

20 years of DIS @HERA - June 19th, 2012

The spin-momentum structure of the nucleon

--highlights from the  hermes collaboration--

20 years ago ...



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- first DIS events at H1 and Zeus



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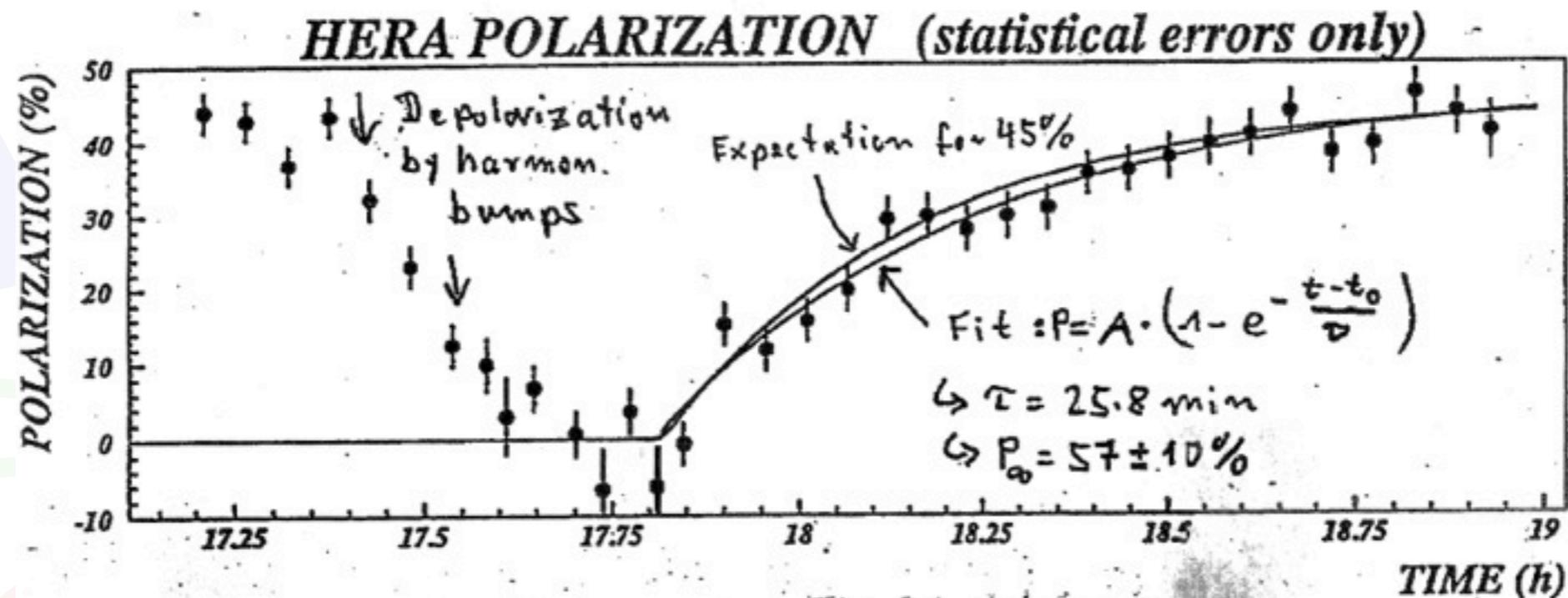


Fig. 4: Observation of rise-time at $E = 26.71 \text{ GeV}$.

- demonstration of lepton polarization at HERA under realistic running conditions



HERMES

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 - "Recommend the DESY directorate to approve HERMES"



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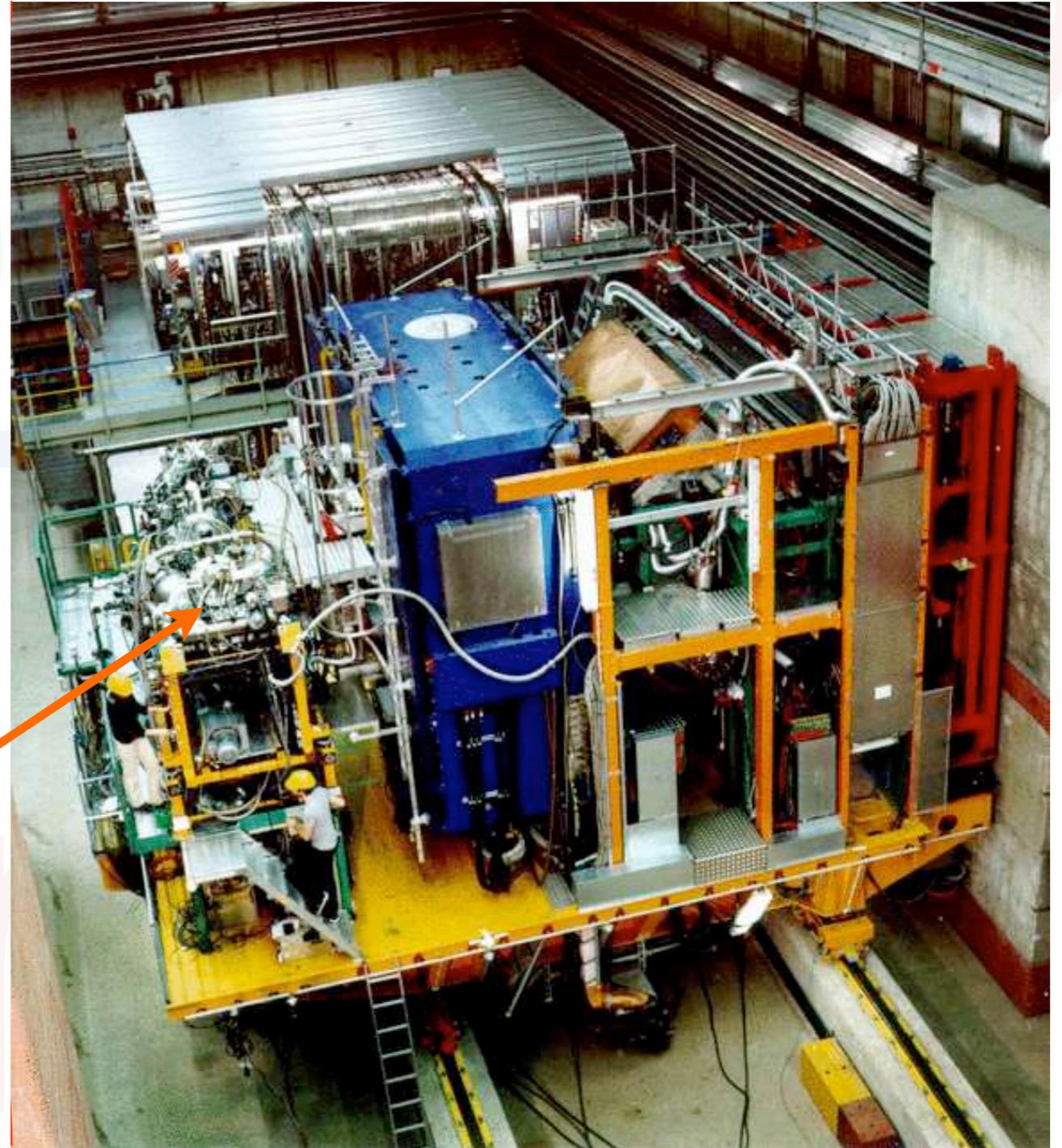
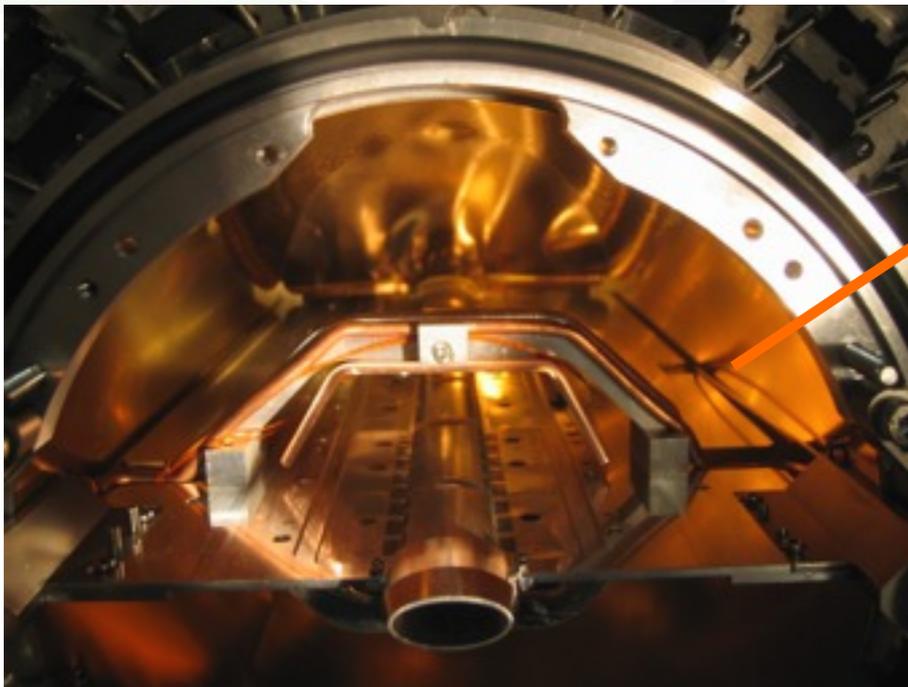
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- November 1992, Scientific Council
 - "Parallel running of ep and HERMES?"
- June 15, 1993
 - full approval of HERMES
- March 31, 1995
 - HERMES interlock set

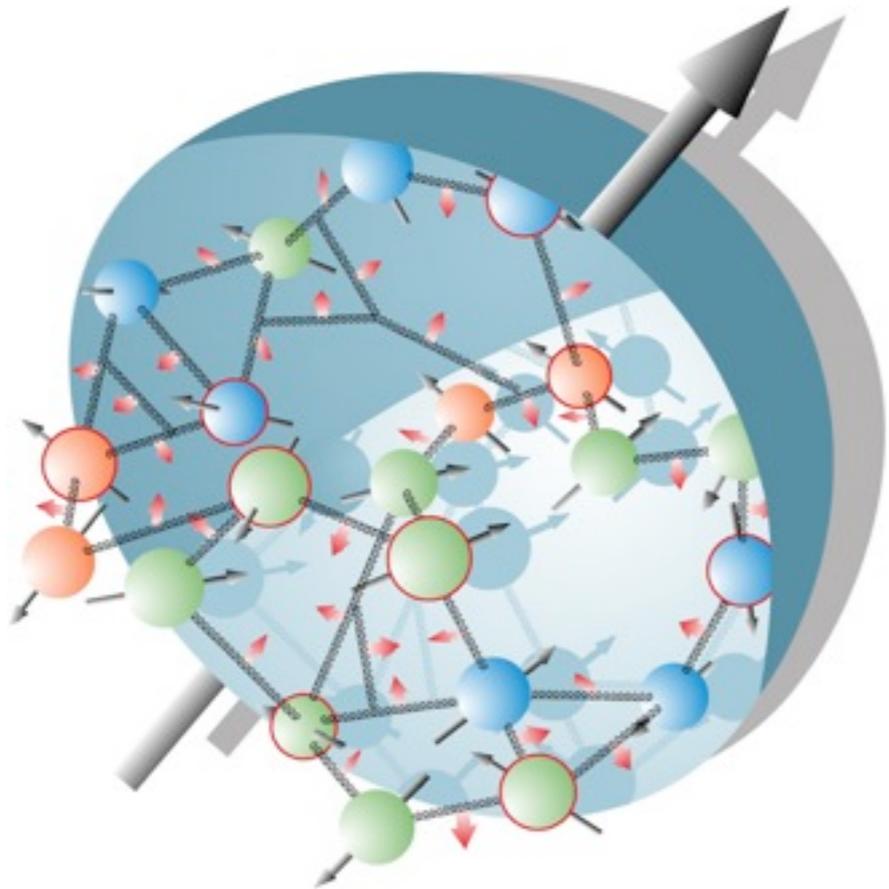
The HERMES experiment

pure gas targets:

- internal to lepton ring
- unpolarized (^1H ... Xe)
- longitudinally polarized: ^1H , ^2H
- transversely polarized: ^1H

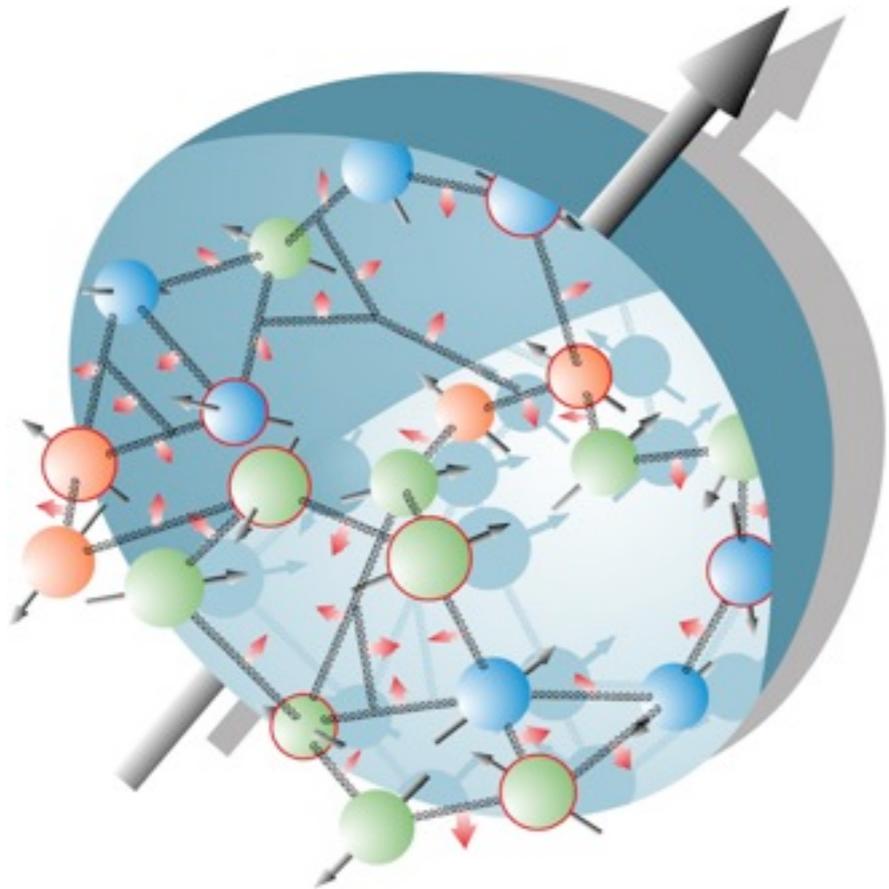


The HERA-I harvest



$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma \quad \leftarrow \text{quark spin}$$
$$+ \Delta G \quad \leftarrow \text{gluon spin}$$
$$+ L_q + L_g \quad \leftarrow \text{orbital angular momentum}$$

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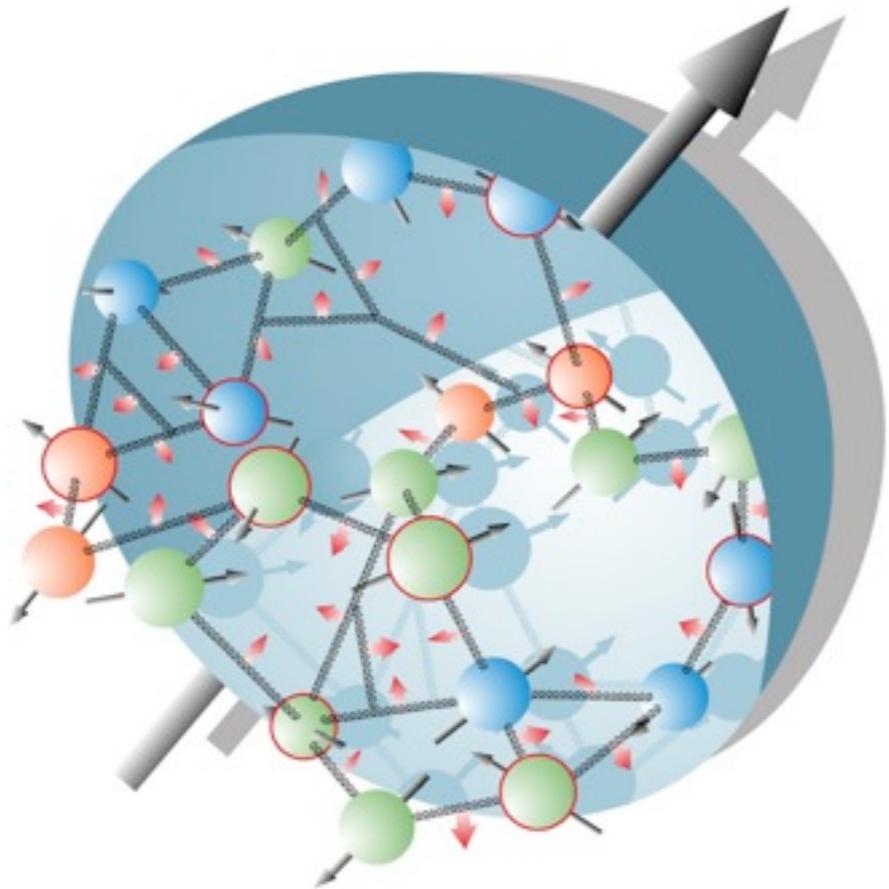
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PRD 75 (2007) 012007

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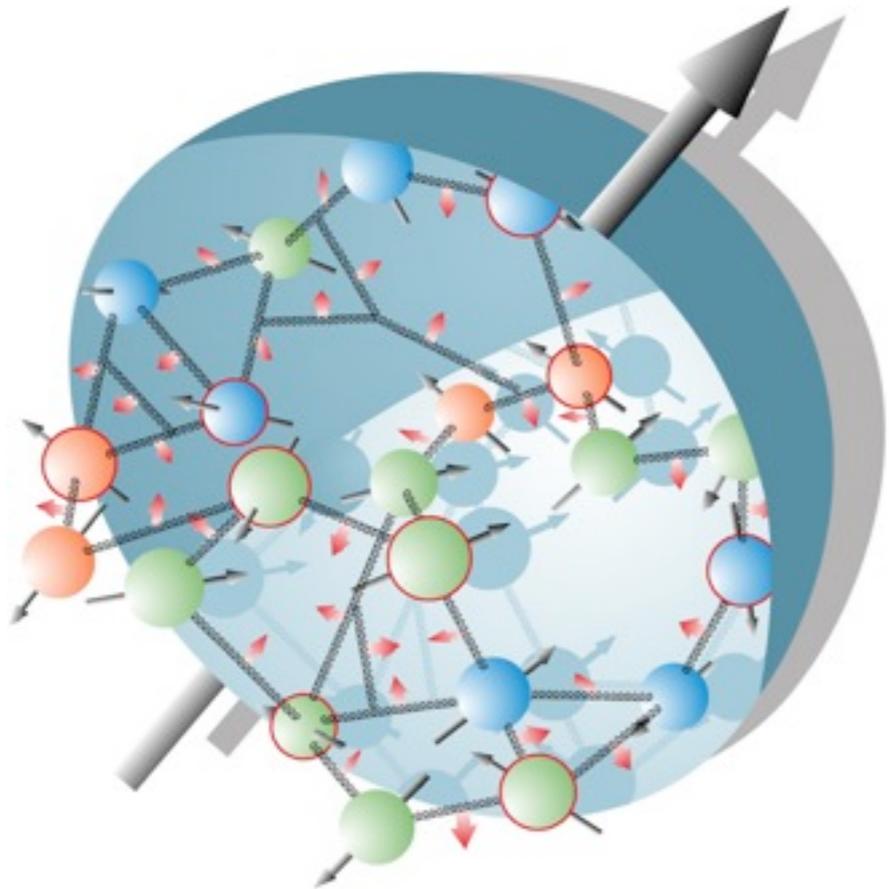
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$$\Delta G/G = 0.071 \pm 0.034 \text{ (stat)} \pm 0.010 \text{ (sys-exp)} \begin{matrix} +0.127 \\ -0.105 \end{matrix} \begin{matrix} \text{JHEP 1008 (2010) 130} \\ \text{(sys-model)} \end{matrix}$$

