}}$ 
  - $\delta^{\text{OS}} m_i^2 = -\widetilde{\text{Re}} \Sigma_{h_i}^{(1)}|_{p^2=m_i^2}$
  - $\delta^{\text{OS}} Z_i = \widetilde{\text{Re}} \frac{\partial}{\partial p^2} \Sigma_{h_i}^{(1)}|_{p^2=m_i^2}$
- > attention (ii): scalar mixing may also require further CTs/tree-level relations

**All bosonic one- & two-point functions and their derivatives for general QFTs are required for flexible OS renormalisation.**



# Features of anyH3, so far

- Import/conversion of any UFO model
- Definition of renormalisation schemes

```
# schemes.yml

renormalization_schemes:
  MS:
    SM_names:
      Higgs-Boson: h1
    VEV_counterterm: MS
    mass_counterterms:
      h1: MS
      h2: MS
  OS:
    SM_names:
      Higgs-Boson: h1
    VEV_counterterm: OS
    custom_CT_hhh: 'dbetaH =
f"({Sigma('Hm1','Hm2',momentum='0'))} +
{Sigma('Hm1','Hm2',momentum='MHm2**2')})/-(
2*MHm2**2)"

    dTanBeta = f"({dbetaH})/cos(betaH)**2"

    ...
```

(extract from  
schemes.yml  
for 2HDM)

- Analytical / numerical / LaTeX outputs
- **3 user interfaces:**
  - Python library

```
from anyBSM import anyH3
myfancymodel = anyH3('path/to/UFO/model')
result = myfancymodel.lambdahhh()
```
  - Command line
  - Mathematica interface
- **Perturbative unitarity checks** available (at tree level and in high-energy limit for now)
- Can be used together with a spectrum generator and **handles SLHA format**
- Efficient **caching** available
- Lots more!

# New results I: mass-splitting effects in various BSM models

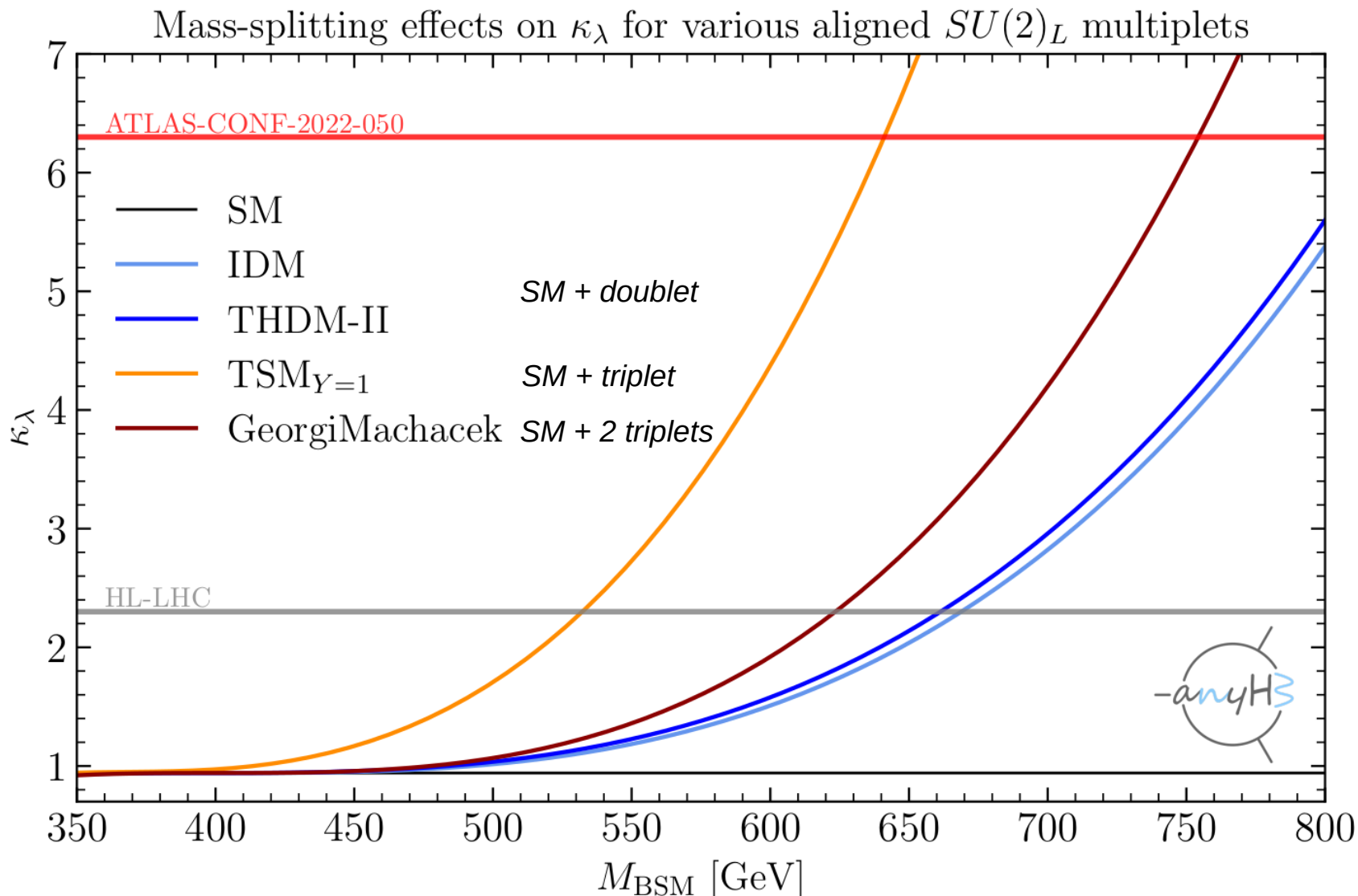
- Consider the non-decoupling limit in several BSM models

$$M_{\text{BSM}}^2 = \mathcal{M}^2 + \tilde{\lambda} v^2$$

- Increase  $M_{\text{BSM}}$ , keeping  $\mathcal{M}$  fixed
  - large mass splittings
  - **large BSM effects!**

- Perturbative unitarity checked with anyPerturbativeUnitarity

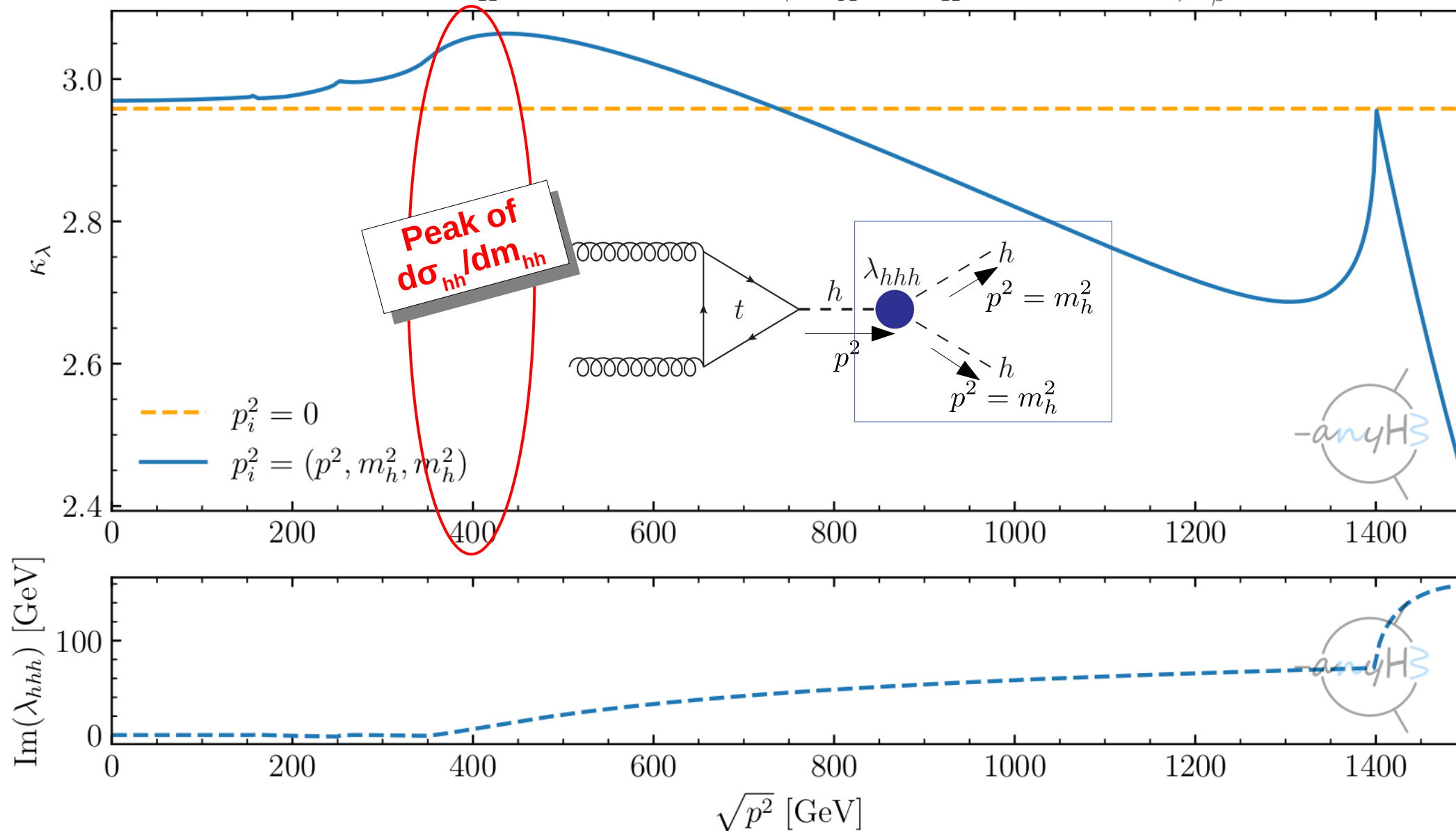
- Constraints on BSM parameter space!**



Here: scenarios with lightest BSM scalar mass & BSM mass param. at 400 GeV; other BSM scalar masses =  $M_{\text{BSM}}$

