# Measuring masses of new particles in central exclusive processes at the LHC

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in collaboration with:

L.A. Harland-Lang (Cambridge U.), C.H. Kom (Liverpool U.)

W.J. Stirling (Cambridge U.)

Based on:

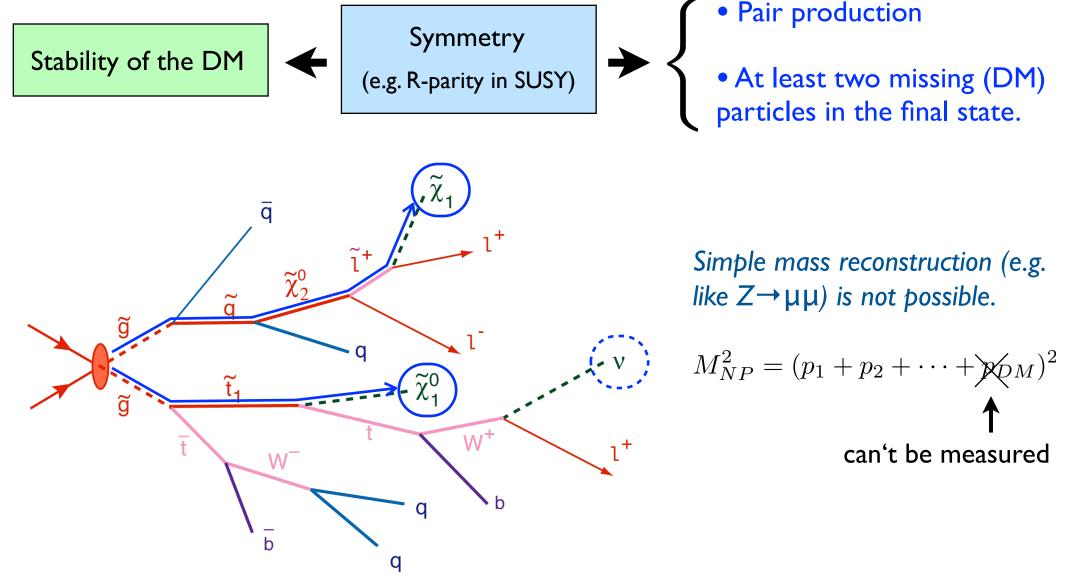
arXiv:1110.4320 [hep-ph]

# **Plan**

- Introduction
- Edge method and mT2
- A new method in central exclusive processes
- Summary

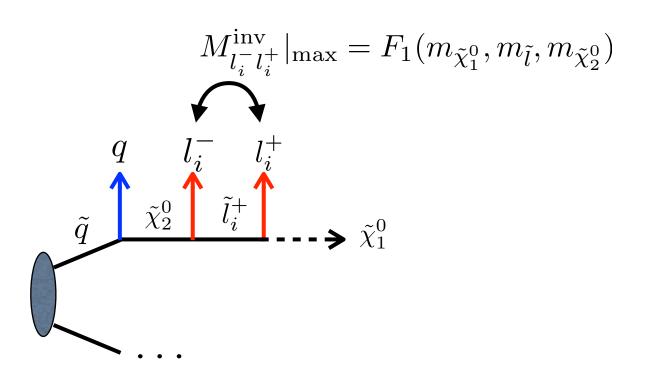
# Introduction

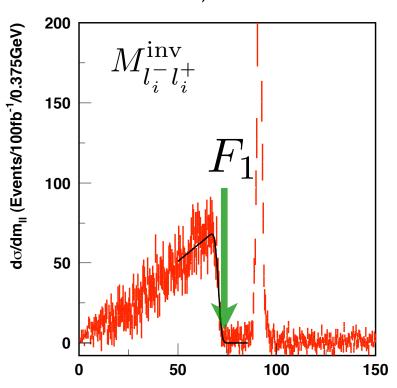
Measuring the masses of new particles may be a bit tricky at the LHC.



# **Edge method**

B.C.Allanach, C.G.Lester, M.A.Parker, B.R.Webber '00





# **Edge method**

B.C.Allanach, C.G.Lester, M.A.Parker, B.R.Webber '00

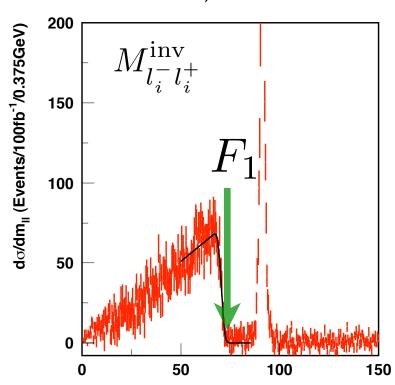
$$M_{lq}^{\text{inv,high}}|_{\text{max}} = F_2(m_{\tilde{\chi}_1^0}, m_{\tilde{l}}, m_{\tilde{\chi}_2^0}, m_{\tilde{q}})$$

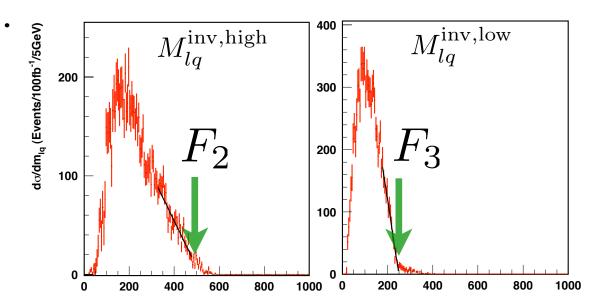
$$M_{lq}^{\text{inv,low}}|_{\text{max}} = F_3(m_{\tilde{\chi}_1^0}, m_{\tilde{l}}, m_{\tilde{\chi}_2^0}, m_{\tilde{q}})$$