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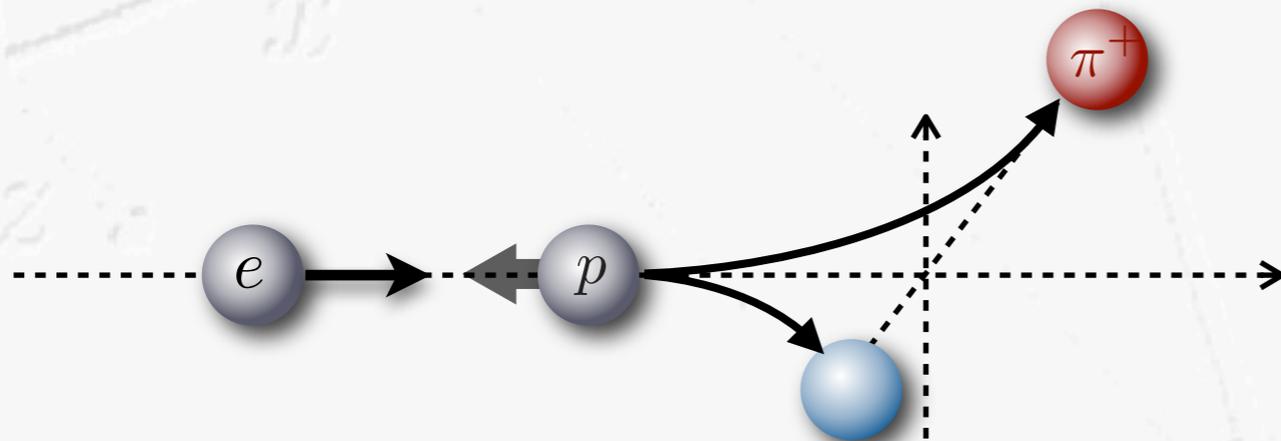
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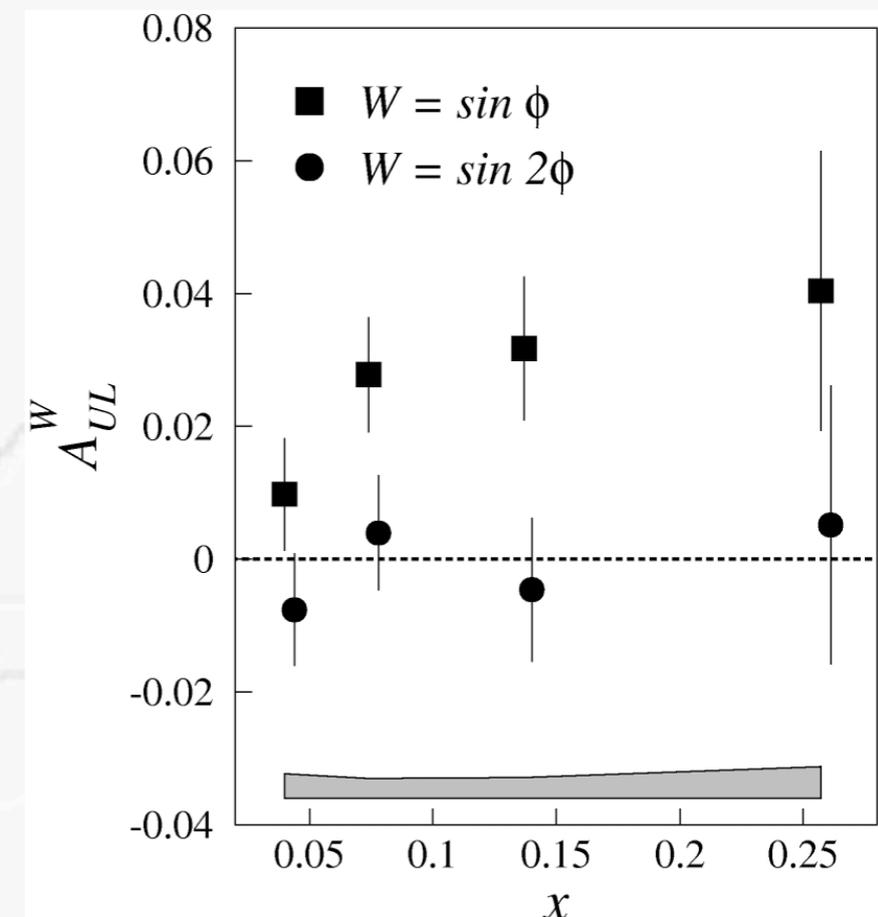
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... during the same time

- HERMES measures non-vanishing A_{UL} in semi-inclusive DIS [1]
- naive-T-odd - not expected from collinear pQCD
- transversity?
- disguised Sivers effect \rightarrow orbital angular momentum?

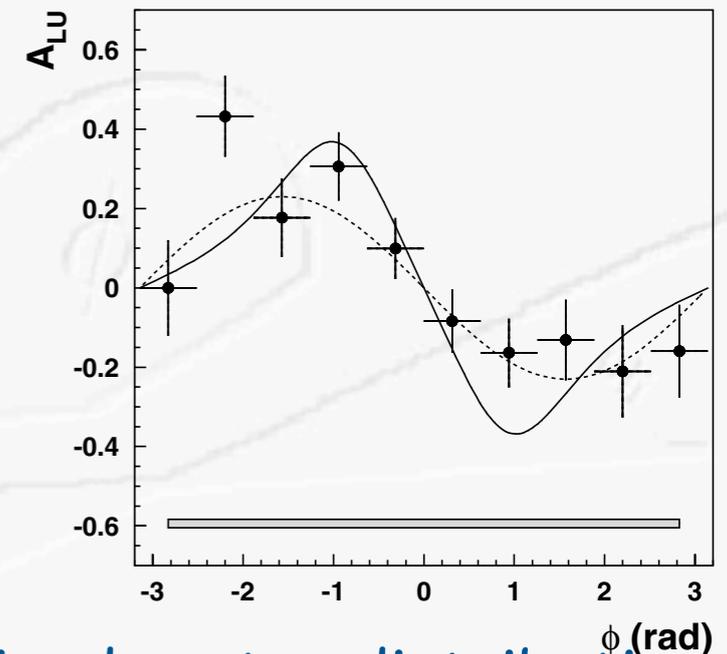


[1] PRL 84 (2000) 4047



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 - naive-T-odd - not expected from collinear pQCD
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- Ji (1997): relates moments of GPDs*) to total angular momentum
 - accessible in DVCS
 - HERMES measures A_{LU} in DVCS [2]



[1] PRL 84 (2000) 4047

[2] PRL 87 (2001) 182001

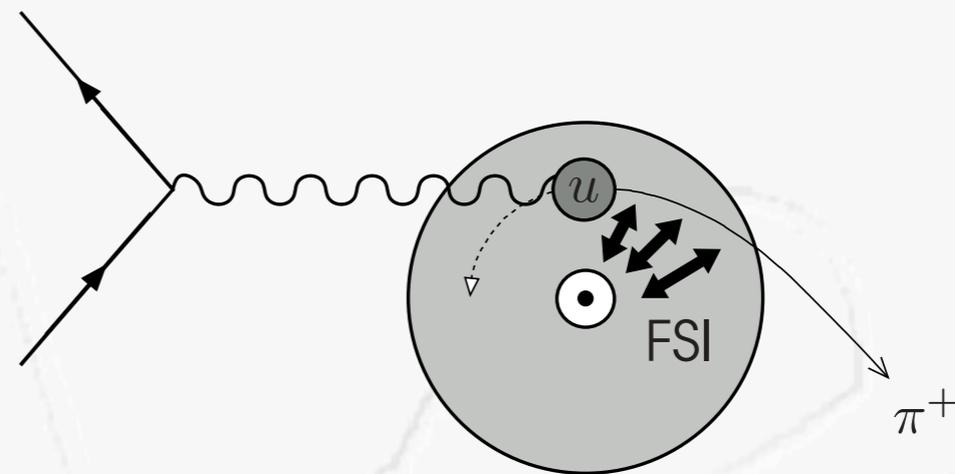
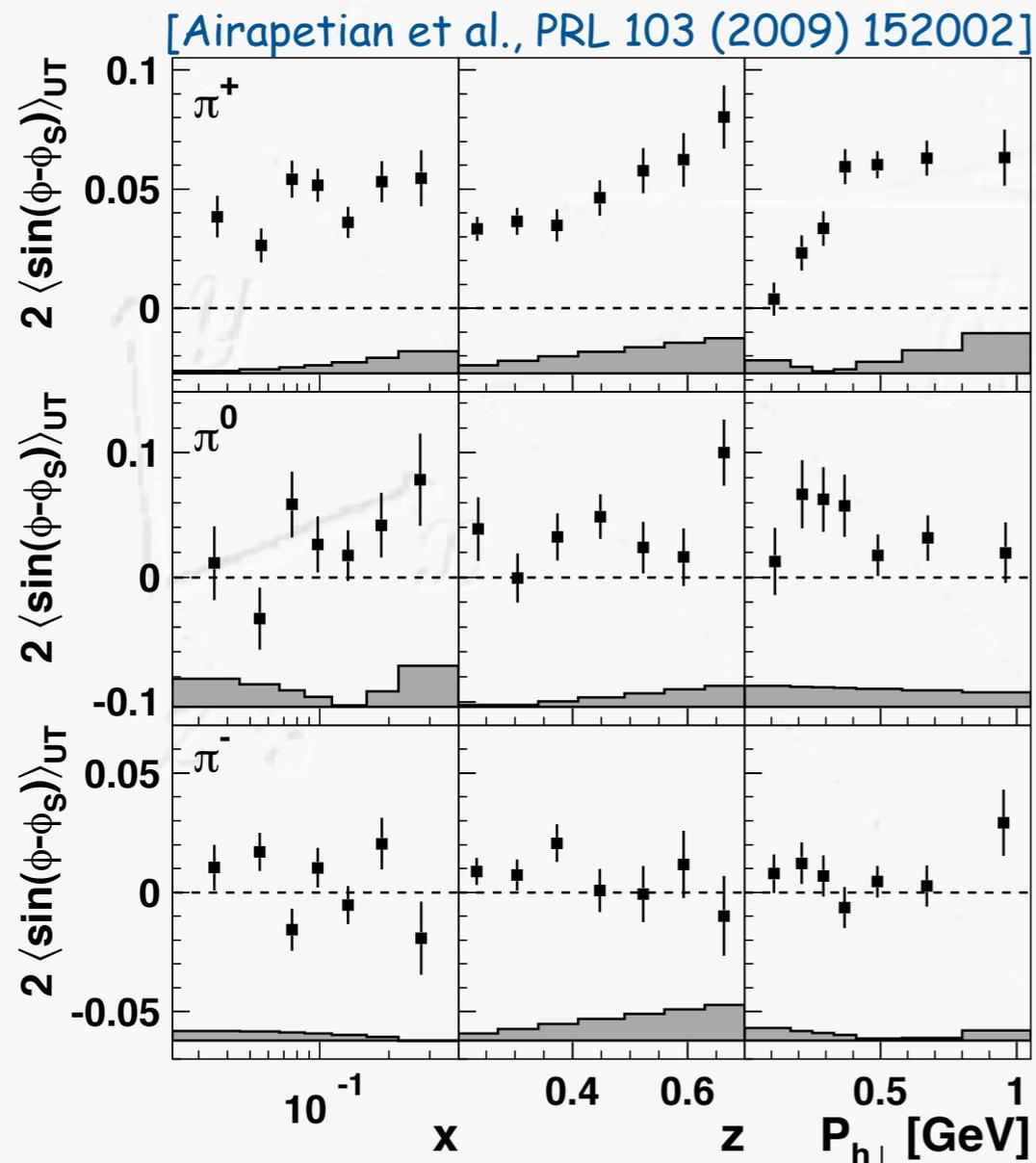
*) GPDs=generalized parton distributions

HERA II: transverse-target program



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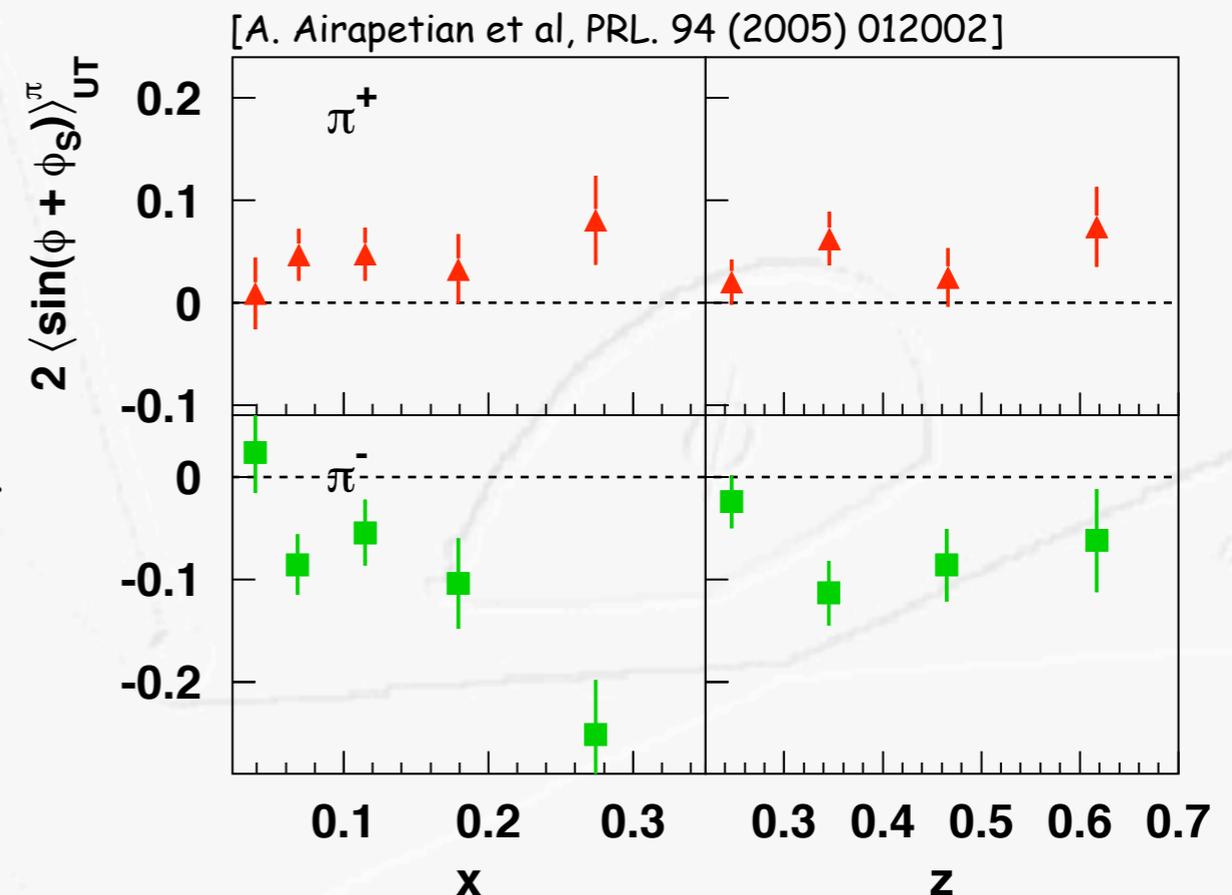
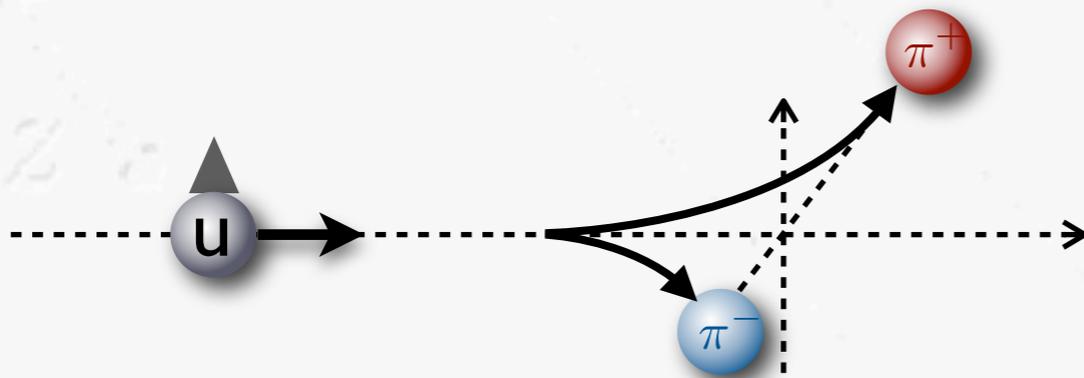
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[M. Burkardt, Phys. Rev. D66 (2002) 114005]

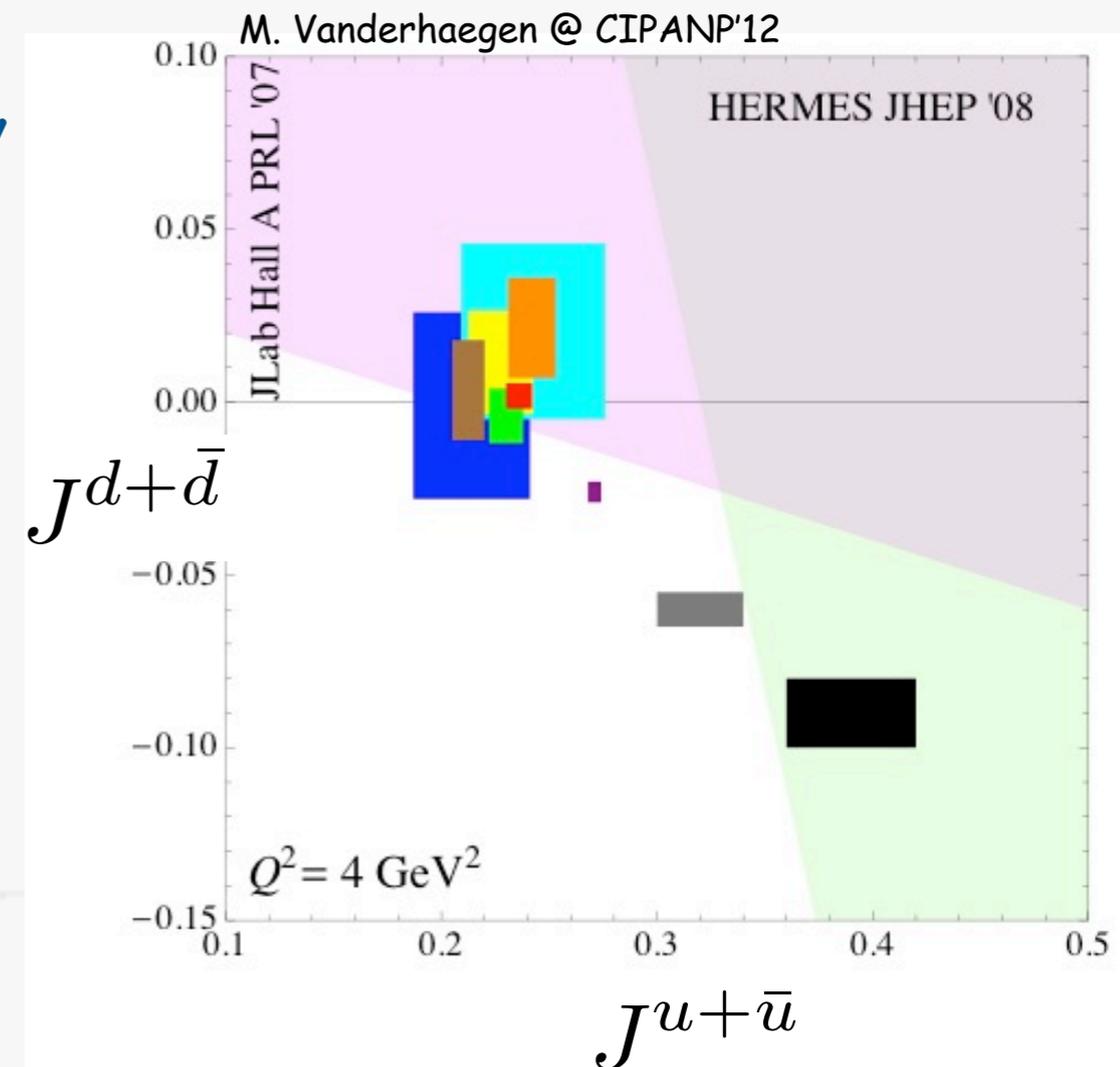
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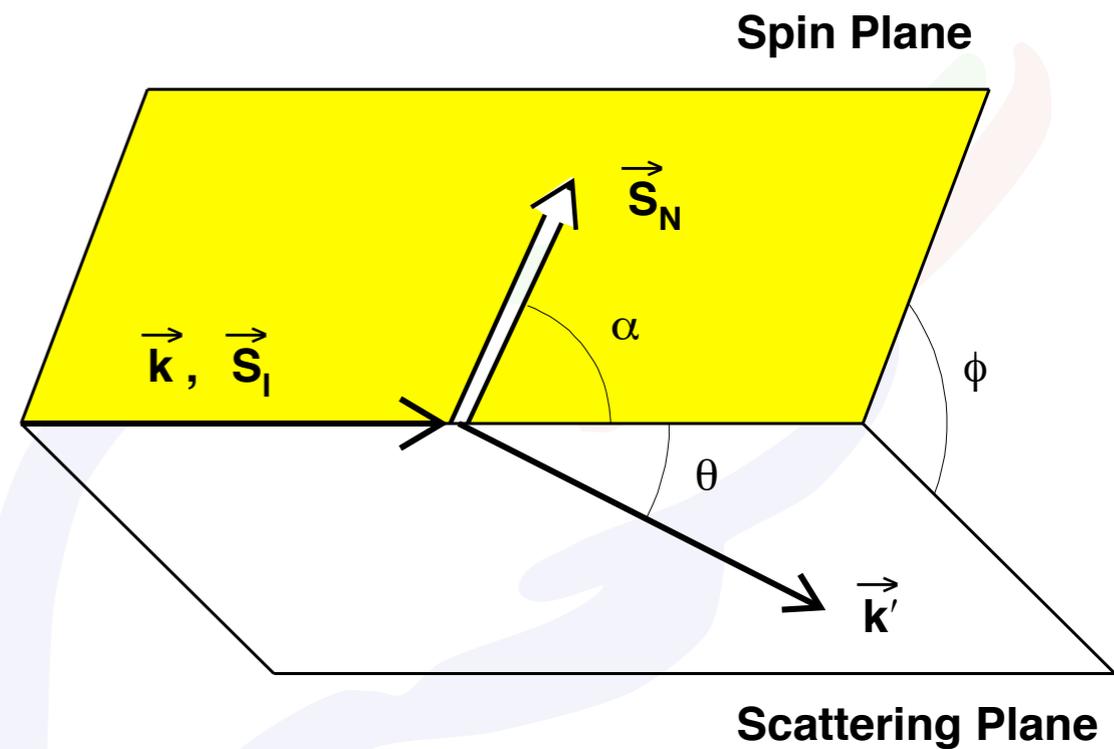


