

INTEGRABILITY BEYOND NEAREST-NEIGHBOR INTERACTIONS

ANA RETORE

FELLOWS 2025





CAMPOS
NOVOS

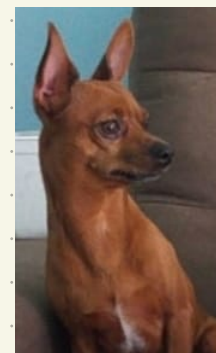
ANA LÚCIA RETORE



PRETA



LILICA

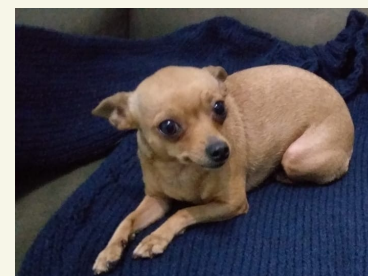


BELA



LUNA

MEL



ANA LÚCIA RETORE

MIAMI



ONE-YEAR PhD
internship

PhD
student

SÃO PAULO



DUBLIN



ANA LÚCIA RETORE

FIRST POSTDOC
POSITION

DUBLIN



HAMBURG



DURHAM



NOW

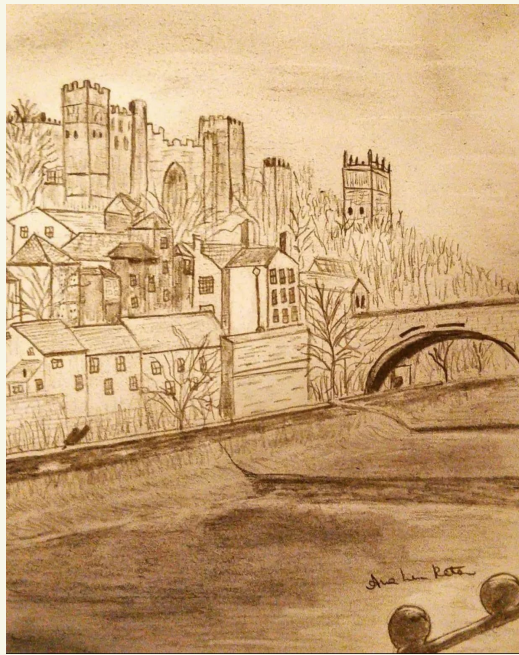
SECOND POSTDOC
POSITION

ANA LÚCIA RETORE

HOBBIES



Reading



Drawing



Video Games



RESEARCH

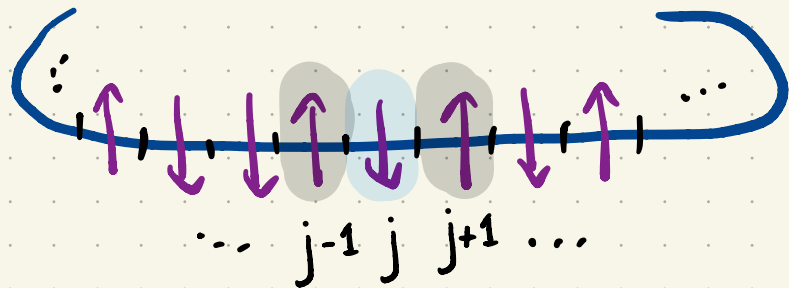
The word "RESEARCH" is written in a black, hand-drawn, uppercase font. Behind the letters, there are five light gray arrows. The first arrow (under 'R') points diagonally up and to the left. The second arrow (under 'E') points diagonally down and to the left. The third arrow (under 'S') points diagonally up and to the right. The fourth arrow (under 'E') points diagonally up and to the right. The fifth arrow (under 'A') points diagonally down and to the right. The background is a light gray grid of small dots.