$$q \quad l_i^- \quad l_i^+$$

$$\tilde{q} \quad \tilde{\chi}_2^0 \quad \tilde{l}_i^+$$

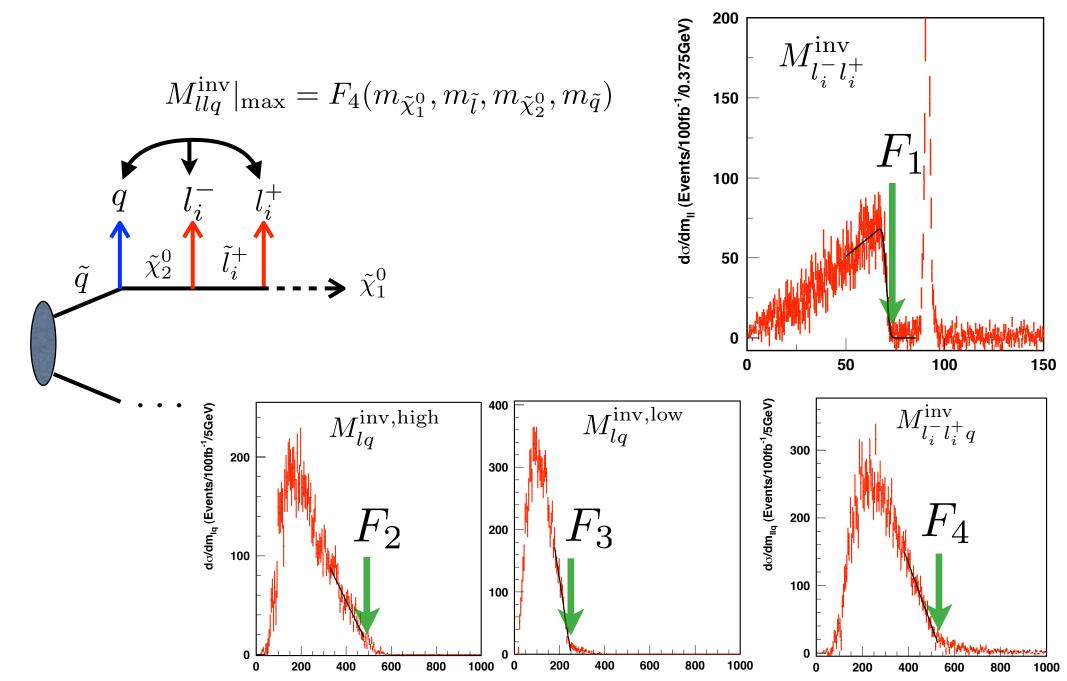
$$\tilde{\chi}_1^0$$



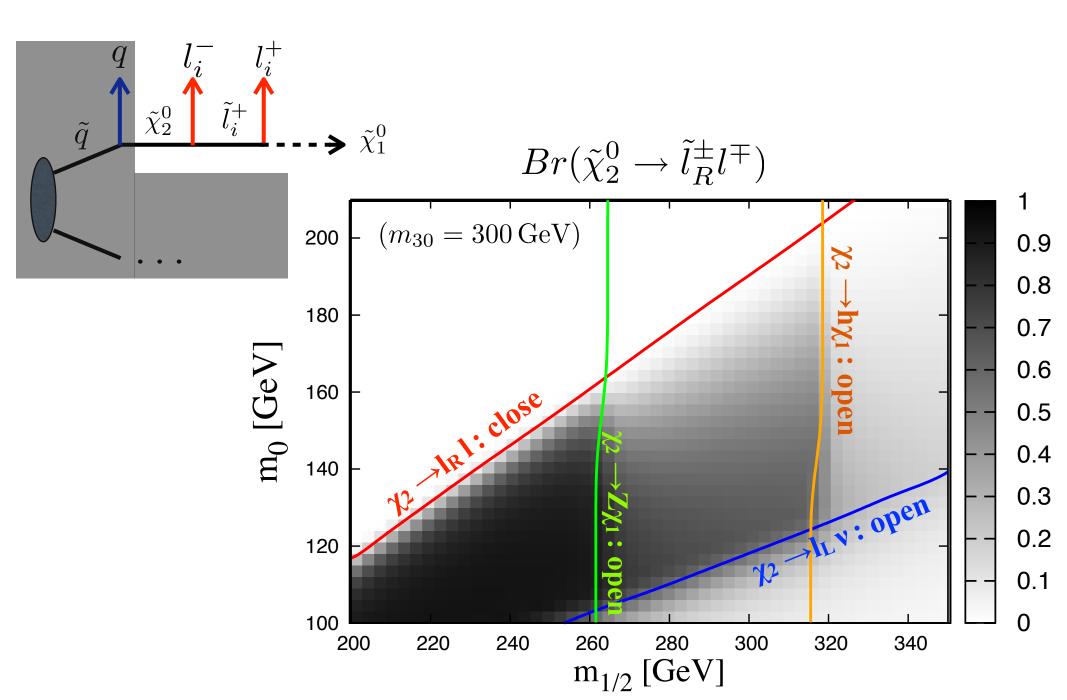


# **Edge method**

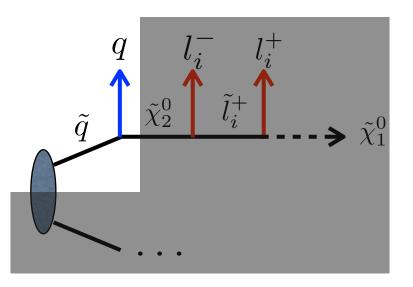
B.C.Allanach, C.G.Lester, M.A.Parker, B.R.Webber '00



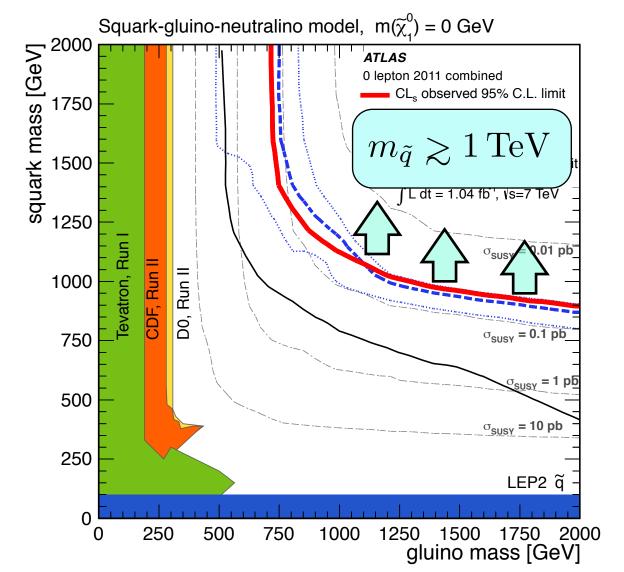
# • The edge method may not be promising ...



## The edge method may not be promising . . .

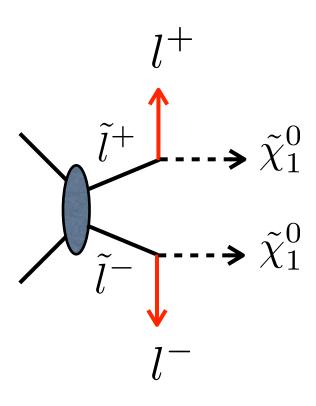


# Large statistics may not be available.



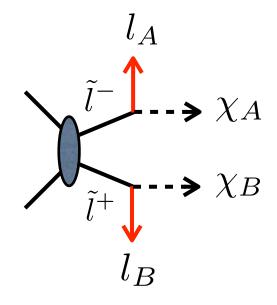
# Slepton pair production

- ullet Unlike squarks, the constraint on the slepton mass is weak:  $m_{ ilde{l}} \gtrsim 100\,{
  m GeV}$
- Observed anomaly in the muon (g-2): light slepton is preferred!



How to extract the masses of the slepton and the neutralino from this event?

#### mT2 method



Let us assume the  $\chi_{A(B)}$  has the mass  $m_{\chi}^{\star}$  and the momentum  $p_{\chi_{A(B)}}^{\star}$ . Then, we have two conditions:

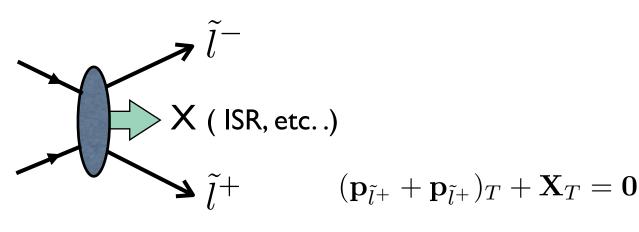
$$\mathbf{p}_{\chi_A}^{\star T} + \mathbf{p}_{\chi_B}^{\star T} = \mathbf{p}_{\text{miss}}^{\text{obs.}T}$$

$$\widetilde{M}_{\tilde{l}}(m_{\chi}^{\star}, p_{\chi_A}^{\star}, p_{\chi_B}^{\star}) \equiv (p_{l_A} + p_{\chi_A}^{\star}(m_{\chi}^{\star}))^2 = (p_{l_B} + p_{\chi_B}^{\star}(m_{\chi}^{\star}))^2$$

$$(2)$$

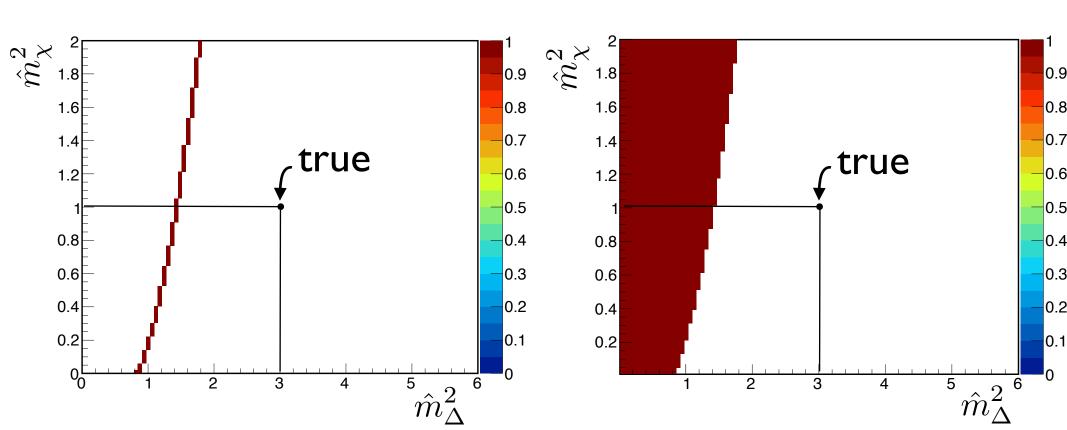
$$M_{T2}(m_{\chi}^{\star}) \equiv \min \left[ \widetilde{M}_{\tilde{l}}(m_{\chi}^{\star}, p_{\chi_A}^{\star}, p_{\chi_B}^{\star}) \right]$$
all possible  $(p_{\chi_A}^{\star}, p_{\chi_B}^{\star})$ 
subject to (1) and (2)