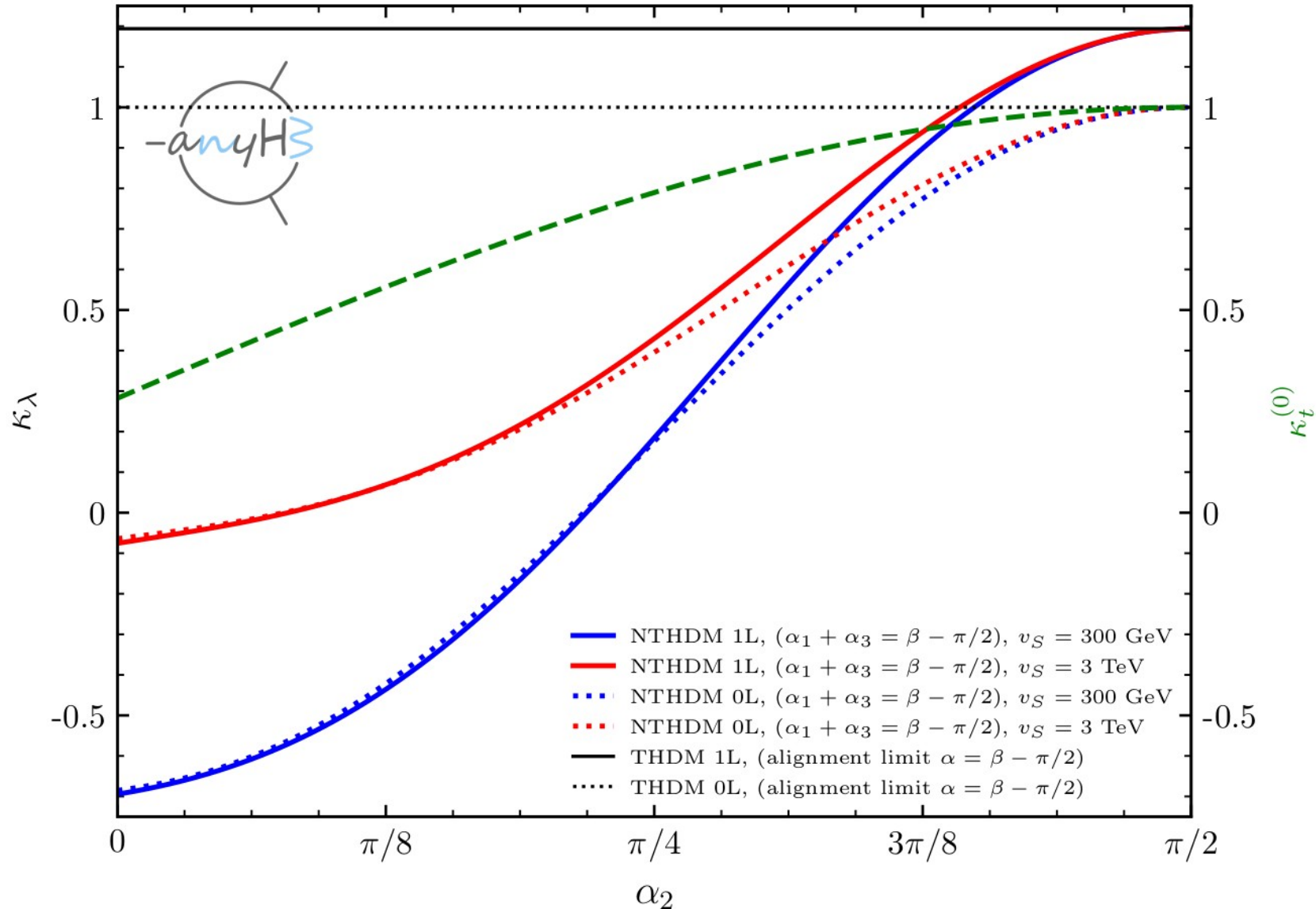
# New results II: momentum dependence in the 2HDM

THDM-I:  $m_H = M = 400 \text{ GeV}$ ,  $m_A = m_{H^\pm} = 700 \text{ GeV}$ ,  $t_\beta = 2$



# More new results with anyH3: an example in the N2HDM

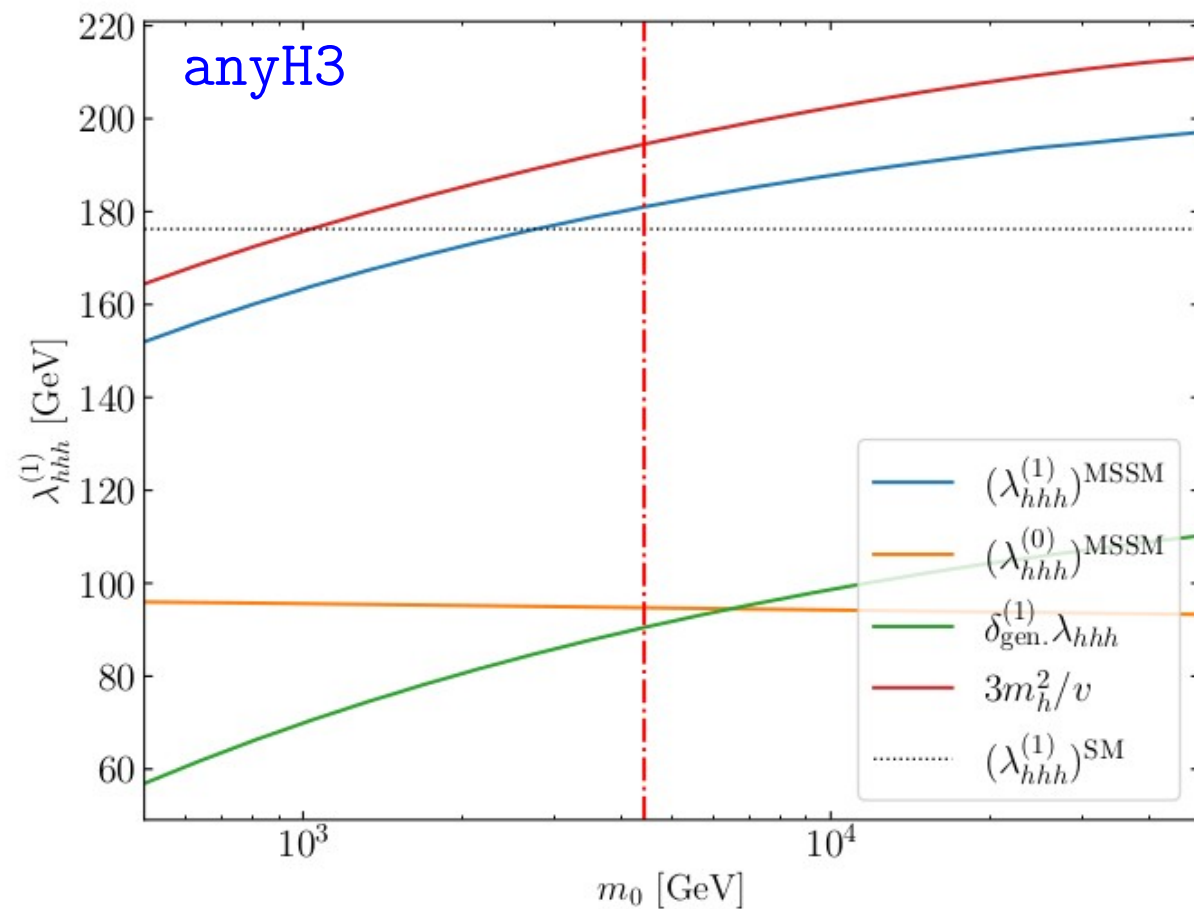
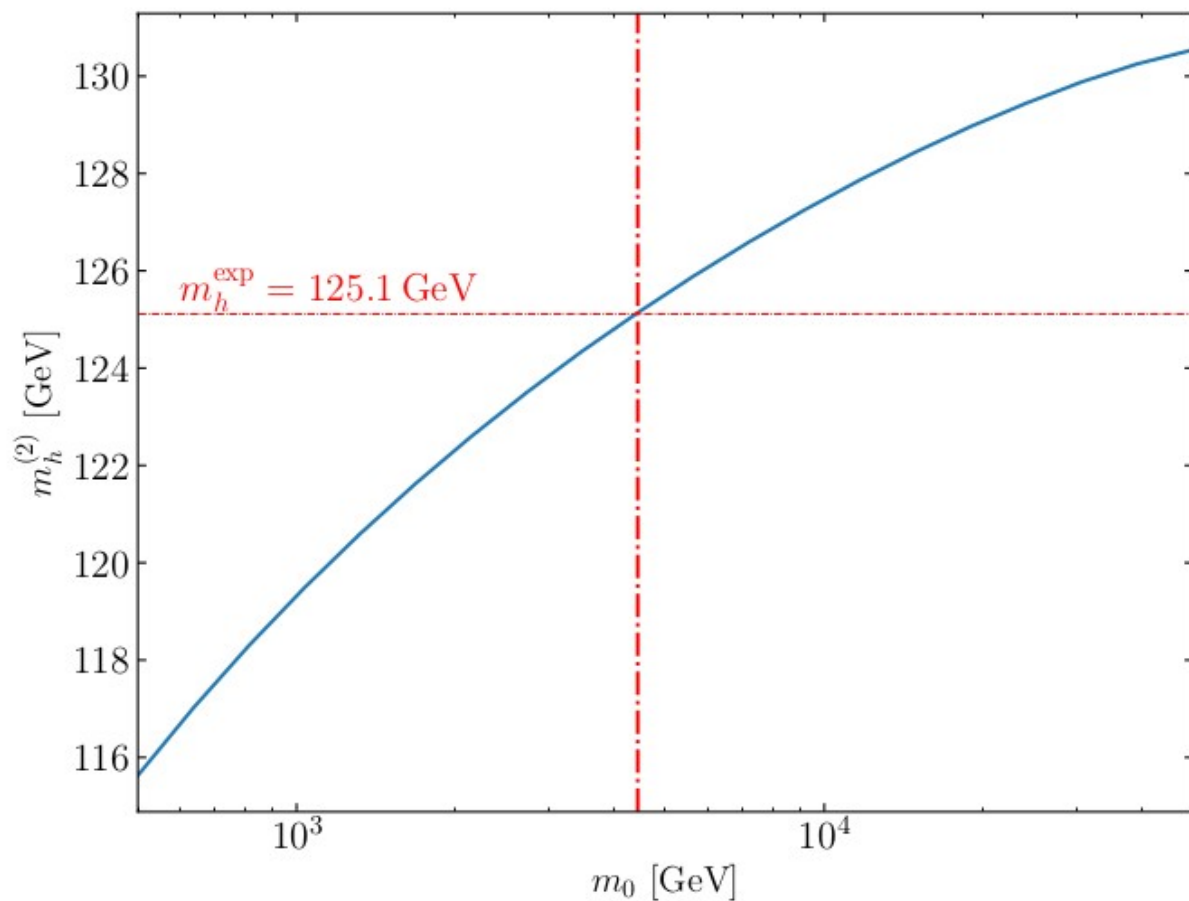
NTHDM:  $m_{h_2} = 125.1$  GeV,  $m_{h_1} = m_{h_3} = m_A = m_{H^\pm} = 300$  GeV,  $\tilde{\mu} = 100$  GeV,  $t_\beta = 2$



- N2HDM = 2HDM + real singlet
- CP-even sector: 3 states  
 $h_1, h_2, h_3$ ,  
with 3 mixing angles  $\alpha_1, \alpha_2, \alpha_3$
- Here  $\alpha_2 \rightarrow \pi/2 \rightarrow$  recover 2HDM  
(itself in alignment limit)
- We can study e.g. the relative  
sign of  $\kappa_\lambda$  and  $\kappa_t \rightarrow$  affects  
double-Higgs production
- $\kappa_t$  too far away from 1 excluded

# Full one-loop calculation of $\lambda_{hhh}$ in the MSSM

CMSSM,  $m_0 = m_{1/2} = -A_0$ ,  $\tan\beta = 10$ ,  $\text{sgn}(\mu) = 1$ , with  $m_h$  computed at 2L in SPheno



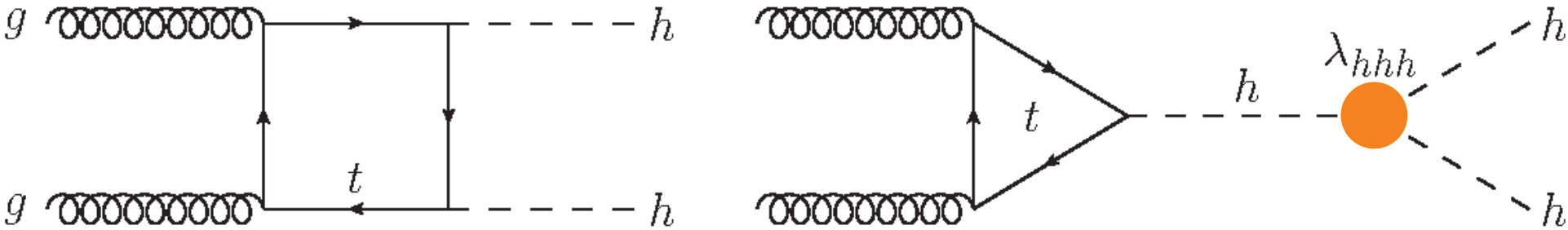
- Example for a very simple version of the constrained MSSM → BSM parameters  $m_0$ ,  $m_{1/2}$ ,  $A_0$ ,  $\text{sgn}(\mu)$ ,  $\tan\beta$
- For each point,  $M_h$  computed at 2L with SPheno, and SLHA output of SPheno used as input of anyH3

