

Beyond the Standard Model from a Neutrino Perspective

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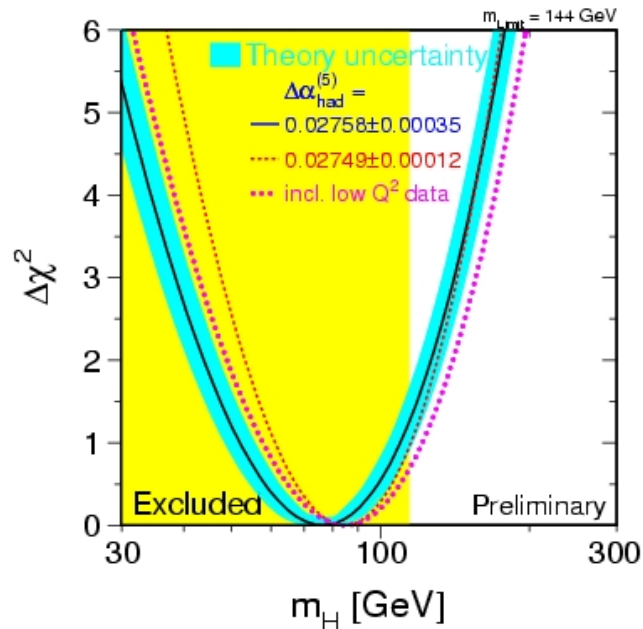


DESY THEORY WORKSHOP
25 - 28 September 2012

**Lessons from the first phase
of the LHC**

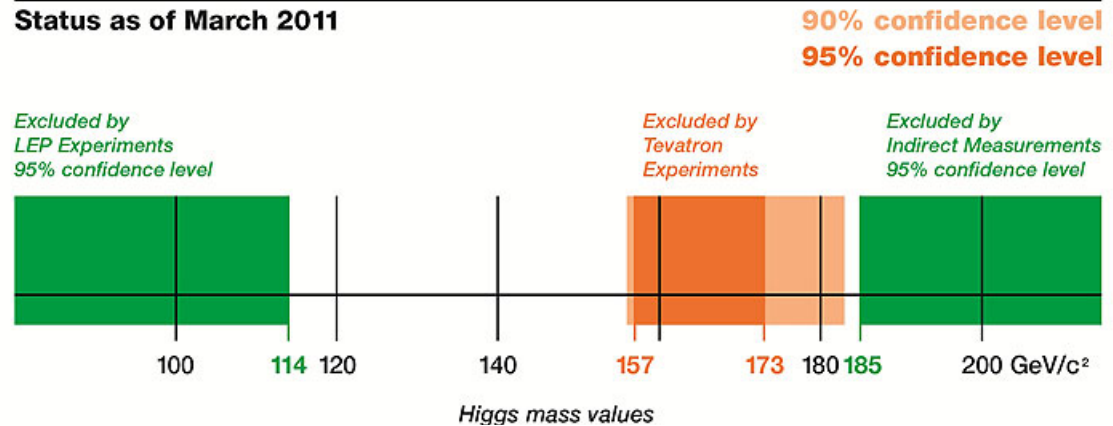


The SM works perfectly



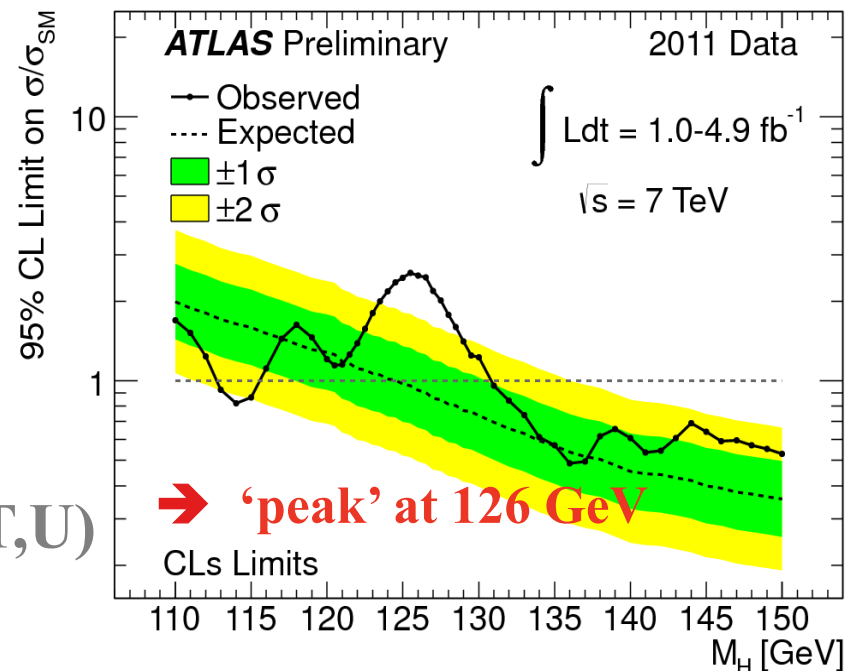
Search for the Higgs Particle

Status as of March 2011

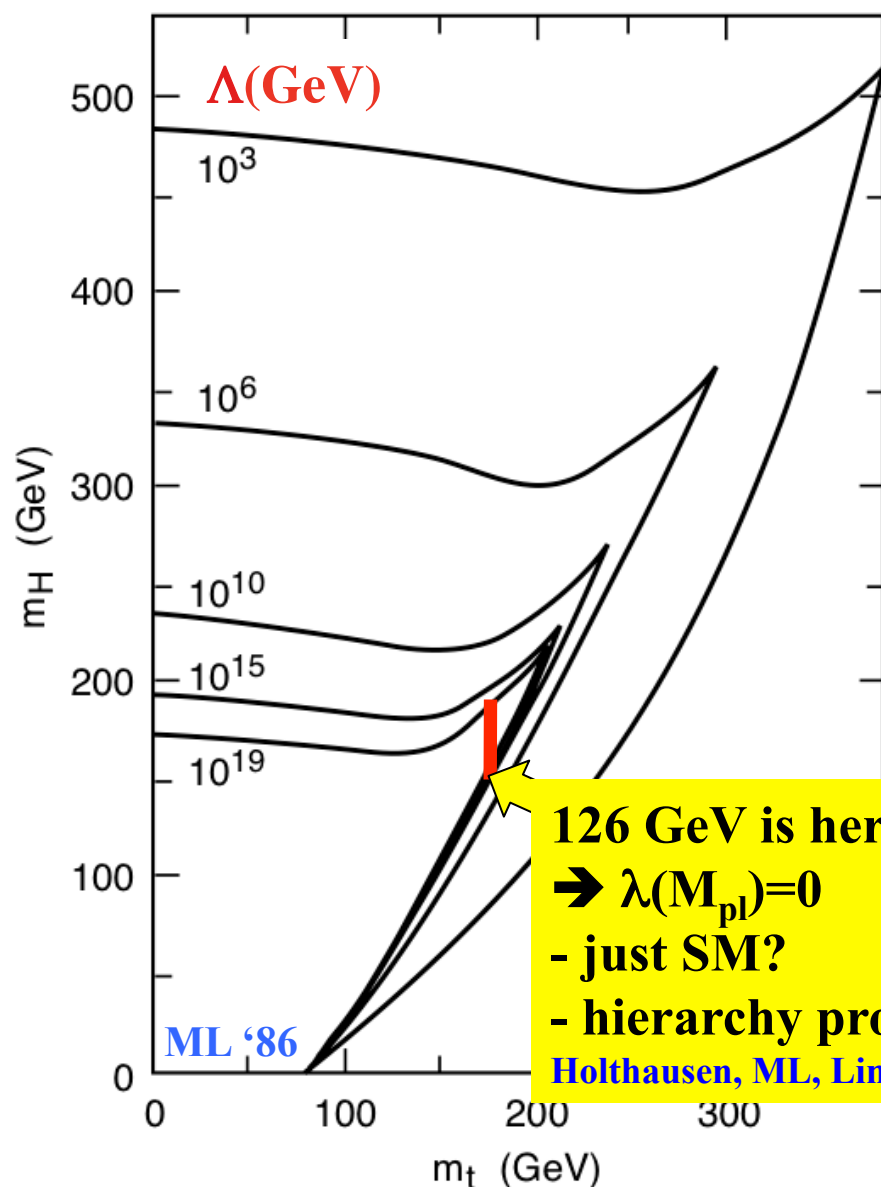


mass range was shrinking...

- if SM Higgs $\rightarrow$ light
 - no (clear) sign for anything else
 - no signs in quantum effects (S,T,U)
- $\rightarrow$ just the SM?

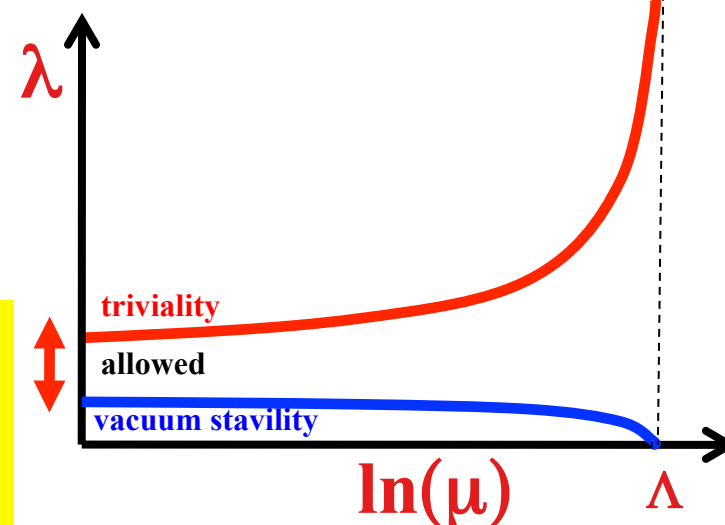


Triviality and Vacuum Stability



$$126 \text{ GeV} < m_H < 174 \text{ GeV}$$

SM does not exist w/o embedding
 - U(1) coupling, Higgs self-coupling



$\rightarrow$ RGE arguments seem to work
 $\rightarrow$ we need some embedding

The SM works perfect but must be extended....

- Many theoretical reasons for BSM physics...

- **Hierarchy problem:** separation of two scalar scales is unstable
- SUSY, DSB, gauge extensions, new ideas, Planck scale physics?
- ???

- Experimental facts:

- SM must be amended by neutrino masses → SM+
- SM cannot explain Baryon Asymmetry of the Universe
neutrinos → leptogenesis = one of the best BAU explanations
- **Dark Matter**
- an extra particle is needed which is DM
- particles connected to the hierarchy problem, strong CP, ...

???

→ massive neutrinos require new physics → BSM → connections?

The Standard 3 Neutrino Framework

Mass & mixing parameters: m_1 , Δm_{21}^2 , $|\Delta m_{31}^2|$, $\text{sign}(\Delta m_{31}^2)$

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix} \text{diag}(e^{i\alpha}, e^{i\beta}, 1)$$

Questions:

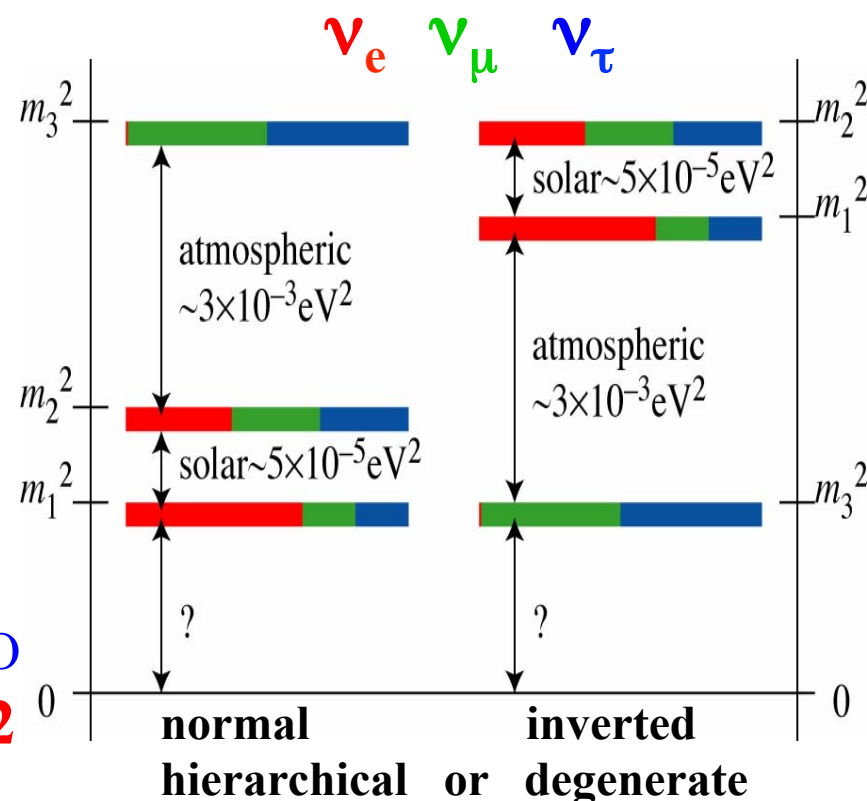
- Dirac / Majorana,
- mass scale & ordering: m_1 , $\text{sgn}(\Delta m_{31}^2)$
- θ_{23} maximal?
- leptonic CP violation
- 3 flavour unitarity?
- why 3 generations ? $\leftrightarrow$ steriles?