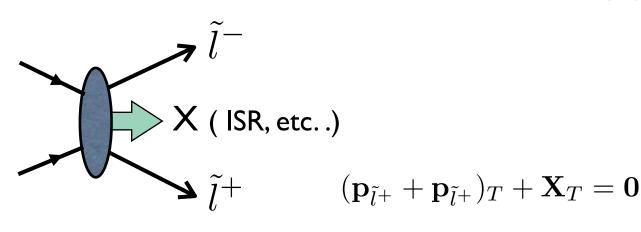
The  $M_{T2}$  provides the upper bound on the  $M_{\rm slep}$  under the assumption on the  $m_\chi$  of  $m^*_\chi$ .



$$\hat{m}_{\Delta}^2 \equiv (m_{\tilde{l}}^{\star 2} - m_{\chi}^{\star 2}) / (m_{\tilde{\chi}}^{\text{true}})^2$$
$$\hat{m}_{\chi}^2 \equiv (m_{\chi}^{\star})^2 / (m_{\tilde{\chi}}^{\text{true}})^2$$

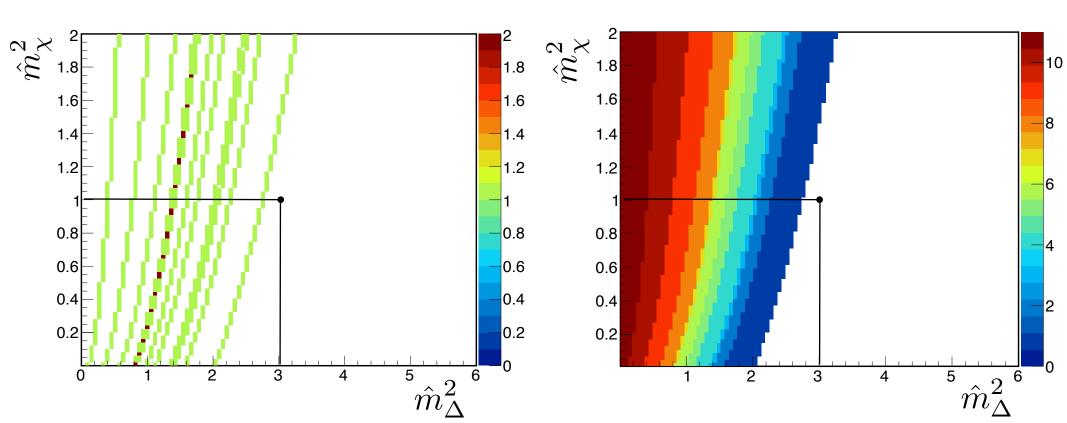
— 1 event with  $|\mathbf{X}_T| = 0$  —

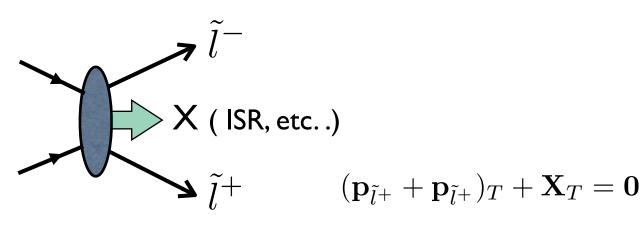




$$\hat{m}_{\Delta}^{2} \equiv (m_{\tilde{l}}^{\star 2} - m_{\chi}^{\star 2}) / (m_{\tilde{\chi}}^{\text{true}})^{2}$$
$$\hat{m}_{\chi}^{2} \equiv (m_{\chi}^{\star})^{2} / (m_{\tilde{\chi}}^{\text{true}})^{2}$$

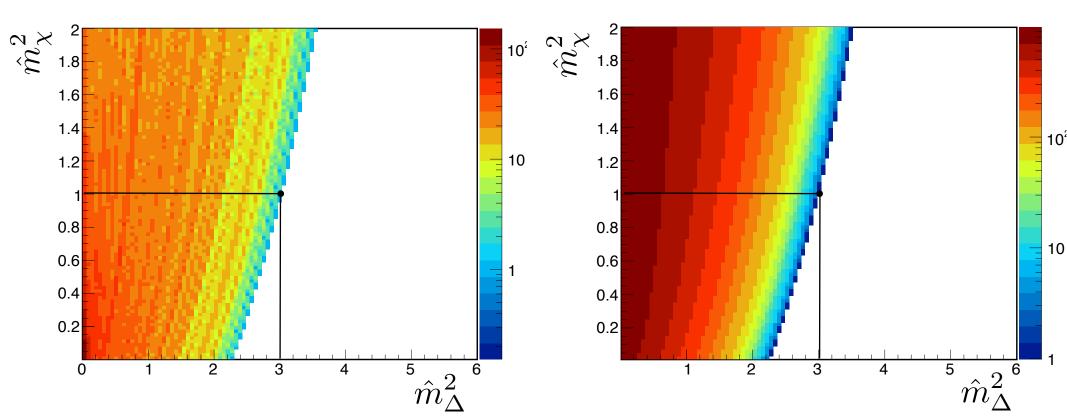
—— 10 event with  $|\mathbf{X}_T| = 0$  ——

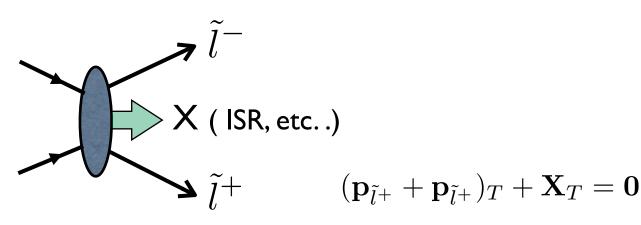




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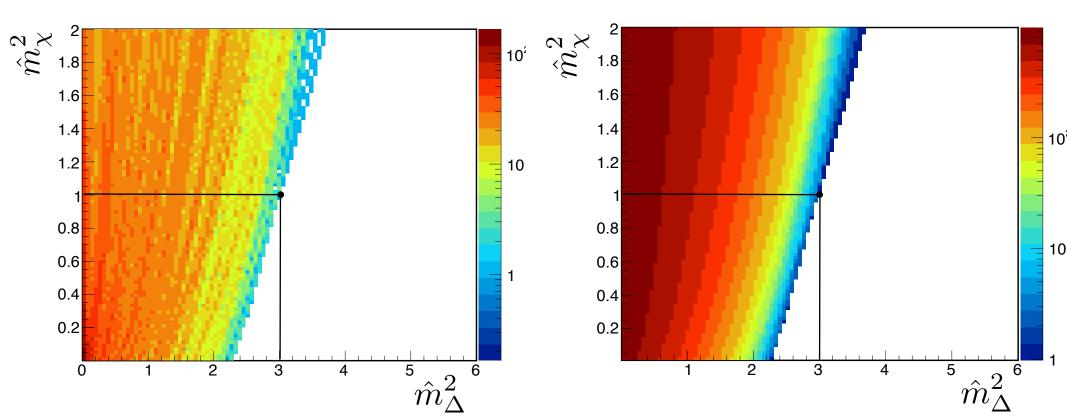
— 1000 event with  $|\mathbf{X}_T| = 0$  —