# Trilinear Higgs self-coupling

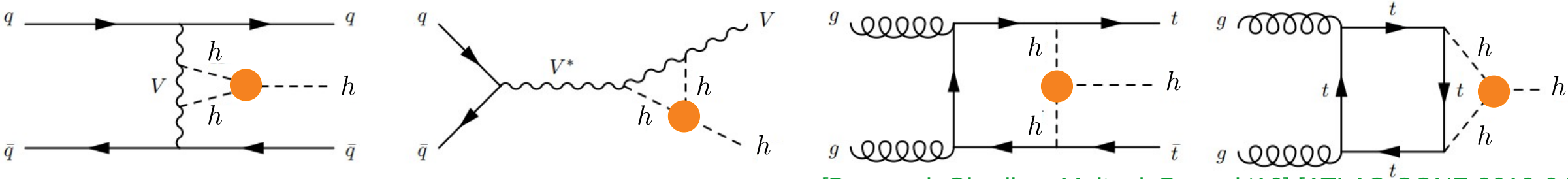


# Experimental probes of $\lambda_{hhh}$

➤ **Double-Higgs production**  $\rightarrow \lambda_{hhh}$  enters at leading order (LO)  $\rightarrow$  **most direct probe!**

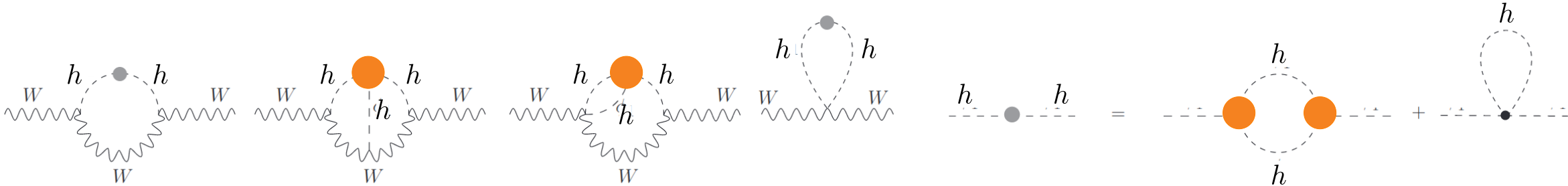


➤ **Single-Higgs production**  $\rightarrow \lambda_{hhh}$  enters at NLO



[Degrassi, Giardino, Maltoni, Pagani '16] [ATLAS-CONF-2019-049]

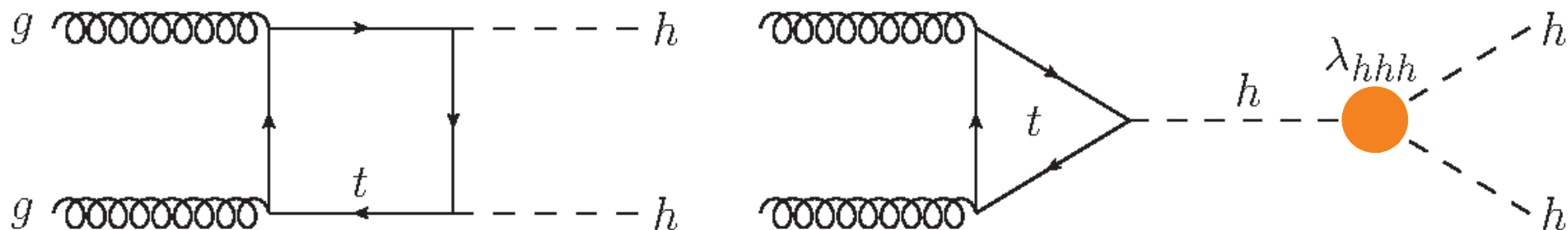
➤ **Electroweak Precision Observables (EWPOs)**  $\rightarrow \lambda_{hhh}$  enters at NNLO



[Degrassi, Fedele, Giardino '17]

# Accessing $\lambda_{hhh}$ via di-Higgs production

- **Di-Higgs production**  $\rightarrow \lambda_{hhh}$  enters at leading order (LO)  $\rightarrow$  **most direct probe of  $\lambda_{hhh}$**



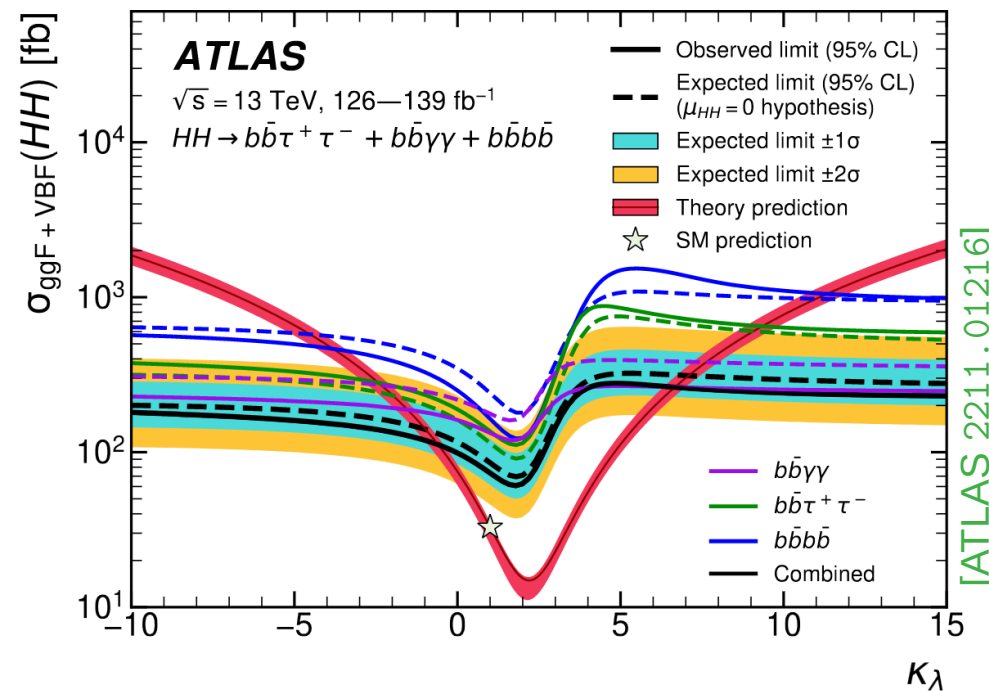
[ Note: Single-Higgs production (EW precision observables)  $\rightarrow \lambda_{hhh}$  enters at NLO (NNLO) ]

- Box and triangle diagrams **interfere destructively**  
 $\rightarrow$  small di-Higgs cross-section  $\sigma_{hh}$  in SM

$\rightarrow$  BSM deviation in  $\lambda_{hhh}$  can **significantly alter di-Higgs production!**

- Upper limit on di-Higgs cross-section  
 $\rightarrow$  **limits on  $\kappa_\lambda \equiv \lambda_{hhh} / (\lambda_{hhh}^{(0)})^{SM}$**

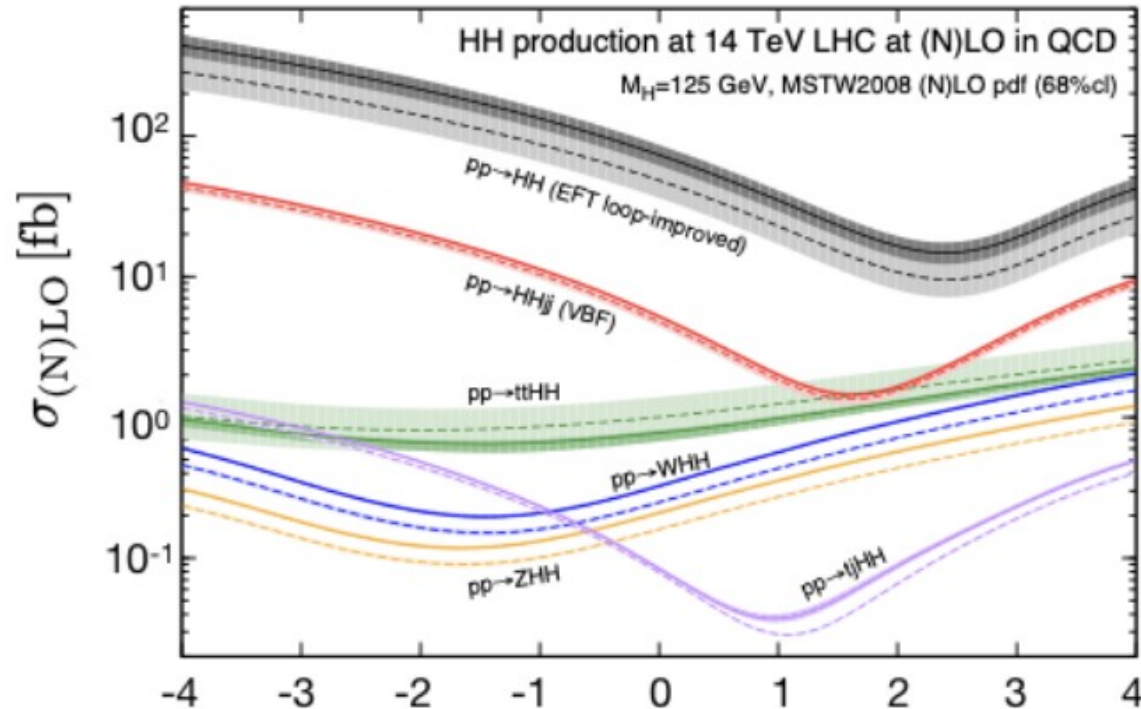
- $\kappa_\lambda$  as an *effective coupling*:  $\mathcal{L} \supset -\kappa_\lambda \times \frac{3m_h^2}{v^2} \cdot h^3 + \dots$



# Di-Higgs production cross-sections as a function of $\lambda_{hhh}$

Plots taken from  
[de Blas et al., 1905.03764]

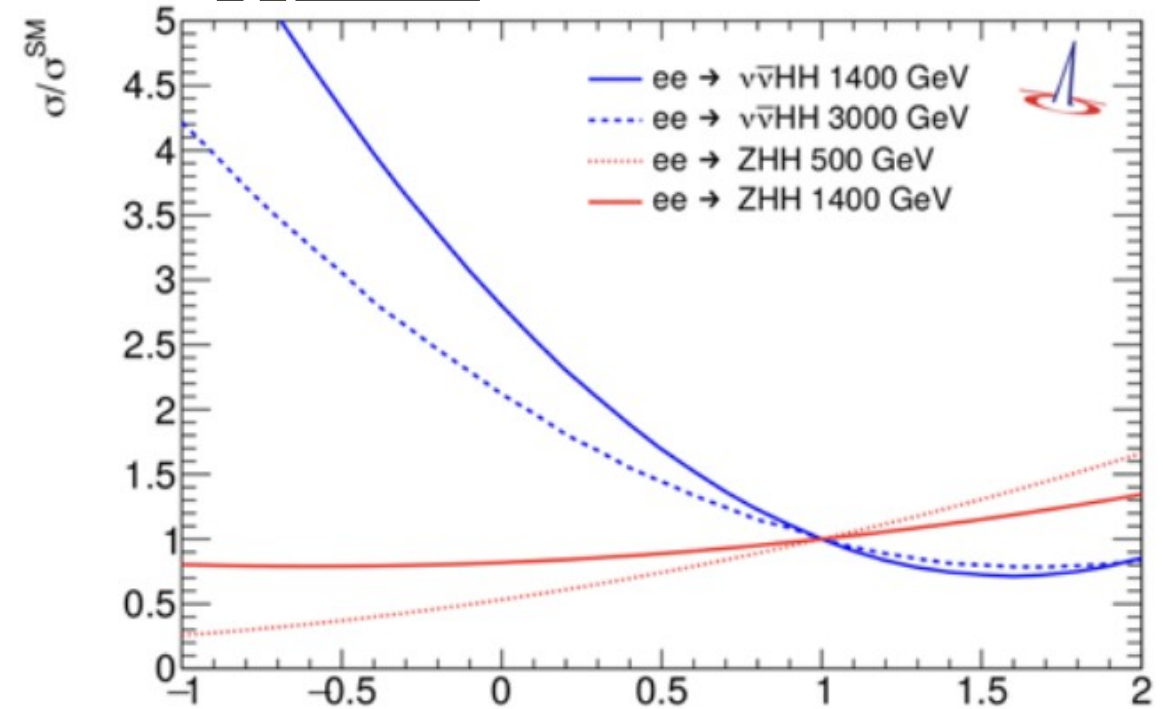
## Hadron collider



[Frederix et al., 1401.7340]

