Single top at LC after the Tevatron/LHC

Edward Boos

Theoretical and Experimental High Energy Physics Divisions Skobeltsyn Institute of Nuclear Physics, Lomonosov Moscow State University

Outline

- Why single top is interesting?
- Single top production at the Tevatron and at the LHC
- Single top at LC
- Spin correlations in single top
- BSM in single top (few examples)
- Concluding remarks

At hadron colliders top quarks may be produced either in pairs or singly

Two mechanisms of top pair production:



Top pair production and top-W-b coupling in decay

Single top electroweak top-W-b coupling in production

Three mechanisms of single top production:



Why Single top is interesting?

- Independent electroweak channel of the top quark production
- Direct |Vtb| CKM matrix element measurement
- Significant background to Higgs and many "new physics" (MSSM) processes
- Unique spin correlation properties
- Process of interest for "New physics"
 - Wtb anomalous couplings
 - FCNC

- ...

- Searches for W' (e.g. Kaluza-Klein excitation of W-boson)
- Searches for new strong dynamics (π_T , ho_T , vector-like top parner)

Top quark pair production cross sections NLO + NLL resummation		
Tevatron, 1.96 TeV: σ= 7.1 ± 0.5 pb		
LHC, 7 TeV: σ= 163 ± 11 pb 14 TeV: σ= 920 ± 60 pb	Kide	onakis
Single top quark production cross sections NLO + NLL resummation		
Tevatron, 1.96 TeV: s-channel σ= 0.88 ± 0.11 pb t-channel σ= 1.98 ± 0.25 pb	3 pb	Sullivan
LHC, 7 TeV: t-channel σ = 64.3 ± 3.1 pb s-channel σ = 4.6 ± 0.2 pb tW-channel σ = 15.6 ± 1.1 pb	89 pb	Kidonakis
LHC, 14 TeV: t-channel σ = 243 ± 6 pb s-channel σ = 11.9 ± 0.5 pb tW-channel σ = 84 ± 6 pb	339 pb	

Single top rate is about ~40% of the top pair rate

Computations and MC Tools: Dicus, Willenbrock, Smith, Yuan, Pittau, Cortese, Petronzio, Jikia, Slabospitsky, R-K Ellis, Parke, Mahlon, Kane, Ladinsky, , Heinson, Belyaev, Boos, Dudko, Ohl, Stelzer, Tait, Cao, Wudka, Berger, Sullivan, Weinzierl, Harris, Laenen, Phaf, Sherstnev, Bunichev, Schwienhorst, Frixione, Motylinski, Webber, Benitez, Brock, Beccaria, Macorini, Renard, Verzegnassi, Hollik, Campbell, Nason, Oleari, Alioli, Re....

Single top was observed by the Tevatron collaborations at 5 sigma level using multivariate methods (boosted decision tree, NN...)



Theory (NLO) : $\sigma = 2.9 \pm 0.3$ pb



Discriminant	Expected	Observed
	cross section	cross section
tb	$1.12^{+0.45}_{-0.43}$ pb	$0.68^{+0.38}_{-0.35} \text{ pb}$
tqb	$2.43^{+0.67}_{-0.61}$ pb	$2.86^{+0.69}_{-0.63}$ pb
tb + tqb	$3.49^{+0.77}_{-0.71}$ pb	$3.43^{+0.73}_{-0.74}$ pb

Single top has been observed at the LHC





 $\sigma = 83.6 \pm 29.8 \text{ (stat. + syst.)} \pm 3.3 \text{ (lumi.) pb}$ $|V_{tb}| = \sqrt{\frac{\sigma^{exp}}{\sigma^{th}}} = 1.16 \pm 0.22(exp) \pm 0.02(th)$

Theory (NLO) :
$$\sigma = 64.3 \pm 3.1 \text{ pb}$$

$$= 90^{+9}_{-9}(\text{stat}) + 31_{-20}(\text{syst}) = 90^{+32}_{-22} \text{ pb}$$