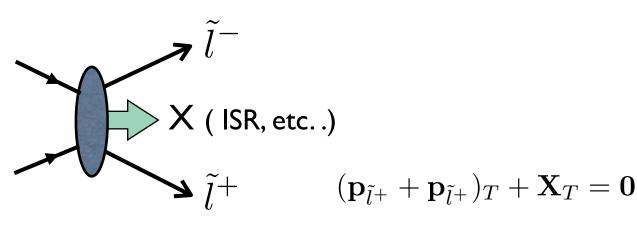




$$\hat{m}_{\Delta}^2 \equiv (m_{\tilde{l}}^{\star 2} - m_{\chi}^{\star 2}) / (m_{\tilde{\chi}}^{\text{true}})^2$$
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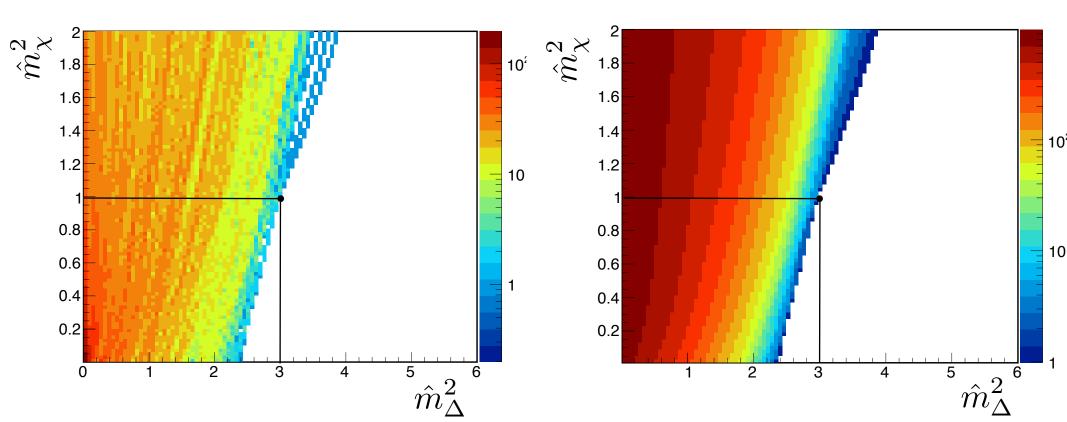
— 1000 event with  $|\mathbf{X}_T| = m_{\tilde{\chi}}^{\mathrm{true}}(\mathrm{Random}[0,1])$  —

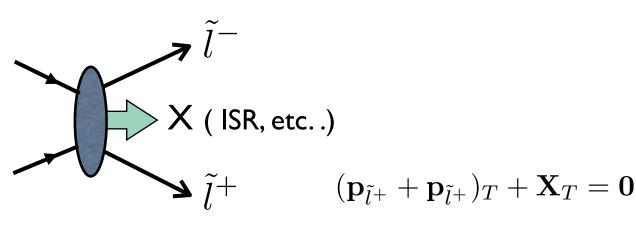




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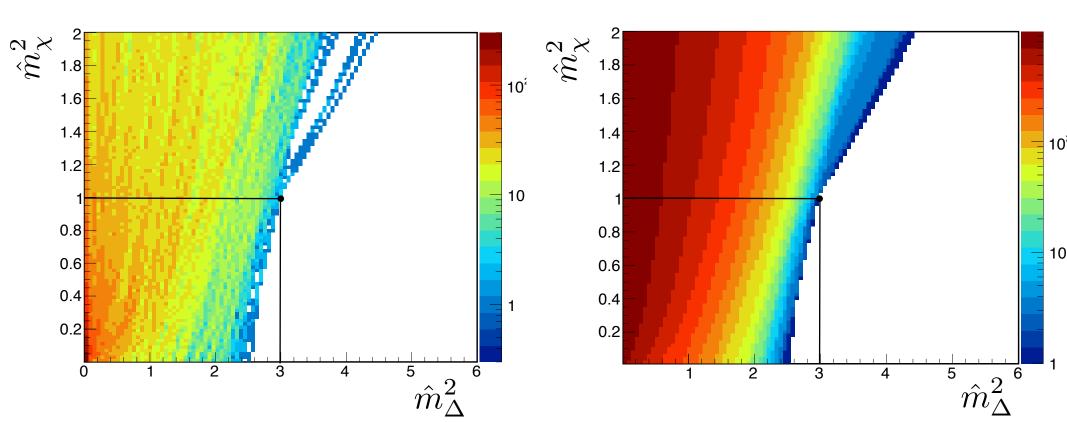
—— 1000 event with  $|\mathbf{X}_T| = m_{\tilde{\chi}}^{\mathrm{true}}(\mathrm{Random}[0,2])$  ——

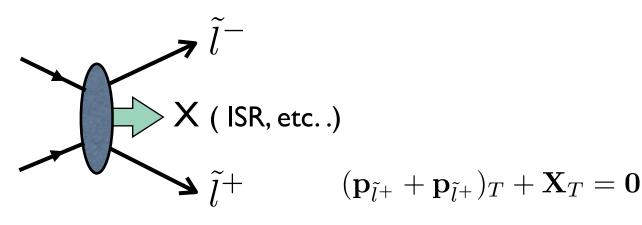




$$\hat{m}_{\Delta}^2 \equiv (m_{\tilde{l}}^{\star 2} - m_{\chi}^{\star 2}) / (m_{\tilde{\chi}}^{\text{true}})^2$$
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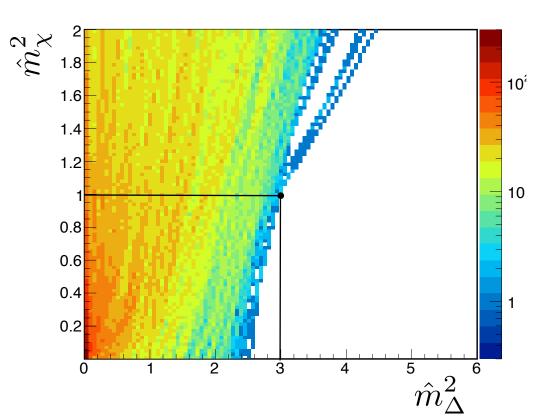
—— 1000 event with  $|\mathbf{X}_T| = m_{\tilde{\chi}}^{\mathrm{true}}(\mathrm{Random}[0,5])$  ——





$$\hat{m}_{\Delta}^2 \equiv (m_{\tilde{l}}^{\star 2} - m_{\chi}^{\star 2}) / (m_{\tilde{\chi}}^{\text{true}})^2$$
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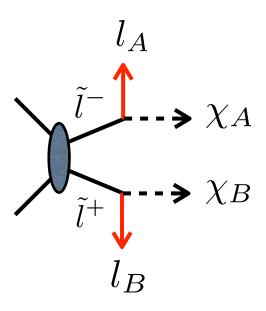
— 1000 event with  $|\mathbf{X}_T| = m_{\tilde{\chi}}^{\mathrm{true}}(\mathrm{Random}[0,5])$  —



- X<sub>T</sub> cannot be very large.
  ( most of the ISR is soft and collinear )
- Small event population at the kink point
- The kink is very fragile against the BG and the momentum mismeasurement.

