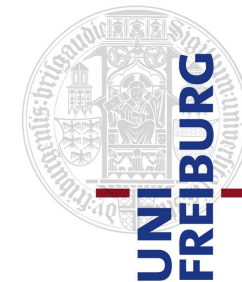


# The Quest for the Higgs Boson

## a Theory Perspective

Stefan Dittmaier

Albert-Ludwigs-Universität Freiburg

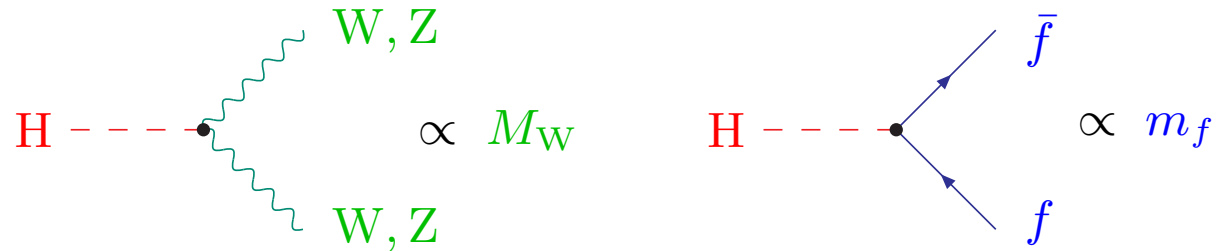


# Introduction



## Higgs search at present and future colliders

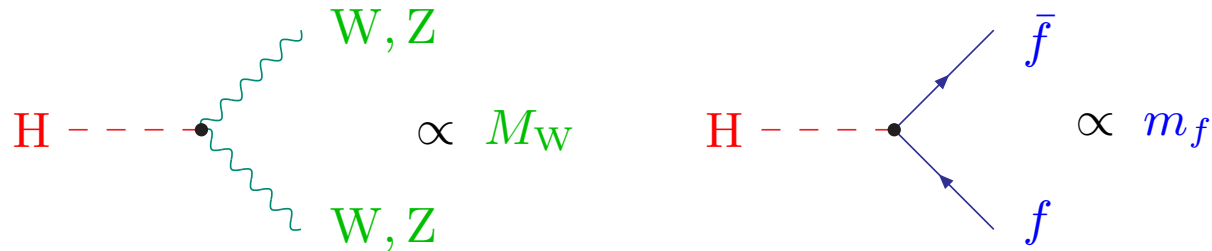
Higgs bosons couple proportional to particle masses:



⇒ Higgs production/decay mainly via coupling to W/Z bosons or top quarks

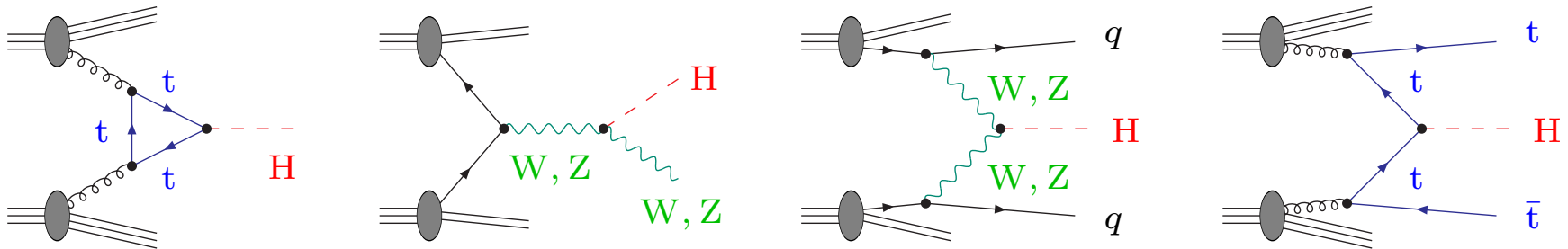
# Higgs search at present and future colliders

Higgs bosons couple proportional to particle masses:



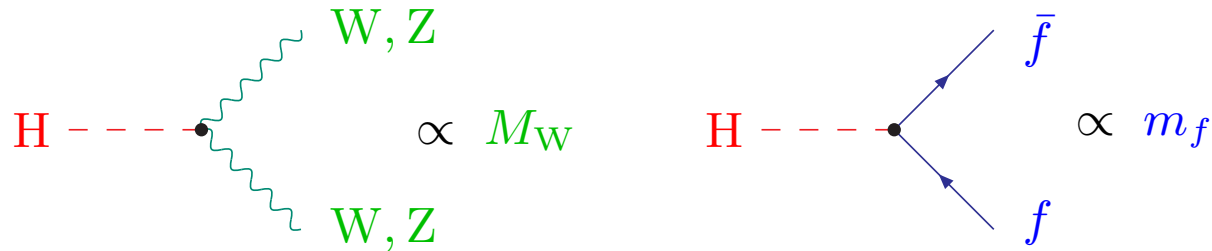
⇒ Higgs production/decay mainly via coupling to W/Z bosons or top quarks

Processes at hadron colliders ( $p\bar{p}/pp$ ):



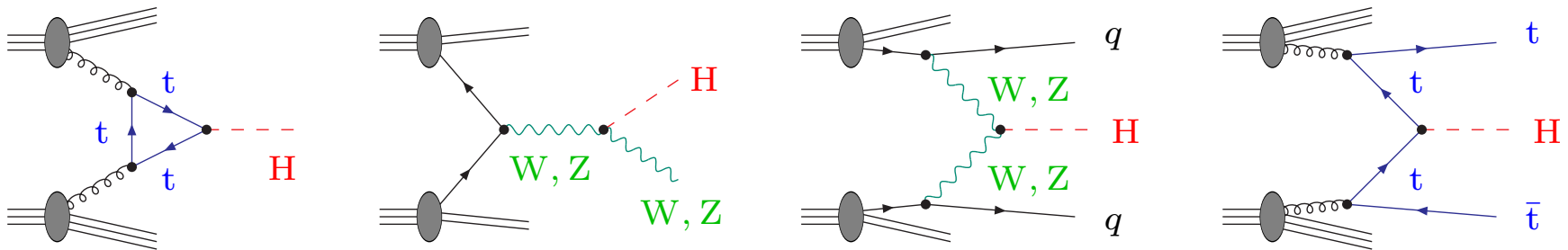
# Higgs search at present and future colliders

Higgs bosons couple proportional to particle masses:

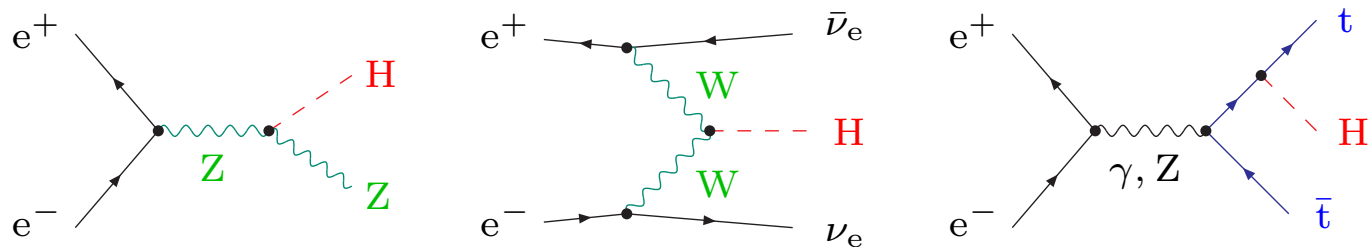


⇒ Higgs production/decay mainly via coupling to W/Z bosons or top quarks

Processes at hadron colliders ( $p\bar{p}/pp$ ):

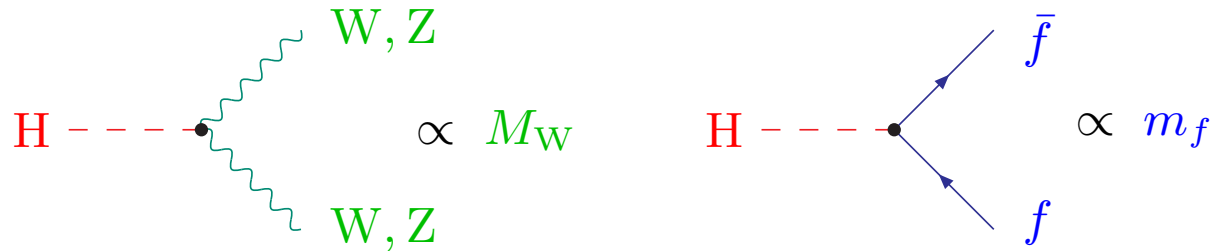


Processes at  $e^+e^-$  colliders:



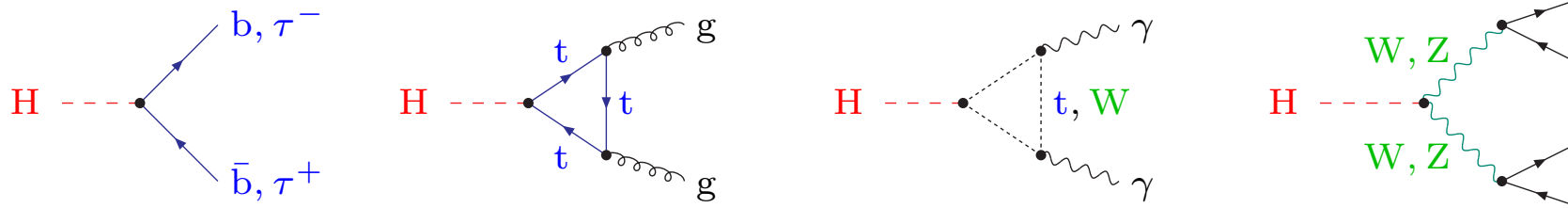
# Higgs search at present and future colliders

Higgs bosons couple proportional to particle masses:



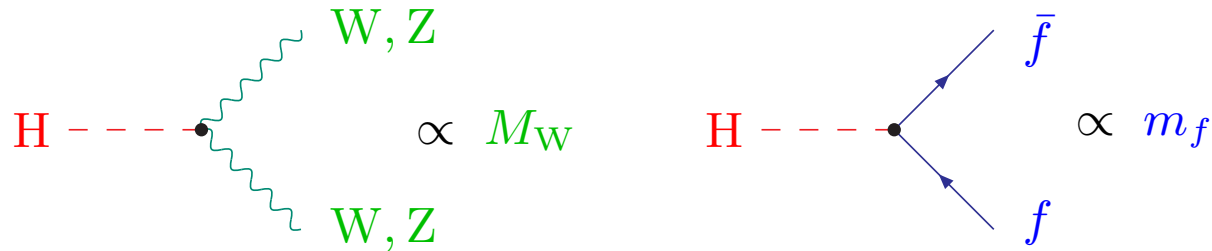
⇒ Higgs production/decay mainly via coupling to W/Z bosons or top quarks

Decay channels for Higgs bosons of moderate mass ( $M_H \lesssim 300 \text{ GeV}$ ):



## Higgs search at present and future colliders

Higgs bosons couple proportional to particle masses:



⇒ Higgs production/decay mainly via coupling to W/Z bosons or top quarks

## The role of Higgs physics in theoretical predictions

- Higgs mass enters EW precision calculations  
↪  $M_H$  sensitivity of SM fit to precision data
- Preparation for Higgs-boson searches  
↪ particularly complicated at hadron colliders

⇒ Multi-loop and multi-leg higher-order calculations at the frontier !

# Theory constraints on the Higgs-boson mass

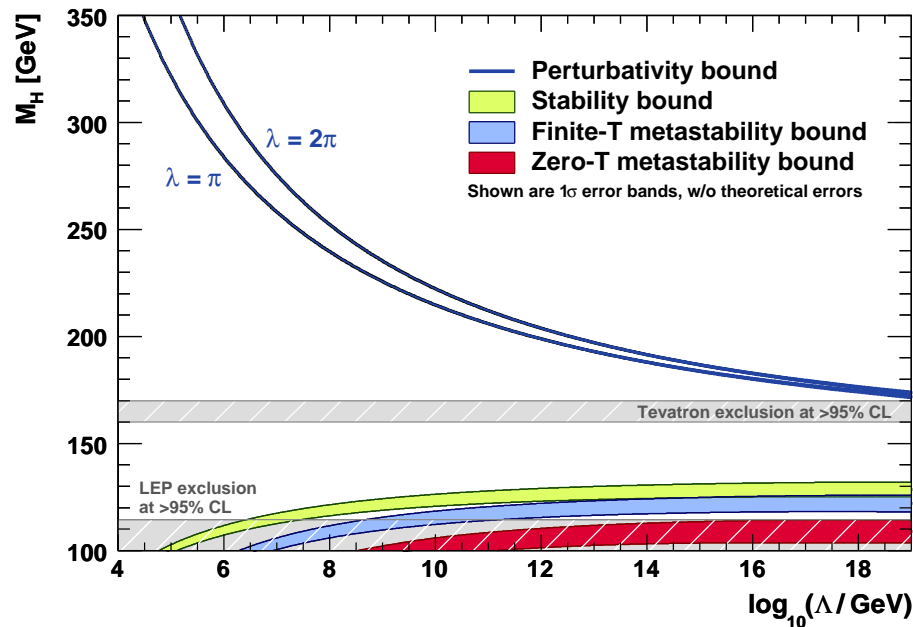
- Upper limits from
    - ◇ **unitarity** of  $W_L$  scattering amplitudes ( $W_L W_L \rightarrow W_L W_L$ , etc.) for  $s \gg M_W^2$   
Lee, Quigg, Thacker '77, ...
    - ◇ **triviality** ( $\lambda = 0$ ) of Higgs sector for too large  $M_H$   
Hambye, Riesselmann '97, ...
  - Lower limit from **vacuum stability** Coleman, Weinberg '73; Lindner, Sher, Zaglauer '89, ...
- ⇒ SM valid up to new-physics scale  $\Lambda$  requires  $M_{H,\text{vac.stab.}}(\Lambda) < M_H < M_{H,\text{triv.}}(\Lambda)$



# Theory constraints on the Higgs-boson mass

- Upper limits from
    - ◇ **unitarity** of  $W_L$  scattering amplitudes ( $W_L W_L \rightarrow W_L W_L$ , etc.) for  $s \gg M_W^2$   
Lee, Quigg, Thacker '77, ...
    - ◇ **triviality** ( $\lambda = 0$ ) of Higgs sector for too large  $M_H$   
Hambye, Riesselmann '97, ...
  - Lower limit from **vacuum stability** Coleman, Weinberg '73; Lindner, Sher, Zaglauer '89, ...
- ⇒ SM valid up to new-physics scale  $\Lambda$  requires  $M_{H,vac.stab.}(\Lambda) < M_H < M_{H,triv.}(\Lambda)$

Ellis et al. '09



SM valid up to Planck scale  
with Universe in metastable vacuum ?

←  $M_H = 126$  GeV Higgs candidate

## Intention of the talk – brief theorist's account ...

- on the history Higgs searches before LHC  
↳ EW precision physics, searches via  $e^+e^-$
- on Higgs physics at hadron colliders  
↳ Where do we stand ?
- on future challenges for theory

... being more topical than comprehensive, restricted to the SM

## Contents

- 1 Electroweak precision observables**
- 2 Higgs-boson decays**
- 3 Higgs production at hadron colliders**
- 4 Outlook – next steps**
- 5 Conclusions**



# Electroweak precision observables

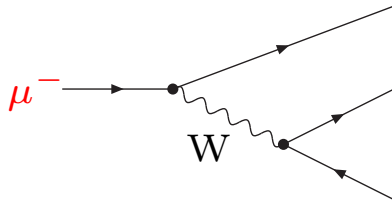
—

## window to the Higgs sector



## Important electroweak experiments

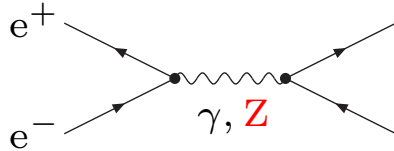
- **Muon decay:** Fermi constant  $G_\mu$  delivers constraint on  $\alpha, M_W, M_Z$



$$G_\mu = \frac{\pi\alpha M_Z^2}{\sqrt{2}M_W^2(M_Z^2 - M_W^2)} + \dots$$

## Important electroweak experiments

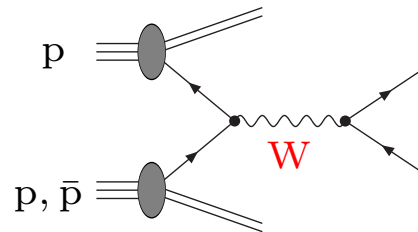
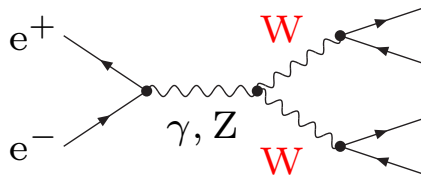
- **Muon decay:** Fermi constant  $G_\mu$  delivers constraint on  $\alpha, M_W, M_Z$
- **Z production (LEP1/SLC):**  $M_Z$  and precision observables at the Z pole



$\Gamma_Z, \sigma_{\text{had}}, A_{\text{FB}}, A_{\text{LR}}, \text{etc.}$

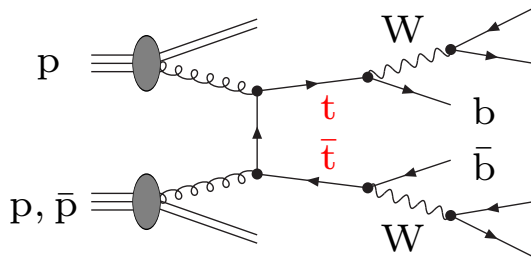
## Important electroweak experiments

- **Muon decay:** Fermi constant  $G_\mu$  delivers constraint on  $\alpha, M_W, M_Z$
- **Z production** (LEP1/SLC):  $M_Z$  and precision observables at the Z pole
- **W production** (LEP2/Tevatron/LHC): W-boson mass  $M_W$



## Important electroweak experiments

- **Muon decay:** Fermi constant  $G_\mu$  delivers constraint on  $\alpha, M_W, M_Z$
- **Z production** (LEP1/SLC):  $M_Z$  and precision observables at the Z pole
- **W production** (LEP2/Tevatron/LHC): W-boson mass  $M_W$
- **top-quark production** (Tevatron/LHC): top-quark mass  $m_t$



## Important electroweak experiments

- **Muon decay:** Fermi constant  $G_\mu$  delivers constraint on  $\alpha, M_W, M_Z$
- **Z production** (LEP1/SLC):  $M_Z$  and precision observables at the Z pole
- **W production** (LEP2/Tevatron/LHC): W-boson mass  $M_W$
- **top-quark production** (Tevatron/LHC): top-quark mass  $m_t$

## Theoretical predictions

parametrized by  $\alpha(M_Z), M_W, M_Z, m_t, m_f, \alpha_s(M_Z)$  and  $M_H$

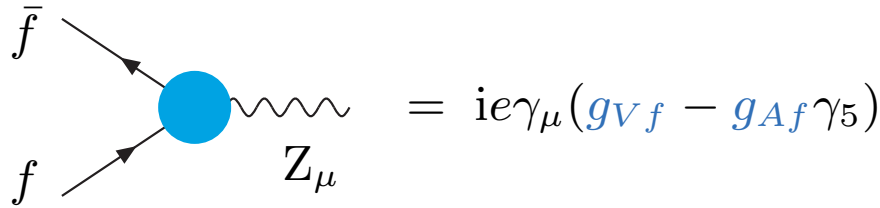
↪ global fit of SM to data yields bounds on  $M_H$

**But:** high precision necessary,  
since  $M_H$  sensitivity weak  $\sim \frac{\alpha}{\pi} \log(M_H/M_W)$   
(in contrast to top-loops where sensitivity  $\sim G_\mu m_t^2$ )



An example: the leptonic effective weak mixing angle  $\sin^2 \theta_{\text{eff}}^{\text{lept}}$

Effective Z-boson couplings measured from various asymmetries at LEP1/SLC

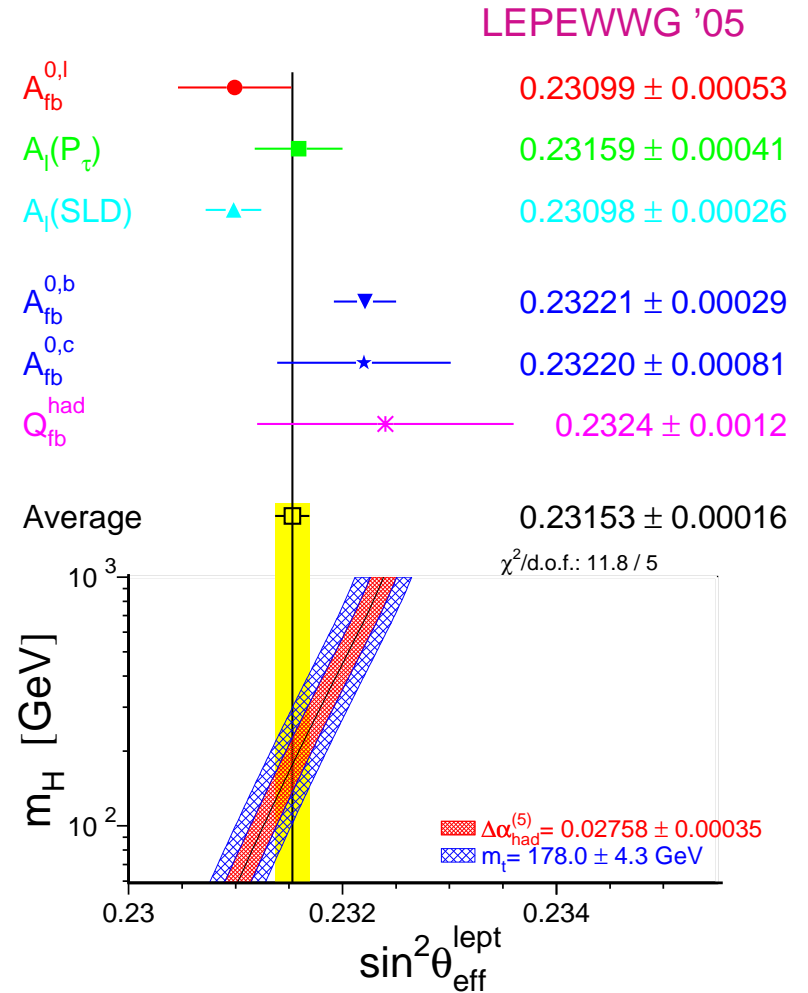
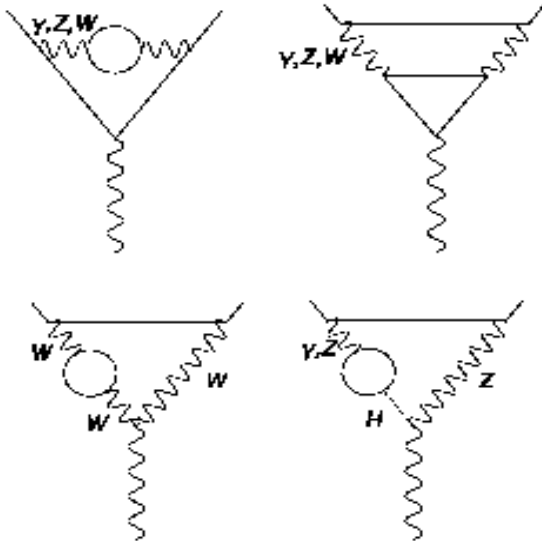


“Effective weak mixing angle”:

$$\sin^2 \theta_{\text{eff}}^{\text{lept}} = \frac{1}{4} \left( 1 - \text{Re} \left\{ \frac{g_V^{\text{lept}}}{g_A^{\text{lept}}} \right\} \right)$$

