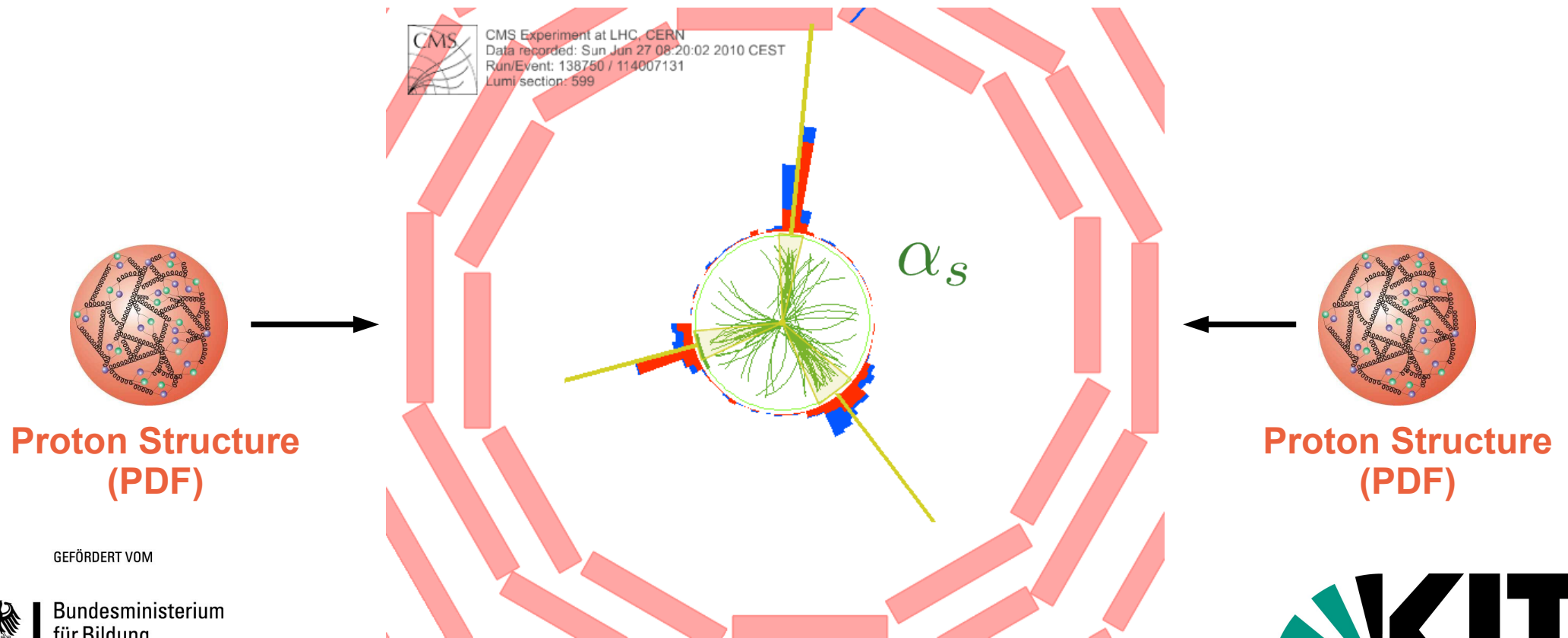


## Determination of the strong Coupling from 3-Jet Rates at the Terascale



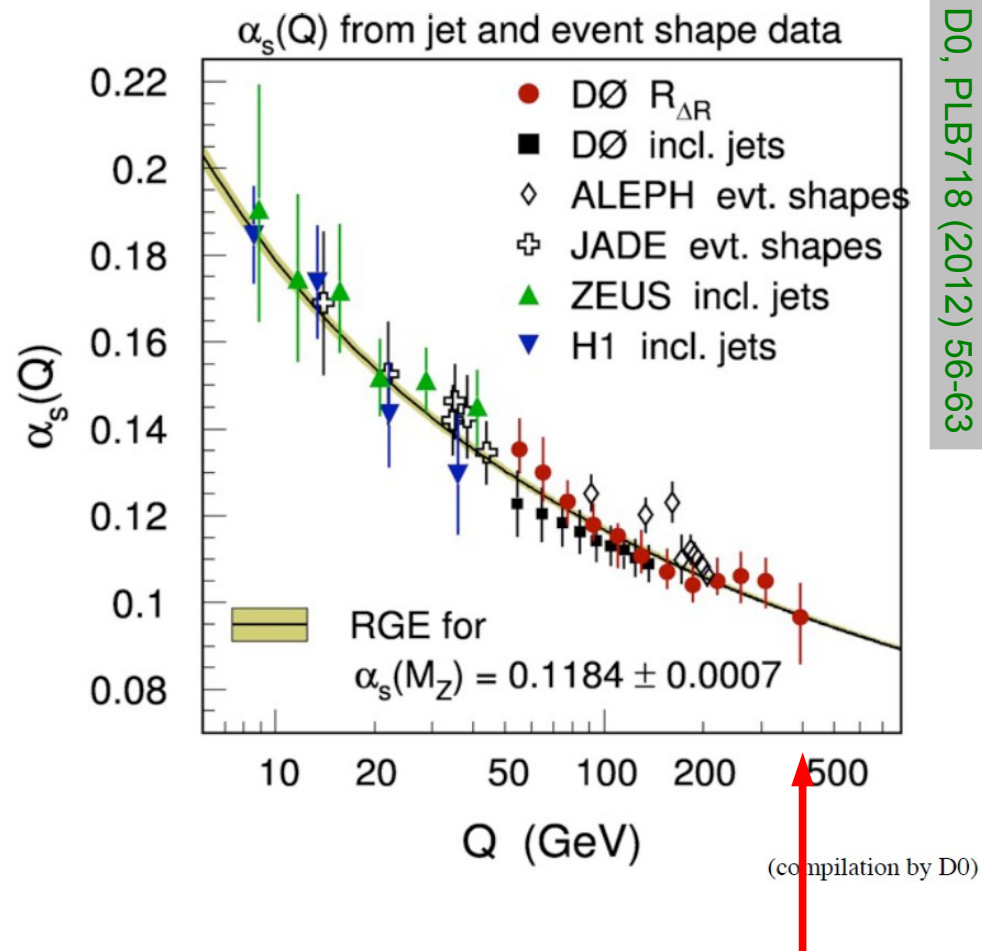
GEFÖRDERT VOM



Bundesministerium  
für Bildung  
und Forschung

Klaus Rabbertz, KIT

- Motivation
- The Measurement
- Uncertainties
- Comparison to Theory
- Extraction of the strong Coupling  $\alpha_s$
- Conclusions and Outlook



DØ, PLB718 (2012) 56-63

CMS-PAS-QCD-11-003 (2012).

