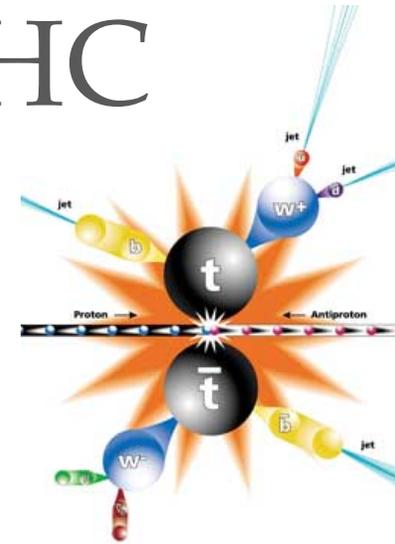


# Theoretical predictions for top anti-top production at NLO

Malgorzata Worek  
Wuppertal Uni.

# top anti-top at the LHC



- One of the first measurements carried out by LHC
- Produced predominantly through strong interactions
- Decays without forming hadrons via  $t \rightarrow W b$
- Distinguished by its large mass
- Is the top quark mass generated by the Higgs mechanism ?
- Does it play more fundamental role ?
  
- LHC tt factory! Large statistics -  $10^7$  tt pairs per year**
- Experimental uncertainty reached 6% (!) level**
  
- Tests of QCD, intrinsic properties of top and its EW interactions
- Accurate determination of  $\sigma_{tt}$  provides indirect determination of  $m_t$
- Anomalies in the total rate would indicate non-QCD production channels
- Must be confirmed by precise studies of the top quark distributions
- Distributions would be distorted by the presence of anomalous couplings or s-channel resonances expected in several BSM scenarios

# Why LO is not enough ?

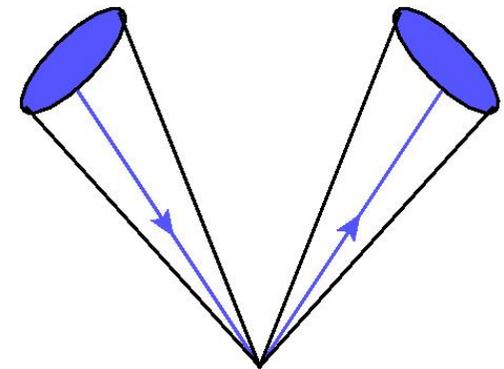
- ❑ Many partons in the final state, all off-shell effects, interferences, non-resonance contributions, full color information, spin correlations, etc.
- ❑ Standard Model and beyond tools

ALPGEN, COMPHEP, HELAC-PHEGAS, MADEVENT, SHERPA, WHIZARD, ...

- ❑ Predictions can be matched with General purpose Monte Carlo programs (parton shower, hadronization, multiple interactions, hadrons decays, etc.)

HERWIG, HERWIG++, PYTHIA 6.4, PYTHIA 8.1, SHERPA, ...

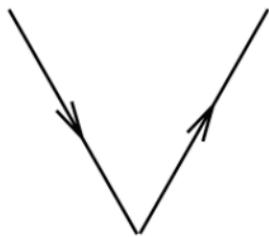
- ❑ High sensitivity to unphysical input scales
- ❑ Huge theoretical errors related to the scale dependence
- ❑ Very crude description of differential distributions
- ❑ Very simplified description of jets: parton = jet



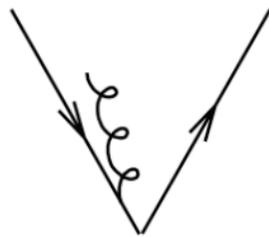
**JETS: LO**

# At least NLO QCD

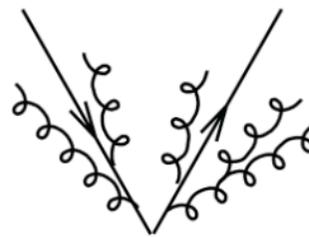
- ❑ Stabilizing the scale in the QCD input parameters:  $\alpha_s$  and PDFs
- ❑ More reliable theoretical error related to the scale dependence
- ❑ Normalization and shape of distributions first known at NLO
  
- ❑  $2 \rightarrow 4(5)$  processes are many scale processes:
  - ❖  $Z + 3j, ttH \rightarrow ttbb, ttbb, bbbb, 4j, W + 4j$
  - ❖ better understanding of how to choose scale
  - ❖ dynamic variables that depend on the event structure
  
- ❑ Improved description of jets



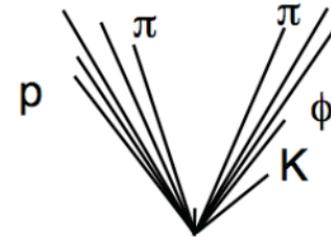
Jets: LO



NLO



Parton  
Shower



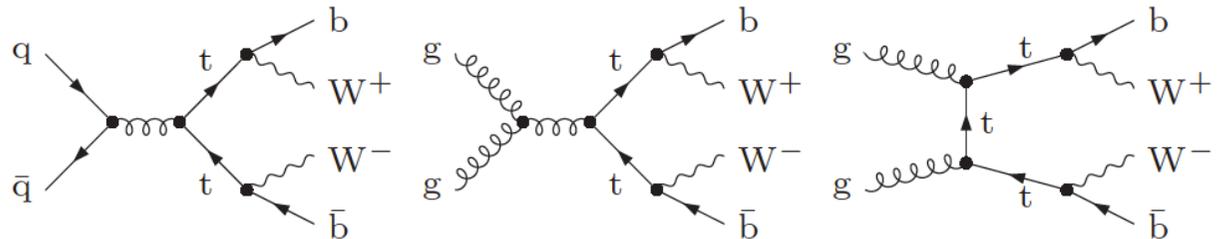
Hadron  
Level

The strongest argument in support of NLO calculations is their success in an accurate description of the LEP and TeVatron data !

# In this talk

- A good theoretical understanding of top pair production is crucial for many analyses at Tevatron and LHC
  - ❖ top a signal (precise measurement of top quark properties)
  - ❖ top a background in new physics searches (Higgs boson, BSM)
  
- Top pair phenomenology has been widely investigated since many years with impressive progress in several directions (NLO, NNLO, resummation...)
  
- In this talk: few (quite recent) selected topics which show current status of NLO predictions at the LHC and forward-backward asymmetry at the Tevatron for processes:

- ❖  $pp \rightarrow tt + X$
- ❖  $pp \rightarrow tt + 1 \text{ jet} + X$
- ❖  $pp \rightarrow tt + 2 \text{ jets} + X$



# top anti-top @ NLO QCD

- ❑ **Narrow-width approximation**
- ❑ NLO corrections to both production and decay, neglecting non-factorizable corrections, including spin correlations at NLO
  - ❖ Double differential angular distributions to probe spin correlations of top

*W. Bernreuther, A. Brandenburg, Z. G. Si and P. Uwer (2004)*
  - ❖ Flexible Monte Carlo implementation, fully differential level
  - ❖ Spin correlations of top anti-top via decay products
  - ❖  $pp \rightarrow tt + X \rightarrow WWbb + X \rightarrow lv lv bb + X$  (di-lepton)
  - ❖  $pp \rightarrow tt + X \rightarrow WWbb + X \rightarrow ud lv bb + X$  (lepton + jet)

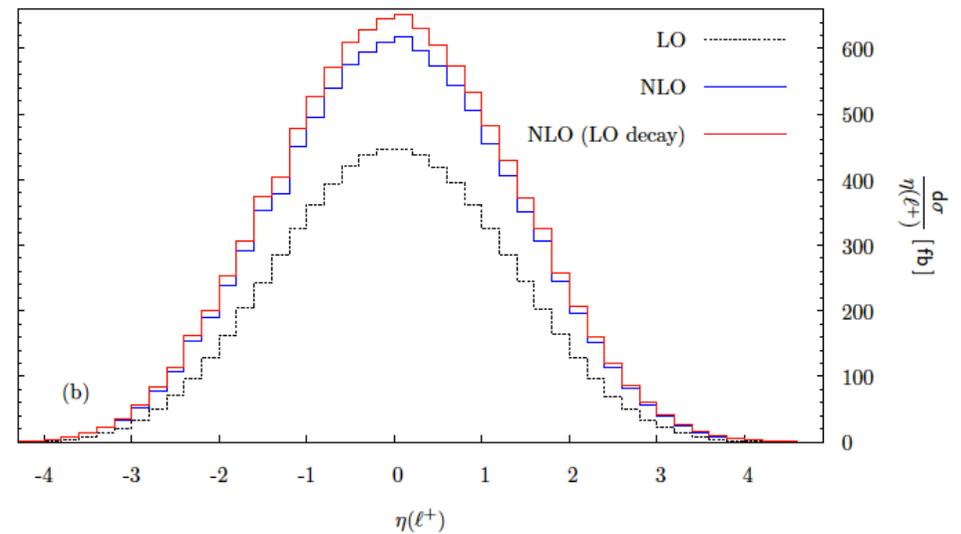
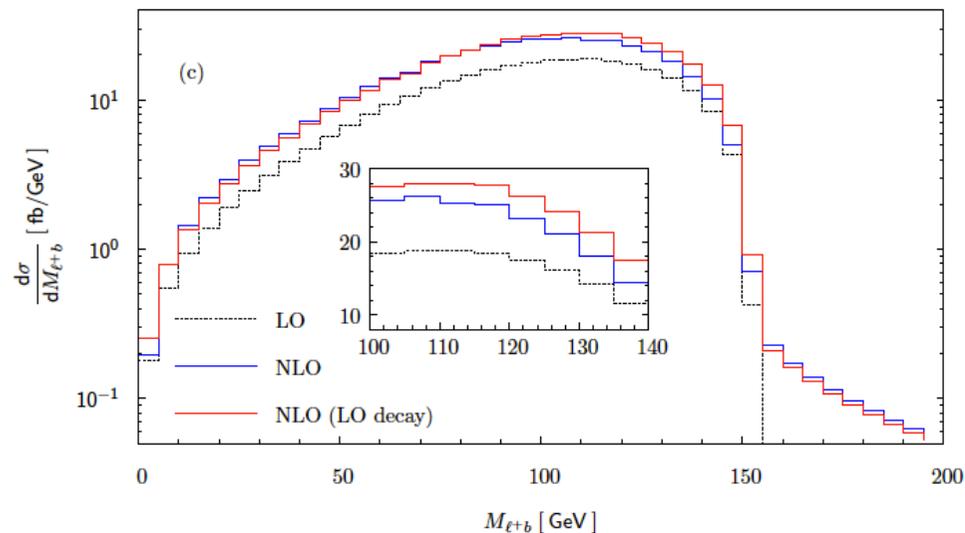
*K. Melnikov and M. Schulze (2009)*
- ❑ Results of NLO+PS matching available since quite some time
  - ❖ MC@NLO
  - ❖ POWHEG