$$\lambda_3/\lambda_3^{SM} = \kappa_\lambda$$

## $e^+e^-$ collider

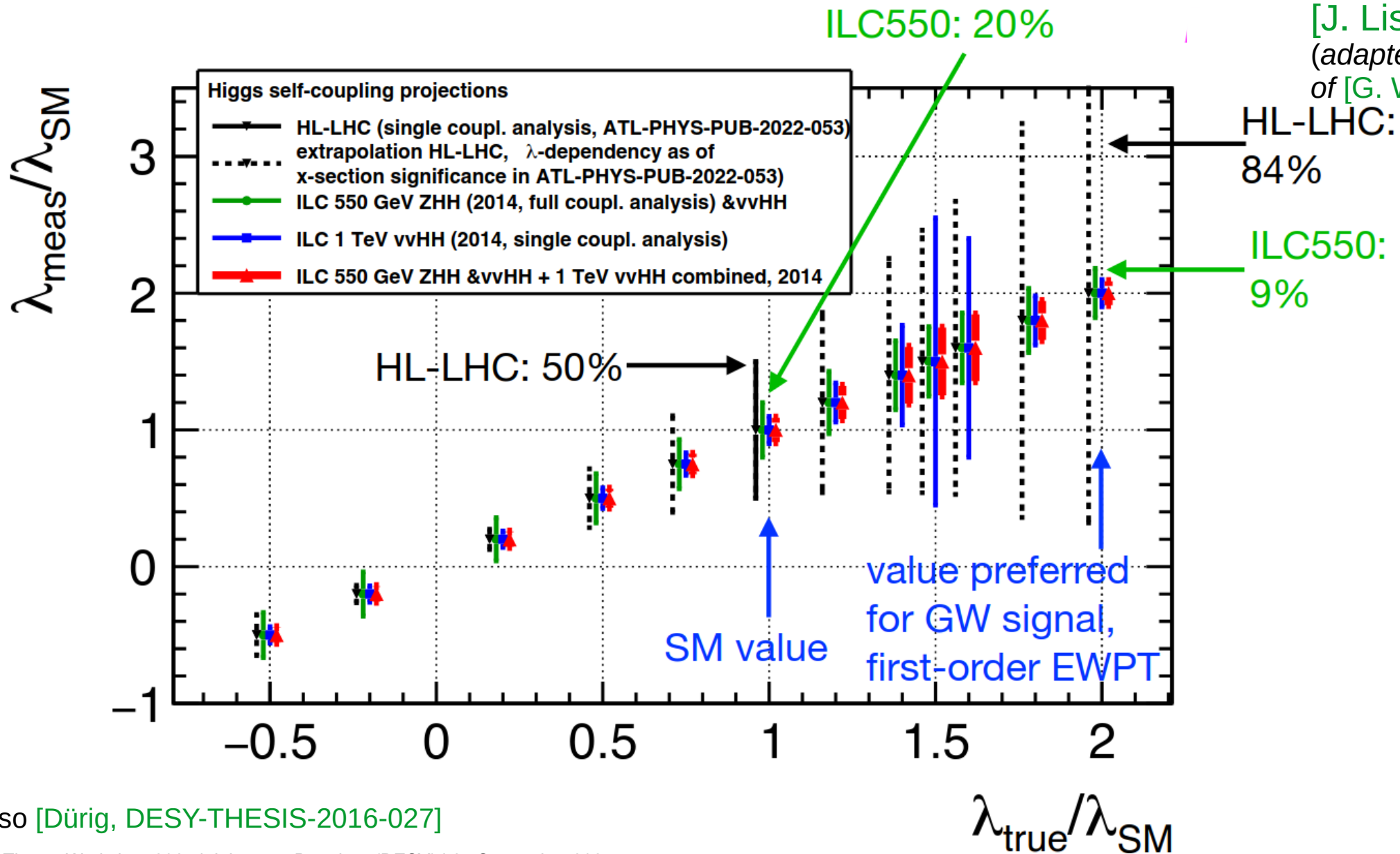


$$\lambda_3/\lambda_3^{SM} = \kappa_\lambda \quad [\text{Reuter '19}]$$

- **BSM deviation in  $\kappa_\lambda$  modifies the interference between different contributions to di-Higgs production**
- Strong impact on total cross-sections (and also on differential distributions, see later slides)

# Precision on the determination of $\lambda_{\text{hhh}}$ as a function of $\lambda_{\text{hhh}}$

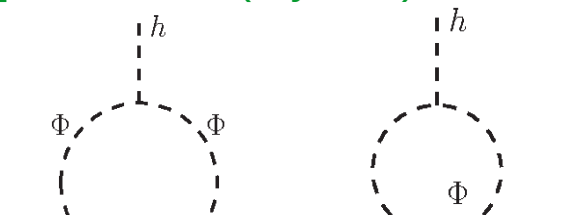
[J. List et al '24]  
(adapted from slide  
of [G. Weiglein '24])



See also [Dürig, DESY-THESIS-2016-027]

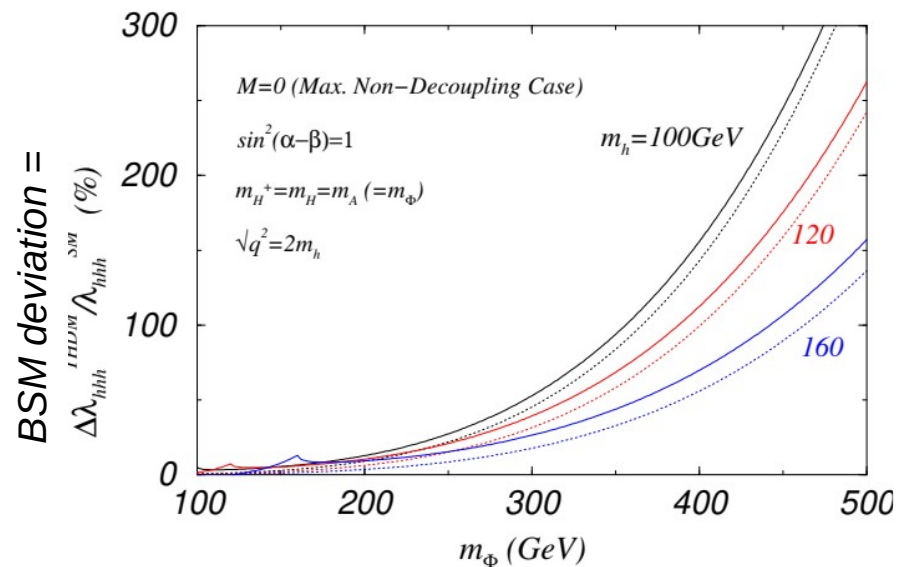
# Mass splitting effects in $\lambda_{hhh}$

- First investigation of 1L BSM contributions to  $\lambda_{hhh}$  in 2HDM: [Kanemura, (Kiyoura), Okada, Senaha, Yuan '02, '04]



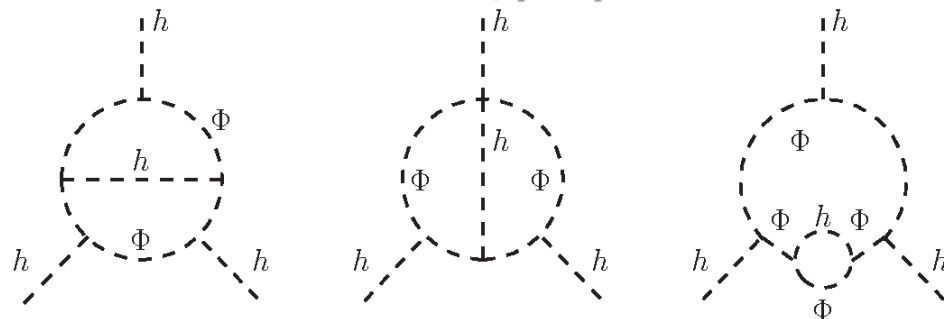
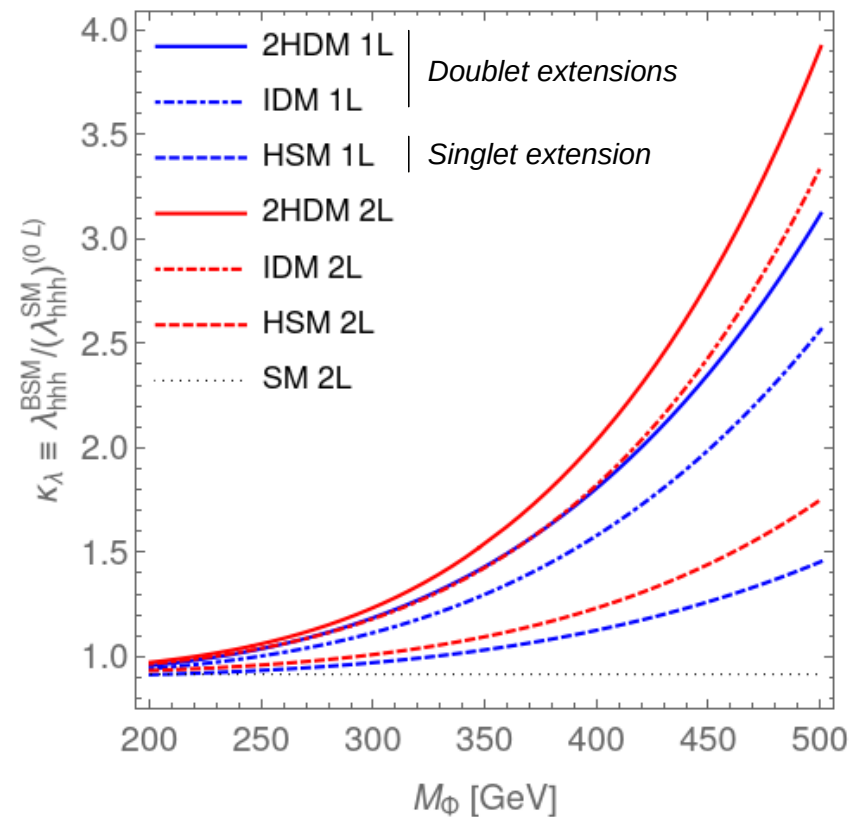
$$g_{hh\Phi\Phi} = -\frac{2(M^2 - m_\Phi^2)}{v^2}$$

$(\Phi \in \{H, A, H^\pm\})$



- Deviations of tens/hundreds of % from SM possible, for large  $g_{h\Phi\Phi}$  or  $g_{hh\Phi\Phi}$  couplings
- Mass splitting effects**, now found in various models (2HDM, inert doublet model, singlet extensions, etc.)