 $\begin{array}{l} \text{ATLAS (0.7 fb}^{-1} \text{)} \\ \sigma(pp \to Wt + X) = 14.4^{+5.3}_{-5.1}(\text{stat})^{+9.7}_{-9.4}(\text{syst}) \text{ pb} \\ \sigma(pp \to Wt + X) < 39.1 \text{ pb} \end{array} \qquad \begin{array}{l} \sigma_{\text{tW}} = 22^{+9}_{-7} \text{pb} \\ \sigma_{\text{tW}} = 22^{-9}_{-7} \text{pb} \end{array}$

Boos, Sachwitz, Schreiber, Shichanin

Top pair and single top in e^+e^- collisions (ILC) - both electroweak

 $e^+e^- \rightarrow t\bar{t} \rightarrow WWb\bar{b}, \qquad W \rightarrow f\bar{f}',$ where e.g. for W^+ $f = u, c, \nu_e, \nu_\mu, \nu_\tau \nu_\mu; f' = d, s, e, \mu, \tau$ $e^-e^+ \rightarrow \nu_e e t b$

Gauge invariant s-channel subset of 10 diagrams



One should substract top pair from the total contribution in the s-channel subset $\sigma_{singletop} = \int dM_{e\nu b} \left(d\sigma^{CTL} / dM_{e\nu b} - d\sigma^{BW} / dM_{e\nu b} \right)$ CTL - complete tree-level contribution; BW - Breit-Wigner contribution Gauge invariant t-channel subset of 10 diagrams





 $e \xrightarrow{\gamma, Z} e$ $b \xrightarrow{\overline{b}} t$ $e \xrightarrow{W^+} \overline{\nu}_e$



diagr.1,2

diagr.3,4

diagr.5,6



diagr.10

All the diagrams contribute to Single Top (at LEP2 the rate is too small, about 10^{-5} pb) Hagiwara, Tanaka M, Stelzer; Boos, Sachwitz, Schreiber, Shichanin, Ilyin, Pukhov,

Ishikawa, Kaneko, Kawabata, Kurihara, Shimizu, Tanaka H

(SM single top cross section is less than 1 fb at HERA) Stelzer, Sullivan, Willenbrock

In case of $\gamma\gamma$ collisions there are no nontrivial gauge invariant subsets. A situation is similar to single top at the LHC in Wt mode. Boos, Ohl



The top pair rate has to be removed in order to get the correct single top rate. Single Top Diagrams in γe Collisions



This is one of so called "gold plated" processes in γe collision mode of ILC

Cross sections of Top production processes at LC



Cross sections of Single top production for polarized collisions



NLO corrections are available for ye and e+e-



$\left|V_{tb}\right|$ measurements

If CKM unitarity and 3 generations are assumed $|V_{tb}| = 0.9991^{+0.000034}_{-0.00004}$

Without the 3-generation unitarity constrain $\left|Vtb\right|$ is left practically unconstrained

|Vtb| = 0.07 - 0.9993

From top quark loop contributions to $\Gamma(Z \to b\bar{b})$ $|V_{tb}| = 0.77^{+0.18}_{-0.24}$

From measurements of $R = \frac{|V_{tb}|^2}{|V_{tb}|^2 + |V_{ts}|^2 + |V_{td}|^2}$ by D0 and CDF analysing top pair production $R = 1.03^{+0.19}_{-0.17} => |V_{tb}| > 0.78$

Measurements from the single top: Production*Decays => $|V_{tb}|^2 \frac{|V_{tb}|^2}{|V_{tb}|^2 + |V_{ts}|^2 + |V_{td}|^2 + (Exotics)}$ Assumptions (no 3-generation unitarity constrain):

- * V-A interaction
- * $|V_{tb}|^2 >> |V_{ts}|^2 + |V_{td}|^2 + (Exotics)$

Direct measurements from single top



Spin correlations in single top



 $d\Gamma \sim |\mathcal{M}|^2 \sim (t+ms) \cdot \ell b \cdot \nu$



where in the top-quark rest frame, the spin four-vectors = $(0, \hat{s})$ is a unity \hat{s} vector that defines the spin quantization axis of the top quark. In the top quark rest frame: $\frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta_{\ell}} = \frac{1}{2} (1 + \cos\theta_{\ell})$

