

Impact of QCD and SUSY-QCD Corrections on the Neutralino Dark Matter Relic Density.

Julia Harz, DESY Hamburg

in collaboration with B. Herrmann, M. Klasen, K. Kovarik and Q. Le Boulc'h

DESY Theory Workshop, Hamburg

26.09.2012



Overview

- 1 Interplay of particle and astro particle physics
- 2 Calculating the dark matter relic density
- 3 DM@NLO - an extension for numerical relic density calculators



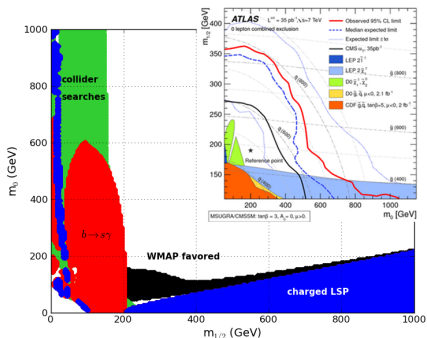
Overview

- 1 Interplay of particle and astro particle physics
- 2 Calculating the dark matter relic density
- 3 DM@NLO - an extension for numerical relic density calculators



Constraining the SUSY parameter space

Neutralino - LSP and cold dark matter candidate



Interplay between LHC and PLANCK data will be even more interesting

Particle physics bounds

- Collider searches

e.g.

$$m_{\tilde{\chi}_1^0} > 46 \text{ GeV}, m_{\tilde{t}} > 95.7 \text{ GeV}$$

PDG (2012)

- Precision measurements

e.g.

$$\text{Br}(b \rightarrow s\gamma) = (3.55 \pm 0.26) \cdot 10^{-4}$$

HFAG collaboration (2010)

Cosmology bounds

- 7 year data of WMAP

$$\Rightarrow \Omega h^2 = 0.1123 \pm 0.035$$

WMAP collaboration (2011)



Overview

- 1 Interplay of particle and astro particle physics
- 2 Calculating the dark matter relic density
- 3 DM@NLO - an extension for numerical relic density calculators



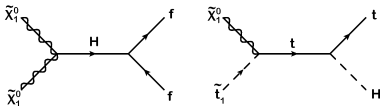
Calculating the relic density

Today's number density can be calculated via Boltzmann equation.

$$\dot{n} + 3Hn = -\langle\sigma v\rangle\left(n^2 - n_{eq}^2\right)$$

σ cross section of annihilation and coannihilation

$$\langle\sigma v\rangle = \sum_{ij} \frac{2}{g_j} \left\langle \sigma_{ij} v_{ij} \frac{n_i^{eq}}{n^{eq}} \frac{n_j^{eq}}{n^{eq}} \right\rangle \quad \text{with} \quad \frac{n_i^{eq}}{n^{eq}} \propto \exp\left[\frac{-(m_i - m_\chi)}{T}\right]$$



Coannihilation...

gets important, when masses of LSP and NLSP almost degenerate

K. Griest, D. Seckel. Phys. Rev. D **43** (1991) 10, 3191-3203



Calculating the relic density

On the basis of the number density one can calculate the relic density.

$$\Omega_{CDM} h^2 = \frac{m_\chi n_0}{\rho_C} \propto \frac{1}{\langle \sigma v \rangle}$$

Public computational programs (e.g.):

DarkSUSY

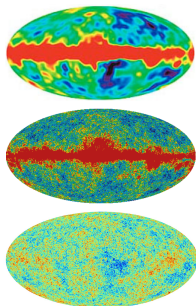
Gondolo, Edsjö, Ullio, Bergström, Bringmann et al. [astro-ph/0406204]

MicrOMEGAs

Bélanger, Boudjema, Pukhov et al. [hep-ph/1004.1092]

SuperIso Relic

Arbey, Mahmoudi [hep-ph/0906.0369]



Theoretical uncertainties in the relic density prediction

In cosmology

- Choice of cosmological model
Hamann, Hannestad, et.al. (2006) [hep-ph/0611582]
- Variation in Hubble expansion rate
Arbey, Mahmoudi (2008) [hep-ph/0803.0741]