SM prediction known to two loops

Awramik, Czakon, Freitas '06; Hollik, Meier, Uccirati '06



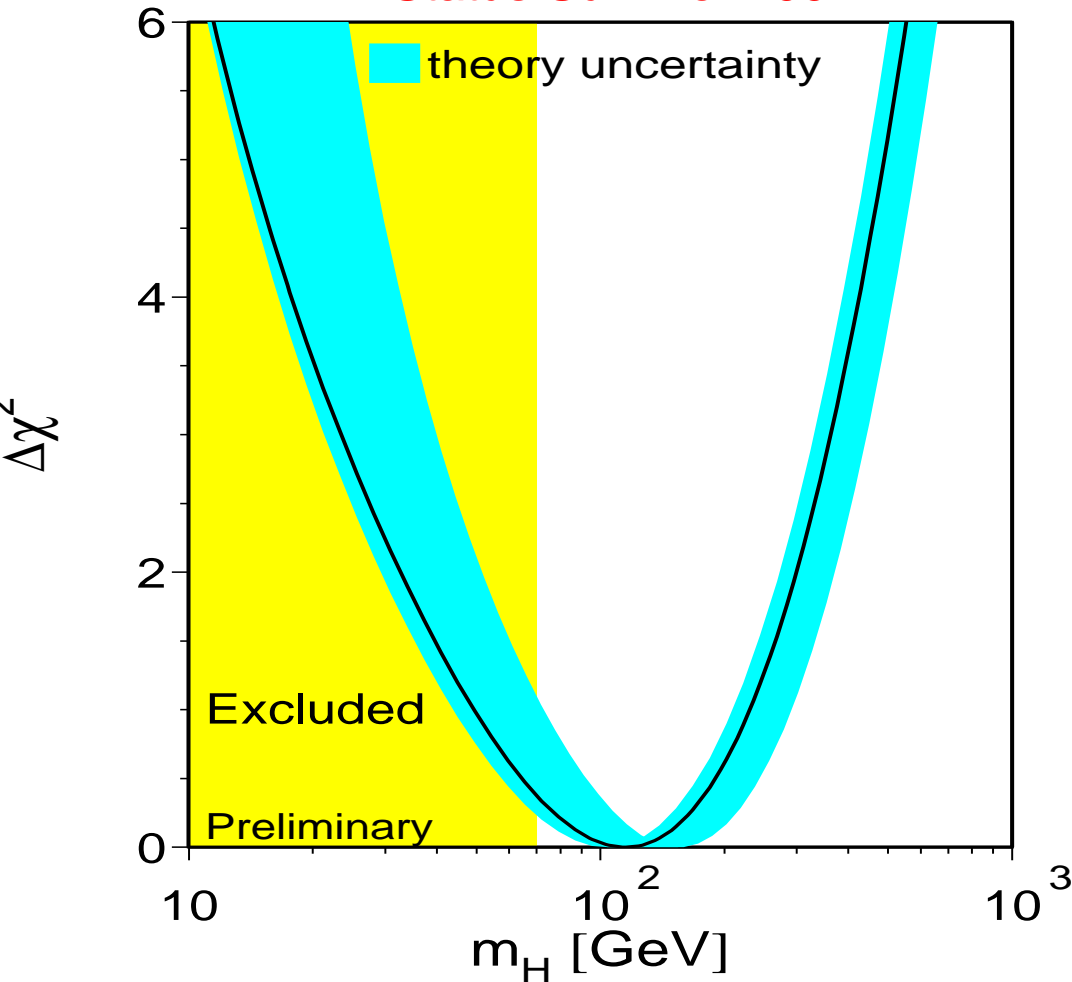
Expected ILC precision:

$$\Delta \sin^2 \theta_{\text{eff}}^{\text{lept}} \sim 1.3 \times 10^{-5}$$

# Bounds on $M_H$ (95% C.L.) – a brief history

LEPEWWG '97-'12

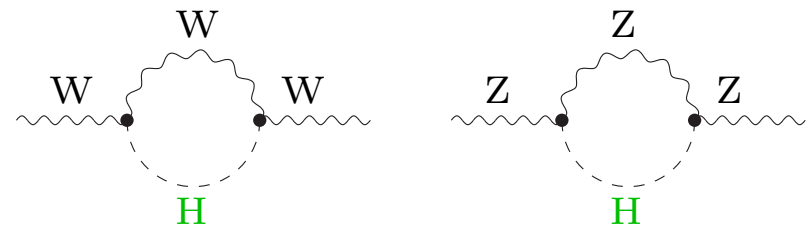
Status Summer 1997



$M_H > 114.4 \text{ GeV}$  (LEPHIGGS '02)

$e^+e^- \not\rightarrow ZH$  at LEP2

SM fit favours  
perturbative regime for  $M_H$



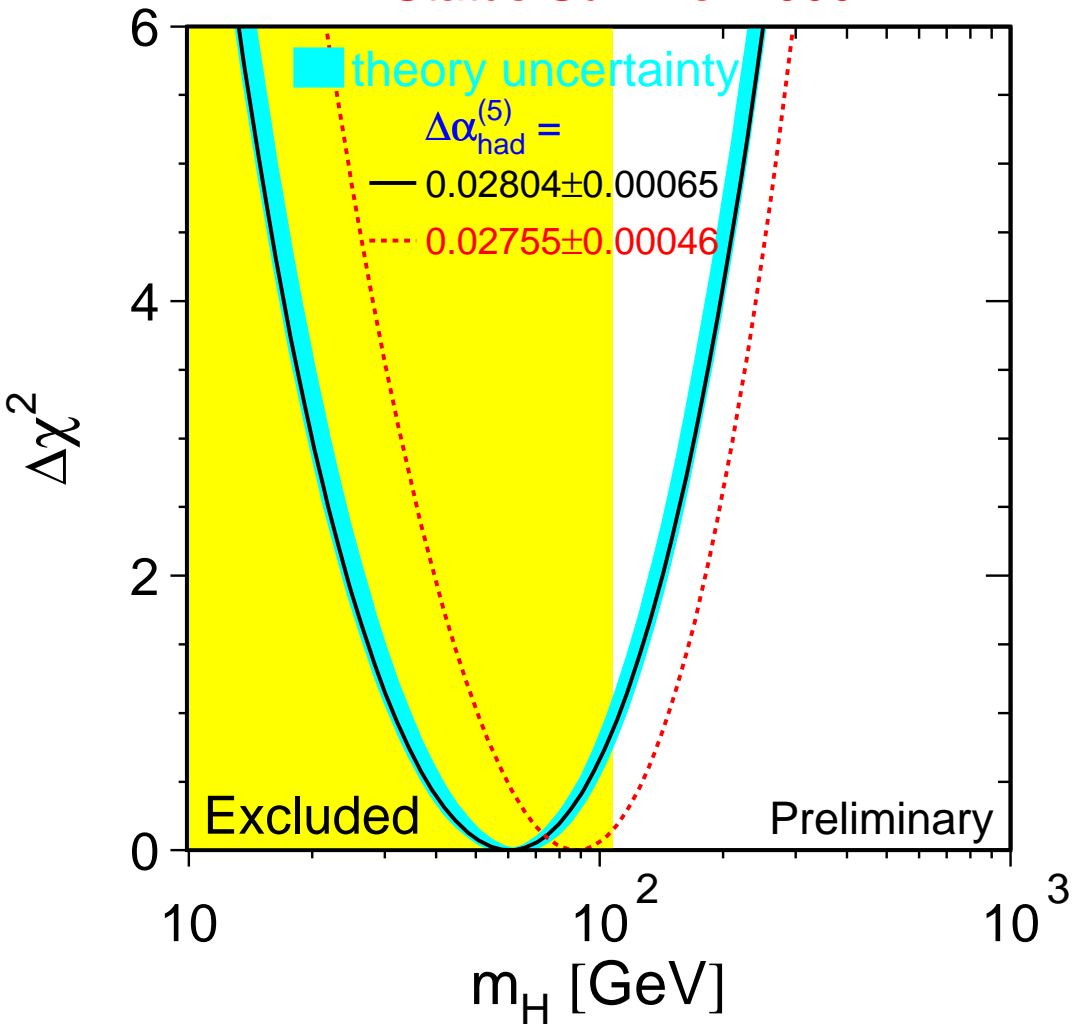
Highest sensitivity via  
“high-precision observables”:

$m_t, M_W, \sin^2 \theta_{\text{eff}}^{\text{lept}}$ , etc.

# Bounds on $M_H$ (95% C.L.) – a brief history

LEPEWWG '97-'12

Status Summer 2000

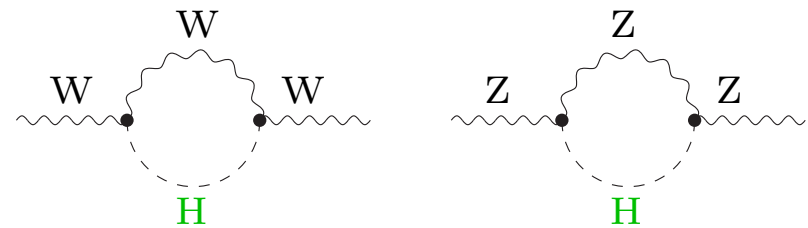


$M_H > 114.4 \text{ GeV}$  (LEPHIGGS '02)

$e^+e^- \not\rightarrow ZH$  at LEP2

SM fit favours

$M_H \lesssim 200 \text{ GeV}$



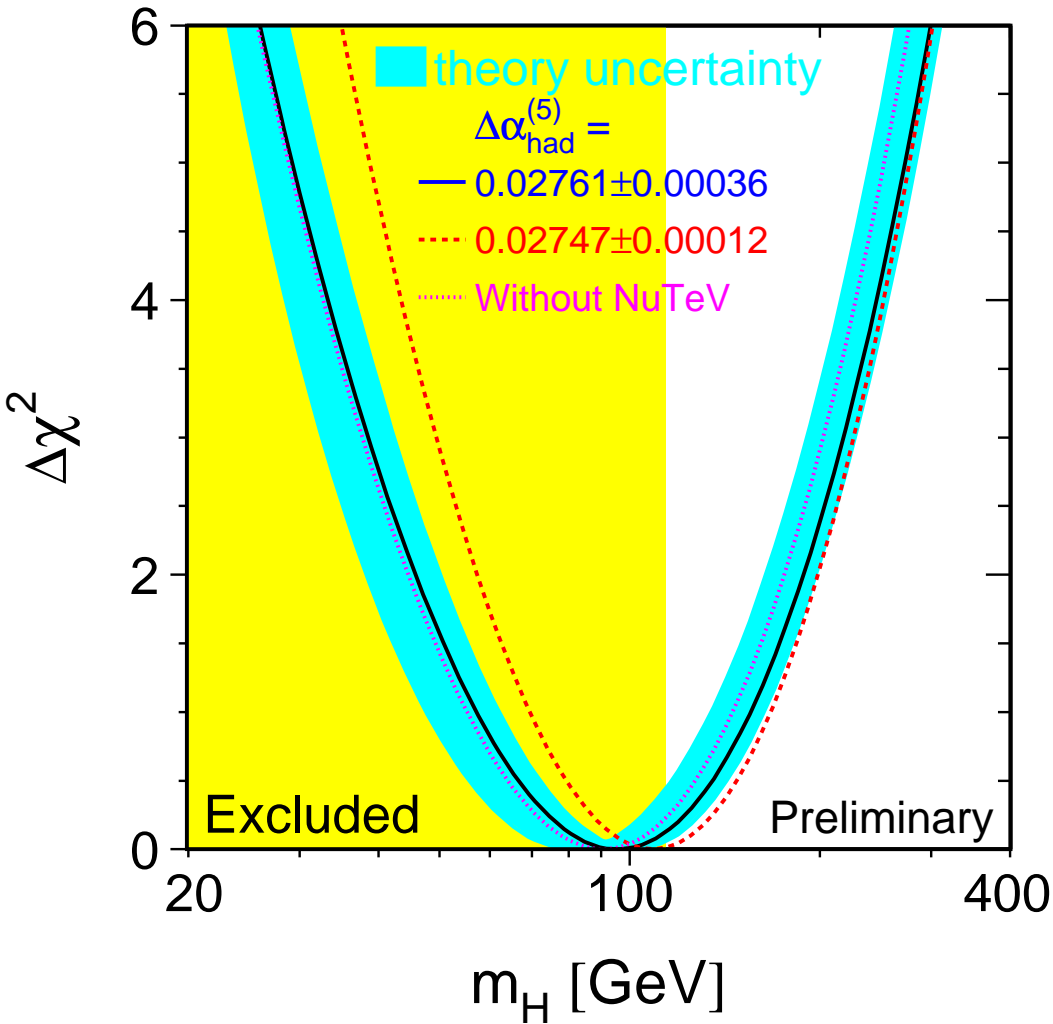
Highest sensitivity via  
"high-precision observables":

$m_t, M_W, \sin^2 \theta_{\text{eff}}^{\text{lept}}$ , etc.

# Bounds on $M_H$ (95% C.L.) – a brief history

LEPEWWG '97-'12

Status Summer 2003

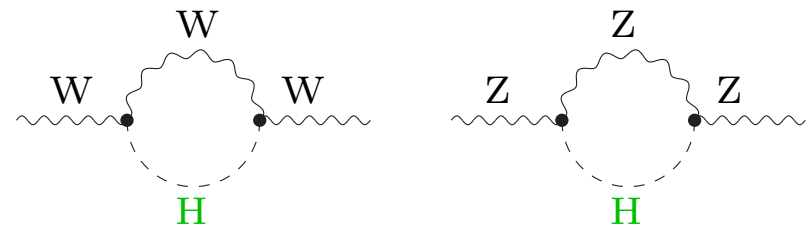


$M_H > 114.4 \text{ GeV}$  (LEPHIGGS '02)

$e^+e^- \not\rightarrow ZH$  at LEP2

SM fit favours

$M_H \lesssim 200 \text{ GeV}$

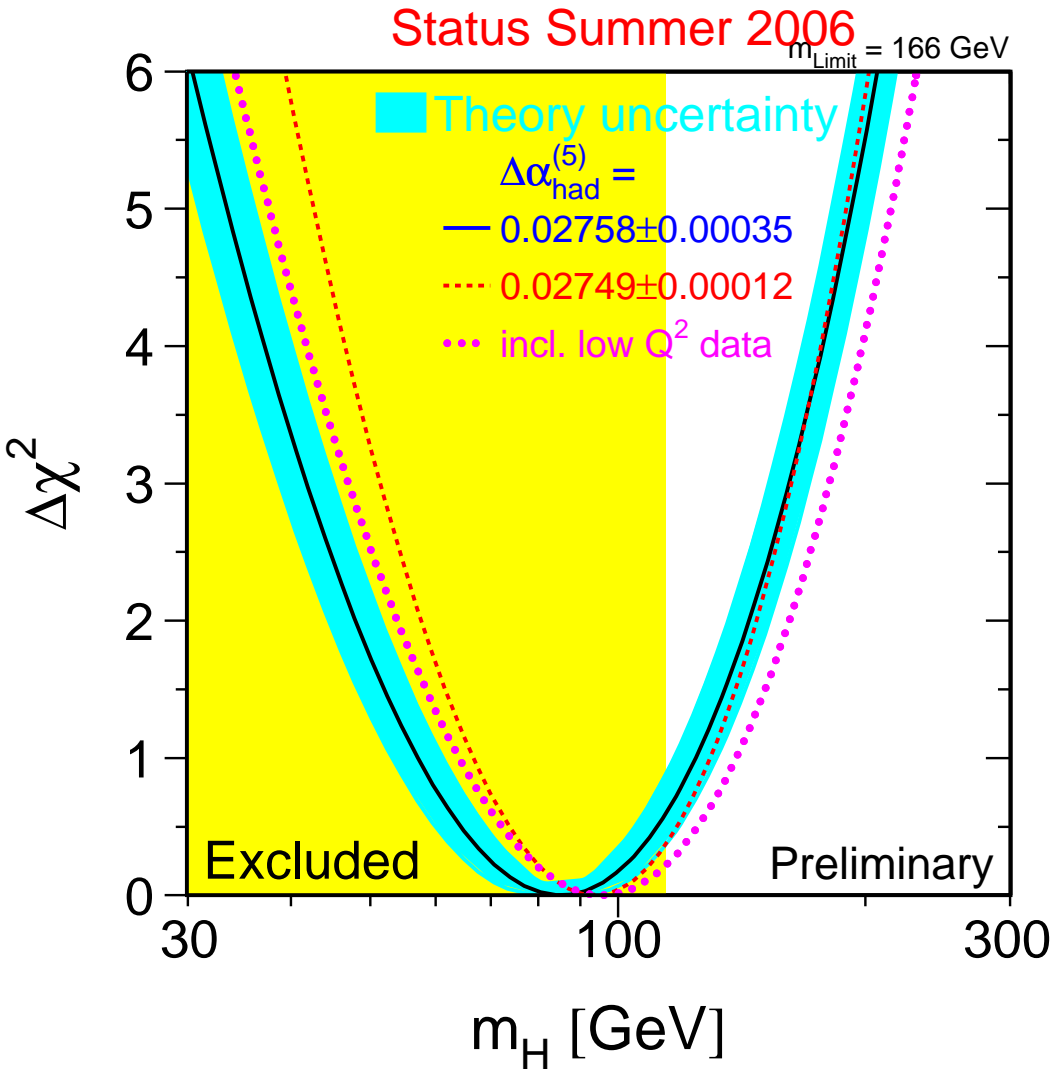


Highest sensitivity via  
“high-precision observables”:

$m_t, M_W, \sin^2 \theta_{\text{eff}}^{\text{lept}}$ , etc.

# Bounds on $M_H$ (95% C.L.) – a brief history

LEPEWWG '97-'12

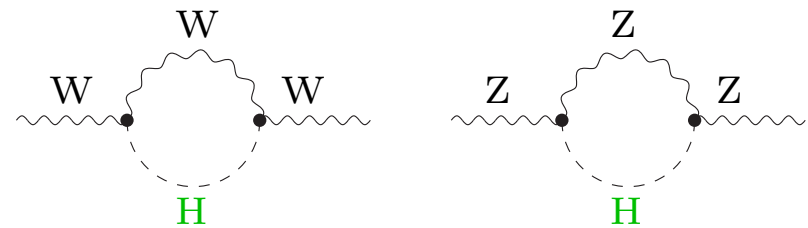


$M_H > 114.4 \text{ GeV}$  (LEPHIGGS '02)

$e^+e^- \not\rightarrow ZH$  at LEP2

SM fit favours

$M_H < 166 \text{ GeV}$

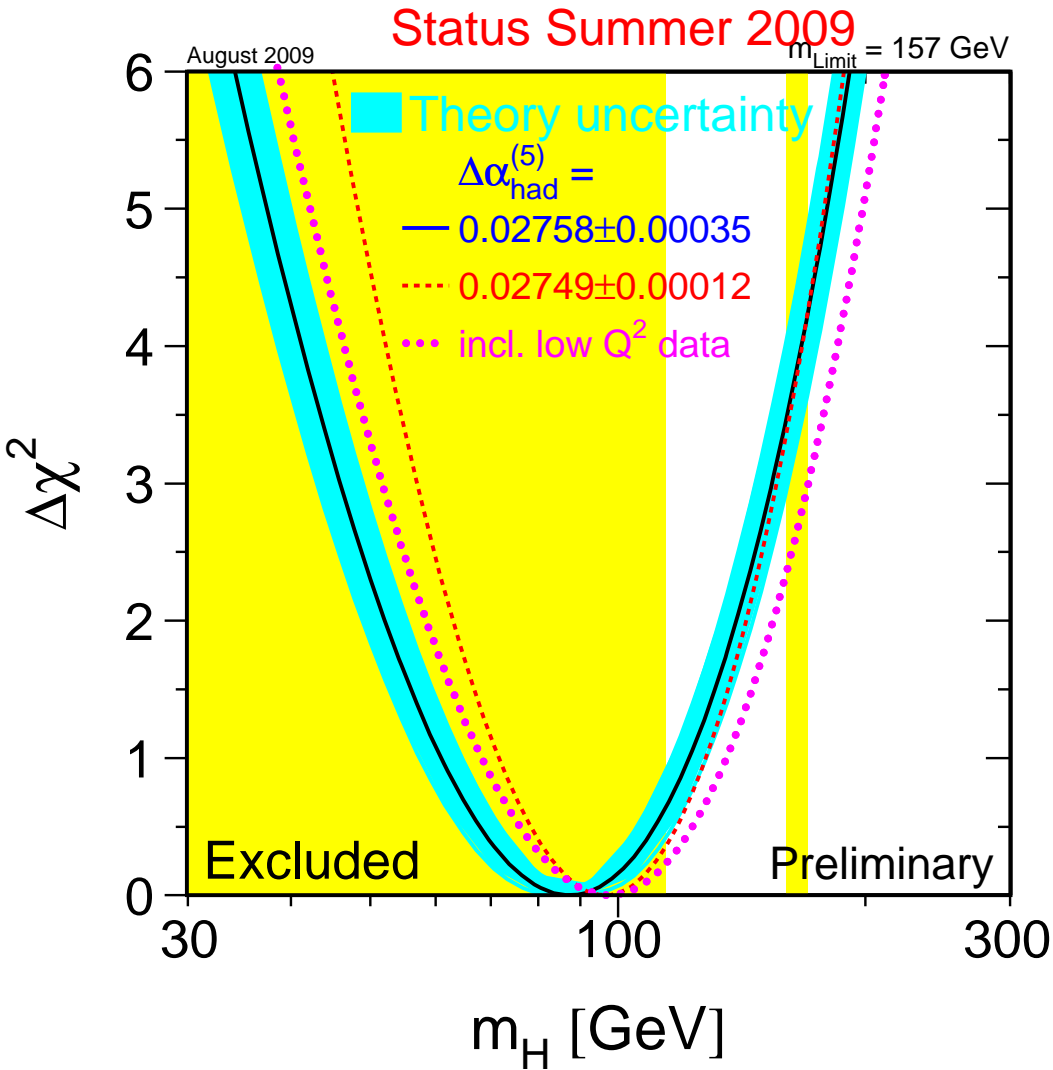


Highest sensitivity via  
“high-precision observables”:

$m_t, M_W, \sin^2 \theta_{\text{eff}}^{\text{lept}}$ , etc.

# Bounds on $M_H$ (95% C.L.) – a brief history

LEPEWWG '97-'12

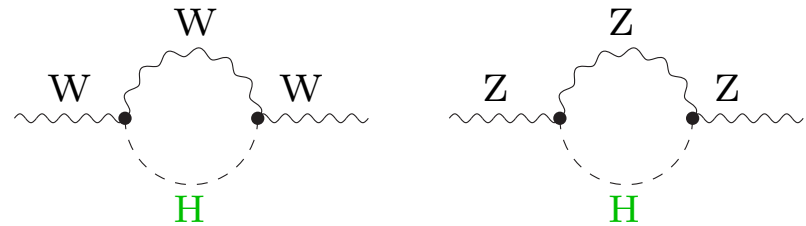


$M_H > 114.4 \text{ GeV}$  (LEPHIGGS '02)

$e^+e^- \not\rightarrow ZH$  at LEP2

SM fit favours

$M_H < 157 \text{ GeV}$

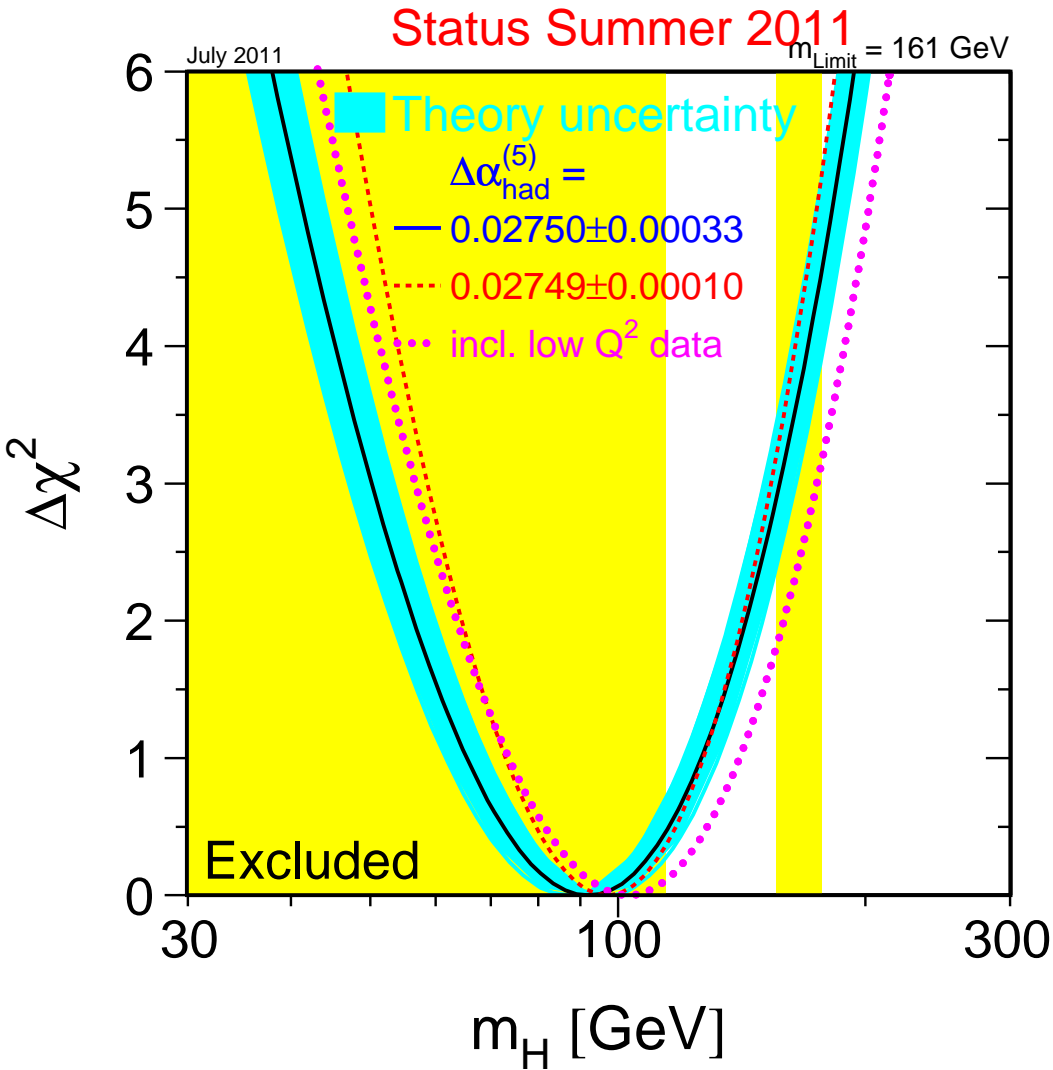


Highest sensitivity via  
“high-precision observables”:

$m_t, M_W, \sin^2 \theta_{\text{eff}}^{\text{lept}}$ , etc.