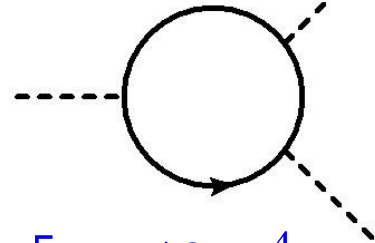
- Large effects **confirmed at 2L** in [JB, Kanemura '19]  
→ **leading 2L corrections involving BSM scalars ( $H, A, H^\pm$ ) and top quark**, computed in effective potential approximation



# One-loop mass-splitting effects

- **Leading one-loop** corrections to  $\lambda_{hhh}$  in models with extended sectors (like 2HDM):

*SM top quark loop*



$$\delta^{(1)}\lambda_{hhh} \supset \frac{1}{16\pi^2} \left[ -\frac{48m_t^4}{v^3} \right]$$

*BSM scalar loops*



$$+ \sum_{\Phi} \frac{4n_{\Phi}m_{\Phi}^4}{v^3} \left( 1 - \frac{\mathcal{M}^2}{m_{\Phi}^2} \right)^3$$

*First found in 2HDM:  
[Kanemura, Kiyoura,  
Okada, Senaha, Yuan '02]*

$\mathcal{M}$  : **BSM mass scale**, e.g. soft breaking scale  $M$  of  $Z_2$  symmetry in 2HDM

$n_{\Phi}$  : # of d.o.f of field  $\Phi$

- Size of new effects depends on how the BSM scalars acquire their mass:  $m_{\Phi}^2 \sim \mathcal{M}^2 + \tilde{\lambda}v^2$

$$\left( 1 - \frac{\mathcal{M}^2}{m_{\Phi}^2} \right)^3 \longrightarrow \begin{cases} 0, & \text{for } \mathcal{M}^2 \gg \tilde{\lambda}v^2 \\ 1, & \text{for } \mathcal{M}^2 \ll \tilde{\lambda}v^2 \end{cases}$$

**Huge BSM  
effects possible!**



# Examples of scalar contributions to $\lambda_{hhh}$ in aligned 2HDM

BSM scalars:  
 $\Phi \in \{H, A, H^\pm\}$   
 $m_\Phi^2 = M^2 + \tilde{\lambda}_\Phi v^2$

Coupling/Order	0L	1L	2L	3L
$g_{hhhh}$		<i>subleading</i> 	<i>subleading</i>	<i>subleading</i>
$g_{(h)h\Phi\Phi}$ $\left[ g_{hh\Phi\Phi} = -\frac{2(M^2 - m_\Phi^2)}{v^2} \right]$	-			
$g_{(h)H\Phi\Phi'}$ [ $g_{(h)G\Phi\Phi'}$ case similar]	-	-		
$g_{\Phi\Phi\Phi'\Phi'}$ [2 BSM scalars of species $\Phi$ , 2 of species $\Phi'$ ]	-	-		

[NB: 1  $h$  can be replaced by a VEV] → no further type of coupling entering after 2L  
→ for each class of diagrams, perturbative convergence can be checked!

# Constraining BSM models with $\lambda_{hhh}$

- i. Can we apply the limits on  $\kappa_\lambda$ , extracted from experimental searches for di-Higgs production, for BSM models?*
- ii. Can large BSM deviations occur for points still allowed in light of theoretical and experimental constraints? If so, how large can they become?*

**As a concrete example, we consider an aligned 2HDM**

**Based on**

**arXiv:2202.03453 (Phys. Rev. Lett.) in collaboration with Henning Bahl and Georg Weiglein**

# Can we apply di-Higgs results for the aligned 2HDM?

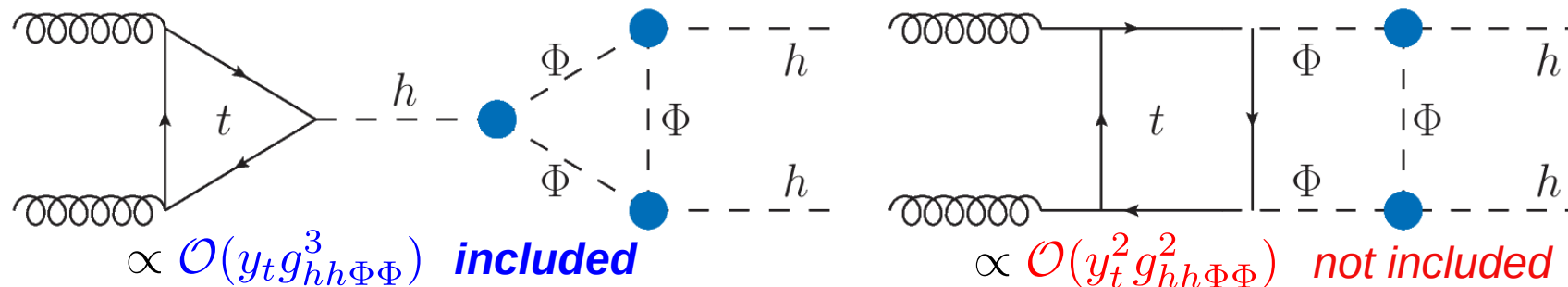
- Current strongest limits on  $\kappa_\lambda$  from ATLAS di-Higgs searches

$$-1.2 < \kappa_\lambda < 7.2 \text{ [ATLAS-CONF-2024-006]}$$

$$[\text{where } \kappa_\lambda \equiv \lambda_{\text{hhh}} / (\lambda_{\text{hhh}}^{(0)})^{\text{SM}}]$$

- What are the *assumptions* for the ATLAS limits?

- All other Higgs couplings (to fermions, gauge bosons) are SM-like  
→ this is **ensured by the alignment** ✓
- The modification of  $\lambda_{\text{hhh}}$  is the only source of deviation of the *non-resonant Higgs-pair production cross section* from the SM



→ We **correctly include all leading BSM effects to di-Higgs production, in powers of  $g_{hh\Phi\Phi}$ , up to NNLO!** ✓

- **We can apply the ATLAS limits to our setting!**

# A parameter scan in the aligned 2HDM

[Bahl, JB, Weiglein PRL '22]

- Our strategy:
  1. **Scan BSM parameter space**, keeping only points passing various theoretical and experimental constraints (*see below*)
  2. Identify regions with **large BSM deviations in  $\lambda_{hhh}$**
  3. Devise a **benchmark scenario** allowing large deviations and investigate impact of experimental limit on  $\lambda_{hhh}$
- Here: we consider an **aligned 2HDM of type-I**, but similar results expected for other 2HDM types, or other BSM models with extended Higgs sectors
- Constraints in our parameter scan:
  - experimental

    - 125-GeV Higgs measurements with HiggsSignals
    - Direct searches for BSM scalars with HiggsBounds
    - b-physics constraints, using results from [Gfitter group 1803.01853]
    - EW precision observables, computed at two loops with THDM\_EWPOS [Hessenberger, Hollik '16, '22]

Checked with ScannerS  
[Mühlleitner et al. 2007.02985]
  - theoretical

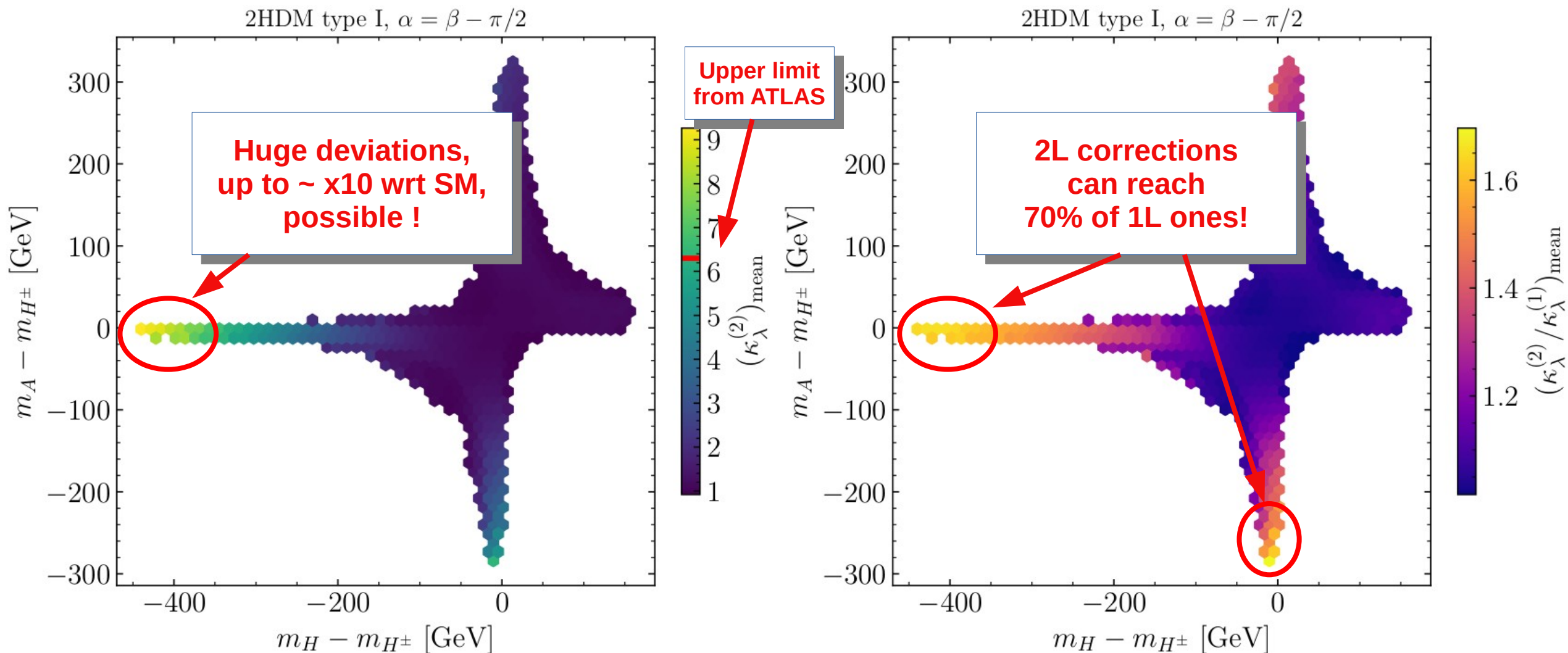
    - Vacuum stability
    - Boundedness-from-below of the potential
    - NLO perturbative unitarity, using results from [Grinstein et al. 1512.04567], [Cacchio et al. 1609.01290]

Checked with ScannerS
- For points passing these constraints, we **compute  $\kappa_\lambda$  at 1L and 2L**, using results from [JB, Kanemura '19]

# Parameter scan results

[Bahl, JB, Weiglein PRL '22]

Mean value for  $\kappa_\lambda^{(2)} = (\lambda_{hhh}^{(2)})^{2\text{HDM}} / (\lambda_{hhh}^{(0)})^{\text{SM}}$  [left] and  $\kappa_\lambda^{(2)} / \kappa_\lambda^{(1)} = (\lambda_{hhh}^{(2)})^{2\text{HDM}} / (\lambda_{hhh}^{(1)})^{2\text{HDM}}$  [right] in  $(m_H - m_{H^\pm}, m_A - m_{H^\pm})$  plane



- 2L corrections can become **significant** (up to  $\sim 70\%$  of 1L)
- **Huge enhancements** (by a factor  $\sim 10$ ) of  $\lambda_{hhh}$  possible for  $m_A \sim m_{H^\pm}$  and  $m_H \sim M$