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- first attempts to constrain (in very model-dependent way) angular momentum of quarks via DVCS
- add one more piece to the structure-function landscape: g_2

Inclusive DIS

$$\frac{d^2\sigma(s, S)}{dx dQ^2} = \frac{2\pi\alpha^2 y^2}{Q^6} \mathbf{L}_{\mu\nu}(s) \mathbf{W}^{\mu\nu}(S)$$

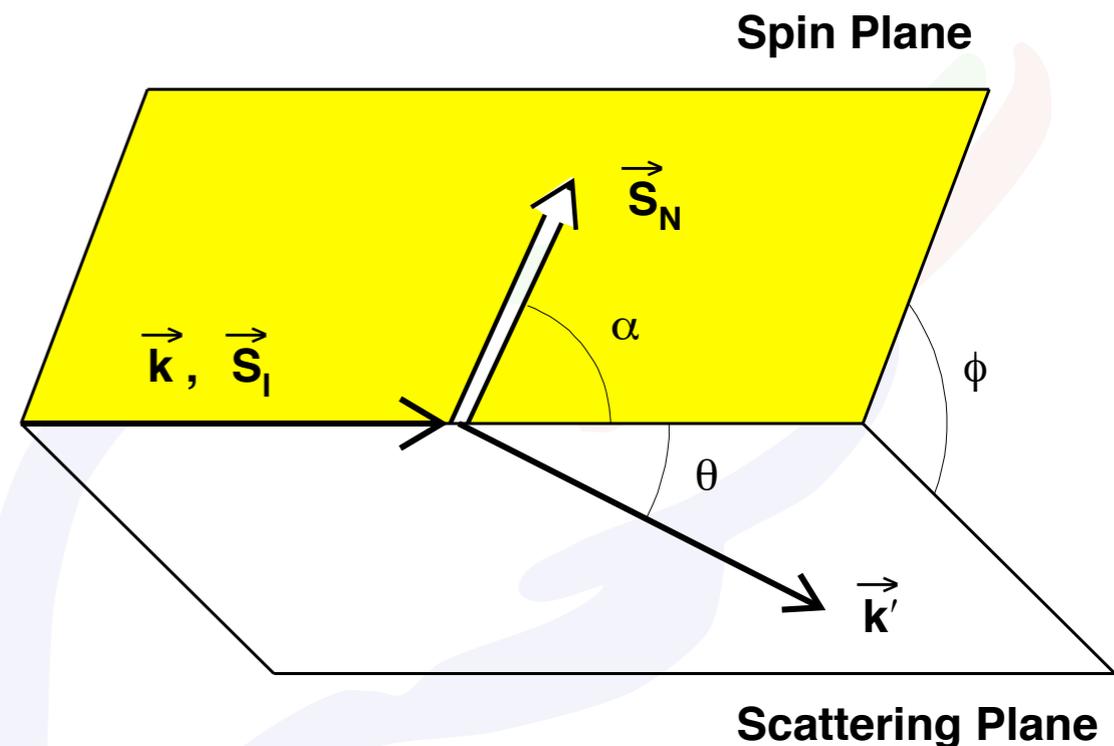


HERMES

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Lepton Tensor



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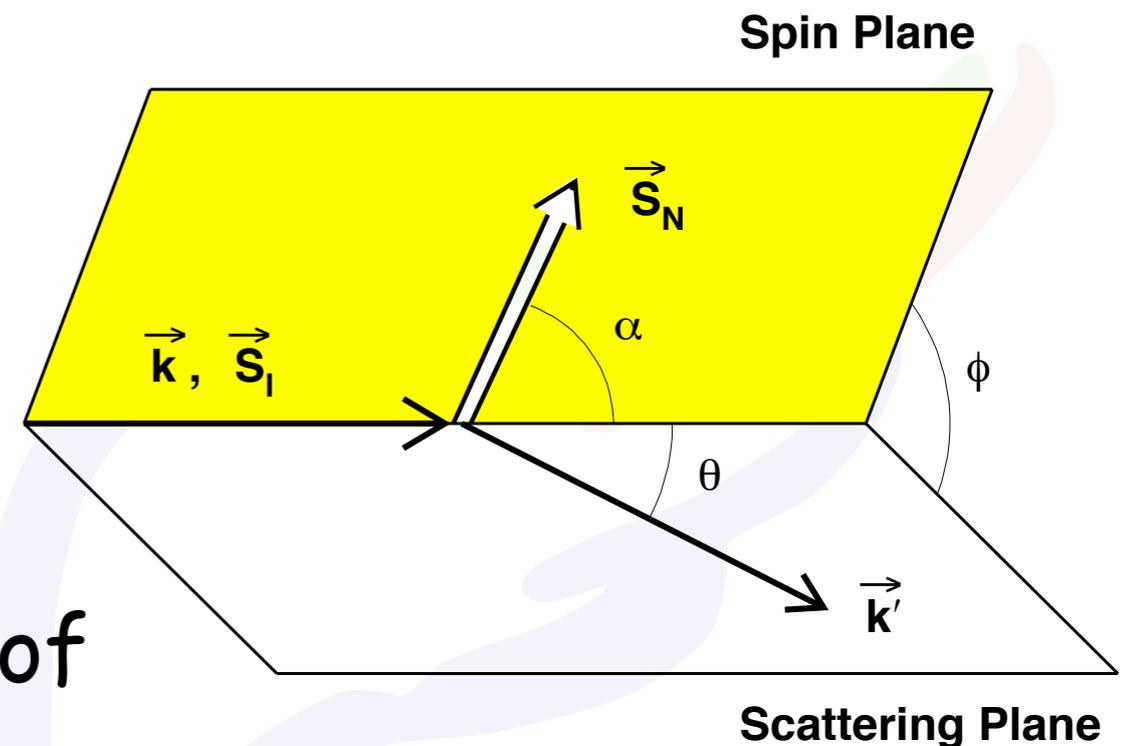
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Lepton Tensor

Hadron Tensor

parametrized in terms of

Structure Functions



Inclusive DIS

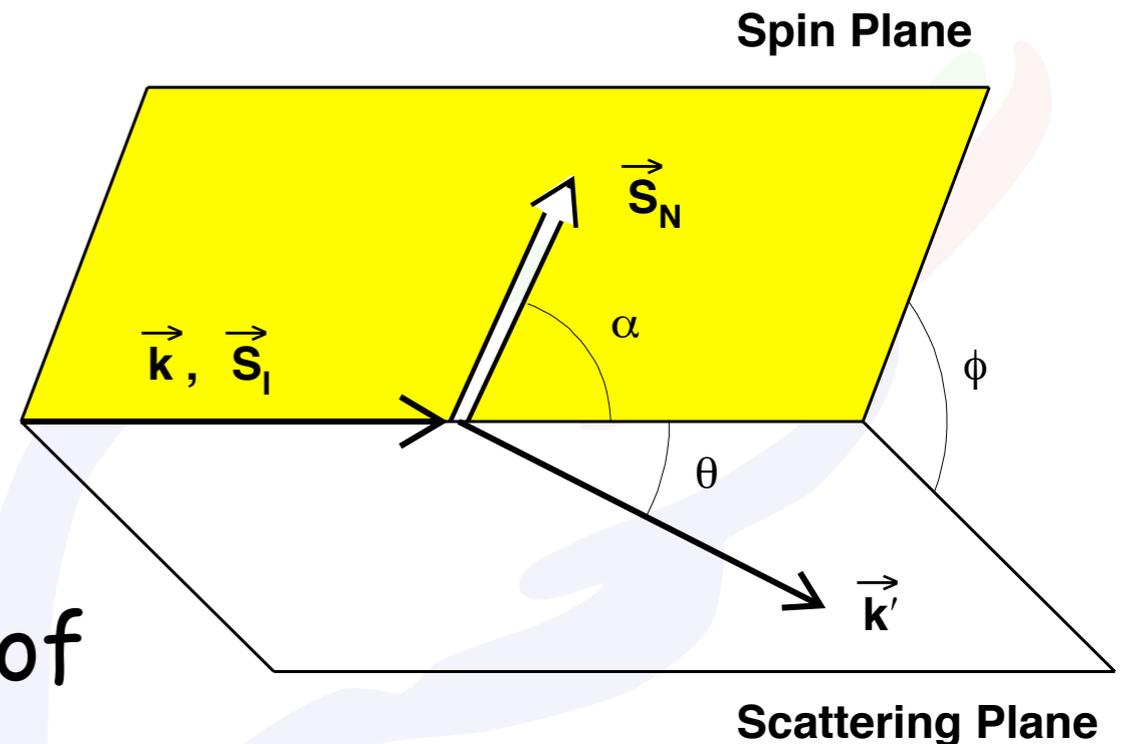
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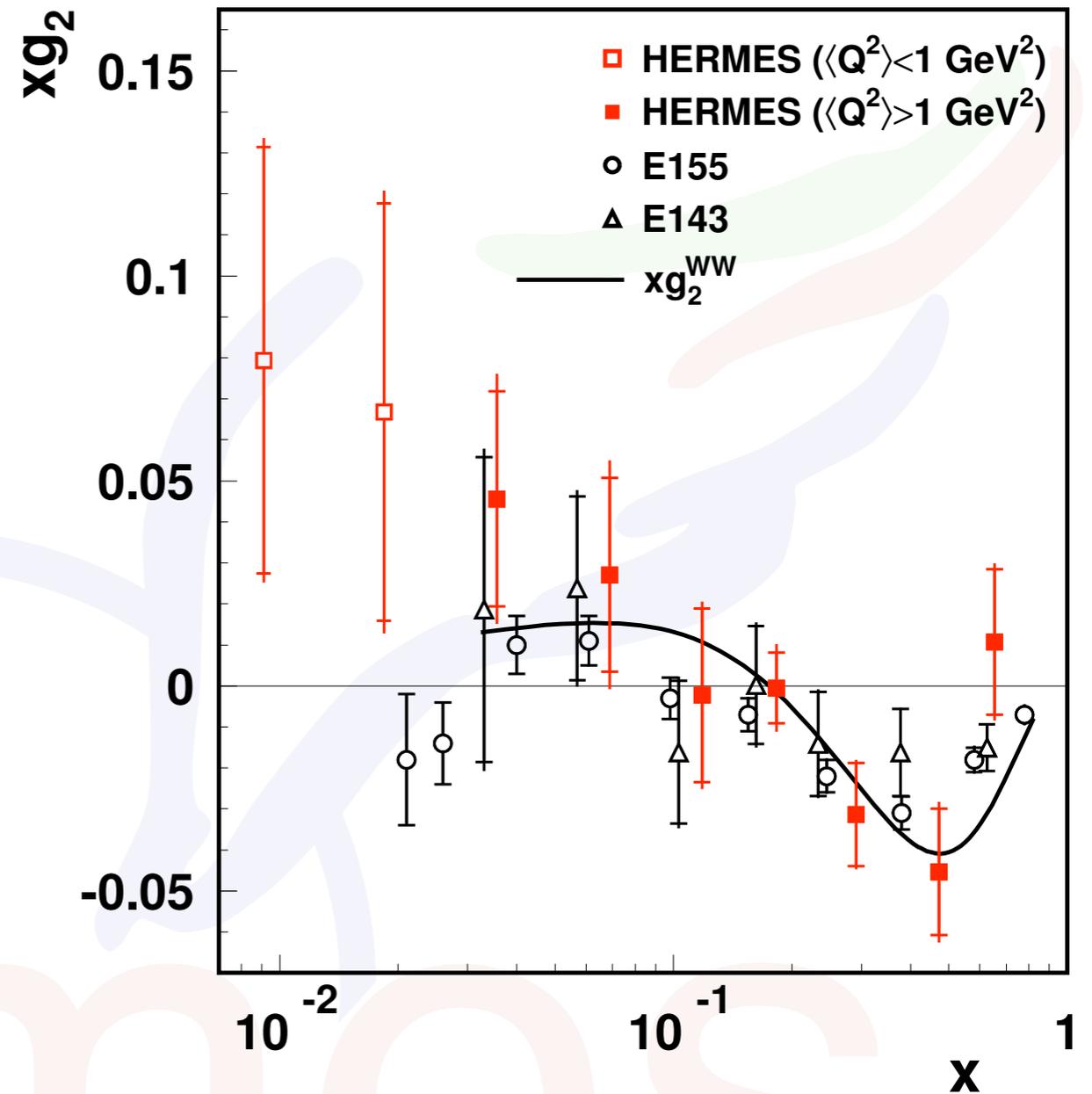
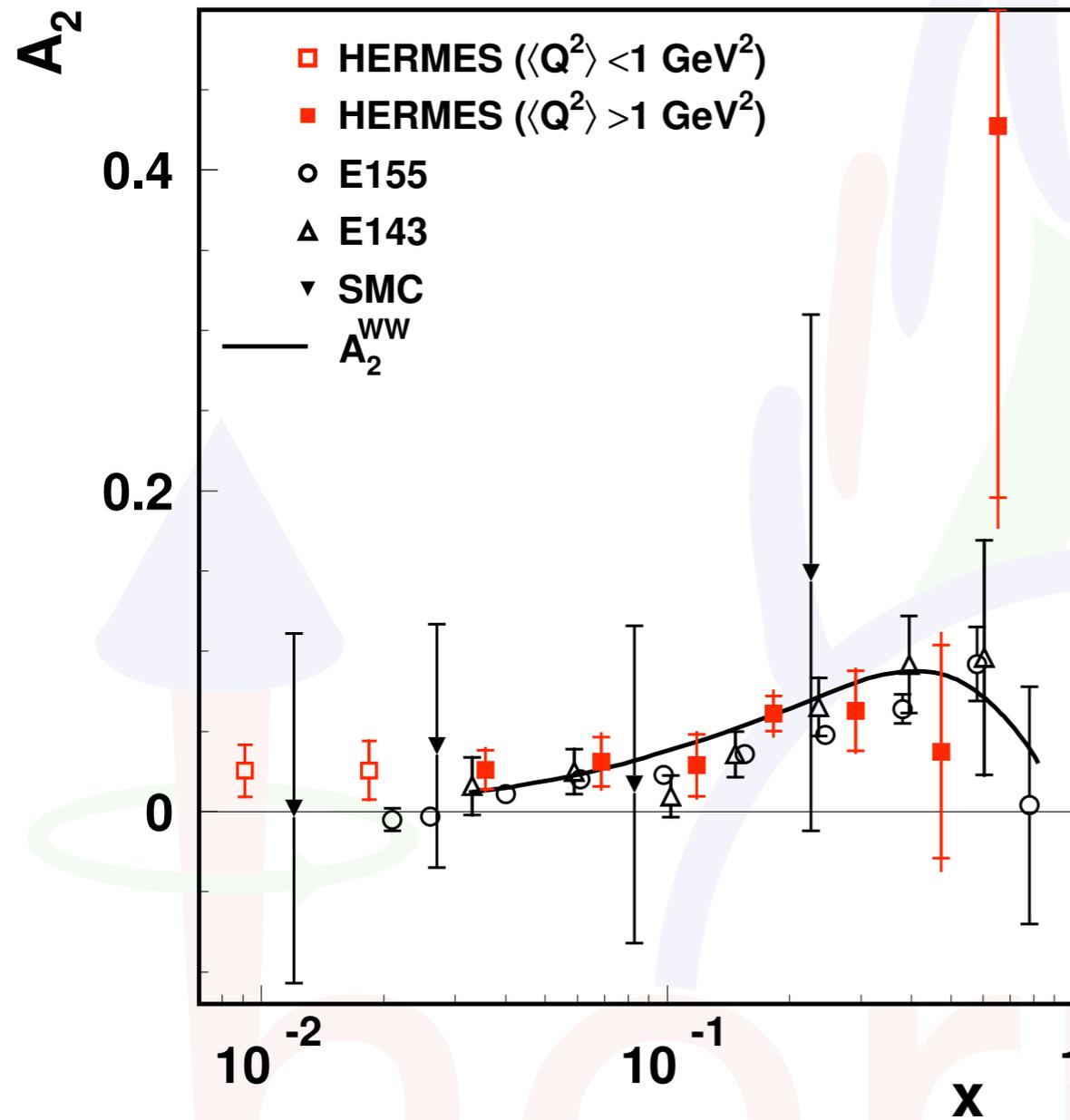
Structure Functions



$$\frac{d^3\sigma}{dx dy d\phi} \propto \frac{y}{2} F_1(x, Q^2) + \frac{1 - y - \gamma^2 y^2 / 4}{2xy} F_2(x, Q^2) - S_l S_N \cos \alpha \left[\left(1 - \frac{y}{2} - \frac{\gamma^2 y^2}{4} \right) g_1(x, Q^2) - \frac{\gamma^2 y}{2} g_2(x, Q^2) \right] + S_l S_N \sin \alpha \cos \phi \gamma \sqrt{1 - y - \frac{\gamma^2 y^2}{4}} \left(\frac{y}{2} g_1(x, Q^2) + g_2(x, Q^2) \right)$$

Results on A_2 and xg_2

A. Airapetian et al. [HERMES], EPJ C72 (2012) 1921



$$\int_{0.023}^{0.9} g_2(x, Q^2) dx = 0.006 \pm 0.024_{\text{stat}} \pm 0.017_{\text{syst}}$$

$$d_2(Q^2) \equiv 3 \int_0^1 x^2 \bar{g}_2(x, Q^2) dx = 0.0148 \pm 0.0096_{\text{stat}} \pm 0.0048_{\text{syst}}$$

... going 3D

Spin-Momentum Structure of the Nucleon

$$\frac{1}{2}\text{Tr}\left[(\gamma^+ + \lambda\gamma^+\gamma_5)\Phi\right] = \frac{1}{2}\left[f_1 + S^i\epsilon^{ij}k^j\frac{1}{m}f_{1T}^\perp + \lambda\Lambda g_1 + \lambda S^i k^i\frac{1}{m}g_{1T}\right]$$

$$\frac{1}{2}\text{Tr}\left[(\gamma^+ - s^j i\sigma^{+j}\gamma_5)\Phi\right] = \frac{1}{2}\left[f_1 + S^i\epsilon^{ij}k^j\frac{1}{m}f_{1T}^\perp + s^i\epsilon^{ij}k^j\frac{1}{m}h_1^\perp + s^i S^i h_1\right. \\ \left.+ s^i(2k^i k^j - \mathbf{k}^2\delta^{ij})S^j\frac{1}{2m^2}h_{1T}^\perp + \Lambda s^i k^i\frac{1}{m}h_{1L}^\perp\right]$$

quark pol.

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

nucleon pol.

- each TMD describes a particular spin-momentum correlation
- functions in black survive integration over transverse momentum
- functions in green box are chirally odd
- functions in red are naive T-odd

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helicity

quark pol.

nucleon pol.