*S. Frixione, P. Nason, B. R. Webber (2003)*  
*S. Frixione, P. Nason, G. Ridolfi (2007)*

# top anti-top @ NLO in NWA

- ❑ Predictions at LO and NLO with and without corrections to the decay
- ❑  $pp \rightarrow tt + X \rightarrow WWbb + X \rightarrow lv lv bb + X$

@ LHC 10 TeV



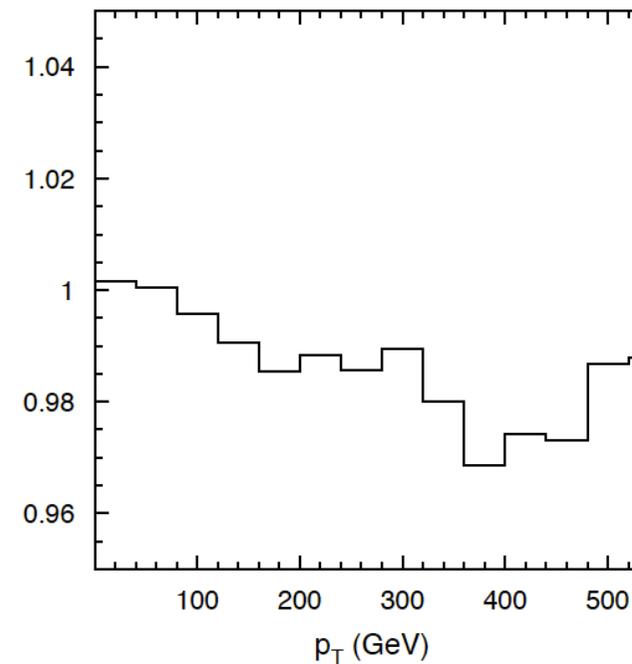
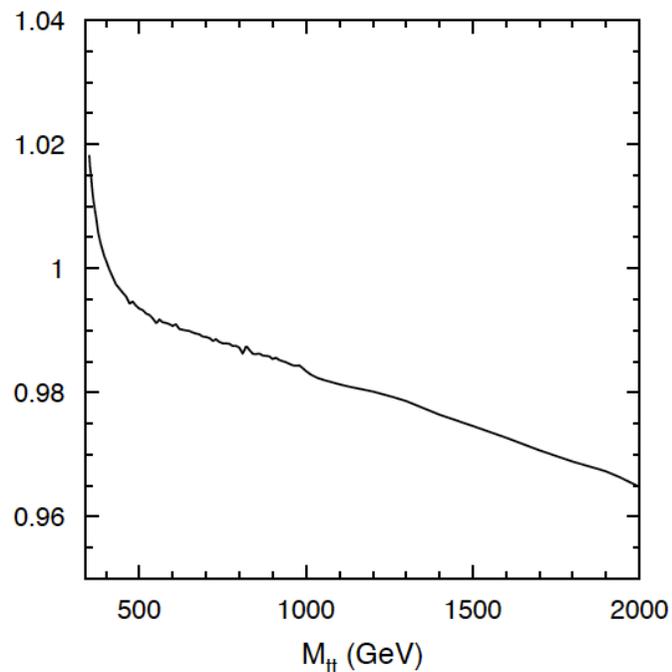
*K. Melnikov and M. Schulze (2009)*

# Mixed QCD-EW Corrections

- NLO order in the strong and weak gauge couplings (NLOW with NWA)
- The ratio of the distributions evaluated at NLOW and NLO:  $m_{tt}$  and  $p_T(t)$
- $pp \rightarrow tt + X \rightarrow WWbb + X \rightarrow lv lv bb + X$

*W. Bernreuther, Z. G. Si (2010)*

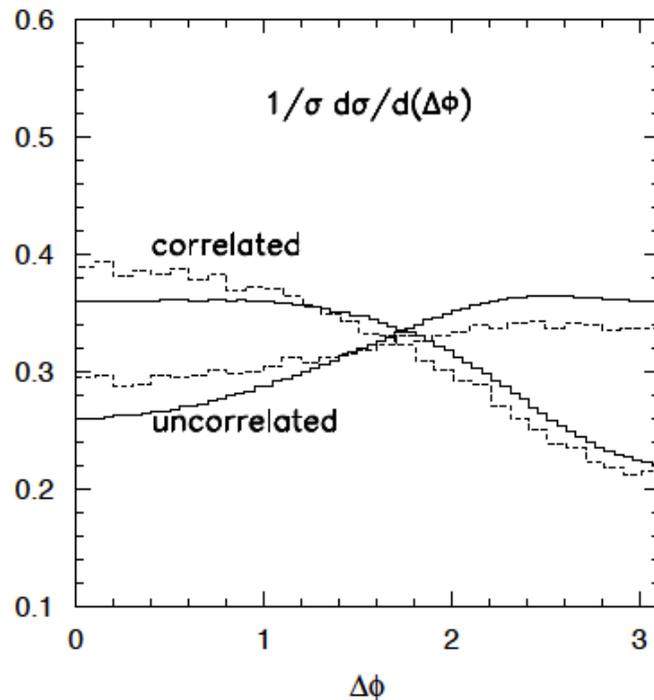
@ LHC 14 TeV



# Mixed QCD-EW Corrections

- NLO order in the strong and weak gauge couplings (NLOW), with NWA
- $pp \rightarrow tt + X \rightarrow WWbb + X \rightarrow lv lv bb + X$

*W. Bernreuther, Z. G. Si (2010)*



- Effect of top anti-top spin correlations
- Azimuthal angle distribution of two leptons
- With and without top anti-top spin correlations
- Solid line is LO
- Dashed line is NLOW

@ LHC 14 TeV

# Beyond NWA

- ❑ Complete NLO description of the production of top anti-top pairs including interferences, off-shell effects, and non-resonant backgrounds, spin correlations
- ❑ State of the art description of  $t\bar{t}$  process
- ❑ Two independent calculations with per-mille agreement

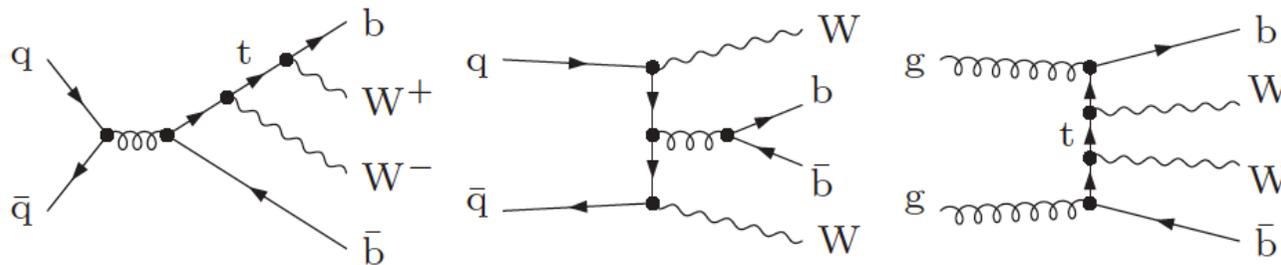
$$pp \rightarrow WWbb + X \rightarrow l\nu l\nu bb + X$$

*A. Denner, S. Dittmaier, S. Kallweit, S. Pozzorini (2011)*

$$pp \rightarrow l\nu l\nu bb + X$$

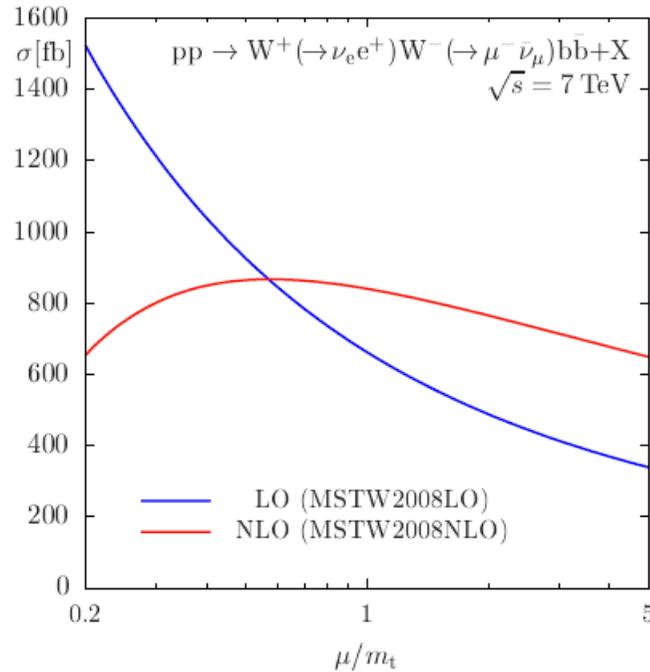
*G. Bevilacqua, M. Czakon, A. van Hameren, C. G. Papadopoulos, M. Worek (2011)*

Finite-width effects on  $\sigma_{t\bar{t}}$   
small, around 1%, both at  
the Tevatron and the LHC



# Beyond NWA

@ LHC 7 TeV & 10 TeV



NLO QCD Corrections

$$K = \text{NLO}/\text{LO} = \mathbf{1.47}$$

Scale dependence

LO 37%  $\rightarrow$  NLO 9%

Algorithm	$\sigma_{\text{LO}}$ [fb]	$\sigma_{\text{NLO}}^{\alpha_{\text{max}}=1}$ [fb]	$\sigma_{\text{NLO}}^{\alpha_{\text{max}}=0.01}$ [fb]
<i>anti-k<sub>T</sub></i>	550.54 $\pm$ 0.18	808.46 $\pm$ 0.98	808.29 $\pm$ 1.04
<i>k<sub>T</sub></i>	550.54 $\pm$ 0.18	808.67 $\pm$ 0.97	808.86 $\pm$ 1.03
C/A	550.54 $\pm$ 0.18	808.74 $\pm$ 0.97	808.28 $\pm$ 1.03

Algorithm	$\sigma_{\text{LO}}$ [fb]	$\sigma_{\text{NLO}}^{\alpha_{\text{max}}=1}$ [fb]	$\sigma_{\text{NLO}}^{\alpha_{\text{max}}=0.01}$ [fb]
<i>anti-k<sub>T</sub></i>	1394.72 $\pm$ 0.75	1993.3 $\pm$ 2.5	1993.9 $\pm$ 2.7
<i>k<sub>T</sub></i>	1394.72 $\pm$ 0.75	1995.2 $\pm$ 2.5	1994.3 $\pm$ 2.7
C/A	1394.72 $\pm$ 0.75	1995.0 $\pm$ 2.5	1994.3 $\pm$ 2.7