→ Recent improvements:

θ_{13} is determined: → $\theta_{13} \simeq 9 \pm 1^\circ$

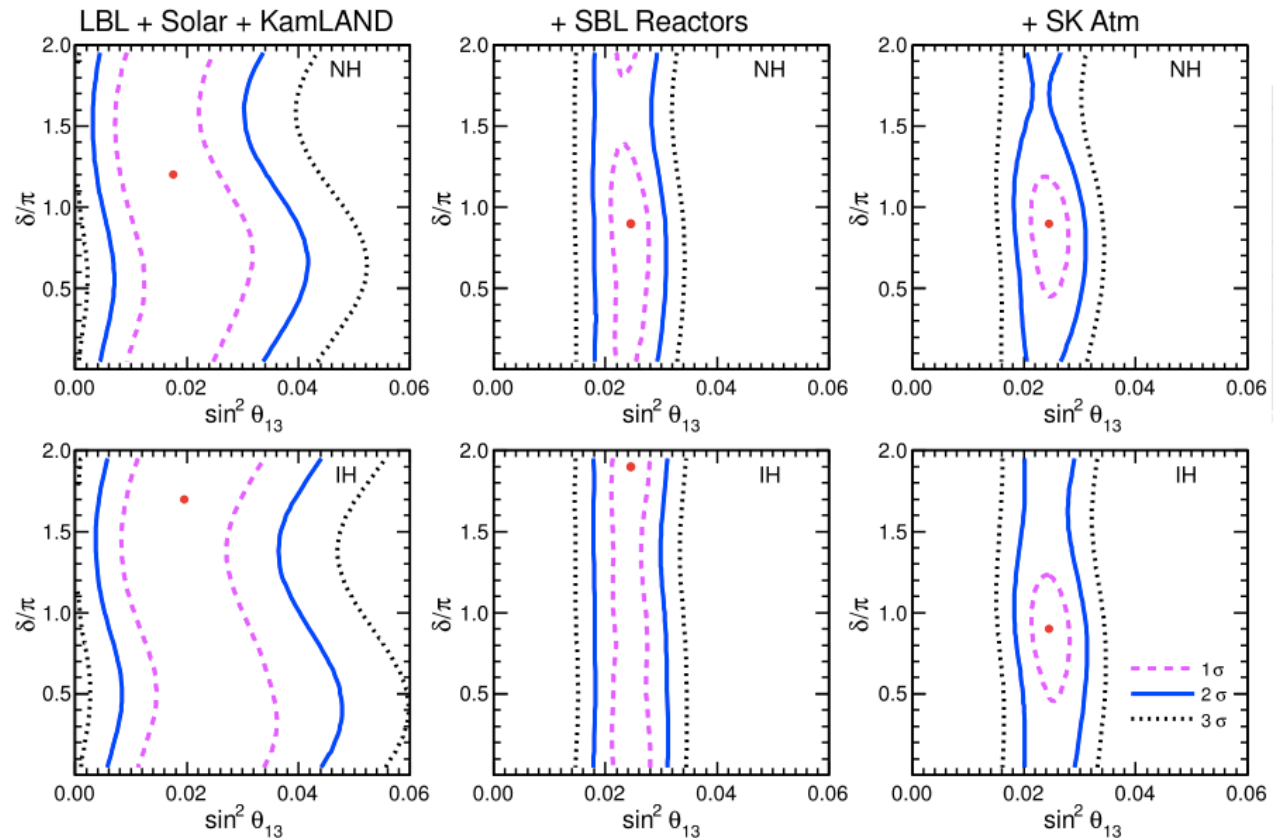
T2K, MINOS, Double Chooz, Daya Bay, RENO

θ_{23} : Indications for deviation from $\pi/2$



normal
hierarchy

inverted
hierarchy



$\sim 1\sigma$ preference for $\delta \sim \pi$ Fogli et al. , others $\rightarrow$ first glimpse?
 $\rightarrow$ enhances the interference oscillation term and gives extra
 electron appearance for atmospheric events O(GeV),
 “explaining” part of the persisting SK electron excess.

New Physics: Neutrino Mass Terms

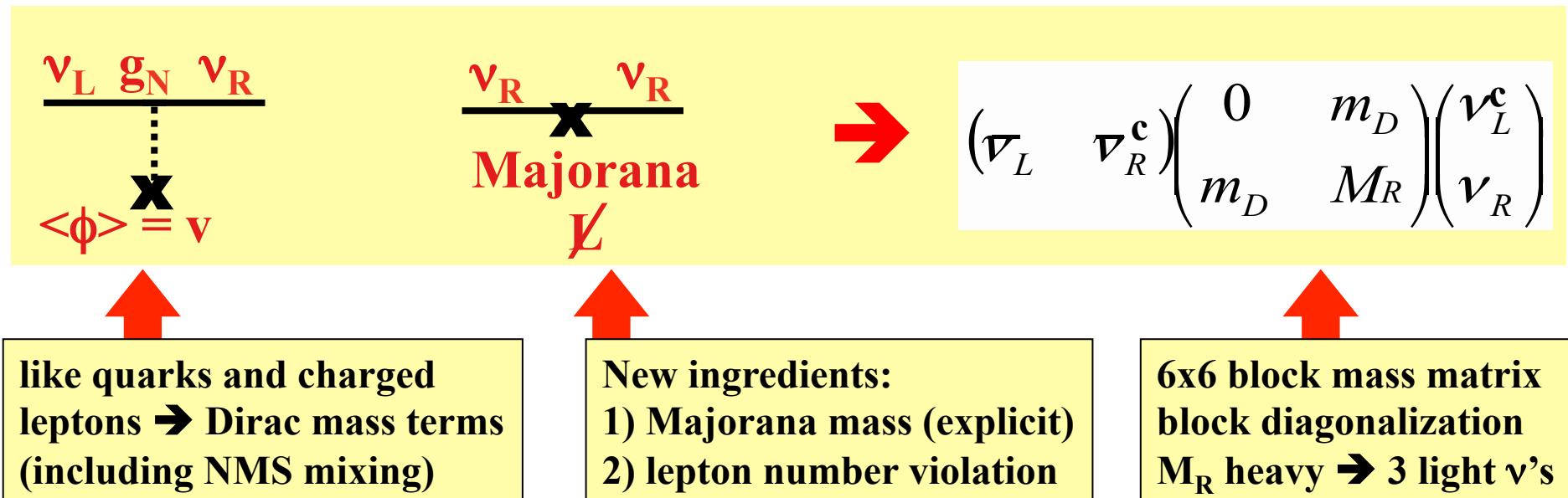
$$\text{SM} \sim m \bar{L} \phi R = (2,1)$$

→ new fields



1) Simplest possibility:
add 3 right handed neutrino fields

Field	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$
$L_Q = \begin{pmatrix} l_u \\ l_d \end{pmatrix}$	3	2	1/3
r_u	3	1	4/3
r_d	3	1	-2/3
$L_L = \begin{pmatrix} l_\nu \\ l_e \end{pmatrix}$	1	2	-1
$r_\nu ???$	1	1	0
r_e	1	1	-2



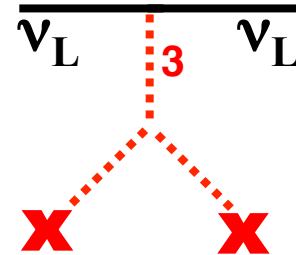
NEW ingredients, 9 parameters → SM+ and sea-saw

2) Maybe 3+N right handed neutrino fields

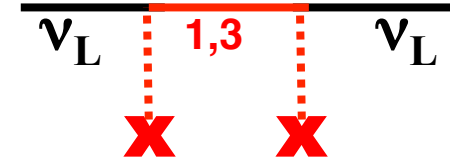
→ (6+N) x (6+N) mass matrix

→ how many of the 6+N eigenvalues are light (also for N=0)

3) new: scalar triplets (3_L) or fermionic 1_L or 3_L



→ left-handed Majorana mass term:



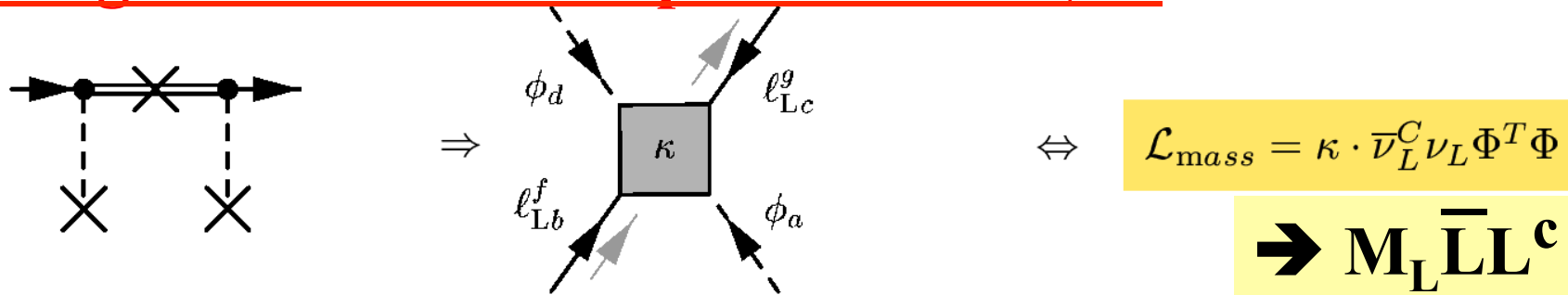
$$\rightarrow M_L \bar{L} L^c$$

4) Both ν_R and new singlets / triplets:

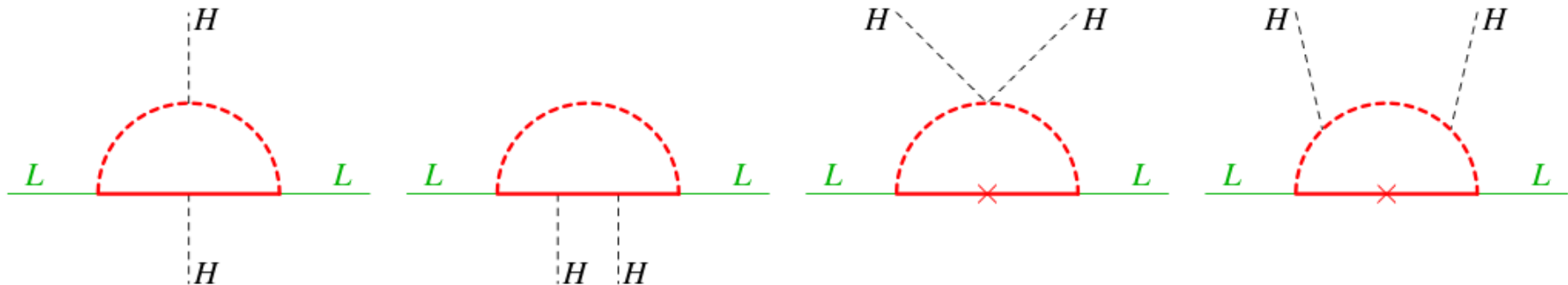
→ see-saw type II, III

$$m_\nu = M_L - m_D M_R^{-1} m_D^T$$

5) Higher dimensional operators: d=5, ...



6) Radiative neutrino mass generation



- Lagrangians where neutrino masses are forbidden at tree level
 $\leftrightarrow$ symmetries
- interactions induce neutrino mass terms

7) GUT's (and SUSY GUTs)

Gauge unification suggests that some GUT exists

Requirements:

gauge unification

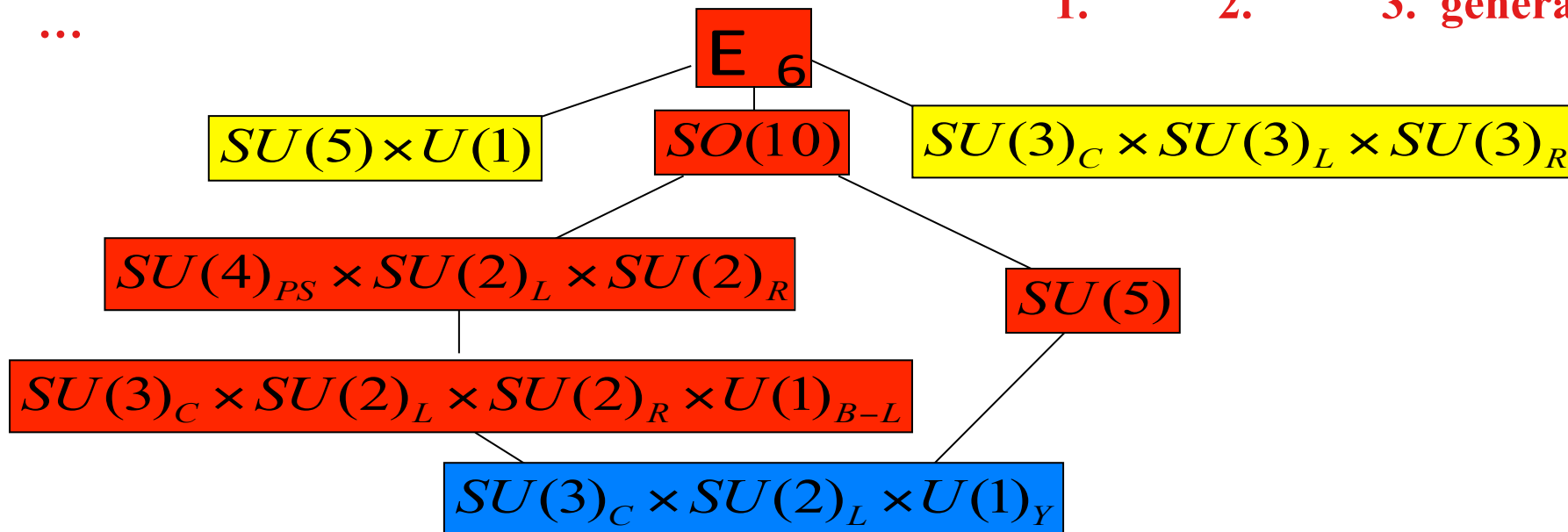
particle multiplets $\leftrightarrow \nu_R$

proton decay

...