In particle physics

- Precision of masses
Allanach, Kraml, Porod (2003) [hep-ph/0302102]
- Uncertainties of spectrum calculators
Bélanger, Kraml, Pukhov (2005) [hep-ph/0502079]
- Precision in the calculation of (co)annihilation cross section
Baro, Boudjema, Semenov (2007) [hep-ph/0710.1821]

Current status in calculating the relic density:

- Calculation in public programs only on effective tree level
- Current theoretical uncertainties bigger than future precision of PLANCK
- Significant impact of NLO-corrections on the relic density



Theoretical uncertainties in the relic density prediction

In cosmology

- Choice of cosmological model

Hamann, Hannestad, et.al. (2006) [hep-ph/0611582]

- Variation in Hubble expansion rate

Arbey, Mahmoudi (2008) [hep-ph/0803.0741]

In particle physics

- Precision of masses

Allanach, Kraml, Porod (2003) [hep-ph/0302102]

- Uncertainties of spectrum calculators

Bélanger, Kraml, Pukhov (2005) [hep-ph/0502079]

- Precision in the calculation of (co)annihilation cross section

Baro, Boudjema, Semenov (2007) [hep-ph/0710.1821]

Current status in calculating the relic density:

- Calculation in public programs only on effective tree level
- Current theoretical uncertainties bigger than future precision of PLANCK
- Significant impact of NLO-corrections on the relic density

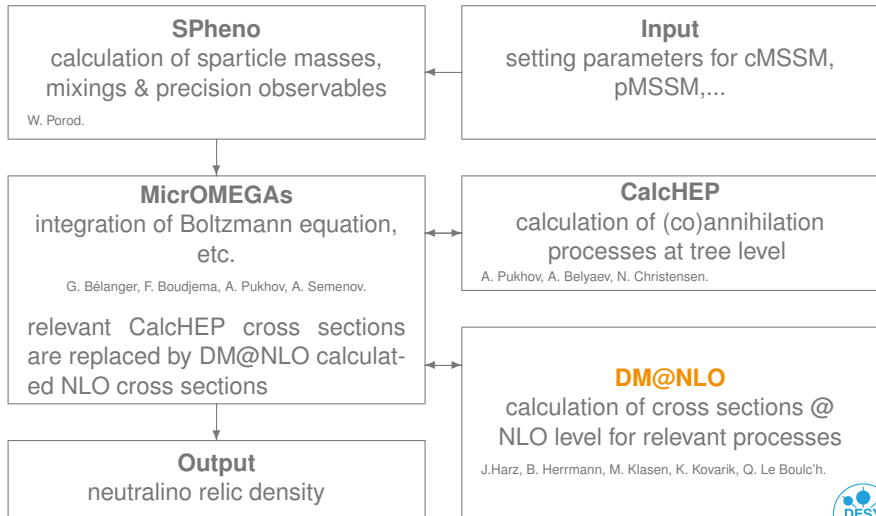


Overview

- 1 Interplay of particle and astro particle physics
- 2 Calculating the dark matter relic density
- 3 DM@NLO - an extension for numerical relic density calculators



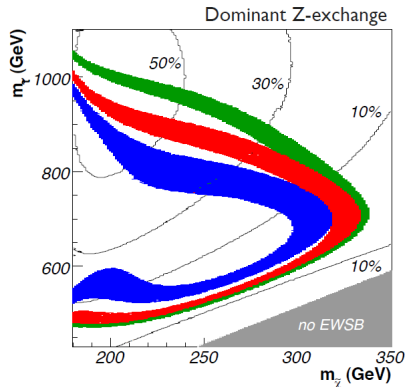
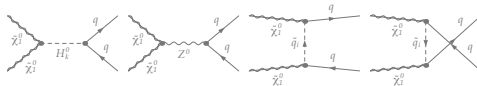
DM@NLO - relic density including QCD corrections



Impact of SUSY-QCD-corrections to annihilation

Example: Dominant Z-exchange

- Enhancement of annihilation cross section into quarks by 50 % through QCD-corrections
- Reduction of the predicted relic density
- Significant shift of the WMAP favoured region

