Quantum (and classical) detection of gravitational waves: scope and limitations

Paolo Bilisco Quantum Universe Attract.Workshop DESY, Hamburg, Germany 25/11/2025

Based on: C. Beadle, PB, R.T. D'Agnolo, S.A.R. Ellis, arXiv:2512.XXXXX









Question (and conclusions)

Q: Will we ever be able to detect primordial-background gravitational-wave signals at very high frequencies?

Question (and conclusions)

Q: Will we ever be able to detect primordial-background gravitational-wave signals at very high frequencies?

A: Probably not. A shift in technology could be required.

Preceding work: Classical and quantum heuristics for gravitational-wave detection [S.A.R. Ellis, R.T. D'Agnolo, arXiv:2412.17897]

Question (and conclusions)

Q: Will we ever be able to detect primordial-background gravitational-wave signals at very high frequencies?

A: Probably not. A shift in technology could be required.

Preceding work: Classical and quantum heuristics for gravitational-wave detection [S.A.R. Ellis, R.T. D'Agnolo, arXiv:2412.17897]

Can we analytically confirm this statement, starting from an *ab initio* computation in quantum mechanics and taking into account all form factors?

BSM signals and sources

• Which high frequencies?

Characteristic wavelength
$$\longrightarrow$$
 $\{\lambda_*\} \le H_*^{-1}$ (Process occurring at temperature T_*) $\omega_0 = a(t_*)/a(t_0)\,\omega_*$ (Redshift of gravitons)

Signal at GUT scale:

$$\omega_0 \gtrsim 100 \; \mathrm{MHz} \left(rac{T_*}{10^{15} \; \mathrm{GeV}}
ight) \left(rac{g_*(T_*)}{100}
ight)^{1/6}$$

What could have produced GW stochastic backgrounds?

Vacuum fluctuations, phase transitions, cosmic strings, domain walls,...

[M. Maggiore, Gravitational waves (Oxford University Press, 2007); Aggarwal et al., Living Rev. Rel. 24, 4 (2021)]

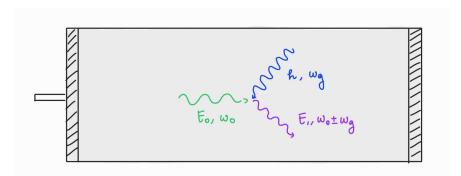
Main shortcoming: the minimal detectable strain

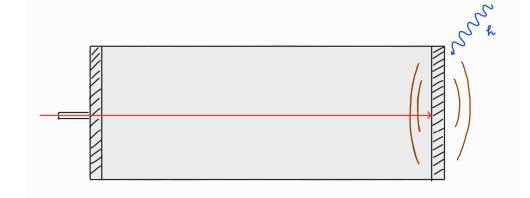
• The study of **cosmological stochastic backgrounds of GWs** can be performed by means of an *energy density* per unit logarithmic interval of frequency:

• Bound on minimal signal strength for detection of GWs coming from primordial backgrounds [M. Kawasaki *et al.*, Phys. Rev. Lett. 82, 4168 (1999) & Phys. Rev. D 62, 023506 (2000), M. Maggiore, *Physics Reports* 331 (2000), 283-367]

Reduced hubble parameter
$$\int d\log \omega \oint_{\text{eff}}^2 \Omega_g(\omega) \lesssim 5 \times 10^{-6} \Delta N_{\text{eff}} \longleftarrow \text{number of neutrino species}$$

Two toy models to describe (almost) any detector





EM resonators

- Large static magnetic field
- Readout: $\omega_1 \approx \omega_g$
- MADMAX [arXiv:2409.06462], CAST [arXiv:1705.02290], IAXO [Eur. Phys. J. C 79 (2019) 1032]
- Transition mode
 0 (loaded) → 1 (readout)
- Readout: $\omega_1 = \omega_0 \pm \omega_g$
 - MAGO [*Phys. Rev. D* **108** (2023) 084058]

Resonant EM microwave cavities [Physical Review D 105 116011 (2022)], Lumped LC resonators [Phys. Rev. Lett. 129 (2022) 041101]

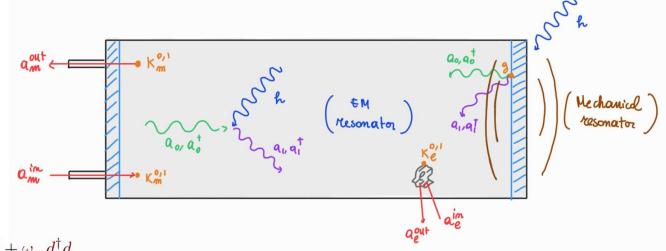
Mechanical resonators

- Like test masses. Their position is measured through an **EM readout**
- Interferometers (LVK, Holometer), Optomechanical sensors (levitating sphere [A. Arvanitaki, A. A. Gercai, *Phys. Rev. Lett.* 110 (2013) 071105]), Weber bars (AURIGA [M. Cerdonio *et al.*, Classical and Quantum Gravity 14 (1997) 1491]), Magnetic Weber bars [V. Domcke, S.A.R. Ellis, N. L. Rodd, *Phys. Rev. Lett.* 134, 231401]