SPIN CHAIN

Discrete 1d quantum system, whose
Hamiltonian acts on L copies of a Hilbert space

$$H : \underbrace{\mathbb{C}^2 \otimes \dots \otimes \mathbb{C}^2}_L \mapsto \mathbb{C}^2 \otimes \dots \otimes \mathbb{C}^2$$

$$H = \sum_{j=1}^L h(j)$$



INTEGRABLE



The presence of many
hidden SYMMETRIES

—
|
INTEGRABLE
MODELS
|

$$Q_1 = e^{iP}$$

$$Q_2 = H$$

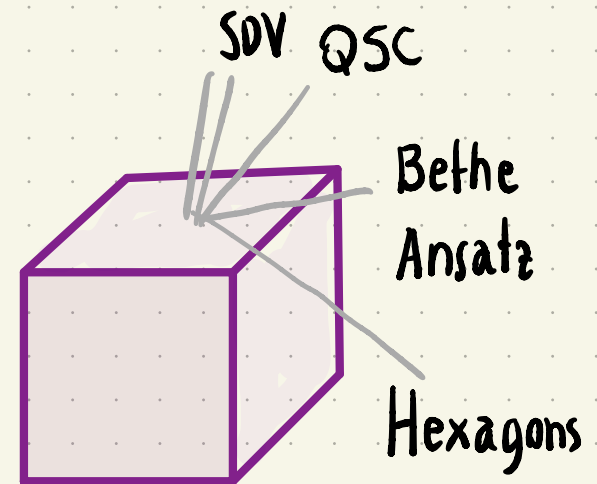
$$Q_3$$

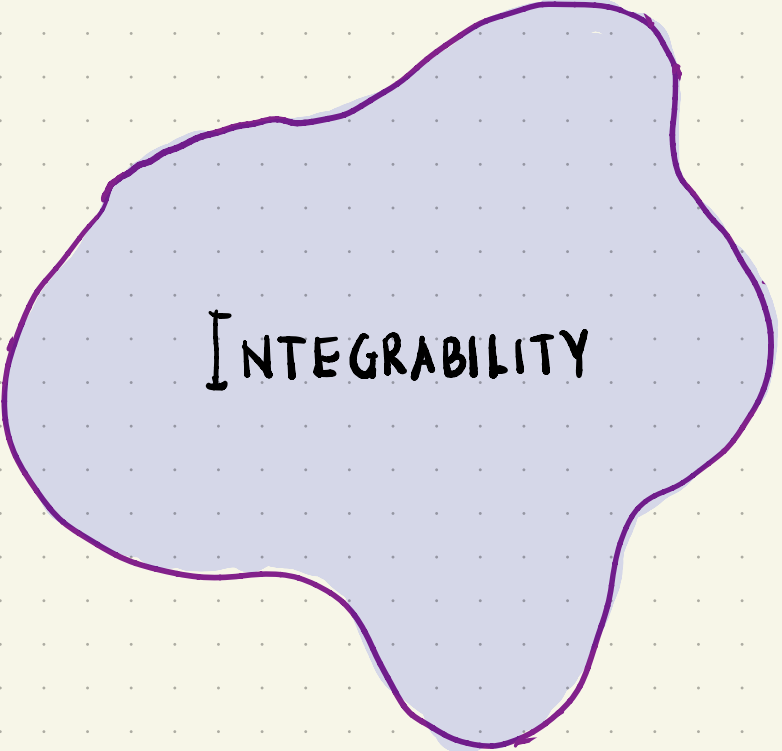
and MANY MORE

$$[Q_n, Q_m] = 0$$

$$m, n = 1, 2, \dots$$

R-MATRIX $\Rightarrow$ CHARGES $\Rightarrow$





INTEGRABILITY

* MAGNETISM

Heisenberg spin chain
Potts model,

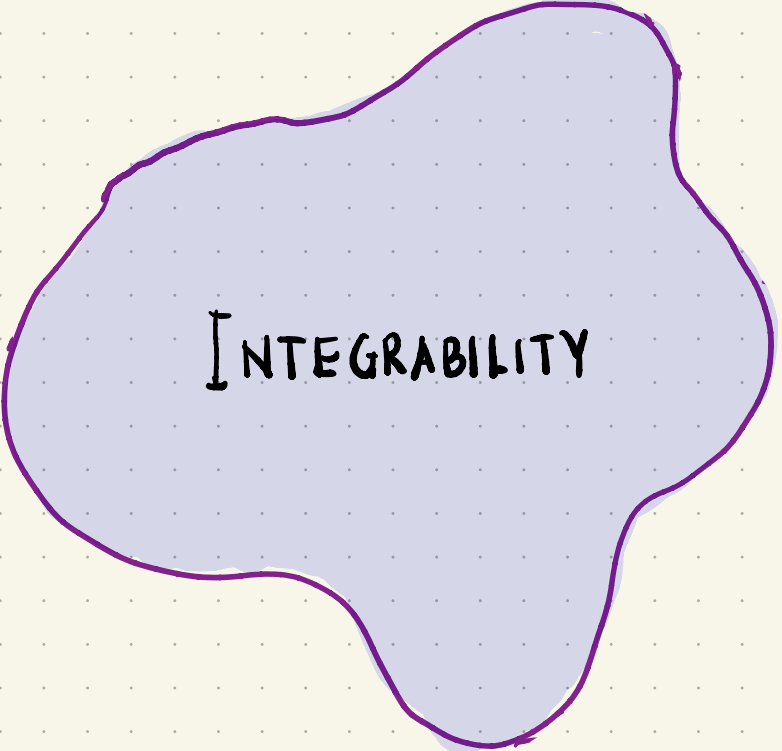
* SUPERCONDUCTIVITY

1d. Hubbard model