**Tevatron limit published this year**

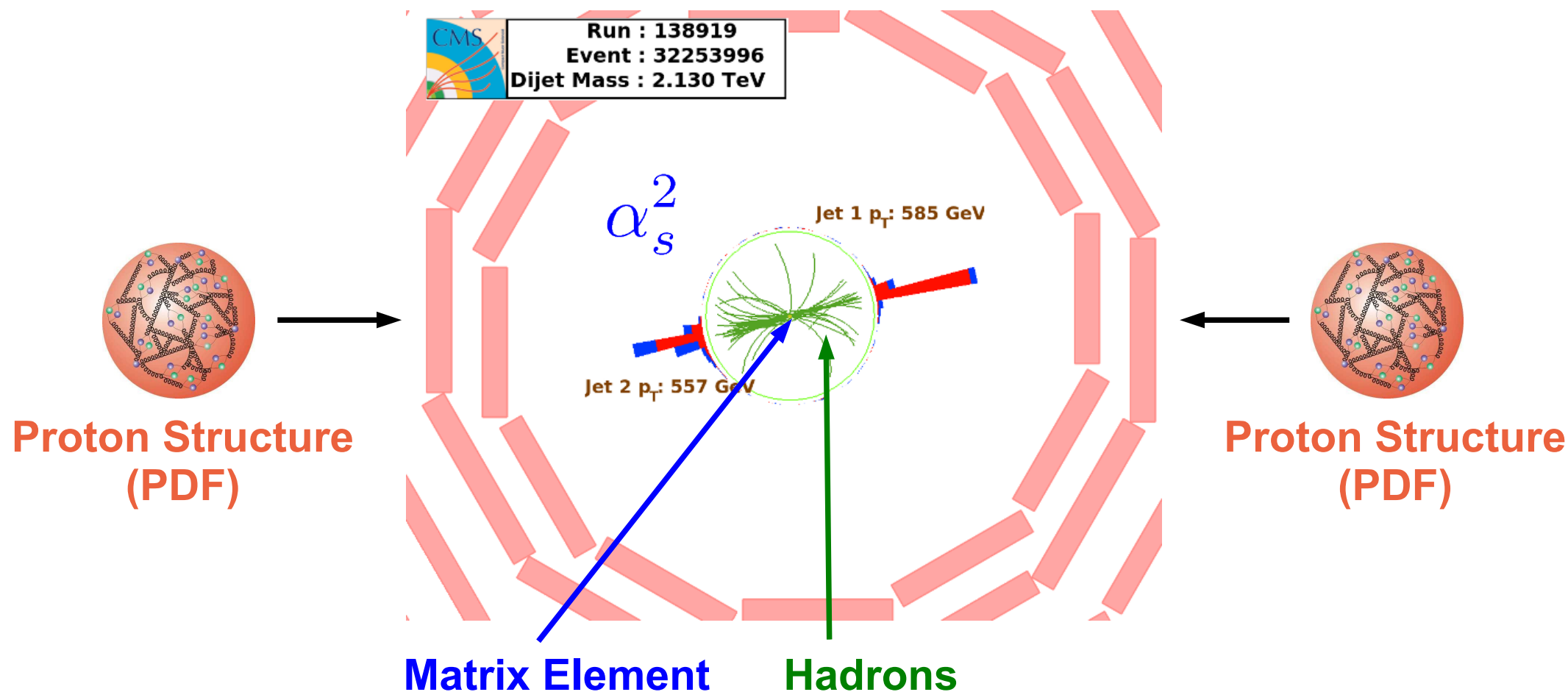
**We'll start here ...**



**All results without explicit reference are taken from this CMS analysis!**

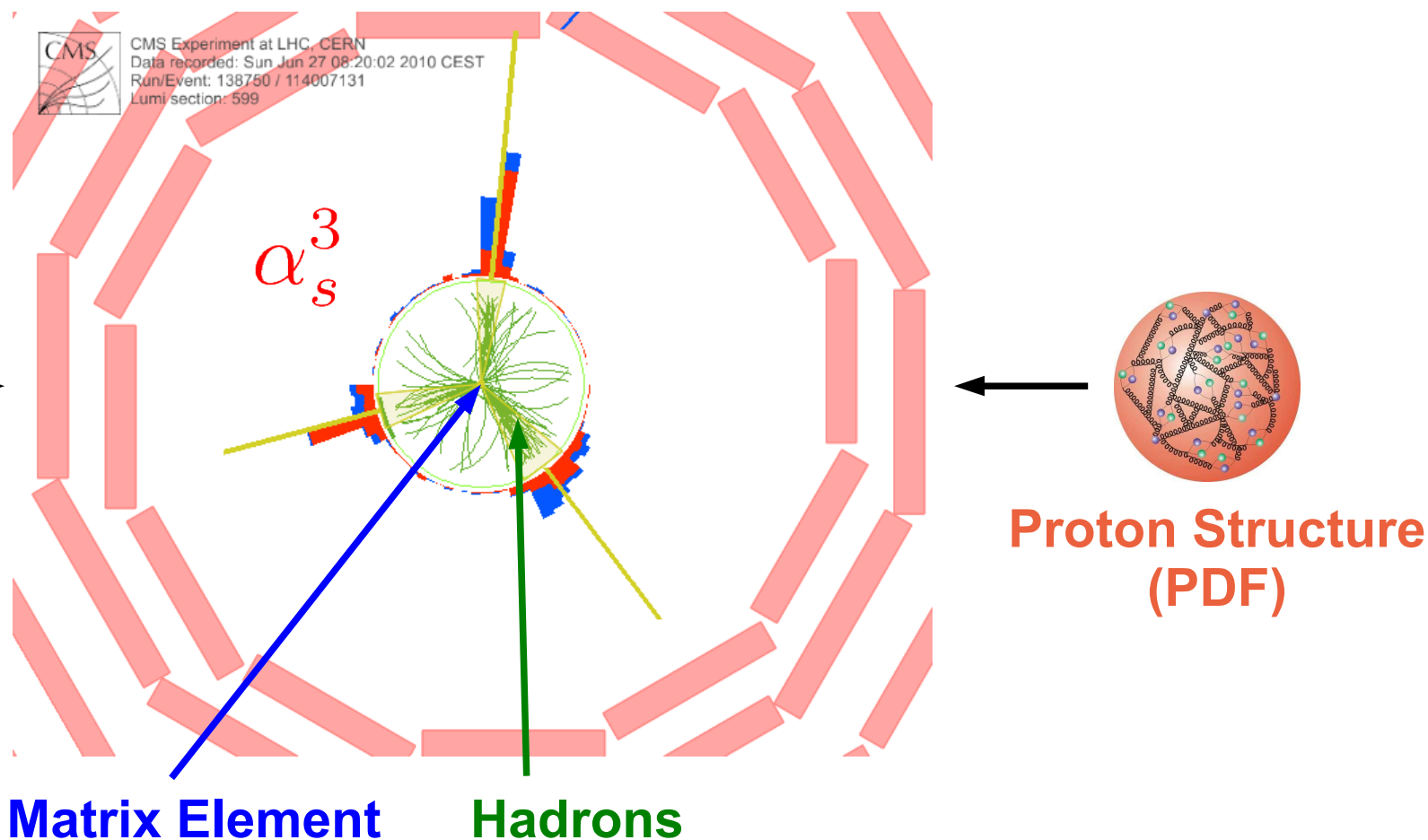
# Jets at LHC

Abundant production of jets → hadron colliders are “jet laboratories”  
Learn about hard QCD, the proton structure, non-perturbative effects ...



# Jets at LHC

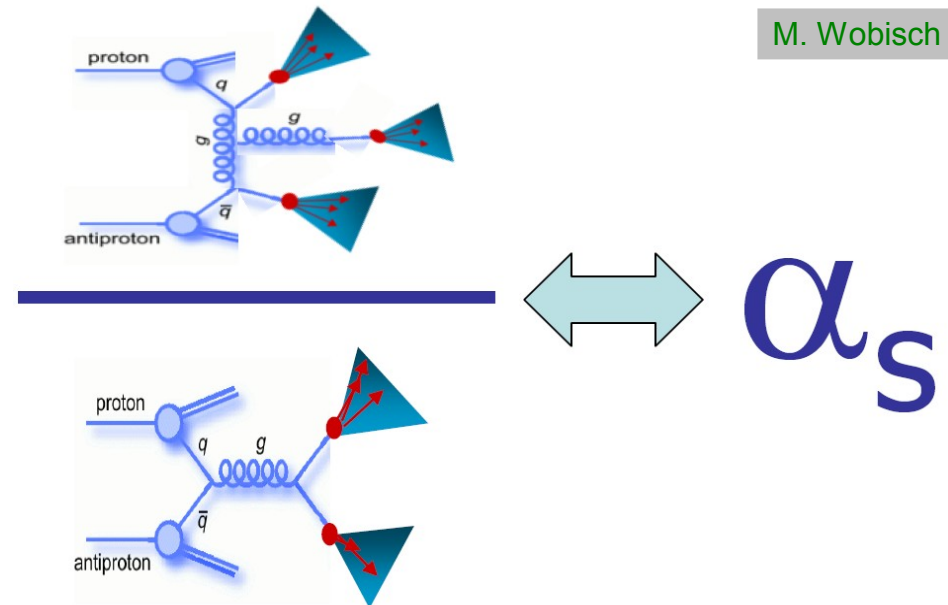
**Abundant production of jets → hadron colliders are “jet laboratories”  
... and the strong coupling  $\alpha_s$  !**



# 3-Jets and $\alpha_s$

M. Wobisch

- Avoids direct dependence on PDFs and the RGE of QCD
- Use cross-section ratios!
- → reduces other theor. and exp. uncertainties along the way
- → eliminates luminosity dependence (normalization)
- Choices of CMS:
  - ➔ Ratio of inclusive 3-jet to 2-jet production
  - ➔ Average dijet  $p_T$  as scale
  - ➔ Scalar  $p_T$  sum ( $H_T$ ) disfavoured
- Other 3-jet observables possible, see e.g. propositions by D0



$$R_{32} = \frac{d\sigma_{3+}/dp_T}{d\sigma_{2+}/dp_T} \propto \alpha_s(Q)$$

$$Q = \langle p_{T1,2} \rangle = \frac{p_{T1} + p_{T2}}{2}$$

D0, PLB718 (2012) 56-63

# Analysis Setup

- CMS data of 2011
- Anti-kT jet algorithm with  $R = 0.7$ 
  - ➔ Compatible results with  $R = 0.5$  as alternative
- Selection in rapidity  $y$  (1 bin):
  - ➔ Ensure tracker coverage
  - ➔ Two jets leading in  $p_T$  must be selected
  - ➔ Ensure hard dijet event
- Minimal transverse momentum  $p_T$ :
  - ➔ Alternative thresholds 50 and 100 GeV checked
  - ➔ Alternative relative cut on hardness of 3<sup>rd</sup> jet tested
- Minimal average 2-jet  $\langle p_{T1,2} \rangle$  (27 bins):
- O(2000) 2-jet ev. incl. O(300) 3-jet events above 1 TeV

$$\mathcal{L}_{\text{int}} = 5.0 \text{ fb}^{-1}$$

$$|y| < 2.5$$

$$p_T > 150 \text{ GeV}$$

$$\langle p_{T1,2} \rangle > 250 \text{ GeV}$$

# Data Treatment

- Three single-jet triggers (highest  $p_T$  threshold 370 GeV)  $\epsilon = 100\%$ 
  - ➔ Efficiency checked separately for incl. 2- and 3-jet events
- Particle-flow technique to reconstruct input objects to jet clustering  $\epsilon > 99\%$
- Standard CMS event and jet selection criteria apply
- $(\eta, p_T)$ -dependent jet energy correction factors, typically:  $c_{\text{JEC}} \approx 1.2 \dots 1.0$
- Correction of detector effects using Bayesian iterative unfolding (RooUnfold)  $c_{\text{DET}} < 5\%$ 
  - ➔ Propagation of stat. uncertainties & correlations with MC toy method
  - ➔ Cross-checked with SVD unfolding
  - ➔ Comparison of directly unfolded ratio  $R_{32}$  versus separate unfolding of inclusive 2- and 3-jet spectra



# Experimental Uncertainties

- **Jet energy correction, known to 2.0 - 2.5%:**

$$\Delta R/R \approx 1.2\%$$

- ➔ Provided as 16 mutually uncorrelated sources; fully correlated within source; Gaussian behaviour assumed
- ➔ Dominated by absolute scale, followed by high pT extrapolation

- **Unfolding uncertainty accounting for:**

$$\Delta R/R < 1.0\%$$

- ➔ Variation of jet  $p_T$  spectral slopes following differences from Pythia6 Z2 (agrees with MadGraph) and Herwig++ 2.3
- ➔ Variation of jet energy resolution (JER)
- ➔ Addition of non-Gaussian tails to JER

- **Luminosity (normalization) uncertainty cancels**

- **No assumptions on bin-to-bin correlations with respect to  $y$  necessary, only 1 bin considered**