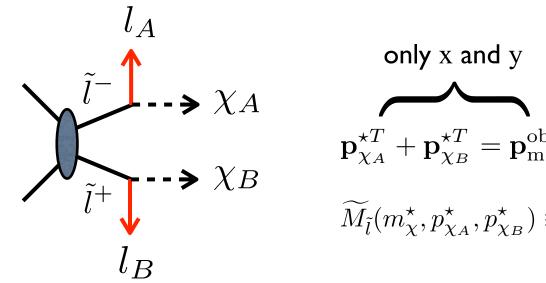
• taking account of more information:

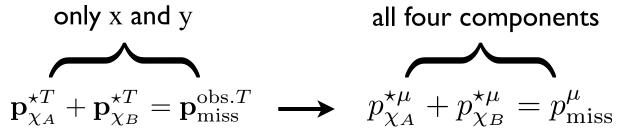
• taking account of more information:



only x and y all four components 
$$\mathbf{p}_{\chi_A}^{\star T} + \mathbf{p}_{\chi_B}^{\star T} = \mathbf{p}_{\mathrm{miss}}^{\mathrm{obs}.T} \longrightarrow p_{\chi_A}^{\star \mu} + p_{\chi_B}^{\star \mu} = p_{\mathrm{miss}}^{\mu}$$
$$\widetilde{M}_{\tilde{l}}(m_{\chi}^{\star}, p_{\chi_A}^{\star}, p_{\chi_B}^{\star}) \equiv (p_{l_A} + p_{\chi_A}^{\star}(m_{\chi}^{\star}))^2 = (p_{l_B} + p_{\chi_B}^{\star}(m_{\chi}^{\star}))^2$$

• taking account of more information:





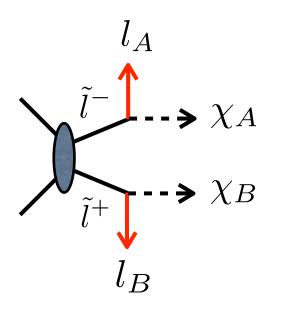
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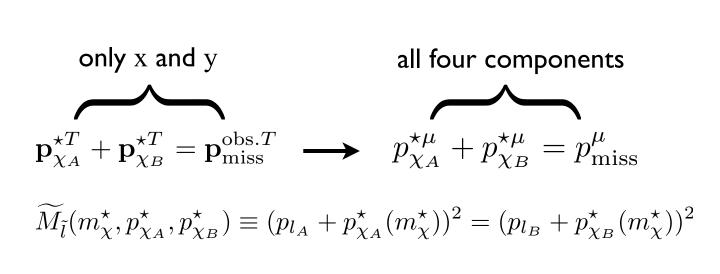
• How can we get  $\,p_{\mathrm{miss}}^{\mu}\,?$ 



$$p_{\rm miss}^{\mu} = p_{\rm initial}^{\mu} - p_{\rm final:visible}^{\mu}$$
 parton momenta are unknown

• taking account of more information:





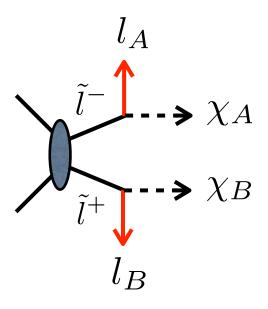
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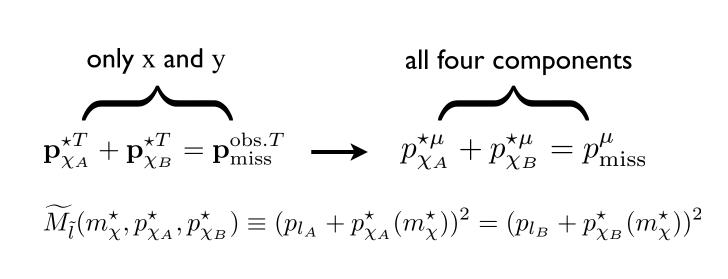


$$p_{\rm miss}^{\mu} = p_{\rm initial}^{\mu} - p_{\rm final:visible}^{\mu}$$
 
$$\mathbf{e^+e^-} \ {\rm energy} \ {\rm is} \ {\rm known}$$



• taking account of more information:





ullet How can we get  $\,p_{
m miss}^{\mu}\,?$ 

$$p_{\rm miss}^{\mu} = p_{\rm initial}^{\mu} - p_{\rm final:visible}^{\mu}$$

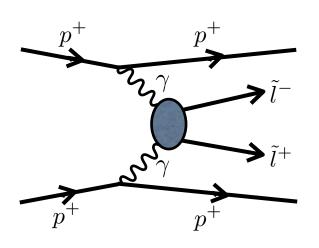




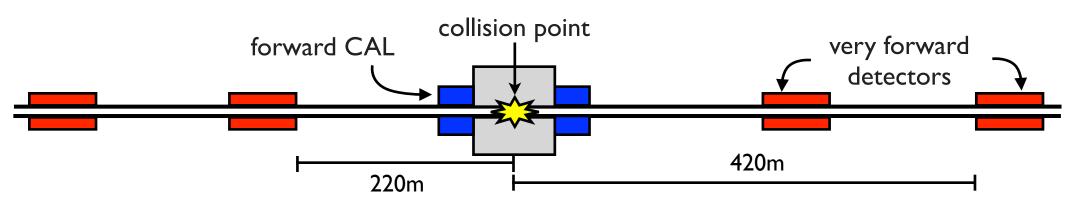


# Central Exclusive Production (CEP) and forward proton tagging

CEP forward proton tagging 
$$p_{\rm miss}^{\mu} = p_{\rm initial}^{\mu} - p_{\rm final:visible}^{\mu}$$



- The proton-proton collisions may create slepton pairs through the two photons, without breaking the protons down.
- ◆ Very clean final state: 2 sleptons + 2 protons remained intact,
   no soft particles in the forward CAL.
- Provided the very forward detectors installed at 220m and 420m away from the collision point (ATLAS forward physics (AFP) project), the energy of the final state protons can be measured with a good accuracy (a few % relative energy resolution).



#### **Cross sections**

• The cross section can be calculated by using the "equivalent photon approx".

$$\begin{split} \sigma(pp \to pXp) &= \int d\sigma_{\gamma\gamma \to X}(m_{\gamma\gamma}, Q_1^2, Q_2^2) \prod_{i=1,2} \left[ \frac{dN(E_{\gamma_i}, Q_i^2)}{dQ_i^2} dQ_i^2 dE_{\gamma_i} \right] \delta(m_{\gamma\gamma} = \sqrt{(p_{\gamma_1} + p_{\gamma_2})^2}) dm_{\gamma\gamma} \\ &\sim \int d\sigma_{\gamma\gamma \to X}(m_{\gamma\gamma}) \prod_{i=1,2} \left[ f(E_{\gamma_i}) dE_{\gamma_i} \right] \delta(m_{\gamma\gamma} = 2\sqrt{E_{\gamma_1} + E_{\gamma_2}}) dm_{\gamma\gamma} \\ &= \int d\sigma_{\gamma\gamma \to X}(m_{\gamma\gamma}) \frac{dL^{\gamma\gamma}}{dm_{\gamma\gamma}} dm_{\gamma\gamma} \\ &= 100 \\ &\downarrow 0.1 \\ &\downarrow$$

#### **Cross sections**

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$$\sigma(pp \to pXp) = \int d\sigma_{\gamma\gamma \to X}(m_{\gamma\gamma}, Q_1^2, Q_2^2) \prod_{i=1,2} \left[ \frac{dN(E_{\gamma_i}, Q_i^2)}{dQ_i^2} dQ_i^2 dE_{\gamma_i} \right] \delta(m_{\gamma\gamma} = \sqrt{(p_{\gamma_1} + p_{\gamma_2})^2}) dm_{\gamma\gamma}$$

$$\sim \int d\sigma_{\gamma\gamma \to X}(m_{\gamma\gamma}) \prod_{i=1,2} \left[ f(E_{\gamma_i}) dE_{\gamma_i} \right] \delta(m_{\gamma\gamma} = 2\sqrt{E_{\gamma_1} + E_{\gamma_2}}) dm_{\gamma\gamma}$$

$$= \int d\sigma_{\gamma\gamma \to X}(m_{\gamma\gamma}) \frac{dL^{\gamma\gamma}}{dm_{\gamma\gamma}} dm_{\gamma\gamma}$$