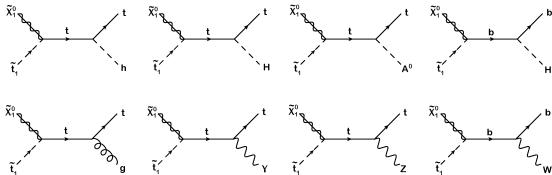
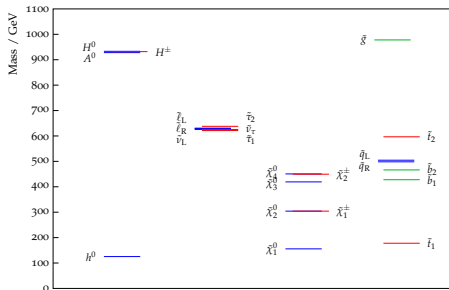


$\tan \beta = 10, A_0 = 0, m_0 = 1500, M_2 = 600, \mu > 0$
 Herrmann, Klasen, Kovarik (2009), arXiv:0907.0030 [hep-ph].

⇒ Effect of corrections to the relic density larger than current experimental uncertainties!

Coannihilation with Squarks

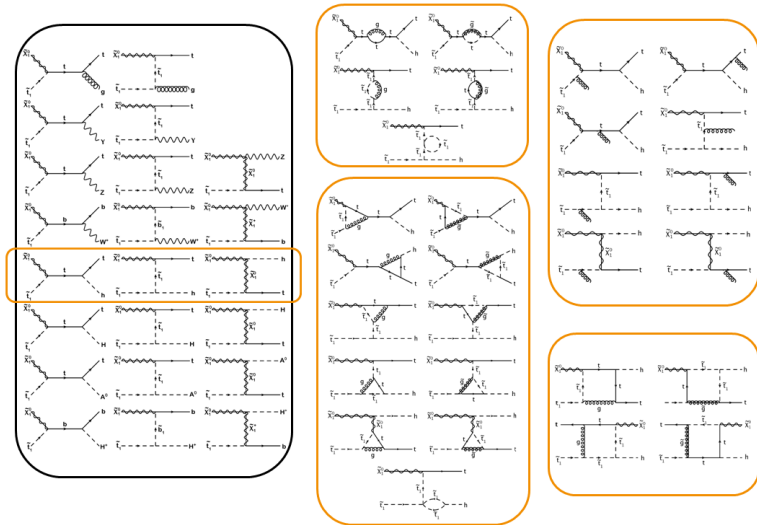
- Contribution if squarks and neutralino almost degenerate
- Dominant in different regions of parameter space
- Extendable to coannihilation of gauginos with sleptons in general



J.H., B. Herrmann, M. Klasen, K. Kovarik, Q. Le Boulc'h (in progress)



Full NLO calculation for coannihilation with Squarks



J.H., B. Herrmann, M. Klasen, K. Kovarik, Q. Le Boulc'h (in progress)



Some technicalities

Handling of IR-divergencies - I

- Phase-space-slicing

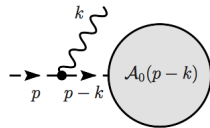
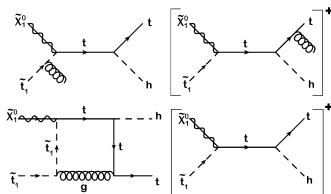
$$\sigma^{NLO} = \int_{2 \rightarrow 3} d\sigma^R + \int_{2 \rightarrow 2} d\sigma^V$$

$$\sigma_{2 \rightarrow 3}^{breds}(\lambda) = \sigma^{soft}(\Delta E, \lambda) + \sigma^{hard}(\Delta E)$$

$$\mathcal{M} = \frac{i(2p-k)^\mu \varepsilon_\mu(k)}{(p-k)^2 - m^2} (-ig_s T^a) A_0(p-k)$$

$$\mathcal{M} = -(g_s T^a) \frac{\varepsilon \cdot p}{p \cdot k} \mathcal{M}_0 \quad \text{with } k^\mu \ll p^\mu$$

$$\left(\frac{d\sigma}{d\Omega} \right)_{soft} = - \left(\frac{d\sigma}{d\Omega} \right)_0 \times \frac{g_s^2 C_F}{(2\pi)^3} \int_{|\vec{k}| \leq \Delta E} \frac{d^3 k}{2\omega} \frac{-2k_1 \cdot p_2}{(p_2 \cdot k)(k_1 \cdot k)}$$