# Bounds on $M_H$ (95% C.L.) – a brief history

LEPEWWG '97-'12

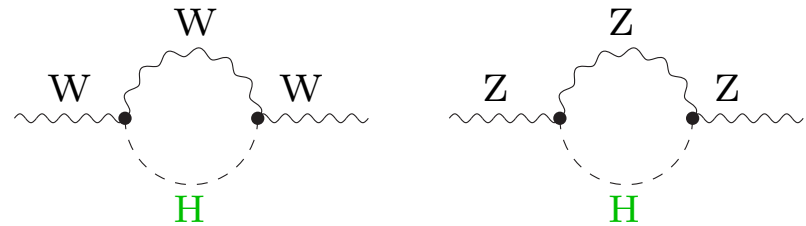


$M_H > 114.4 \text{ GeV}$  (LEPHIGGS '02)

$e^+e^- \not\rightarrow ZH$  at LEP2

SM fit favours

$M_H < 161 \text{ GeV}$

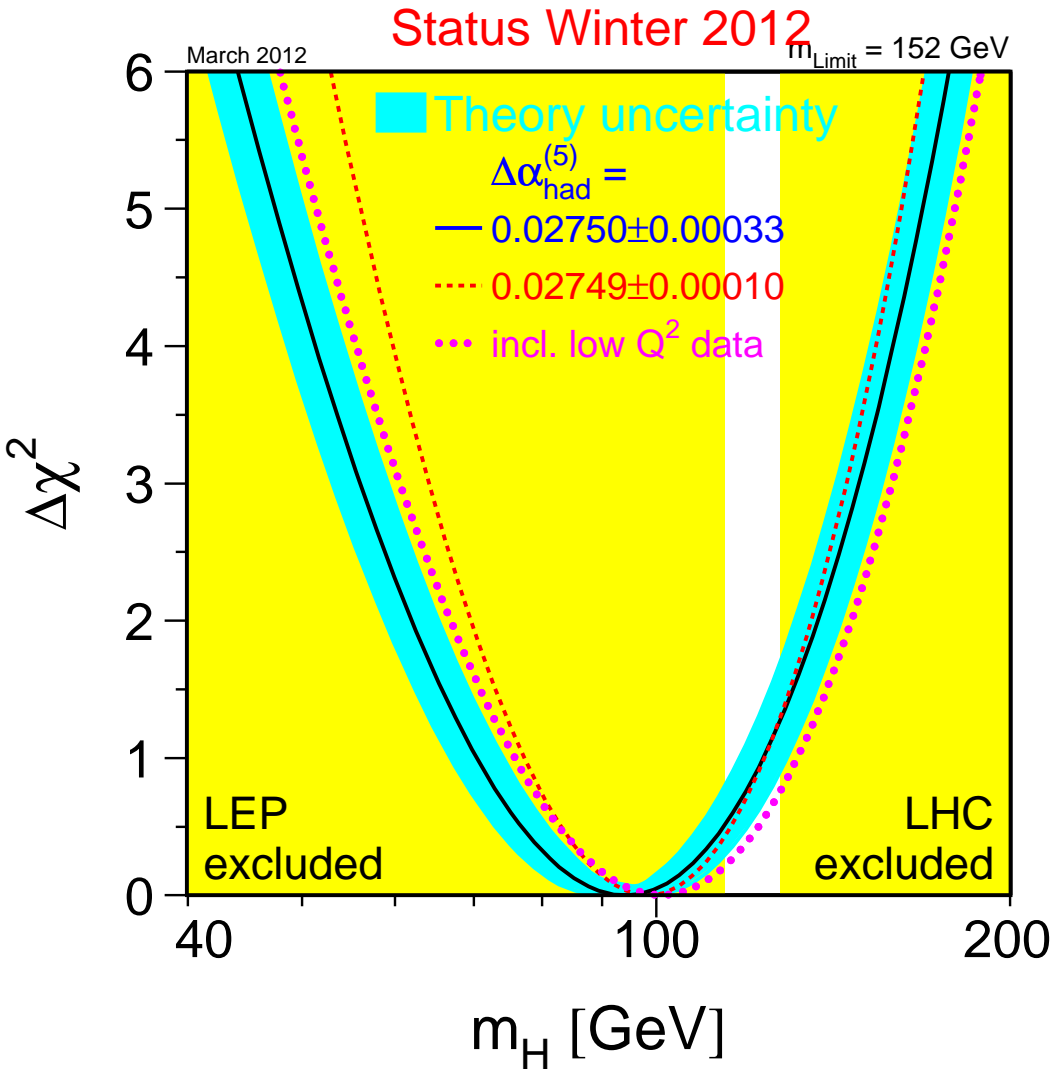


Highest sensitivity via  
“high-precision observables”:

$m_t, M_W, \sin^2 \theta_{\text{eff}}^{\text{lept}}$ , etc.

# Bounds on $M_H$ (95% C.L.) – a brief history

LEPEWWG '97-'12

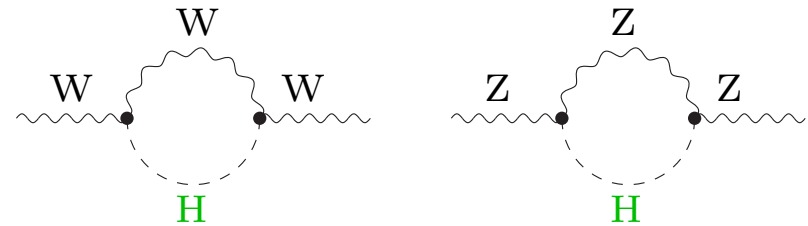


$M_H > 114.4 \text{ GeV}$  (LEPHIGGS '02)

$e^+e^- \not\rightarrow ZH$  at LEP2

SM fit favours

$M_H < 152 \text{ GeV}$



Highest sensitivity via  
“high-precision observables”:

$m_t, M_W, \sin^2 \theta_{\text{eff}}^{\text{lept}}$ , etc.

Open window not excluded by the LHC:

$122 \text{ GeV} < M_H < 127 \text{ GeV}$

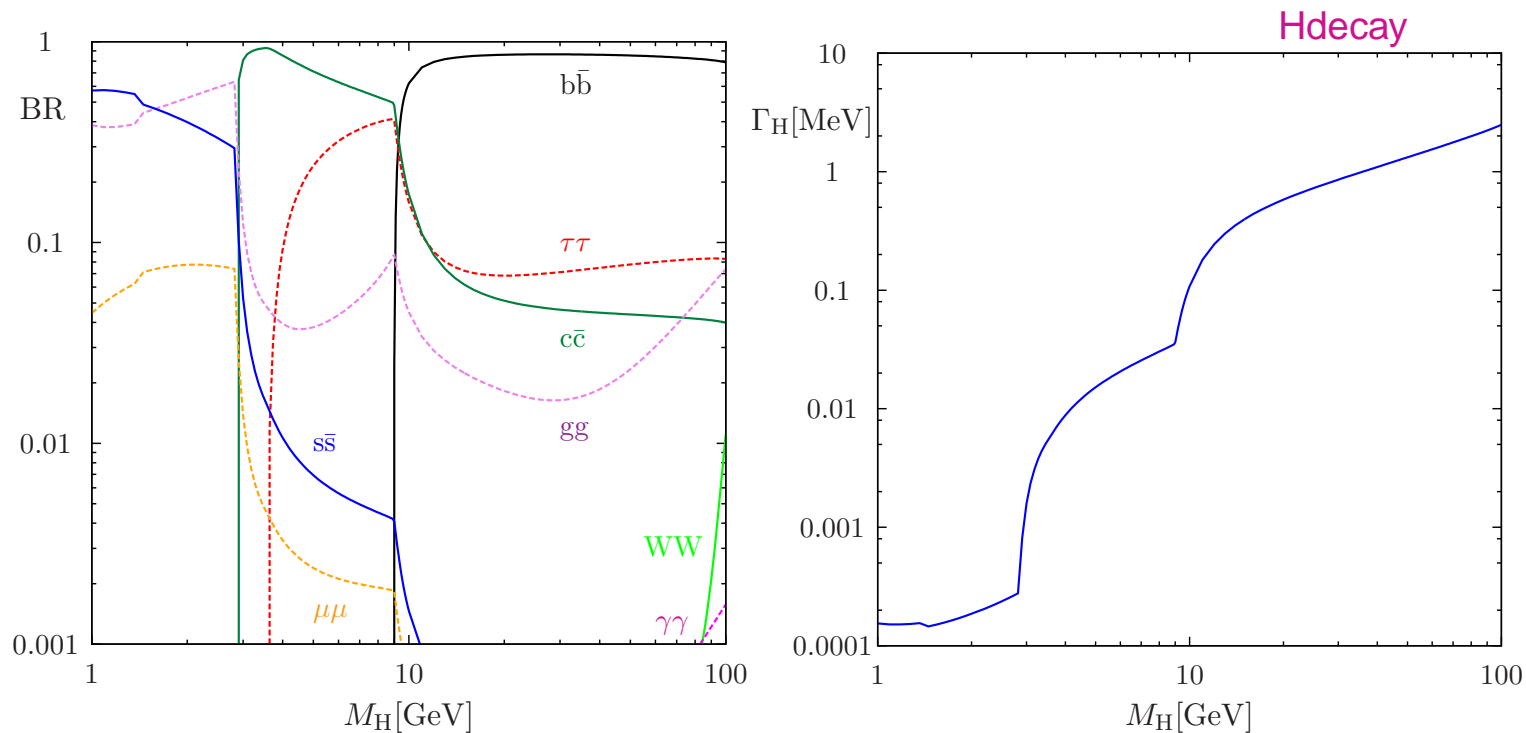


# Higgs-boson decays



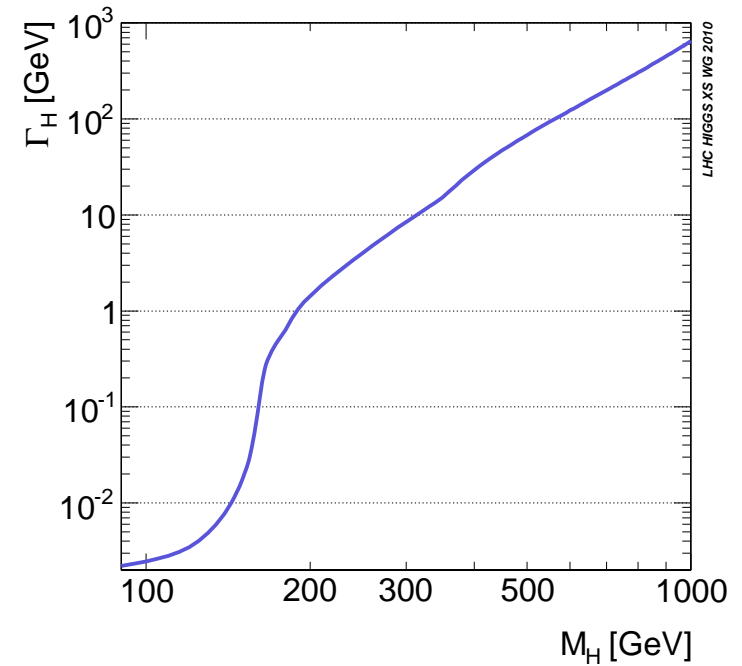
## General considerations

- very light Higgs boson:  $M_H \lesssim 100 \text{ GeV}$ 
  - ◇ large theoretical uncertainties for  $M_H \lesssim 20 \text{ GeV}$   
(threshold effects, large  $\alpha_s$ , hadronic effects)  
↪ LEP1 searches via  $Z \rightarrow Z^* H$  w/o assumptions on or modeled H decays
  - ◇  $\Gamma_H \lesssim \text{few MeV} \ll \text{detector resolutions}$



## General considerations

- very light Higgs boson:  $M_H \lesssim 100 \text{ GeV}$
  - heavy Higgs boson:  $M_H \gtrsim 600 \text{ GeV}$ 
    - ◇  $\Gamma_H \gtrsim 100 \text{ GeV}$ 
      - ↪ broad resonance,  
large interference signal–background interference
      - ↪ **Simultaneous treatment of signal + background required**
    - ◇ perturbation theory runs out of control  
(often two-loop  $\sim$  one-loop for  $M_H \sim 700 \text{ GeV}$ )
- ⇒ **Precision of calculations seriously degrades,**  
**but high-mass SM Higgs excluded**  
**by candidate with  $M_H = 126 \text{ GeV}$  and SM fit**

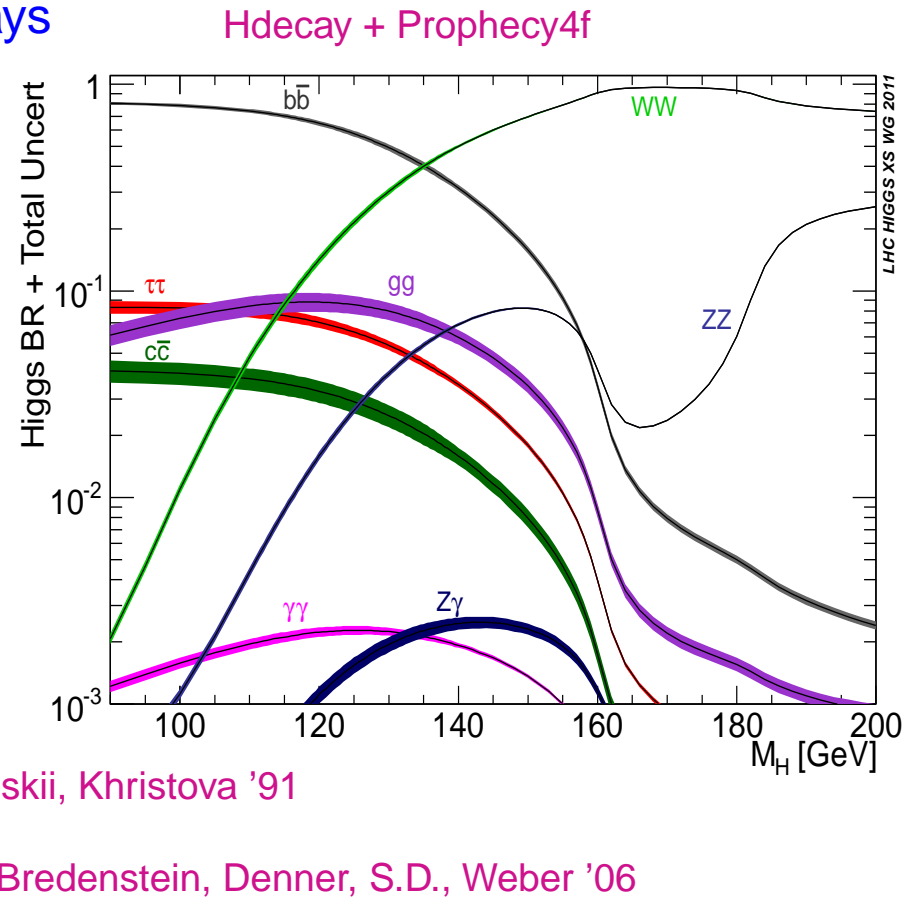


## General considerations

- very light Higgs boson:  $M_H \lesssim 100 \text{ GeV}$
  
  - heavy Higgs boson:  $M_H \gtrsim 600 \text{ GeV}$
  
  - $100 \text{ GeV} \lesssim M_H \lesssim 600 \text{ GeV}$ 
    - ◇  $114 \text{ GeV} < M_H \lesssim 200 \text{ GeV}$ : favoured mass range after LEP
    - ◇  $M_H \lesssim 135 \text{ GeV}$ :  $H \rightarrow b\bar{b}$  dominant,  $H \rightarrow \gamma\gamma$  well accessible
    - ◇  $M_H \gtrsim 135 \text{ GeV}$ :  $H \rightarrow WW/ZZ \rightarrow 4f$  dominant and very well exp. accessible
- Note:**  $H \rightarrow VV \rightarrow 4f$  for  $M_H < 2M_V$  to be treated as four-body decays

## Precision calculations for SM Higgs-boson decays

- $H \rightarrow f\bar{f}$  Bardin, Vilenskii, Khristova '91  
Dabelstein, Hollik '92; Kniehl '92; ...  
QCD up to NNNLO QCD for  $b\bar{b}$   
... Baikov, Chetyrkin, Kühn, Steinhauser ('97-'05)
- $H \rightarrow \gamma\gamma/gg$   
full 2-loop result + h.o. improvements  
Spira, Djouadi, Graudenz, Zerwas '95; ...  
(Actis,) Passarino, Sturm, Uccirati '07,'08
- $H \rightarrow WW/ZZ \rightarrow 4f$ 
  - ◇ NLO for stable W/Z bosons  
Fleischer, Jegerlehner '81; Kniehl '91; Bardin, Vilenskii, Khristova '91
  - ◇ NLO for off-shell/decaying W/Z bosons



## Tools

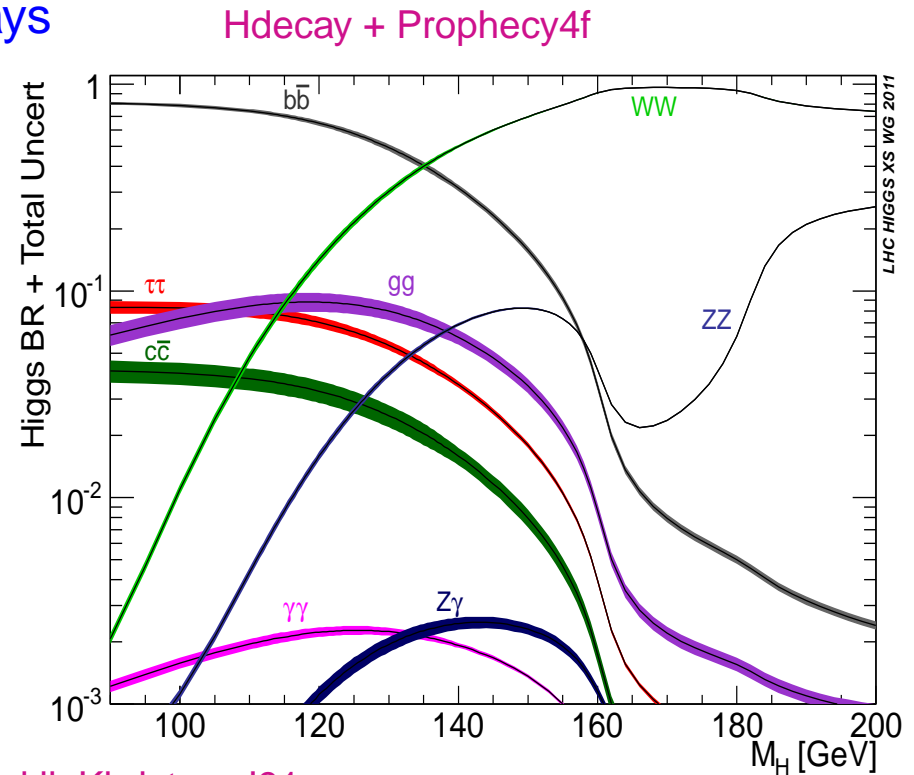
- HDECAY: all  $1 \rightarrow 2$  decays (integrated) Djouadi, Kalinowski, Mühlleitner, Spira
- PROPHECY4F:  $H \rightarrow 4f$  decays (integrated & differential) Bredenstein, Denner, S.D., Mück, Weber

# Precision calculations for SM Higgs-boson decays

- $H \rightarrow f\bar{f}$  Bardin, Vilenskii, Khristova '91  
Dabelstein, Hollik '92; Kniehl '92; ...  
QCD up to NNNLO QCD for  $b\bar{b}$   
... Baikov, Chetyrkin, Kühn, Steinhauser ('97-'05)

- $H \rightarrow \gamma\gamma/gg$   
full 2-loop result + h.o. improvements  
Spira, Djouadi, Graudenz, Zerwas '95; ...  
(Actis,) Passarino, Sturm, Uccirati '07,'08

- $H \rightarrow WW/ZZ \rightarrow 4f$ 
  - ◊ NLO for stable W/Z bosons  
Fleischer, Jegerlehner '81; Kniehl '91; Bardin, Vilenskii, Khristova '91
  - ◊ NLO for off-shell/decaying W/Z bosons  
Bredenstein, Denner, S.D., Weber '06

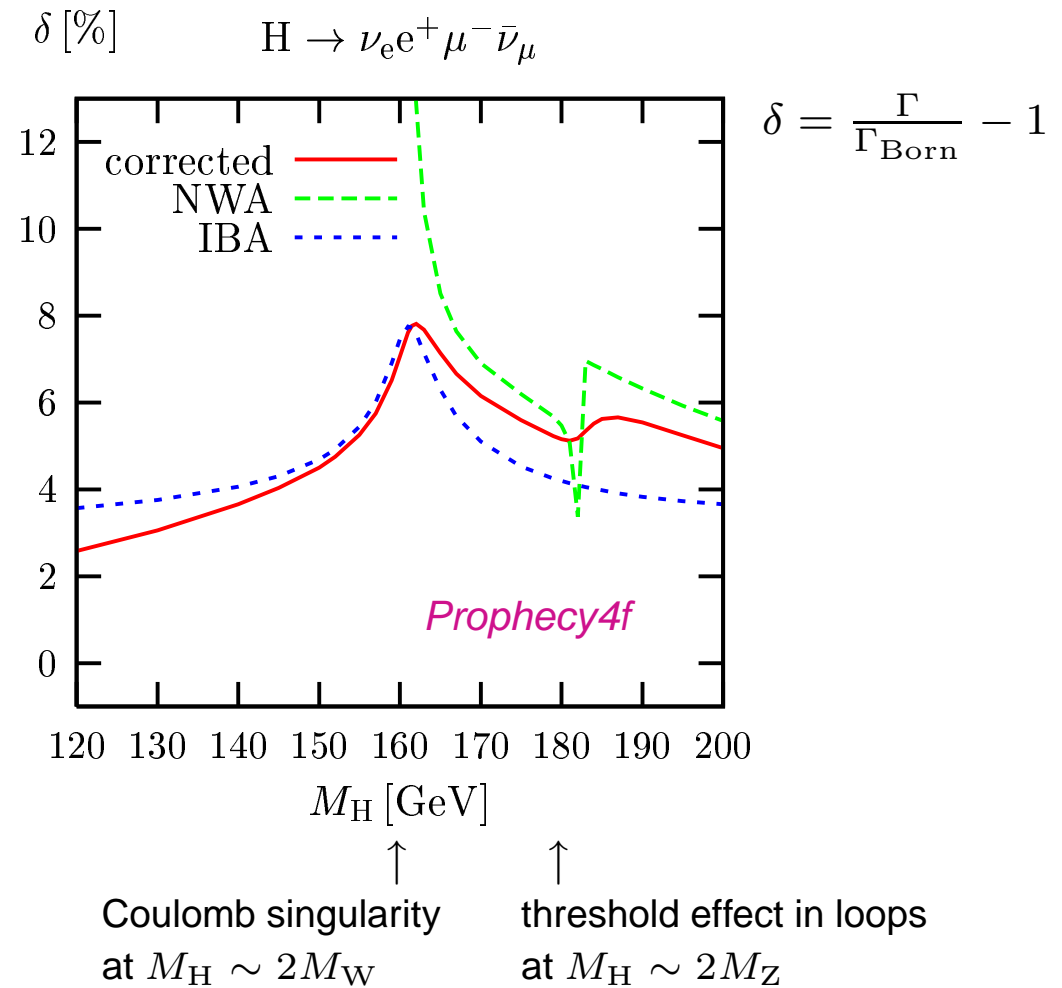
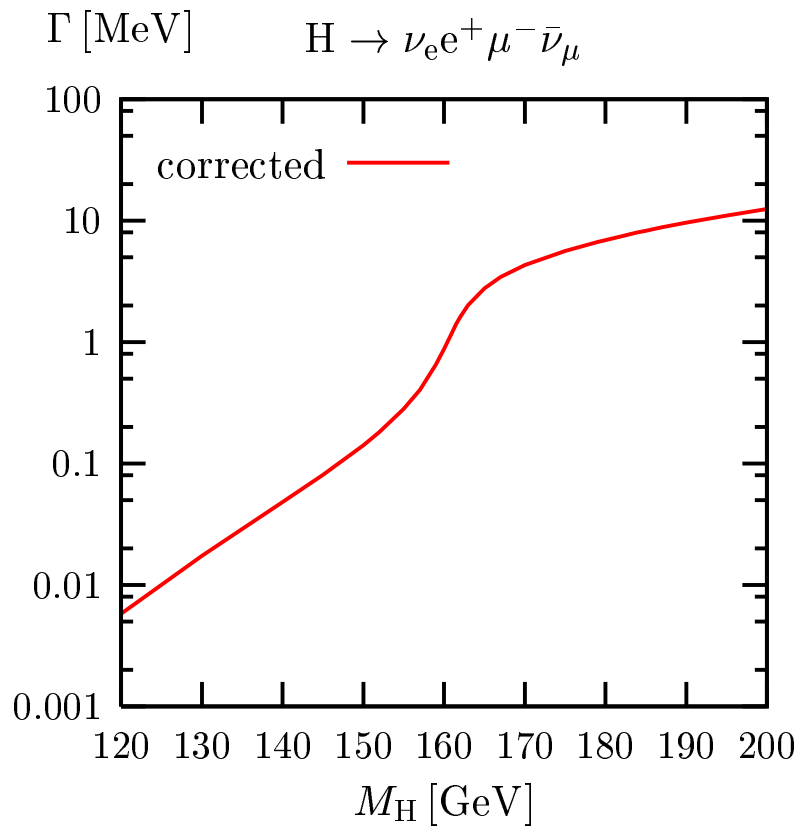