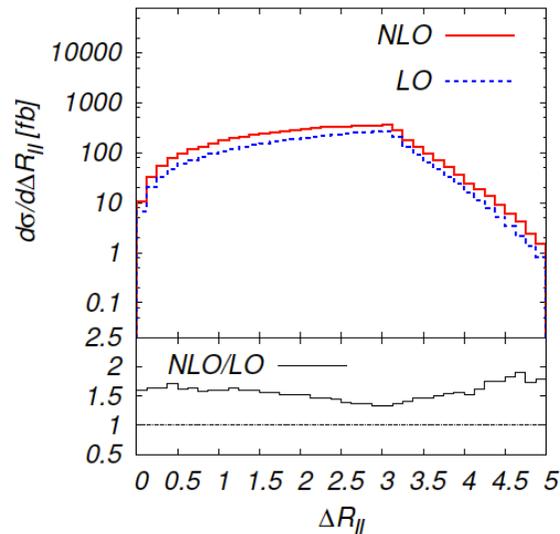
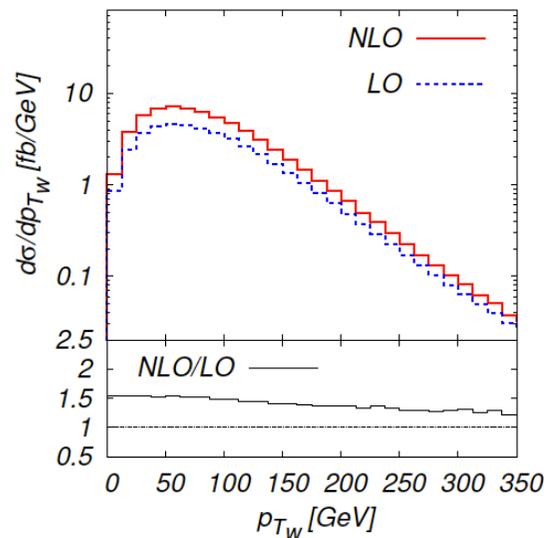
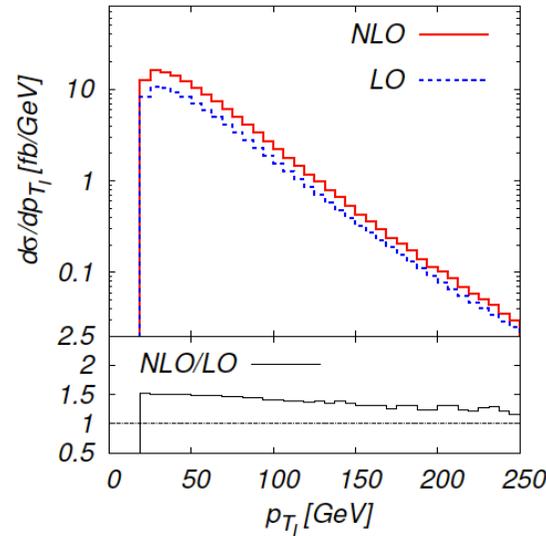
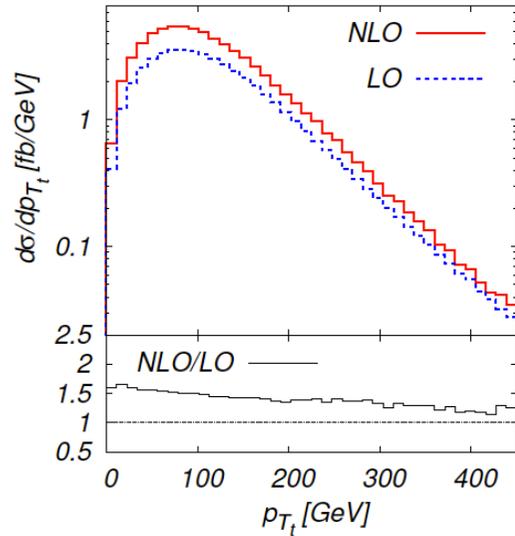
- Double-, single- and non-resonant top quark contributions
- Complex-mass scheme for unstable top
- W gauge bosons are treated off-shell

G. Bevilacqua, M. Czakon, A. van Hameren, C. G. Papadopoulos, M. Worek (2011)

A. Denner, S. Dittmaier, S. Kallweit, S. Pozzorini (2011)

# Beyond NWA

@ LHC 7 TeV



□ The size of NLO QCD corrections to the differential distributions at the LHC

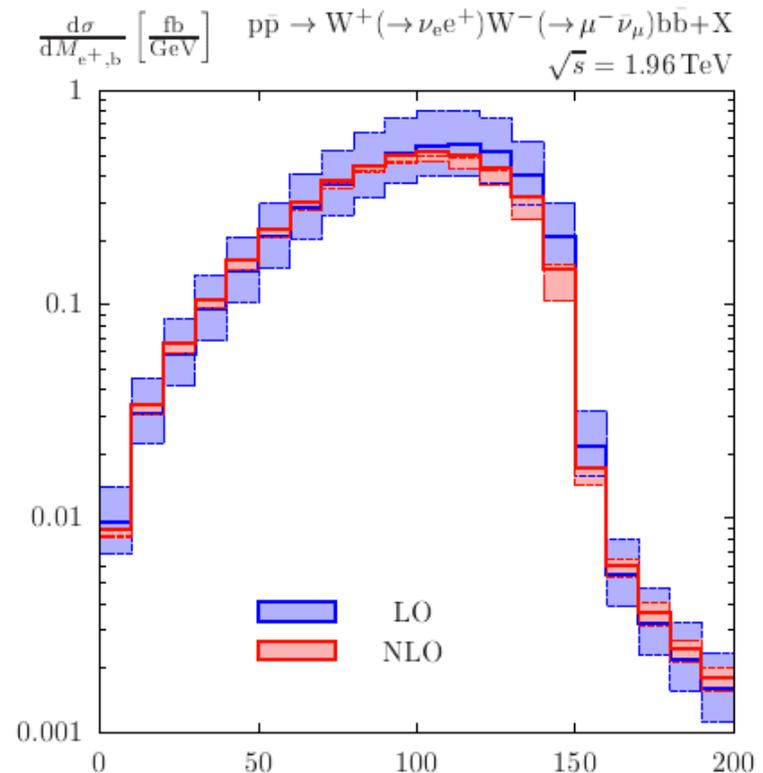
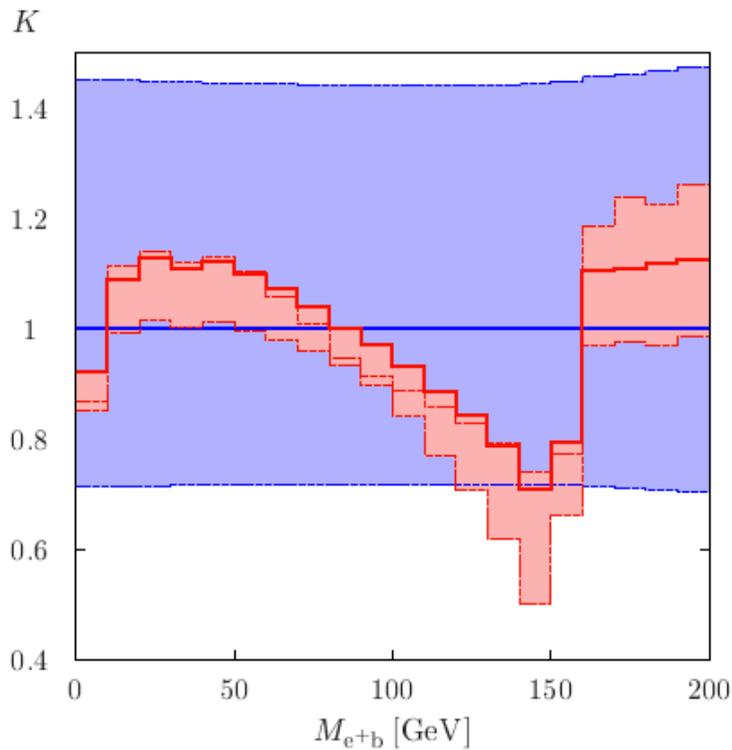
□ For a fixed scale  $m_t$  at LHC the NLO QCD corrections are always positive and large at the level of 50% – 60%

$pp \rightarrow lv \, lv \, bb + X$

# Finite Width Corrections

@ TeVatron 1.96 TeV

- ❑ Invariant mass distribution  $m_{eb}$  at the Tevatron
- ❑ In NWA the LO has upper bound  $m_{eb}^2 \leq m_t^2 - m_W^2 \sim 150$  GeV
- ❑ NLO prediction is barely consistent with the LO uncertainty band close to the kinematic bound



*A. Denner, S. Dittmaier, S. Kallweit, S. Pozzorini (2011)*

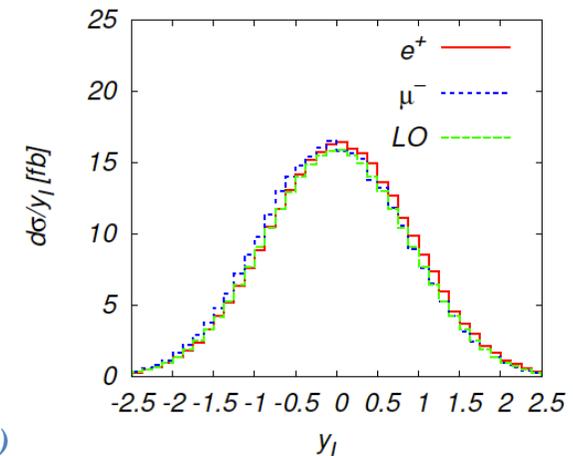
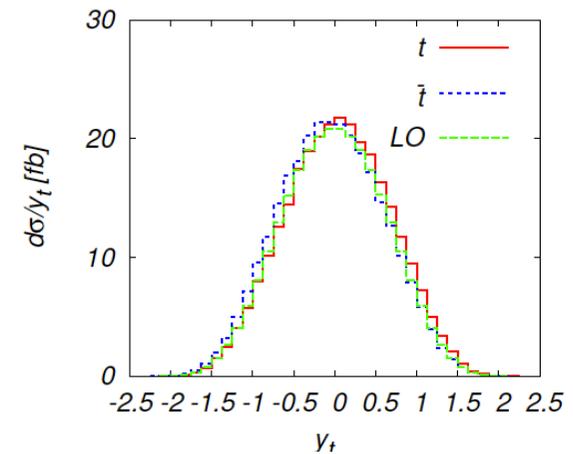
# $A_{FB}$ for top anti-top