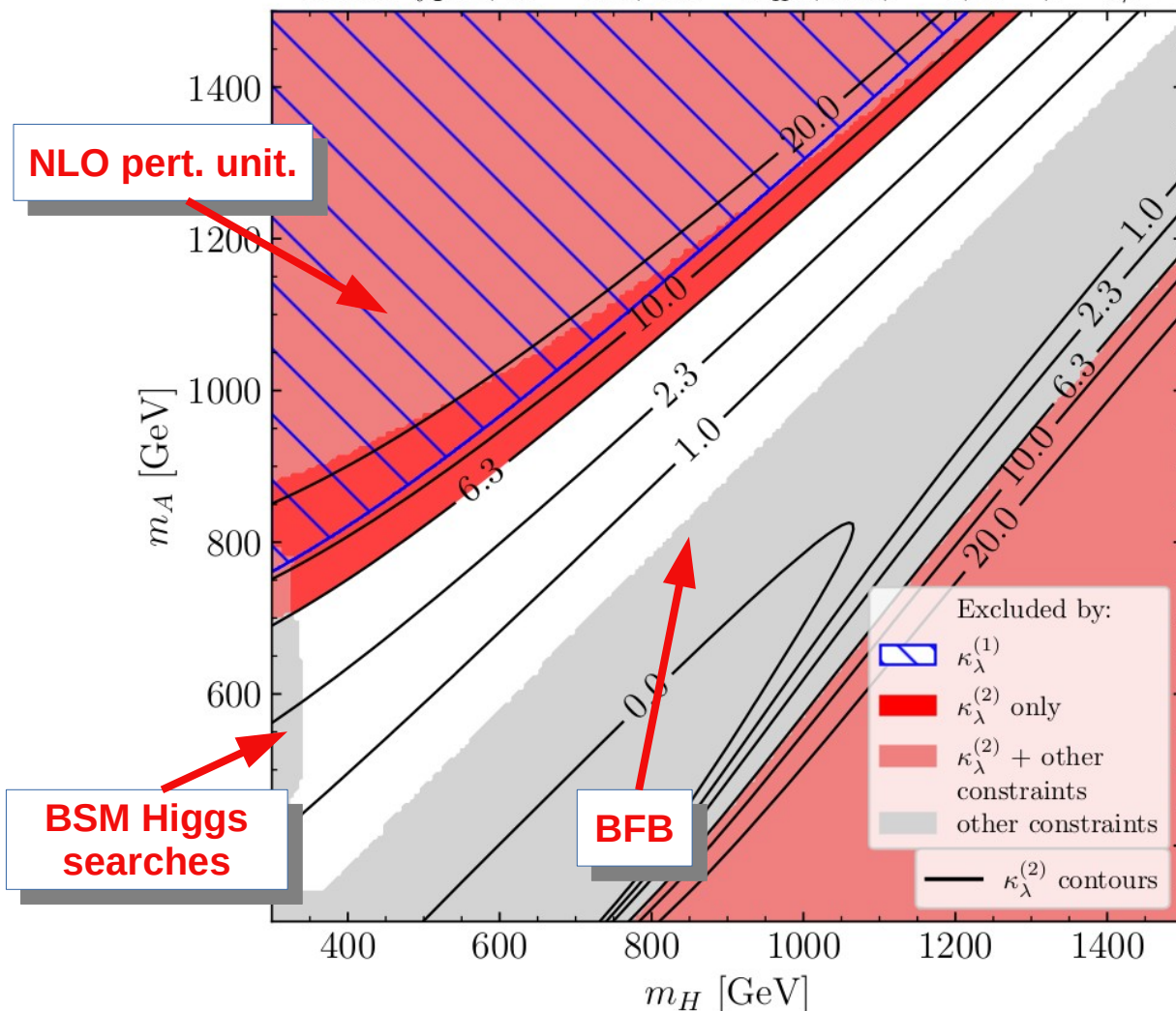
# A benchmark scenario in the aligned 2HDM

[Bahl, JB, Weiglein PRL '22]

Results shown for aligned 2HDM of type-I, similar for other types (*available in backup*)

We take  $m_A = m_{H^\pm}$ ,  $M = m_H$ ,  $\tan\beta = 2$

2HDM type I,  $M = m_H$ ,  $m_A = m_{H^\pm}$ ,  $\tan\beta = 2$ ,  $\alpha = \beta - \pi/2$



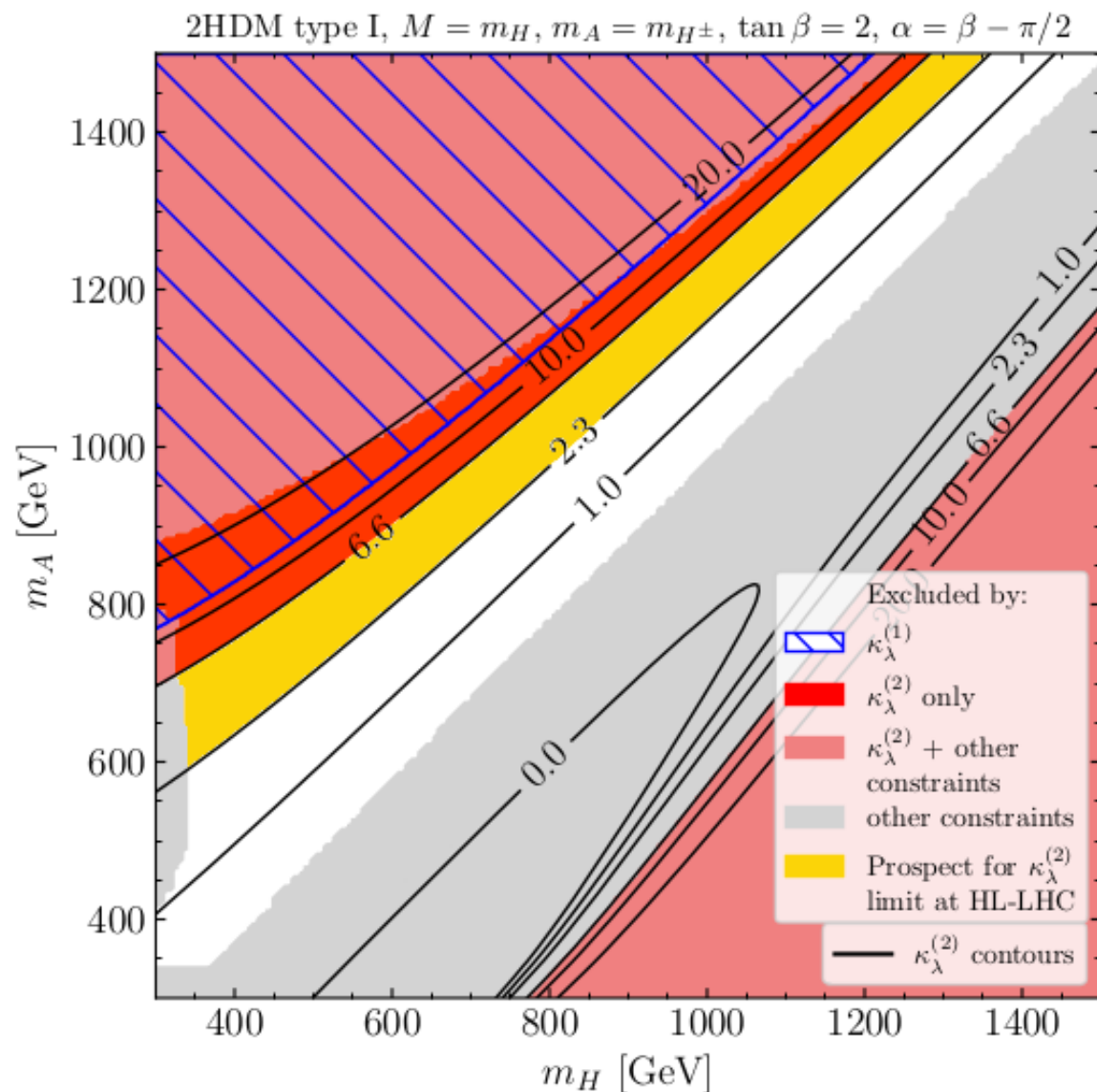
- **Grey area:** area excluded by other constraints, in particular BSM Higgs searches, boundedness-from-below (BFB), perturbative unitarity
- **Light red area:** area excluded both by other constraints (BFB, perturbative unitarity) and by  $\kappa_\lambda^{(2)} > 6.3$  [in region where  $\kappa_\lambda^{(2)} < -0.4$  the calculation isn't reliable]
- **Dark red area:** new area that is **excluded ONLY by  $\kappa_\lambda^{(2)} > 6.3$** . Would otherwise not be excluded!
- **Blue hatches:** area excluded by  $\kappa_\lambda^{(1)} > 6.3 \rightarrow$  impact of including 2L corrections is significant!



# A benchmark scenario in the aligned 2HDM – future prospects

Suppose for instance the upper bound on  $\kappa_\lambda$  becomes  $\kappa_\lambda < 2.3$

[Bahl, JB, Weiglein '23]



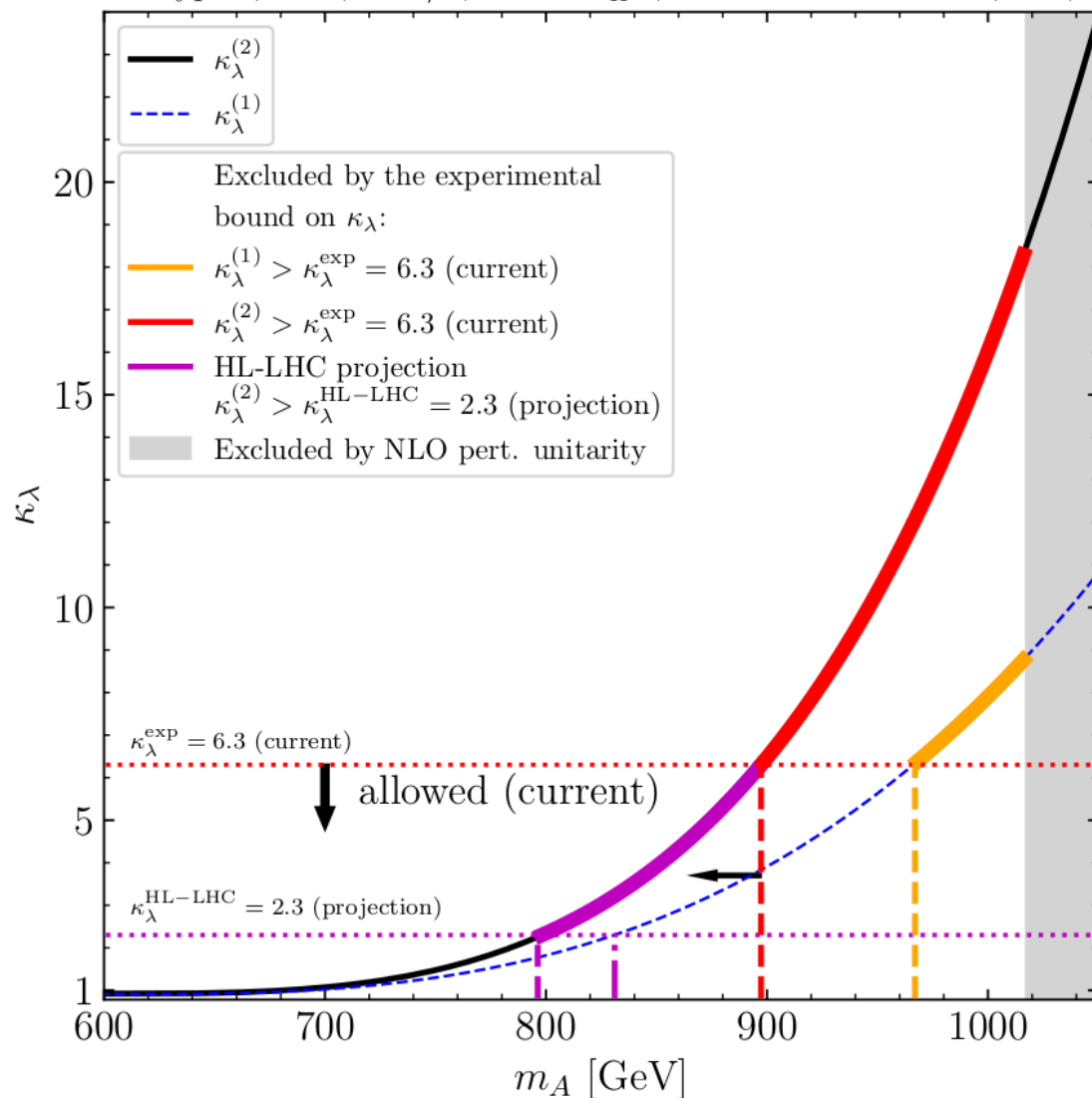
- **Golden area:** additional exclusion if the limit on  $\kappa_\lambda$  becomes  $\kappa_\lambda^{(2)} < 2.3$  (achievable at HL-LHC)
- Of course, **prospects even better with an e<sup>+</sup>e<sup>-</sup> collider!**
- Experimental constraints, such as Higgs physics, may also become more stringent, however **not** theoretical constraints (like BFB or perturbative unitarity)