## Parametric + theoretical uncertainty of BRs: LHC Higgs XS WG 2011

| $M_H$ [GeV] | $H \rightarrow b\bar{b}$ | $\tau^+\tau^-$ | $c\bar{c}$ | $gg$ | $\gamma\gamma$ | $WW$   | $ZZ$   |   |
|-------------|--------------------------|----------------|------------|------|----------------|--------|--------|---|
| 120         | 3%                       | 6%             | 12%        | 10%  | 5%             | 5%     | 5%     | ← driven by $\delta\Gamma_{H \rightarrow b\bar{b}}$ |
| 150         | 4%                       | 3%             | 10%        | 8%   | 2%             | 1%     | 1%     |   |
| 200         | 5%                       | 3%             | 10%        | 8%   | 2%             | < 0.1% | < 0.1% |   |

# Partial H width for $H \rightarrow WW \rightarrow \nu_e e^+ \mu^- \bar{\nu}_\mu$

Bredenstein, Denner,  
S.D., Weber '06



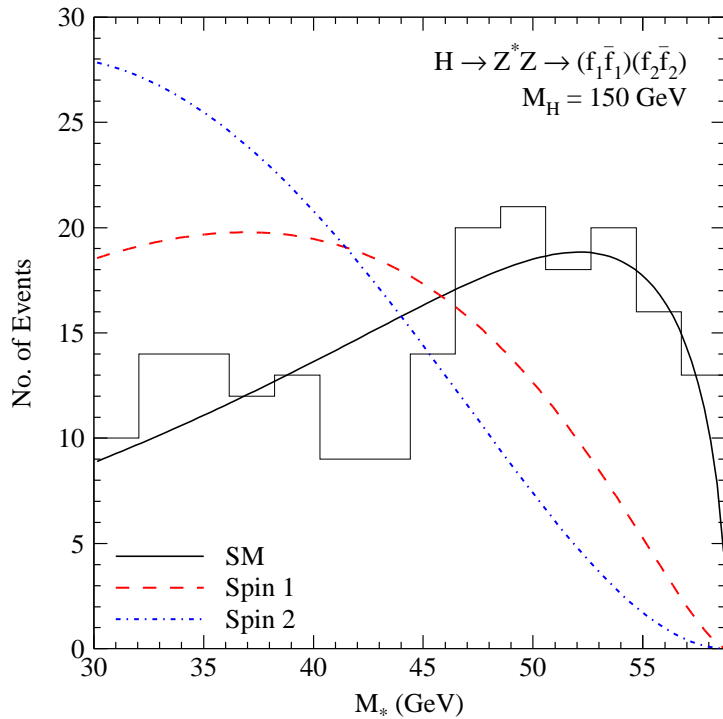
**NWA** = “narrow-width approximation” (on-shell W bosons)

**IBA** = “improved Born approximation” (universal corrections)

**Corrections  $\sim 4-8\%$ , NWA not useful for  $M_H \lesssim 165$  GeV**

# Kinematical studies of $H \rightarrow ZZ \rightarrow f_1 \bar{f}_1 f_2 \bar{f}_2$

## Invariant Z mass:



$$M_* = M_{f_1 \bar{f}_1}$$

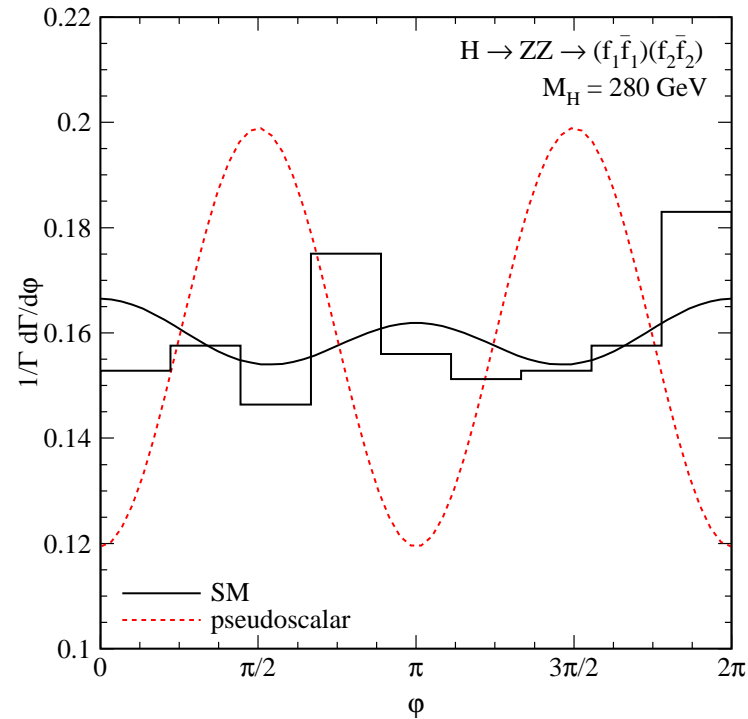
Histograms = SM simulation for  $L = 300 \text{ fb}^{-1}$

↪ **distributions sensitive to spin and parity**

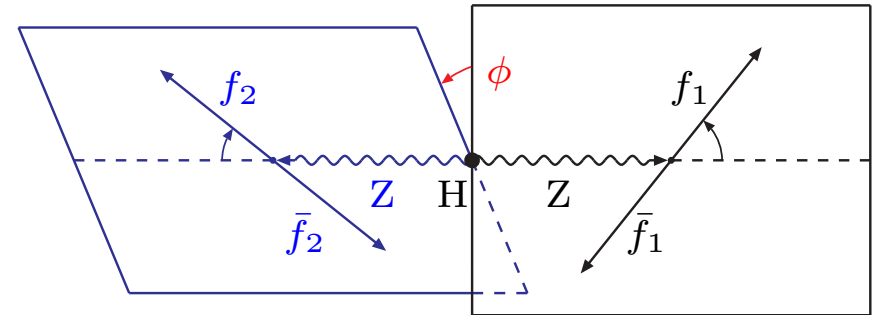
corrections available via **PROPHECY4F**

Bredenstein, Denner, S.D., Mück, Weber

## Angle between Z decay planes:



Choi, Miller,  
Mühlleitner,  
Zerwas '02



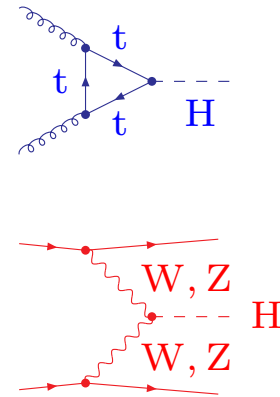
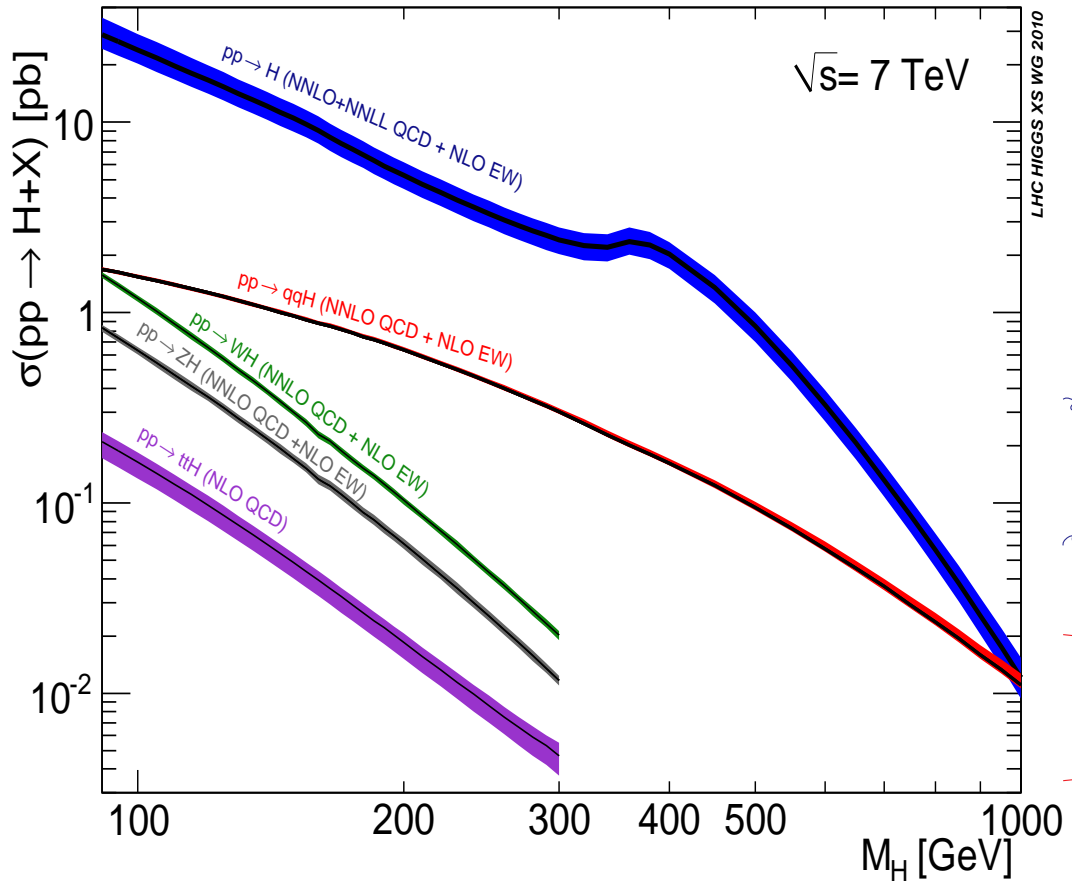
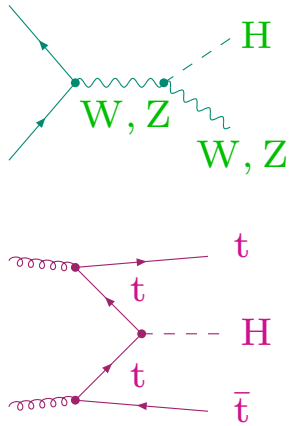


# Higgs production at hadron colliders



# SM Higgs XS predictions for the LHC at $\sqrt{s} = 7\text{ TeV}$

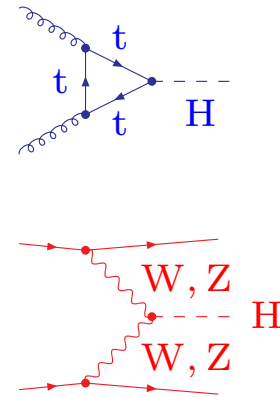
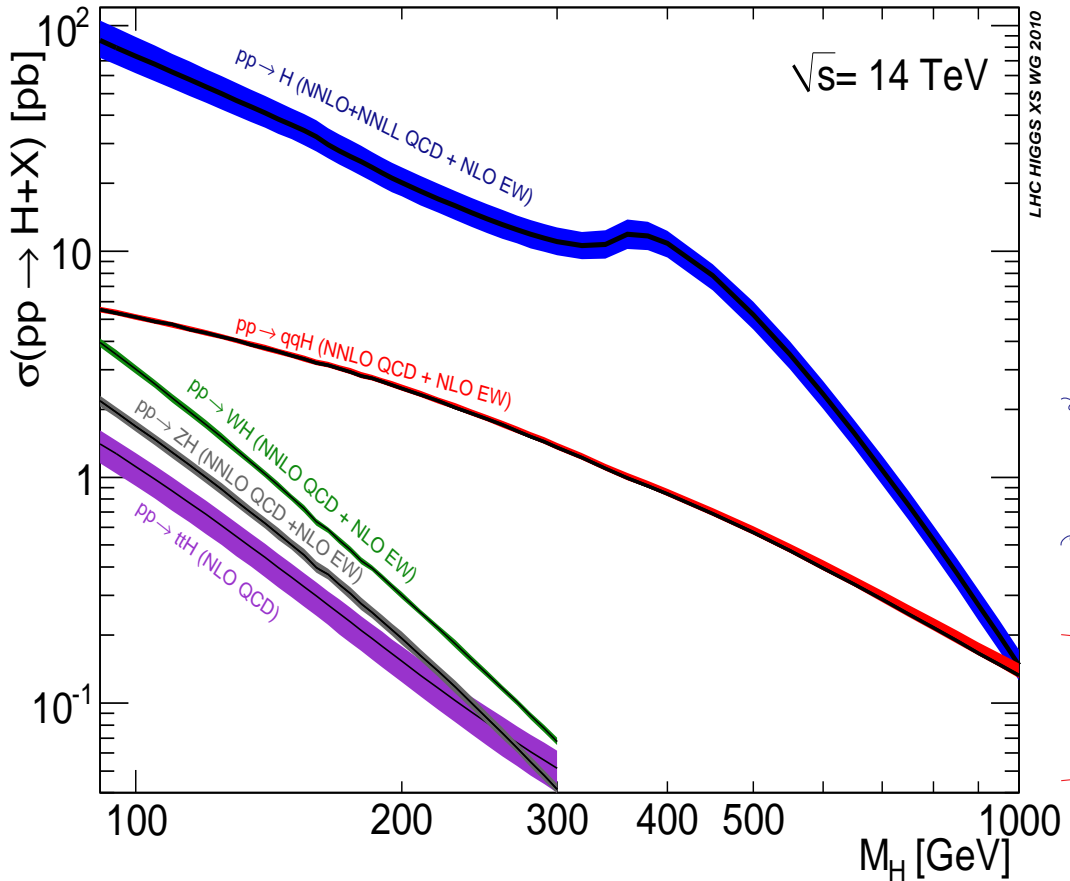
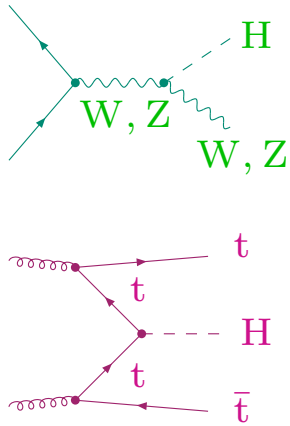
LHC Higgs XS WG 2010



Rough numbers:

|     | $M_H$     | Uncertainties |         | NLO/NNLO/NNLO+ |       |
|-----|-----------|---------------|---------|----------------|-------|
|     |           | scale         | PDF4LHC | QCD            | EW    |
| ggF | < 500 GeV | 6–10%         | 8–10%   | >100%          | 5%    |
| VBF | < 500 GeV | 1%            | 2–7%    | 5%             | 5%    |
| WH  | < 200 GeV | 1%            | 3–4%    | 30%            | 5–10% |
| ZH  | < 200 GeV | 1–2%          | 3–4%    | 40%            | 5%    |
| ttH | < 200 GeV | 10%           | 9%      | 5%             | ?     |

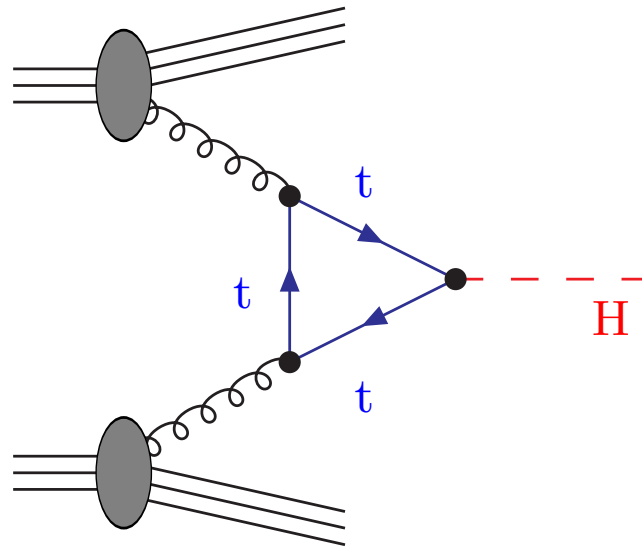
SM Higgs XS predictions  
for the LHC at  $\sqrt{s} = 14 \text{ TeV}$   
LHC Higgs XS WG 2010



Rough numbers:

|     | $M_H$     | Uncertainties |         | NLO/NNLO/NNLO+ |       |
|-----|-----------|---------------|---------|----------------|-------|
|     |           | scale         | PDF4LHC | QCD            | EW    |
| ggF | < 500 GeV | 6–14%         | 7%      | >100%          | 5%    |
| VBF | < 500 GeV | 1%            | 3–4%    | 5%             | 5%    |
| WH  | < 200 GeV | 1%            | 3–4%    | 30%            | 5–10% |
| ZH  | < 200 GeV | 2–4%          | 3–4%    | 45%            | 5%    |
| ttH | < 200 GeV | 10%           | 9%      | 15–20%         | ?     |

## Higgs production via gluon fusion



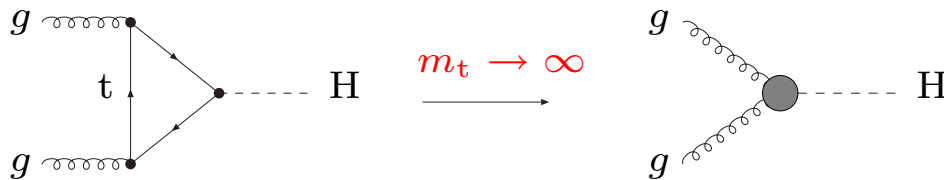
# Corrections to Higgs-boson production via gluon fusion

- QCD corrections:

- ◇ complete NLO correction known
- ◇ NNLO correction known as expansion for  $m_t \rightarrow \infty$  matched with  $\hat{s} \rightarrow \infty$

$$K = \frac{\sigma_{\text{NNLO}}}{\sigma_{\text{LO}}} \sim 2.0$$

- ◇ resummations / virtual / soft terms to NNNLO in limit  $m_t \rightarrow \infty$



Graudenz, Spira, Zerwas '93  
Djouadi, Graudenz, Spira, Zerwas '95

Harlander, Kilgore '01,'02  
Catani, de Florian, Grazzini '01  
Anastasiou, Melnikov '02  
Ravindran, Smith, v.Neerven '03,'04  
Anastasiou, Melnikov, Petriello '04  
Marzani et al. '08  
Pak, Rogal, Steinhauser '09  
Harlander, Ozeren '09

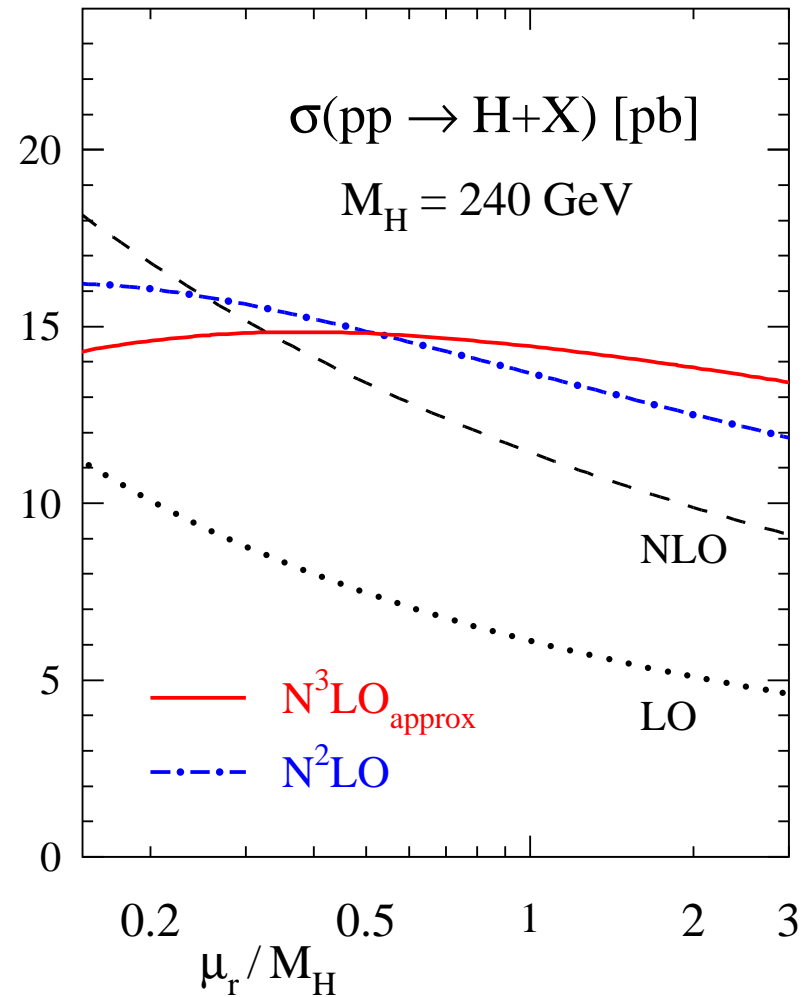
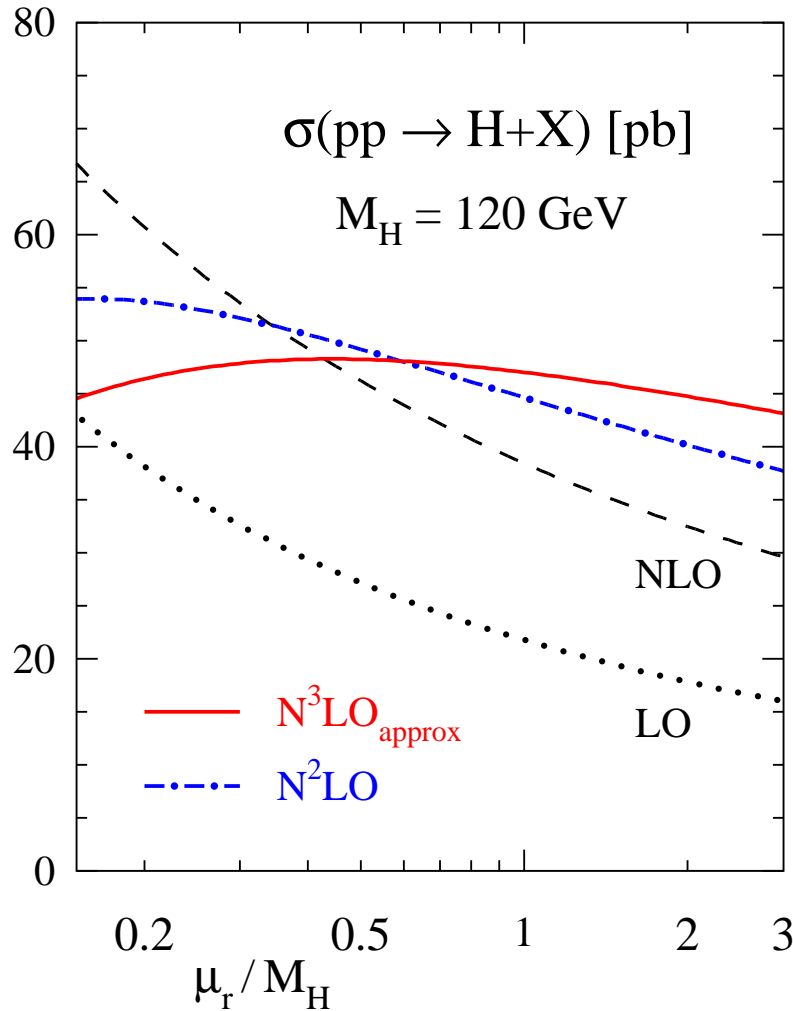
Catani et al. '03; Moch, Vogt '05  
Laenen, Magnea '05; Idilbi, Ji, Ma, Yuan '05  
Ravindran '05,'06; Ravindran, Smith, v.Neerven '06  
Ahrens, Becher, Neubert, Yang '08,'11  
Berger et al. '10; Stewart, Tackmann '11  
Banfi, (Monni,) Salam, Zanderighi '12  
Becher, Neubert '12

- EW corrections

- ◇ complete NLO correction known  $\sim \mathcal{O}(5\%)$
- ◇ mixed  $\mathcal{O}(\alpha\alpha_s)$  corrections for small  $M_H$

Aglietti, Bonciani, Degrassi, Vicini '04,'06  
Degrassi, Maltoni '04  
Actis, Passarino, Sturm, Uccirati '08

Anastasiou, Boughezal, Petriello '08

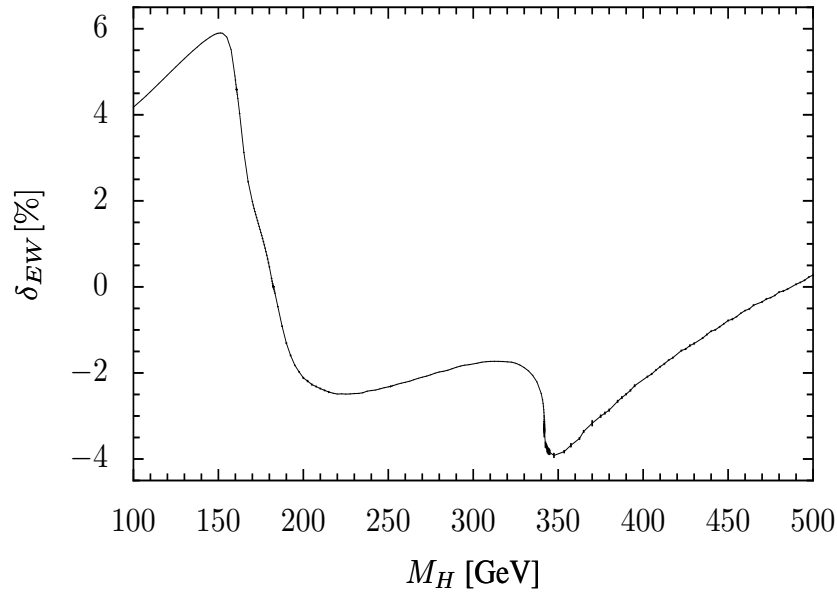


Reduction of renormalization-scale dependence with increasing orders !