- Charge asymmetry and pair asymmetry of top quarks and leptonic charge asymmetry and lepton pair asymmetry for di-leptonic final state at the Tevatron with and without spin correlations

$$A^t = A_{FB}^t = -A_{FB}^{\bar{t}} \quad @ \text{ Tevatron } 1.96 \text{ TeV}$$

$$A^{\ell^+} = A_{FB}^{\ell^+} = -A_{FB}^{\ell^-}$$

$\mu$	Tevatron ( $t\bar{t}$ correlated))			Tevatron ( $t\bar{t}$ uncorrelated))		
	$m_t/2$	$m_t$	$2m_t$	$m_t/2$	$m_t$	$2m_t$
$A$ (NLO')	0.053	0.048	0.044	0.053	0.047	0.043
$A$ (NLOW')	0.054	0.049	0.046	0.054	0.049	0.046
$A^{t\bar{t}}$ (NLO')	0.074	0.068	0.062	0.075	0.067	0.061
$A^{t\bar{t}}$ (NLOW')	0.078	0.071	0.066	0.077	0.070	0.065
$A^\ell$ (NLO')	0.038	0.033	0.031	0.037	0.033	0.030
$A^\ell$ (NLOW')	0.039	0.034	0.032	0.038	0.035	0.032
$A^{\ell\ell}$ (NLO')	0.047	0.042	0.038	0.050	0.045	0.041
$A^{\ell\ell}$ (NLOW')	0.048	0.044	0.040	0.052	0.047	0.043

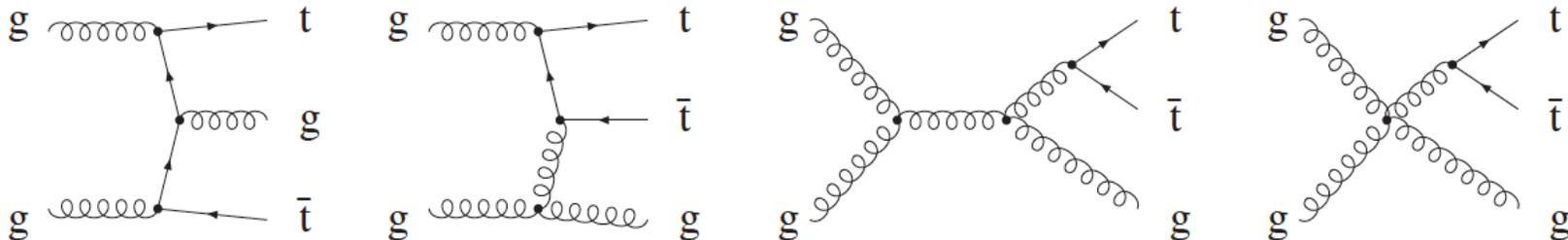


W. Bernreuther, Z. G. Si (2010)

G. Bevilacqua, M. Czakon, A. van Hameren, C. G. Papadopoulos, M. Worek (2011)

# top anti-top + jet @ NLO

- ❑ Substantial number of events in the inclusive top-quark sample is accompanied by the additional jet
- ❑ Top quarks are produced with larger energies and  $p_T$  at the LHC
- ❑ Higher probability for top to radiate gluons
- ❑ Ratio of  $\sigma_{tt+j} / \sigma_{tt}$  @ NLO
  - ❖ At the TeVatron: 30% and 11% for  $p_T$  cut of 20 GeV and 40 GeV
  - ❖ At the LHC: 47% and 22% for  $p_T$  cut of 50 GeV and 100 GeV
- ❑ Important background to various new physics searches
- ❑ Example: Higgs boson production via vector-boson fusion
- ❑ Need for precise theoretical predictions for this process



# top anti-top + jet @ NLO

## □ Complete phenomenological studies at NLO QCD

### ❖ On shell production

*S. Dittmaier, P. Uwer, S. Weinzierl (2007) (2009)*

### ❖ NLO corrections to the production with LO decays in NWA

### ❖ NLO corrections to the production and decays (with radiative one) in NWA

### ❖ $pp \rightarrow ttj + X \rightarrow WWbbj + X \rightarrow lv lv bbj + X$

### ❖ $pp \rightarrow ttj + X \rightarrow WWbbj + X \rightarrow lv jj bbj + X$

*K. Melnikov, M. Schulze (2010)*

*K. Melnikov, A. Scharf, M. Schulze (2012)*

## □ First results of NLO+PS matching for top anti-top plus jet

### ❖ leading soft and collinear logarithms are resummed

### ❖ exclusive, hadron level events can be generated

## □ Two calculations based on the POWHEG BOX method

*A. Kardos, C. G. Papadopoulos, Z. Trocsanyi (2011)*

*S. Alioli, S. Moch, P. Uwer (2012)*

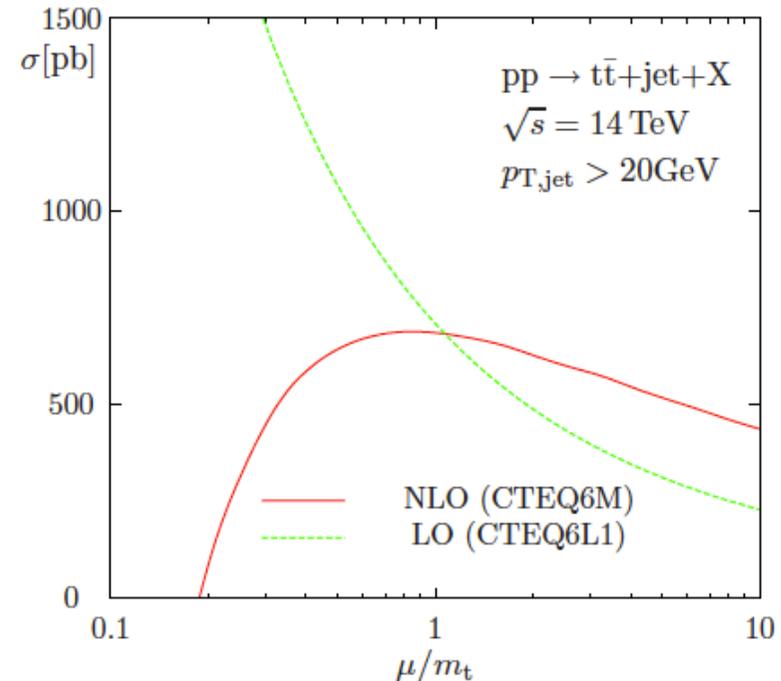
# top quarks on-shell

$p_{T,\text{jet,cut}}$ [GeV]	$\sigma_{t\bar{t}\text{jet}}$ [pb]	
	LO	NLO
20	$710.8(8)^{+358}_{-221}$	$692(3)3^{-40}_{-62}$
50	$326.6(4)^{+168}_{-103}$	$376.2(6)^{+17}_{-48}$
100	$146.7(2)^{+77}_{-47}$	$175.0(2)^{+10}_{-24}$
200	$46.67(6)^{+26}_{-15}$	$52.81(8)^{+0.8}_{-6.7}$

NLO QCD Corrections  
 $K = \text{NLO}/\text{LO} = \mathbf{1.15}$

Scale dependence  
 LO **51%**  $\rightarrow$  NLO **12%**

@ LHC 14 TeV



- ❑ Scale dependence of the LO and NLO cross sections at the LHC
- ❑ Integrated cross sections for different values of  $p_{T}(\text{jet})$  cut

# $A_{\text{FB}}$ for top anti-top plus jet

@ TeVatron 1.96 TeV

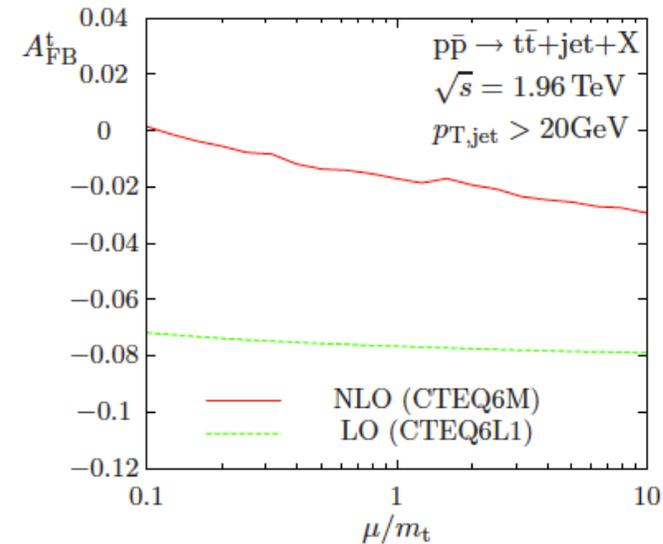
- Forward-backward charge asymmetry at the Tevatron for different values of  $p_{\text{T}}(\text{jet})$  cut
- Scale dependence of the LO and NLO forward-backward charge asymmetry of the top quark

$$A_{\text{FB,LO}}^t = \frac{\sigma_{\text{LO}}(y_t > 0) - \sigma_{\text{LO}}(y_t < 0)}{\sigma_{\text{LO}}(y_t > 0) + \sigma_{\text{LO}}(y_t < 0)}$$

$$A_{\text{FB,NLO}}^t = \frac{\sigma_{\text{LO}}^- + \delta\sigma_{\text{NLO}}^-}{\sigma_{\text{LO}}^+ + \delta\sigma_{\text{NLO}}^+}$$

$$A_{\text{FB,NLO}}^t = \frac{\sigma_{\text{LO}}^-}{\sigma_{\text{LO}}^+} \left( 1 + \frac{\delta\sigma_{\text{NLO}}^-}{\sigma_{\text{LO}}^-} - \frac{\delta\sigma_{\text{NLO}}^+}{\sigma_{\text{LO}}^+} \right)$$

$p_{\text{T,jet,cut}}$ [GeV]	$A_{\text{FB}}^t$ [%]	
	LO	NLO
20	$-7.69(4)^{+0.10}_{-0.085}$	$-1.77(5)^{+0.58}_{-0.30}$
30	$-8.29(5)^{+0.12}_{-0.085}$	$-2.27(4)^{+0.31}_{-0.51}$
40	$-8.72(5)^{+0.13}_{-0.10}$	$-2.73(4)^{+0.35}_{-0.49}$
50	$-8.96(5)^{+0.14}_{-0.11}$	$-3.05(4)^{+0.49}_{-0.39}$