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

Boer-Mulders

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pretzelosity

red are naive T-odd

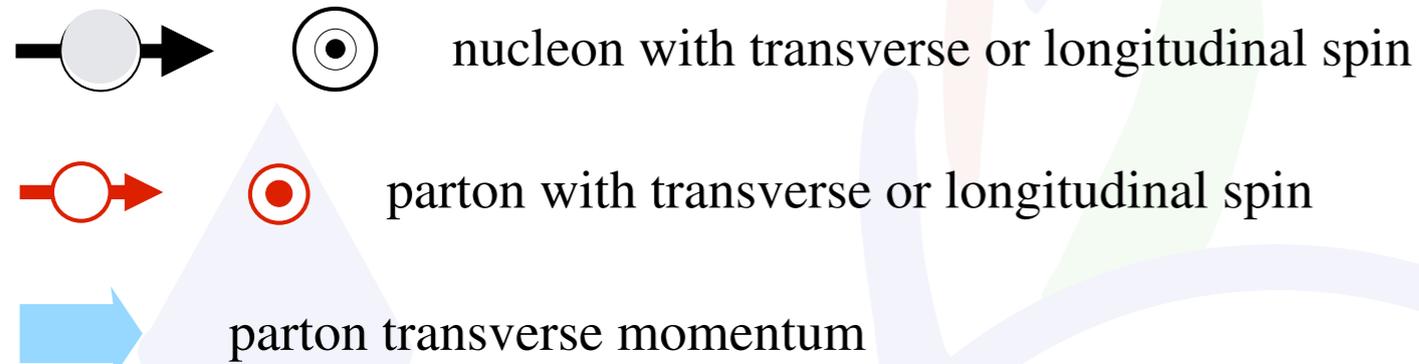
Sivers

transversity

worm-gear

Probabilistic interpretation

Proton goes out of the screen/
photon goes into the screen



[courtesy of A. Bacchetta, Pavia]

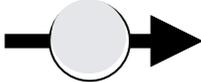
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$$g_1 = \text{[Diagram: circle with black dot and red dot in center]} - \text{[Diagram: circle with black dot and red cross in center]}$$

$$h_1 = \text{[Diagram: circle with red arrow pointing right]} - \text{[Diagram: circle with red arrow pointing left]}$$

Probabilistic interpretation

Proton goes out of the screen/
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  nucleon with transverse or longitudinal spin

  parton with transverse or longitudinal spin

 parton transverse momentum

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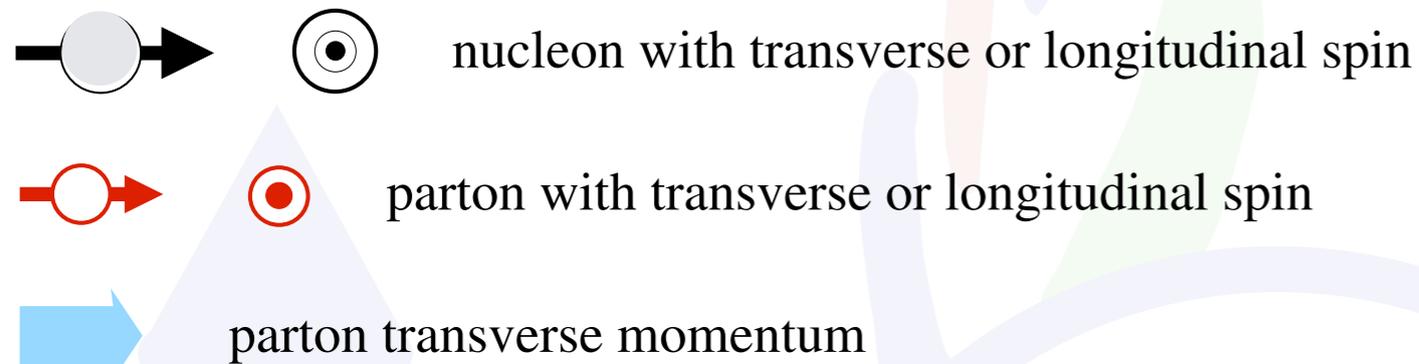
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$$h_1 = \text{[Diagram: circle with red dot and right arrow]} - \text{[Diagram: circle with red dot and left arrow]}$$

$$f_{1T}^\perp = \text{[Diagram: circle with red dot and blue down arrow]} - \text{[Diagram: circle with red dot and blue up arrow]}$$

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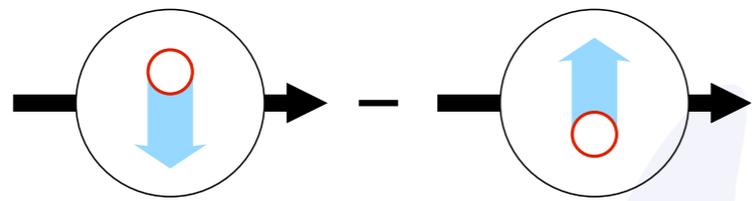
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$$f_{1T}^\perp = \text{[diagram: a circle with a red dot and a blue arrow pointing down]} - \text{[diagram: a circle with a red dot and a blue arrow pointing up]}$$

correlates transverse momentum & spin

$f_{1T}^\perp =$



Sivers function



$$f_{1T}^\perp = \text{---} \left(\begin{array}{c} \circ \\ \downarrow \\ \circ \end{array} \right) \rightarrow \text{---} \left(\begin{array}{c} \circ \\ \uparrow \\ \circ \end{array} \right) \rightarrow$$

Sivers function

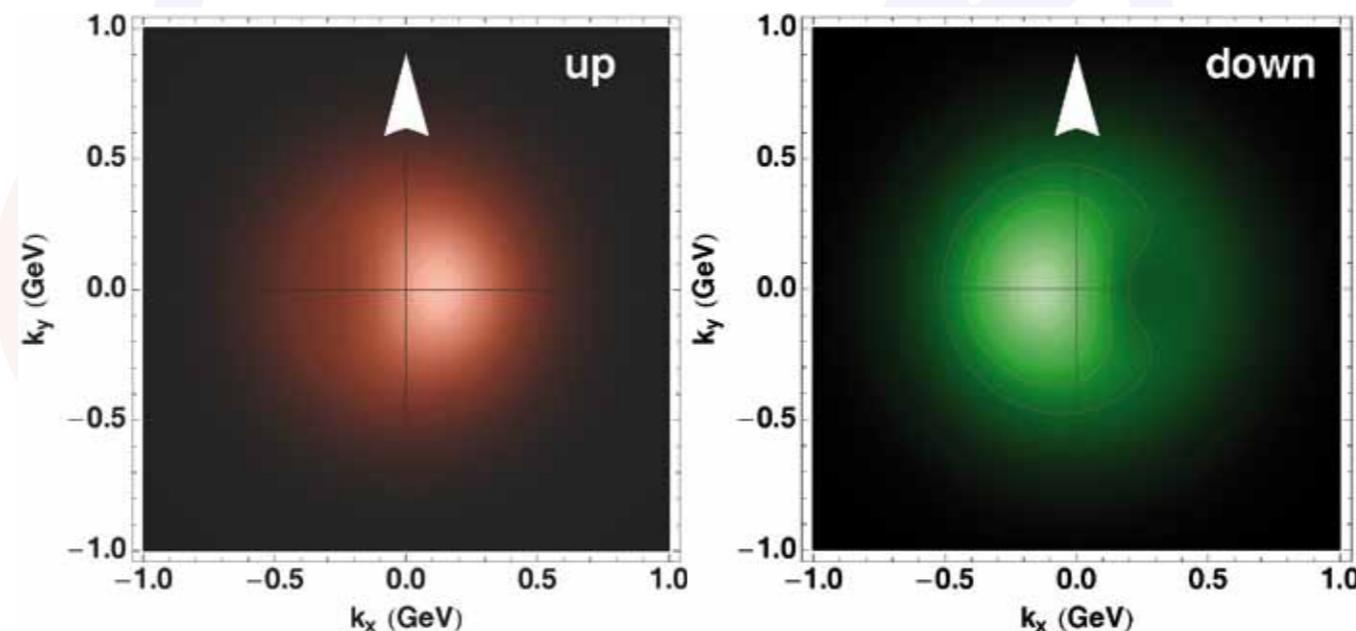
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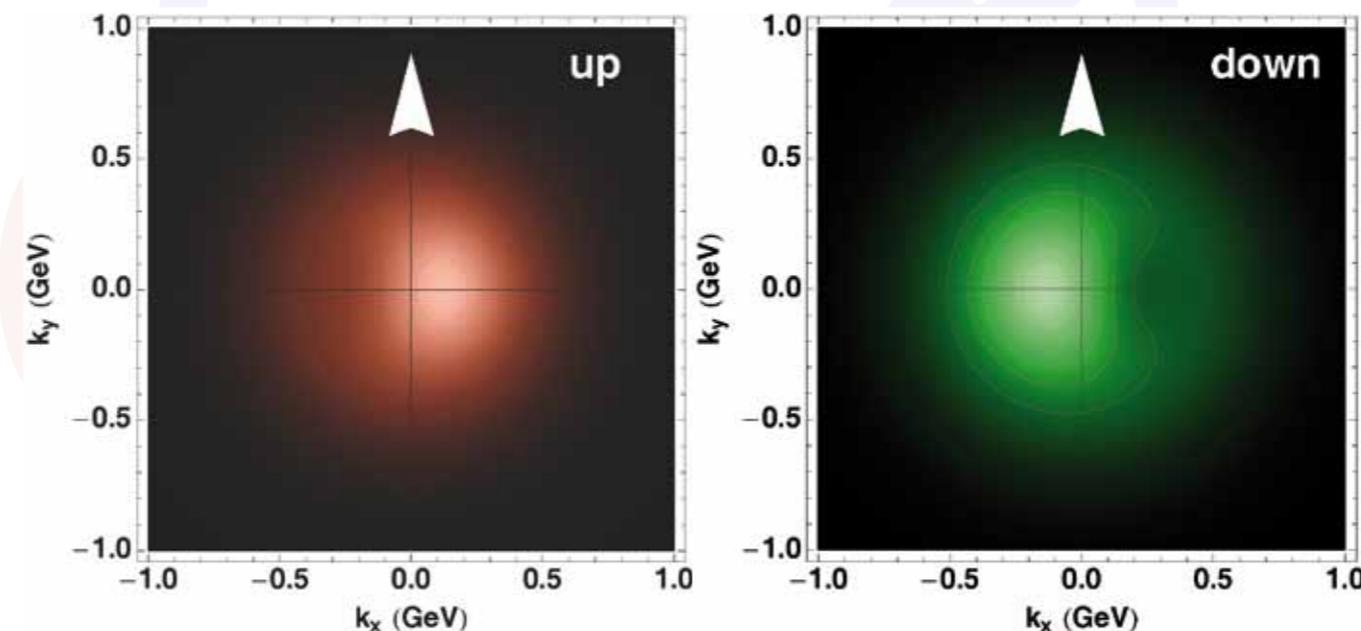


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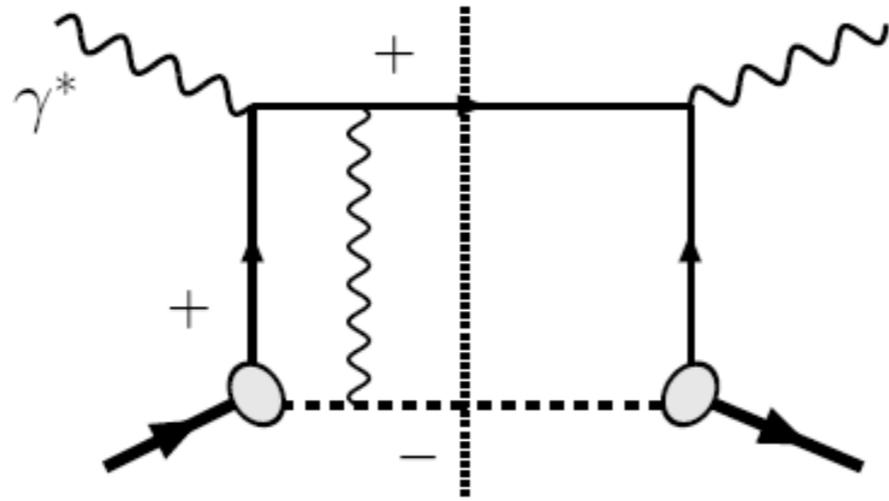
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- (naive) T-odd structure: $S_N \cdot (p_\perp \times P_N)$ -- requires ISI/FSI
- leads to peculiar calculable universality breaking (DIS vs. Drell-Yan)



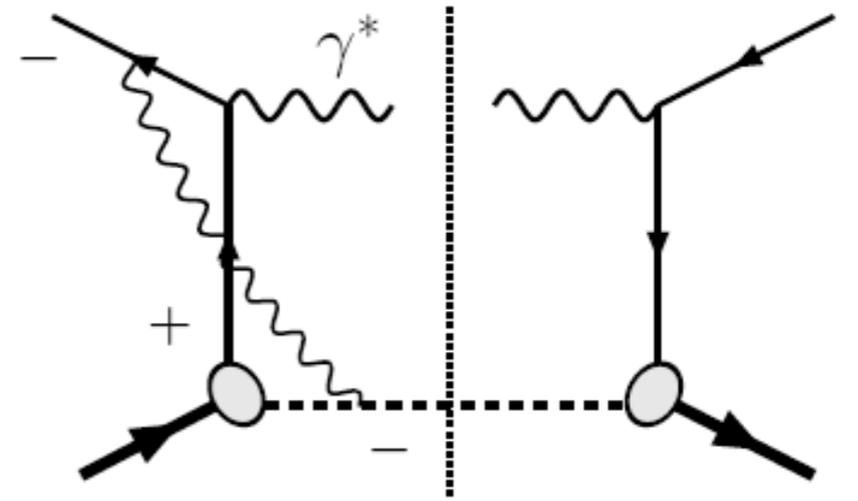
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Process dependence

simple QED
example



DIS: attractive



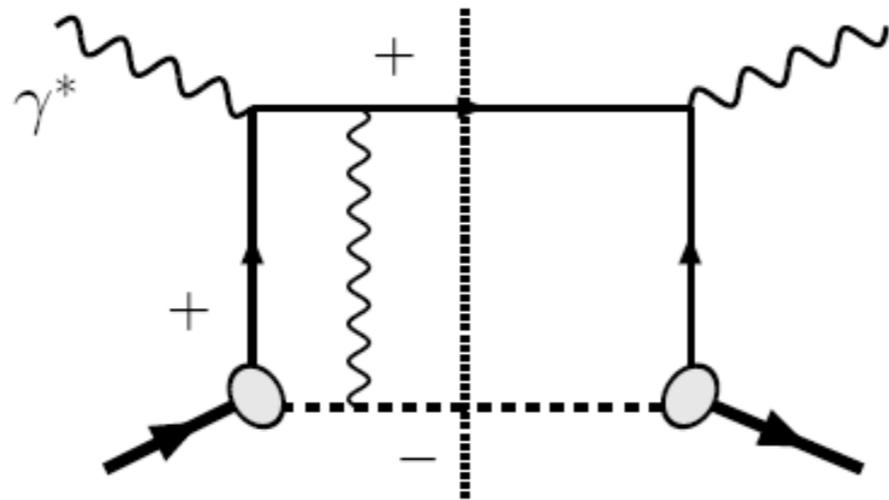
Drell-Yan: repulsive



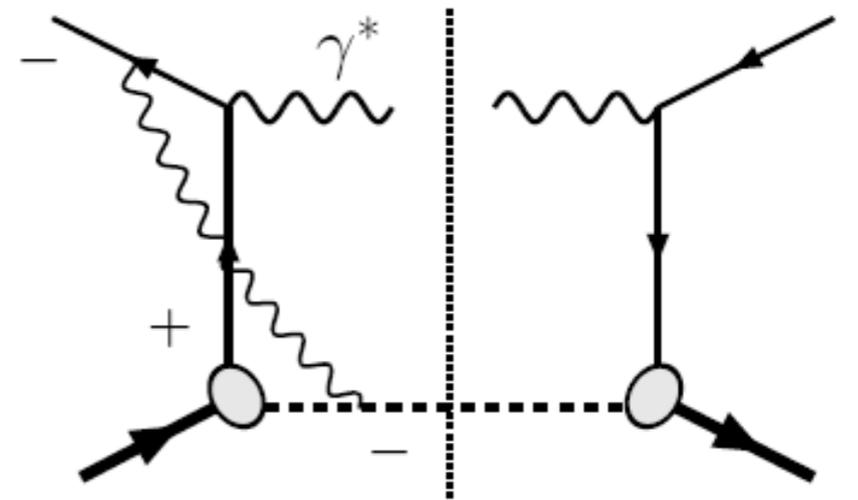
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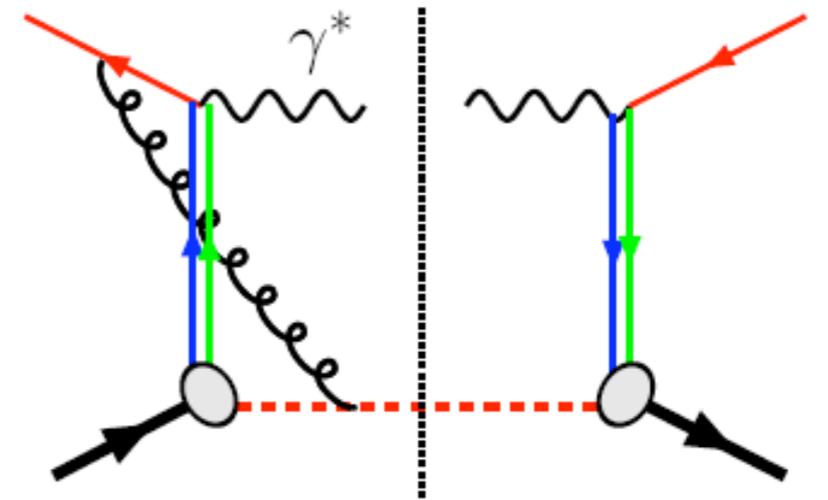
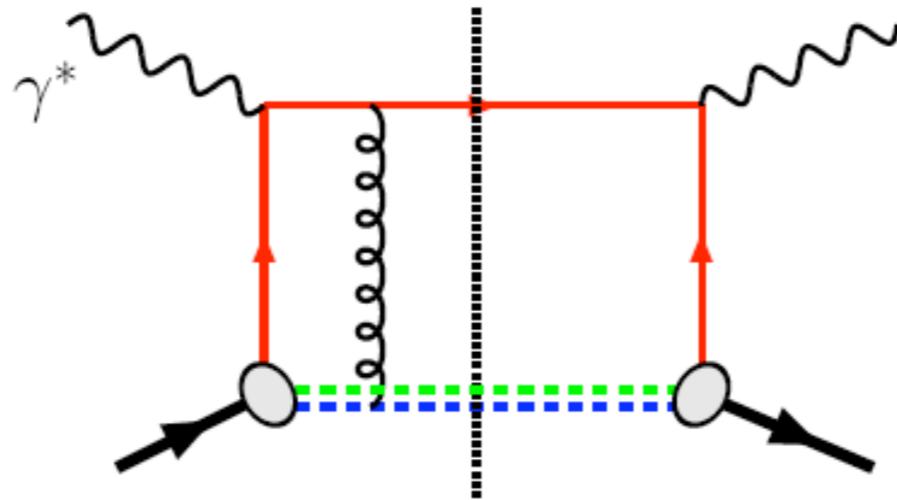


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Drell-Yan: repulsive

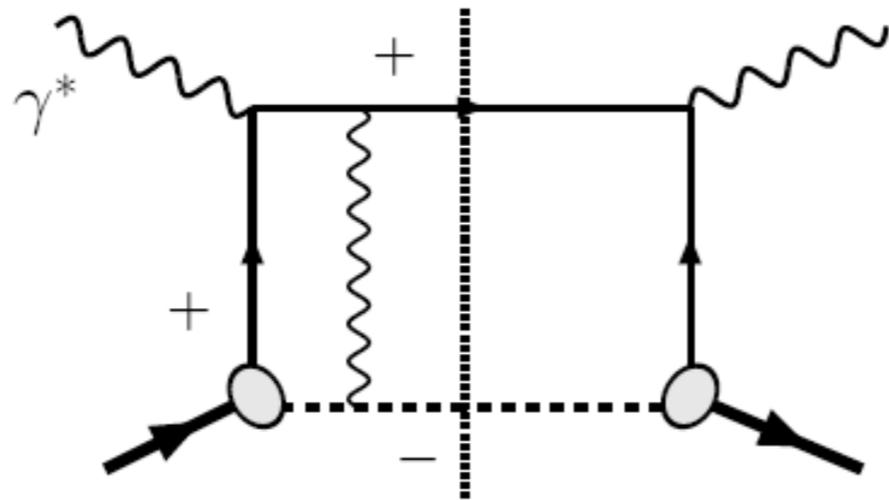
add color:
QCD



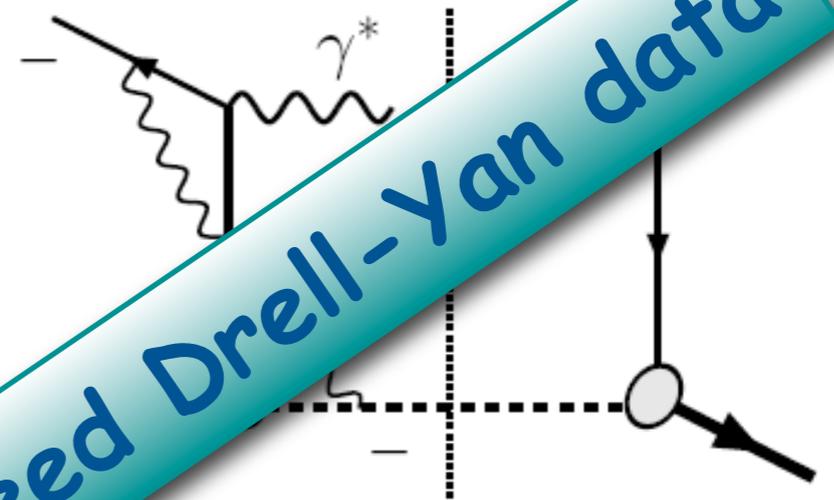
result: $\text{Sivers}|_{\text{DIS}} = - \text{Sivers}|_{\text{DY}}$