* STATISTICAL MECHANICS

GENERALISED GIBBS - ENSEMBLE

* NON-ISOLATED SYSTEMS LINDBLADIANS



INTEGRABILITY

* QUANTUM COMPUTING.

* STOCHASTIC SYSTEMS

* GAUGE THEORIES

* MATHEMATICS (QUANTUM GROUPS
YANGIANS
TEMPERLEY-LIEB)

WHEN PRESENT
IS A VERY
USEFUL TOOL



- * We can rarely solve problems exactly;
- * Perturbation theory works very well at weak coupling
- * At strong coupling Perturbation theory stops working
- * **INTEGRABLE MODELS**
can be solved even for
medium and strong coupling.

Q₁. IS THIS AN INTEGRABLE
HAMILTONIAN ?

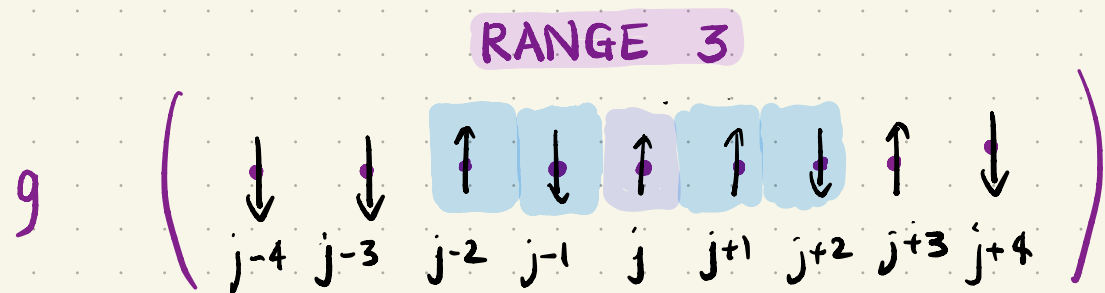
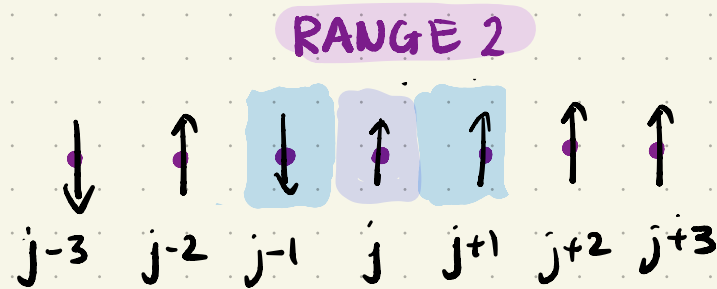
Q₂. CAN WE GO BEYOND MODELS
WITH A LOT OF SYMMETRY ?
(including $R(u,v) \neq R(u-v)$)