Some technicalities

Handling of IR-divergencies - I

- Phase-space-slicing

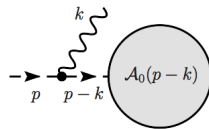
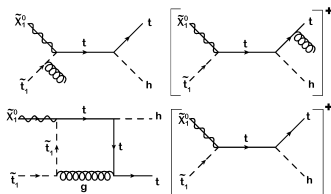
$$\sigma^{NLO} = \int_{2 \rightarrow 3} d\sigma^R + \int_{2 \rightarrow 2} d\sigma^V$$

$$\sigma_{2 \rightarrow 3}^{brem}(\lambda) = \sigma^{soft}(\Delta E, \lambda) + \sigma^{hard}(\Delta E)$$

$$\mathcal{M} = \frac{i(2p - k)^\mu \varepsilon_\mu(k)}{(p - k)^2 - m^2} (-ig_s T^a) \mathcal{A}_0(p - k)$$

$$\mathcal{M} = - (g_s T^a) \frac{\varepsilon \cdot p}{p \cdot k} \mathcal{M}_0 \quad \text{with } k^\mu \ll p^\mu$$

$$\left(\frac{d\sigma}{d\Omega} \right)_{soft} = - \left(\frac{d\sigma}{d\Omega} \right)_0 \times \frac{g_s^2 C_F}{(2\pi)^3} \int_{|\vec{k}| \leq \Delta E} \frac{d^3 k}{2\omega} \frac{-2k_1 \cdot p_2}{(p_2 \cdot k)(k_1 \cdot k)}$$



Some technicalities

Handling of IR-divergencies - I

- Phase-space-slicing

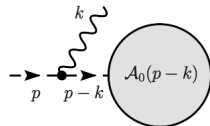
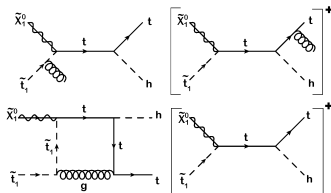
$$\sigma^{NLO} = \int_{2 \rightarrow 3} d\sigma^R + \int_{2 \rightarrow 2} d\sigma^V$$

$$\sigma_{2 \rightarrow 3}^{breds}(\lambda) = \sigma^{soft}(\Delta E, \lambda) + \sigma^{hard}(\Delta E)$$

$$\mathcal{M} = \frac{i(2p - k)^\mu \varepsilon_\mu(k)}{(p - k)^2 - m^2} (-ig_s T^a) \mathcal{A}_0(p - k)$$

$$\mathcal{M} = - (g_s T^a) \frac{\varepsilon \cdot p}{p \cdot k} \mathcal{M}_0 \quad \text{with } k^\mu \ll p^\mu$$

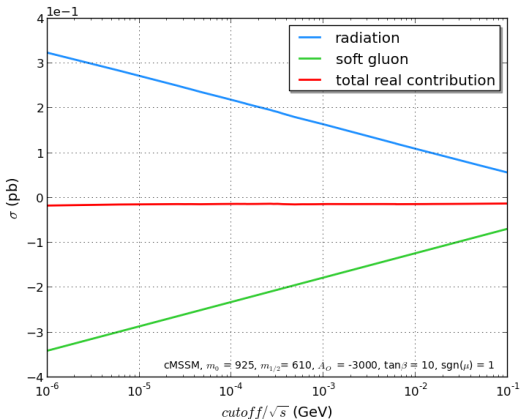
$$\left(\frac{d\sigma}{d\Omega} \right)_{soft} = - \left(\frac{d\sigma}{d\Omega} \right)_0 \times \frac{g_s^2 C_F}{(2\pi)^3} \int_{|\vec{k}| \leq \Delta E} \frac{d^3 k}{2\omega} \frac{-2k_1 \cdot p_2}{(p_2 \cdot k)(k_1 \cdot k)}$$