$\hookrightarrow$  residual scale uncertainty  $\lesssim 5-10\%$

# NLO EW corrections

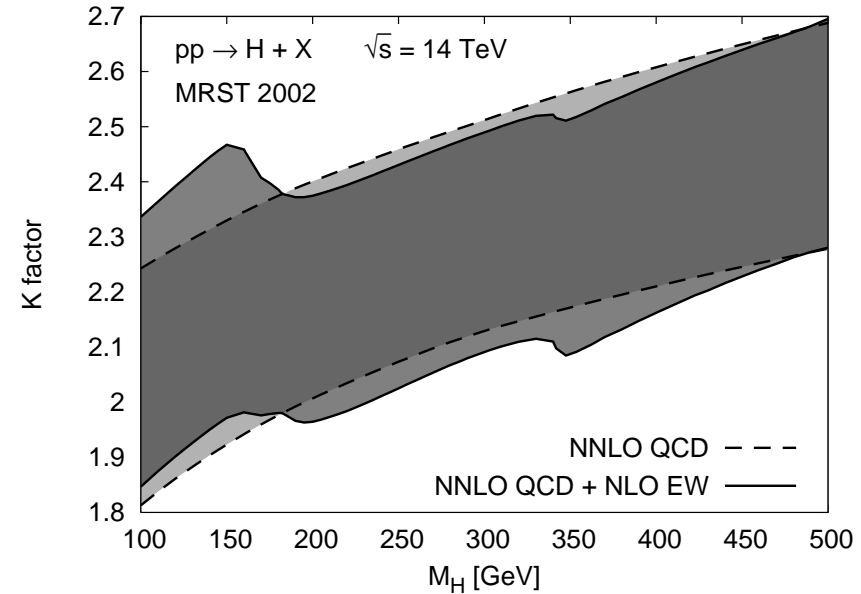
Correction to partonic cross section:



Actis, Passarino, Sturm, Uccirati '08

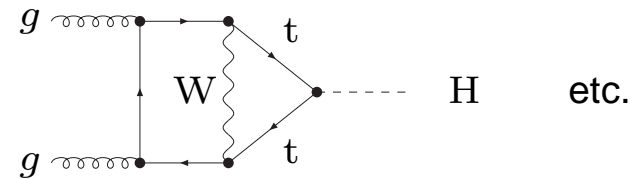
$K$  factors for  $pp$  cross section:

(band width:  $M_H/2 < \mu_{R/F} < 2M_H$ ,  $\mu_R/2 < \mu_F < 2\mu_R$ )



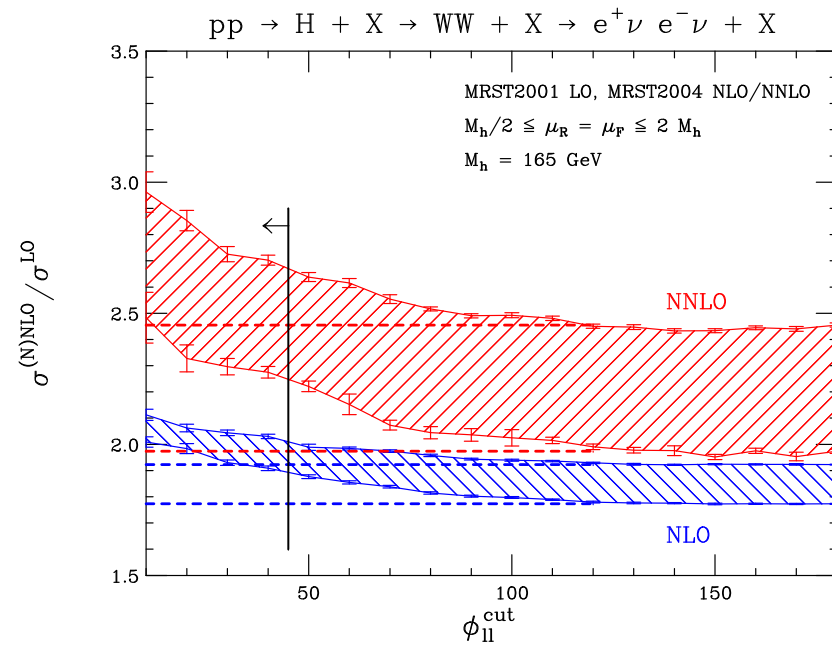
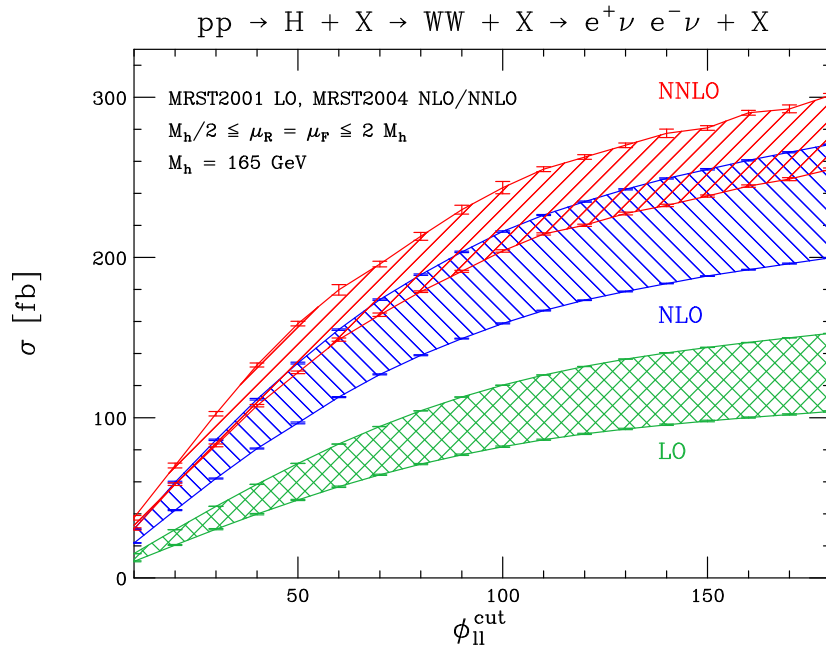
EW corrections ...

- matter at the **5% accuracy level**
- show non-trivial structures near  $WW$ ,  $ZZ$ ,  $t\bar{t}$  thresholds  
 $\hookrightarrow$  finite widths of particles in loops required (otherwise unphysical peaks)
- mixed  $\mathcal{O}(\alpha\alpha_s)$  corrections for small  $M_H$  Anastasiou, Boughezal, Petriello '08 suggest **factorization of QCD and EW corrections** within good accuracy



# Combination of Higgs production and decay $H \rightarrow WW \rightarrow ll\nu\nu$

Anastasiou, Dissertori, Stöckli '07

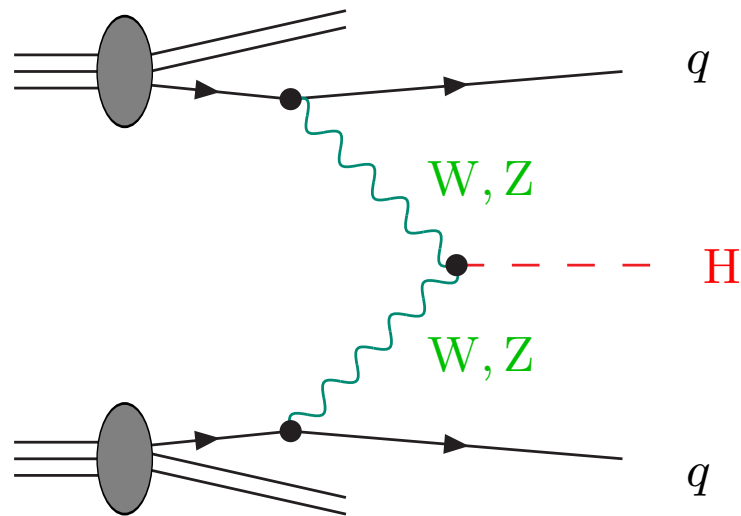


$\phi_{ll} =$  angle between charged decay leptons in the transverse plane

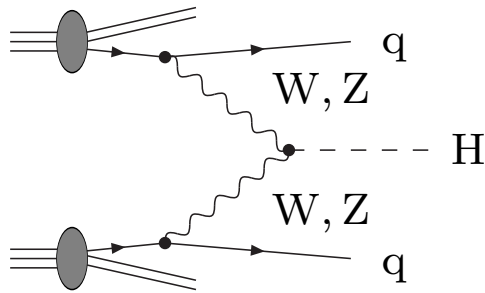
$K$  factors in general depend on decay phase space.



## Higgs production via vector-boson fusion



## A multi-leg example: Higgs production via weak vector-boson fusion (VBF)



colour exchange between quark lines suppressed

⇒ **small QCD corrections**

Han, Valencia, Willenbrock '92; Spira '98;  
Djouadi, Spira '00; Figy, Oleari, Zeppenfeld '03

↔ *t*-channel approximation (vertex corrections)

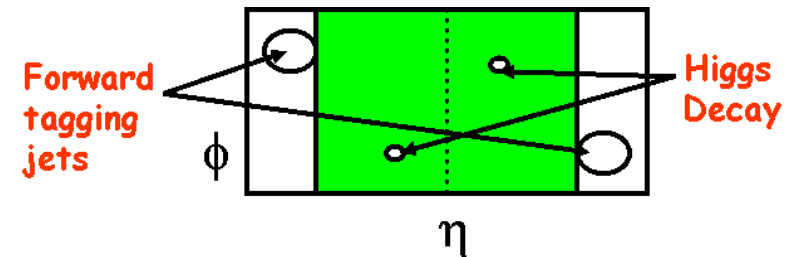
### VBF cuts and background suppression:

- 2 hard “tagging” jets demanded:  
 $p_{Tj} > 20 \text{ GeV}, \quad |y_j| < 4.5$
- tagging jets forward–backward directed:  
 $\Delta y_{jj} > 4, \quad y_{j1} \cdot y_{j2} < 0.$

### ↪ **Suppression of background**

- from other (non-Higgs) processes,  
such as  $t\bar{t}$  or  $WW$  production Zeppenfeld et al. '94-'99
- induced by Higgs production via gluon fusion,  
such as  $gg \rightarrow ggH$  Del Duca et al. '06; Campbell et al. '06

signature = Higgs + 2jets



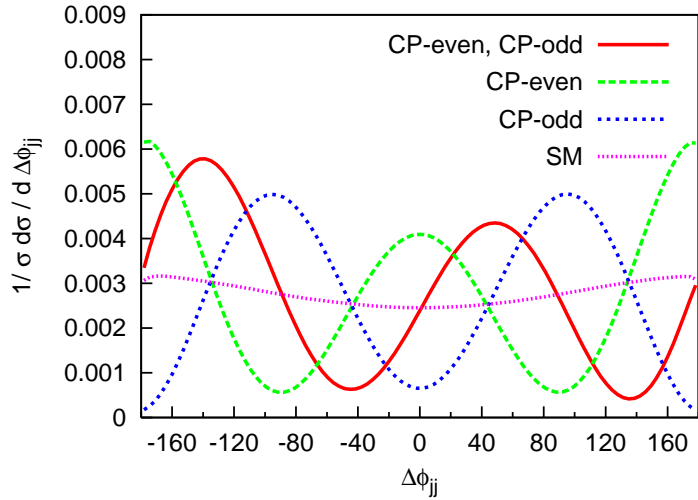
# Work on radiative corrections to the production of Higgs+2jets

- NLO QCD corrections to VBF in DIS-like approximation
  - ◇ total cross section Han, Valencia, Willenbrock '92; Spira '98; Djouadi, Spira '00
  - ◇ distributions Figy, Oleari, Zeppenfeld '03; Berger, Campbell '04
  - ◇ matching with parton shower (POWHEG) Nason, Oleari '09
- (full) NLO QCD+EW corrections to VBF
  - ↔ NLO QCD  $\sim$  NLO EW  $\sim$  5–10% Ciccolini, Denner, S.D. '07  
Figy, Palmer, Weiglein '10 (DIS-like EW)
- NNLO QCD corrections to VBF in DIS-like approximation Bolzoni, Maltoni, Moch, Zaro '10
  - ↔ NNLO QCD  $\sim$  1–2%
- NLO QCD corrections to  $gg \rightarrow H_{gg}$ , etc. Campbell, R.K.Ellis, Zanderighi '06
  - ↔ contribution to VBF  $\sim$  5% Nikitenko, Vazquez '07 (NLO scale uncertainty  $\sim$  35%)
- QCD loop-induced interferences between VBF and  $H_{gg}$ -initiated channels
  - ↔ impact  $\lesssim 10^{-3}$  % (negligible!) Andersen, Binoth, Heinrich, Smillie '07  
Bredenstein, Hagiwara, Jäger '08
- loop-induced VBF in  $gg$  scattering Harlander, Vollinga, Weber '08
  - ↔ impact  $\sim$  0.1%
- SUSY QCD+EW corrections Hollik, Plehn, Rauch, Rzehak '08
  - ↔  $|MSSM - SM| \lesssim 1\%$  for SPS points (2–4% for low SUSY scales)

# Distribution in the azimuthal angle difference $\Delta\phi_{jj}$ of the tagging jets

Sensitivity to non-standard effects:

Hankele, Klämke, Zeppenfeld, Figy '06



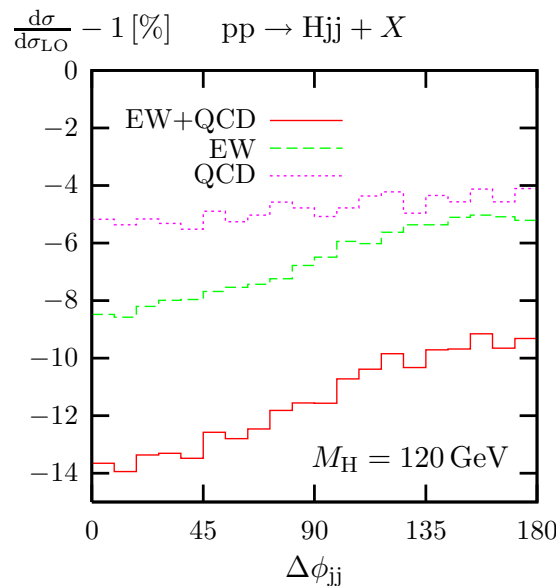
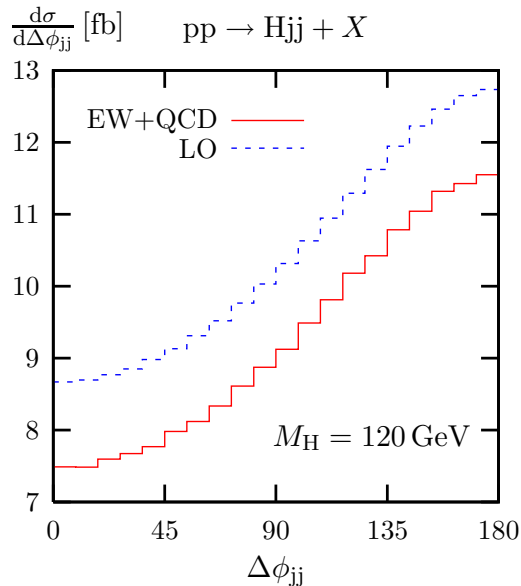
(Individual contributions without SM)

CP-even:  $\mathcal{L} \propto HW_{\mu\nu}^+ W^{-,\mu\nu}$

CP-odd:  $\mathcal{L} \propto H\tilde{W}_{\mu\nu}^+ W^{-,\mu\nu}$

Corrections to the  $\Delta\phi_{jj}$  distribution:

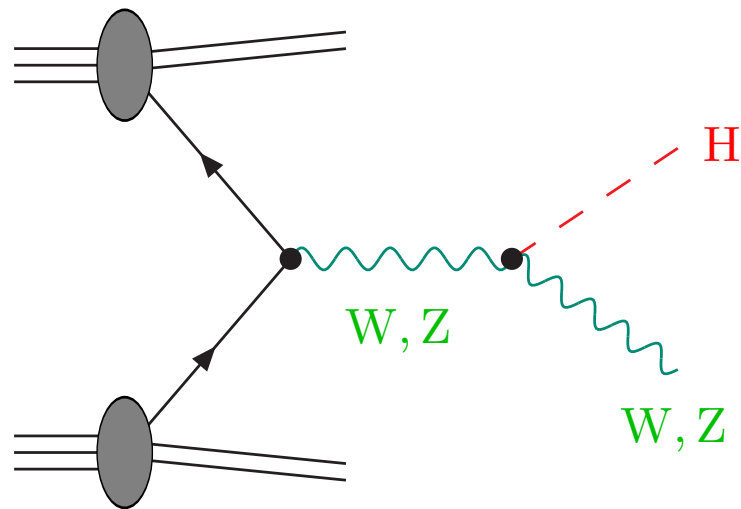
Ciccolini, Denner, S.D. '07



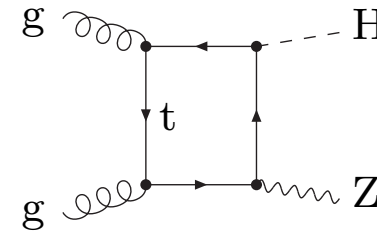
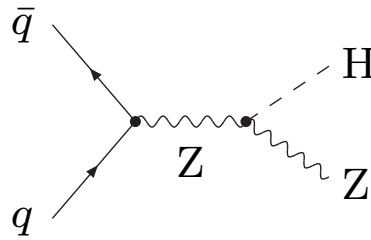
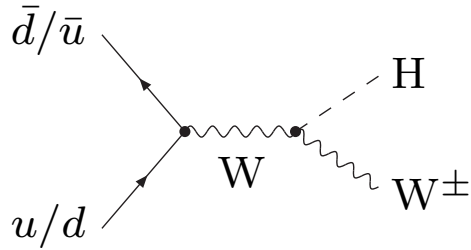
HAWK

Neglected corrections could be misinterpreted as non-standard couplings

## Production via Higgs-strahlung



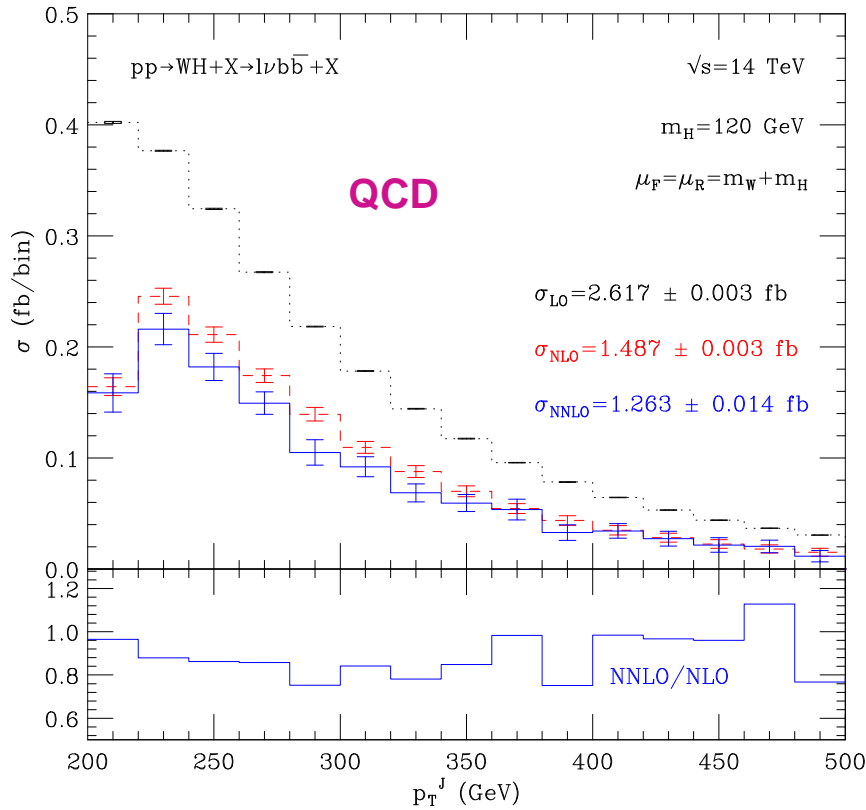
## Current status of theoretical predictions



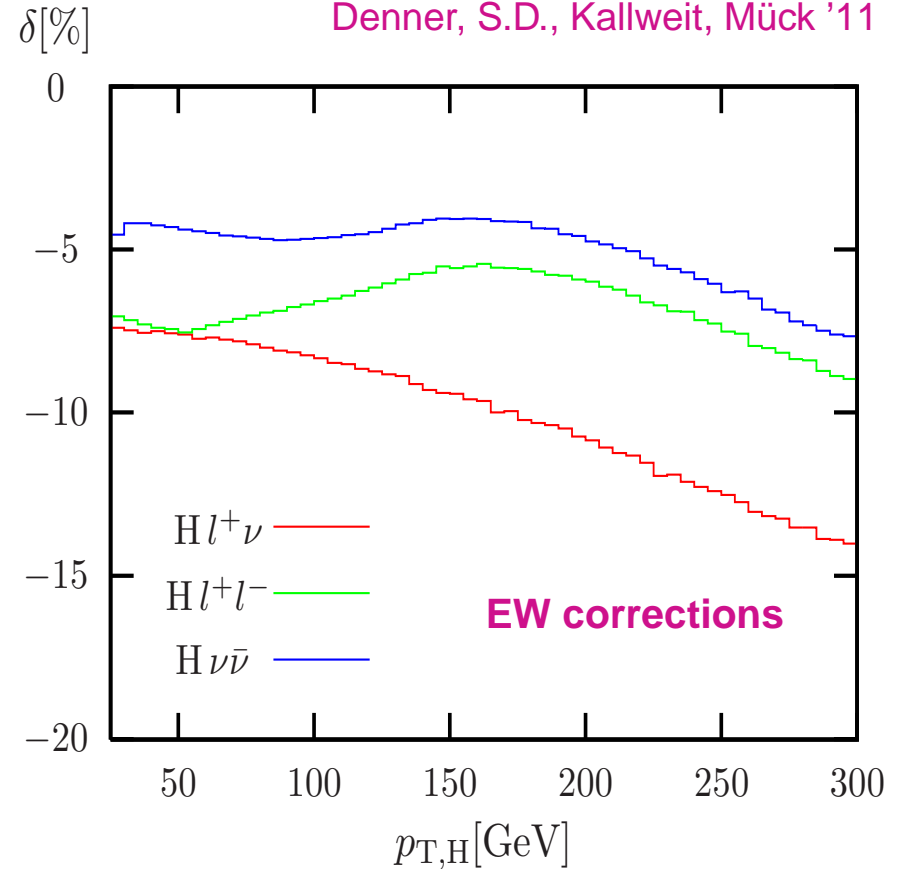
- **NLO QCD:** corrections entirely Drell–Yan like  
Han, Willenbrock '91; Ohnemus, Stirling '93; Baer, Bailey, Owens '93  
V2VH (Spira); MCFM (Campbell, R.K.Ellis)
- **NLO EW:** **total** cross section, stable W/Z bosons  
Ciccolini, S.D., Krämer '03  
**differential** cross sections, via HAWK with W/Z decays  
Denner, S.D., Kallweit, Mück '11
- **NNLO QCD:** **total** cross section, stable W/Z bosons  
Drell–Yan-like part,  $gg \rightarrow ZH$   
Brein, Djouadi, Harlander '03 (VH@NNLO)  
**differential** WH XS, with W decay, Drell–Yan-like part  
Ferrera, Grazzini, Tramontano '11  
**total** cross section, non-Drell–Yan-like parts  
Brein, Harlander, Wiesemann, Zirke '11
- **NNNLO QCD:** **total** cross section,  $gg$  channel  
Altenkamp et al. '12

