### Top-Quark Charge Asymmetry with a Jet Handle

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- QCD predicts a charge asymmetry for top quark pair production in hadron-hadron scattering
- The corresponding forward-backward asymmetry has been measured at CDF and D0
- Discrepancy to SM prediction
  remains between 2-3 σ
- ➡ Sign of new Physics?
- Need to measure the charge asymmetry at the LHC

Parton Level	POWHEG	CDF 9.4 fb <sup>-1</sup>	exceeding SM prediction
Inclusive	6.6%	16.4 ± 4.5 %	2.2 σ
M <sub>tt</sub> slope	(3.4 ± 1.2)10 -4 GeV -1	(15.2 ± 5)10 -4 GeV -1	2.3 σ
∆y  slope	(10. ± 2.3)10 <sup>-2</sup> GeV <sup>-1</sup>	(28.6 ± 8.5)10 <sup>-2</sup> GeV <sup>-1</sup>	2.Ι σ

(CDF, arXiv 1211.1003)

 Problem: predicted SM charge asymmetry in inclusive top pair production at LHC is very small

### Motivation



LO: no charge asymmetry

NLO: Charge asymmetry is generated due to virtual corrections (box diagrams) and real gluon emission diagrams (ISR-FSR interference)

Separating contributions with a gluon E<sup>cut</sup>:

- virtual corrections generate positive asymmetry
- real emission diagrams contribute with negative asymmetry
- need to understand the tt+jet contribution especially in different phase space regions



## tī+jet in the SM





### Charge asymmetry of $q\bar{q} \rightarrow t\bar{t} + jet$ in QCD

Differential charge asymmetry at a fixed point in phase space:

$$\frac{\mathrm{d}\hat{\sigma}_{a}}{\mathrm{d}\cos\theta} = \frac{\mathrm{d}\hat{\sigma}_{t\bar{t}}}{\mathrm{d}\cos\theta}\Big|_{\theta=\theta_{t}^{t\bar{t}}} - \frac{\mathrm{d}\hat{\sigma}_{\bar{t}t}}{\mathrm{d}\cos\theta}\Big|_{\theta=\theta_{\bar{t}}^{t\bar{t}}}$$

 $\bar{t}$  under  $t \leftrightarrow \bar{t}$ 

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 $d\hat{\sigma}_a \sim d^2_{abc} \cdot \text{antisymmetric}$ 







### Charge asymmetry of $q\bar{q} \rightarrow t\bar{t} + g$ in QCD at LO



- $\hat{A}_{C}$  [%],  $\sqrt{\hat{s}} = 1 \text{ TeV}$ 400 400 -10 500 -20600 300  $E_j$  [GeV]  $M_{t\bar{t}\bar{t}}$  [GeV 700 200 800 100 900 1000 0  $\frac{\pi}{4}$  $\frac{\pi}{2}$  $\frac{3\pi}{4}$ 0  $\pi$  $\theta_i$  [rad]
- LO symmetric tt+g diagrams are IR divergent and collinear divergent
- a transverse momentum cut on the gluon momentum, e.g. p<sub>T</sub> > 25 GeV, regulates both divergencies

 $M_{t\bar{t}}^2 \stackrel{\text{LO}}{=} \hat{s} \left(1 - 2E_i / \sqrt{\hat{s}}\right)$ 

the LO asymmetric tt+g diagrams,
 σ<sub>a</sub>, are IR divergent

- →  $\hat{A}_c = \hat{\sigma}_a / \hat{\sigma}_s$  is finite for small gluon energies
- A<sub>c</sub> strongly tends to zero for  $\hat{\theta}_j \to 0, \pi$
- → A<sub>c</sub> can be as large as -40% for central gluons

### **Results:** Tevatron

- proton-antiproton initial state
- Charge asymmetry corresponds to forwardbackward asymmetry

$$A_C^y = \frac{\sigma(\Delta y > 0) - \sigma(\Delta y < 0)}{\sigma(\Delta y > 0) + \sigma(\Delta y < 0)}, \quad \Delta y = y_t - y_{\bar{t}}$$

- ➡ Asymmetry is largest for central jets
- Cut on the jet should be applied in the partonic rest frame
- Combination of cuts results in largest asymmetry with moderate reduction of the cross section



	no cuts	$M_{t\bar{t}} \ge 450 \mathrm{GeV}$	$ \hat{y}_j  \le 0.5$	$ \Delta y  \ge 0.5$	$\begin{vmatrix}  \hat{y}_j  \le 1\\  \Delta y  \ge 0.5 \end{vmatrix}$
$A_C^y \ [\%]$	-12.6	-17.0	-24.0	-19.1	-27.5
$\sigma_s [\mathrm{pb}]$	1.42	0.61	0.43	0.78	0.48
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### Results: LHC @ 8 TeV