Quarks	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
	u ~5	c ~1350	t 175000
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$
	d ~9	s ~175	b ~4500
Leptons	0?	0?	0?
	ν_1	ν_2	ν_3
	e 0.511	μ 105.66	τ 1777.2

1. 2. 3. generation



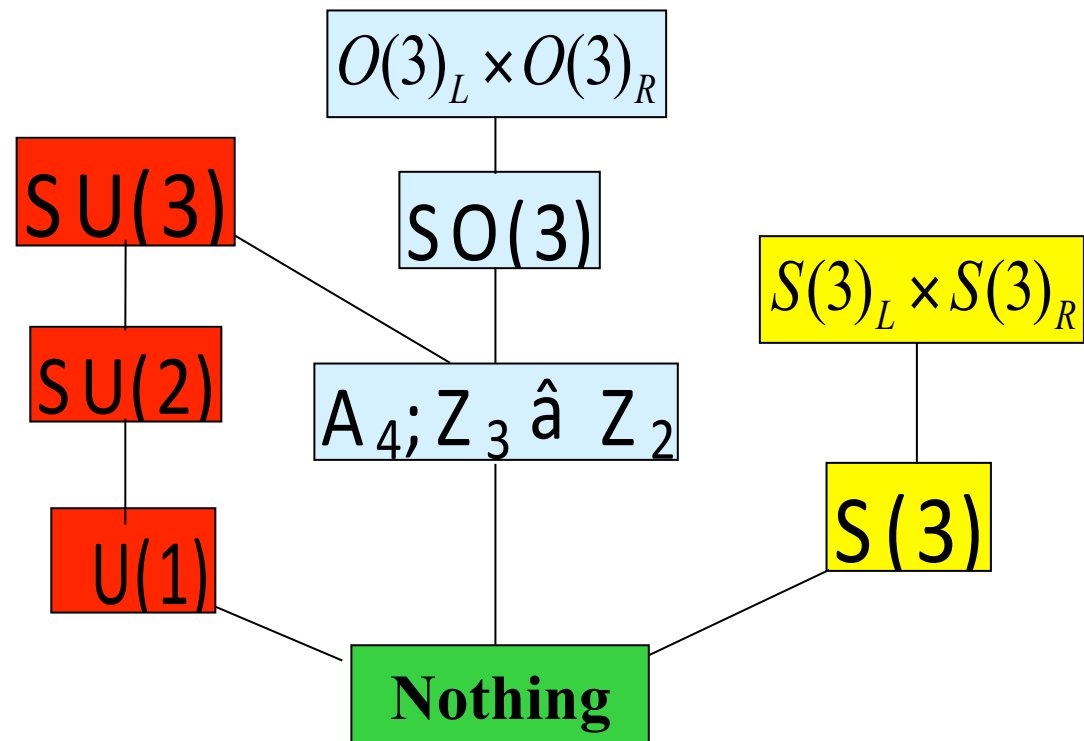
many possibilities...

7) Flavour Symmetries

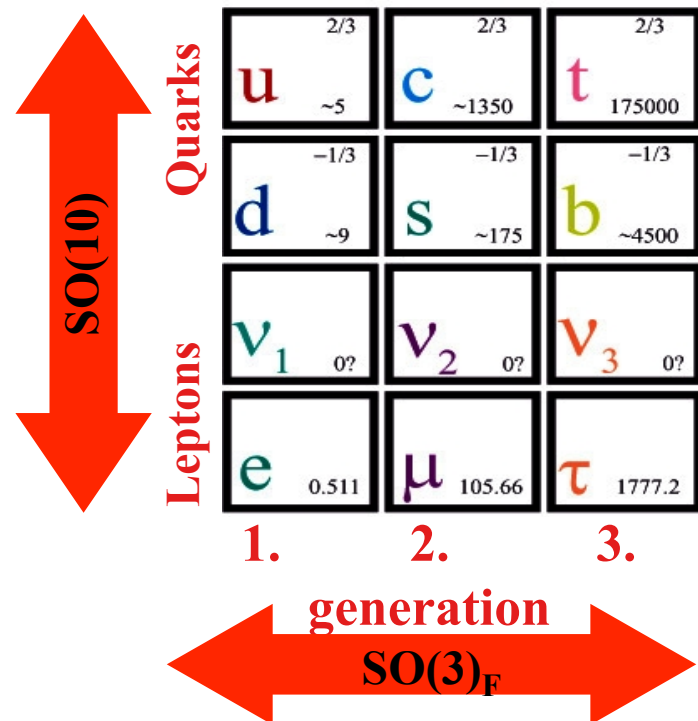
- so far **no understanding of flavour, 3 generations**
- apparant regularities in quark and lepton parameters
- ➔ flavour symmetries (finite number for limited rank)
- ➔ **symmetry** not texture zeros
- ➔ Breaking sequences...

Quarks	2/3		
	u	c	t
	~5	~1350	175000
	2/3		
Leptons	-1/3		
	d	s	b
	~9	~175	~4500
	-1/3		
	ν_1	ν_2	ν_3
	0?	0?	0?
	e	μ	τ
	0.511	105.66	1777.2
1. 2. 3.			
generation			

Examples:



8) GUTs x Flavour Symmetries



→ GUT group $\otimes$ flavour group

example: $SO(10) \otimes SU(3)_F$

- SSB of $SU(3)_F$ between Λ_{GUT} and Λ_{Planck}

- all flavour Goldstone Bosons eaten

- discrete sub-groups survive $\leftrightarrow$ SSB

e.g. Z_2 , S_3 , D_5 , A_4

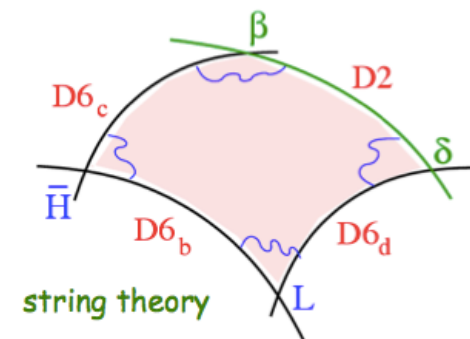
→ structures in flavour space

→ compare with data

→ rather restricted... few solutions

9) extra dimensions, strings, ...

→ many options → different secondary effects

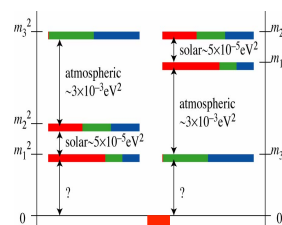


Suggestive Seesaw Features

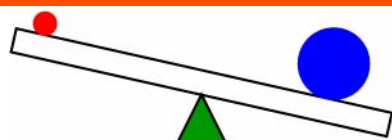
QFT: natural value of mass operators $\leftrightarrow$ scale of symmetry

$m_D \sim$ electro-weak scale

$M_R \sim$ L violation scale $\leftrightarrow ? \rightarrow$ embedding (GUTs, ...)



See-saw (type I)



$$m_\nu = m_D M_R^{-1} m_D^T$$

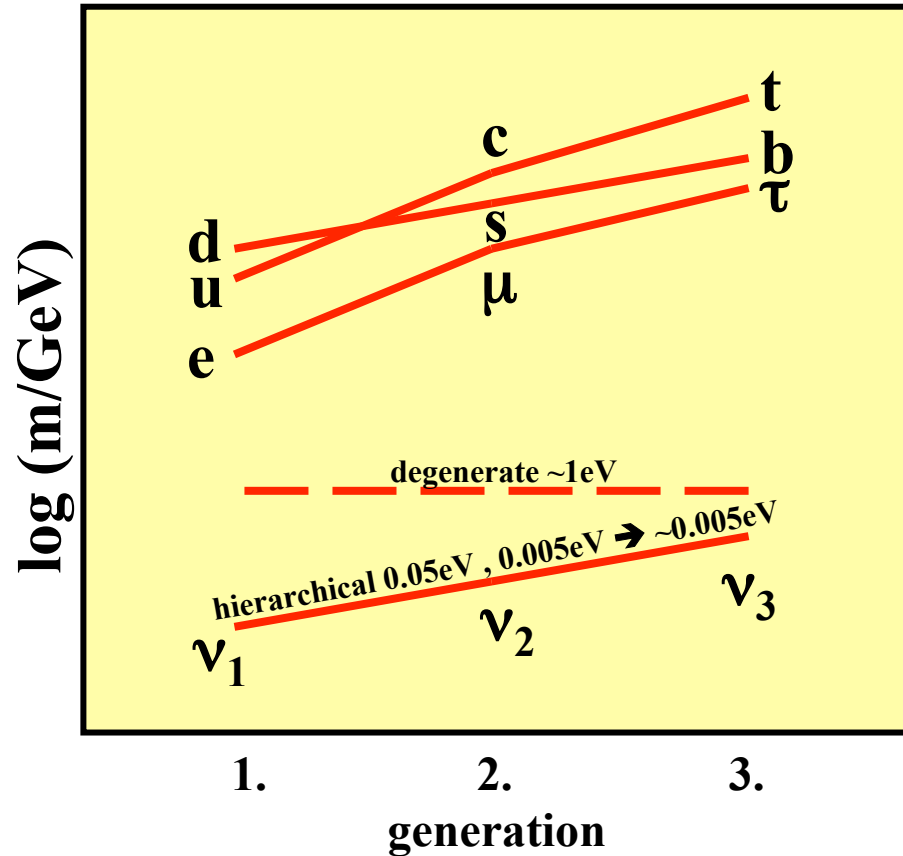
$$m_h = M_R$$

Numerical hints:

For $m_3 \sim (\Delta m_{\text{atm}}^2)^{1/2}$, $m_D \sim$ leptons $\rightarrow M_R \sim 10^{11} - 10^{16} \text{ GeV}$
 $\rightarrow \nu$'s are **Majorana particles**, m_ν probes $\sim$ **GUT scale physics!**
 $\rightarrow$ smallness of $m_\nu \leftrightarrow$ high scale of L, symmetries of m_D, M_R

2nd Look Questions

Quarks & charged leptons $\rightarrow$ hierarchical masses $\rightarrow$ neutrinos?



Quarks and charged leptons:

$$m_D \sim H^n ; n = 0, 1, 2 \rightarrow H \geq 20 \dots 200$$

Neutrinos: $m_\nu \sim H^n \rightarrow H \leq \sim 10$

See-saw:

$$m_\nu = -m_D^T M_R^{-1} m_D$$

	$\updownarrow$	$\updownarrow$	$\updownarrow$	$\updownarrow$
H	$\simeq 10$	≥ 20	?	≥ 20

- less hierarchy in m_D or corr. hierarchy in M_R ? $\rightarrow$ theoretically not connected!
- Dirac masses
- other version of see-saw? $\rightarrow$ type II, III, ... $\rightarrow$

The Double Seesaw

- Assume right handed neutrinos N and singlets $S \rightarrow (\nu, N, S)$
- Assign quantum numbers such that mass matrix is

$$\mathcal{M} = \begin{pmatrix} 0 & Y_\nu \langle \phi \rangle & 0 \\ Y_\nu^T \langle \phi \rangle & 0 & Y_N^T \langle \sigma \rangle \\ 0 & Y_N \langle \sigma \rangle & M_S \end{pmatrix}$$

$$M_S = \text{O(Planck scale)} \simeq 10^{19} \text{ GeV}$$

$$Y_N \langle \sigma \rangle = \text{O(GUT scale)} \simeq 10^{16} \text{ GeV}$$

$$Y_\nu \langle \phi \rangle = \text{O(EW scale)} \simeq 10^2 \text{ GeV}$$

1st seesaw $\rightarrow$ eigenvalues M_S and $Y_N^T (M_S)^{-1} Y_N \langle \sigma \rangle^2 = \text{O}(10^{16} \text{ GeV})$

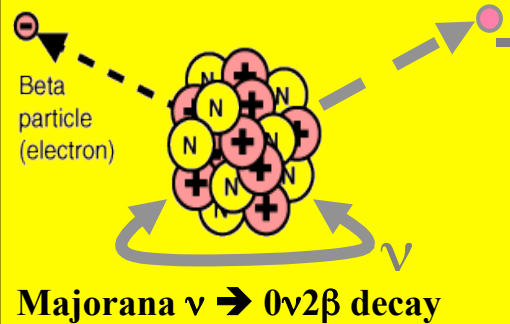
2nd seesaw

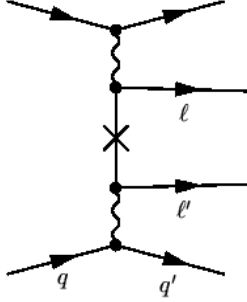
$$\rightarrow m_\nu^0 = \left[\frac{\langle \phi \rangle}{\langle \sigma \rangle} \right]^2 Y_\nu (Y_N)^{-1} M_S (Y_N^T)^{-1} Y_\nu^T = \text{O(eV)}$$

Possibility: $Y_N \sim Y_\nu \rightarrow$ structure of m_ν from M_S ML, Schmidt, Smirnov

Is the Picture complete? Correct?