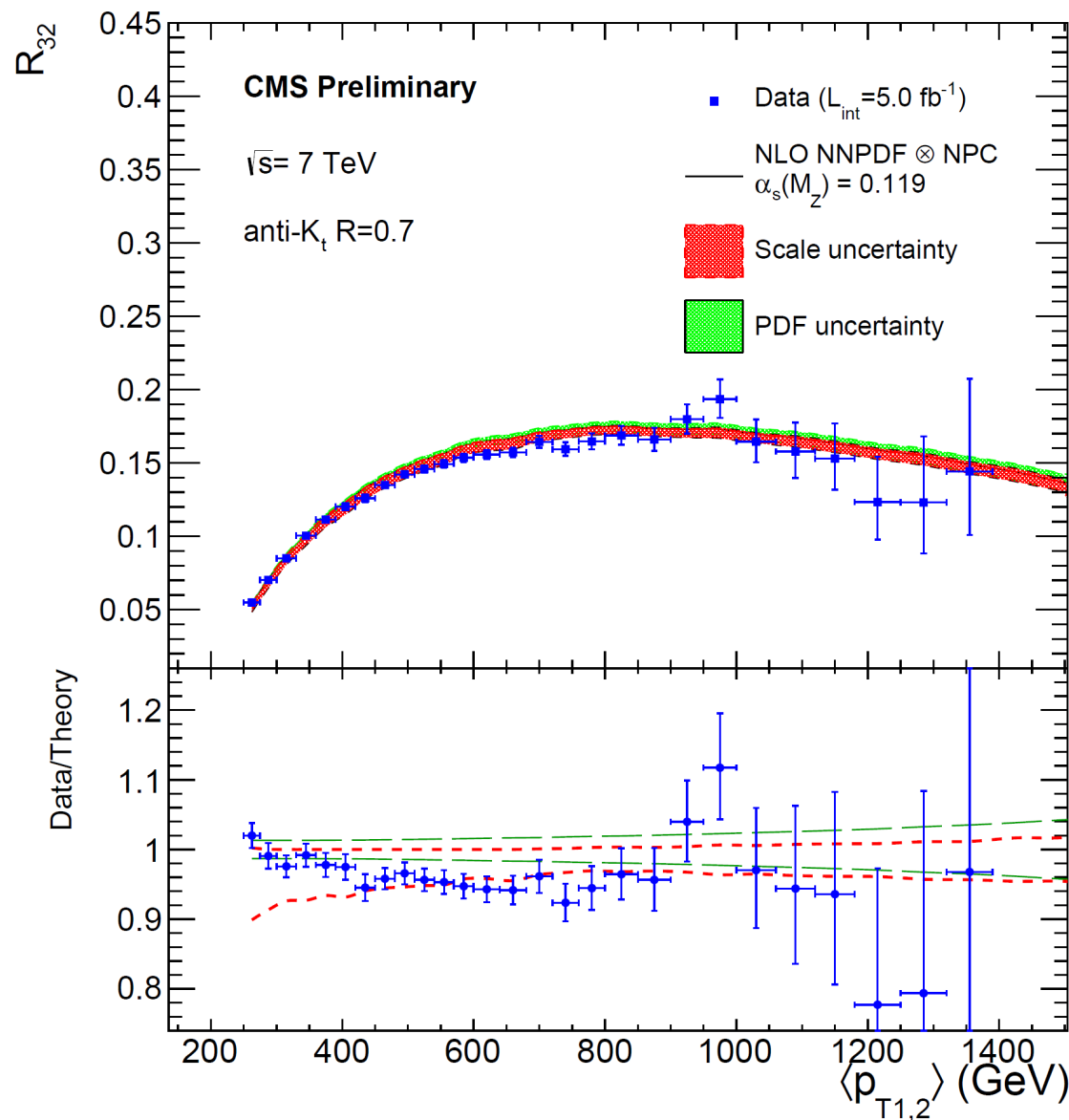
- **Statistical uncertainties propagated via unfolding**



- Using NLOJet++ within fastNLO framework
  - ➔ Fast recalculable NLO incl. 2- and 3-jet cross sections
  - ➔ Same binning as the data
- Using global PDF sets at NNLO with fits for series of  $\alpha_s$  values
  - ➔ NNPDF21, MSTW2008, CT10 and **ABM11**
  - ➔ Difference between use of NLO vs. NNLO PDF found negligible for  $R_{32}$
- Scale uncertainties evaluated via 6-point scheme
  - ➔ Max. deviations using scale factors (1/2,1/2), (1/2,1), (1,1/2), (1,2), (2,1), (2,1/2) for renormalization and factorization scales
- Non-perturbative corrections account for effects of multiple parton interactions and hadronization
  - ➔ Correction below 2%, uncertainty negligible

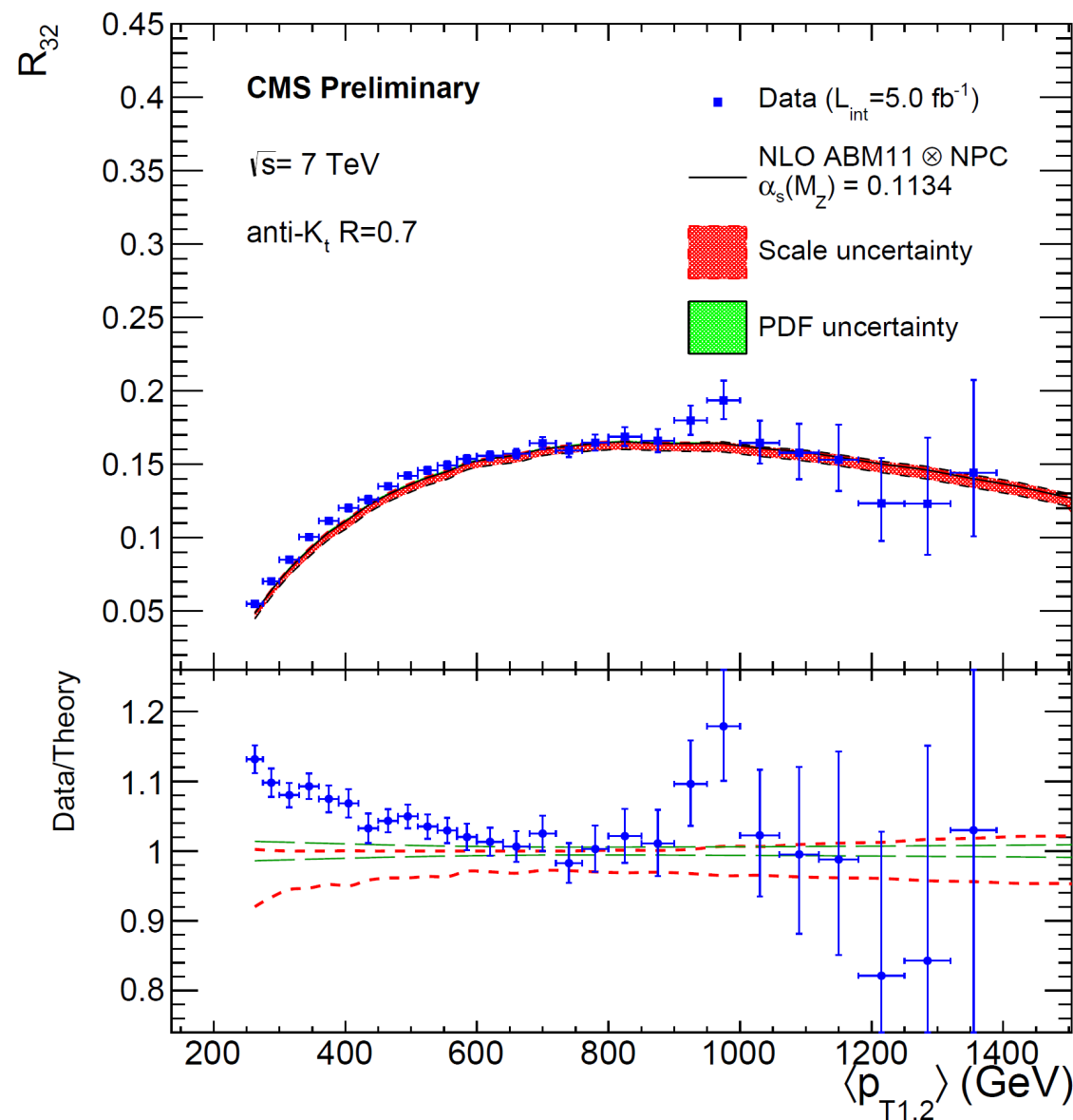
# Data comparison to NNPDF21

- Agreement within uncertainties
  - Scale uncertainty:  $+2\%$   
 $-5\%$
  - PDF uncertainty:  $1.5 - 2.3\%$
- Fits only above 400 GeV to avoid threshold effects
- Similarly described by CT10 and even better by MSTW2008
- Discrepancies observed with ABM11



# Data comparison to ABM11

- **Discrepancies with ABM11 especially below 600 GeV**
- **Fits of the strong coupling tend versus the upper edge of the available series in  $\alpha_s$**
- ➡ **No result from ABM11 to report**
- **Much smaller gluon down to 50% at high  $x$  at the same time as preference for smaller couplings**
- **Decorrelation of gluon and  $\alpha_s$  via higher twist not present in other global PDFs ?**
- **Provide ABM11 PDFs with different settings for higher twist ?**
- **To be further discussed ...**