Some technicalities

Handling of IR-divergencies - I

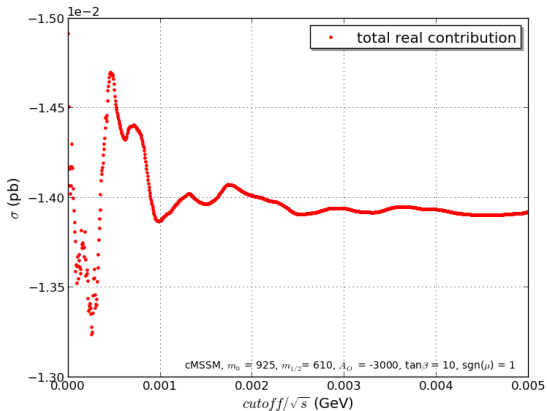
- Phase-space-slicing



Some technicalities

Handling of IR-divergencies - I

- Phase-space-slicing



Some technicalities

Handling of IR-divergencies - II

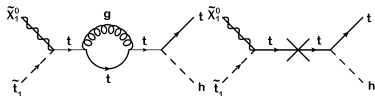
- Dipole-Subtraction-formalism

$$\sigma^{NLO} = \int_{2 \rightarrow 3} \left[d\sigma^R - d\sigma^A \right] |_{\epsilon=0} + \int_{2 \rightarrow 2} \left[d\sigma^V + \int_1 d\sigma^A \right] |_{\epsilon=0}$$

Handling of UV-divergencies

- input parameters:

$$m_b^{\overline{MS}}, m_t^{\overline{OS}}, A_b^{\overline{DR}}, A_t^{\overline{DR}}, m_{b_1}^{\overline{OS}}, m_{b_2}^{\overline{OS}}, m_{t_1}^{\overline{OS}}$$



$$\begin{pmatrix} M_Q^2 + m_q^2 + M_Z^2 c_{2\beta} (T_q^3 - Q_q S_W^2) \\ m_q (A_q - \mu \kappa) \end{pmatrix} = U_{\bar{q}} \begin{pmatrix} m_{q_1}^2 & 0 \\ 0 & m_{q_2}^2 \end{pmatrix} U_{\bar{q}}^\dagger$$

- consistent renormalization scheme for all (co-)annihilation processes

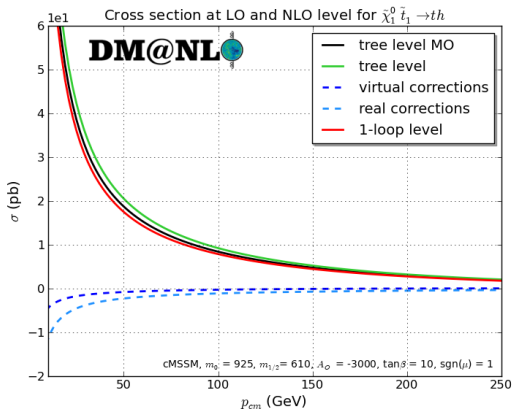


Impact of SUSY-QCD-corrections to coannihilation

Example scenario: cMSSM

$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow th$	34.3 %
$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow tg$	16.1 %
$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow bW^+$	3.4 %
$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow tZ$	1.4 %
$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow t\gamma$	0.4 %

For $\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow th$ @ $p_{cm} = 50$ GeV:
 → relative correction: -14.8 %