- Asymmetry at NLO via a consistent expansion in  $\alpha_s$

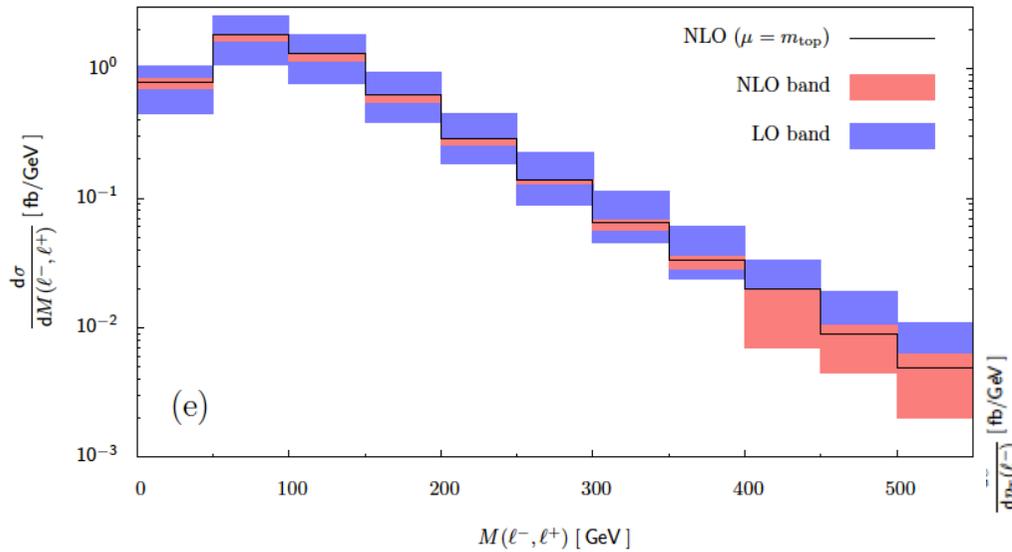
# ttj in NWA with LO decays

$pp \rightarrow ttj + X \rightarrow WWbj + X \rightarrow lv lv bbj + X$

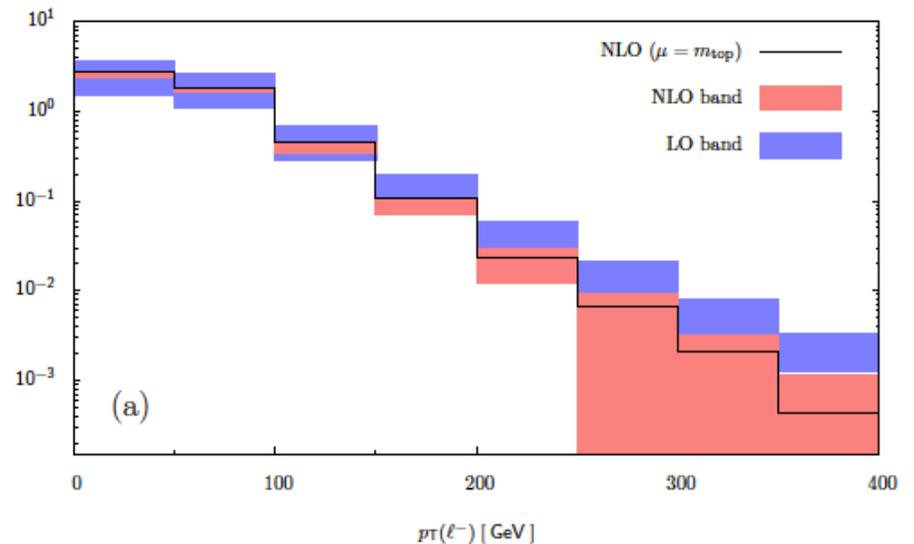
@ LHC 7 TeV

$$\sigma_{\text{LO}} = 229.9^{+133.7}_{-78.2} \text{ fb}$$

$$\sigma_{\text{NLO}} = 256.5^{+14.8}_{-25.6} \text{ fb}$$



- Invariant mass of two leptons
- Transverse momentum of lepton



- For  $\mu = m_t/2$  negative distribution at high  $p_T(l) > 400$  GeV
- Kinematic dependent scale (?)

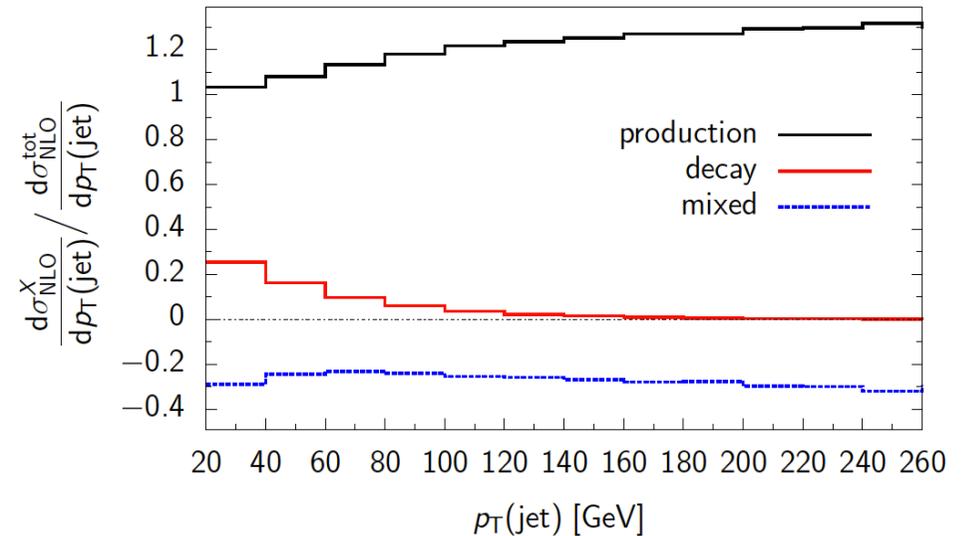
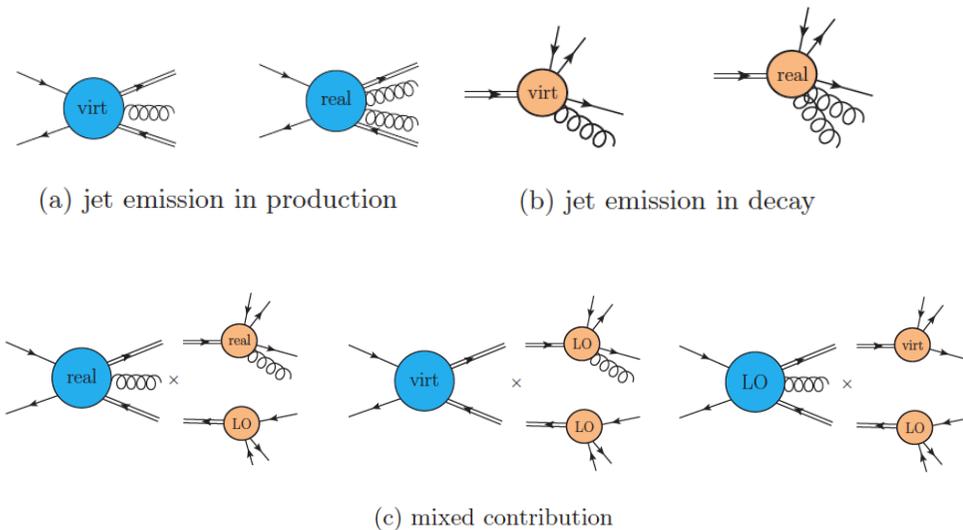
NLO QCD Corrections  
 $K = \text{NLO}/\text{LO} = 1.12$

Scale dependence  
 LO 58%  $\rightarrow$  NLO 10%

# ttj @ NLO in NWA

- ttj → WWbbj in NWA with top decays, including radiative decay (t → Wbj) described consistently at NLO QCD with spin correlations
- State of the art description of ttj process
- Radiation in the production dominates

@ LHC 7 TeV



$$\sigma_{\text{LO}} = 316.9 (\text{P}) + 33.4 (\text{D}) = 350.3 \text{ fb}$$

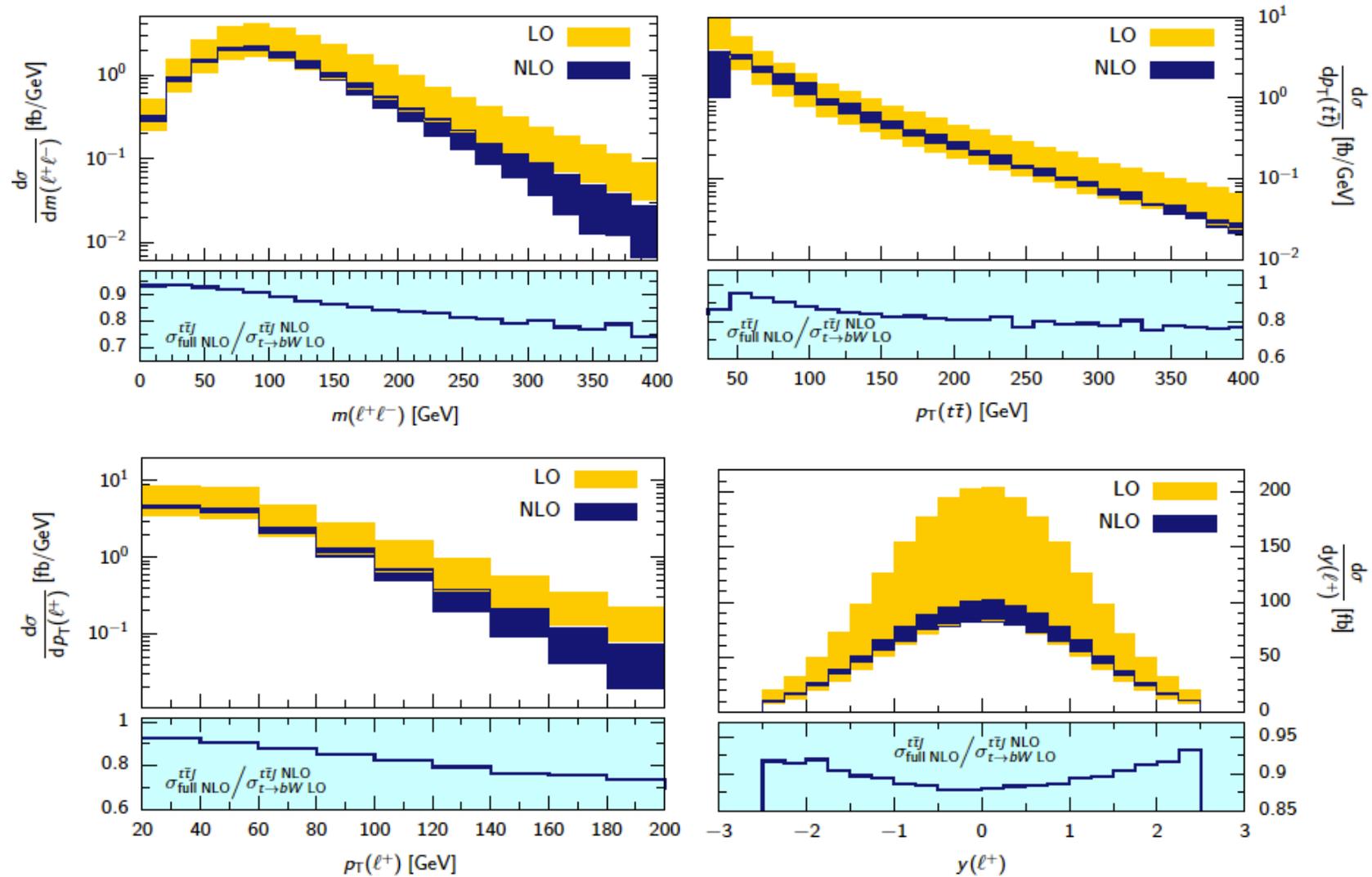
$$\sigma_{\text{NLO}} = 323 (\text{P}) + 40.5 (\text{D}) - 75.5 (\text{Mix}) = 288 \text{ fb}$$