$0\nu\beta\beta$ Beta Decay



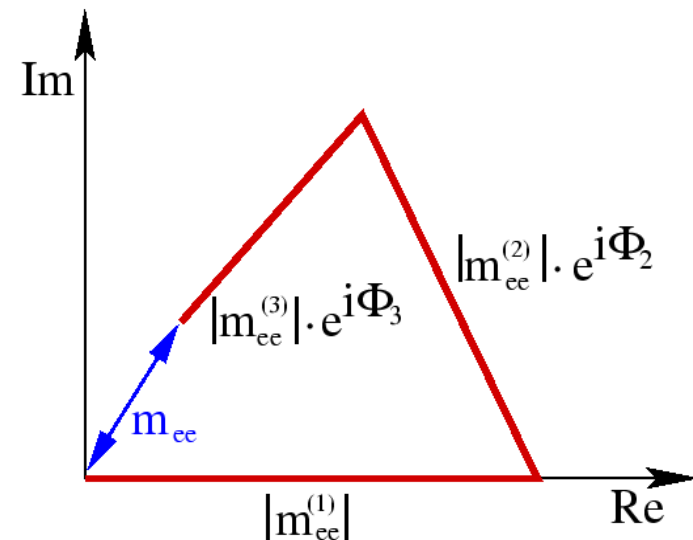
$\propto$


$\propto |\langle \mathbf{m}_{ee} \rangle| = \left| \sum m_i U_{ei}^2 \right| \leq 0.35 \text{ eV ?}$

Heidelberg-Moscow experiment

$$m_{ee} = |m_{ee}^{(1)}| + |m_{ee}^{(2)}| \cdot e^{i\Phi_2} + |m_{ee}^{(3)}| \cdot e^{i\Phi_3}$$

$$\begin{aligned} |m_{ee}^{(1)}| &= |U_{e1}|^2 m_1 \\ |m_{ee}^{(2)}| &= |U_{e2}|^2 \sqrt{m_1^2 + \Delta m_{21}^2} \\ |m_{ee}^{(3)}| &= |U_{e3}|^2 \sqrt{m_1^2 + \Delta m_{31}^2} \end{aligned}$$



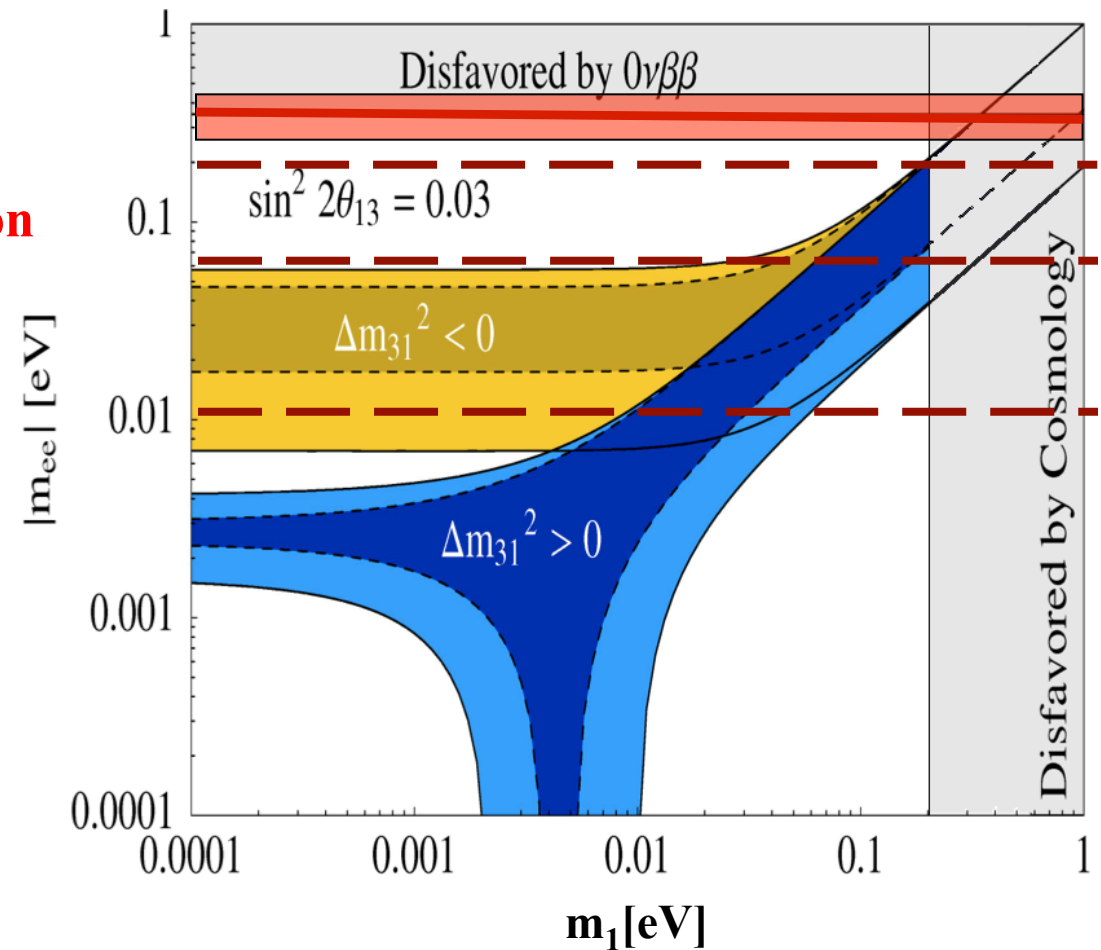
$$\text{solar} \Rightarrow |U_{e1}|^2, |U_{e2}|^2, \Delta m_{21}^2 \quad \text{atmosph.} \Rightarrow |\Delta m_{31}^2| \quad \text{CHOOZ} \Rightarrow |U_{e3}|^2 < 0.05$$

→ free parameters: m_1 , $\text{sign}(\Delta m_{31}^2)$, CP-phases Φ_2, Φ_3

**Claim of part of the original
Heidelberg-Moscow collaboration**
 $\longleftrightarrow$ cosmology $\rightarrow$,tension‘

aims of new experiments:

- test HM claim
- $(\Delta m_{31}^2)^{1/2} \simeq 0.05 \text{eV} \pm \text{errors}$
 $\rightarrow$ reach 0.01eV
 $\rightarrow$ CUORE
 $\rightarrow$ GERDA phases I, II, (III)



Comments:

- cosmology: limitation by systematical errors $\rightarrow$ ~ another factor 5-10?
- $0\nu\beta\beta$ nuclear matrix elements ~factor 1.3-2 **theoretical** uncertainty in m_{ee}
- $\Delta m^2 > 0$ allows complete cancellation
 $\rightarrow$ $0\nu\beta\beta$ signal not guaranteed, but cancelation appears unlikely

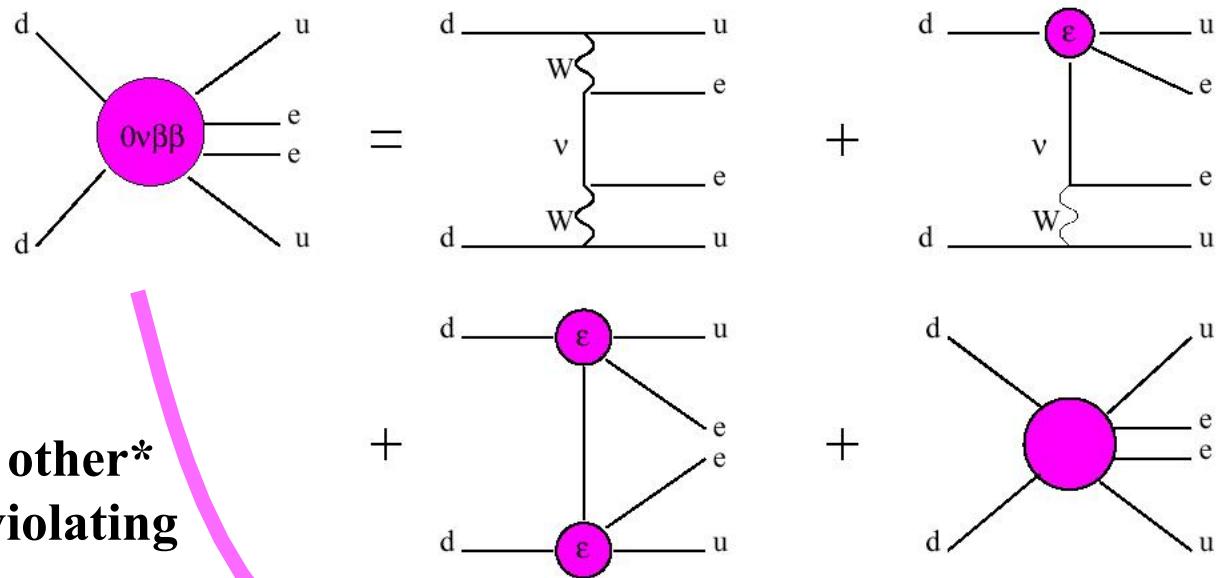
$0\nu\beta\beta$ from Alternative $\Delta L=2$ Operators

Various possibilities:

- LR symmetry
- SUSY (RPV)
- ...

→ $0\nu\beta\beta$ signal from *some other* new BSM lepton number violating operator

→ very promising interplay of neutrino mass determinations, cosmology, LHC, LVF experiments and theory

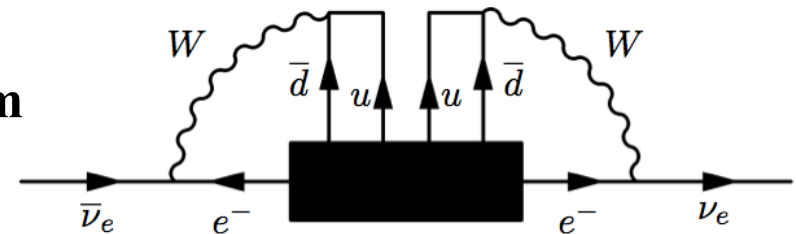


Schechter + Valle: Any $\Delta L=2$ violating operator

→ radiative generation of Majorana mass term

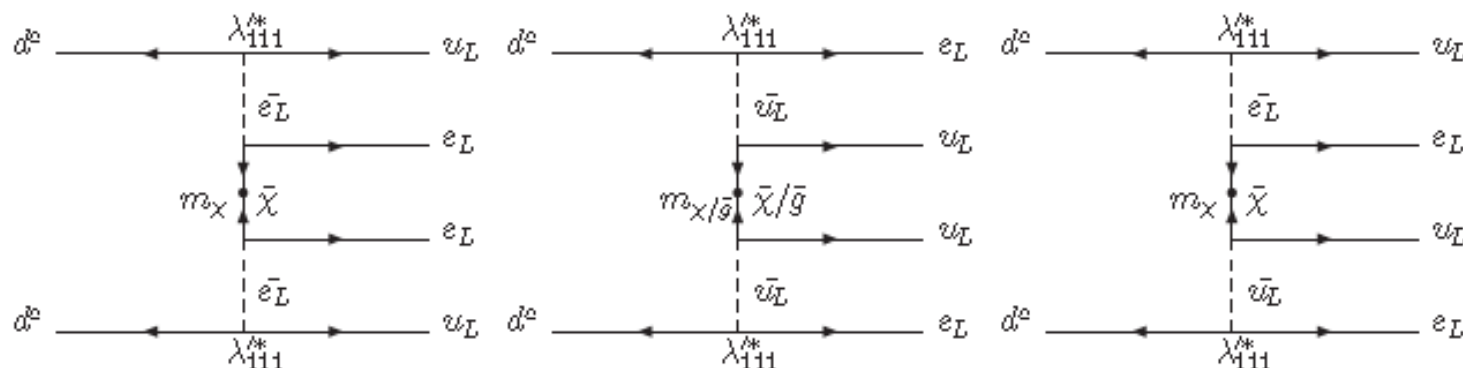
→ Majorana nature of ν 's guaranteed

→ but how big is the mass?



SUSY Example

Direct, TeV scale short range mediation w/o intermediate light ν , e.g.

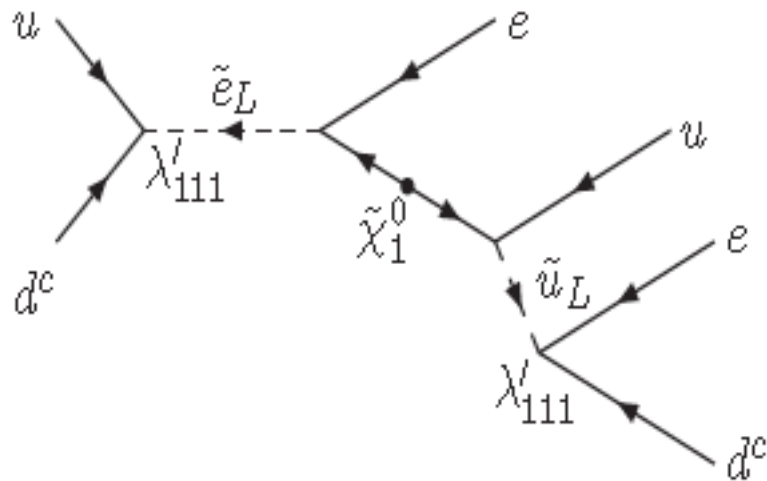


$$\mathcal{L}_{\lambda'_{111}\lambda'_{111}}^{eff, \Delta L_e=2}(x) = \frac{G_F^2}{2} m_p^{-1} [\bar{e}(1+\gamma_5)e^c] \times \left[(\epsilon_{\tilde{g}} + \epsilon_{\chi})(J_{PS}J_{PS} - \frac{1}{4}J_T^{\mu\nu}J_{T\mu\nu}) + (\epsilon_{\chi\tilde{e}} + \epsilon'_{\tilde{g}} + \epsilon_{\chi\tilde{f}})J_{PS}J_{PS} \right]$$

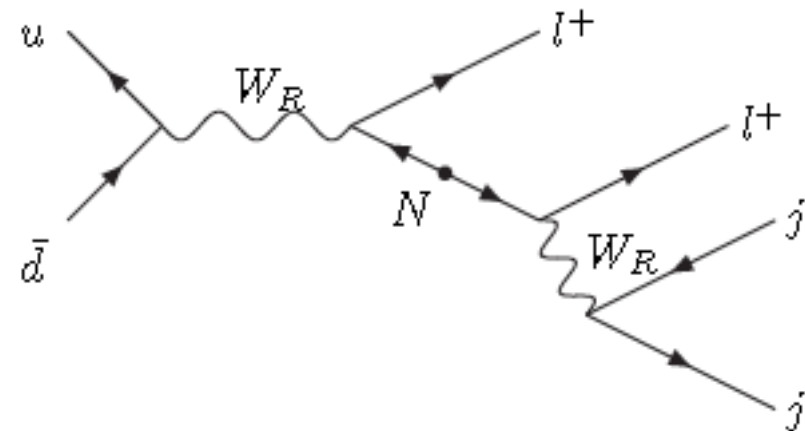
$$\epsilon_i \sim \pi\alpha_{(\text{Strong,EW})} \frac{\lambda_{111}^2}{G_F^2} \frac{m_P}{m_{(\tilde{g},\chi)}} \frac{1}{m_{(\tilde{u},\tilde{d},\tilde{e})}^4}.$$

$\Delta L=2$ Operators and TeV Scale Physics

SUSY: direct test of λ'_{111}



L-R symmetry: heavy N's



Relative strength of 'light' and 'heavy' $0\nu\beta\beta$ amplitudes:

A Feynman diagram for the 'light' $0\nu\beta\beta$ amplitude. It shows two vertices, each labeled ϵ , connected by a vertical line labeled ν . The left vertex has incoming d and d lines and outgoing u and e lines. The right vertex has incoming e and e lines and outgoing u and u lines.