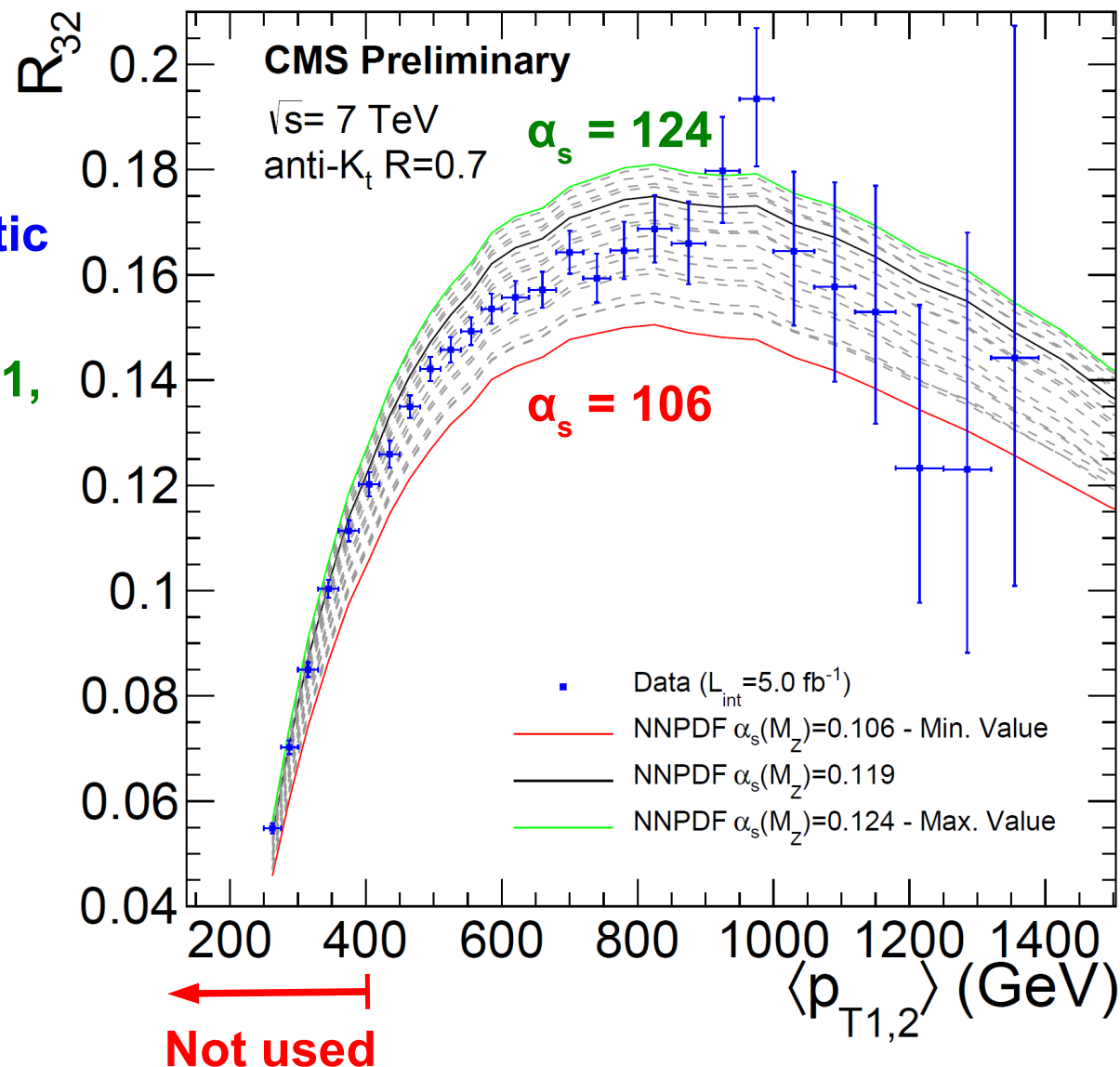
# Sensitivity to $\alpha_s$

- Fits only above 400 GeV to avoid threshold effects
- Error bars show full uncertainty including the correlated systematic ones
- Compatible results from NNPDF21, CT10 and MSTW2008 with  $\chi^2$  fit using correlated experimental uncertainties:

**NNPDF21:**  $\alpha_s(M_Z) = 0.1143 \pm 0.0064$

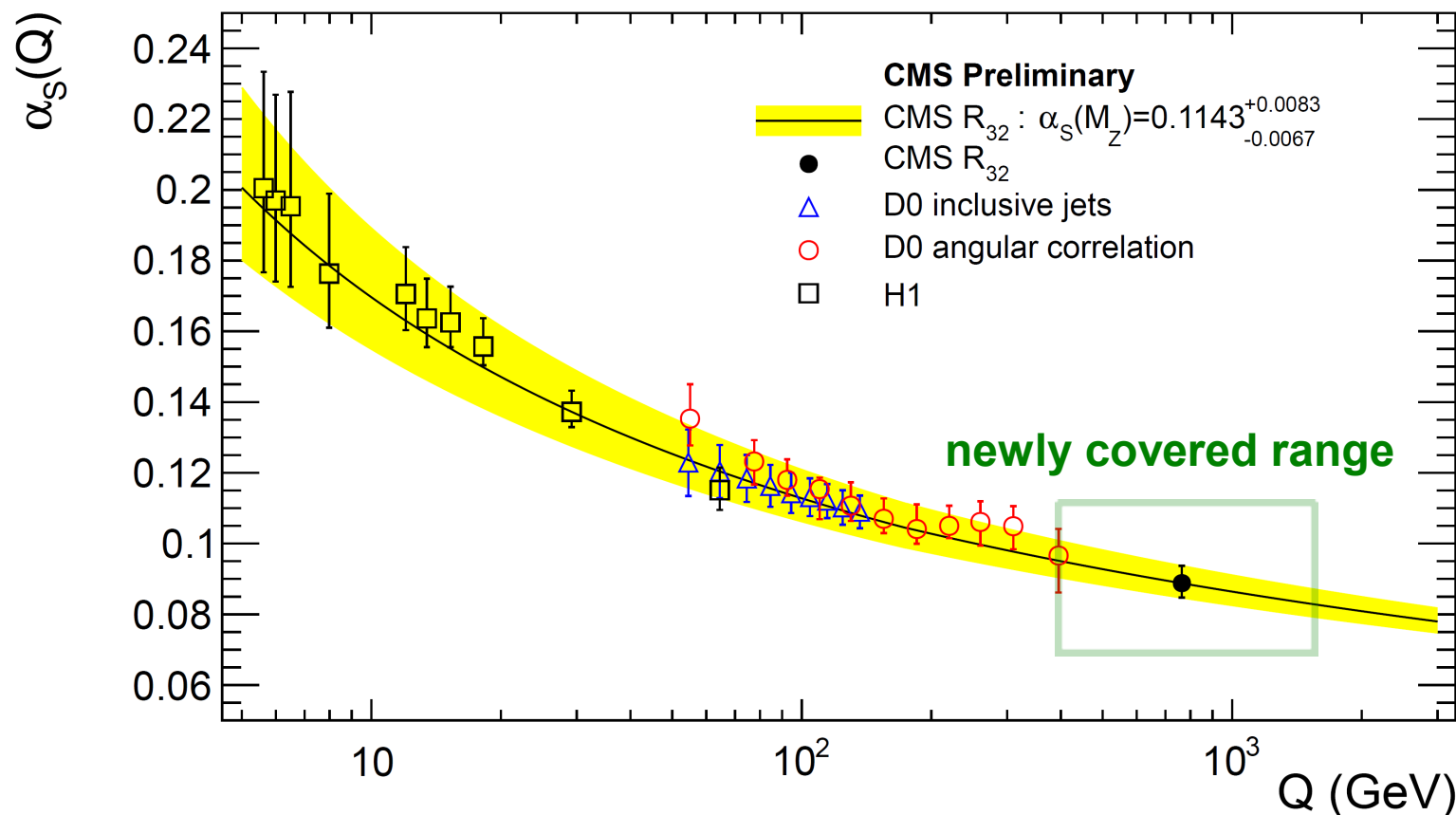
**CT10:**  $\alpha_s(M_Z) = 0.1130 \pm 0.0080$

**MSTW2008:**  $\alpha_s(M_Z) = 0.1135 \pm 0.0096$



# Determination of $\alpha_s$

- Comparison to extractions from other hadron collider experiments
- Although only one point shown here extraction works equally well in e.g. four subranges



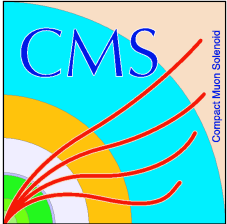
**PDF uncertainty:** Repeat fit for each replica  $\rightarrow$  get estimators for  $\mu$  and  $\sigma$   
**Scale uncertainty:** Repeat fit for all six variations  $\rightarrow$  get maximal deviation

$$\alpha_s(M_Z) = 0.1143 \pm 0.0064 \text{ (exp)} \pm 0.0019 \text{ (PDF)} \pm_{0.0000}^{0.0050} \text{ (scale)}$$

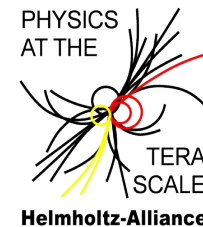
# Conclusions & Outlook

- First determination of the strong coupling at the Terascale (TeV)
- Running of  $\alpha_s$  tested with mostly PDF independent ratio observable  $R_{32}$
- No deviation from expected running, i.e. almost flat at high  $p_T$ , observed as could be expected from new coloured particles e.g. gluinos
- More data at high  $p_T$  and test of other observables may still improve achievable statistical and experimental accuracy
- More precise theory (jets at NNLO ...) desperately wanted!