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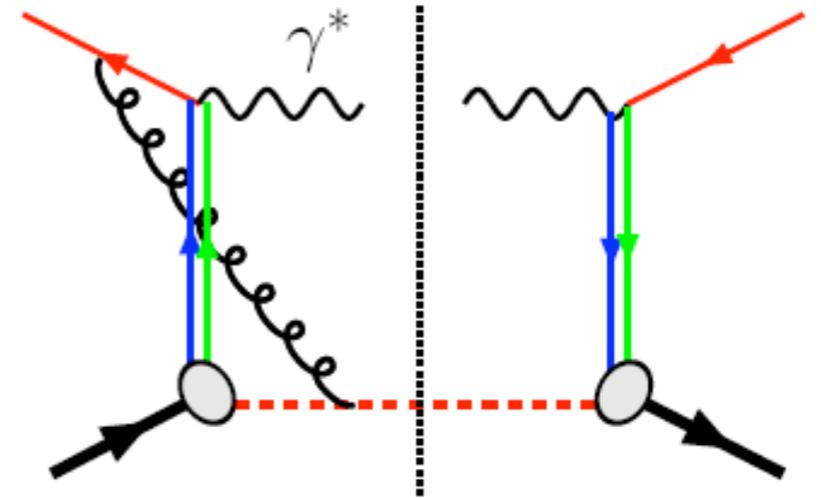
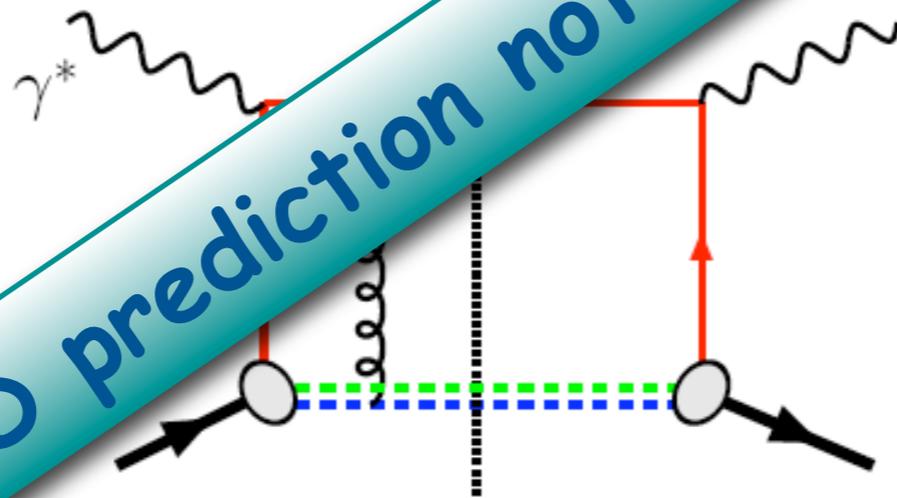


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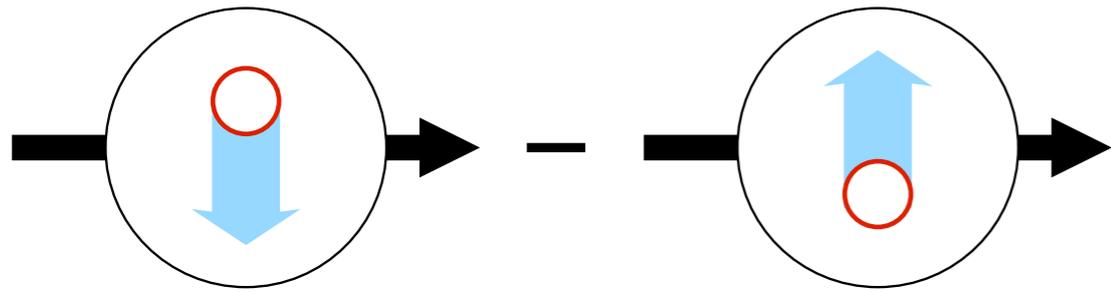


Drell-Yan: repulsive

add color:
QCD

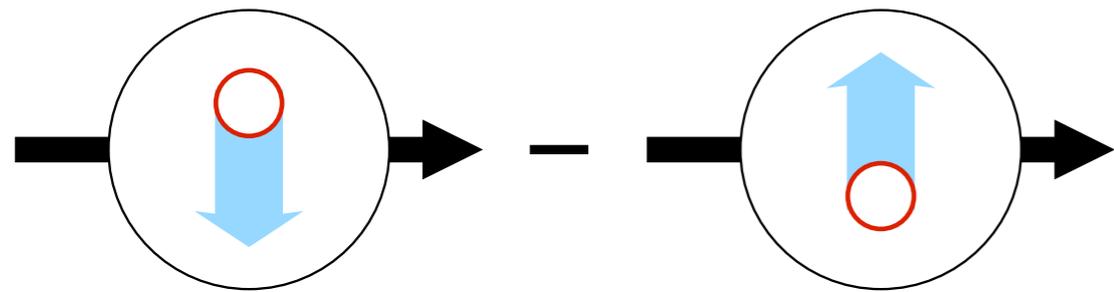


result: $Sivers|_{DIS} = - Sivers|_{DY}$



Sivers effect

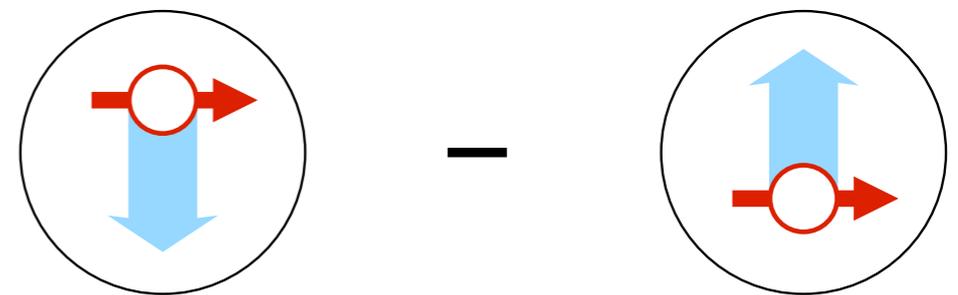
naively T-odd distributions
"Wilson-line physics"



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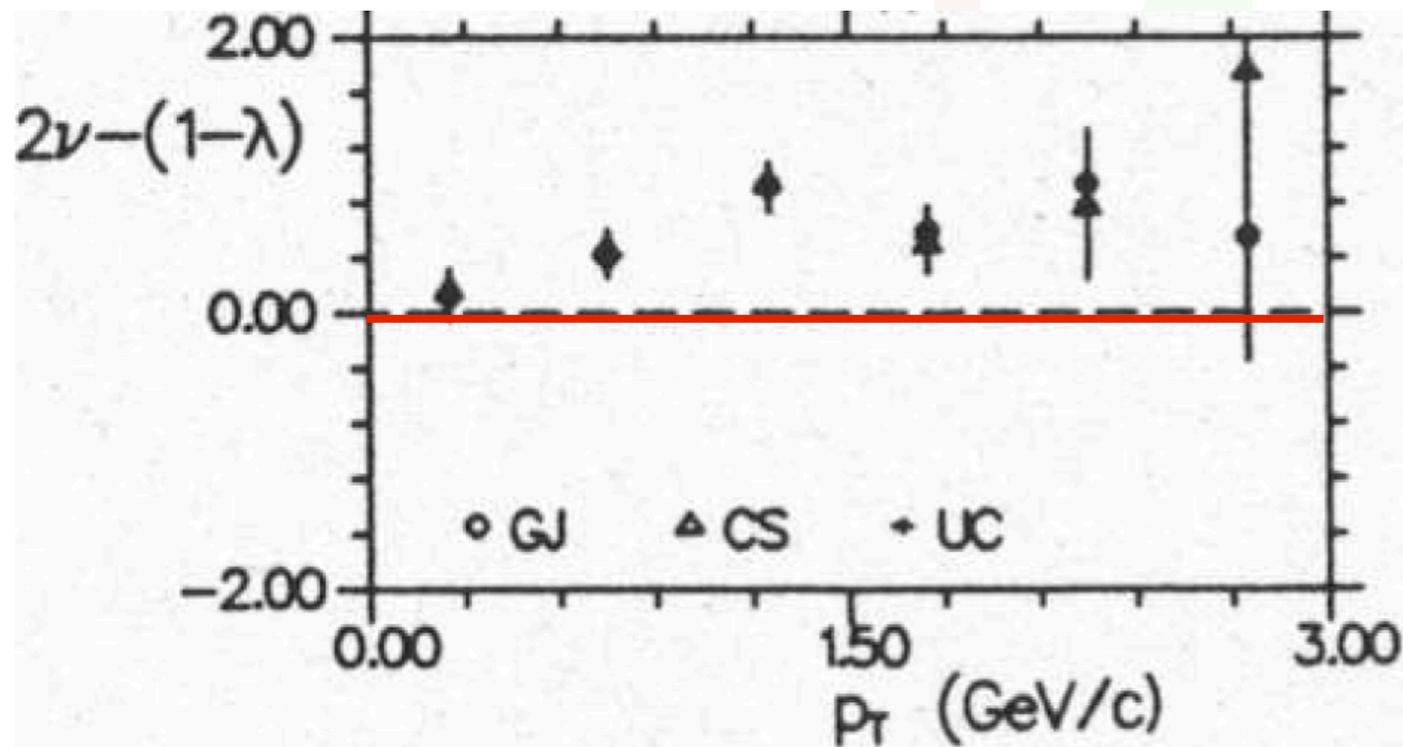
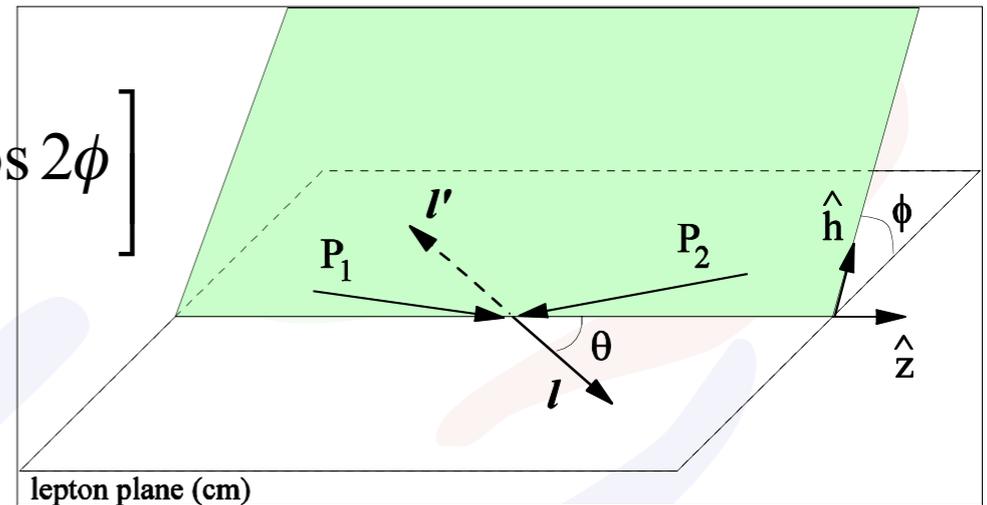
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Boer-Mulders effect



Unpolarized Drell-Yan

$$\left(\frac{1}{\sigma}\right)\left(\frac{d\sigma}{d\Omega}\right) = \left[\frac{3}{4\pi}\right] \left[1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi \right]$$

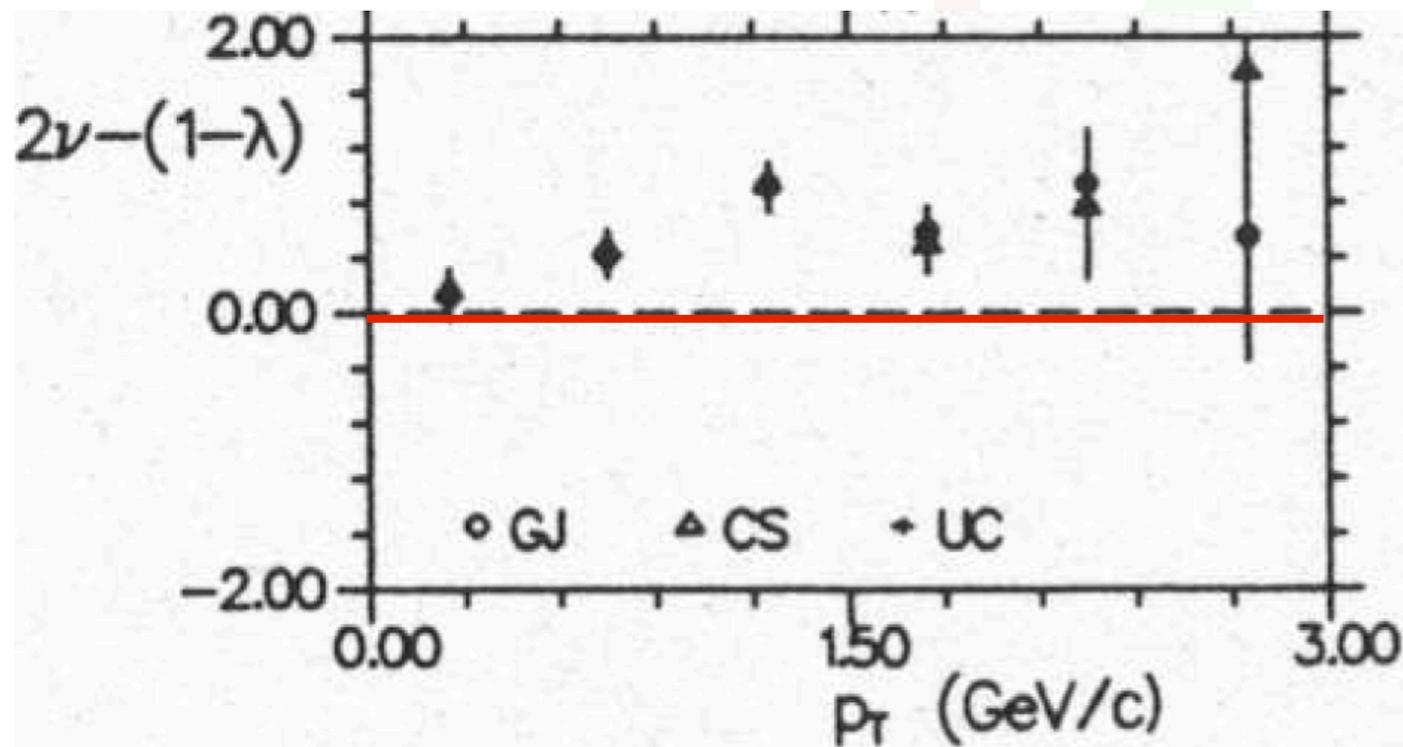
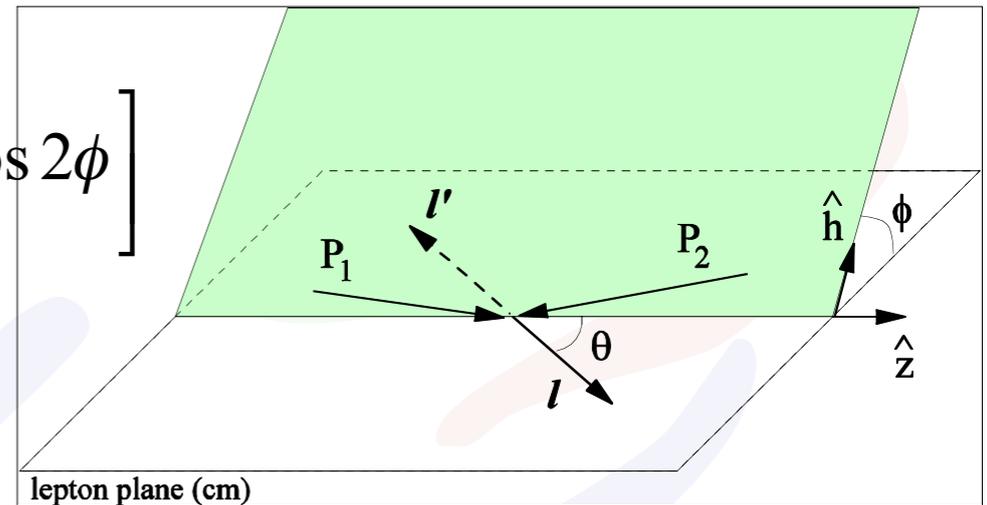


$$1 - \lambda - 2\nu = 0$$

Large deviations from Lam-Tung relation observed in DY
[NA10 ('86/'88) & E615 ('89)]

Unpolarized Drell-Yan

$$\left(\frac{1}{\sigma}\right)\left(\frac{d\sigma}{d\Omega}\right) = \left[\frac{3}{4\pi}\right] \left[1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi \right]$$



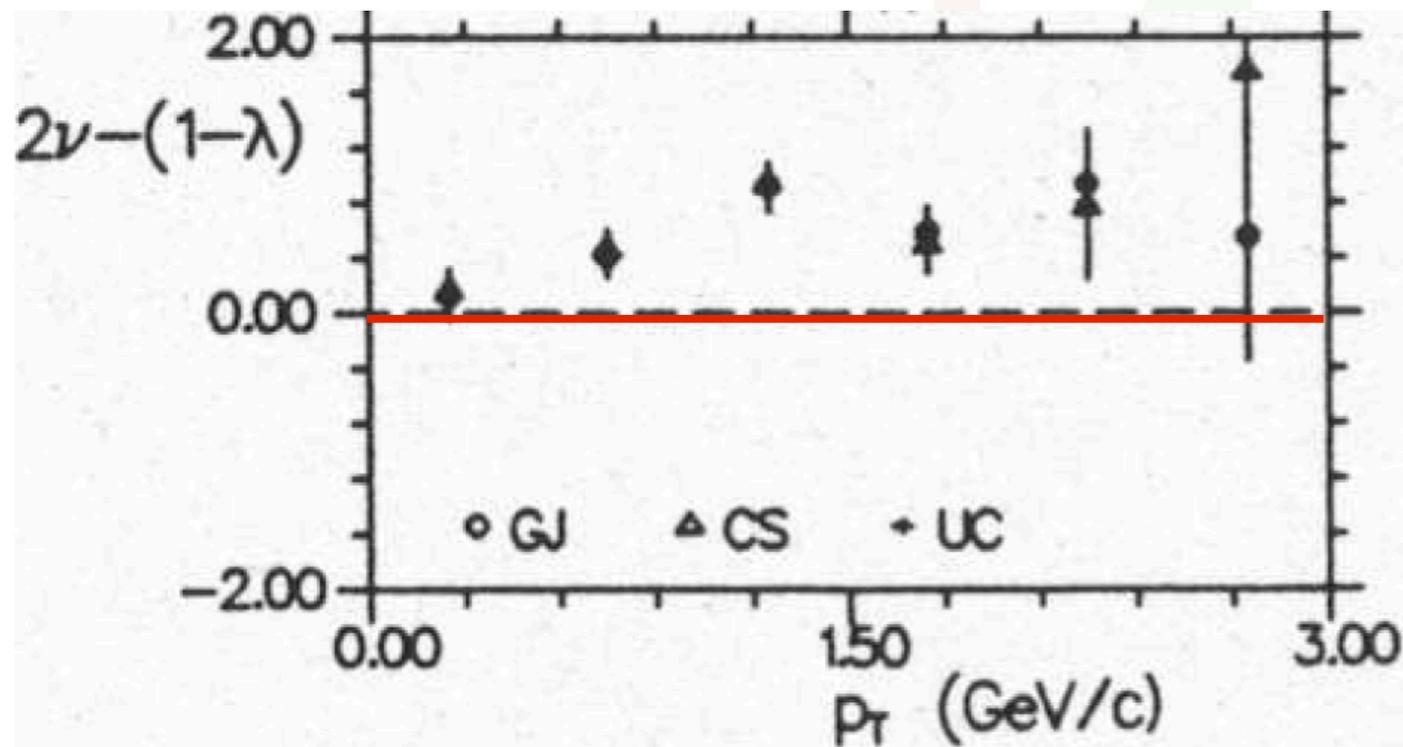
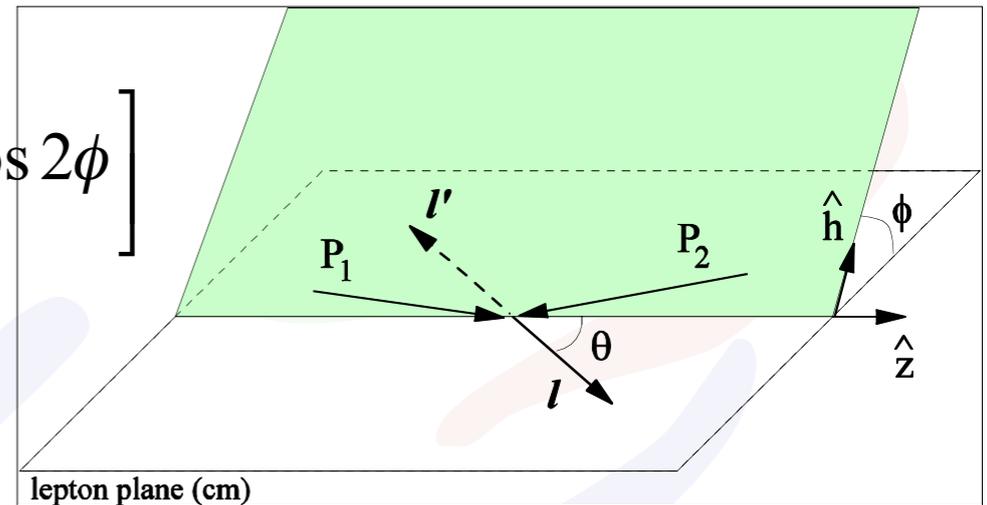
$$1 - \lambda - 2\nu = 0$$