NLO QCD Corrections  
 $K = \text{NLO}/\text{LO} = 0.82$  (-18%)

Scale dependence  
 LO 61% → NLO 16%

# ttj @ NLO in NWA

@ LHC 7 TeV



K. Melnikov, A. Scharf, M. Schulze (2012)

# top anti-top + 2j @ NLO

- ❑ Number of events in the inclusive tt sample accompanied by two additional jets
- ❑ Ratio of  $\sigma_{tt+j} / \sigma_{tt}$  @ NLO
  - ❖ At the TeVatron: 4% and 1% for  $p_T$  cut of 20 GeV and 40 GeV
  - ❖ At the LHC: 6% and 1% for  $p_T$  cut of 50 GeV and 100 GeV
- ❑ Important background for Higgs boson searches: ttj and ttbb
- ❑  $H \rightarrow WW^*$  produced via weak boson fusion ( $m_H \sim 130$  GeV)
  - ❖ Higgs boson mass peak cannot be directly reconstructed
- ❑  $H \rightarrow bb$  produced via associated production with a top anti-top ( $m_H < 140$  GeV)
  - ❖ Reconstruction of the  $H \rightarrow bb$  mass peak difficult
  - ❖ The bb pair can be chosen incorrectly
  - ❖ b-tagging efficiency, two b-jets can arise from mistagged light jets

Very precise knowledge of QCD backgrounds is necessary !

# top anti-top + 2j @ NLO

- Complete phenomenological studies at NLO QCD with on shell top quarks
  - ❖ ttbb at the LHC completed by two groups with per-mille agreement

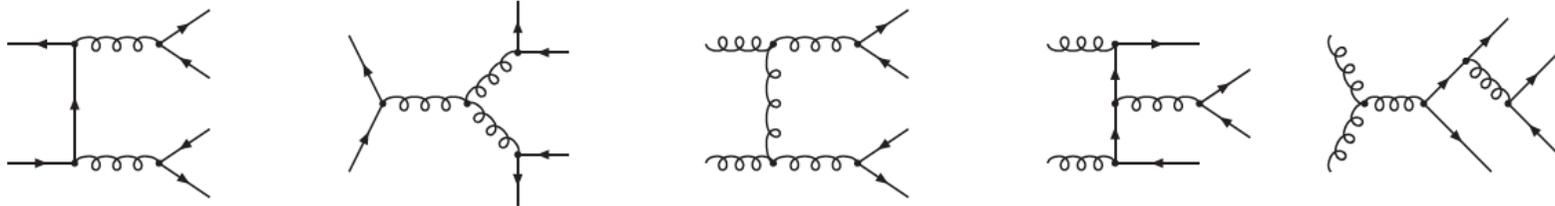
*A. Bredenstein, A. Denner, S. Dittmaier, S. Pozzorini (2008) (2009) (2010)*  
*G. Bevilacqua, M. Czakon, C. G. Papadopoulos, R. Pittau, M. Worek (2009)*

- ❖ ttbb also completed for the Tevatron

*M. Worek (2012)*

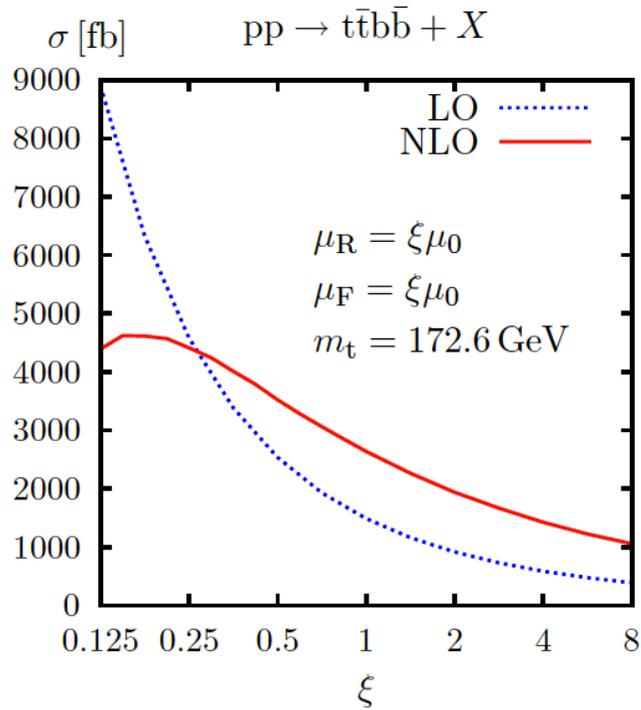
- ❖ ttjj calculation both for the Tevatron and the LHC

*G. Bevilacqua, M. Czakon, C. G. Papadopoulos, M. Worek (2010) (2011)*



# ttbb @ NLO – top on shell

@ LHC 14 TeV



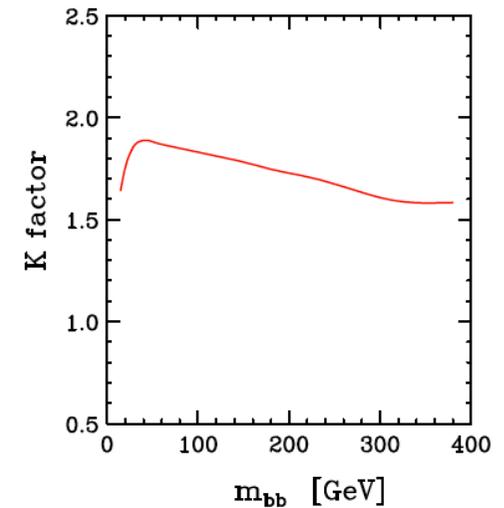
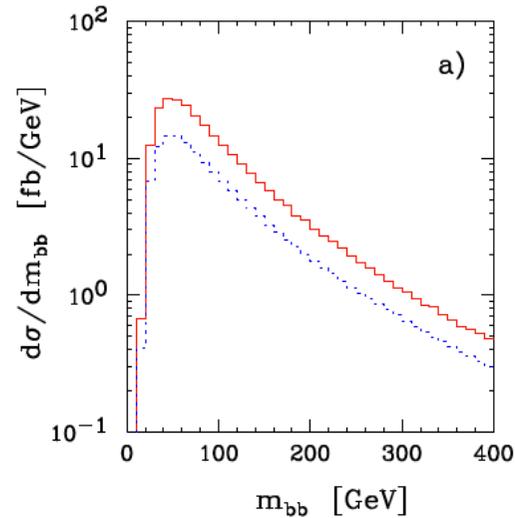
NLO QCD Corrections

$$K = \text{NLO}/\text{LO} = \mathbf{1.77}$$

Scale dependence

LO 70%  $\rightarrow$  NLO 33%

- Scale dependence for fixed scale  $m_t$
- Invariant mass distribution of two b jets



$$\sigma_{t\bar{t}b\bar{b}}^{\text{LO}} = 1489.2 \begin{matrix} +1036.8 \text{ (70\%)} \\ -565.8 \text{ (38\%)} \end{matrix} \text{ fb}$$

$$\sigma_{t\bar{t}b\bar{b}}^{\text{NLO}} = 2636 \begin{matrix} +862 \text{ (33\%)} \\ -703 \text{ (27\%)} \end{matrix} \text{ fb}$$