A Feynman diagram for the 'heavy' $0\nu\beta\beta$ amplitude. It shows a single large vertical oval labeled ϵ . The left side has incoming d and d lines and outgoing u and u lines. The right side has incoming e and e lines and outgoing u and u lines.

$$M_{\text{light}} \sim G_F^2 \frac{m_{\beta\beta}}{\langle k^2 \rangle}$$

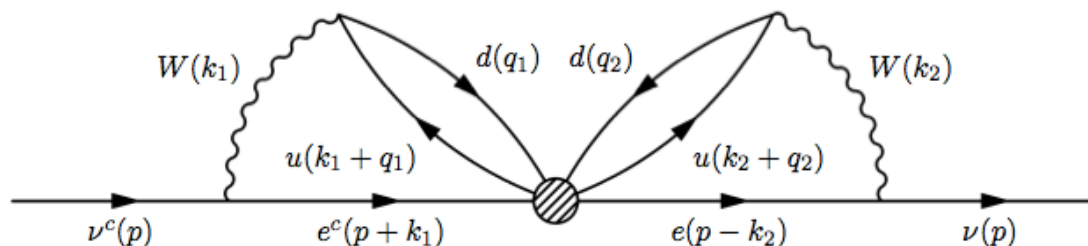
$$M_{\text{heavy}} \sim G_F^2 \left(\frac{\lambda}{g_2} \right)^4 \frac{M_W^4}{\Lambda^5}$$

SV-induced Neutrino Masses

General Lorentz-invariant Lagrangian for $0\nu\beta\beta$ (point operator)

$$\mathcal{L} = \frac{G_F^2}{2} m_p^{-1} (\epsilon_1 J J j + \epsilon_2 J^{\mu\nu} J_{\mu\nu} j + \epsilon_3 J^\mu J_\mu j + \epsilon_4 J^\mu J_{\mu\nu} j^\nu + \epsilon_5 J^\mu J j_\mu)$$

$$J = \bar{u} (1 \pm \gamma_5) d, \quad J^\mu = \bar{u} \gamma^\mu (1 \pm \gamma_5) d \text{ etc.}$$



Outcome:

M. Dürr, ML, A. Merle, arXiv:1105.0901

If other $\Delta L=2$ physics drives $0\nu\beta\beta \rightarrow$ SV gives $\delta m_\nu = 10^{-24}$ eV

$\rightarrow$ mass correction too small to explain observed masses and splittings

$\rightarrow$ other explicit neutrino mass operators required

Dirac: $0\nu\beta\beta$ essentially unrelated to neutrino masses $\leftrightarrow$ other BSM

Majorana: dominates over SV contribution

$0\nu\beta\beta$ may be a mixture of Majorana mass and other $\Delta L=2$ physics

$\rightarrow$ mimics higher Majorana neutrino mass

Non Standard Interactions (NSIs)

Effective Operators Beyond the SM

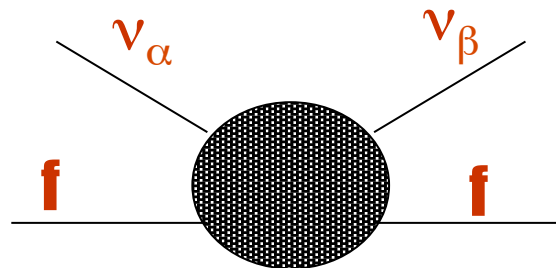
→ effects beyond 3 flavours

→ **Non Standard Interactions = NSIs** → effective 4f operators

$$\mathcal{L}_{NSI} \simeq \epsilon_{\alpha\beta} 2\sqrt{2}G_F (\bar{\nu}_{L\beta} \gamma^\rho \nu_{L\alpha}) (\bar{f}_L \gamma_\rho f_L)$$

- **integrating out heavy physics (c.f. $G_F \leftrightarrow M_W$)**

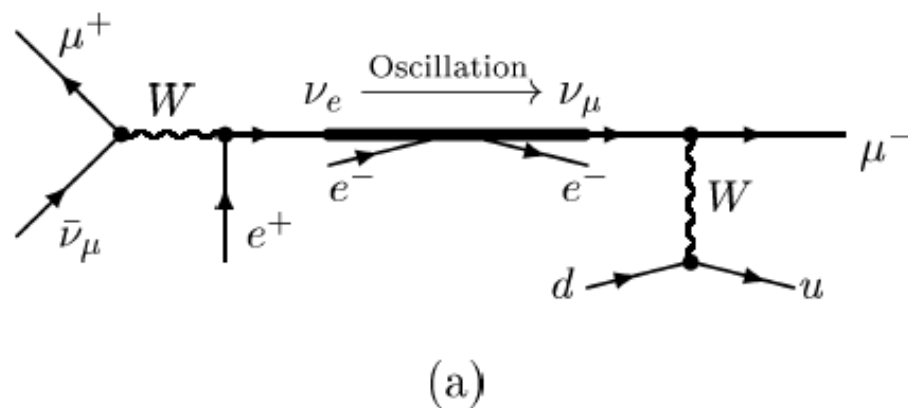
$$|\epsilon| \simeq \frac{M_W^2}{M_{NSI}^2}$$



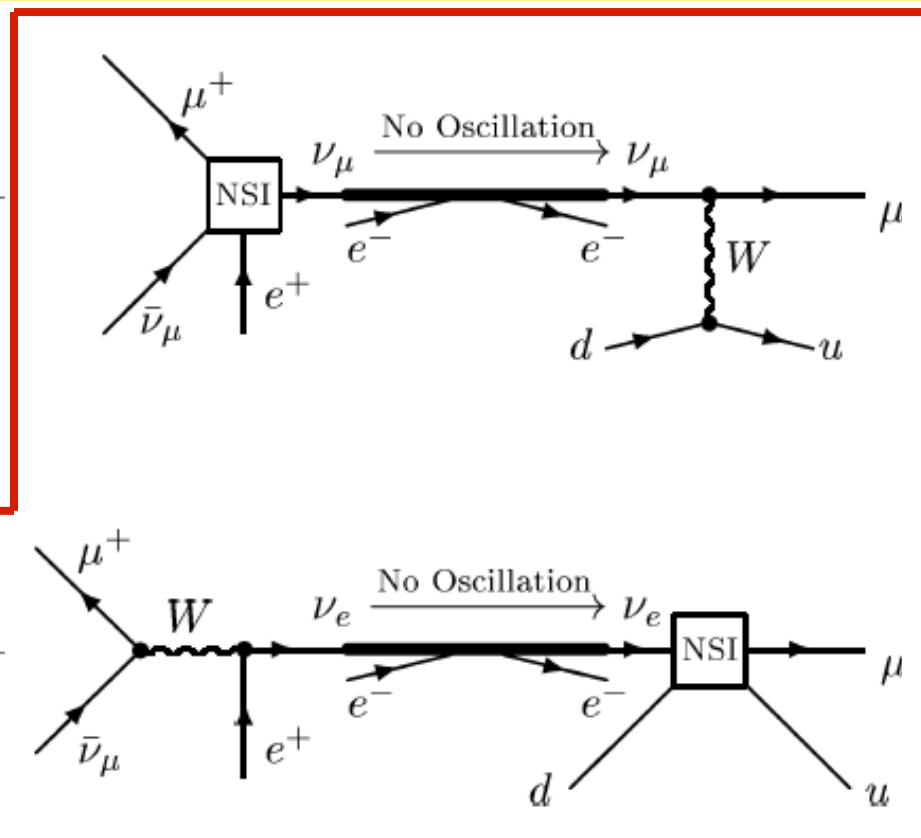
Grossman, Bergmann+Grossman, Ota+Sato, Honda et al., Friedland+Lunardini, Blennow+Ohlsson+Skrotzki, Huber+Valle, Huber+Schwetz+Valle, Campanelli+Romanino, Bueno et al., Barranco+Miranda+Rashba, Kopp+ML+Ota, ...

NSIs interfere with Oscillations

the “golden” oscillation channel

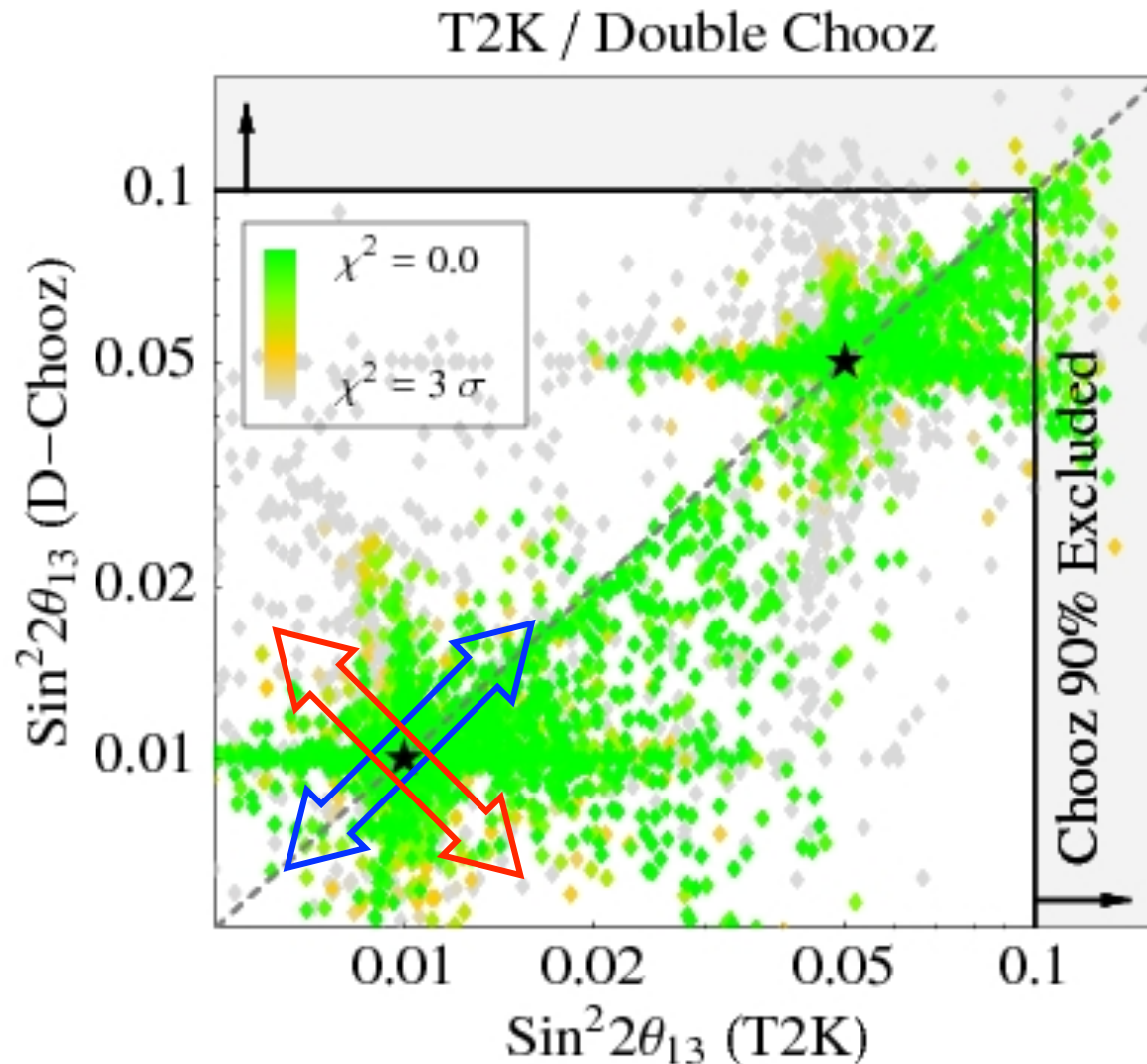


NSI contributions to the “golden” channel



note: interference in oscillations $\sim \epsilon$ $\leftrightarrow$ FCNC effects $\sim \epsilon^2$

NSI: Offset and Mismatch in θ_{13}



Kopp, ML, Ota, Sato

Redundant measurements:

Double Chooz + T2K

***=assumed 'true' values of θ_{13}**

scatter-plot: ϵ values random

- below existing bounds

- random phases

NSIs can lead to:

- **offset**

- **mismatch**

→ redundancy

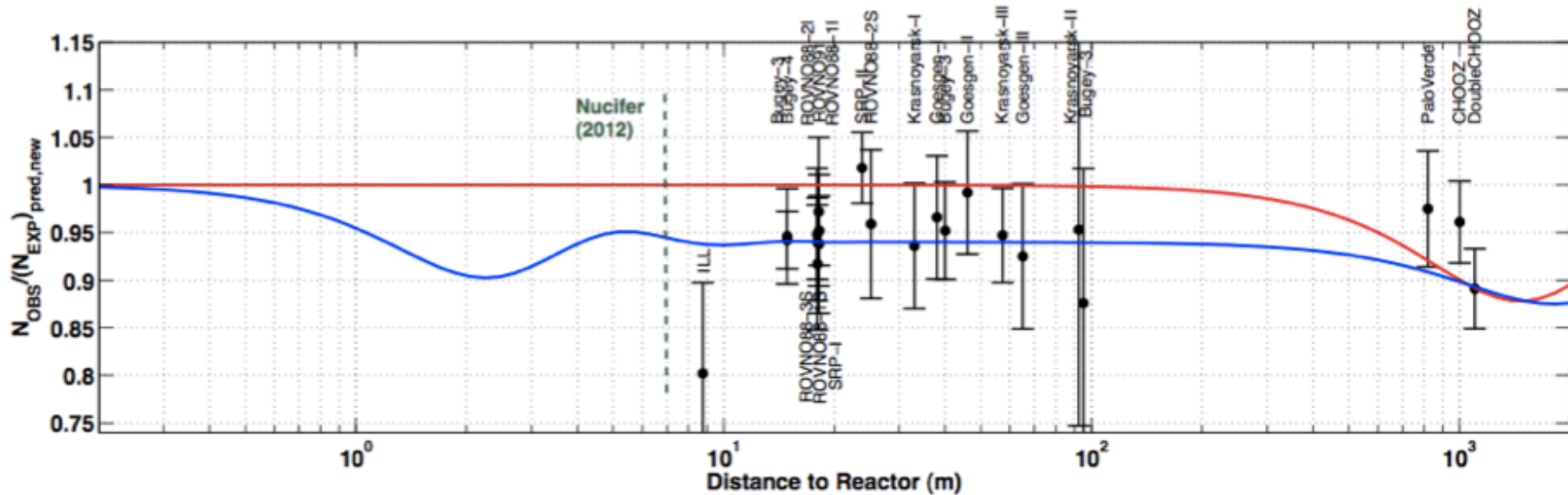
→ interesting potential

→ might first show up
as tension in global fits

Sterile Neutrinos

The Reactor Anomaly

New reactor fluxes and global reactor data: Mention et al.



θ_{13} can reduce flux at $L \geq 1$ km, but not at shorter baselines
Sterile neutrino with $\Delta m^2 \sim \text{eV}^2$ can nicely account for reduction
 $\rightarrow$ 3+1 fits ; all evidences for eV scale $\rightarrow$ 3+2, ...

See e.g. T. Schwetz at NEUTRINO 2012

$\rightarrow$ will be tested by new experiments (e.g. NUCIFER @ few meters)

Evidences for Light Sterile Neutrinos

Particle Physics:

Reactor anomaly, LSND, MiniBooNE, MINOS, Gallex...

- New and better data / experiments are needed to clarify the situation
- maybe something exciting around the corner?
- would hint at eV scale and sizable percentage type mixings

CMB: Extra eV-ish neutrinos possible J. Hamann et al. , ...

BBN: Extra ν 's possible: $N_\nu \simeq 3.7 \pm 1$

E. Aver, K. Olive, E. Skillman (2010), Y. Izotov, T. Thuan(2010)

Astrophysics: keV-ish sterile neutrinos could explain pulsar kicks

Kusenko, Segre, Mocioiu, Pascoli, Fuller et al., Biermann & Kusenko, Stasielak et al., Loewenstein et al., Dodelson, Widrow, Dolgov, ...

My believe: Most likely not all of them are correct

→ but any one has far reaching consequences!

The Neutrino Spectrum

The standard picture:

3 heavy sterile neutrinos typ. $\geq 10^{13}$ GeV

→ leptogenesis, role in GUTs, ...

Some mechanism which makes
1, 2, ... heavy states light?

→ light sterile neutrino(s)

→ tiny heavy-light mixing expected
 $\theta^2 < O(m_v/m_s)$

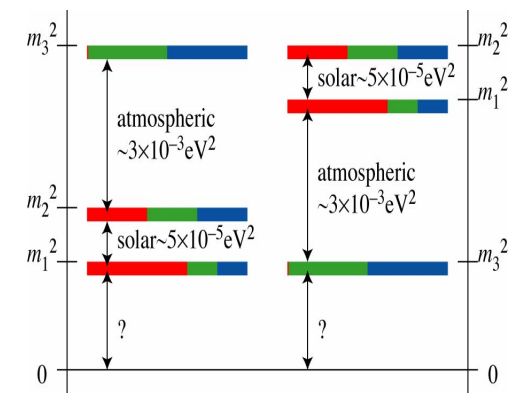
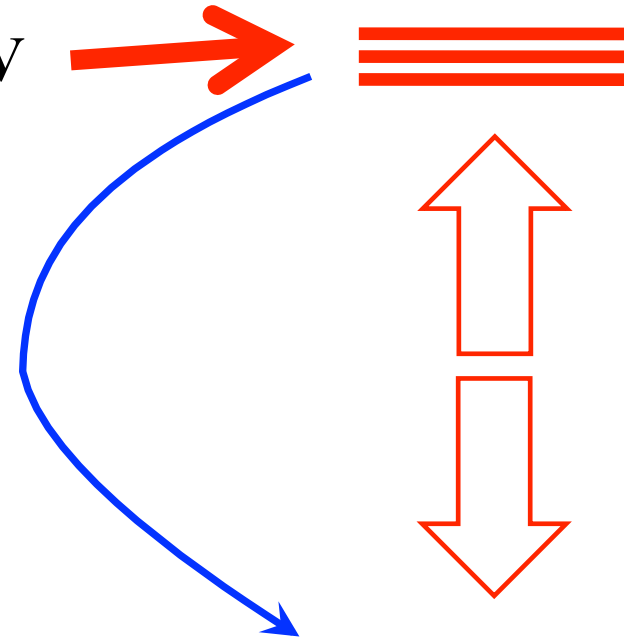
3 light active neutrinos

→ this could easily be wrong

- more than 3 N_R states, ...

- M_R may have special eigenvalues, ...

→ light sterile neutrinos ?!



keV sterile Neutrinos as WDM

Could Neutrinos be Dark Matter?

- Active neutrinos would be perfect Hot Dark Matter
 - ruled out:
 - destroys small scale structures in cosmological evolution
 - measured neutrino masses too small → maybe HDM component
- keV sterile neutrinos: Warm Dark Matter
 - works very well:
 - relativistic at decoupling
 - non-relativistic at radiation to matter dominance transition
 - OK for $M_X \simeq \text{few keV}$ with very tiny mixing
 - ↔ tiny active – sterile mixings $O(m_\nu/M_R)$ expected
 - reduced small scale structure → smoother profile, less dwarf satellites

Note: Right-handed neutrinos exist probably anyway

The ν MSM

Asaka, Blanchet, Shaposhnikov, Asaka, Shaposhnikov

Particle content:

- Gauge fields of $SU(3)_c \times SU(2)_W \times U(1)_Y$: $\gamma, W_{\pm}, Z, g$
- Higgs doublet: $\Phi=(1,2,1)$

• Matter

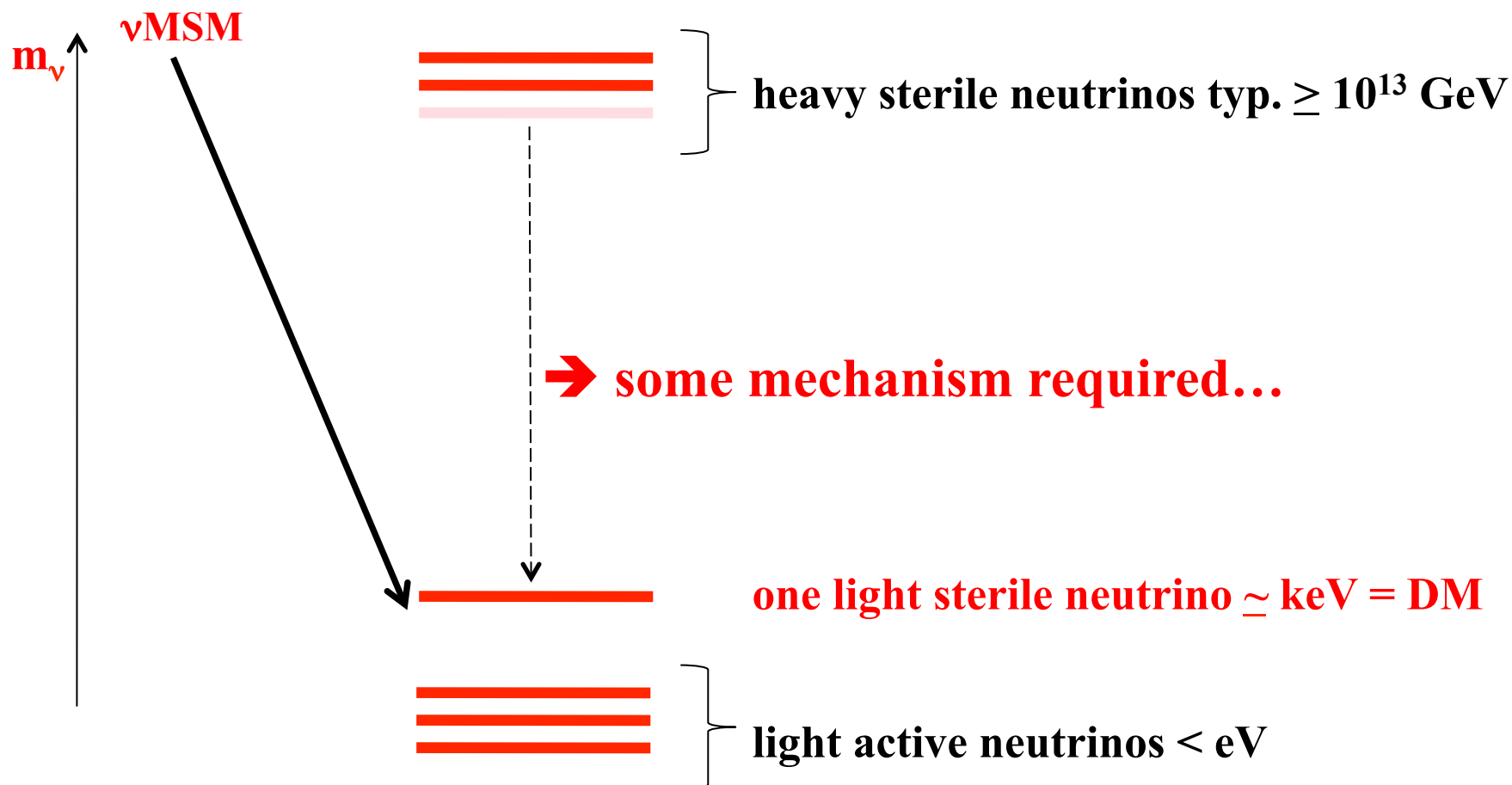
	$SU(3)_c$	$SU(2)_W$	$U(1)_Y$	$U(1)_{em}$
$\begin{pmatrix} u \\ d \end{pmatrix}_L$	3	2	+1/3	$\begin{pmatrix} +2/3 \\ -1/3 \end{pmatrix}$
u_R	3	1	+4/3	+2/3
d_R	3	1	-2/3	-1/3
$\begin{pmatrix} \nu_e \\ e \end{pmatrix}_L$	1	2	-1	$\begin{pmatrix} 0 \\ -1 \end{pmatrix}$
e_R	1	1	-2	-1
N	1	1	0	0

x3 generations

- lepton sector more symmetric to the quark sector
- Majorana masses for N
- choose for one sterile $\nu \sim \text{keV}$ mass → exceeds lifetime of Universe