**Thank you for your attention!**

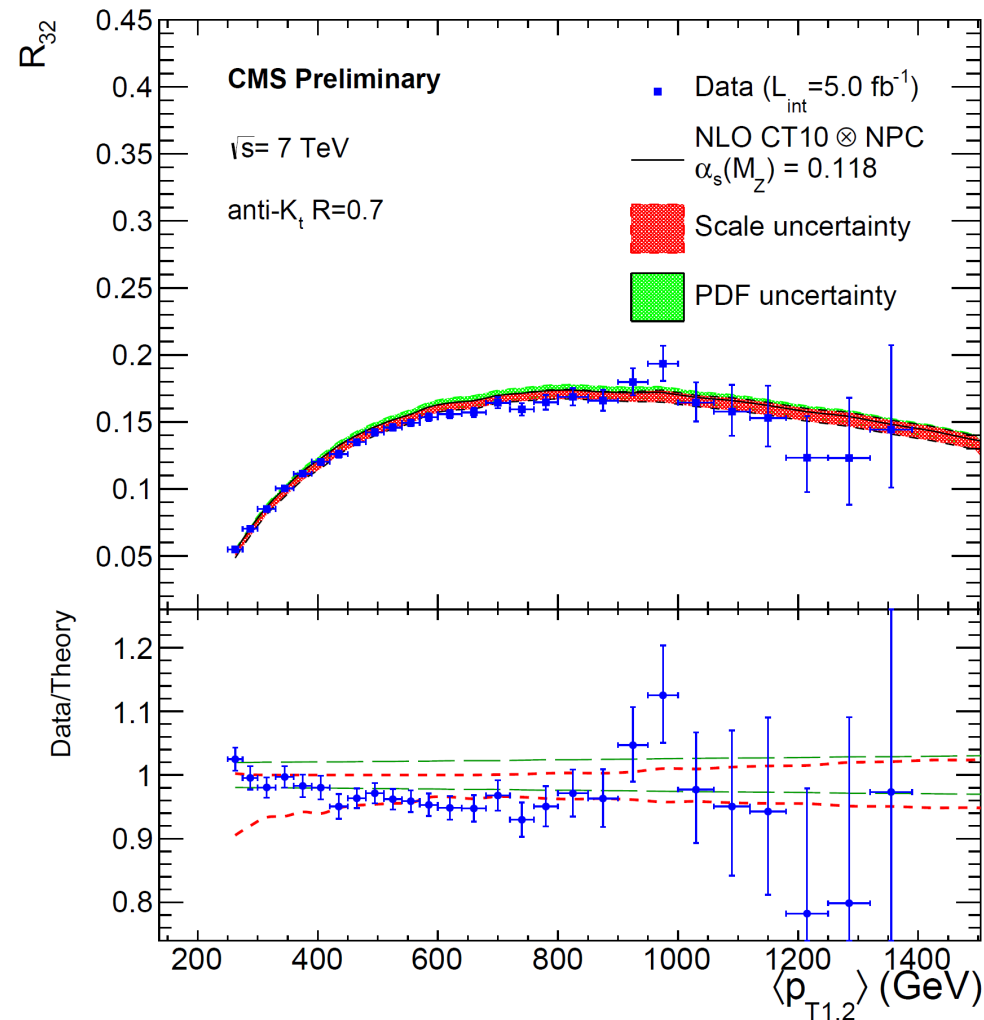
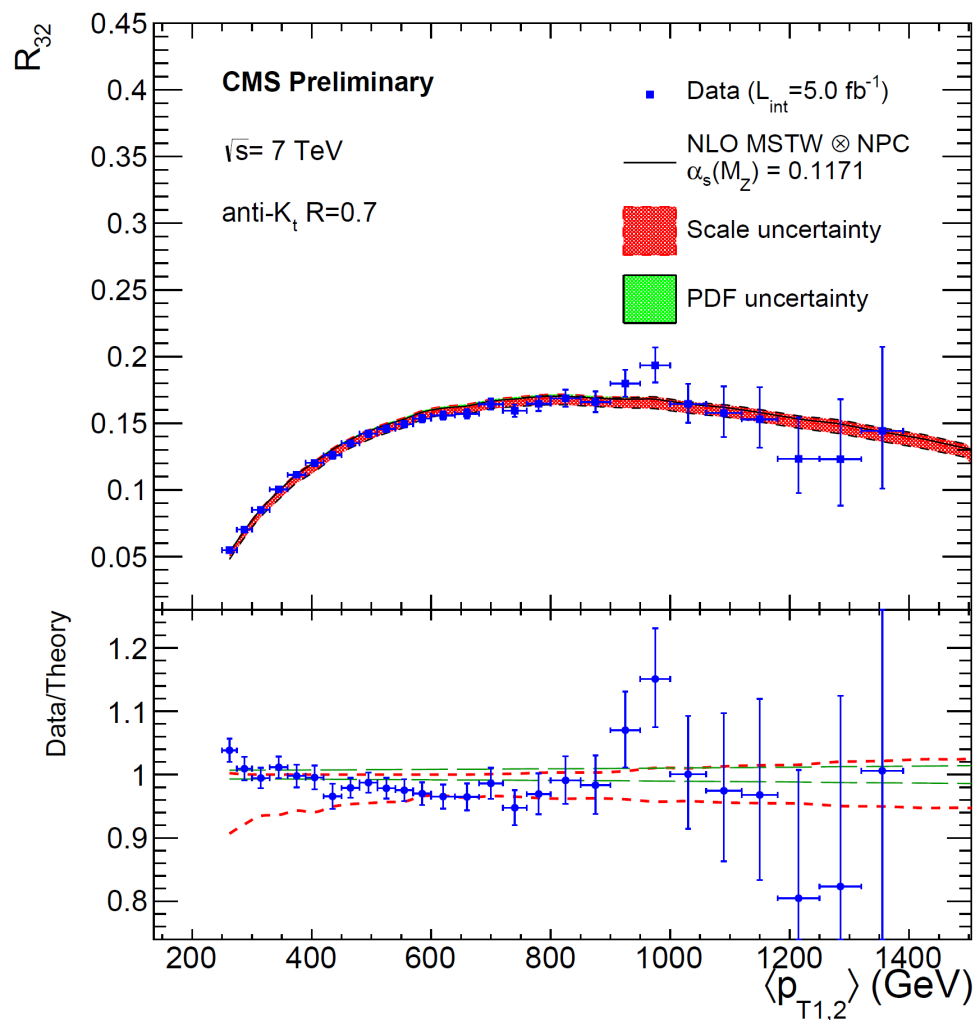