Hence the charged lepton tends to point along the direction of top spin

Single top production as top decay back in time

Mahlon, Parke; Boos, Sherstnev







Best spin correlation variable – the angle between the lepton from W-decay and momentum of outgoing light jet in the top-quark rest frame. Polarization

$$\frac{1}{\sigma} \frac{d\sigma}{d\cos\theta^*_{al}} = \frac{1 + P\cos\theta^*_{ql}}{2} \qquad P_{top} \approx 90 \,\%$$



Spin correlations in tW-mode

Boos, Sherstnev





$$M_{gtt}(-,t \to be^{+}\nu + g)|^{2} = \frac{2 g_{s}^{2} g_{W}^{2} |V_{tb}|^{2}}{(w^{2} - m_{W}^{2})^{2} + (m_{W}\Gamma_{W})^{2}} \frac{1}{(t \cdot g)^{2}} (b \cdot \nu) \left[m_{t} E_{e}^{*} E_{g}^{*2} (1 - \bar{n_{e}^{*}} \bar{n_{g}^{*}})^{2}\right]$$



$$X_{g,e^-} = E_g^* (1 - \cos \theta_{e^-,g}^*)$$

 $X_{g,e^-} < 110 \text{ GeV}$

Spin correlations in e-gamma collisions





 γ

$$\frac{1}{\sigma} \frac{d\sigma}{d\cos\theta_{e,\mu}^*} = \frac{1 + P\cos\theta_{e,\mu}^*}{2}$$

Charged Higgs in Top Decay (impact of tau polarization)



In the rest frame of top $t \to bR \to b\tau\nu_{\tau} \to b\nu_{\tau}\bar{\nu}_{\tau}\pi$ where a resonance R is W boson or charged H

$$\begin{split} \frac{1}{\Gamma} \frac{d\Gamma}{dy_{\pi}} &= \frac{1}{x_{max} - x_{min}} \\ \begin{cases} (1 - P_{\tau}) log \frac{x_{max}}{x_{min}} + 2P_{\tau} y_{\pi} (\frac{1}{x_{min}} - \frac{1}{x_{max}}), & 0 < y_{\pi} < x_{min} \\ (1 - P_{\tau}) log \frac{x_{max}}{y_{\pi}} + 2P_{\tau} (1 - \frac{y_{\pi}}{x_{max}}), & x_{min} < y_{\pi} \end{cases} \\ \text{where } y_{\pi} &= \frac{E_{\pi}^{top}}{M_{top}}, \quad x_{min} = \frac{E_{\pi}^{min}}{M_{top}}, \quad x_{max} = \frac{E_{\pi}^{max}}{M_{top}}, \quad E_{\tau}^{min} = \frac{M_{R}^{2}}{2M_{top}}, \quad E_{\tau}^{max} = \frac{M_{top}}{2} \\ P_{\tau} &= -1 \text{ for W boson and } P_{\tau} = 1 \text{ for charged Higgs} \end{split}$$

140

M_{H⁺} [GeV]

160

(M.Nojiri; E.B., G.Moortgat-Pick, M.Sachwitz, A.Sherstnev, P.Zerwas; E.B., S.Bunichev, M.Carena, C.Wagner)

One can explore both top and tau polarization informations

Boos, Bunichev



Two possibilities in general

Collision energy E < production thresholds

⇒New effective anomalous interactions of the top with other SM particles (modification of top decay and production properties)

Collision energy E > production thresholds

⇒New resonances decaying to tops ⇒New states produced in association with the top

FCNC couplings

• Couplings: tqg, $tq\gamma$, tqZ, where q = u, c

$$\Delta \mathcal{L}^{eff} = \frac{1}{\Lambda} \left[\kappa_{tq}^{\gamma,Z} e \bar{t} \sigma_{\mu\nu} q F^{\mu\nu}_{\gamma,Z} + \kappa_{tq}^g g_s \bar{t} \sigma_{\mu\nu} \frac{\lambda^i}{2} q G^{i\mu\nu} \right] + h.c.$$