Impact of SUSY-QCD-corrections to coannihilation

Example scenario: cMSSM

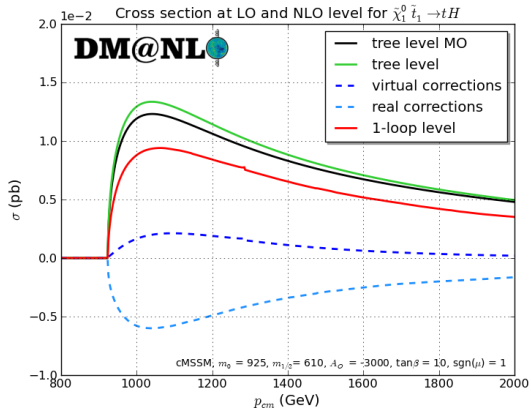
$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow t h$	34.3 %
$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow t g$	16.1 %
$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow b W^+$	3.4 %
$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow t Z$	1.4 %
$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow t \gamma$	0.4 %

For $\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow t h$ @ $p_{cm} = 50$ GeV:

→ relative correction: -14.8 %

For $\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow t H$ @ $p_{cm} = 1000$ GeV:

→ relative correction: -32.0 %



Impact of SUSY-QCD-corrections to coannihilation

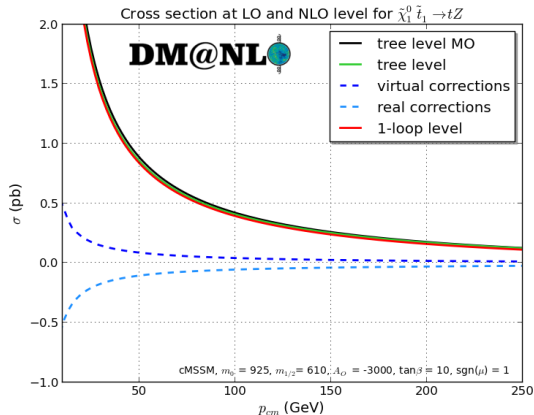
Example scenario: cMSSM

$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow t h$	34.3 %
$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow t g$	16.1 %
$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow b W^+$	3.4 %
$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow t Z$	1.4 %
$\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow t \gamma$	0.4 %

For $\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow t h$ @ $p_{cm} = 50$ GeV:
 → relative correction: -14.8 %

For $\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow t H$ @ $p_{cm} = 1000$ GeV:
 → relative correction: -32.0 %

For $\tilde{\chi}_1^0 \tilde{t}_1 \rightarrow t Z$ @ $p_{cm} = 50$ GeV:
 → relative correction: -2.2 %



⇒ NLO-corrections to coannihilation have significant impact on cross section

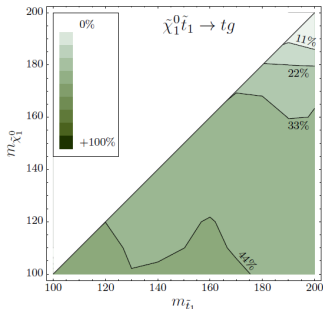


Consequences on the relic density

- huge impact on relic density through

$$\Omega_{CDM} h^2 = \frac{m_\chi n_0}{\rho_C} \propto \frac{1}{\langle \sigma V \rangle}$$

- vector boson and gluon final states will be soon finished
- similar effects up to 50% through corrections expected



Freitas (2007), arXiv:0705.4027v2 [hep-ph].

⇒ SUSY-QCD-corrections to coannihilation will have sizeable impact on relic density prediction!

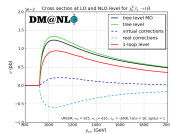
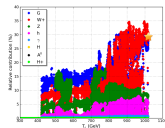
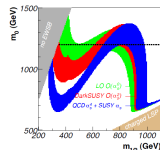
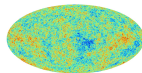


Conclusion and Outlook

- Public codes do not take into account full NLO corrections
- DM@NLO will contain SUSY-QCD corrections to Gaugino annihilation and Neutralino-Squark coannihilation
- Sizeable corrections expected and thus a huge impact on the relic density prediction
- Package DM@NLO allows to link SUSY-QCD corrections to the public codes

→ Code will be public available!