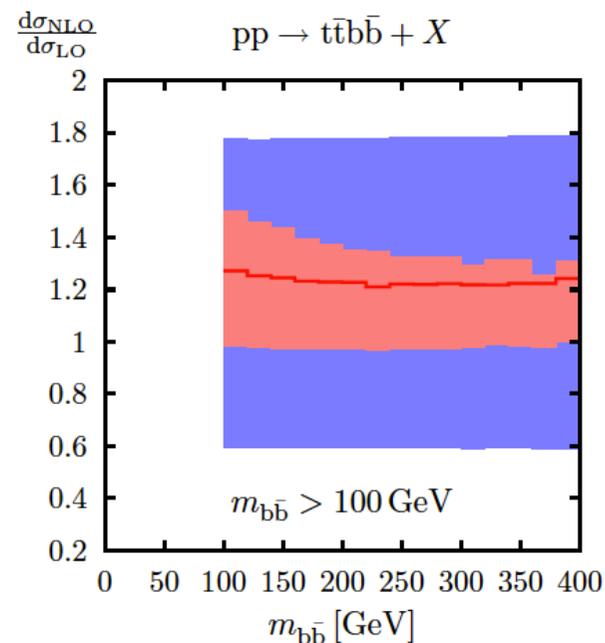
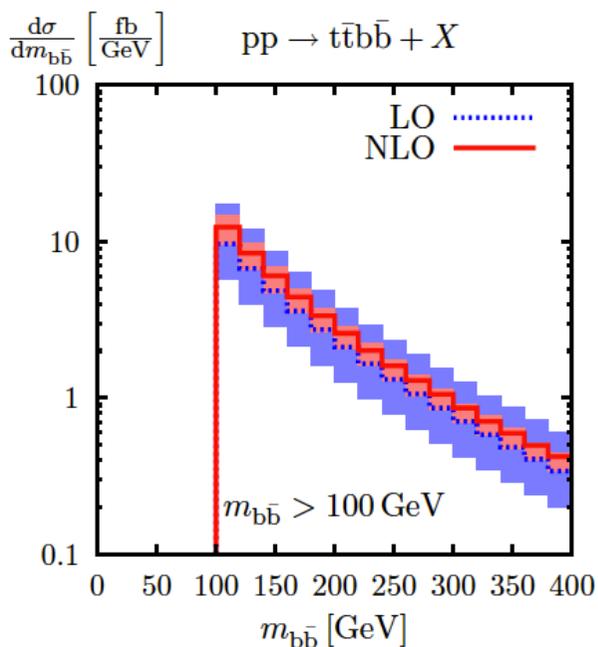
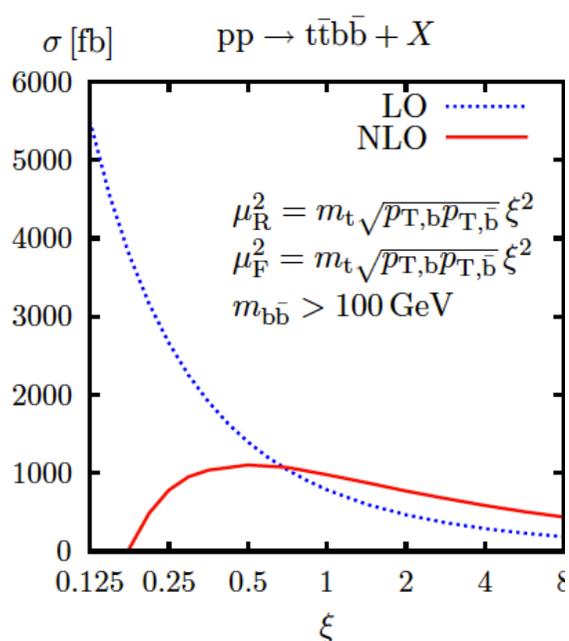
*A. Bredenstein, A. Denner, S. Dittmaier, S. Pozzorini (2009)*

*G. Bevilacqua, M. Czakon, C. G. Papadopoulos, R. Pittau, M. Worek (2009)*

# ttbb @ NLO – top on shell

@ LHC 14 TeV

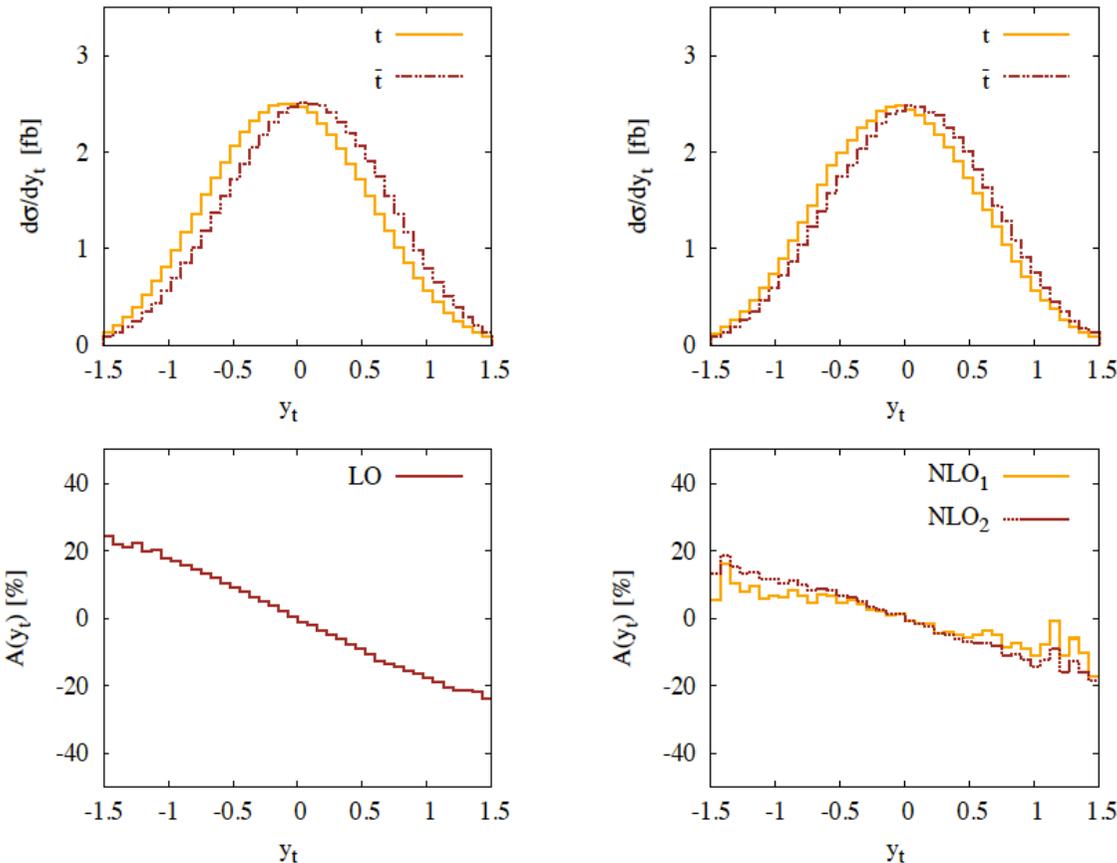
Setup	$m_{b\bar{b},\text{cut}}$	$p_{T,b\bar{b},\text{cut}}$	$p_{\text{jet,veto}}$	$p_{T,b,\text{cut}}$	$y_{b,\text{cut}}$	$\sigma_{\text{LO}}$ [fb]	$\sigma_{\text{NLO}}$ [fb]	$K$
I	100	-	-	20	2.5	786.3(2) <sup>+78%</sup> <sub>-41%</sub>	978(3) <sup>+13%</sup> <sub>-21%</sub>	1.24
II	-	200	-	20	2.5	451.8(2) <sup>+79%</sup> <sub>-41%</sub>	592(4) <sup>+13%</sup> <sub>-22%</sub>	1.31
III	100	-	100	20	2.5	786.1(6) <sup>+78%</sup> <sub>-41%</sub>	700(3) <sup>+0.4%</sup> <sub>-19%</sub>	0.89
IV	100	-	-	50	2.5	419.4(1) <sup>+77%</sup> <sub>-40%</sub>	526(2) <sup>+13%</sup> <sub>-21%</sub>	1.25



# $A_{\text{FB}}$ for $t\bar{t}b\bar{b}$

- Rapidity distributions of the top and anti-top
- Differential asymmetry  $A(y_t)$  as a function of top quark rapidity

@ TeVatron 1.96 TeV



*M. Worek (2012)*

- Integrated forward-backward asymmetry of the top quark at LO and NLO

$$A_{\text{FB,LO}}^t = -0.088(2)$$

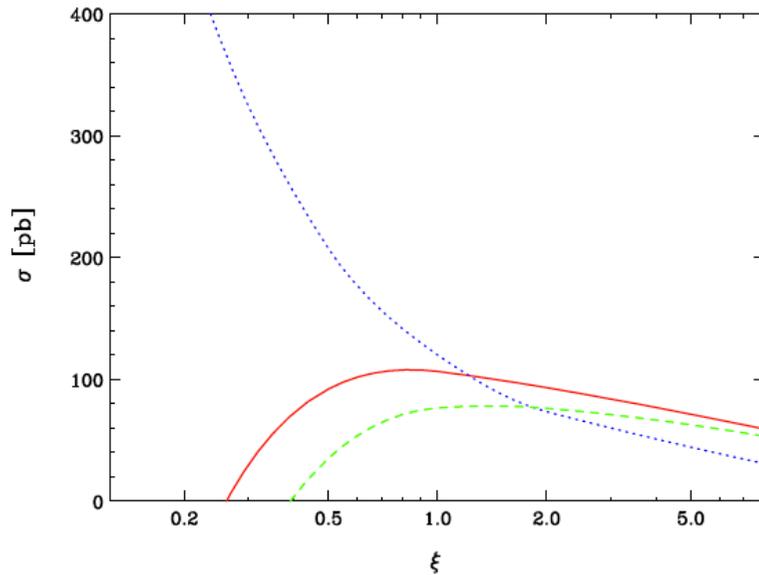
$$A_{\text{FB,NLO}}^t = -0.044(6)$$

- For an unexpanded ratio of the NLO cross sections

$$A_{\text{FB,NLO}}^t = -0.061(14)$$

# ttjj @ NLO – top on shell

@ LHC 14 TeV



- Scale dependence of total cross section at LO and NLO as well as NLO with jet veto of 50 GeV

$$\sigma_{pp \rightarrow t\bar{t}jj+X}^{\text{NLO}} = (106.94 \pm 0.17) \text{ pb}$$

$$\sigma_{pp \rightarrow t\bar{t}jj+X}^{\text{NLO}}(p_{T,X} < 50 \text{ GeV}) = (76.58 \pm 0.17) \text{ pb}$$

PROCESS	$\sigma^{\text{LO}}$ [pb]	CONTRIBUTION
$pp \rightarrow t\bar{t}jj$	120.17(8)	100 %
$qg \rightarrow t\bar{t}qg$	56.59(5)	47.1 %
$gg \rightarrow t\bar{t}gg$	52.70(6)	43.8 %
$qq' \rightarrow t\bar{t}qq', q\bar{q} \rightarrow t\bar{t}q'\bar{q}'$	7.475(8)	6.2 %
$gg \rightarrow t\bar{t}q\bar{q}$	1.981(3)	1.6 %
$q\bar{q} \rightarrow t\bar{t}gg$	1.429(1)	1.2 %

NLO QCD Corrections  
 $K = \text{NLO}/\text{LO} = 0.89$  (-11%)

Scale dependence  
 LO 72%  $\rightarrow$  NLO 13%

# ttjj @ NLO – top on shell

@ LHC 7 TeV

CUTS	$\sigma_{\text{LO}}$ [pb]	$\sigma_{\text{NLO}}^{\text{anti-}k_T}$ [pb]	$\sigma_{\text{NLO}}^{k_T}$ [pb]	$\sigma_{\text{NLO}}^{C/A}$ [pb]
$p_{T_j} > 50$ GeV $\Delta R_{jj} > 1.0$ $ y_j  < 2.5$	11.561(4)	9.95(2)	10.06(2)	10.04(2)

$\Delta R_{jj} > 1$   
NLO QCD Corrections  
 $K = \text{NLO}/\text{LO} = \mathbf{0.86 (-14\%)}$