To compare FCNC limits from top decays and top production one can express limits on FCNC couplings in term of Br fractions

$$\begin{split} \Gamma(t \to qg) &= \left(\frac{\kappa_{tq}^g}{\Lambda}\right)^2 \frac{8}{3} \alpha_s m_t^3 \quad , \quad \Gamma(t \to q\gamma) = \left(\frac{\kappa_{tq}^\gamma}{\Lambda}\right)^2 2\alpha m_t^3, \\ \Gamma(t \to qZ)_\gamma &= \left(|v_{tq}^Z|^2 + |a_{tq}^Z|^2\right) \alpha m_t^3 \frac{1}{4M_Z^2 \sin^2 2\theta_W} \left(1 - \frac{M_Z^2}{m_t^2}\right)^2 \left(1 + 2\frac{M_Z^2}{m_t^2}\right), \\ \Gamma(t \to qZ)_\sigma &= \left(\frac{\kappa_{tq}^Z}{\Lambda}\right)^2 \alpha m_t^3 \frac{1}{\sin^2 2\theta_W} \left(1 - \frac{M_Z^2}{m_t^2}\right)^2 \left(2 + \frac{M_Z^2}{m_t^2}\right) \end{split}$$

D0:

CDF:

	tgu	tgc
Cross section	0.20 pb	$0.27~{ m pb}$
κ_{tgf}/Λ	$0.013 { m ~TeV^{-1}}$	$0.057 { m ~TeV^{-1}}$
$\mathcal{B}(t \to qg)$	2.0×10^{-4}	3.9×10^{-3}

$$\mathcal{B}(t \to u + g) < 3.9 \cdot 10^{-4}$$
$$\mathcal{B}(t \to c + g) < 5.7 \cdot 10^{-3}$$

LHC: $B(t - > gq) < 1 \times 10^{-5}$



A total luminosity of 40 fb-1 would be enough to overcame the LHC 100 fb-1 bound almost independently of the collider center of mass energy.

Structure of the Wtb vertex

$$\Gamma^{\mu}_{Wtb} = -\frac{g}{\sqrt{2}} \underbrace{V_{tb}}_{tb} \left\{ \gamma^{\mu} \left[f_1^L P_L + f_1^R P_R \right] - \frac{i\sigma^{\mu\nu}}{M_W} \left(p_t - p_b \right)_{\nu} \left[f_2^L P_L + f_2^R P_R \right] \right\}$$

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & \mathbf{V_{tb}} \end{pmatrix}$$

B CM:
$$f_1^L = 1$$
, $f_1^R = 0$, $f_2^{L,R} = 0$

Expectations for Wtb anomalous couplings for the Tevatron and LHC



DO limits based on 900 pb⁻¹ data

Scenario	Cross Section	Coupling
(L_1,L_2)	$4.4^{+2.3}_{-2.5} \text{ pb}$	$ V_{tb}f_1^L ^2 = 1.4^{+0.6}_{-0.5}$
		$ V_{tb}f_2^L ^2 < 0.5 \text{ at } 95\% \text{ C.L.}$
(L_1,R_1)	$5.2^{+2.6}_{-3.5}$ pb	$ V_{tb}f_1^L ^2 = 1.8^{+1.0}_{-1.3}$
		$ V_{tb}f_1^R ^2 < 2.5 \text{ at } 95\% \text{ C.L.}$
(L_1, R_2)	$4.5^{+2.2}_{-2.2} \text{ pb}$	$ V_{tb}f_1^L ^2 = 1.4^{+0.9}_{-0.8}$
		$ V_{tb}f_2^R ^2 < 0.3$ at 95% C.L.

The total integrated luminosity was assumed to be 500 fb⁻¹ for e^+e^- collisions and 250 fb⁻¹ and 500 fb⁻¹ for γe collisions at 500 GeV and 2 TeV, respectively.