# ***Backup Slides***

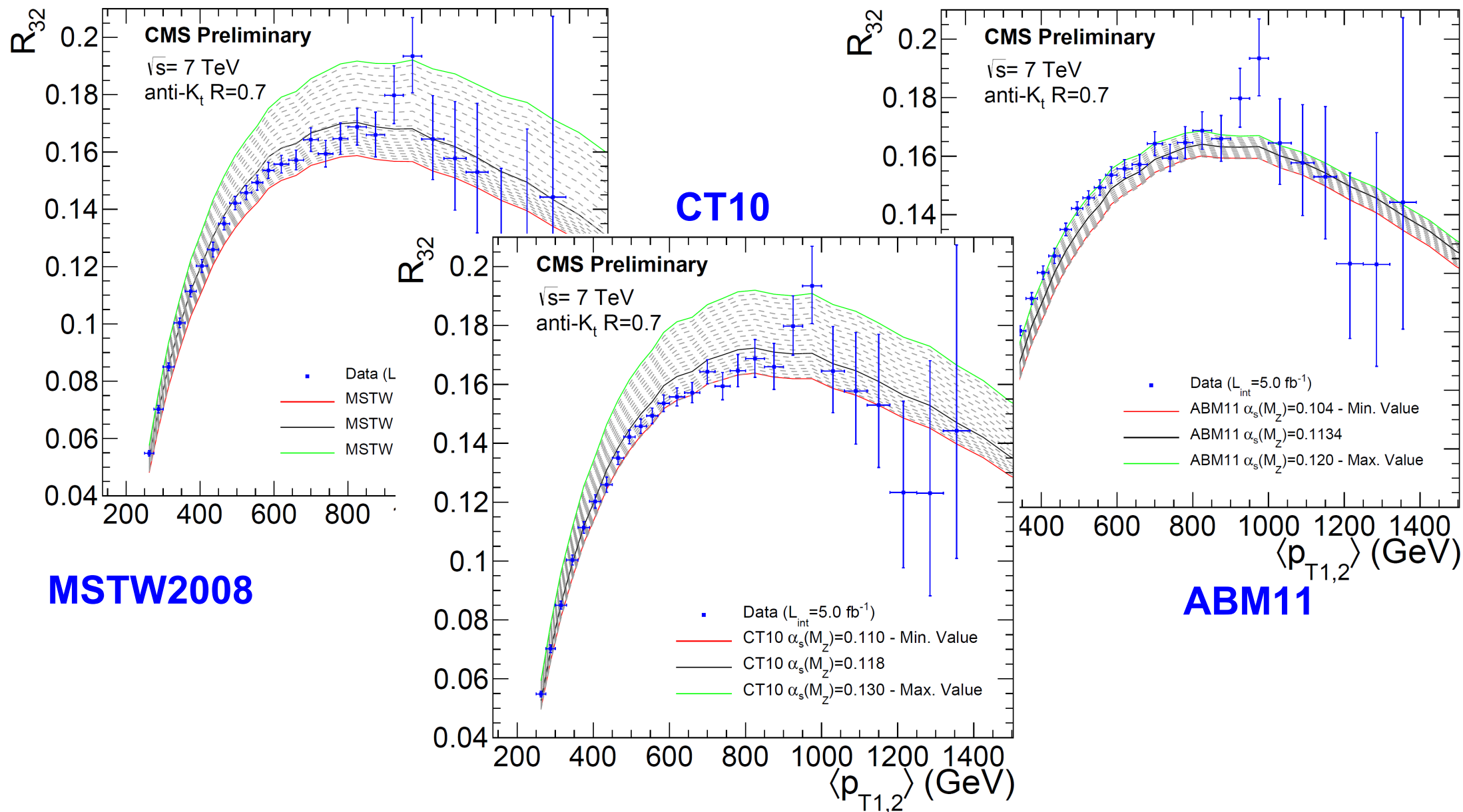




# Data comparison to MSTW2008 and CT10

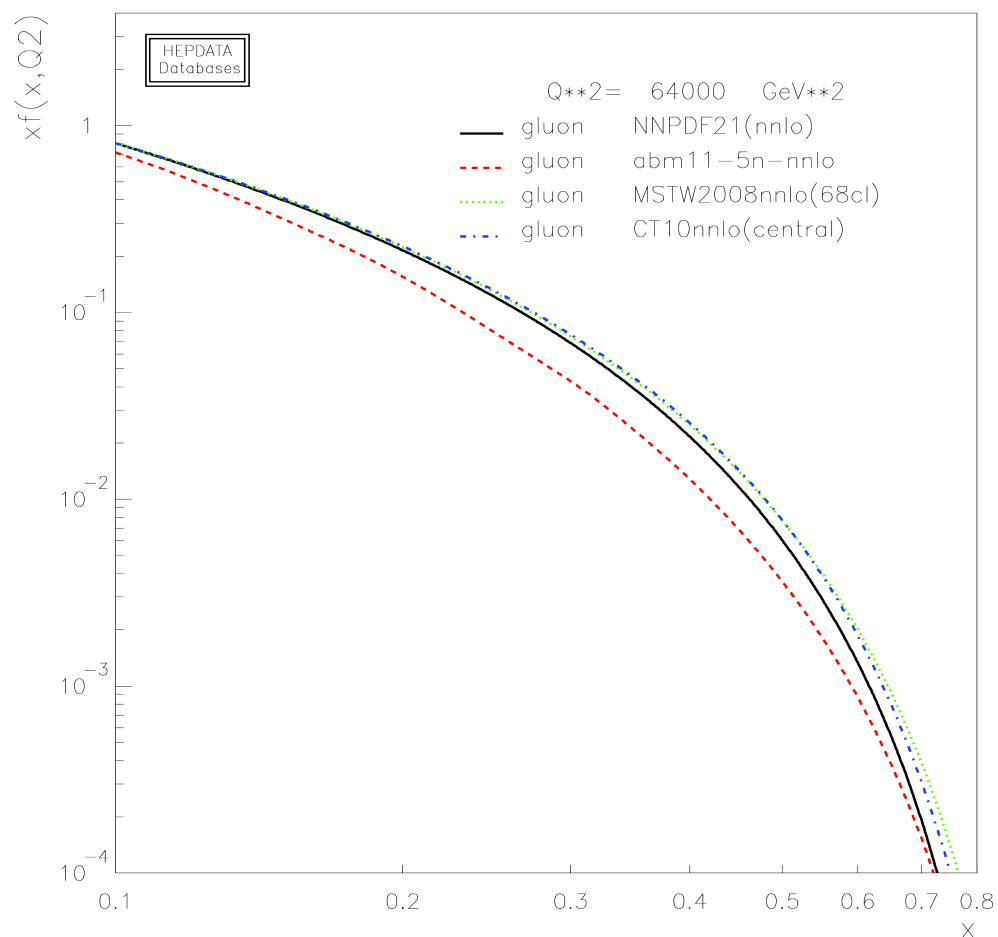


# Sensitivity to $\alpha_s$ (other PDFs)

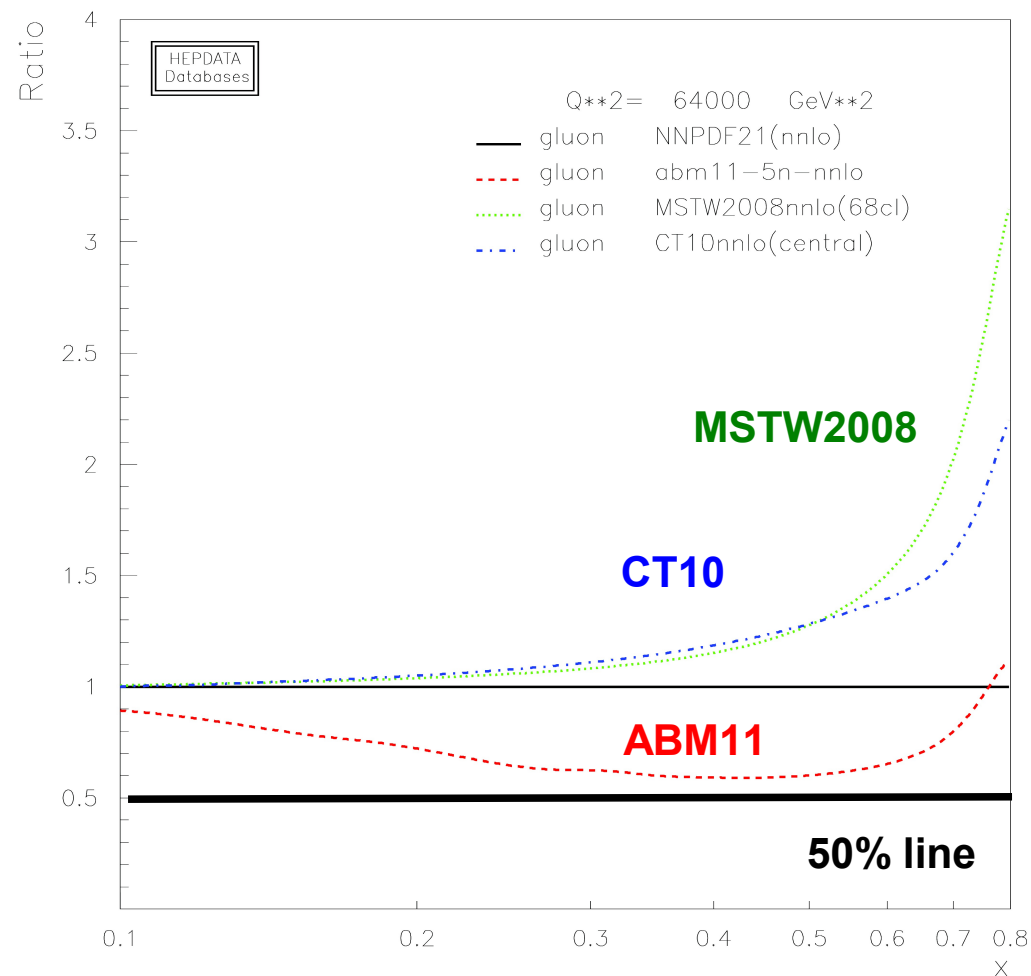


# Gluon PDF at high $x$

$xg(x, Q^2)$



Ratio to NNPDF21

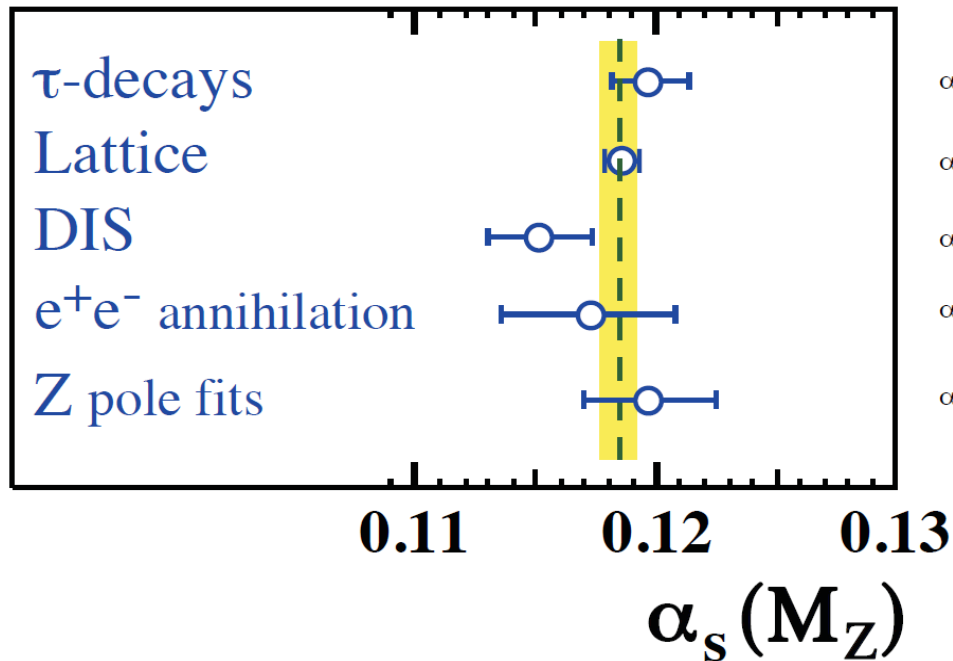


$x$  from 0.1 to 0.8;  $Q^2 = 64000 \text{ GeV}^2$

HEPDATA PDF Plotter

# Strong Coupling $\alpha_s$

## World Summary of $\alpha_s$ 2012, S. Bethke:



$$\alpha_s(M_Z) = 0.1197 \pm 0.0016$$

$$\alpha_s(M_Z) = 0.1185 \pm 0.0007$$

$$\alpha_s(M_Z) = 0.1151 \pm 0.0022$$

$$\alpha_s(M_Z) = 0.1172 \pm 0.0037$$

$$\alpha_s(M_Z) = 0.1197 \pm 0.0028$$

$$\rightarrow \alpha_s(M_Z) = 0.1184 \pm 0.0007$$

PDG2012

### NLO $\alpha_s$ in global PDFs:

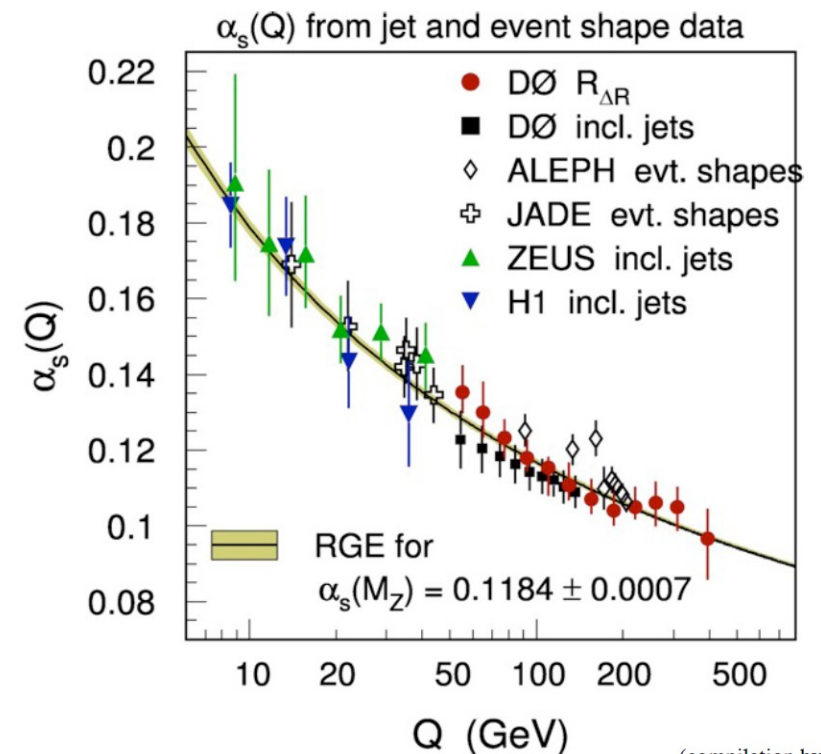
ABM11:	0.1134 (NNLO)
CT10:	0.1180
GJR08:	0.1178
HERAPDF1.5:	0.1176
MSTW2008:	0.1200
NNPDF2.1:	0.1190

But:

Jet data from hadron colliders  
not included!