<http://dmnlo.hepforge.org>





Coannihilation with Squarks

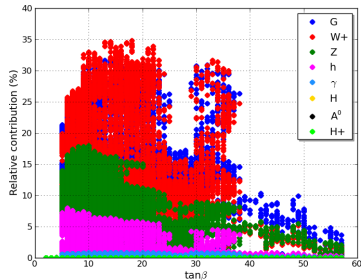
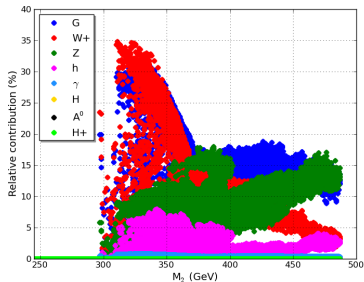
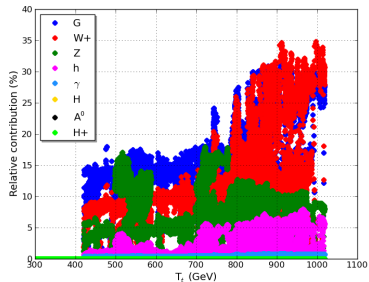
Interesting scenario: pMSSM8

- 8 free parameters:

$$\mu, \tan\beta, A_t, M_2, m_A, M_{\tilde{q}_{1,2}}, M_{\tilde{q}_3}, M_{\tilde{l}}$$

$$A_b = A_\tau = 0$$

$$M_2 = 2M_1 = M_3/3$$



Coannihilation with Squarks

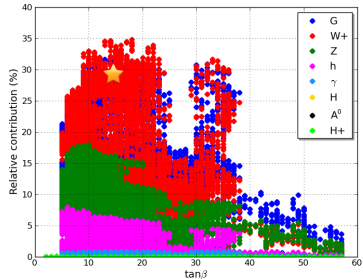
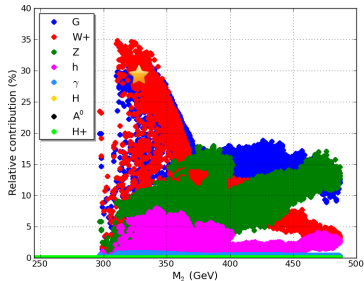
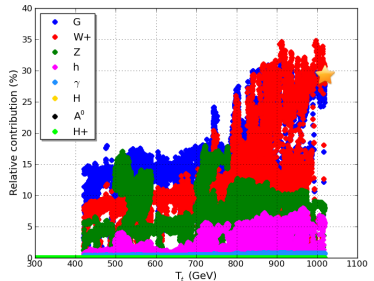
Interesting scenario: pMSSM8

- 8 free parameters:

$$\mu, \tan\beta, A_t, M_2, m_A, M_{\tilde{q}_{1,2}}, M_{\tilde{q}_3}, M_{\tilde{l}}$$

$$A_b = A_\tau = 0$$

$$M_2 = 2M_1 = M_3/3$$



Coannihilation with Squarks

One example point in pMSSM8

- $\mu = 421$, $\tan\beta = 14$, $T_t = 1017$,
 $m_A = 928$, $M_{\tilde{q}_{1,2}} = 434$, $M_{\tilde{q}_3} = 388$,
 $M_{\tilde{l}_1} = 627$,
 $A_b = A_\tau = 0$,
 $M_2 = 2M_1 = M_3/3 = 325$

- fully dominated by coannihilation processes:

$$\begin{aligned}
 \tilde{\chi}_1^0 \tilde{t}_1 &\rightarrow bW^+ & 29\% \\
 \tilde{\chi}_1^0 \tilde{t}_1 &\rightarrow tg & 26\% \\
 \tilde{t}_1 \tilde{t}_1 &\rightarrow gg & 15\% \\
 \tilde{\chi}_1^0 \tilde{t}_1 &\rightarrow tZ & 8\% \\
 \tilde{\chi}_1^0 \tilde{t}_1 &\rightarrow th & 6\%
 \end{aligned}$$

- in agreement with experimental bounds

$$\begin{aligned}
 m_h &= 125.4 \text{ GeV} \\
 \Omega h^2 &= 0.1159
 \end{aligned}$$

⇒ precise relic density prediction needs next-to-leading order corrections for coannihilation