# QCD and EW corrections to the $p_{T,H}$ distributions

Ferrera, Grazzini, Tramontano '11



Denner, S.D., Kallweit, Mück '11



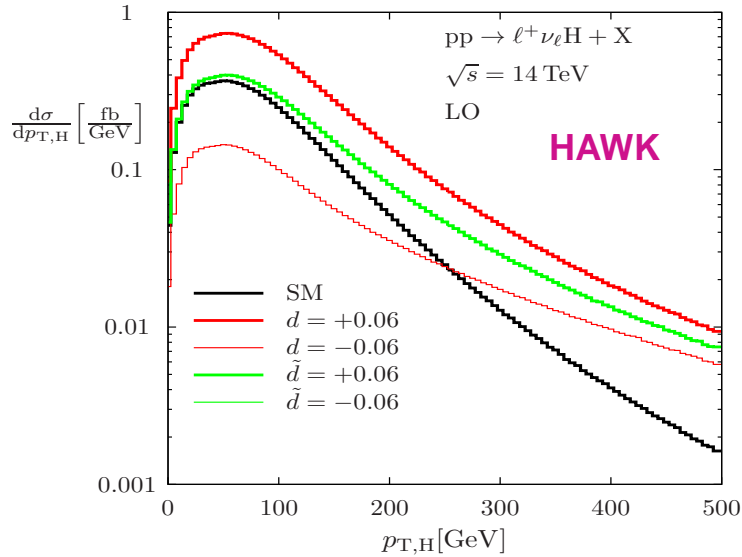
Boosted-Higgs  $p_{T,H} > 200 \text{ GeV}$  (“fat jet” with  $b\bar{b}$  substructure) Butterworth et al. '08  
ATL-PHYS-PUB-2009-088

pronounces corrections to  $HW \rightarrow Hl^+\nu$  at  $p_{T,H} \sim 200-300 \text{ GeV}$

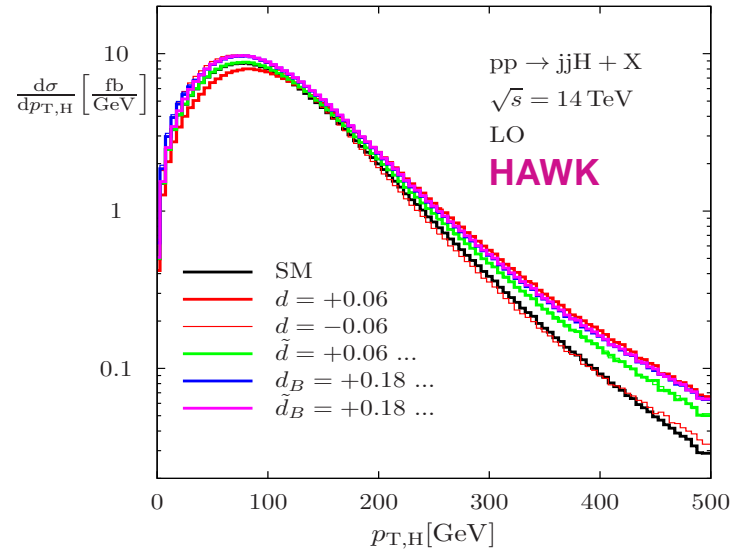
- $\delta_{\text{QCD}} \sim -5-20\%$
- $\delta_{\text{EW}} \sim -10-15\%$

# Anomalous VHH couplings in $p_{T,H}$ spectra

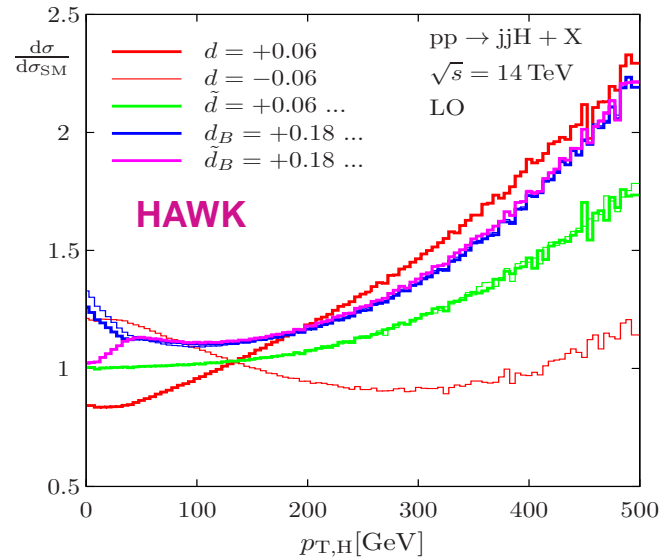
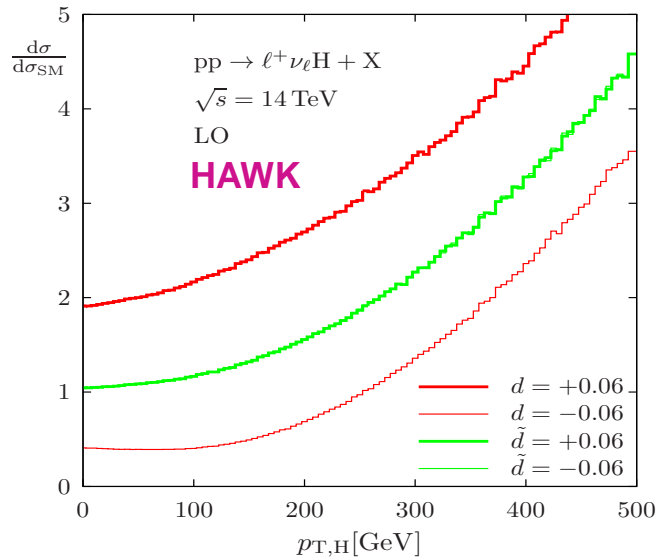
$W^+H$  (acc. cuts)



VBF (with VBF cuts)



similar VBF results by  
 Hankele, Klämke,  
 Zeppenfeld, Figy '06



$$\mathcal{L} \propto HW_{\mu\nu}W^{\mu\nu}$$

$$\mathcal{L} \propto H\tilde{W}_{\mu\nu}W^{\mu\nu}$$

$$\mathcal{L} \propto HB_{\mu\nu}B^{\mu\nu}$$

$$\mathcal{L} \propto H\tilde{B}_{\mu\nu}B^{\mu\nu}$$

Impact of ACs larger in WH production than in VBF !



A loop-theorist's summary of ...

## Two decades of Higgs precision calculations

Successful predictions required + triggered great leaps forward

- at the **multi-loop frontier**
  - ↪ two loops with masses, massless multi-loop calculations
- at the **LO multi-leg frontier**
  - ↪ automatized MCs based on full MEs
- at the **NLO multi-leg frontier**
  - ↪ full  $2 \rightarrow 4(5)$  calculations, automation
- for calculation **beyond fixed orders**
  - ↪ QCD resummations / parton showering / matching at NLO
- in many **conceptual issues**
  - ↪ unstable particles, etc.



# Outlook – next steps

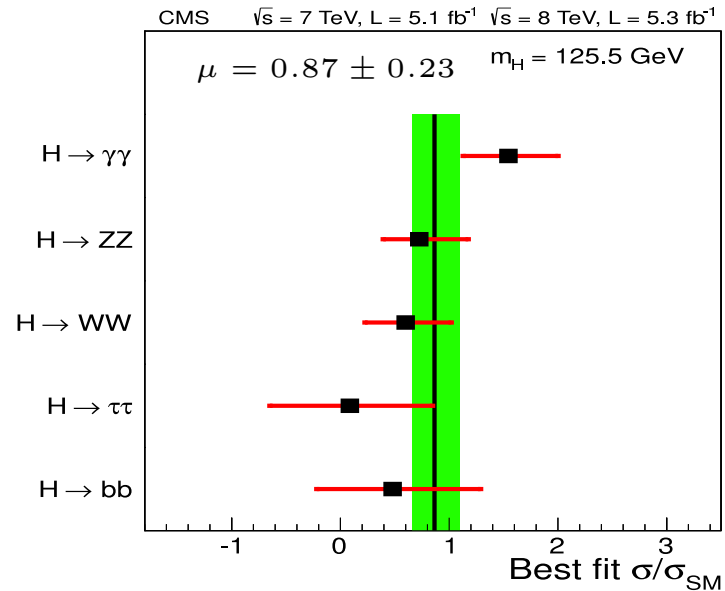
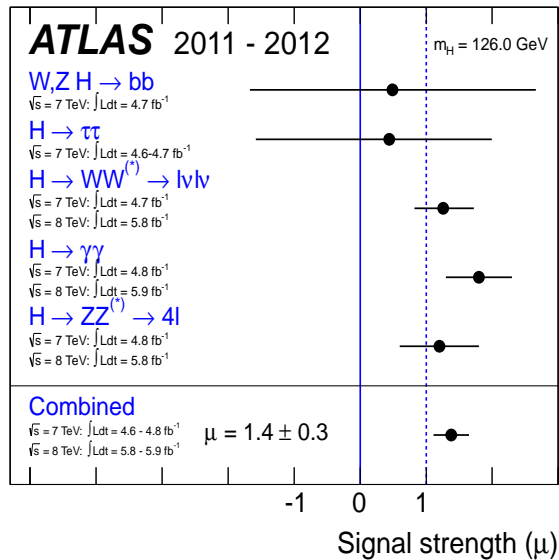


# Higgs coupling analysis

- 1st step: global analysis of signal strengths  $\mu$

Signal strength  $\mu$ :  $\sigma_{\text{obs}} = \mu \times \sigma_{\text{SM}} \times \text{BR}_{\text{SM}}$

Status July 2012:



## Higgs coupling analysis

- 1st step: global analysis of signal strengths  $\mu$
- 2nd step: rescaling of SM couplings  
... different variant proposed by many authors

Zeppenfeld et al. '00; Dührssen et al. '04; Lafaye et al. '09; ...

### Interim recommendation of the LHC HXS WG '12:

↪ rescale all SM Higgs couplings:  $g_i = \kappa_i \times g_i^{\text{SM}}$   $i = \text{HWW, HZZ, Htt, ...}$   
with simplifying assumptions:

- ◇ **no new tensor structures** in couplings  
↪ ignores shape distortions by BSM effects (e.g. CP-odd couplings)
- ◇ **rescaling of SM corrections** (to avoid artificial deviations in SM limit)  
↪ QCD corrs: reasonable, since dominant correction factorize  
EW corrs: failure for BSM → additional uncertainties of  $\sim 5\text{--}10\%$
- ◇ narrow-width approximation for Higgs, no  $gg \rightarrow ZH$ , etc.

### Recipe can give qualitative picture:

- ◇ deviations from SM rates significant ?
- ◇ pattern of deviations (W/Z sector? Custodial symmetry? fermion sector? ...)

## Higgs coupling analysis

- 1st step: global analysis of signal strengths  $\mu$
- 2nd step: rescaling of SM couplings
- 3rd+ steps: more sophisticated approaches
  - ◇ **model-independent effective-field theory (EFT)**
    - SM with Higgs boson = low-energy theory
    - inclusion of, e.g., all  $d = 6$  operators for “Higgs” couplings
    - consistent inclusion of higher-order corrections in EFT approach
    - ↪ hints for BSM model building ?
  - ◇ **precision analyses in specific BSM models**
    - THDM, triplet models
    - with and w/o SUSY
    - ↪ constraints on or hints for additional new Higgs-like states

# Future challenges

- Analyse  $t\bar{t}H$  production

- ◇ **Relevance:** direct experimental access to  $t\bar{t}H$  Yukawa coupling

- ◇ **Problem:** control background by  $pp \rightarrow t\bar{t}b\bar{b}, t\bar{t} + \text{jets}$  ( $S/B \sim 1/10$ )

status 2008: signal not significant due to background contamination

↪ activities: – more sophisticated tricks in analysis

e.g. “fat jet” with  $b\bar{b}$  substructure

Plehn, Salam, Spannowsky '09

– NLO QCD prediction also for background

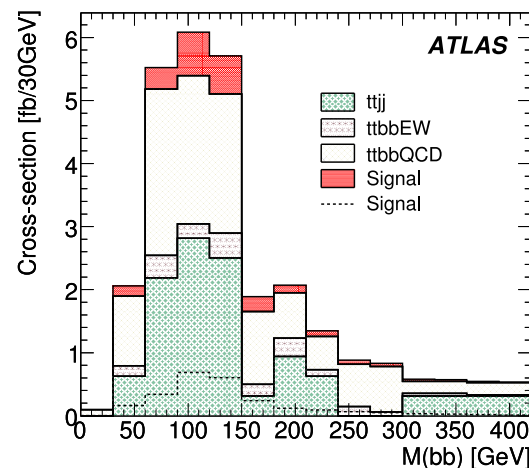
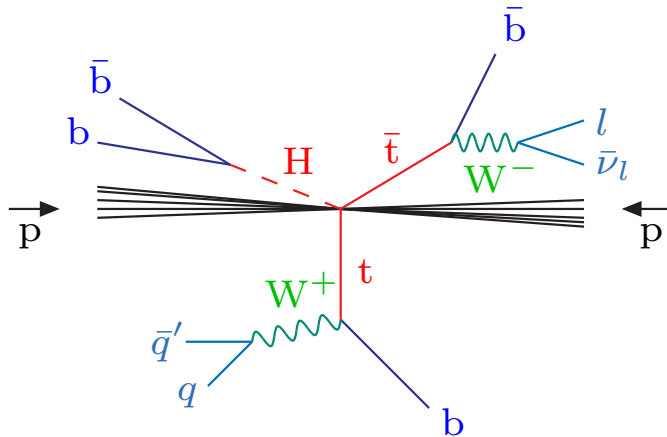
$pp \rightarrow t\bar{t}b\bar{b}$

Bredenstein, Denner, S.D., Pozzorini '09

Bevilacqua, Czakon, Papadopoulos, Pittau, Worek '09

$pp \rightarrow t\bar{t} + 2\text{jets}$

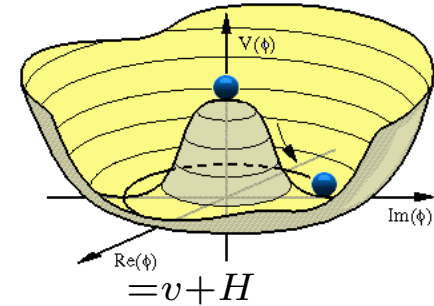
Bevilacqua, Czakon, Papadopoulos, Worek '09



“CSC book”  
CERN-OPEN-2008-020

## Future challenges

- Analyse  $t\bar{t}H$  production
- Triple-Higgs coupling
  - ◇ **Relevance:** reconstruction of the Higgs potential (at least partially)



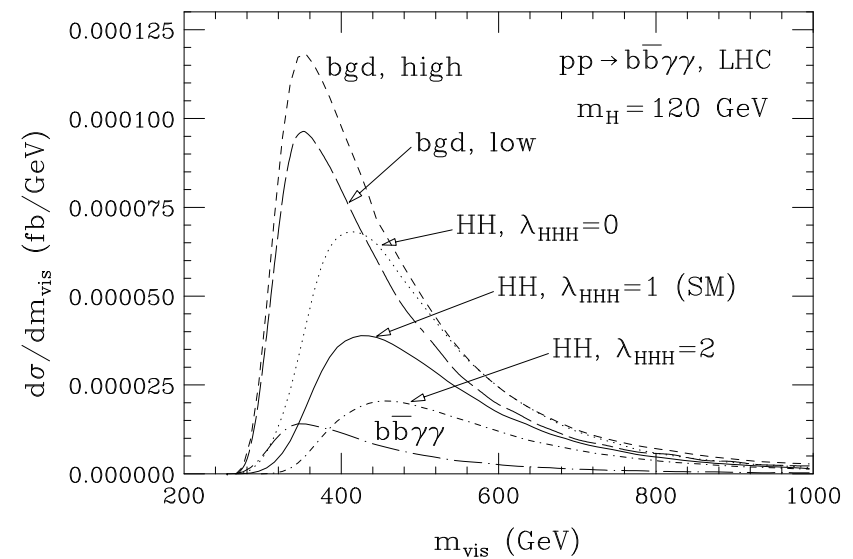
$$V(H) \Big|_{\text{SM, U gauge}} = \text{const} + \frac{1}{2} M_H^2 H^2 + \frac{g M_H^2}{4 M_W} H^3 + \frac{g^2 M_H^2}{32 M_W^2} H^4$$

- ◇ **Problem:**
  - small Higgs pair production cross sections
  - $M_H \sim 126 \text{ GeV} \rightarrow b\bar{b}\gamma\gamma$  final state with BR suppression

- ◇  $H^3$  coupling requires at least high-luminosity LHC  
 $\hookrightarrow$  ILC highly desirable here

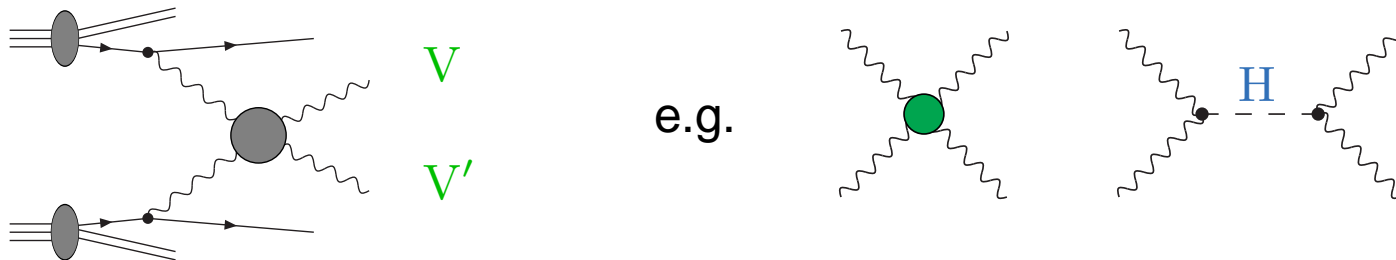
- ◇  $H^4$  coupling out of reach ( $\sigma_{HHH}$  way too small)

Baur, Plehn, Rainwater '03



## Future challenges

- Analyse  $t\bar{t}H$  production
- Triple-Higgs coupling
- Vector-boson scattering
  - ◇ **Relevance:** – test of weak coupling of longitudinal vector bosons
    - analysis of quartic gauge couplings
    - high sensitivity to new physics related to EWSB
  - ◇ **Problem:** small cross sections, large background
  - ◇ Role of the Higgs boson:  
**Off-shell Higgs exchange rescues unitarity in SM.**  
↪ SM with low-mass Higgs boson = background in BSM searches !
  - ◇ Full potential of channels require high-luminosity LHC





# Conclusions



## Higgs physics – status 2012

- **SM predictions in good shape** for  $gg \rightarrow H$ , VBF, and WH/ZH uncertainties  $\sim 5\text{--}20\%$  depending on final state
- **ATLAS/CMS find Higgs candidate** at  $M_H = 126 \text{ GeV}$  via  $H \rightarrow \gamma\gamma/ZZ^*/WW^*$  compatible with Tevatron  $3\sigma$  evidence for  $H \rightarrow b\bar{b}$ 
  - ↪ **spectacular agreement with SM fit to EW precision data**
- **BUT:** scale of BSM physics might be very large
  - ↪ precision might be the way to new discoveries

## The near future

- Establishment of  $H \rightarrow b\bar{b}/\tau\tau$  and  $t\bar{t}H$  signals (hopefully)
- **Higgs coupling analysis** beyond simple rescalings of XS and BR
- Constraints on **specific BSM models** (MSSM, THDM, etc.)

## The far future (including high-luminosity LHC)

Precision BSM physics, triple-Higgs coupling,  $W_L$  scattering, etc. (?)

⇒ **Tremendous homework for theorists**

**Higgs physics might guide the way to more comprehensive theories beyond SM !**

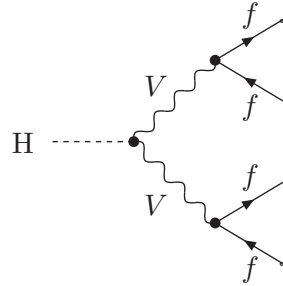
# Backup slides



# An example: $H \rightarrow WW/ZZ \rightarrow 4f$

## Survey of Feynman diagrams for NLO corrections

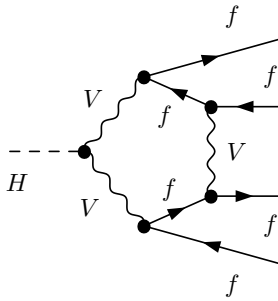
Lowest order:



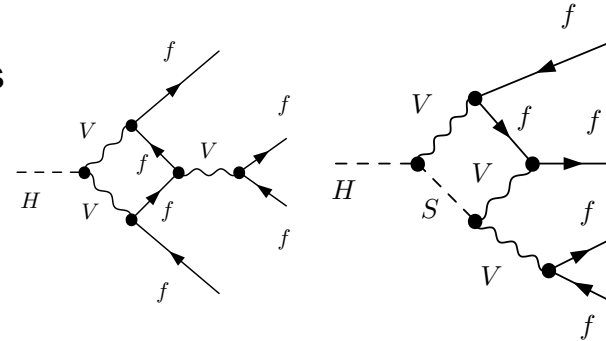
Typical one-loop diagrams:

# diagrams =  $\mathcal{O}(200-400)$

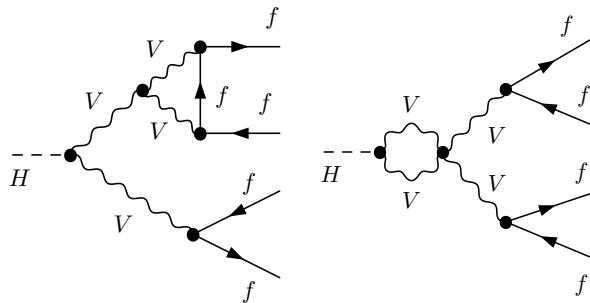
pentagons



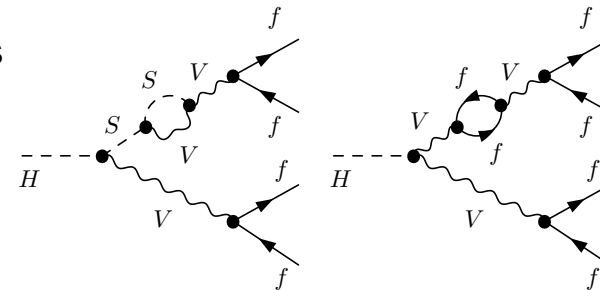
boxes



vertices



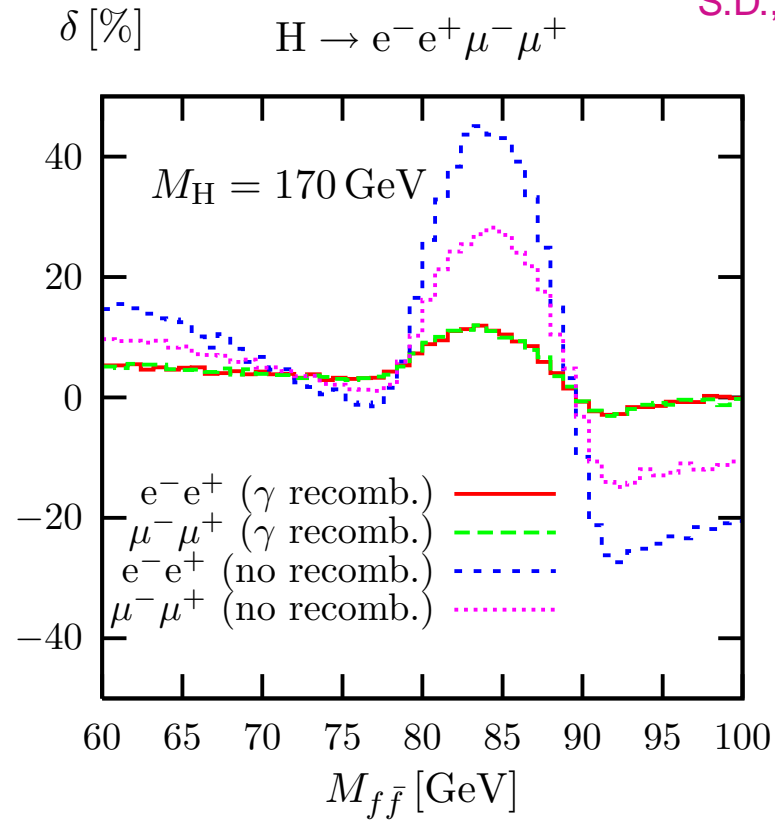
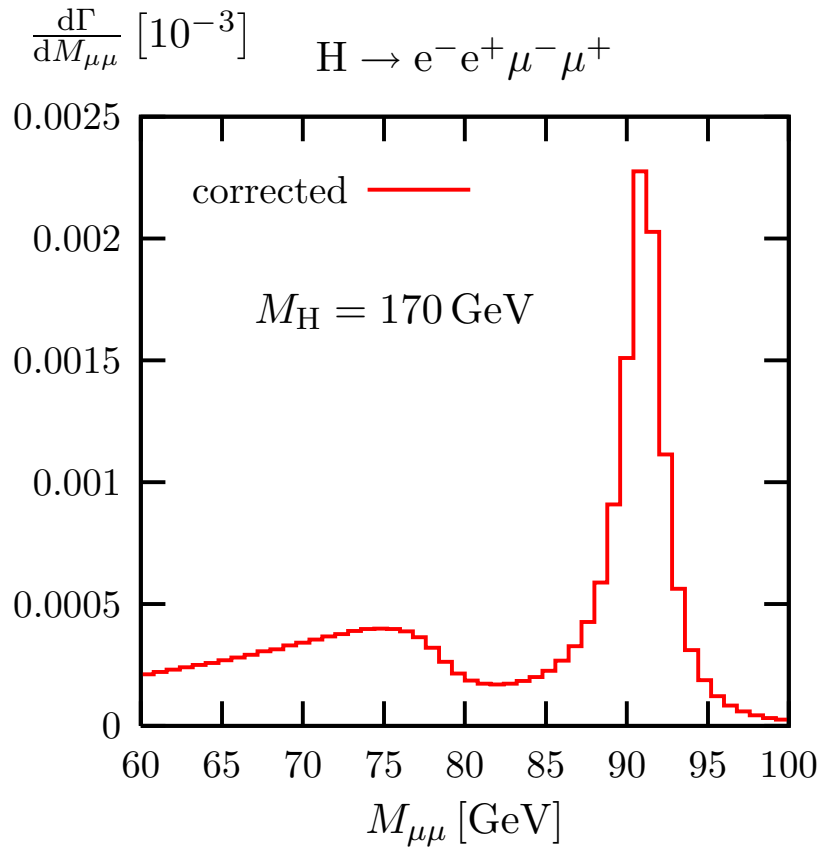
self-energies



+ tree graphs with real gluon or photons

# Distribution of invariant $Z$ mass in $H \rightarrow ZZ \rightarrow e^-e^+\mu^-\mu^+$

Bredenstein, Denner,  
S.D., Weber '06



*Prophecy4f*

$\gamma$  recombination if  $M_{e\gamma/\mu\gamma} < 5 \text{ GeV}$

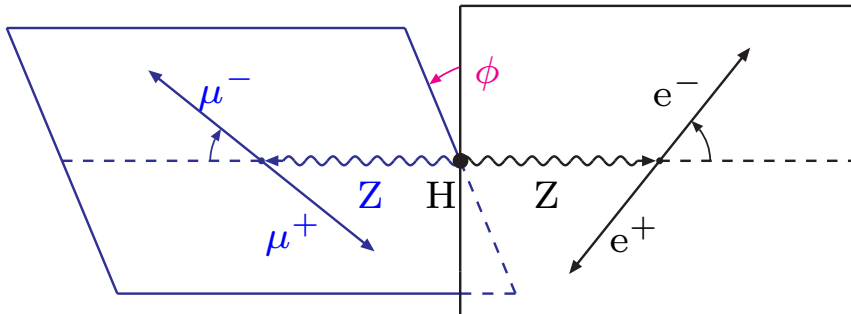
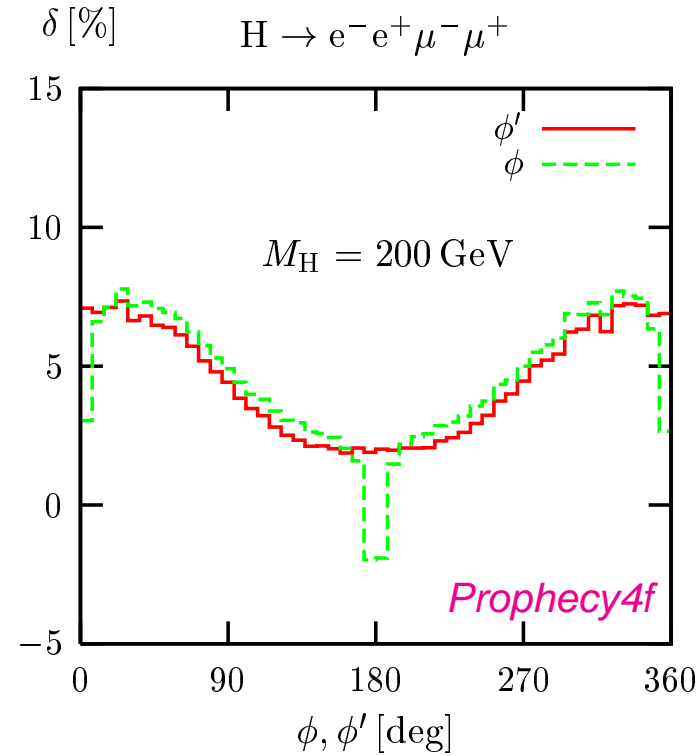
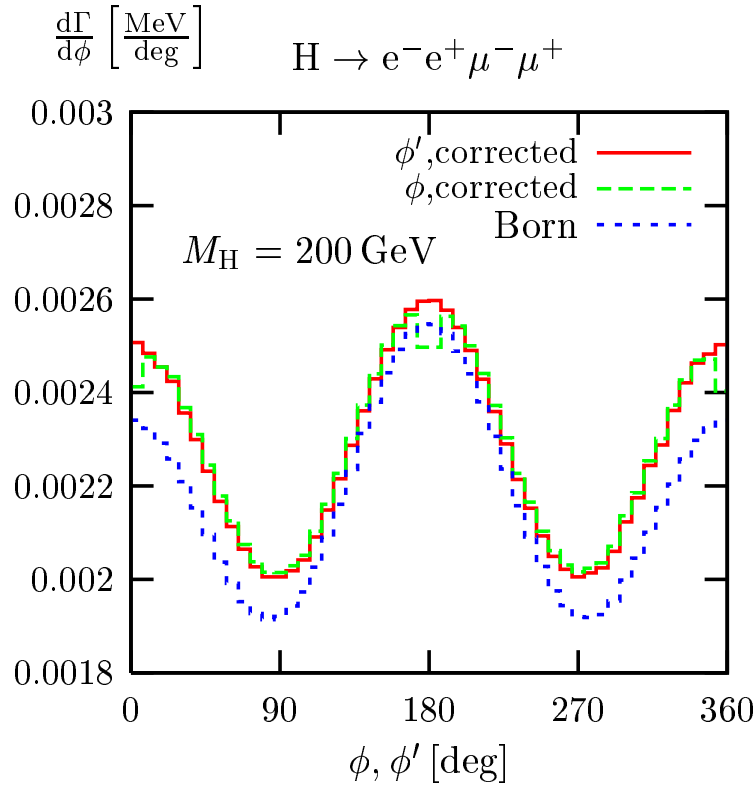
Large corrections due to photon emission in  $Z$  reconstruction

# Corrections to distribution in angle between Z decay planes

Bredenstein, Denner,  
S.D., Weber '06

↪ **5–10% effects** that in general distort shapes of distributions

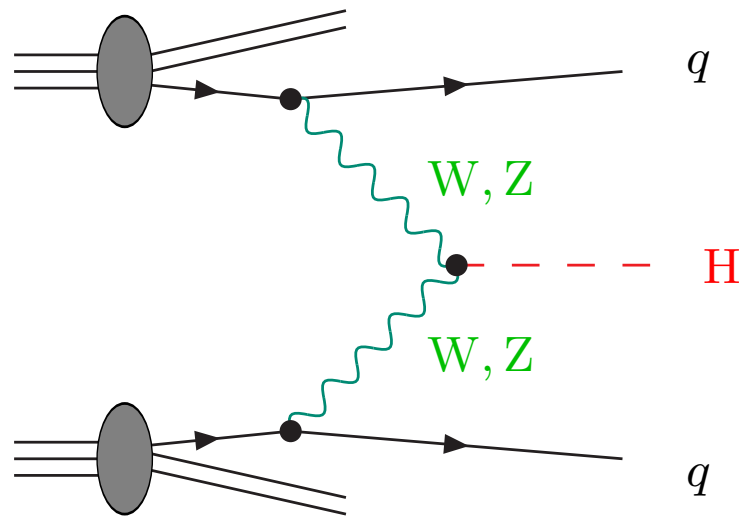
An example:



$$\cos \phi = \frac{(\mathbf{p}_{e^-e^+} \times \mathbf{p}_{e^-}) \cdot (-\mathbf{p}_{\mu^- \mu^+} \times \mathbf{p}_{\mu^-})}{|\mathbf{p}_{e^-e^+} \times \mathbf{p}_{e^-}| \cdot |-\mathbf{p}_{\mu^- \mu^+} \times \mathbf{p}_{\mu^-}|}$$

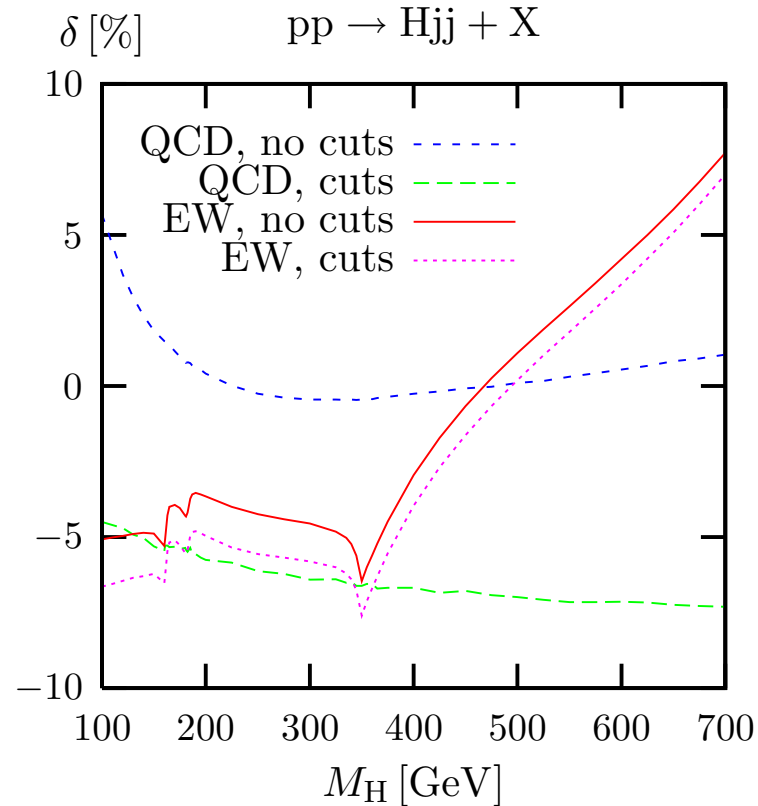
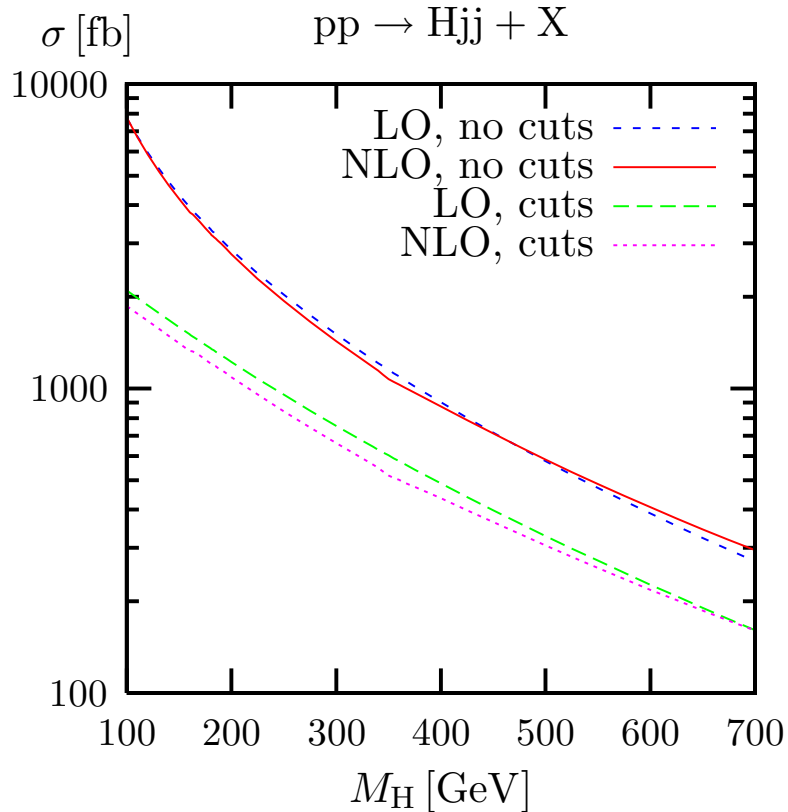
$$\cos \phi' = \frac{(\mathbf{p}_{e^-e^+} \times \mathbf{p}_{e^-}) \cdot (\mathbf{p}_{e^-e^+} \times \mathbf{p}_{\mu^-})}{|\mathbf{p}_{e^-e^+} \times \mathbf{p}_{e^-}| \cdot |\mathbf{p}_{e^-e^+} \times \mathbf{p}_{\mu^-}|}$$

## Higgs production via vector-boson fusion



# Integrated VBF cross section at NLO QCD $\oplus$ EW

Ciccolini, Denner,  
S.D. '07

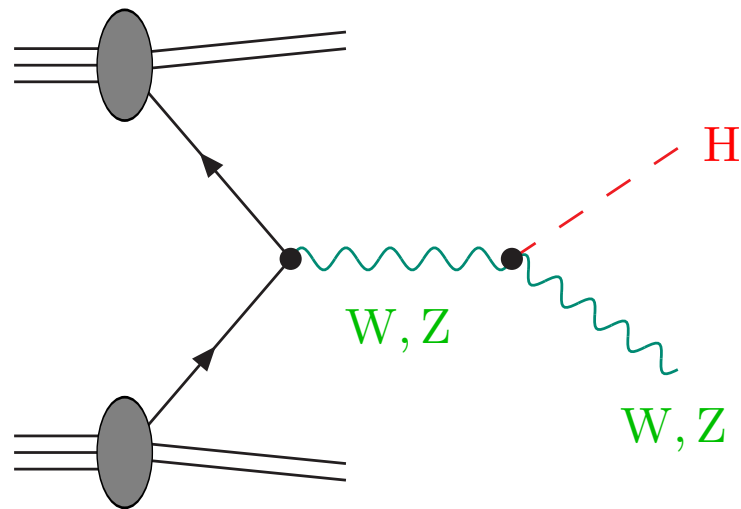


HAWK

- **QCD** and **EW** corrections are of same generic size
- W/Z resonances in  $s$ -channels described via complex-mass scheme
- sensitivity to cuts: large for **QCD**, small for **EW** corrections
- heavy-Higgs corrections at  $M_H \sim 700$  GeV:  $\underbrace{G_\mu M_H^2}_{1\text{-loop}} \sim \underbrace{(G_\mu M_H^2)^2}_{2\text{-loop}} \sim 4\%$   
 $\hookrightarrow$  breakdown of perturbation theory



## Production via Higgs-strahlung



# Total cross section: NNLO QCD and NLO EW corrections

LHC Higgs XS report

CERN-2011-002, arXiv:1101.0593 [hep-ph]

$$\sigma_{\text{WH}} = \sigma_{\text{WH}}^{\text{VH@NNLO}} \times (1 + \delta_{\text{WH,EW}})$$

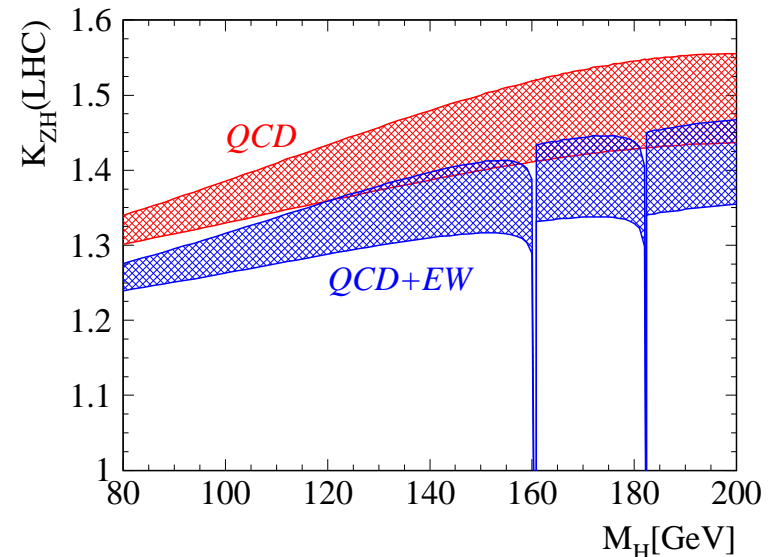
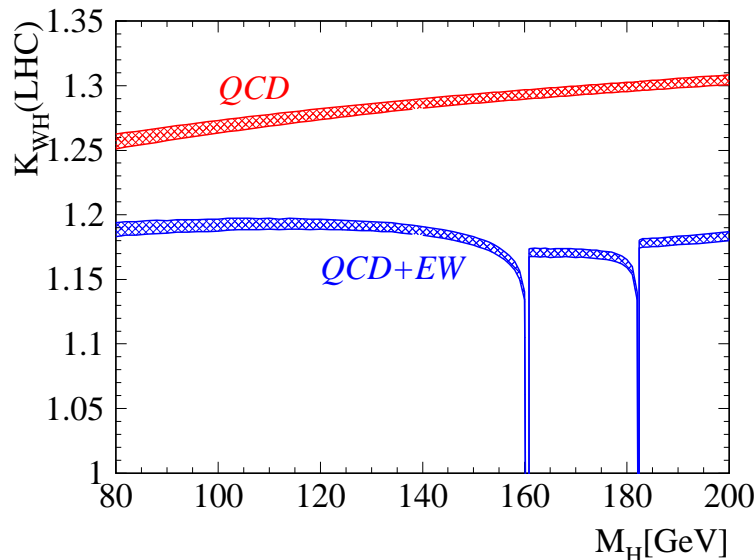
$$\sigma_{\text{ZH}} = \sigma_{\text{ZH}}^{\text{VH@NNLO}} \times (1 + \delta_{\text{ZH,EW}}) + \sigma_{\text{gg} \rightarrow \text{ZH}}$$

Note:

$\delta_{\text{VH,EW}}$  insensitive to PDFs !

$K$  factors for  $pp \rightarrow \text{VH} + X$  @  $\sqrt{s} = 14 \text{ TeV}$ :

Brein et al. & Ciccolini et al. '04



- typical size of corrections:  $\mathcal{O}(\alpha_s^2) \sim \mathcal{O}(\alpha) \sim 5-10\%$
- spikes at  $M_H = 2M_W$  and  $M_H = 2M_Z$   
 = perturbative artifacts from WW/ZZ threshold  
 $\hookrightarrow$  require inclusion of W/Z decays (see below)

# Differential cross section: (N)NLO QCD and NLO EW corrections

LHC Higgs XS report

CERN-2012-002, arXiv:1201.3084 [hep-ph]

$$d\sigma_{\text{WH}} = d\sigma_{\text{WH}}^{\text{VH@NNLO(DY)}} \times (1 + \delta_{\text{WH,EW}})$$

$$d\sigma_{\text{ZH}} = d\sigma_{\text{ZH}}^{\text{VH@NLO}} \times (1 + \delta_{\text{ZH,EW}})$$

Again:

$\delta_{\text{VH,EW}}$  insensitive to PDFs !

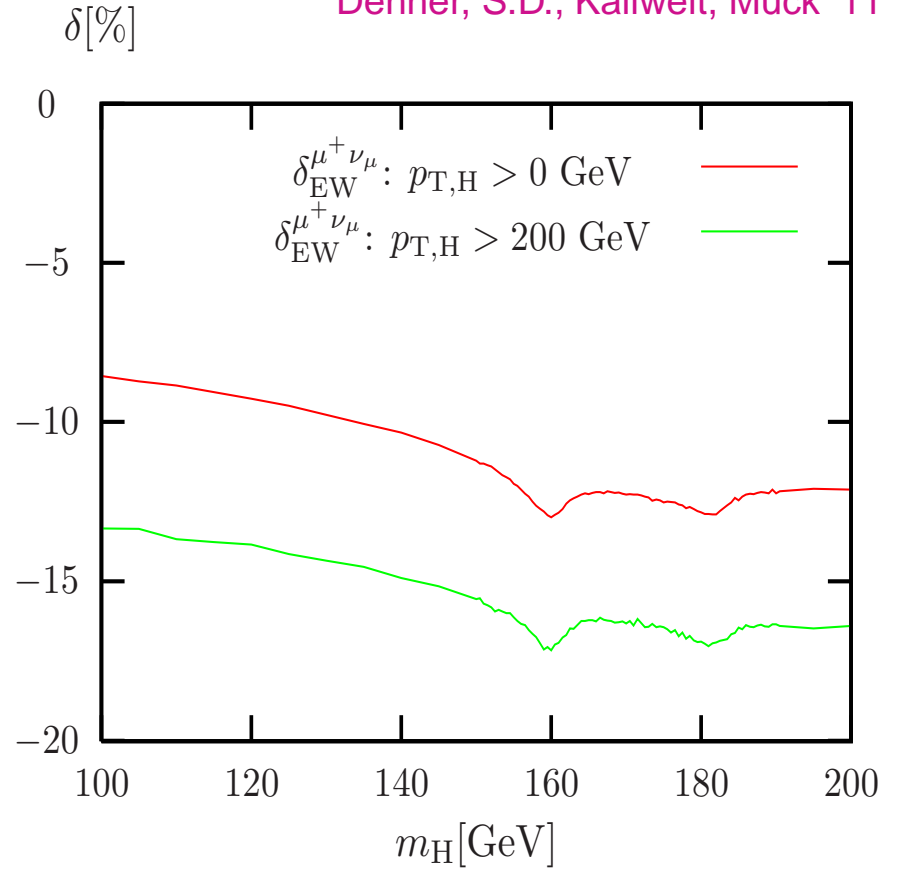
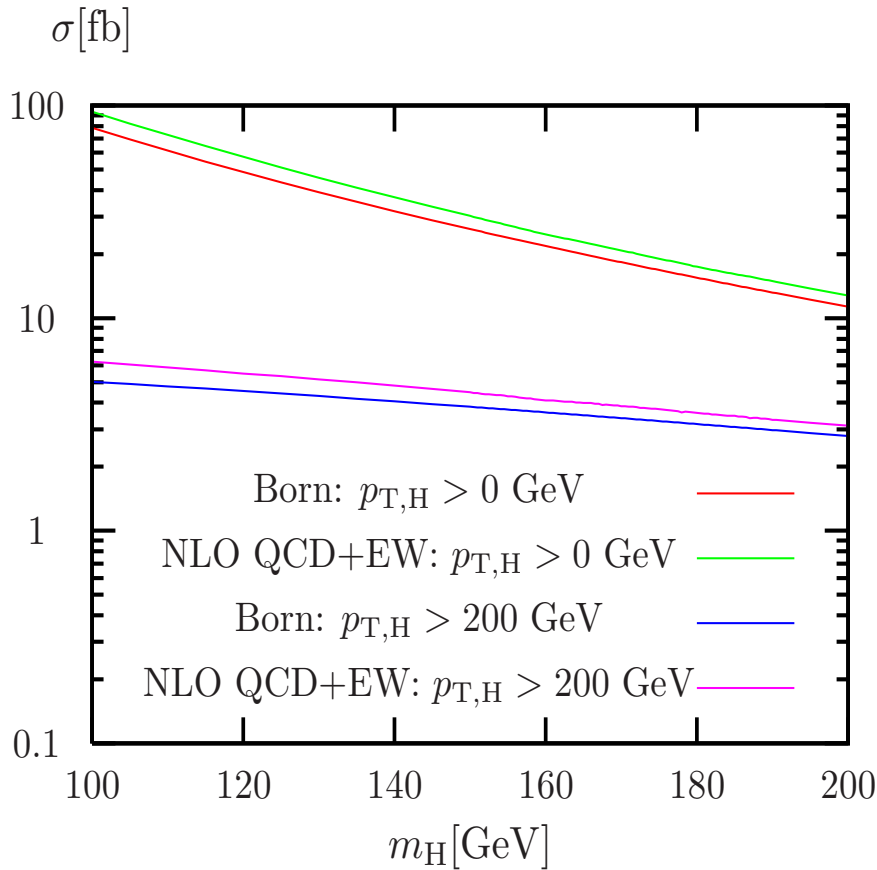
## Features:

- **NNLO QCD** for WH in Drell–Yan-like approximation (ZH in progress)  
Ferrera, Grazzini, Tramontano '11
- **NLO EW (+QCD)** calculated with HAWK  
Denner, S.D., Kallweit, Mück '11
- size of corrections and TH uncertainties larger than for  $\sigma_{\text{tot}}$

| channel                                 | $\text{Hl}^+ \nu_1$ | $\text{Hl}^- \bar{\nu}_1$ | $\text{Hl}^+ 1^-$ | $\text{H}\nu_1 \bar{\nu}_1$ |
|---|---------------------|---------------------------|-------------------|-----------------------------|
| $\delta_{\text{EW}}^{\text{bare}} / \%$ | -14                 | -14                       | -11               | -7                          |
| $\Delta_{\text{PDF}} / \%$              | $\pm 5$             | $\pm 5$                   | $\pm 5$           | $\pm 5$                     |
| $\Delta_{\text{scale}} / \%$            | $\pm 2$             | $\pm 2$                   | $\pm 2$           | $\pm 2$                     |
| $\Delta_{\text{HO}} / \%$               | $\pm 1$             | $\pm 1$                   | $\pm 7$           | $\pm 7$                     |

# NLO EW corrections to the integrated cross section of $pp \rightarrow H\ell^+\nu_\ell + X$

Denner, S.D., Kallweit, Mück '11

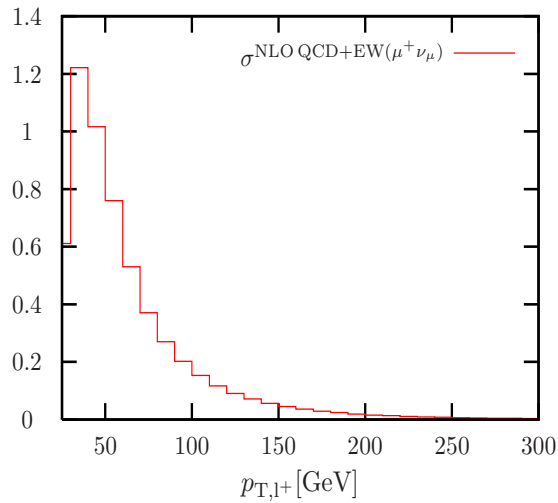


- sound behaviour of  $\delta_{EW}$  near WW/ZZ thresholds
- **size of EW corrections increases for boosted-Higgs scenario wrt  $\sigma_{tot}$  !**

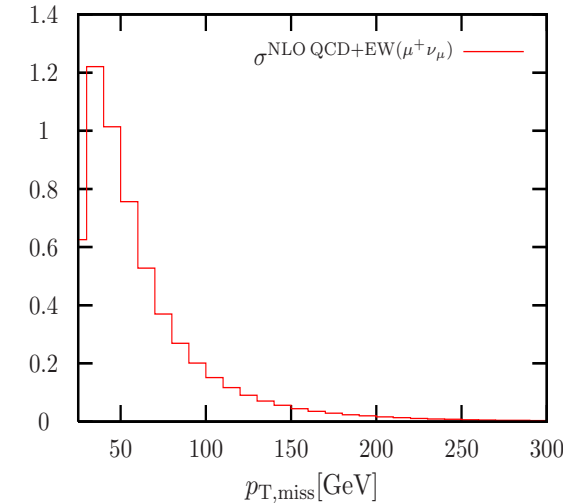
# NLO EW corrections to $p_{T,\ell}$ and $p_{T,\text{miss}}$ distributions for $pp \rightarrow H\ell^+ \nu_\ell + X$

Denner, S.D., Kallweit, Mück '11

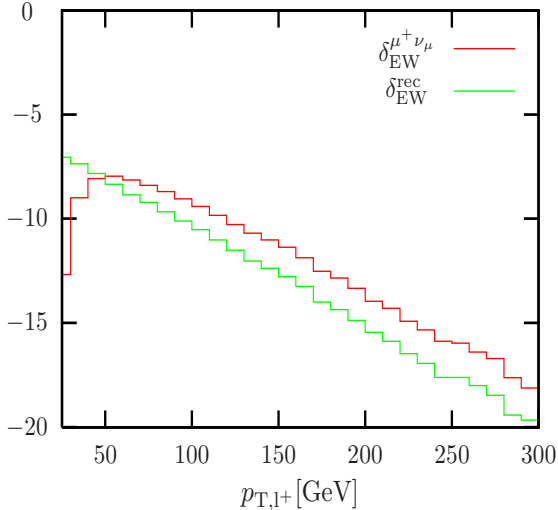
$d\sigma/dp_{T,\ell^+}[\text{GeV}][\text{fb}]$



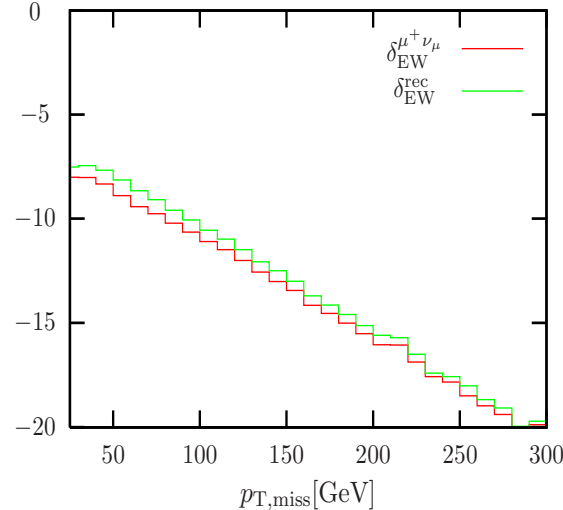
$d\sigma/dp_{T,\text{miss}}[\text{GeV}][\text{fb}]$



$\delta[\%]$



$\delta[\%]$



“bare muons”: no  $\gamma$  recombination

↪ collinear  $\mu$  and  $\gamma$  assumed separable

↪ mass-singular corrections  $\propto \alpha \ln m_\mu$

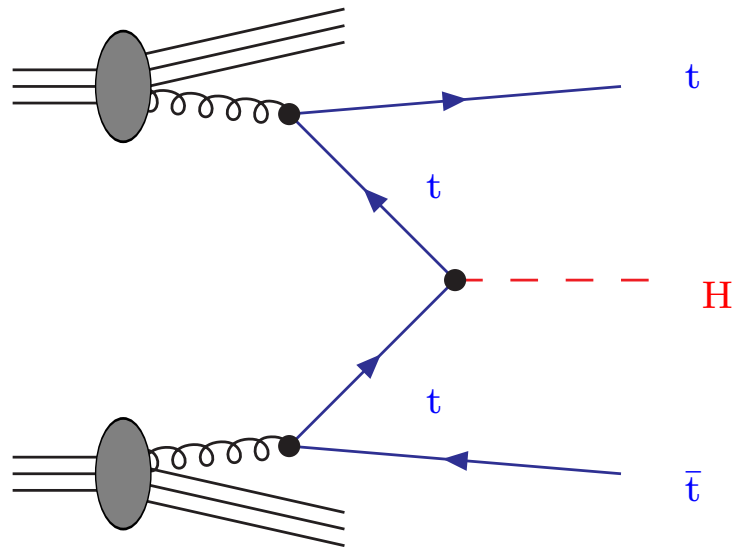
“rec”: recombination of collinear  $\gamma$

↪ collinear  $\mu\gamma = \widetilde{\mu\gamma}$  quasiparticle

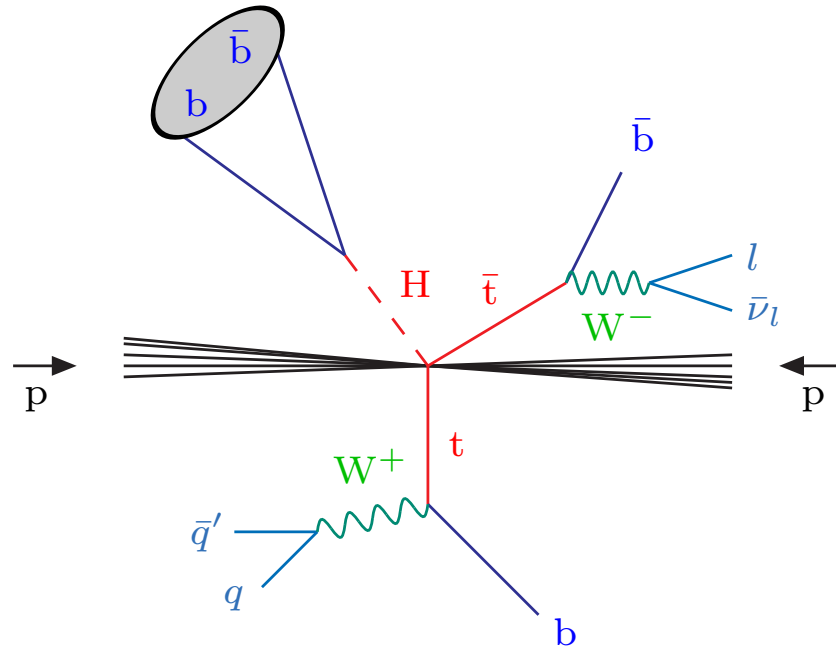
↪ no mass-singular corrections

↪ EW corrections mostly of non-universal origin (not simply FSR!)

## Higgs production in association with $t\bar{t}$ pairs



## Idea under discussion: highly boosted “fat jets”



$\hookrightarrow$  **fat jet** containing  $b\bar{b}$  pair from high- $p_T$  Higgs Butterworth et al. '08; ATL-PHYS-PUB-2009-088 (successful in WH/ZH revival!)

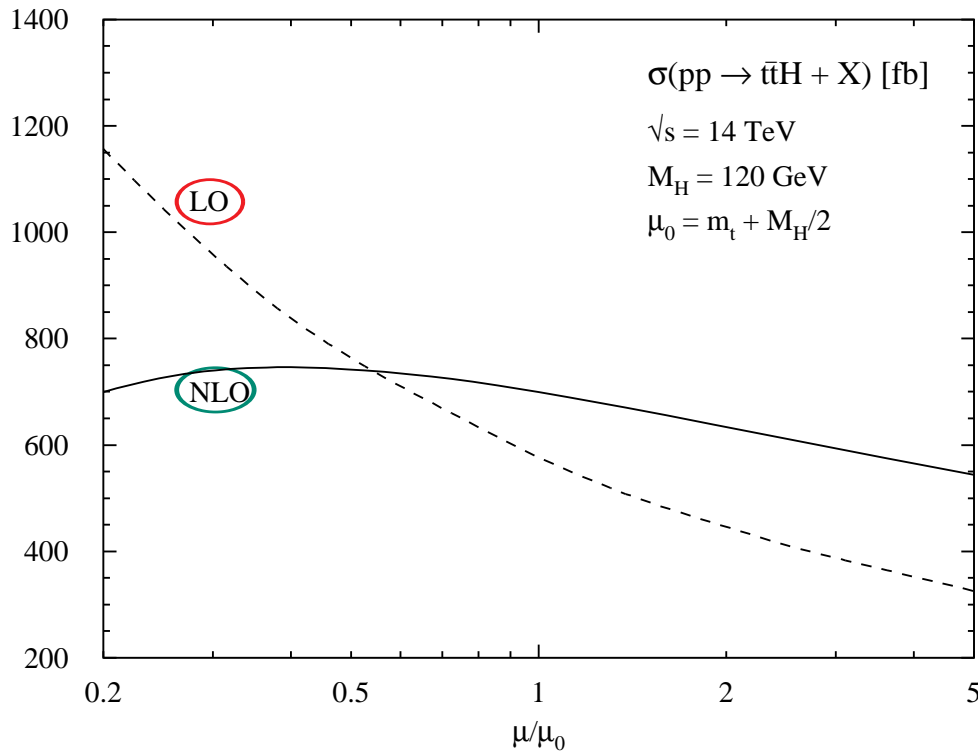
A theoretical study: Plehn, Salam, Spannowsky '09

- fat jets:  $p_T > 200 \text{ GeV}$  and  $R = 1.5$
- substructures:  $b\bar{b}$  pair with  $|m_{b\bar{b}} - M_H| < 10 \text{ GeV}$ , similar for  $t \rightarrow 3j$ , etc.
- $S/\sqrt{B}$  still  $\sim 2.2\text{--}2.6$  for  $\mathcal{L} = 30 \text{ fb}^{-1}$
- $S/B$  raised from  $\sim 0.1$  to  $0.2\text{--}0.4$
- background mainly due to  $t\bar{t}b\bar{b}$  (suppression of  $t\bar{t} + 2\text{jets}$ )

# Scale dependence of cross sections at the LHC

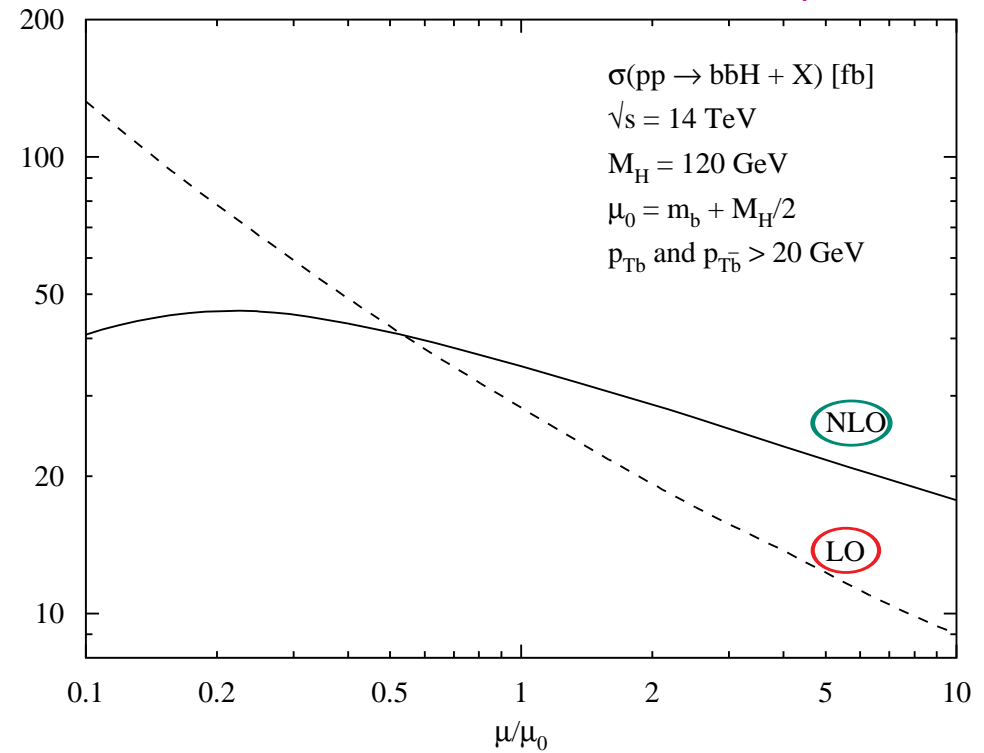
...for  $t\bar{t}H$  production:

Beenakker et al. '03



...for  $b\bar{b}H$  production:

S.D., Krämer, Spira '03



Drastic reduction of scale uncertainty in **LO** ( $\sim 100\%$ )  $\rightarrow$  **NLO** ( $\sim 10-20\%$ )

**Note:** both both b's of  $b\bar{b}H$  tagged at  $p_T > 20$  GeV, otherwise scale dependence larger!

Similar results by

Dawson, Orr, Reina, Wackerth '02; Wu et al. '05 (ttH) and

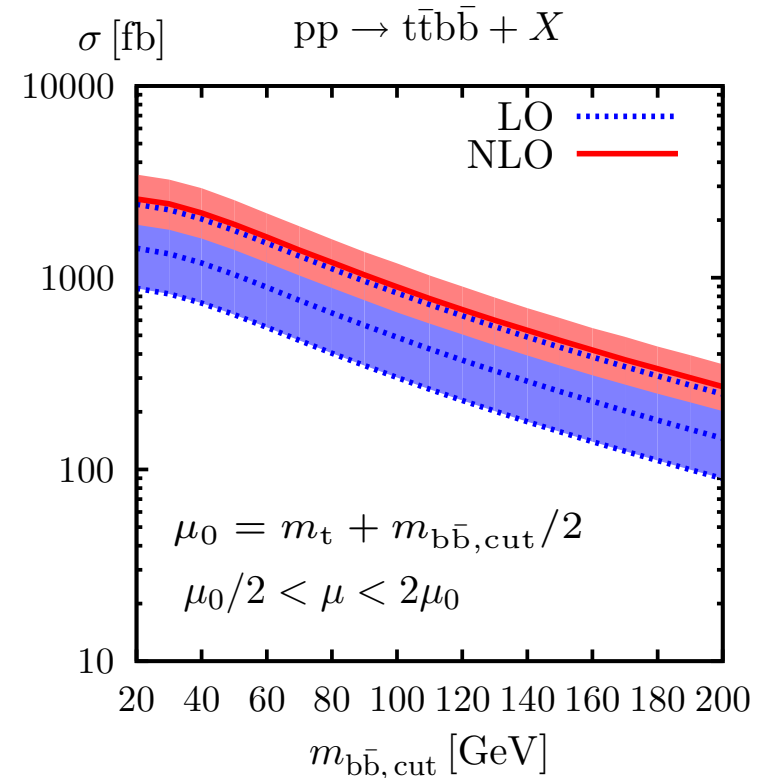
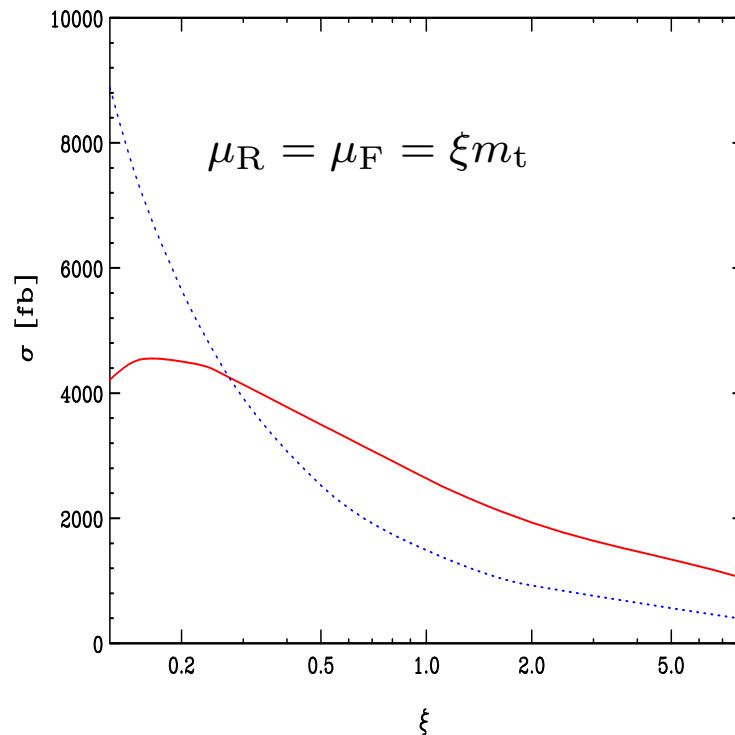
Dawson, Jackson, Reina, Wackerth '05 (bbH)



# Integrated cross section of $pp \rightarrow t\bar{t}b\bar{b} + X$ in NLO QCD

Bevilacqua, Czakon, Papadopoulos, Pittau, Worek '09

Bredenstein, Denner, S.D., Pozzorini '09



## Main results:

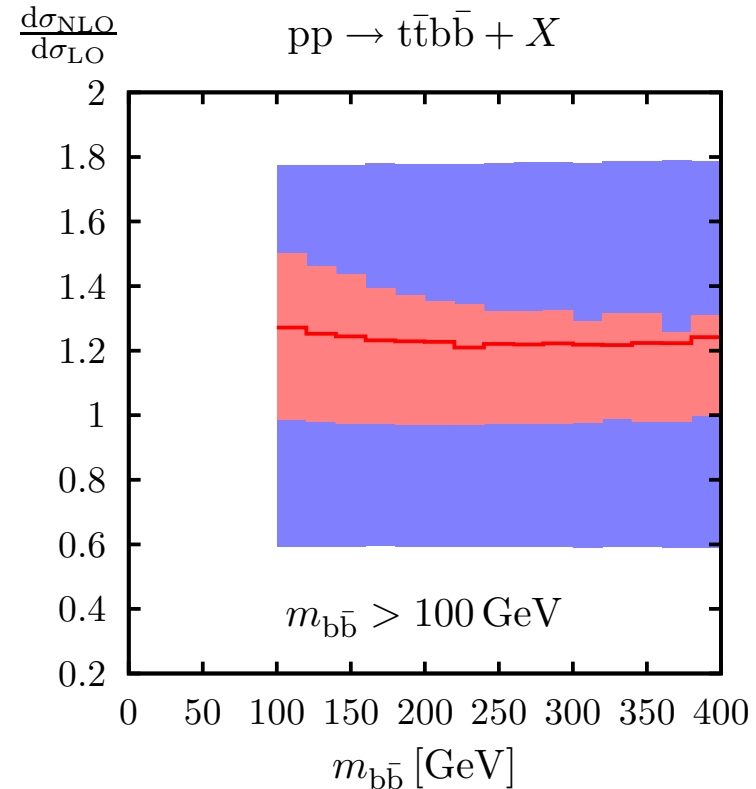
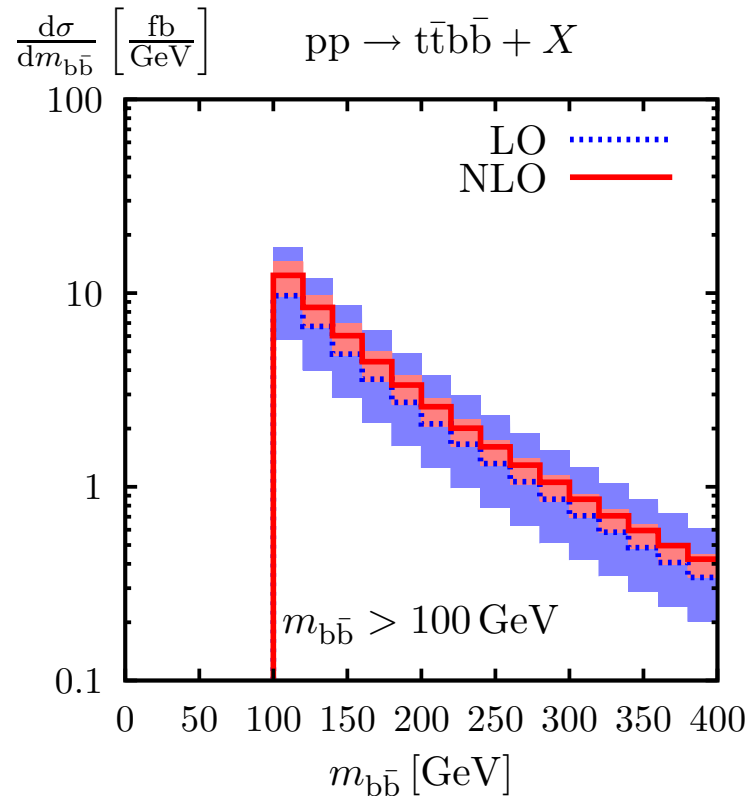
- results of the two groups agree
- correction very large at central scale  $\mu_{R/F} = m_t$ :  $K = 1.77$
- NLO scale dependence still large:  $\sim 33\%$  for  $\mu_0/2 < \mu_{R/F} < 2\mu_0$  ( $\sim 70\%$  at LO)

↪ further theoretical and/or phenomenological tricks necessary to stabilize analysis

## More results on $pp \rightarrow t\bar{t}b\bar{b} + X$

- Improvements on scale choice and selection cuts:

Bredenstein, Denner,  
S.D., Pozzorini '09



$\hookrightarrow$  reduced  $K$  factor  $\sim 1.2$  and NLO scale dependence  $\sim 21\%$   
for new central scale  $\mu_0^2 = m_t \sqrt{p_{\text{T},b} p_{\text{T},\bar{b}}}$

- Another idea under discussion:

Butterworth et al. '08; ATL-PHYS-PUB-2009-088

**fat jets** containing  $b\bar{b}$  pairs from high- $p_{\text{T}}$  Higgs (successful in WH/ZH revival!)

$\hookrightarrow$  better background suppression

Plehn, Salam, Spannowsky '09