with de Leeuw, Paletta, Pribytok, Ryan

Q₃. CAN WE GO BEYOND NEAREST-NEIGHBOUR INTERACTIONS

such as

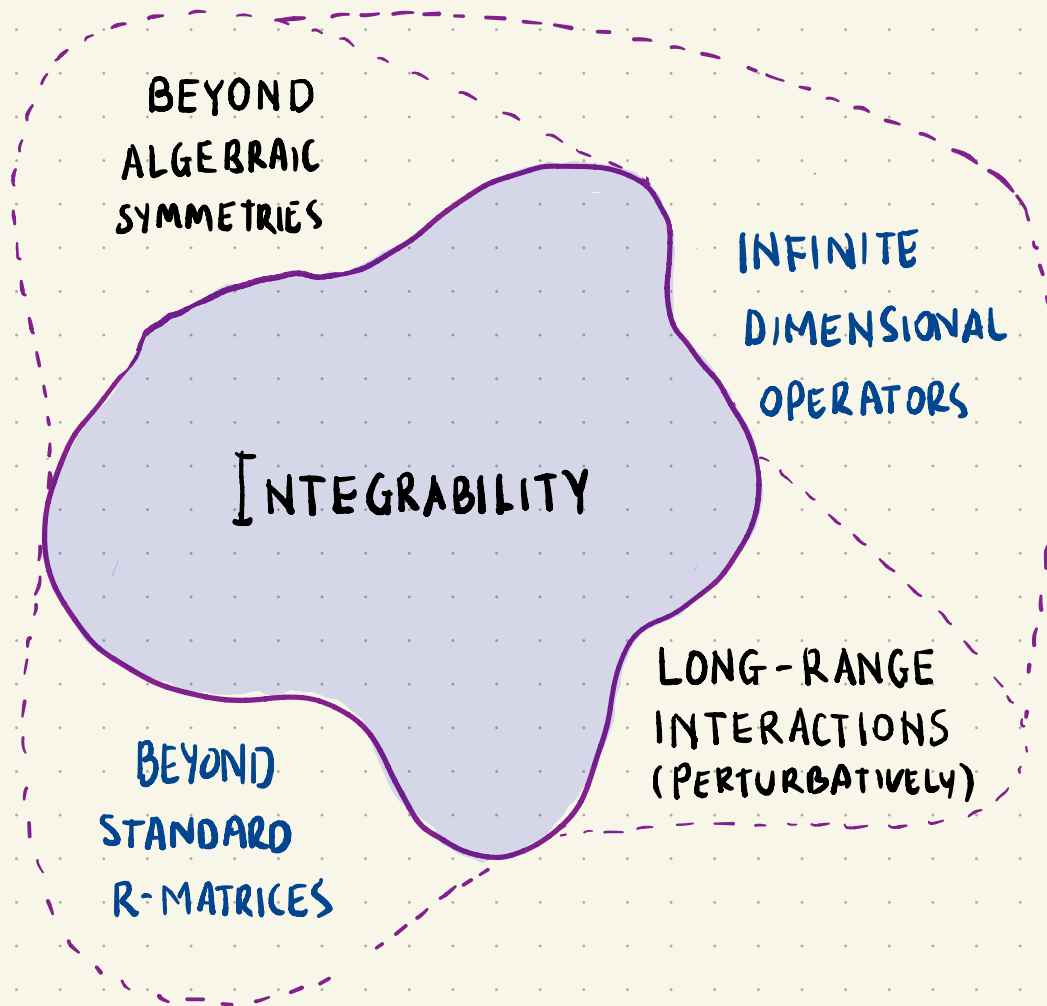
$$H \sim \sum_{j=1} h_{jj+1} + g h_{jj+1j+2}$$