Quantum mechanical set-up

Prototypical system

$$H(t) = H_0(t) + H_{G+OM}(t) + H_R(t)$$



Free
$$H_0(t) = \sum_{n,r} \Delta_n a_{n,r}^{\dagger} a_{n,r} + \int_V d^3x |B_0|^2 + \omega_m d^{\dagger} d$$

Int.
$$H_{G+OM}(t) = \int_{V} \mathrm{d}^3x h_{\mu\nu} T^{\mu\nu} + gx X_1 = h(t) \left\{ \sum_{jj'} C_{jj'} a_j^{\dagger}(t) a_{j'}(t) + \sum_{j} \left[D_j a_j(t) + D_j^* a_j^{\dagger}(t) \right] \right\} + \underbrace{gx X_1} \longleftarrow \text{Back-action}$$

Procedure

• Input-output formalism [Beckey et al., arXiv:2311.07270] $X_n = \frac{a_n + a_n^{\dagger}}{\sqrt{2}}, \quad Y_n = -\frac{i(a_n - a_n^{\dagger})}{\sqrt{2}}$

$$X_n = \frac{a_n + a_n^{\dagger}}{\sqrt{2}}, \quad Y_n = -\frac{i(a_n - a_n^{\dagger})}{\sqrt{2}}$$

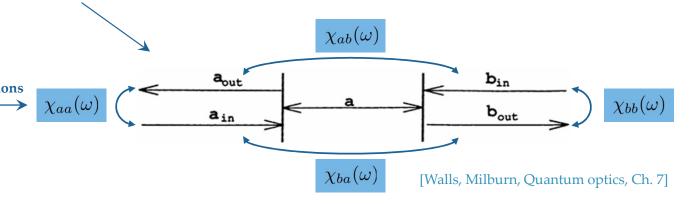
• EoMs

$$\begin{cases} \dot{X}_n(t) = \Delta_n Y_n(t) \mp \frac{1}{2} \sum_k \tilde{k}_j^n X_j(t) + \sum_{\Lambda} \sqrt{\kappa_{\Lambda}^n} X_{\Lambda}^{\frac{\mathrm{in}}{\mathrm{out}}}(t) + F_X^n(t) \\ \dot{Y}_n(t) = -\Delta_n X_n(t) \mp \frac{1}{2} \sum_k \tilde{k}_j^n Y_j(t) + \sum_{\Lambda} \sqrt{\kappa_{\Lambda}^n} Y_{\Lambda}^{\frac{\mathrm{in}}{\mathrm{out}}}(t) + F_Y^n(t) \\ \dot{x}(t) = \frac{p(t)}{M} \\ \dot{p}(t) = -M\omega_m^2 x(t) - \gamma_m p(t) - gX_1(t) + F_m(t) \end{cases}$$

$$\text{Mech.}$$

Input-output relations

$$\begin{cases} X_{\Lambda}^{\mathrm{out}} = X_{m}^{\mathrm{in}} - \sum_{j} \sqrt{\kappa_{\Lambda}^{j}} X_{j} \\ Y_{\Lambda}^{\mathrm{out}} = Y_{m}^{\mathrm{in}} - \sum_{j} \sqrt{\kappa_{\Lambda}^{j}} Y_{j} \end{cases} \xrightarrow{\text{Transfer functions}}$$



Power Spectral Density and Minimal Detectable Strain

• Power Spectral Density:
$$\langle A(t)B^{\dagger}(t')\rangle = \int_{-\infty}^{\infty} \frac{\mathrm{d}\omega}{2\pi} e^{i\omega(t-t')} S_{AB}(\omega)$$

Quadrature PSD:

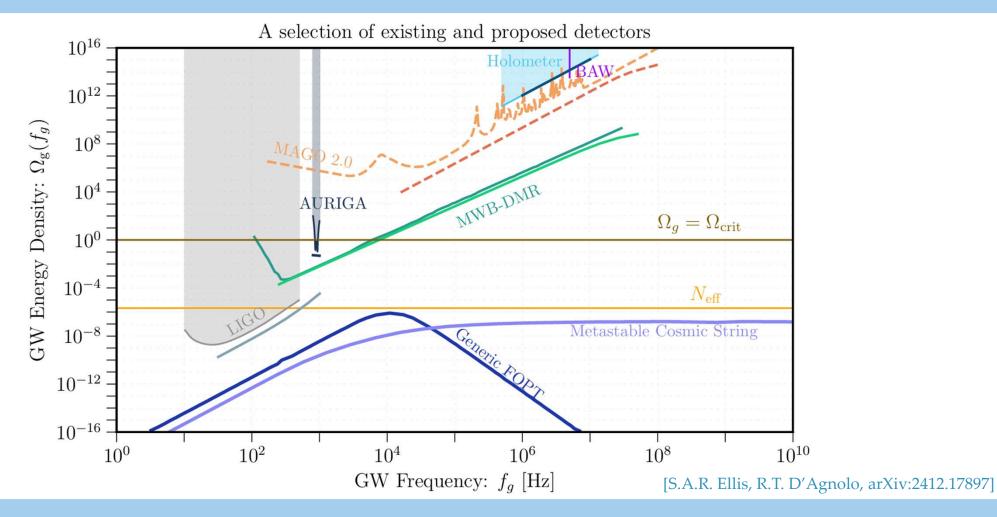
$$S_{Y_{m}Y_{m}}^{\text{out}}(\omega) = \sum_{\Lambda} \left[|\chi_{Y_{m}Y_{\Lambda}}(\omega)|^{2} S_{Y_{\Lambda}Y_{\Lambda}}^{\text{in}}(\omega) + |\chi_{Y_{m}X_{\Lambda}}(\omega)|^{2} S_{X_{\Lambda}X_{\Lambda}}^{\text{in}}(\omega) \right] \\ + \sum_{\Lambda} \left[\chi_{Y_{m}X_{\Lambda}}(\omega) \chi_{Y_{m}Y_{\Lambda}}(\omega)^{*} S_{Y_{\Lambda}X_{\Lambda}}^{\text{in}}(\omega) + \chi_{Y_{m}Y_{\Lambda}}(\omega) \chi_{Y_{m}X_{\Lambda}}(\omega)^{*} S_{X_{\Lambda}Y_{\Lambda}}^{\text{in}}(\omega) \right] \\ + \sum_{I} |\chi_{Y_{m}F_{I}}(\omega)|^{2} S_{F_{I}F_{I}}(\omega) \supset S_{hh}(\omega)$$
Signal

h-PSD ↔ GW energy density

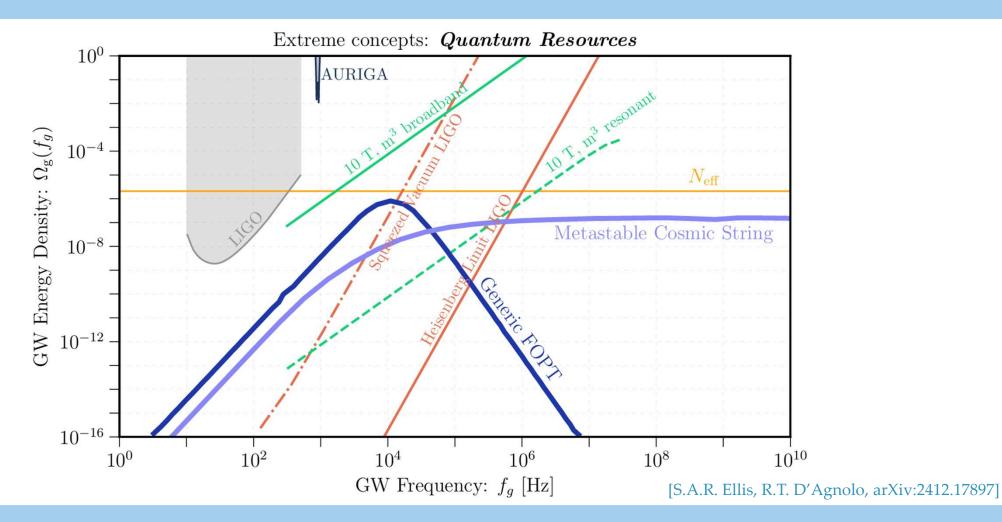
$$\Omega_g(\omega) = \frac{\omega^3 S_{hh}(\omega)}{3\pi H_0^2}$$
 SNR $\simeq 1$

$$\Omega_g(\omega) = \frac{\omega^3 S_{hh}(\omega)}{3\pi H_0^2} \xrightarrow{\text{SNR} \simeq 1} \left(\Omega_g(\omega)\right)_{\min} = \frac{\omega^3}{3\pi H_0^2} \left[t_{\text{int}} \int_{\omega - \Delta\omega/2}^{\omega + \Delta\omega/2} \frac{d\omega'}{2\pi} \left(\frac{|\chi_{Y_m h}(\omega')|^2}{S_{Y_m Y_m}^{\text{out}}(\omega')|_{\text{NOISE}}} \right)^2 \right]^{-\frac{1}{2}}$$

Classical heuristics



Quantum heuristics



Conclusions (again!) and outlook

- The novel analysis based on the input-output formalism is going to give **analytic bounds** (**including form factors**) on GW detection and accurately tell us what we can expect from present and near-future GW detectors
- However we expect the precise quantum computations to confirm the conclusions drawn from the heuristics

<u>Upshot</u>: High-frequency gravitational waves coming from primordial backgrounds might remain out of the experimental reach of current detectors