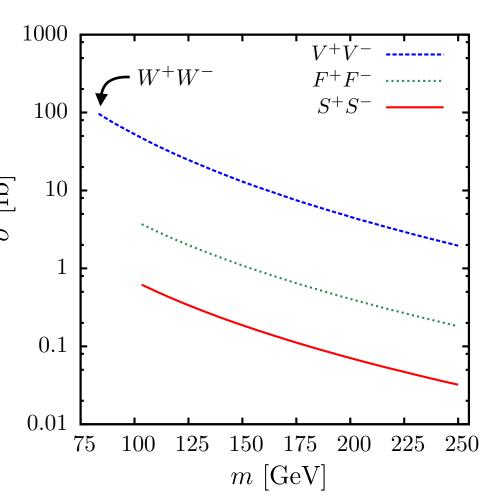
$$1000$$

• The VFDs can only measure the final state protons with:

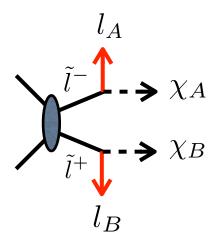
$$0.0015 < \frac{E_p^{\text{ini}} - E_p^{\text{final}}}{E_p^{\text{ini}}} < 0.15$$

• The cross sections after the proton tagging acceptance:

$W^+W^- \to l^+l^-\nu\bar{\nu}$	1.00 fb
$\tilde{l}^+\tilde{l}^- \ (m_{\tilde{l}} = 150 \text{GeV})$	$0.15\mathrm{fb}$



# Finding the allowed mass region



all four components

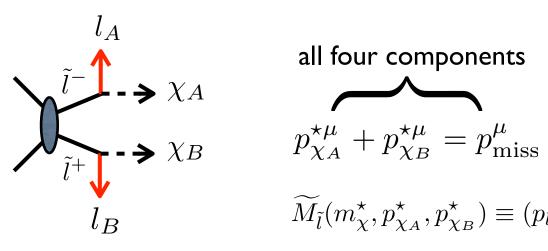
$$p_{\chi_A}^{\star\mu} + p_{\chi_B}^{\star\mu} = p_{\text{miss}}^{\mu}$$

$$\widetilde{M}_{z}(m^{\star}, n^{\star}, n^{\star}) = (m + m)$$

$$\widetilde{M}_{\tilde{l}}(m_{\chi}^{\star}, p_{\chi_A}^{\star}, p_{\chi_B}^{\star}) \equiv (p_{l_A} + p_{\chi_A}^{\star}(m_{\chi}^{\star}))^2 = (p_{l_B} + p_{\chi_B}^{\star}(m_{\chi}^{\star}))^2$$

• Given  $p_{l_A}^{\mu}$ ,  $p_{l_B}^{\mu}$ ,  $p_{\text{miss}}^{\mu}$ , which regain in  $(\tilde{M}_{\tilde{l}}, m_{\chi}^{\star})$  plane is consistent with the above conditions?

# Finding the allowed mass region



$$p_{\chi_A}^{\star\mu} + p_{\chi_B}^{\star\mu} = p_{\text{miss}}^{\mu}$$

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• Given  $p_{l_A}^{\mu}$ ,  $p_{l_B}^{\mu}$ ,  $p_{\text{miss}}^{\mu}$ , which regain in  $(\tilde{M}_{\tilde{l}}, m_{\chi}^{\star})$  plane is consistent with the above conditions?

$$\overline{m}_{\chi}^2 \le c_a (\overline{m}_{\Delta}^2)^2 + c_b \overline{m}_{\Delta}^2 + c_c \qquad \overline{m}_{\chi}^2 = \frac{m_{\chi}^2}{p_{l_A} \cdot p_{l_B}} \quad \overline{m}_{\Delta}^2 = \frac{M_{\tilde{l}}^2 - m_{\chi}^2}{p_{l_A} \cdot p_{l_B}}$$

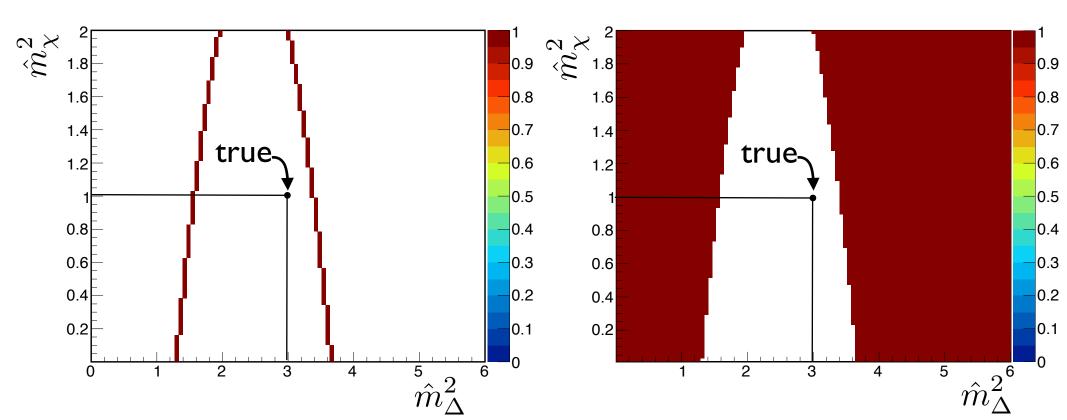
$$c_a = \frac{1}{4} \frac{(\Lambda_1 + \Lambda_2)^2 - 2\Lambda_{\gamma\gamma}}{\Lambda_{\gamma\gamma} - 2\Lambda_1\Lambda_2} \qquad c_b = \frac{1}{2} (\Lambda_1 + \Lambda_2 - 2) \qquad c_c = \frac{1}{4} (\Lambda_{\gamma\gamma} - 2\Lambda_1\Lambda_2)$$

$$\Lambda_1 \equiv \frac{p_{\gamma\gamma} \cdot p_{l_1}}{p_{l_1} \cdot p_{l_2}} \quad \Lambda_2 \equiv \frac{p_{\gamma\gamma} \cdot p_{l_2}}{p_{l_1} \cdot p_{l_2}} \quad \Lambda_{\gamma\gamma} \equiv \frac{m_{\gamma\gamma}^2}{p_{l_1} \cdot p_{l_2}} \quad p_{\gamma\gamma} = p_{l_A} + p_{l_B} + p_{\text{miss}} \quad m_{\gamma\gamma}^2 = p_{\gamma\gamma}^2$$

$$\hat{m}_{\Delta}^2 \equiv (m_{\tilde{l}}^{\star 2} - m_{\chi}^{\star 2}) / (m_{\tilde{\chi}}^{\text{true}})^2$$
$$\hat{m}_{\chi}^2 \equiv (m_{\chi}^{\star})^2 / (m_{\tilde{\chi}}^{\text{true}})^2$$

• Unlike the inelastic case (only  $m_{\Delta}^{upper}$ ), the both upper and lower bounds on  $m_{\Delta}$  are obtained, moreover the upper bound on  $m_{\chi}$  is also obtained.