CUTS	$\sigma_{\text{LO}}$ [pb]	$\sigma_{\text{NLO}}^{\text{anti-}k_T}$ [pb]	$\sigma_{\text{NLO}}^{k_T}$ [pb]	$\sigma_{\text{NLO}}^{C/A}$ [pb]
$p_{T_j} > 50$ GeV $\Delta R_{jj} > 0.5$ $ y_j  < 2.5$	13.398(4)	9.82(2)	9.86(2)	9.86(2)

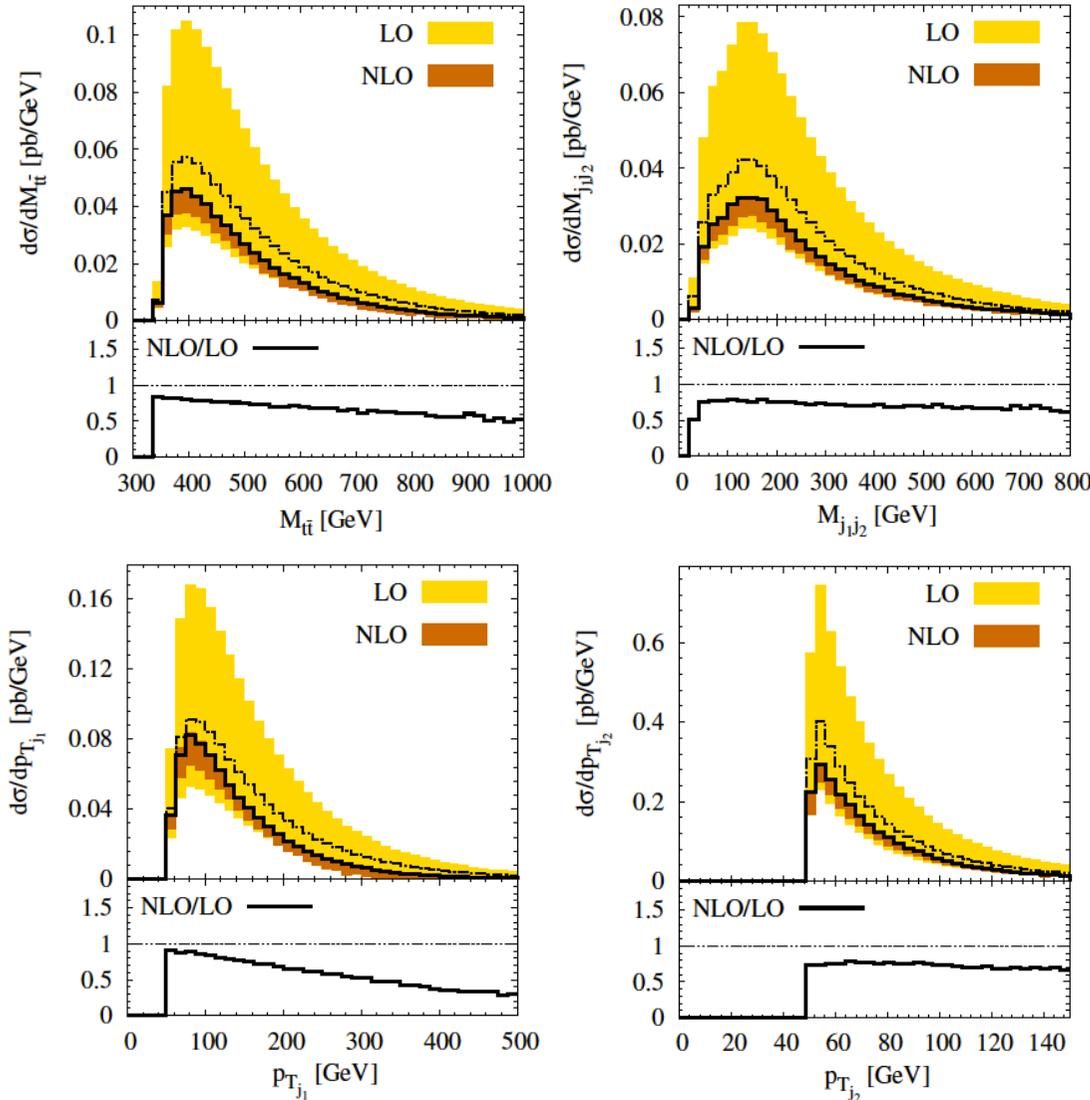
$\Delta R_{jj} > 0.5$   
NLO QCD Corrections  
 $K = \text{NLO}/\text{LO} = \mathbf{0.73 (-27\%)}$

$p_{T_j}$ CUT	$\sigma_{\text{LO}}$ [pb]	$\sigma_{\text{NLO}}^{\text{anti-}k_T}$ [pb]	$\mathcal{K}$	[%]
$p_{T_j} > 50$ GeV	13.398(4)	9.82(2)	0.73	-27
$p_{T_j} > 75$ GeV	5.944(2)	4.115(8)	0.69	-31
$p_{T_j} > 100$ GeV	3.018(1)	1.944(4)	0.64	-36
$p_{T_j} > 125$ GeV	1.665(1)	0.993(2)	0.60	-40

- ❑ Within 50 -100 GeV range corrections are quite stable
- ❑ K-factor changed by 9%

# ttjj @ NLO – top on shell

@ LHC 7 TeV



- NLO QCD corrections to the distributions are negative
- Analysis done for fixed scale
- If large distortions improvement can be achieved via dynamical scale
- Invariant dijet mass do not show major distortions

# $A_{\text{FB}}$ for $t\bar{t}j$

- Rapidity distribution of top and anti-top at LO and NLO
- Differential charge asymmetry  $A(y_t)$  as a function of top rapidity

@ TeVatron 1.96 TeV

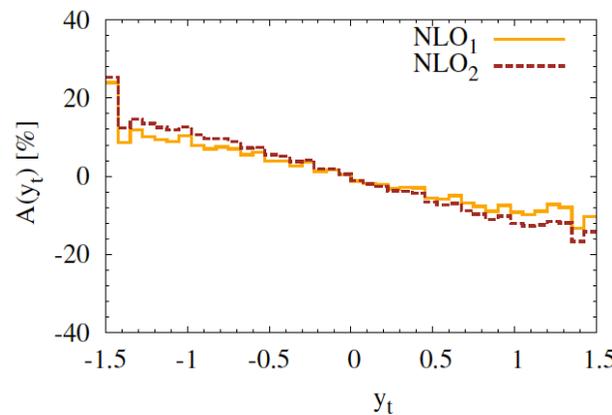
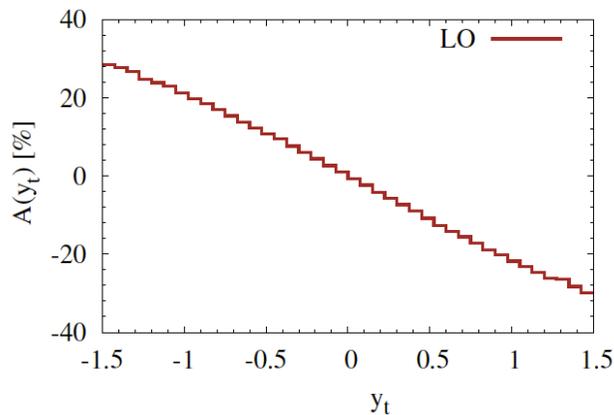
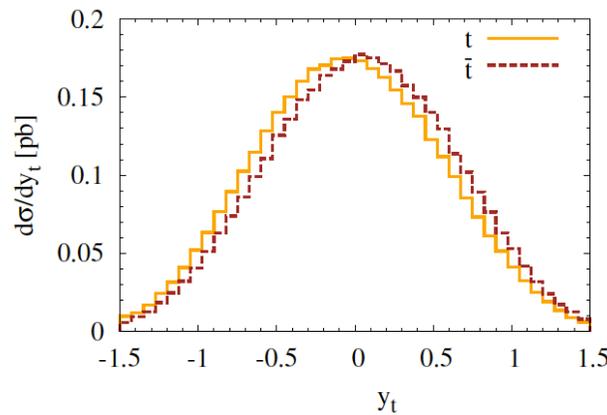
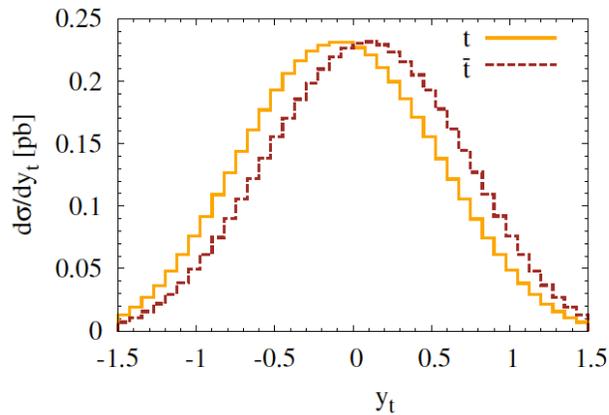
- Integrated  $A_{\text{FB}}$  of the top quark at LO and NLO

$$A_{\text{FB,LO}}^t = -0.103(4)$$

$$A_{\text{FB,NLO}}^t = -0.046(6)$$

- For an unexpanded ratio of the NLO cross sections

$$A_{\text{FB,NLO}}^t = -0.058(42)$$



# Summary

NLO Status	On-shell	NWA	Full	Parton Shower
tt	YES	YES	YES	YES
ttj	YES	YES	NO	YES
ttjj	YES	NO	NO	NO
ttbb	YES	NO	NO	NO

# Summary & Outlook

- ❑ New problem at the LHC, multiparticle final states !
- ❑ Hard emission is less suppressed at LHC energies
- ❑ Remarkable development in NLO calculations driven by the LHC needs
- ❑  $2 \rightarrow 4$  processes currently scrutinized
- ❑  $2 \rightarrow 5$  and maybe  $2 \rightarrow 6$  processes doable with new methods
- ❑ Cannot do better than LO for  $2 \rightarrow 7(8)$  processes
  
- ❑ Better understanding of the scale choice that describes high  $p_T$  region correctly
- ❑ Dynamic scales that depend on the event structure
  
- ❑ **Goal:** Fully realistic final state such as  $WWbbX$  with  $X = j, jj, H, Z, A, \gamma$   
for the LHC matched to parton shower with higher than LL accuracy
  
- ❑ Meanwhile huge progress in the resummation and NNLO calculations for top
- ❑ **First NNLO calculation for  $2 \rightarrow 2$  process at hadron collider is now available !**
- ❑  **$q\bar{q} \rightarrow t\bar{t} + X$  @ TeVatron calculated !**