Large deviations from Lam-Tung relation observed in DY
[NA10 ('86/'88) & E615 ('89)]

- failure of collinear pQCD

Unpolarized Drell-Yan

$$\left(\frac{1}{\sigma}\right)\left(\frac{d\sigma}{d\Omega}\right) = \left[\frac{3}{4\pi}\right] \left[1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi \right]$$



$$1 - \lambda - 2\nu = 0$$

Large deviations from Lam-Tung relation observed in DY
[NA10 ('86/'88) & E615 ('89)]

- failure of collinear pQCD
- possible source: Boer-Mulders effect

Boer-Mulders effect

Sivers effect:

$$f_{1T}^\perp = \text{---} \left(\begin{array}{c} \circ \\ \downarrow \\ \circ \end{array} \right) \text{---} \text{---} \left(\begin{array}{c} \uparrow \\ \circ \end{array} \right) \text{---}$$

$S_N \cdot (\mathbf{p}_\perp \times \mathbf{P}_N)$

Boer-Mulders effect:

$$h_1^\perp = \left(\begin{array}{c} \circ \rightarrow \\ \downarrow \\ \circ \rightarrow \end{array} \right) \text{---} \left(\begin{array}{c} \uparrow \\ \circ \end{array} \right)$$

$S_q \cdot (\mathbf{p}_\perp \times \mathbf{P}_N)$



hermes

Boer-Mulders effect

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- spin-effect in unpolarized reactions



hermes

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- spin-effect in unpolarized reactions
- "QCD Sokolov-Ternov effect" - transverse polarization of "orbiting" quarks

Boer-Mulders effect

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- QCD: sign change for DIS vs. Drell-Yan

Boer-Mulders effect

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$S_N \cdot (\mathbf{p}_\perp \times \mathbf{P}_N)$

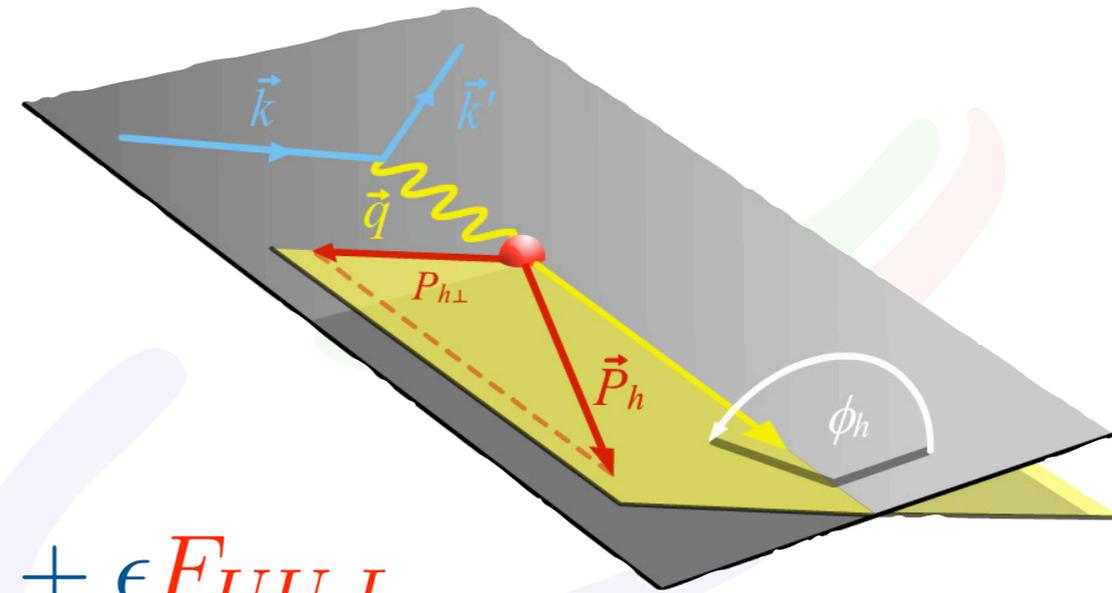
Boer-Mulders effect:

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$S_q \cdot (\mathbf{p}_\perp \times \mathbf{P}_N)$

- spin-effect in unpolarized reactions
 - "QCD Sokolov-Ternov effect" - transverse polarization of "orbiting" quarks
 - QCD: sign change for DIS vs. Drell-Yan
 - up to now little data from DIS
- ➔ HERMES with most comprehensive data set

Cross section without polarization



$$\frac{d^5 \sigma}{dx dy dz d\phi_h dP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \{F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1-\epsilon)} F_{UU}^{\cos \phi_h} \cos \phi_h + \epsilon F_{UU}^{\cos 2\phi_h} \cos 2\phi_h\}$$

$$F_{XY,Z} = F_{XY,Z}(x, y, z, P_{h\perp})$$

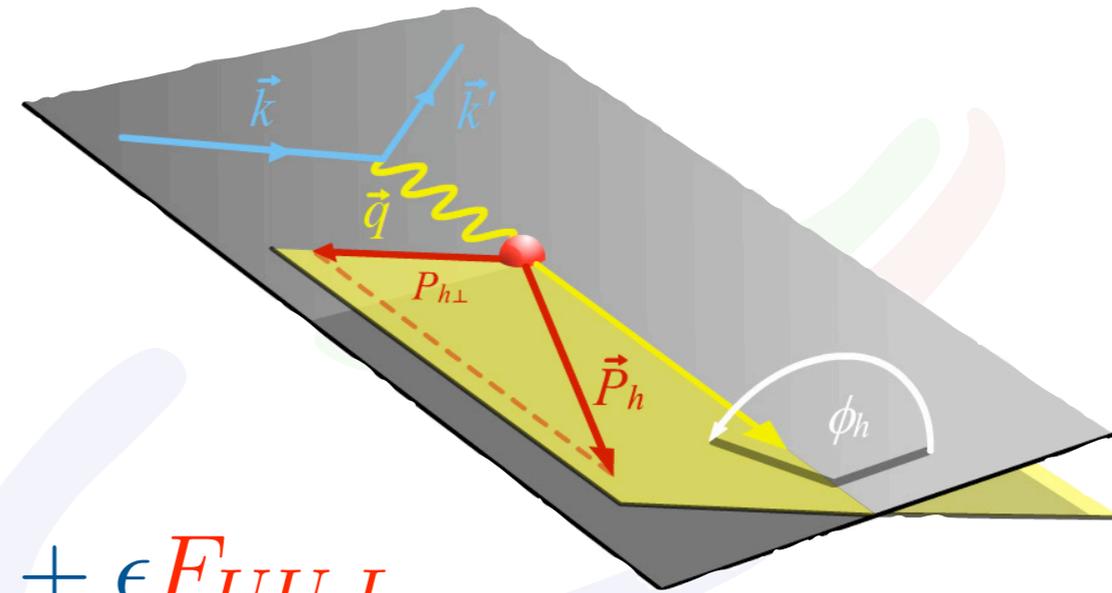
target polarization \downarrow
 \uparrow beam polarization \uparrow virtual-photon polarization

$$\gamma = \frac{2Mx}{Q}$$

$$\epsilon = \frac{1 - y - \frac{1}{4}\gamma^2 y^2}{1 - y + \frac{1}{2}y^2 + \frac{1}{4}\gamma^2 y^2}$$

[see, e.g., Bacchetta et al., JHEP 0702 (2007) 093]

Cross section without polarization



$$\frac{d^5 \sigma}{dx dy dz d\phi_h dP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \{F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1-\epsilon)} F_{UU}^{\cos \phi_h} \cos \phi_h + \epsilon F_{UU}^{\cos 2\phi_h} \cos 2\phi_h\}$$

leading twist
 $F_{UU}^{\cos 2\phi_h} \propto C \left[\frac{2(\hat{P}_{h\perp} \cdot \vec{k}_T)(\hat{P}_{h\perp} \cdot \vec{p}_T) - \vec{k}_T \cdot \vec{p}_T}{MM_h} h_1^\perp H_1^\perp \right]$

next to leading twist
 $F_{UU}^{\cos \phi_h} \propto \frac{2M}{Q} C \left[\frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M_h} x h_1^\perp H_1^\perp - \frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M} x f_1 D_1 + \dots \right]$

BOER-MULDERS EFFECT (points to the blue box in the leading twist equation)

CAHN EFFECT (points to the red box in the next to leading twist equation)

Interaction dependent terms neglected (points to the ellipsis in the next to leading twist equation)

$$\gamma = \frac{2Mx}{Q}$$

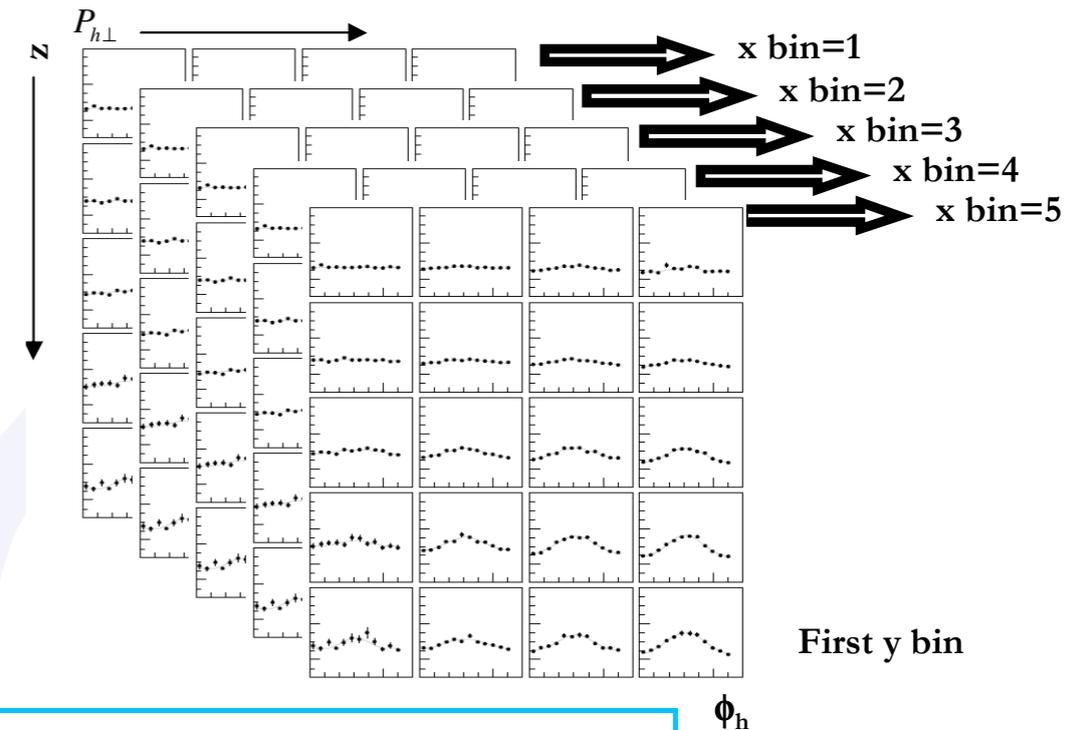
$$\epsilon = \frac{1 - y - \frac{1}{4}\gamma^2 y^2}{1 - y + \frac{1}{2}y^2 + \frac{1}{4}\gamma^2 y^2}$$

[see, e.g., Bacchetta et al., JHEP 0702 (2007) 093]

(Implicit sum over quark flavours)

Extraction of cosine modulations

- **Fully differential analysis** in $(x, y, z, P_{h\perp}, \phi)$
- **Multi-dimensional unfolding:** correction for finite acceptance, QED radiation, kinematic smearing, detector resolution



probability that an event generated with a certain kinematics is measured with a different kinematics

$$n_{EXP} = S n_{BORN} + n_{Bg}$$

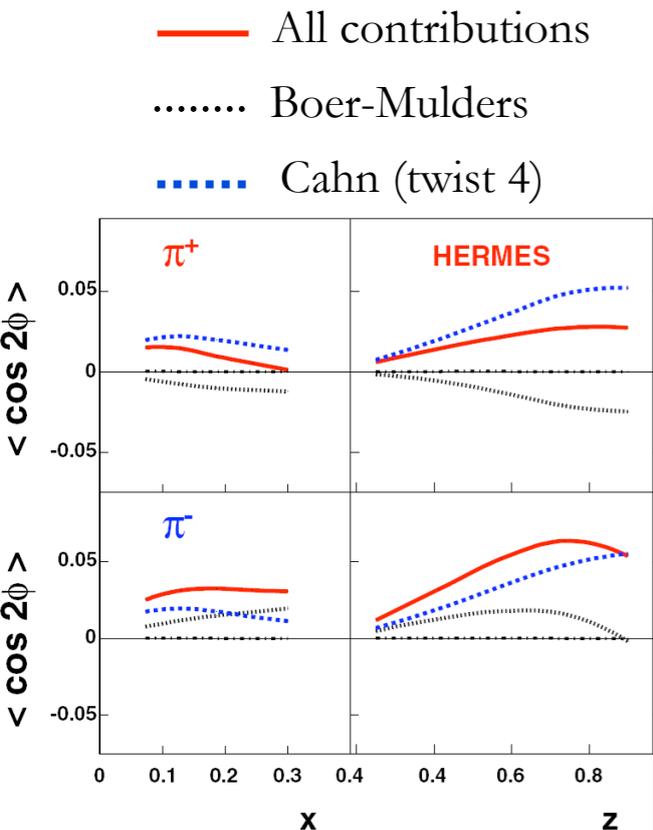
$$n_{BORN} = S^{-1} [n_{EXP} - n_{Bg}]$$

includes the events smeared into the acceptance

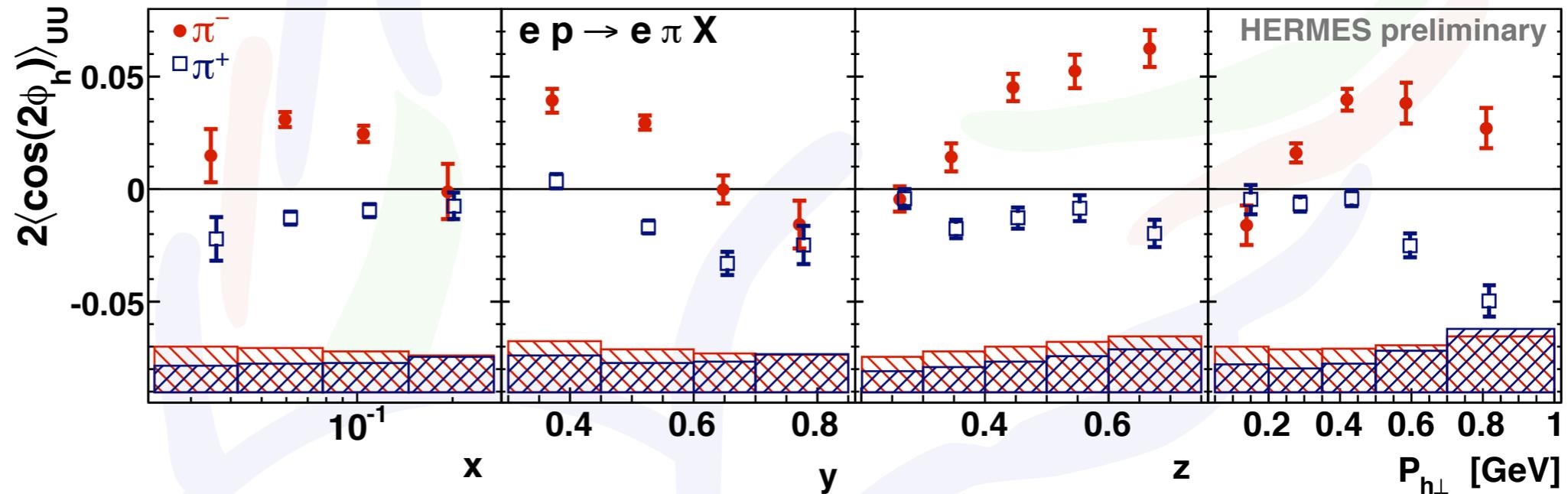
Signs of Boer-Mulders

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

[Airapetian et al., arXiv:1204.4161]



[V. Barone et al., Phys. Rev.D78 (2008) 045022]