Jets at NNLO urgently needed!

Recent progress reported by  
Th. Gehrmann at QCD@LHC.



(compilation by D0)

# $\alpha_s$ from inclusive Jets

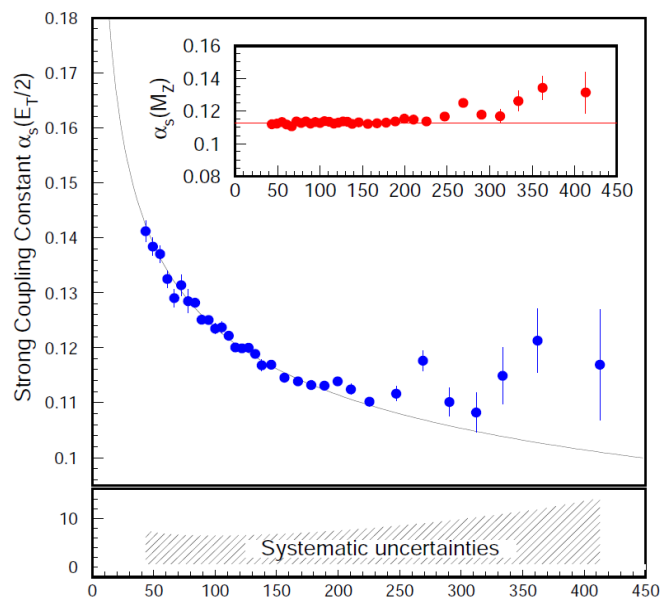
**CDF:**  $\alpha_s(M_Z) = 0.1178 \pm 0.0001(\text{stat})_{-0.0095}^{+0.0081}(\text{expt.syst})$

**D0:**  $\alpha_s(M_Z) = 0.1161_{-0.0048}^{+0.0041}(\text{total})$

**M/S:**  $\alpha_s(M_Z) = 0.1151 \pm 0.0001(\text{stat}) \pm 0.0047(\text{expt.syst})_{-0.0073}^{+0.0080}(p_T, R, \mu, \text{PDF}, \text{NP})$

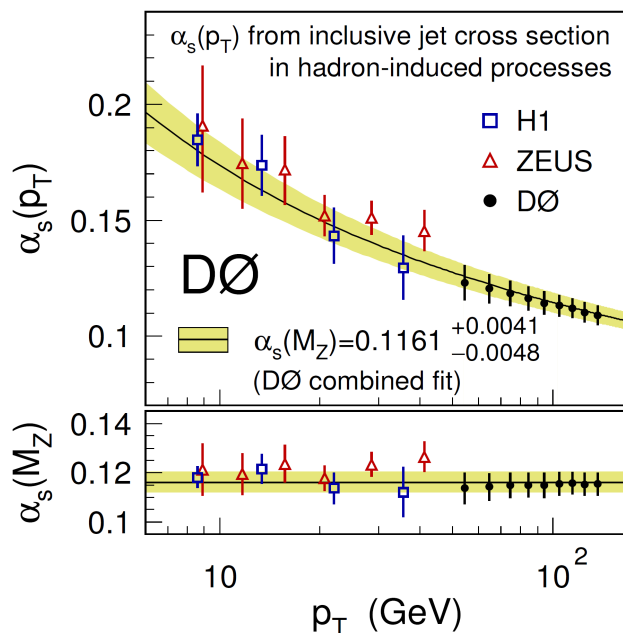
## Problem:

Via the PDFs assumes the validity of the running of  $\alpha_s$  according to the RGE  
D0 explicitly restricts phase space to where the RGE is already established.