Boos, Pukhov, Sachwitz, Schreiber

	$ V_{tb} \cdot f_{R_T} $	$ V_{tb} \cdot f_{L_T} $
Tevatron ($\Delta_{sys.} \approx 10\%$)	$-0.18 \div +0.55$	$-0.24 \div +0.25$
LHC ($\Delta_{sys.} \approx 5\%$)	$-0.052 \div +0.097$	$-0.12 \div +0.13$
$e^+e^- (\sqrt{s_{e^+e^-}} = 0.5 \text{ TeV})$	$-0.025 \div +0.025$	$-0.2 \div +0.2$
$\gamma e \left(\sqrt{s_{e^+e^-}} = 0.5 \text{ TeV} \right)$	$-0.045 \div +0.045$	$-0.045 \div +0.045$
$\gamma e \ (\sqrt{s_{e^+e^-}} = 2.0 \text{ TeV})$	$-0.008 \div +0.035$	$-0.016 \div +0.016$

D0 bounds with 5.4 fb^{-1}

Scenario	Cross section	Coupling
$egin{aligned} (L_V,L_T)\ (L_V,R_V)\ (L_V,R_T) \end{aligned}$	< 1.21 pb < 2.81 pb < 0.60 pb	$ V_{tb} \cdot f_{L_T} ^2 < 0.13 V_{tb} \cdot f_{R_V} ^2 < 0.93 V_{tb} \cdot f_{R_T} ^2 < 0.06$



In case of LC W' would lead to effetive 4-fermion operator

Qing-Hong Cao and Jose Wudka

$$\mathcal{O}_{\ell q}^{(3)} = \frac{1}{2} \left(\bar{\ell} \gamma_{\mu} \tau^{I} \ell \right) \left(\bar{q} \gamma^{\mu} \tau^{I} q \right) \qquad \mathcal{G}_{4f} = C_{\ell q}^{(3)} / 2$$
$$\mathcal{L}_{4f} = \frac{\mathcal{G}_{4f}}{\Lambda^{2}} \left\{ \left(\bar{\nu} \gamma^{\mu} P_{L} e \right) \left(\bar{b} \gamma_{\mu} P_{L} t \right) + \left(\bar{e} \gamma^{\mu} P_{L} \nu \right) \left(\bar{t} \gamma_{\mu} P_{L} b \right) \right\}$$

$$\mathcal{O}_{\phi q}^{(3)} = i \left(\phi^{\dagger} \tau^{I} D_{\mu} \phi \right) \left(\bar{q} \gamma^{\mu} \tau^{I} q \right) + \text{H.c.}, \qquad \mathcal{L}_{Wtb}^{(\text{dim}-6)} = \frac{g}{\sqrt{2}} \left\{ \bar{t} \gamma^{\mu} \left(\mathcal{F}_{L} P_{L} + \mathcal{F}_{R} P_{R} \right) b W_{\mu}^{+} + \text{H.c.} \right\}$$
$$\mathcal{O}_{\phi \phi} = i \left(\phi^{\dagger} \epsilon D_{\mu} \phi \right) \left(\bar{t} \gamma^{\mu} b \right) + \text{H.c.}, \qquad \qquad \mathcal{F}_{L} = \frac{C_{\phi q}^{(3)} v^{2}}{\Lambda^{2}}, \qquad \mathcal{F}_{R} = \frac{C_{\phi \phi} v^{2}}{2\Lambda^{2}},$$



Concluding remarks

Single top quark production has been observed by the Tevatron and the LHC experiments (not yet in all expected production modes, tW at the Tevatron and s-channel at the LHC).

Several precision measurements (Wtb, FCNC tqg, W') have been made at the Tevatron and corresponding limits have been obtained. Stronger limits are expected from the LHC.

Single top at LC allows to improve an accuracy for direct measurements of Vtb CKM element, improve limits on anomalous Wtb and FCNC couplings...

Not all advantages of LC, especially polarization properties of colliding and produced particles, have been fully explored yet. More realistic simulations are needed for more accurate predictions...