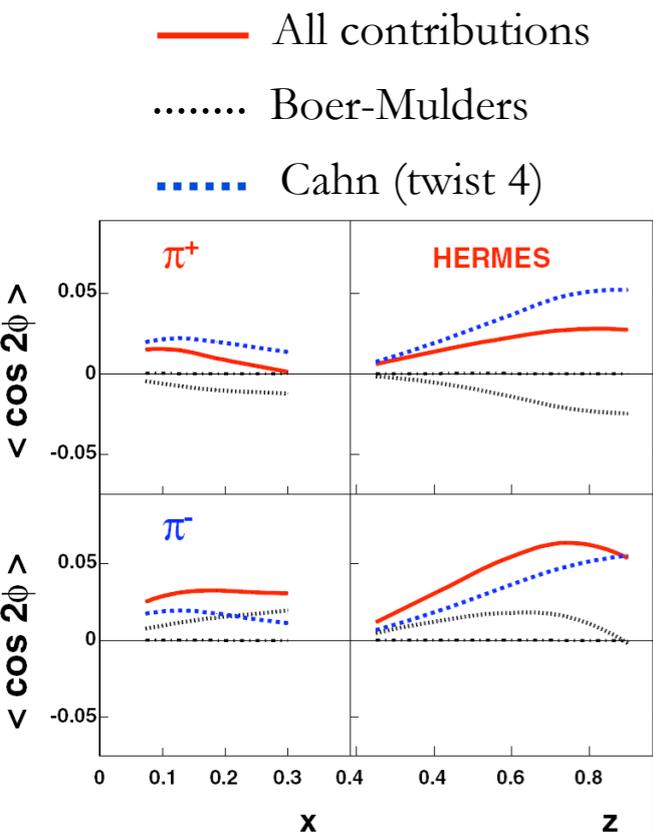


- Cahn effect only does not describe data

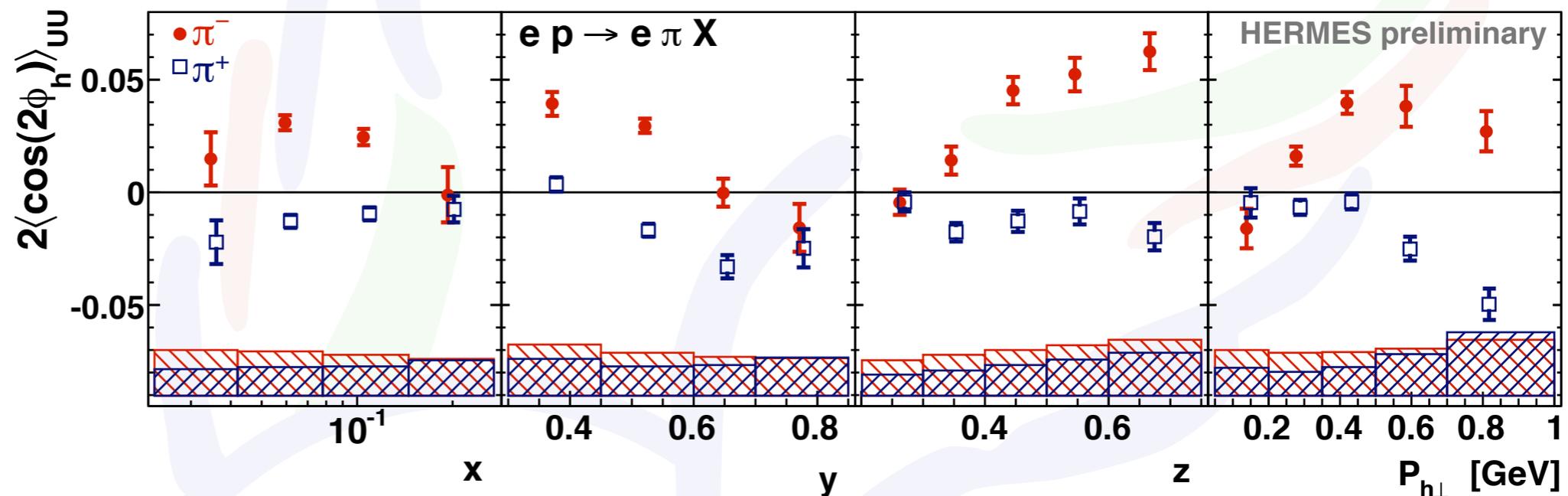
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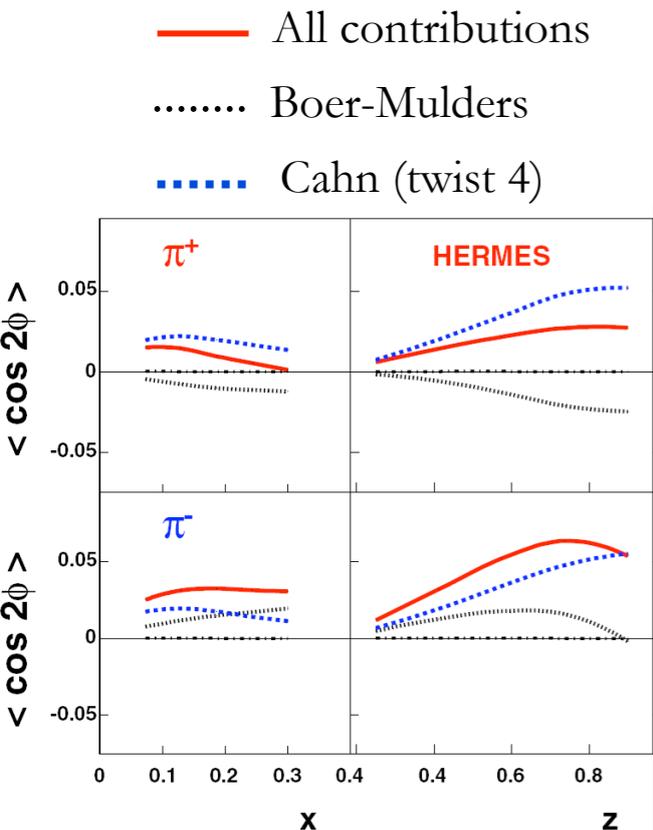


- Cahn effect only does not describe data
 - opposite sign for charged pions with larger magnitude for π^- (as expected)
- > same-sign BM-function for valence quarks

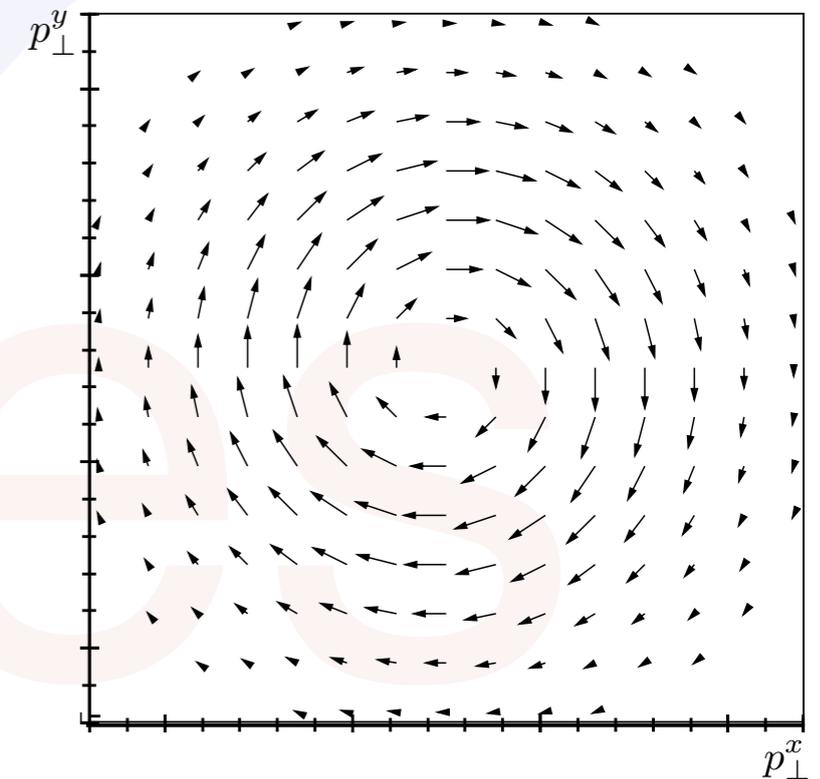
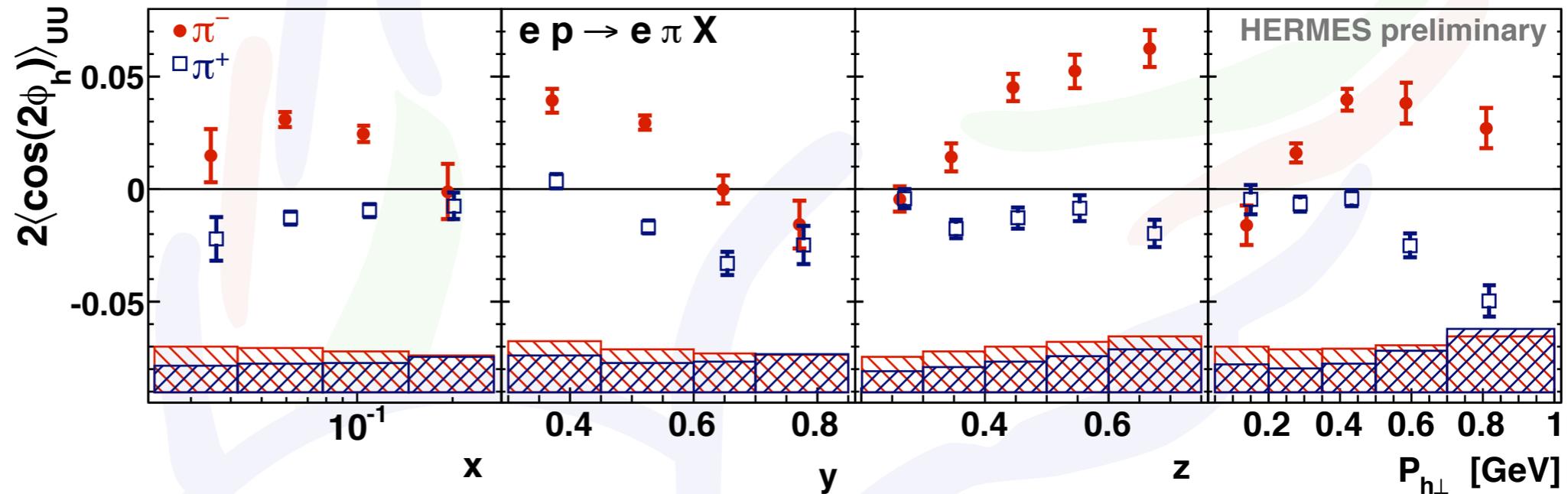
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[Airapetian et al., arXiv:1204.4161]



[V. Barone et al., Phys. Rev.D78 (2008) 045022]



[M. Burkardt and B. Hannfious, PLB658 (2008) 130]

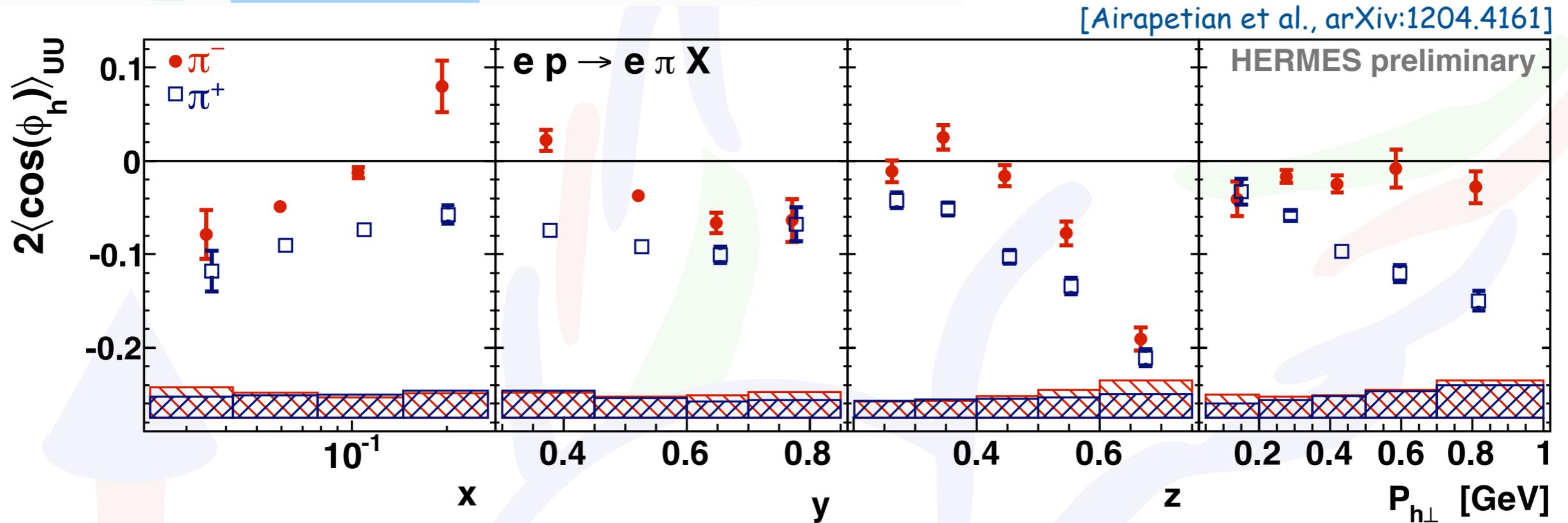
- Cahn effect only does not describe data
 - opposite sign for charged pions with larger magnitude for π^- (as expected)
- > same-sign BM-function for valence quarks

Cahn effect?

next to leading twist

$$F_{UU}^{\cos\phi_h} \propto \frac{2M}{Q} C \left[\underbrace{-\frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M_h} x h_1^\perp H_1^\perp}_{\text{BOER-MULDERS EFFECT}} \underbrace{-\frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M} x f_1 D_1}_{\text{CAHN EFFECT}} + \dots \right]$$

Interaction dependent terms neglected



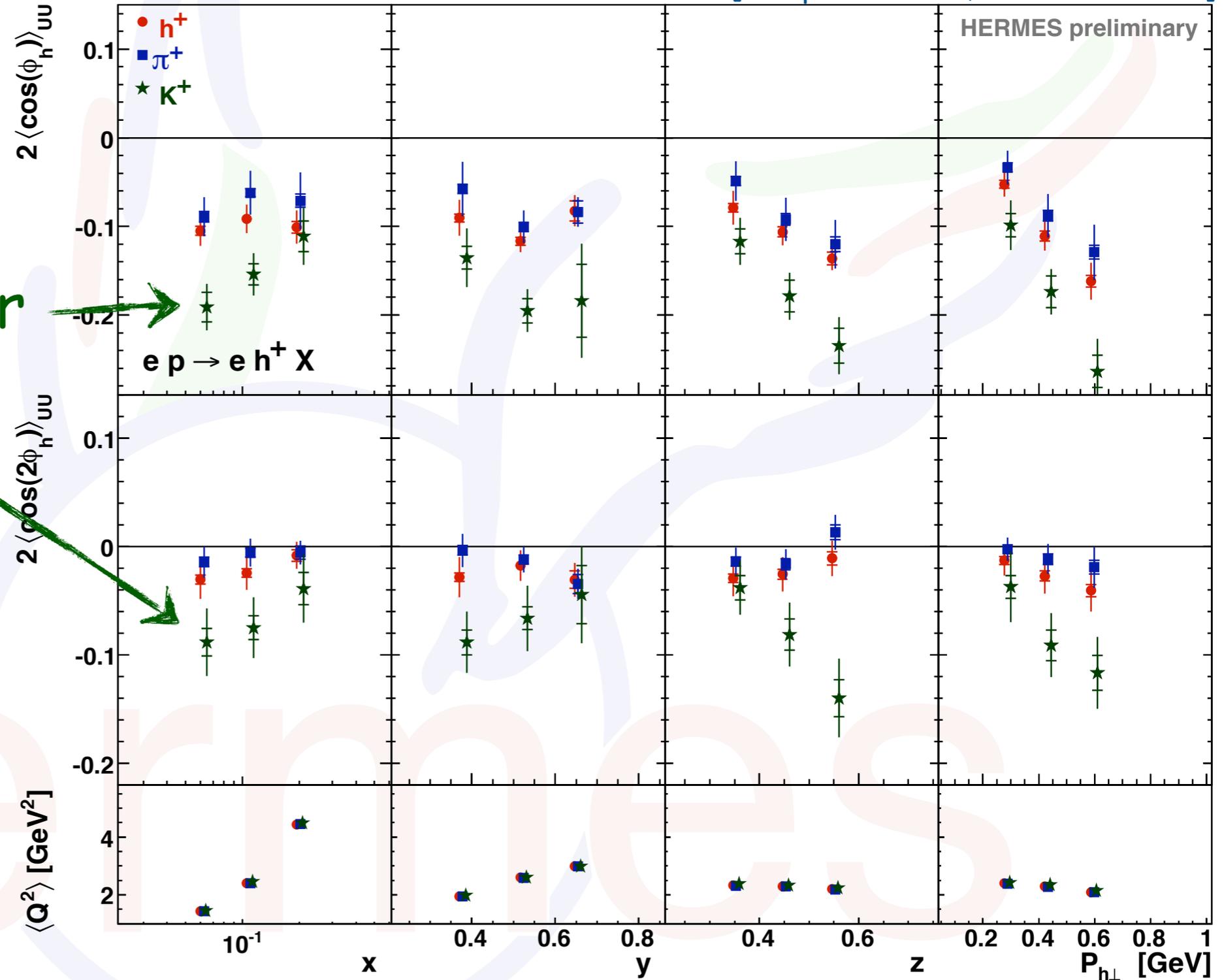
- no dependence on hadron charge expected for Cahn effect
- ➔ flavor dependence of transverse momentum
- ➔ sign of Boer-Mulders in $\cos\phi$ modulation
(indeed, overall pattern resembles B-M modulations)
- ➔ additional "genuine" twist-3?

"strange" results

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

[Airapetian et al., arXiv:1204.4161]

intriguing behavior
for kaons



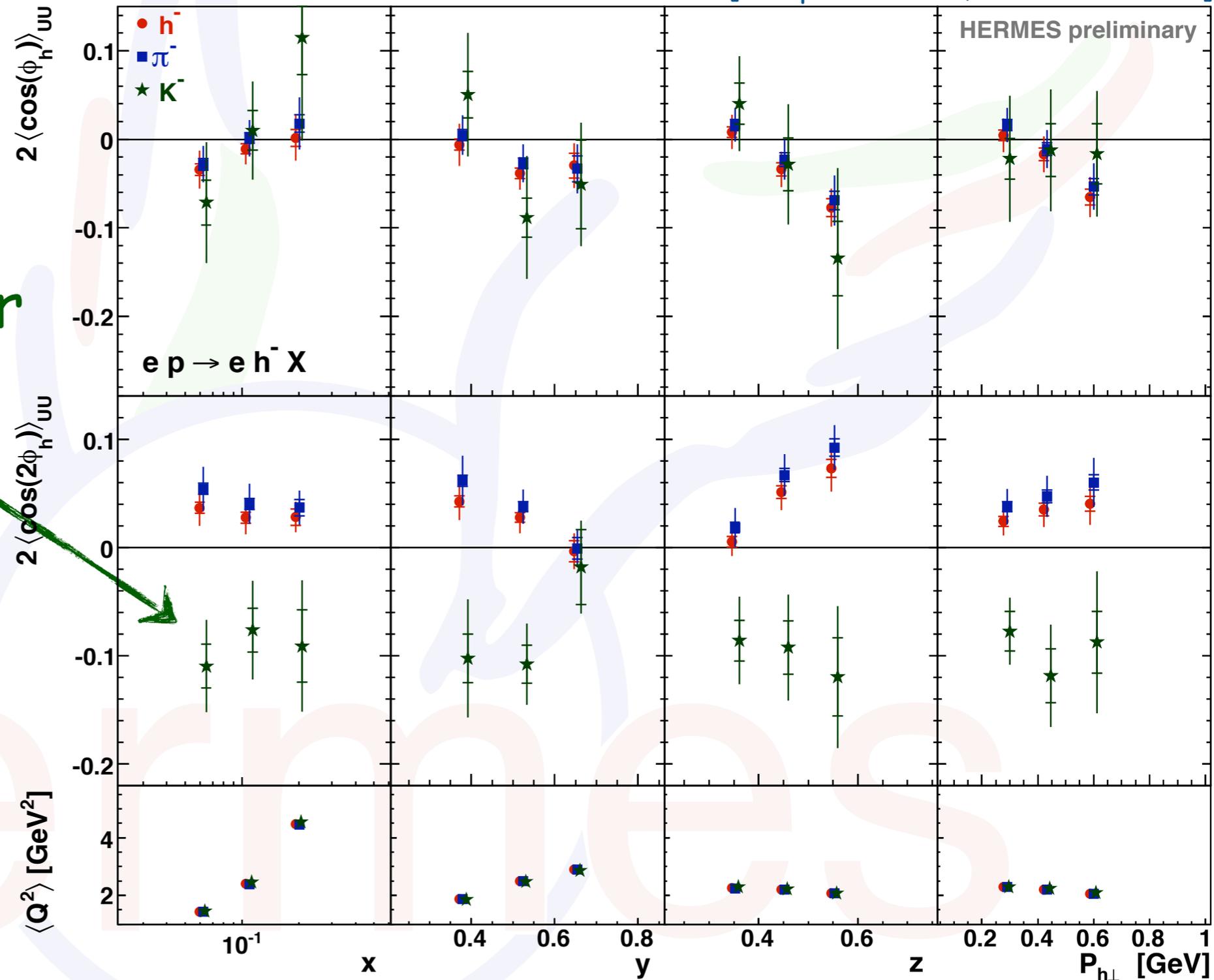
"strange" results

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

[Airapetian et al., arXiv:1204.4161]