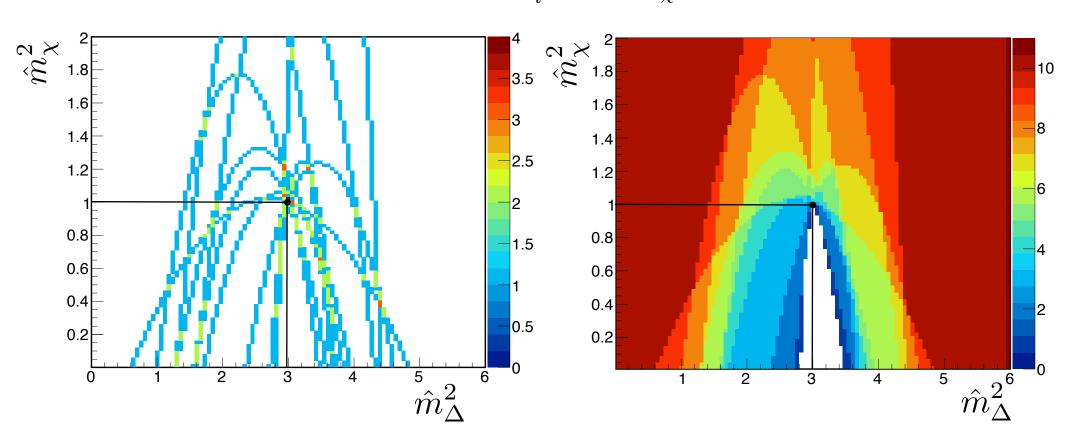
— 1 event with  $|\mathbf{p}_{\tilde{i}}^{\text{initial}}| = m_{\tilde{\chi}}^{\text{true}}(\text{Random}[0,2])$  ——



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- Unlike the inelastic case (only  $m_{\Delta}^{upper}$ ), the both upper and lower bounds on  $m_{\Delta}$  are obtained, moreover the upper bound on  $m\chi$  is also obtained.
- The allowed region shrinks rapidly as the number of events increases.

—— 10 event with  $|\mathbf{p}_{\tilde{i}}^{\text{initial}}| = m_{\tilde{\chi}}^{\text{true}}(\text{Random}[0,2])$  ——



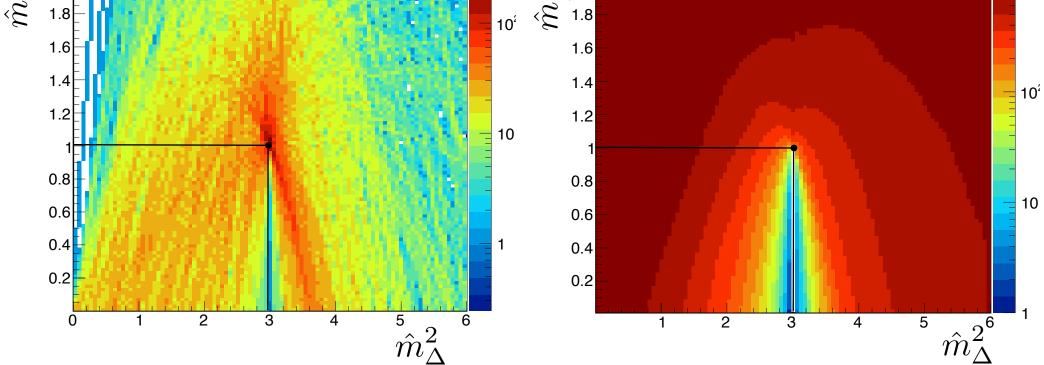
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- The allowed region shrinks rapidly as the number of events increases.
- The population of the events at the true mass point is large ( $\rightarrow$  stable against the BG and errors).

 $|\mathbf{p}_{\tilde{i}}^{\mathrm{initial}}| = m_{\tilde{\chi}}^{\mathrm{true}}(\mathrm{Random}[0, 2])$ 1000 event with 10<sup>2</sup> 1.4 10<sup>2</sup> 1.2 1.2 10 8.0 8.0 10 0.6 0.6 0.4 0.4 0.2 0.2 0 2 3 2

$$\hat{m}_{\Delta}^2 \equiv (m_{\tilde{l}}^{\star 2} - m_{\chi}^{\star 2}) / (m_{\tilde{\chi}}^{\text{true}})^2$$
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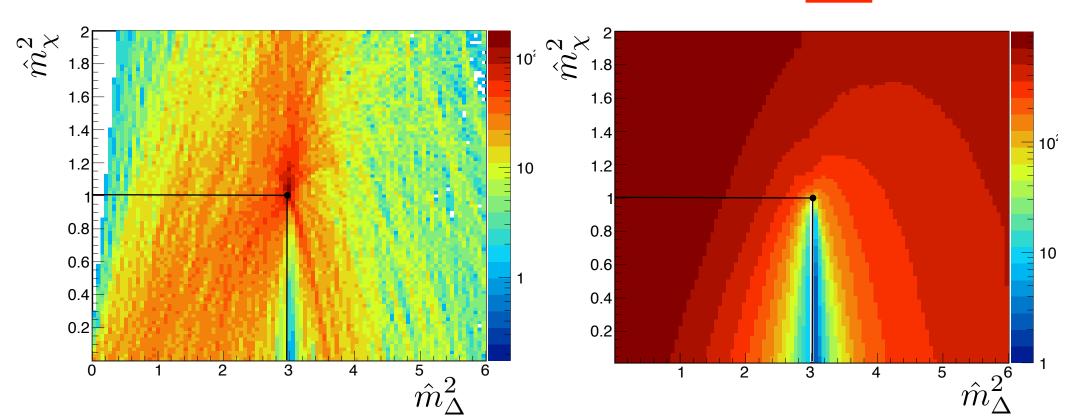
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- The distribution depends on the distribution of the  $p_{slep}^{ini}$  (or equivalently on the CoM of the  $\gamma\gamma$ ).



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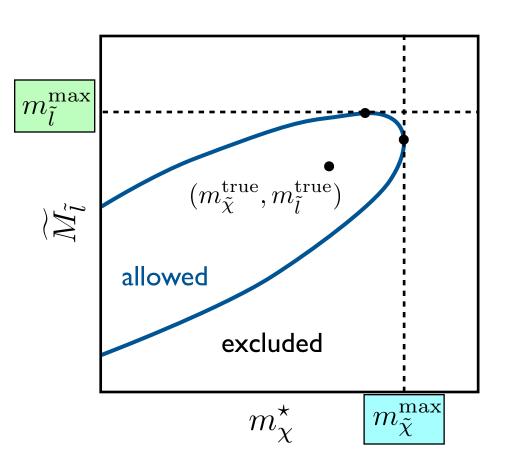
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—— 1000 event with  $|\mathbf{p}^{ ext{initial}}_{ ilde{l}}| = m^{ ext{true}}_{ ilde{\chi}}( ext{Random}[0,10])$  ——



#### Some variables

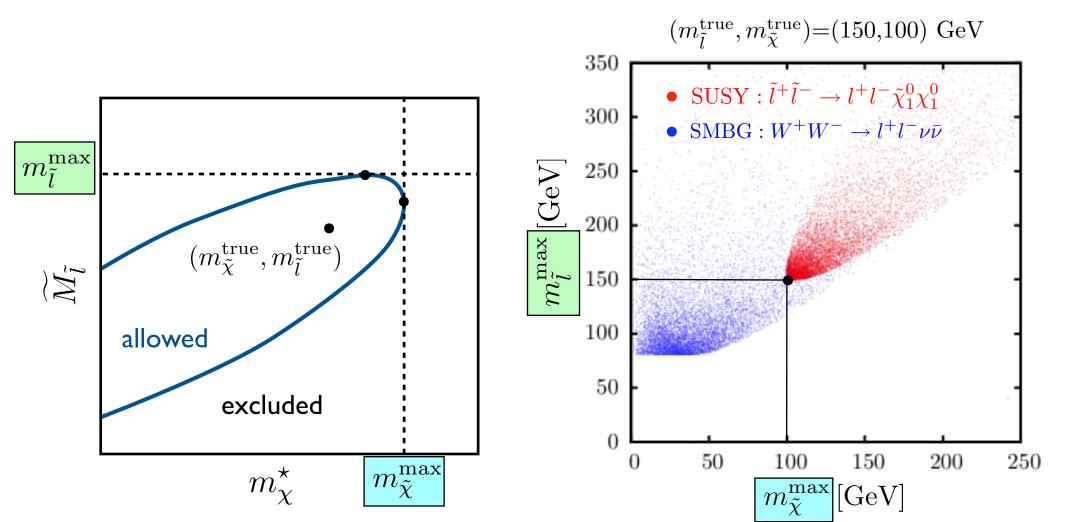
• The event-by-event upper bounds on the  $m_{slep}$  and the  $m_\chi$  can be defined, respectively.



$$(m_{\tilde{l}}^{\max})^2 = (p_{l_1} \cdot p_{l_2}) \times \left(c_c - \frac{(c_b + 1)^2}{4c_a}\right)$$
  
 $(m_{\tilde{\chi}}^{\max})^2 = (p_{l_1} \cdot p_{l_2}) \times \left(c_c - \frac{c_b^2}{4c_a}\right)$ 

#### Some variables

- The event-by-event upper bounds on the  $m_{slep}$  and the  $m_\chi$  can be defined, respectively.
- By looking at the  $m_{slep}^{max}$  and the  $m_{\chi}^{max}$  simultanelously, the SMBG can be significantly removed.