Virtue and Problem of the ν MSM

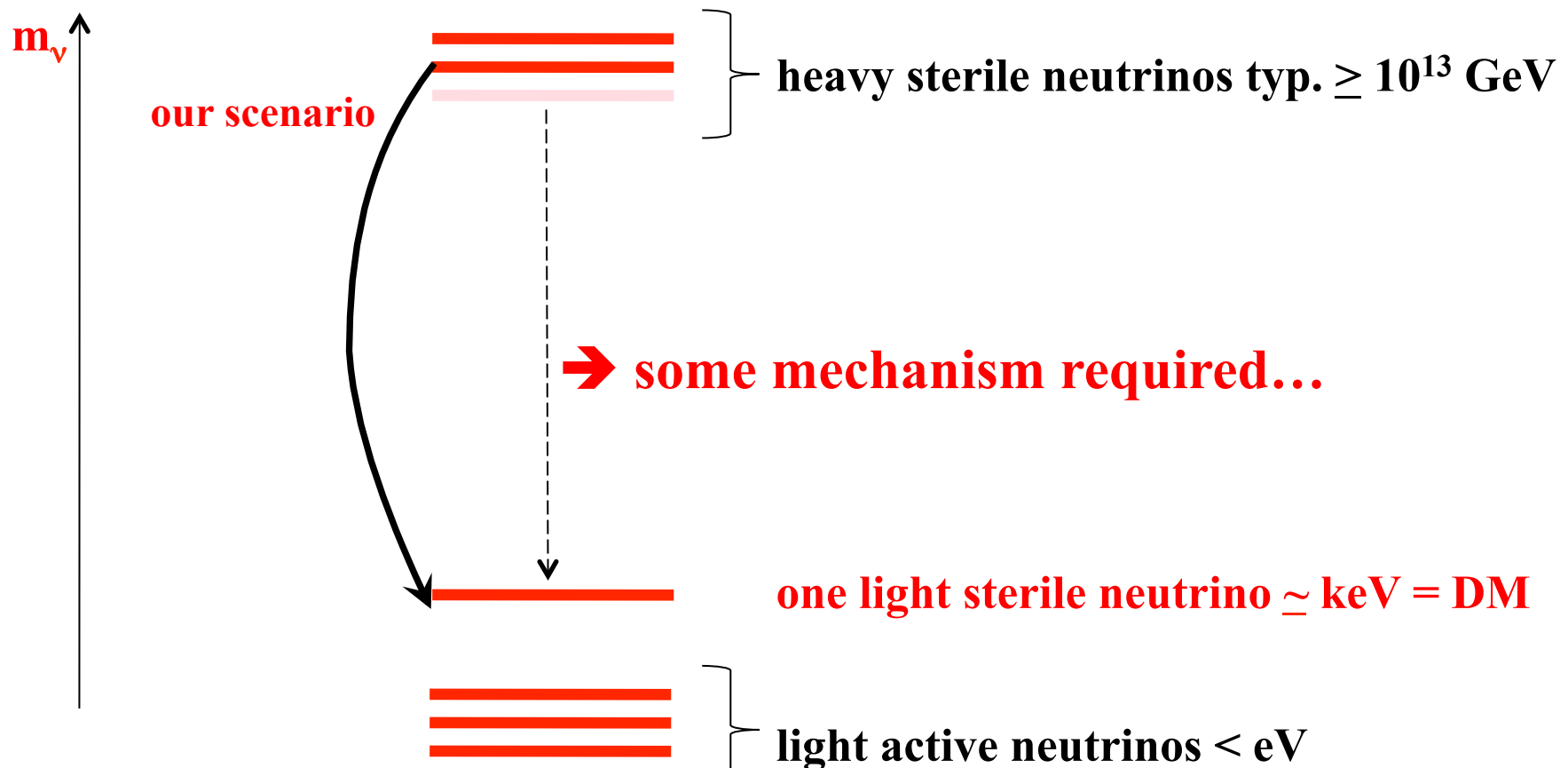
- ν MSM:** Scenario with sterile ν and tiny mixing $\rightarrow$ never enters thermal equilibrium
- $\rightarrow$ requires **non-thermal production** from other particles (avoid over-closure)
 - $\rightarrow$ **new physics** before the beginning of the thermal evolution sets abundance



Alternative Scenario with Thermal Abundance

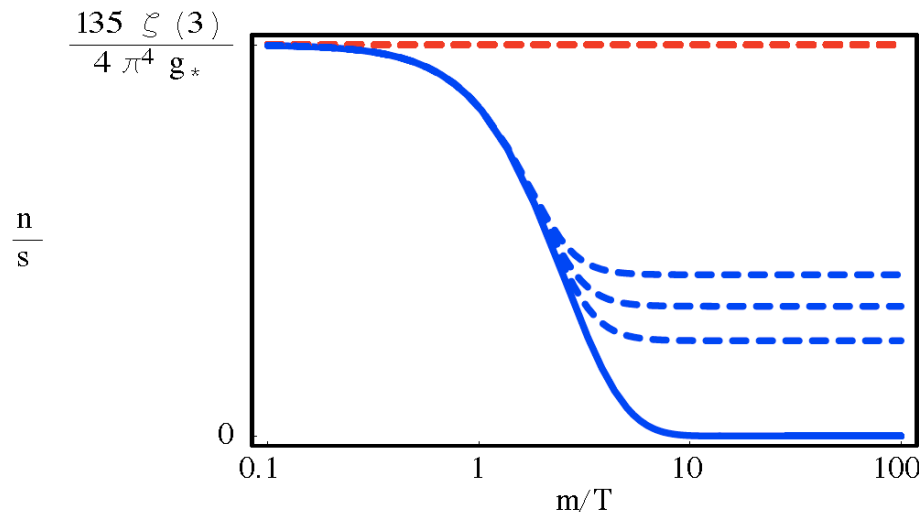
- Three right-handed neutrinos N_1, N_2, N_3 , Dirac and Majorana mass terms
- **N Charged under some (BSM) gauge group $\rightarrow$ scale M ($\sim$ sterile)**
 $\rightarrow$ thermal production of DM abundance
- Specific example: LR-symmetry $SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$

Bezrukov, Hettmannsperger, ML



Obtaining the correct Abundance

Usual thermal WIMP case:



$$\frac{\Omega}{\Omega_{\text{DM}}} \simeq \left(\frac{10}{g_{*f}} \right) \left(\frac{M}{10 \text{ eV}} \right)$$

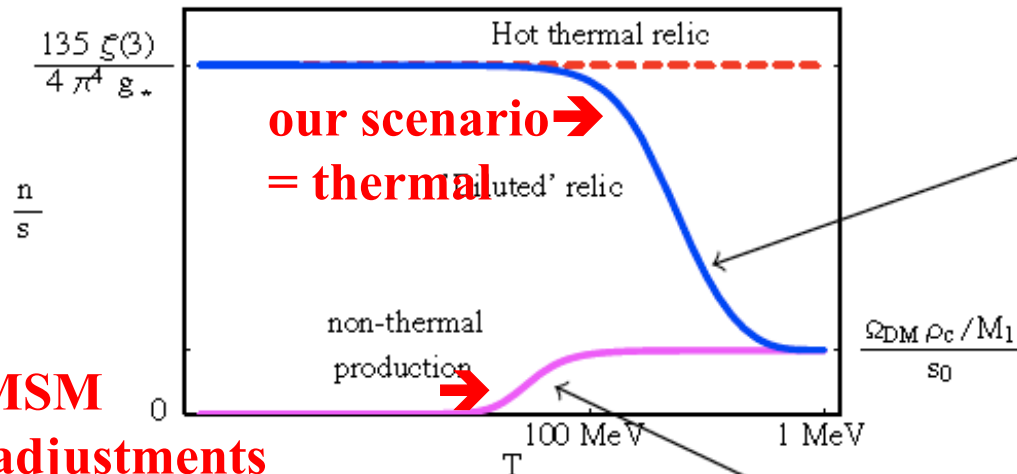
Decoupled relativistic

CDM:
($M \gg \text{MeV}$)

$$\Omega \sim \Omega_{\text{DM}}$$

Decoupled
nonrelativistic

keV sterile neutrinos:



Diluted after decoupling
(entropy generated by other
particle decay)

$$\Omega \sim \Omega_{\text{DM}}$$

Never entered thermal equilibrium

Entropy Generation by out-of Equilibrium Decay

Heavy particle (here: N_3) dropping out of thermal equilibrium while relativistic $T_f > M_2$: $\rightarrow$ **bounds gauge scale from below**

$$M > \frac{1}{g_{*f}^{1/8}} \left(\frac{M_2}{\text{GeV}} \right)^{3/4} (10 \div 16) \text{ TeV}$$

- $\rightarrow$ sufficiently long lived $\rightarrow$ become non-relativistic
- $\rightarrow$ dominates expansion of Universe during its decay

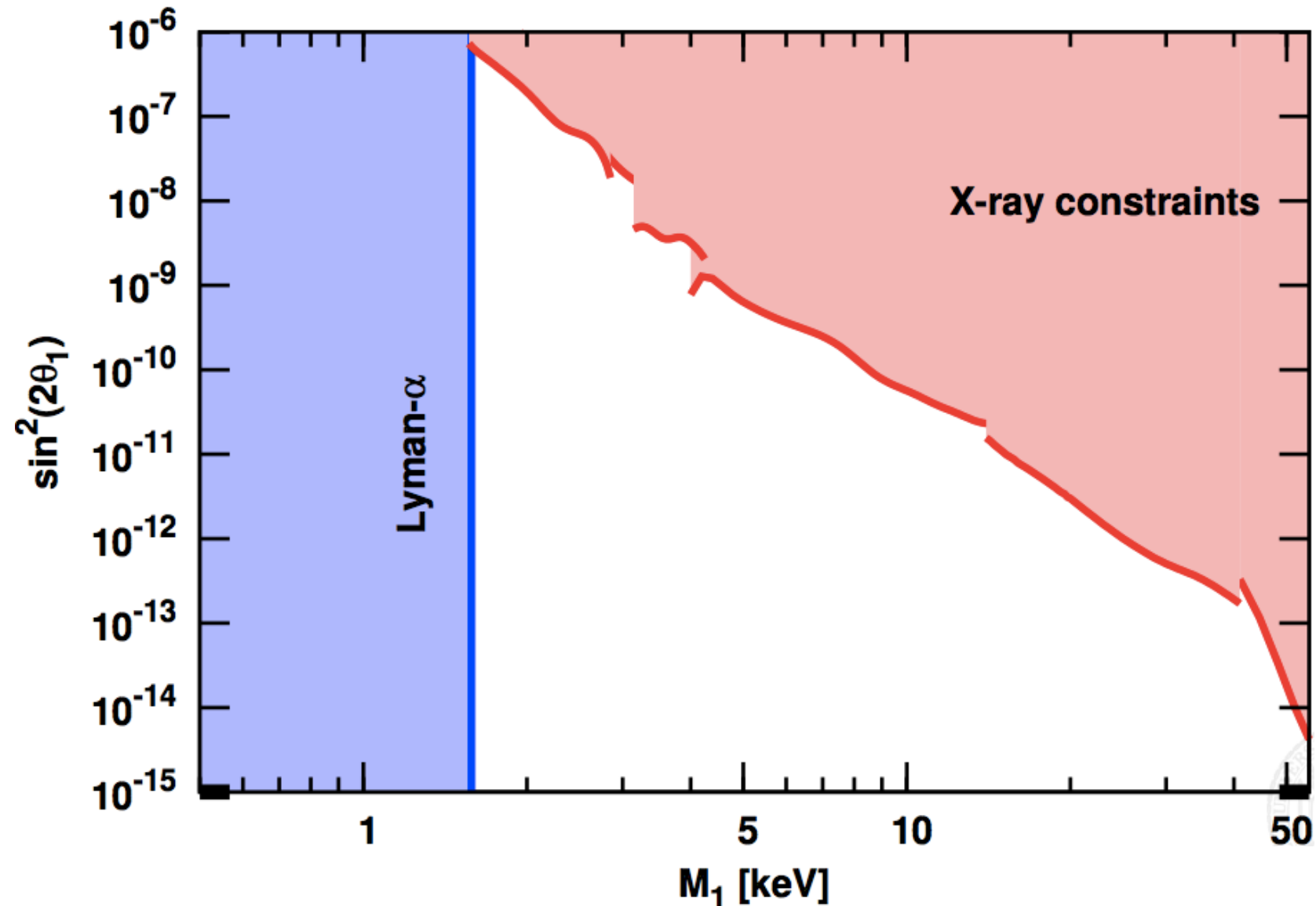
- $\rightarrow$ entropy generation factor $\rightarrow$

$$S \simeq 0.76 \frac{\bar{g}_*^{1/4} M_2}{g_* \sqrt{\Gamma_2 M_{\text{Pl}}}}$$

$$\frac{S_{\text{after}}}{S_{\text{before}}} = S \frac{a_{\text{before}}^3}{a_{\text{after}}^3}$$

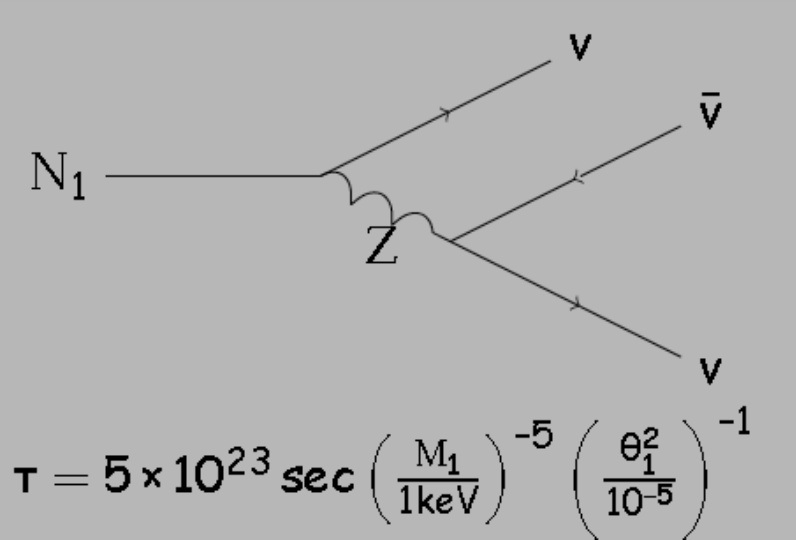
- $\rightarrow$ fixes decay width Γ_2

Allowed Parameter Range



Observing keV-ish Neutrino DM

- LHC
 - sterile neutrino DM is not observable
 - WIMP-like particles still possible – but not DM
- direct searches
 - sterile ν DM extremely difficult; maybe in β -decay (MARE)
- astrophysics/cosmology $\Rightarrow$ at some level: keV X-rays
 - $\Rightarrow$ sterile neutrino DM is decaying into active neutrinos
 - decay $N_1 \rightarrow \nu\bar{\nu}\nu$, $N_1 \rightarrow \nu\bar{\nu}\bar{\nu}$
 - not very constraining since $\tau \gg \tau_{\text{Universe}}$