# A benchmark scenario in the aligned 2HDM – 1D scan

Within the previously shown plane, we fix  $M=m_H=600$  GeV, and vary  $m_A=m_{H^\pm}$

2HDM type I,  $\alpha = \beta - \pi/2$ ,  $m_A = m_{H^\pm}$ ,  $M = m_H = 600$  GeV,  $\tan \beta = 2$

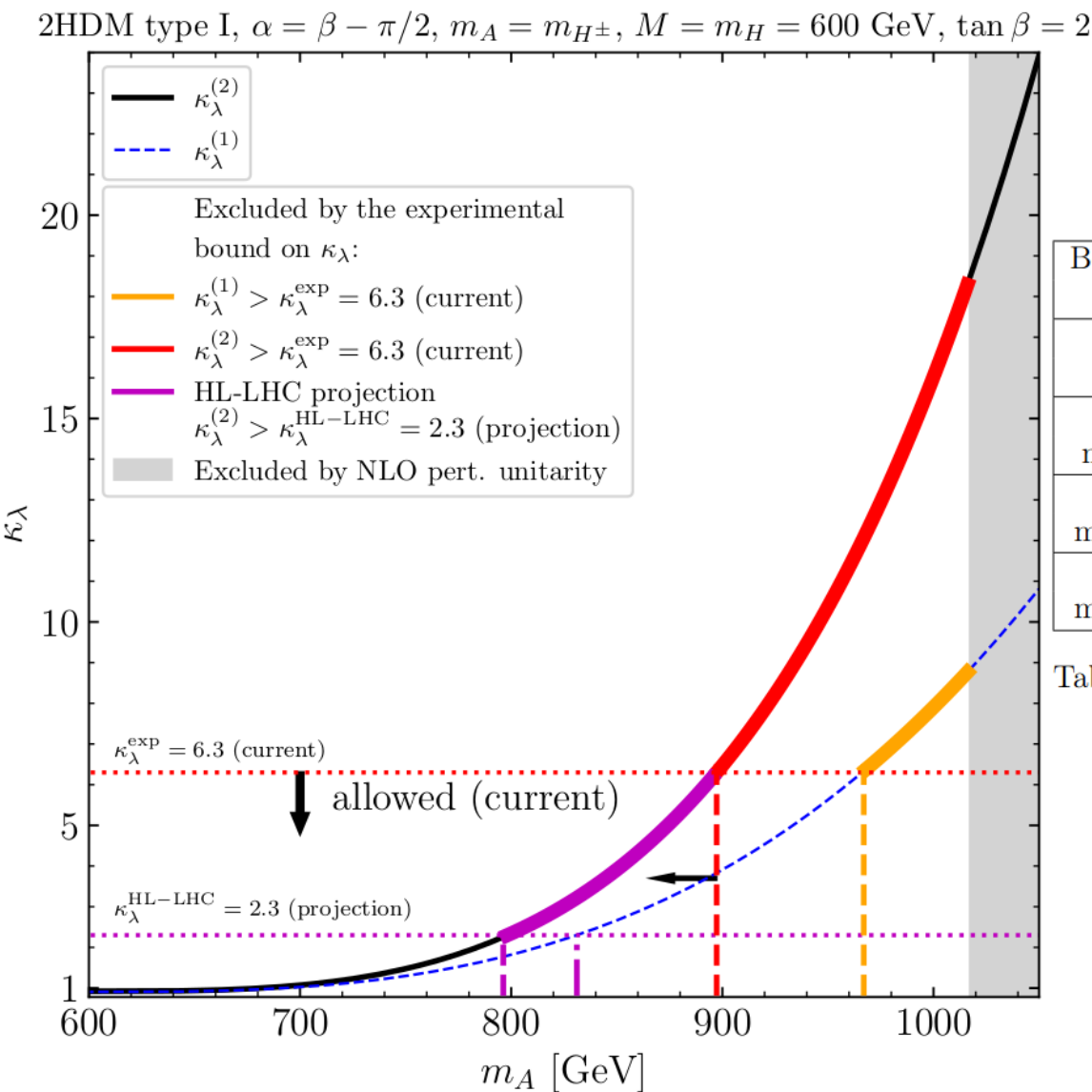
[Bahl, JB, Weiglein PRL '22]



- Illustrates the significantly improved reach of the experimental limit when including **2L corrections** in calculation of  $\kappa_\lambda$
- A stricter choice for the perturbative unitarity constraint (grey) does not significantly change the region excluded by  $\kappa_\lambda^{(2)}$

# A benchmark scenario in the aligned 2HDM – 1D scan

[Bahl, JB, Weiglein PRL '22]



Bound on eigenvalues	$\max(m_A)$ with LO pert. unit.	$\max(m_A)$ with NLO pert. unit.	$\max(m_A)$ with finite $\sqrt{s} \in [3 \text{ TeV}, 10 \text{ TeV}]$
$\max( a_i ) < 1$ $\max( \Re(a_i) ) < 1$	1161 GeV 1161 GeV	1017 GeV 1033 GeV	– 1260 GeV
$\max( a_i ) < 0.5$ $\max( \Re(a_i) ) < 0.5$	917 GeV 917 GeV	937 GeV 958 GeV	– 929 GeV
$\max( a_i ) < 0.49$ $\max( \Re(a_i) ) < 0.49$	911 GeV 911 GeV	933 GeV 956 GeV	– 922 GeV
$\max( a_i ) < 0.45$ $\max( \Re(a_i) ) < 0.45$	889 GeV 889 GeV	912 GeV 948 GeV	– 897 GeV

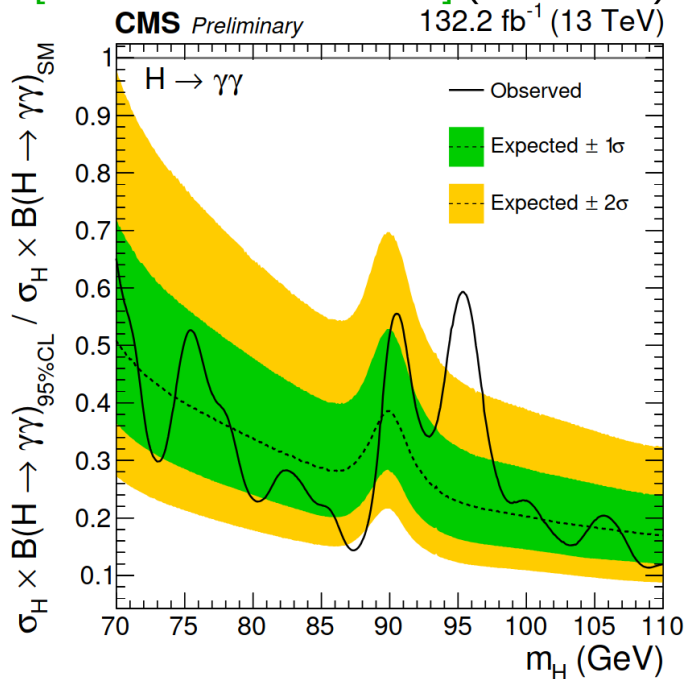
Table 1: Maximal values of  $m_A$  allowed in the benchmark scenario under the constraint of perturbative unitarity, at LO and NLO, and for different upper bounds on the  $2 \rightarrow 2$  scattering eigenvalues used in the perturbative unitarity constraint. Note that tree-level scattering eigenvalues are all real, so there is no difference between using  $\max$  or  $\Re(\max)$  for the left column.

# LHC excesses

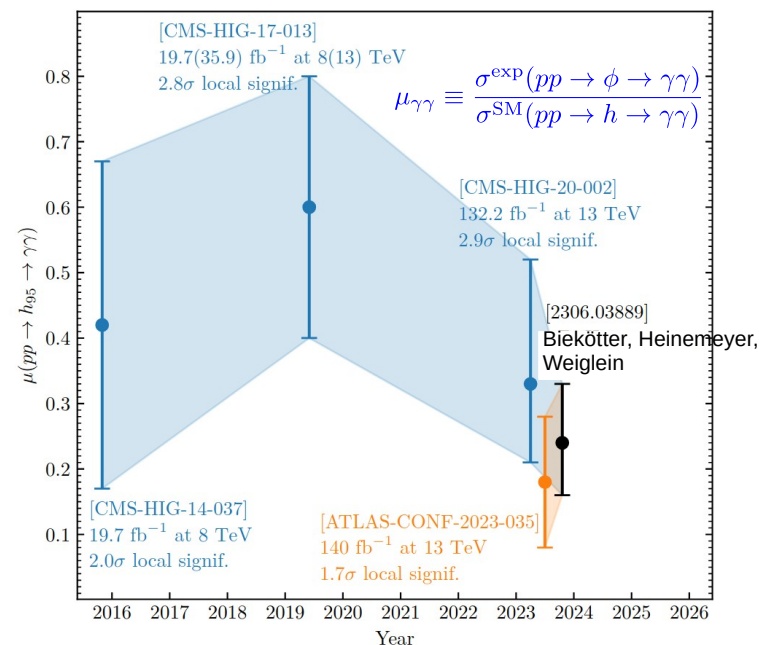
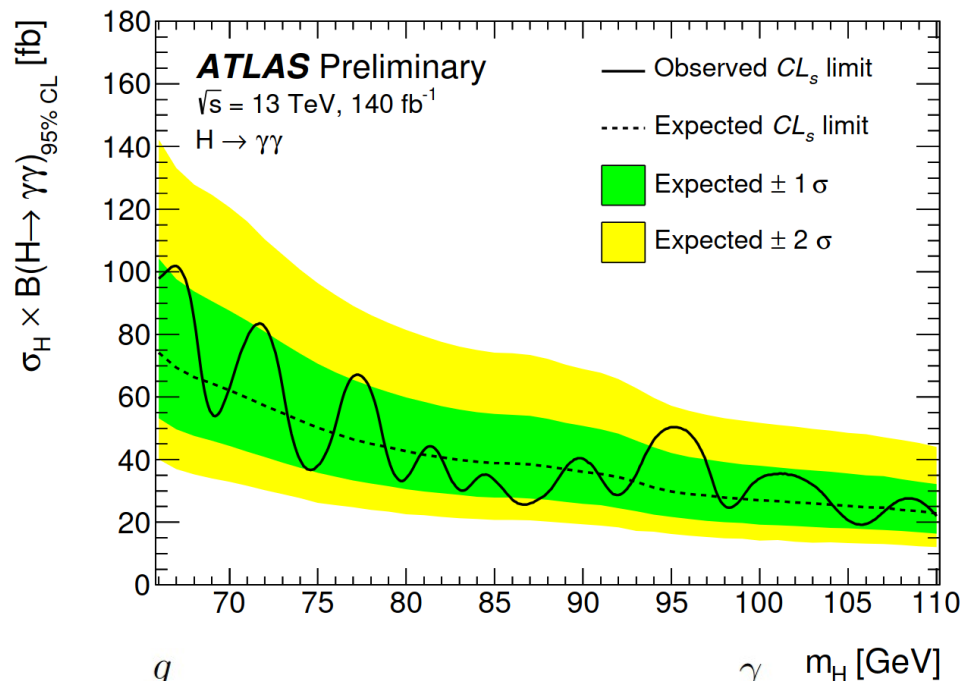
# A Higgs boson at 95 GeV?