- ➡ proton-proton symmetric initial state
- Charge asymmetry generated for large boost along the beam axis:

$$A_C^{|y|} = \frac{\sigma(\Delta|y| > 0) - \sigma(\Delta|y| < 0)}{\sigma(\Delta|y| > 0) + \sigma(\Delta|y| < 0)}$$

- ➡ Asymmetry is largest for central jets
- Cut on the jet should be applied in the partonic rest frame
- Combination of cuts results in largest asymmetry for a similar cross section



$$y_{t\bar{t}j} \stackrel{\text{LO}}{=} \frac{1}{2} \ln \frac{x_1}{x_2} = \frac{1}{2} \ln \frac{1+\beta}{1-\beta}$$

$\begin{array}{ c c c c c } & \text{no cuts} &  \hat{y}_j  \le 0.5 &  \Delta y   \ge 1 & - &  \hat{y}_j  \le 0.5 &  \hat{y}_j  \le 0.5 \le  A  \\ \hline \\ $	$\overline{\chi_{\eta}}$
	<u>- 1911</u>
$ A_C^{ g }[\%]  -0.56   -1.30   -1.35   -1.62   -2.91   -4.04$	
$\sigma_s \text{ [pb]}  97.5  25.7  19.7  19.2  6.63  4.00$	

# tī+jet with massive color-octet bosons





### Lagrangian, contributing diagrams

$$\mathcal{L} = -g_s f_{abc} \left[ \left( \partial_\mu G^a_\nu - \partial_\nu G^a_\mu \right) G^{b\mu} g^{c\nu} + G^{a\mu} G^{b\nu} \left( \partial_\mu g^c_\nu \right) - ig_s \bar{q}_i \gamma^\mu G^a_\mu T^a \left[ g^i_V + \gamma_5 g^i_A \right] q_i$$

- $G^a_\mu$  massive gluon field
- ➡  $q_V^i, q_A^i$  vector, axial-vector couplings of the massive gluons to quarks
- All combinations of diagrams can contribute to the cross sections σ<sub>a</sub> and σ<sub>s</sub>
- Asymmetry depends on the heavy gluon mass M<sub>G</sub>, its width Γ<sub>G</sub> and products of coupling combinations, e.g. g<sup>q</sup><sub>V</sub>g<sup>t</sup><sub>V</sub> or g<sup>q</sup><sub>A</sub>g<sup>t</sup><sub>A</sub>







### **Contributing diagrams**

- Heavy gluon scenario, M<sub>g</sub> = 2 TeV, consistent with top pair cross section measurements and di-jet
- Large M<sub>tt</sub> cut enhances the cross section of the heavy color octet bosons with respect to SM cross section



$M_G = 2 \mathrm{TeV}$	$V^+$	$V^{-}$	$A^+$	$A^-$	$VA^{++}$	$VA^{}$	$VA^{+-}$
$g_V^q$	0.5	0.5	0	0	0.35	0.35	0.35
$g_V^t$	2	-2	0	0	1.5	-1.5	1.5
$g^q_A$	0	0	0.5	0.5	0.35	0.35	0.35
$g_A^t$	0	0	2	-2	1.5	-1.5	-1.5
$\Gamma_G/M_G$ [%]	17.7	17.7	17.3	17.3	19.4	19.4	19.4

### Results: LHC @ 8 TeV

$$\Delta A_C^{|y|} = A_C^{|y|,\text{tot}} - A_C^{|y|,\text{SM}}$$

- Large asymmetries are generated due to axial-vector couplings
- Also vector couplings generate additional asymmetry (not in tt inclusive at LO)
- Similar results for LHC 14, some additional phase space cuts may need to be applied

$M_{t\bar{t}}^{\min} = 1 \mathrm{TeV}$	$\Delta A_C^{ y } \ [\%]$
$V^+, V^-$	-0.22, -2.3
$A^+, A^-$	-6.7, +4.3
$VA^{++}$	+5.4
$VA^{}$	+8.9
$VA^{+-}$	-6.9



### Results: LHC @ 8 TeV

- σ<sub>a</sub> tends to zero for small gluon angles and vector couplings (QCD like)
- σ<sub>a</sub> has a collinear divergency for small gluon angles and axialvector couplings
- opposite for symmetric cross
  section σ<sub>s</sub>



QCD (black), g-G (solid) interference and G-G (dotted) interference for the massive gluon benchmarks V<sup>+</sup> (green) and A<sup>+</sup> (red)

### **Concluding Remarks**

- Promising prospect to measure the charge asymmetry in tt+jet
- SM: Asymmetry is largest for central jets
- SM: Charge asymmetry can be enhanced by suitable phase space cuts
  - Tevatron:  $|\hat{y}_j| \le 1, |\Delta y| \ge 0.5 \rightarrow A_C^y = -27.5\%$
  - LHC @ 8 TeV: for strong cuts up to -4%
- Heavy color octet vector bosons that can explain the Tevatron asymmetry can also generate large asymmetries at the LHC
- Differential distributions with respect to the jet scattering angle can give additional information about the coupling structure