+ O(g²)

AND STILL COMPUTE THE R-MATRIX? with M.de.leeuw

To do :

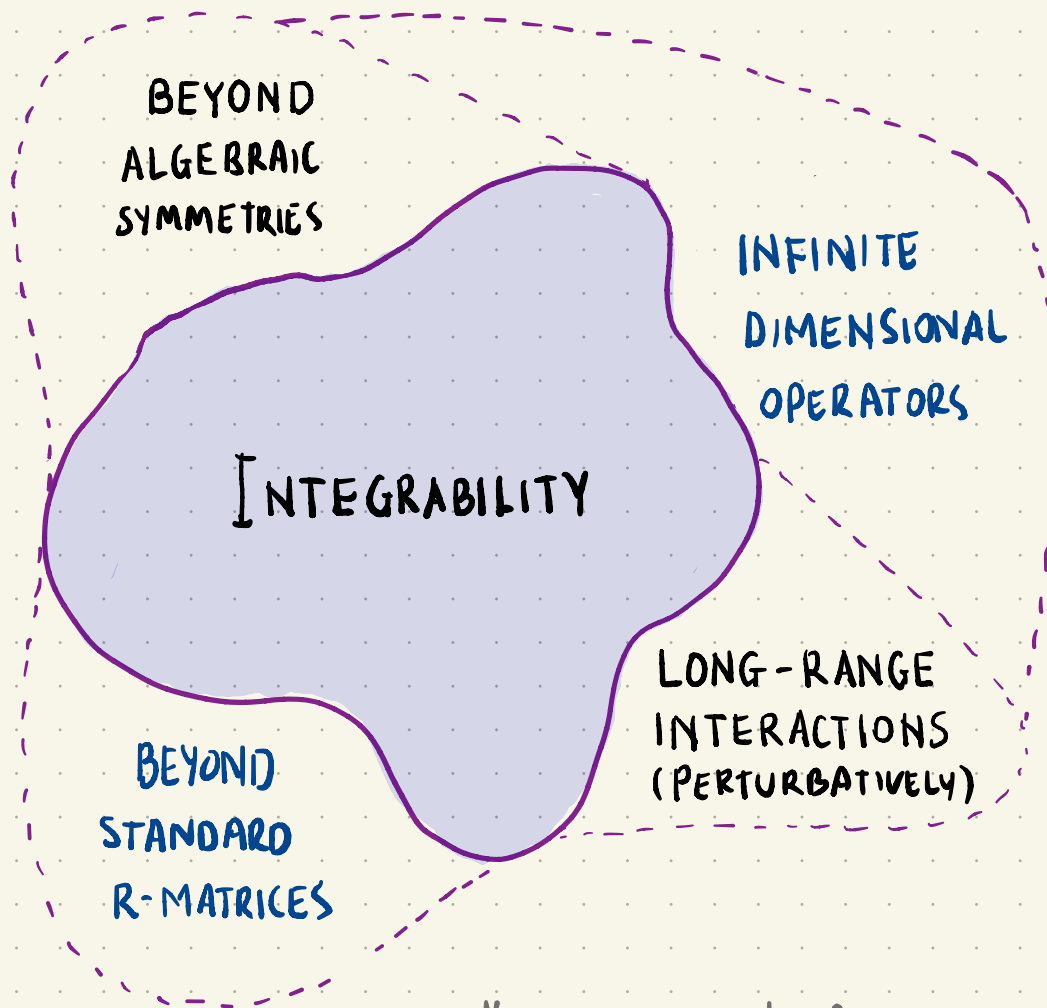


BOUNDARIES ?

APPLICATIONS ?

GENERALISE THE METHODS
TO FIND SOLUTIONS ?

To DO :



BOUNDARIES ?

APPLICATIONS ?

GENERALISE THE METHODS
TO FIND SOLUTIONS ?

THANK

YOU!

"Journey before destination."
(from the Stormlight Archives)