- Excesses at 95 GeV in ATLAS and CMS low mass searches for  $\Phi \rightarrow \gamma\gamma$

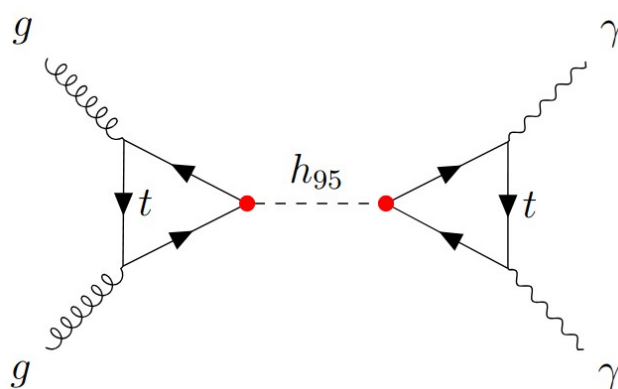
[CMS PAS HIG-20-002] ( $2.9\sigma$  local)



[ATLAS-CONF-2023-035] ( $1.7\sigma$  local)

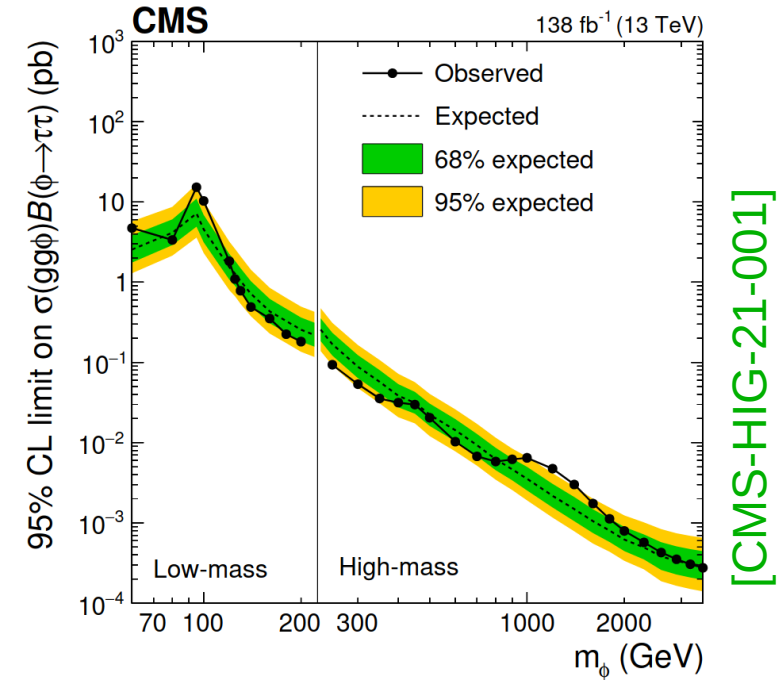
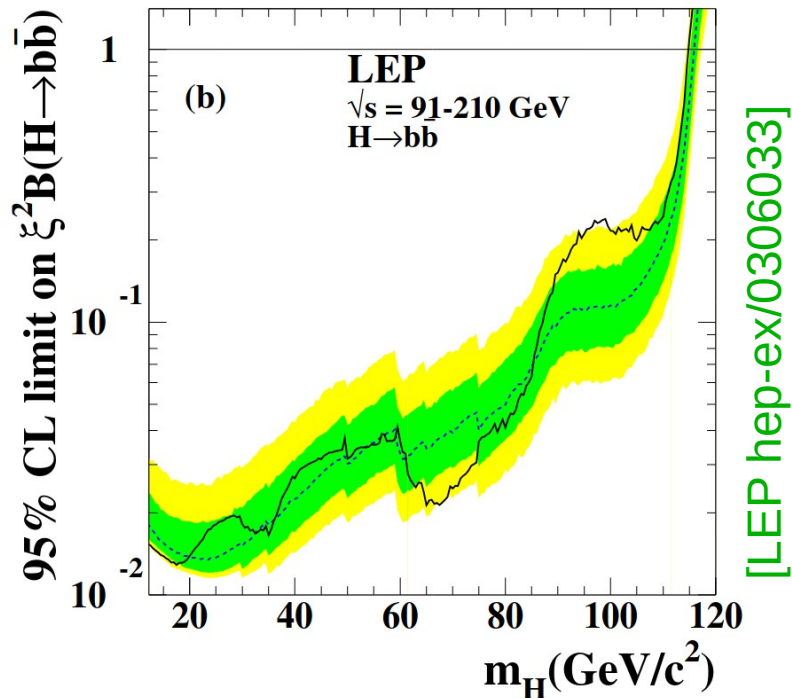
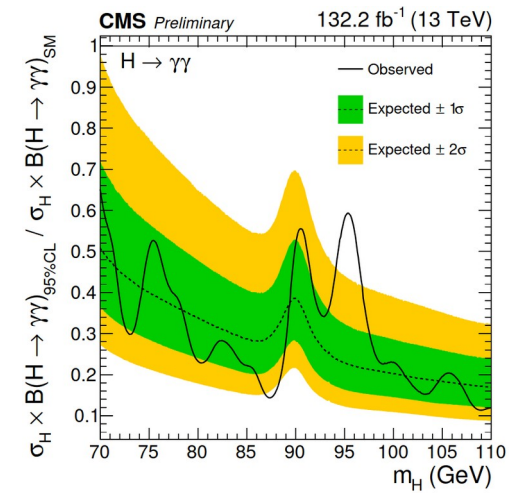


[Biekötter '24]



# A Higgs boson at 95 GeV?

- Excesses at 95 GeV in ATLAS and CMS low mass searches for  $\Phi \rightarrow \gamma\gamma$
- Could correspond to LEP data in  $\Phi \rightarrow b\bar{b}$  (but debated, see [Janot '24])
- CMS also found a broad excess (run 2) in  $\Phi \rightarrow \tau^+\tau^-$ , around 95-100 GeV  
However, only observed in ggF, and not in other production modes, in particular tth (although it should have); also no corresponding ATLAS run 2 result so far





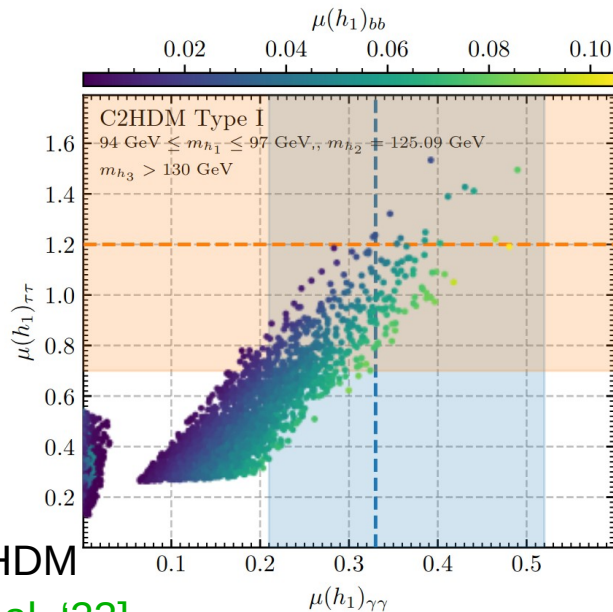
# A Higgs boson at 95 GeV? – a few possible interpretations

➤ Main classes of models accommodating  $h_{95}$ :

1)  $h_{95}$  belongs to an  $SU(2)_L$  multiplet, e.g. 2HDM variants,  $Y=0$  triplet, etc.

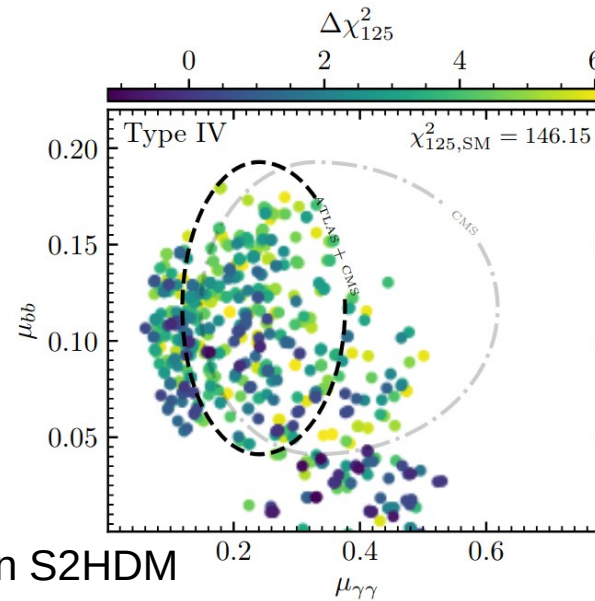
2)  $h_{95}$  comes from a singlet field mixing with  $h_{125}$   
e.g. N2HDM, S2HDM, NMSSM,  $\mu\nu$ SSM, etc.

3)  $h_{95}$  is singlet-like, but  $\mu(h_{95} \rightarrow \gamma\gamma)$  is explained by additional charged states, e.g. extended Georgi-Machacek model, etc.



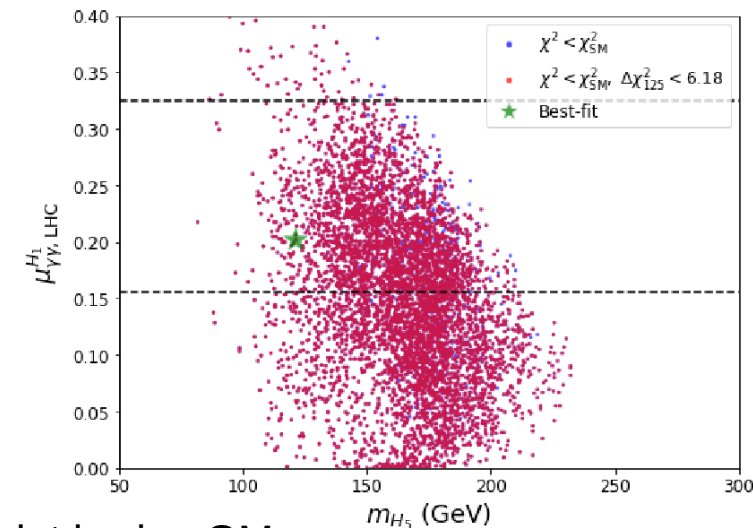
1)  $A_{95}$  in C2HDM

[Azevedo et al. '23]



2)  $h_{95}$  in S2HDM

[Biekötter et al. '23]



3) Singlet  $h_{95}$  in eGM

[Chen et al. '23]

# A Higgs boson at 95 GeV? – a few possible interpretations

➤ Main classes of models accommodating  $h_{95}$ :

1)  $h_{95}$  belongs to an  $SU(2)_L$  multiplet, e.g. 2HDM variants,  $Y=0$  triplet, etc.

2)  $h_{95}$  comes from a singlet field mixing with  $h_{125}$   
e.g. N2HDM, S2HDM, NMSSM,  $\mu\nu$ SSM, etc.

3)  $h_{95}$  is singlet-like, but  $\mu(h_{95} \rightarrow \gamma\gamma)$  is explained by additional charged states, e.g. extended Georgi-Machacek model, etc.

## *What next?*

→ wait for ATLAS  $\Phi \rightarrow \tau^+\tau^-$  run 2 results, and ATLAS and CMS run 3 results

→ look for additional states (e.g.  $H^\pm$ ,  $H^{\pm\pm}$ , ...) of models explaining  $h_{95}$  – directly, via effects on properties of  $h_{125}$  (like  $h_{125} \rightarrow \gamma\gamma$ ), or via mixing effects

# Excesses in soft-lepton and monojet searches