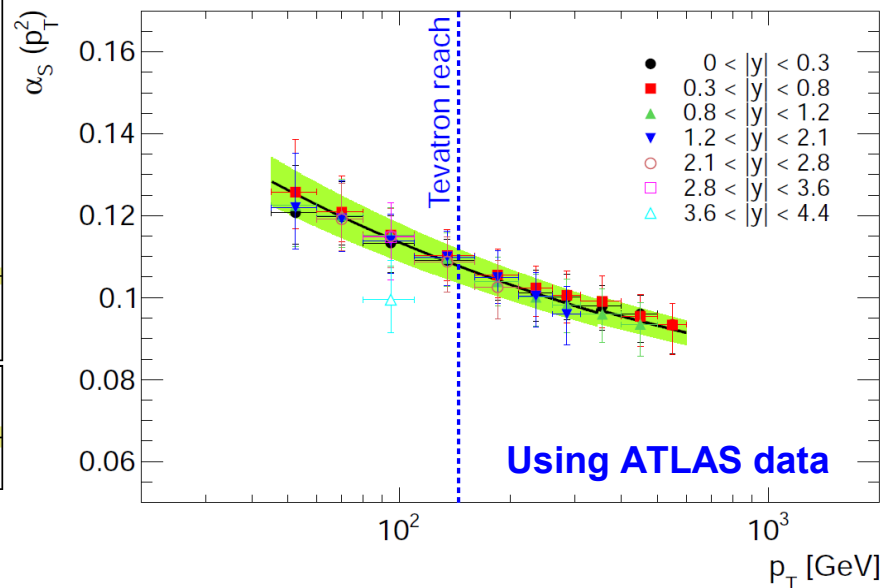
CDF, PRL88, 2002

Klaus Rabbertz



D0, PRD80, 2009

Hamburg, Germany, 03.12.2012

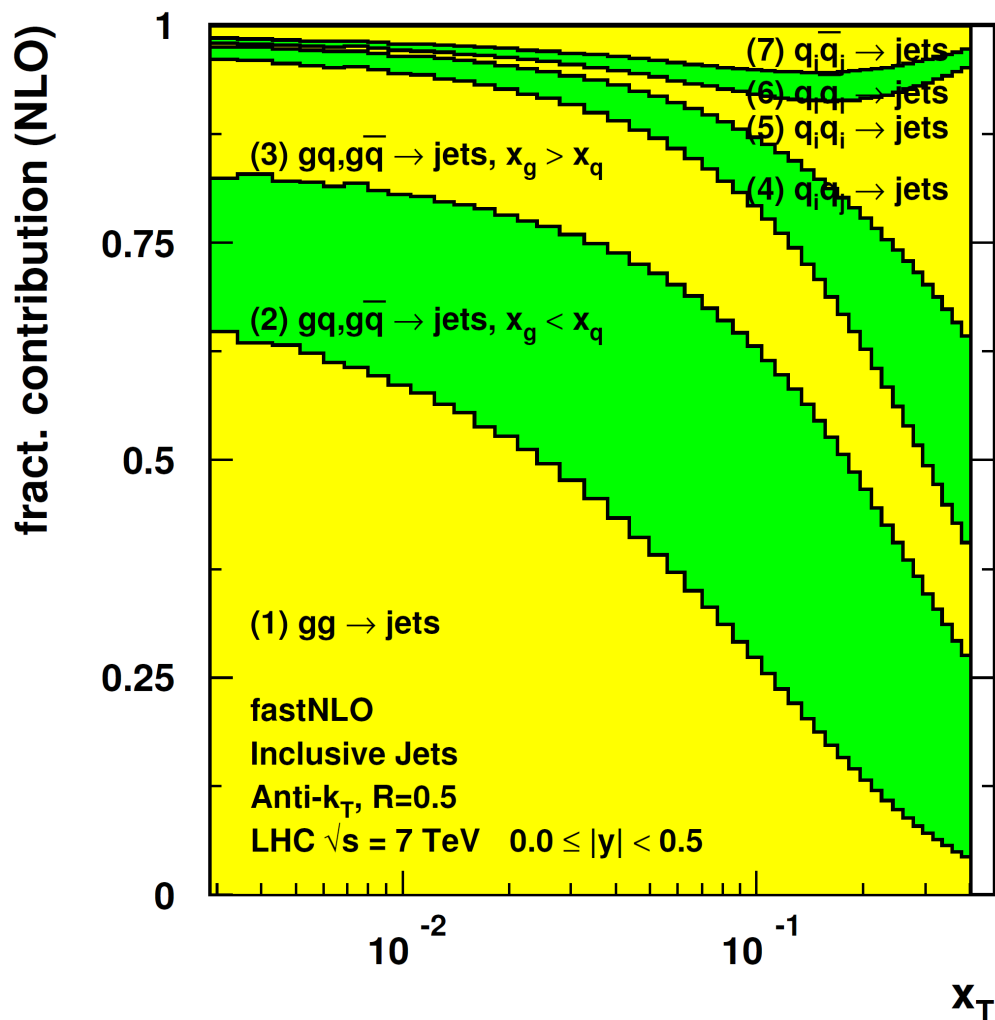


Malaescu/Starovoitov, EPJC72, 2012

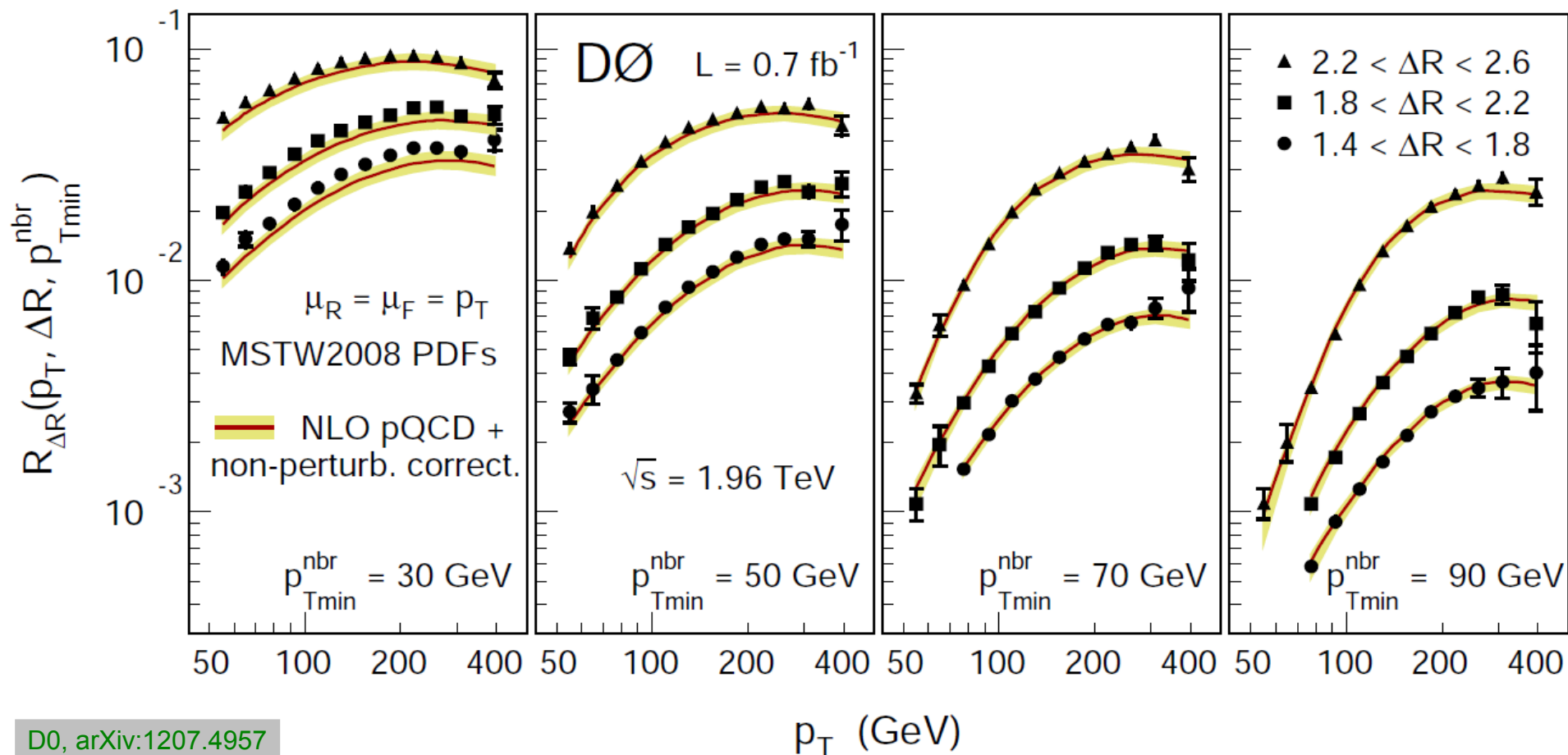
6. Terascale Workshop 2012

20

# Inclusive Jets



# New jet angular correlation Observable from D0



D0, arXiv:1207.4957

$$\alpha_s(M_Z) = 0.1191^{+0.0048}_{-0.0071}(\text{total})$$

$$\pm 0.0003(\text{stat}) + {}^{+0.0007}_{-0.0009}(\text{exp.}) + {}^{+0.0002}_{-0.0001}(\text{NP}) + {}^{+0.0010}_{-0.0005}(\text{MSTW}) + {}^{+0.0000}_{-0.0024}(\text{PDFset}) + {}^{+0.0046}_{-0.0066}(\text{scale})$$

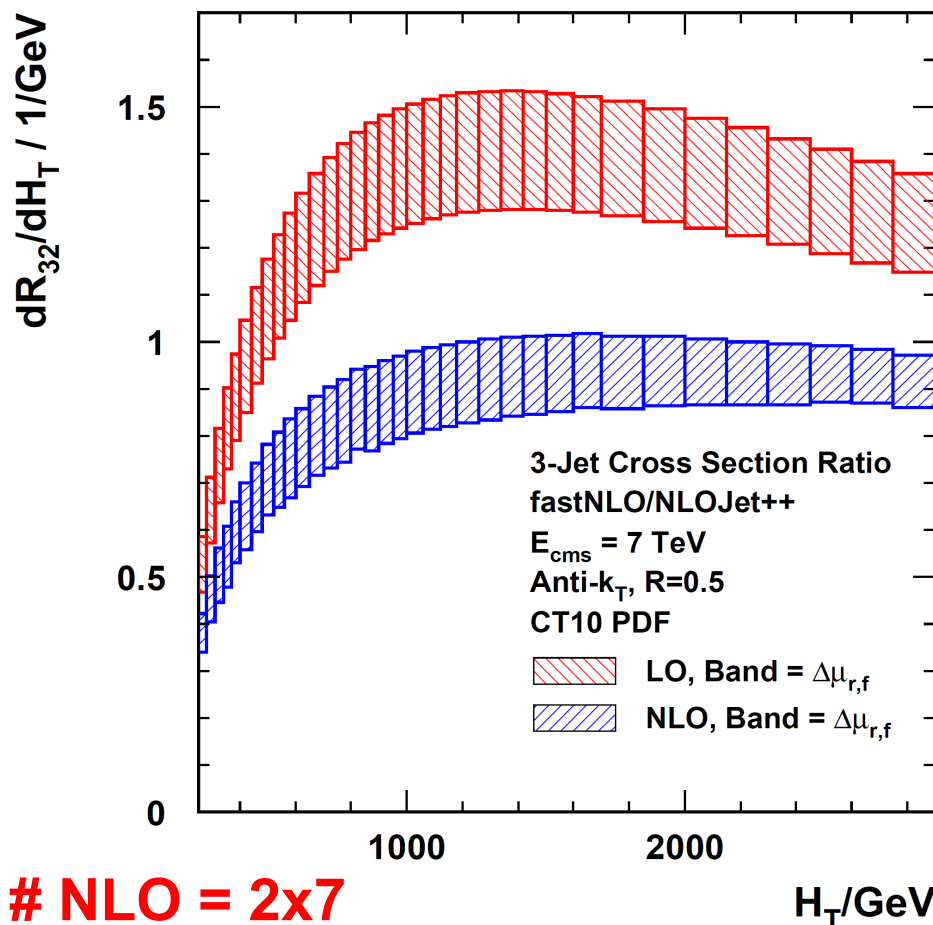


# 3+/2+: NLO Prediction & $\Delta$ PDF

CMS like selection  
(ATLAS not very different)

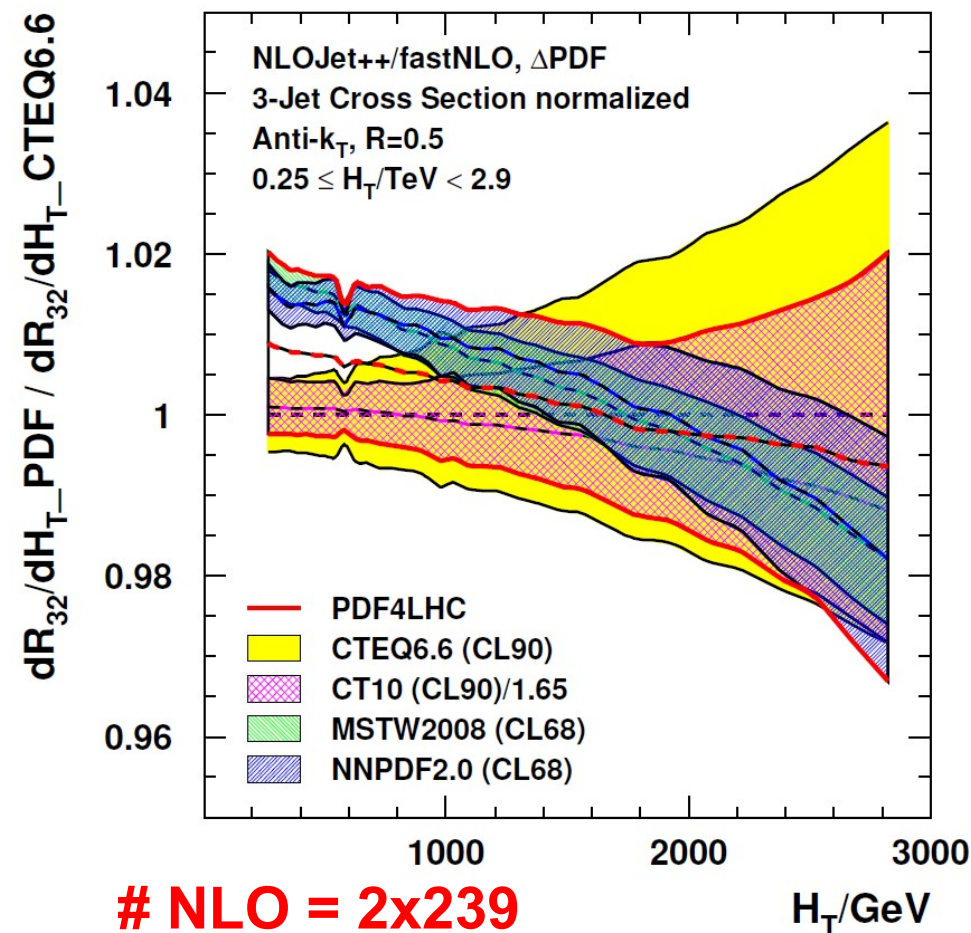
LO > 1 ?!

K factors ~ 0.67



# NLO = 2x7

PDF uncertainty reduced  
by a factor ~ 10 in ratio



# NLO = 2x239