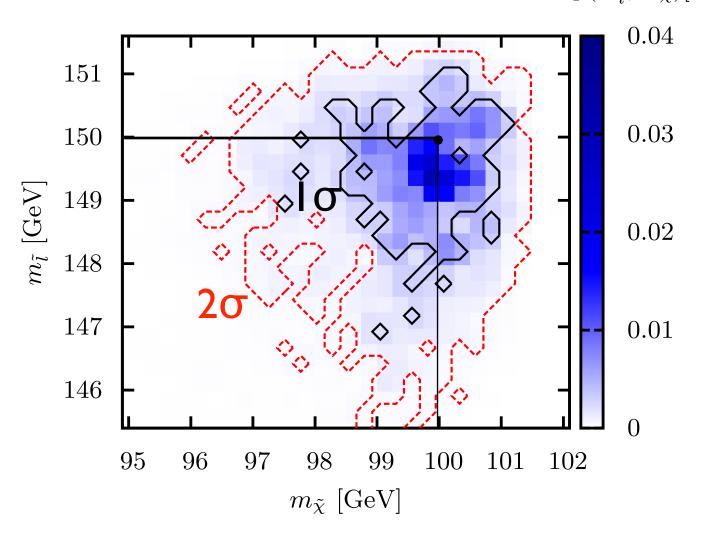


# **Numerical analysis**

- The CEP events are generated by the PhoCEP program, which takes into account of the full spin correlation for production and subsequent decays.
- The lepton momentum cut, the detector acceptance and resolutions are taken account. ( $|p_T^{lep}|>10$ GeV,  $|\eta_{lep}|<2.5$ , Resolution: 10% for lepton, 4% for the tagged proton)
- $(m_{slep}, m_{\chi}) = (150, 100)$  GeV, 14TeV LHC with 300 fb<sup>-1</sup> is assumed.
- The 216 and 38 events are generated for the SMBG and SUSY signal, respectively and used for the pseudo experiment.
- The signal window is defined by  $m_{slep}^{max}$ = [130,230] and  $m_{\chi}^{max}$ = [80,180] reducing the events 216→24 (SMBG) and 38→36 (SUSY), respectively.
- The 2D probability density distributions of the  $(m_{slep}{}^{max}, m_{\chi}{}^{max})$  are estimated by generating  $10^6$  events for various  $(m_{slep}{}^{true}, m_{\chi}{}^{true})$  assumptions and see which assumption can fit the  $(m_{slep}{}^{max}, m_{\chi}{}^{max})$  distribution observed in the pseudo experiment the best.

#### Result

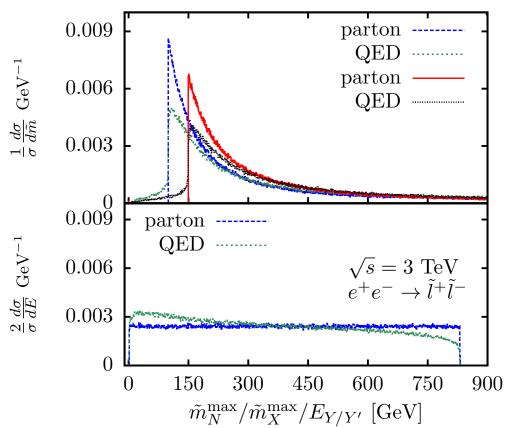
 $p(m_{\tilde{l}}, m_{\tilde{\chi}})[25 \text{GeV}]^2$ 



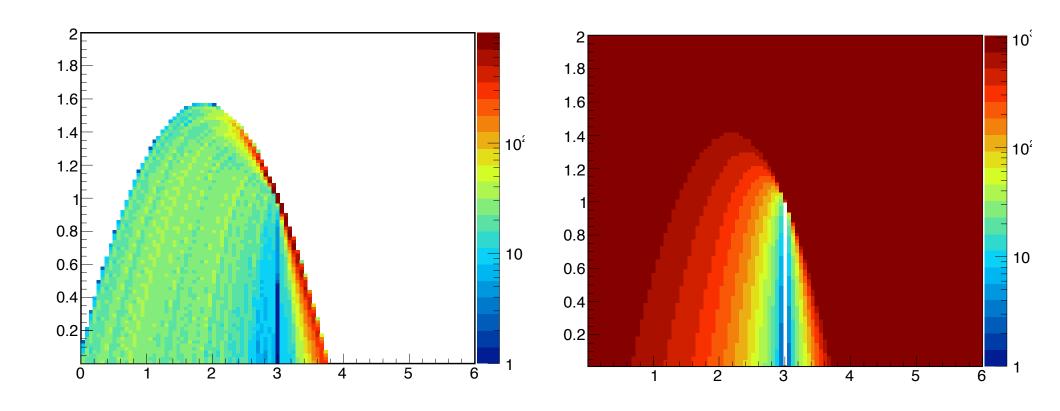
• The expected accuracy of the mass determination is around 1.5 (2.5) GeV for I(2)  $\sigma$  level for both the slepton and the neutralino.

# Summary

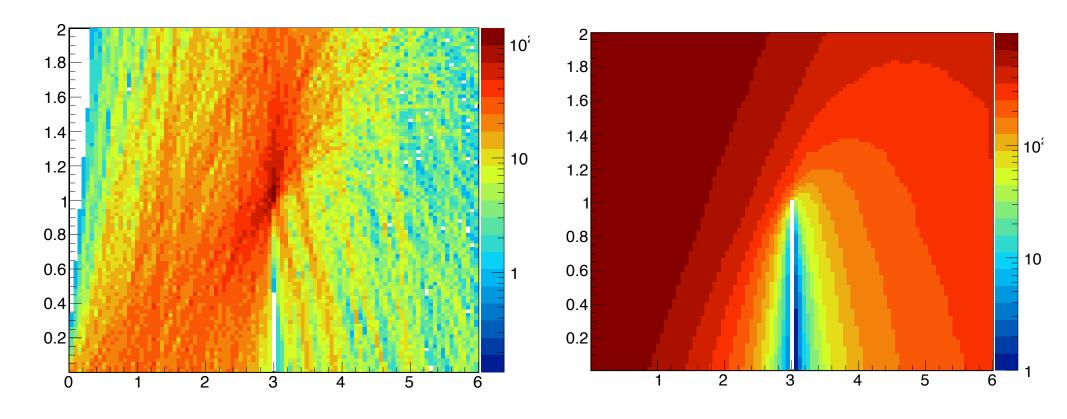
- By looking at the central exclusive slepton pair production with forward proton tagging, all the four components of the sum of the neutralino momenta can be deduced, allowing us to obtain analytically the allowed mass region by all the kinematic constraints.
- Despite the poor statistics of CEP, the new technique for the mass determination is able to determine the masses of both the slepton and the neutralino a few GeV accuracy at 1 or 2  $\sigma$  level.
- This method may improve the traditional slepton, neutralino mass measurement at the ILC, because of making full use of the available kinematic constraints.



# pback = 0



# pback = 10000



# pback = 100000