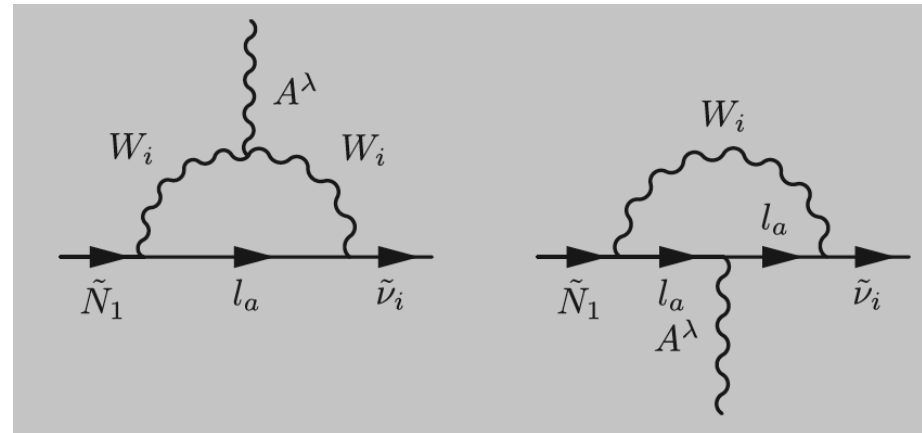


The diagram shows a horizontal line on the left labeled N_1 . This line connects to a vertex, from which a wavy line labeled Z extends to the right. At the end of the Z line is another vertex from which three lines branch out: one goes up and to the right labeled ν , one goes down and to the right labeled $\bar{\nu}$, and one goes down and to the right labeled ν . Below the diagram is the formula for the lifetime τ .

$$\tau = 5 \times 10^{23} \text{ sec} \left(\frac{M_1}{1 \text{ keV}} \right)^{-5} \left(\frac{\theta_1^2}{10^{-5}} \right)^{-1}$$

- radiative decays $N_1 \rightarrow \nu \gamma$

→ photon line $E_\gamma = m_s/2$



- so far: observational limit on active-sterile mixing angle

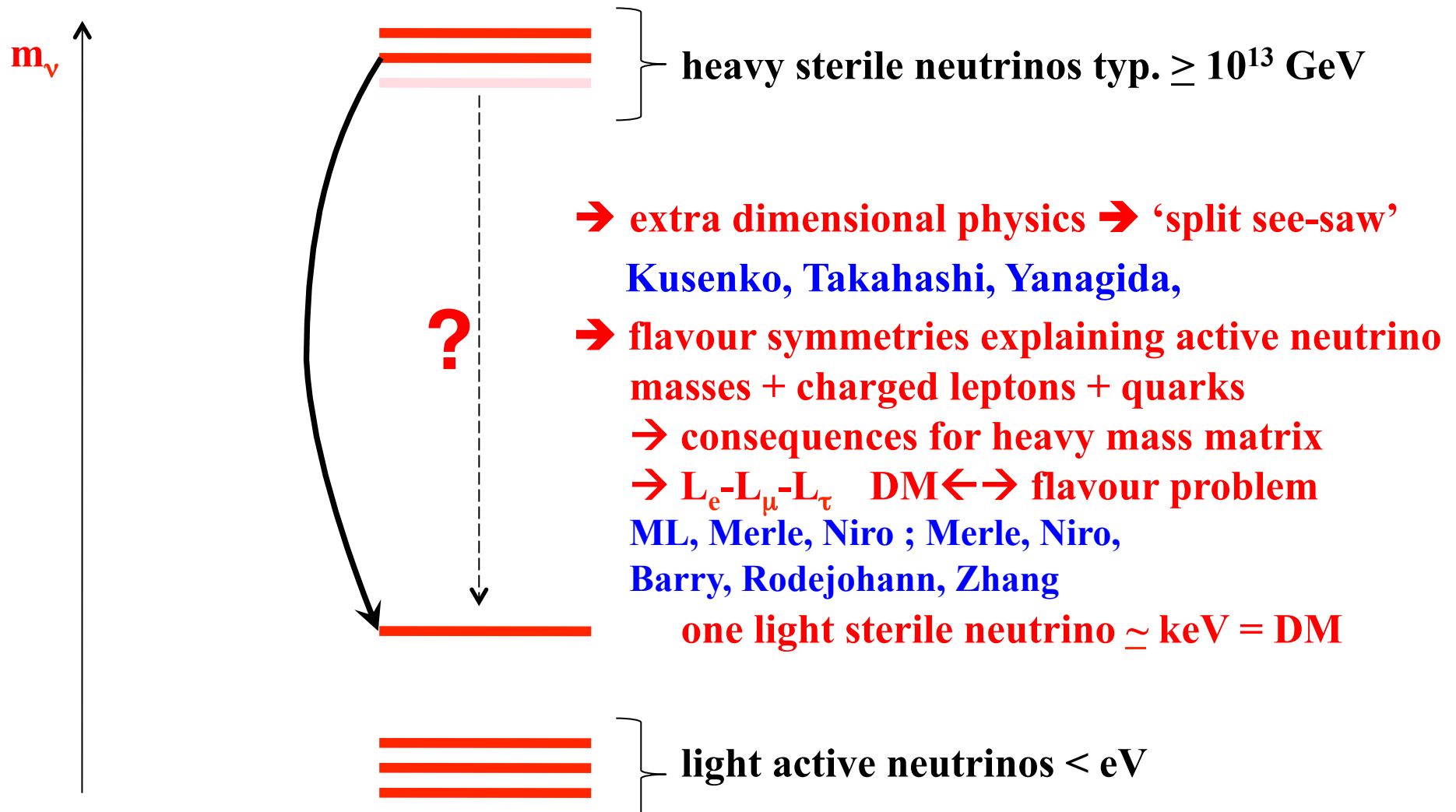
$$\Gamma_{N_1 \rightarrow \nu \gamma} \simeq 5.5 \times 10^{-22} \theta_1^2 \left(\frac{M_1}{1 \text{ keV}} \right)^5 \text{ s}^{-1}$$

$$\theta_1^2 \lesssim 1.8 \times 10^{-5} \left(\frac{1 \text{ keV}}{M_1} \right)^5$$

- mixing tiny, but naturally expected to be tiny: $O(\text{scale ratio})$

Explaining keV-ish Sterile Neutrinos

Possible scenario: See-saw + a reason why 1 sterile ν is light



Light Sterile Neutrinos from $L_e-L_\mu-L_\tau$

- **Flavour symmetries** have been studied to explain apparent regularities of masses and mixing: **A4, S3, D5, ...**
 $\rightarrow$ implications for sterile sector?
 $\rightarrow$ could the same symmetries **explain a keV-ish sterile ν ?**

Model with $L_e-L_\mu-L_\tau$ symmetry:

by **Lavoura & Grimus** $\rightarrow$ extended: **ML, Merle, Niro**

SM + ν_{iR} + softly broken U(1) $\leftrightarrow$ $\mathcal{F} \equiv L_e - L_\mu - L_\tau$
 type II see-saw $\rightarrow$ **+Higgs triplet** $\Delta = \begin{pmatrix} \Delta^+/\sqrt{2} & \Delta^{++} \\ \Delta^0 & -\Delta^+/\sqrt{2} \end{pmatrix}$

	$L_e L$	$L_\mu L$	$L_\tau L$	e_R	μ_R	τ_R	N_{1R}	N_{2R}	N_{3R}	ϕ	Δ
$\mathcal{F}$	1	-1	-1	1	-1	-1	1	-1	-1	0	0

- **Mass matrix for right-handed neutrinos:**

$$\mathcal{L}_{\text{mass}} = -M_R^{12} \overline{(N_{1R})^C} N_{2R} - M_R^{13} \overline{(N_{1R})^C} N_{3R} + h.c.$$

- **Dirac masses**

$$\begin{aligned} \mathcal{L}_{\text{mass}} = & -Y_D^{e1} \overline{L_{eL}} \tilde{\phi} N_{1R} - Y_D^{\mu2} \overline{L_{\mu L}} \tilde{\phi} N_{2R} - Y_D^{\mu3} \overline{L_{\mu L}} \tilde{\phi} N_{3R} - \\ & -Y_D^{\tau2} \overline{L_{\tau L}} \tilde{\phi} N_{2R} - Y_D^{\tau3} \overline{L_{\tau L}} \tilde{\phi} N_{3R} + h.c., \end{aligned}$$

- **In addition: Triplet masses**

$$\mathcal{L}_{\text{mass}} = -Y_L^{e\mu} \overline{(L_{eL})^C} (i\sigma_2 \Delta) L_{\mu L} - Y_L^{e\tau} \overline{(L_{eL})^C} (i\sigma_2 \Delta) L_{\tau L} + h.c.$$

Neutrino mass matrix:

$$\Psi \equiv ((\nu_{eL})^C, (\nu_{\mu L})^C, (\nu_{\tau L})^C, N_{1R}, N_{2R}, N_{3R})^T$$

$$\mathcal{M}_\nu = \left(\begin{array}{ccc|ccc} 0 & m_L^{e\mu} & m_L^{e\tau} & m_D^{e1} & 0 & 0 \\ m_L^{e\mu} & 0 & 0 & 0 & m_D^{\mu2} & m_D^{\mu3} \\ m_L^{e\tau} & 0 & 0 & 0 & m_D^{\tau2} & m_D^{\tau3} \\ \hline m_D^{e1} & 0 & 0 & 0 & M_R^{12} & M_R^{13} \\ 0 & m_D^{\mu2} & m_D^{\tau2} & M_R^{12} & 0 & 0 \\ 0 & m_D^{\mu3} & m_D^{\tau3} & M_R^{13} & 0 & 0 \end{array} \right)$$


$$\det(M_{ij}) = 0 \rightarrow M_1 = 0$$

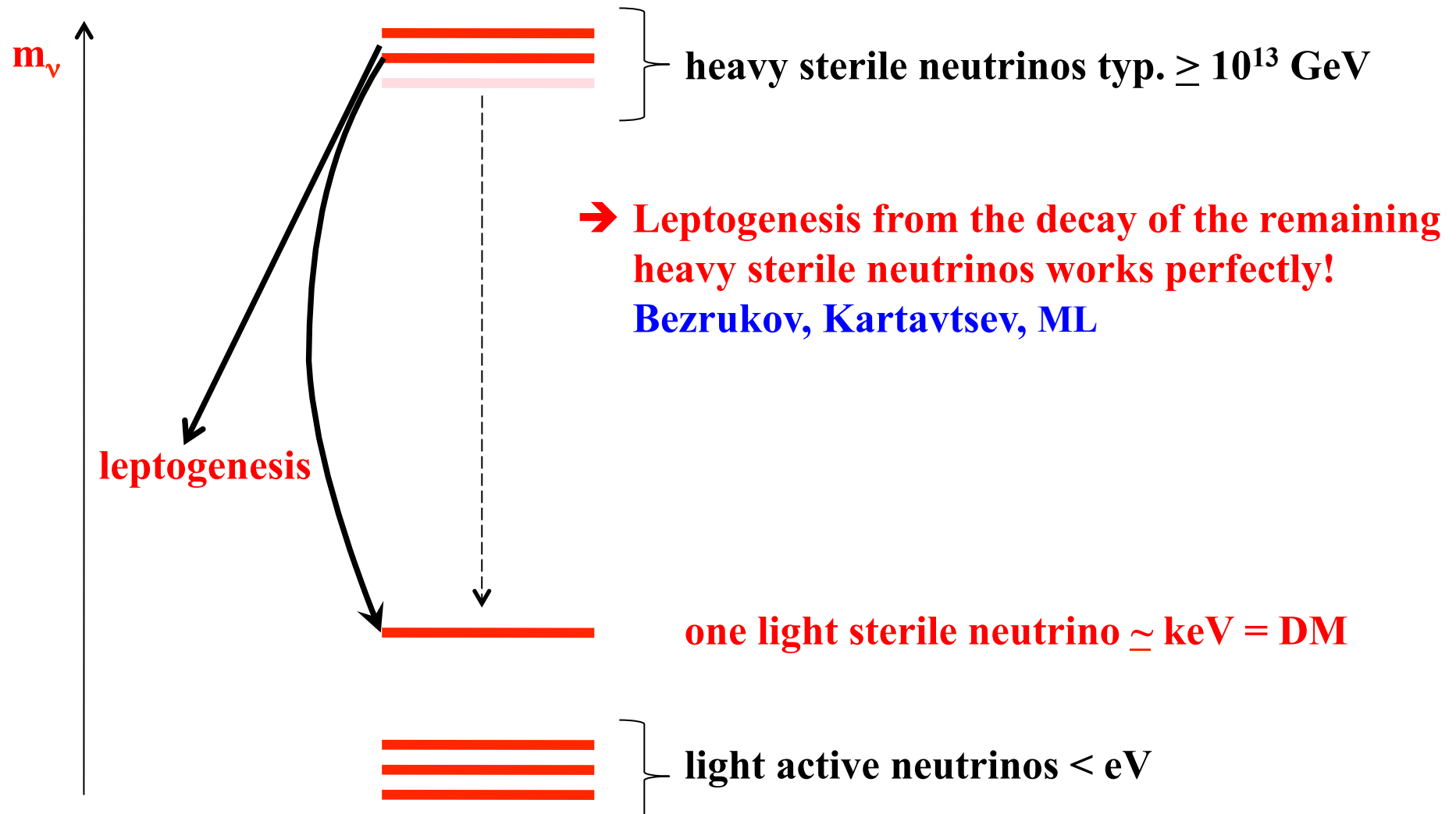
→ massless sterile state + soft breaking

→ naturally light sterile ν

→ mechanism possible in models

Leptogenesis

...there still exist heavy sterile states ...



Conclusions

- Neutrinos are physics a little bit beyond the SM
 - Interesting features & unique insights
 - Models: Many possibilities $\leftrightarrow$ experiment
 - Ways to get fooled: 0nbb, NSIs, ...
 - A **keV-ish sterile neutrino** is a very well motivated and good working **Warm Dark Matter candidate** $\leftrightarrow$ finite ν -masses
 - Right handed neutrinos probably exist
 - $\rightarrow$ requires only some mechanism for light sterile mass $O(\text{keV})$
- $\rightarrow$ Combination with Leptogenesis possible $\rightarrow$ BAU
- $\rightarrow$ More general scenarios: any mechanism which ‘naturally’ explains light sterile neutrinos