HERMES preliminary

intriguing behavior
for kaons

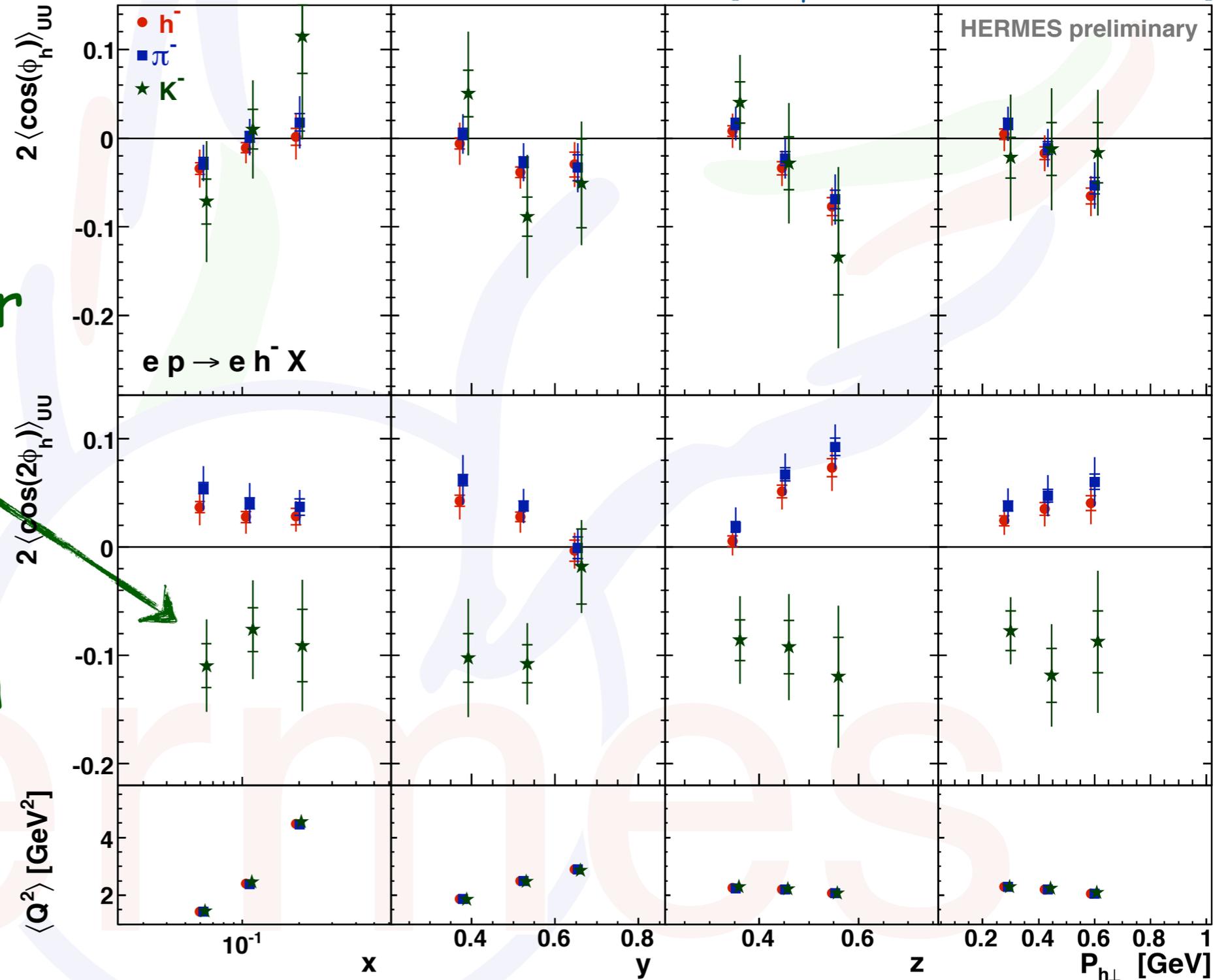


"strange" results

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U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

[Airapetian et al., arXiv:1204.4161]

HERMES preliminary

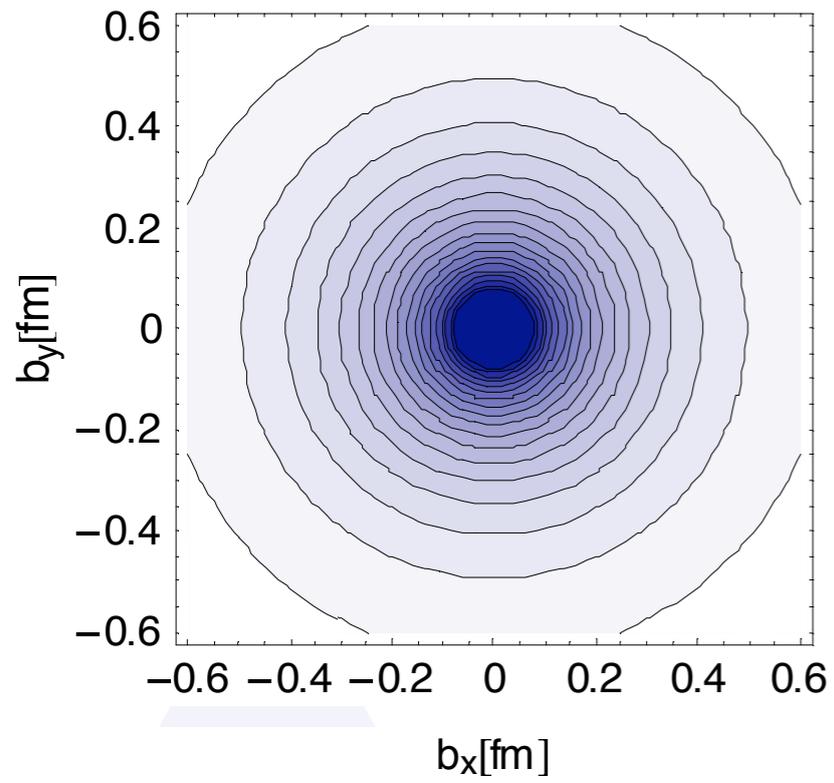


intriguing behavior
for kaons

different pattern
for kaon Collins
function?
(cf. BRAHMS A_N
and SIDIS Collins)

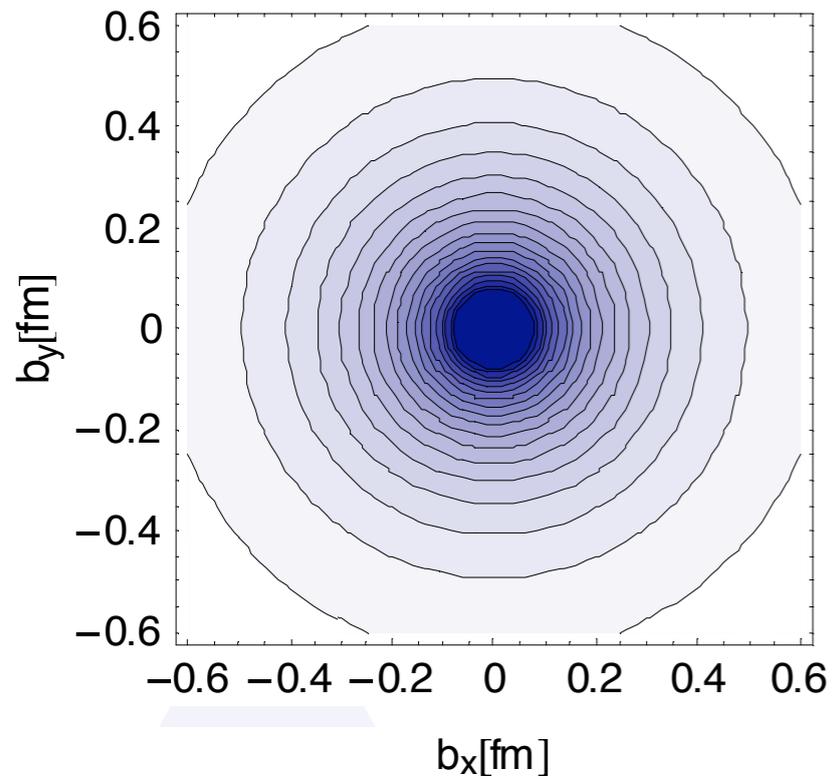
Exclusive reactions

Another 3D picture of the nucleon

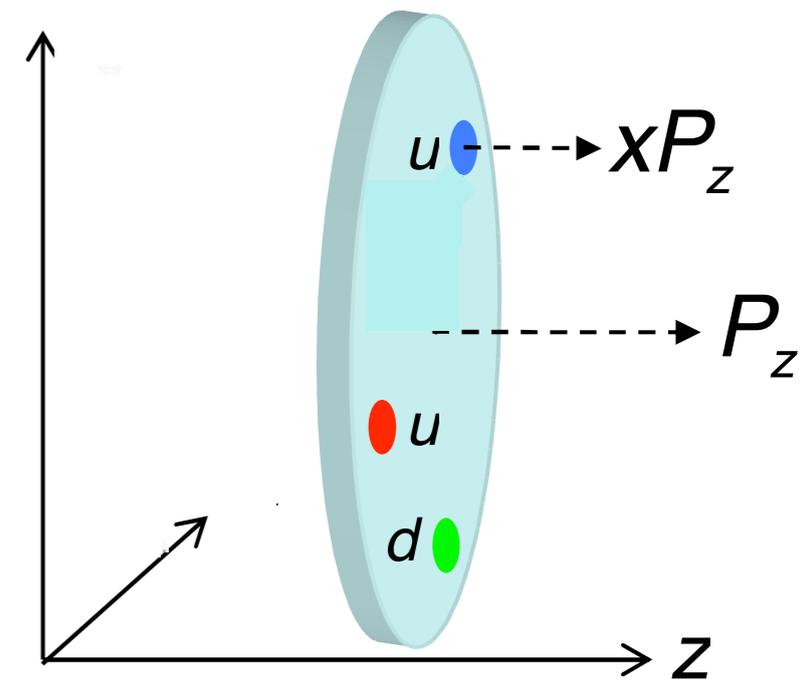


Form factors:
transverse distribution
of partons

Another 3D picture of the nucleon

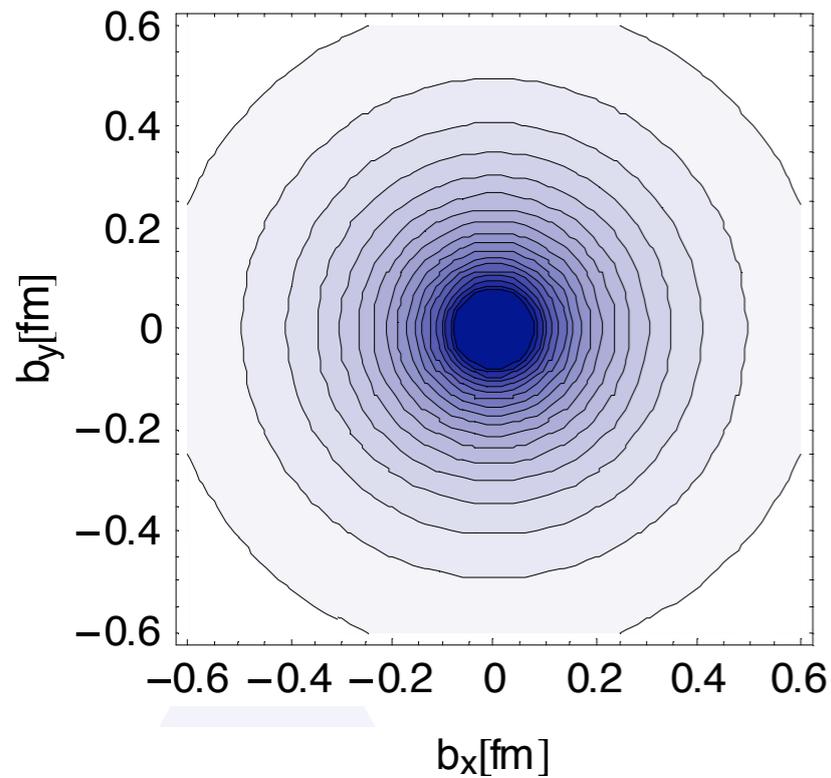


Form factors:
transverse distribution
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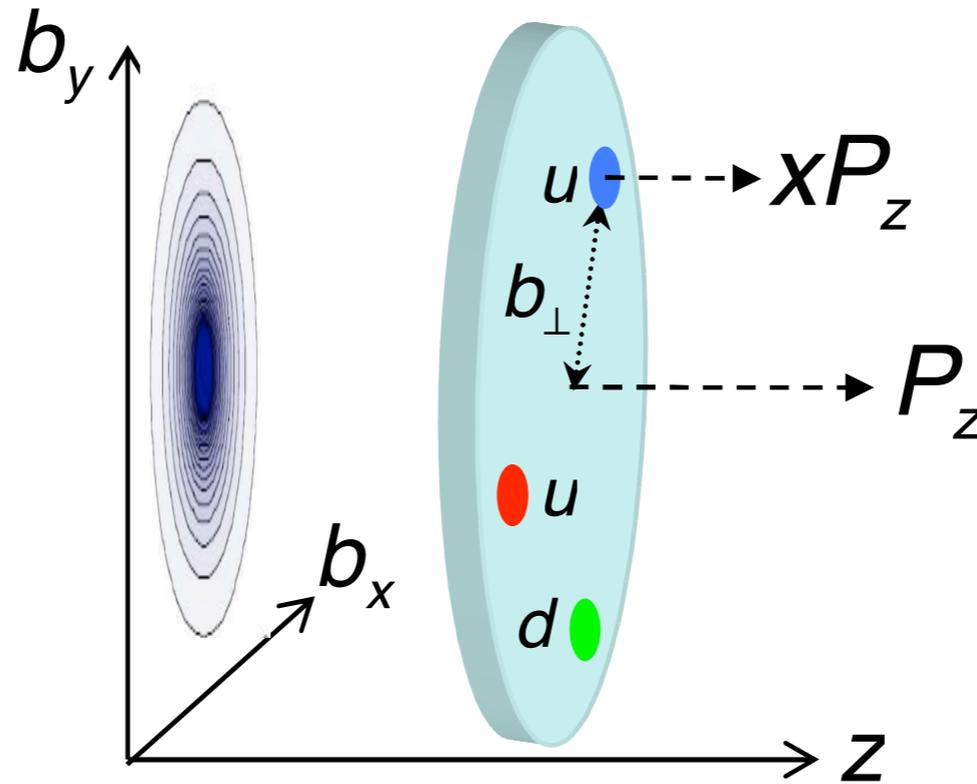


Parton distributions:
longitudinal momentum
of partons

Another 3D picture of the nucleon

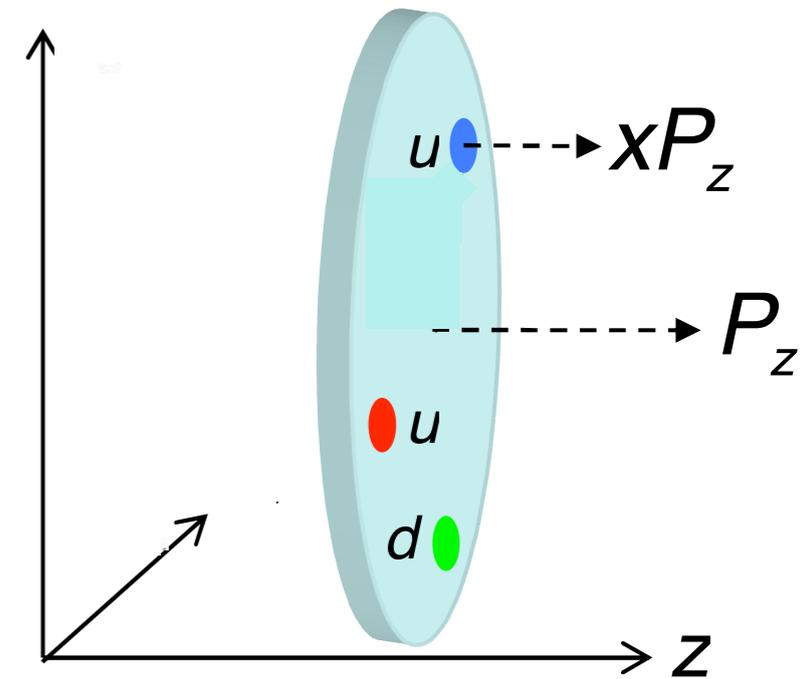


Form factors:
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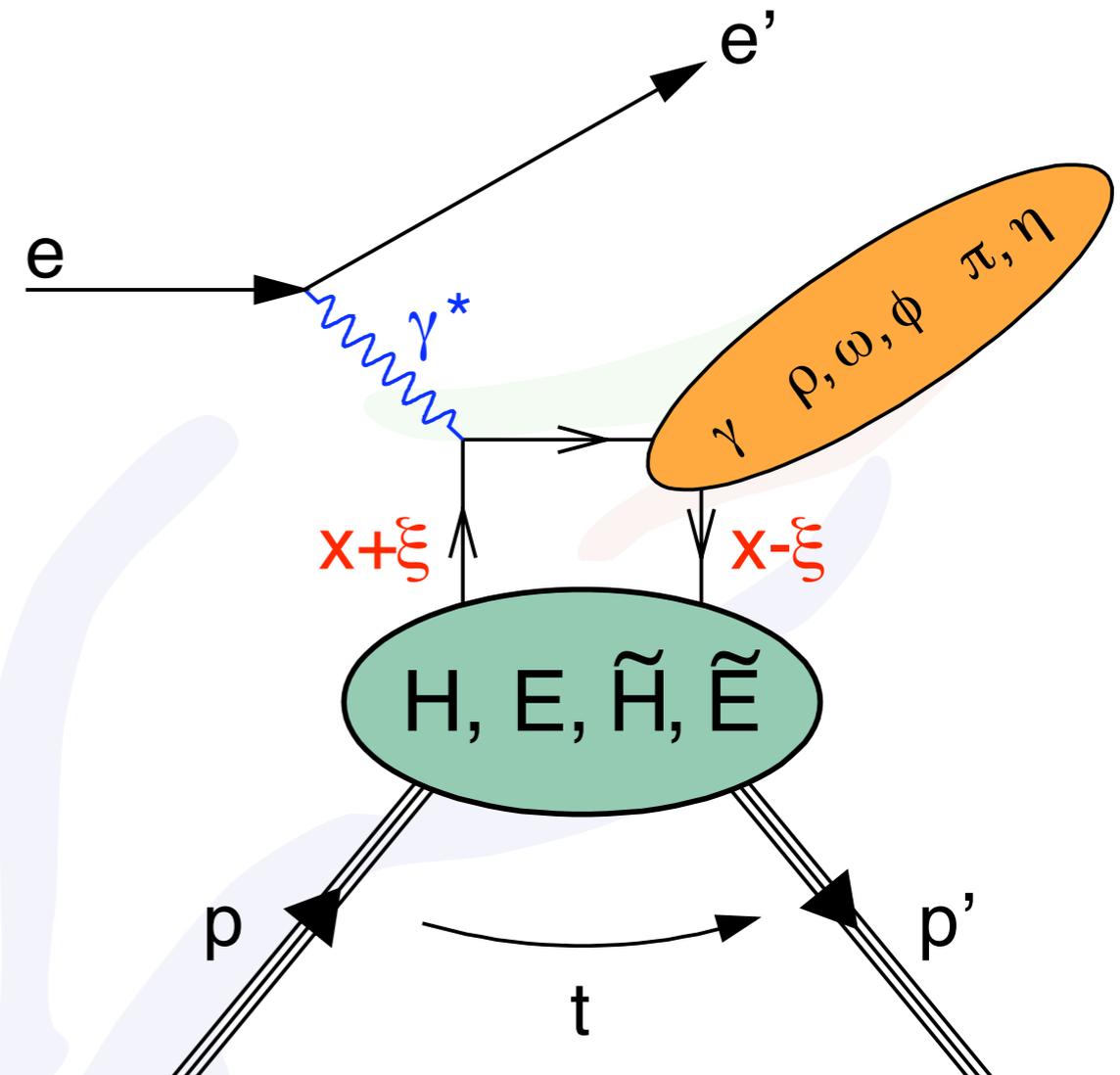
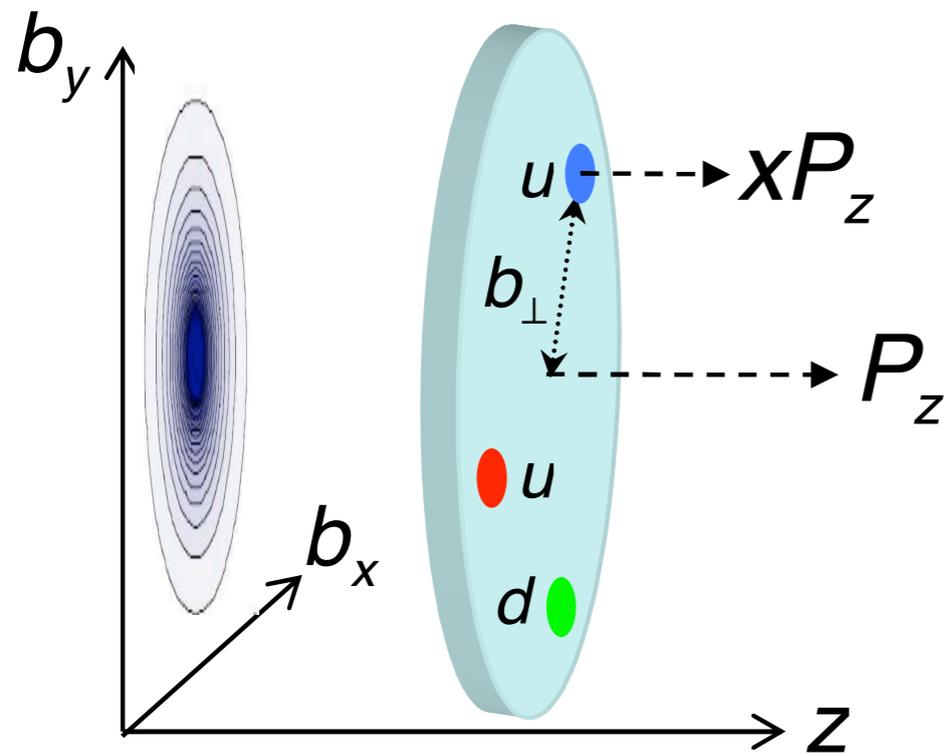
Nucleon Tomography

correlated info on transverse position and longitudinal momentum



Parton distributions:
longitudinal momentum
of partons

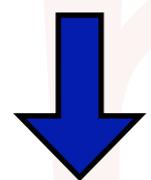
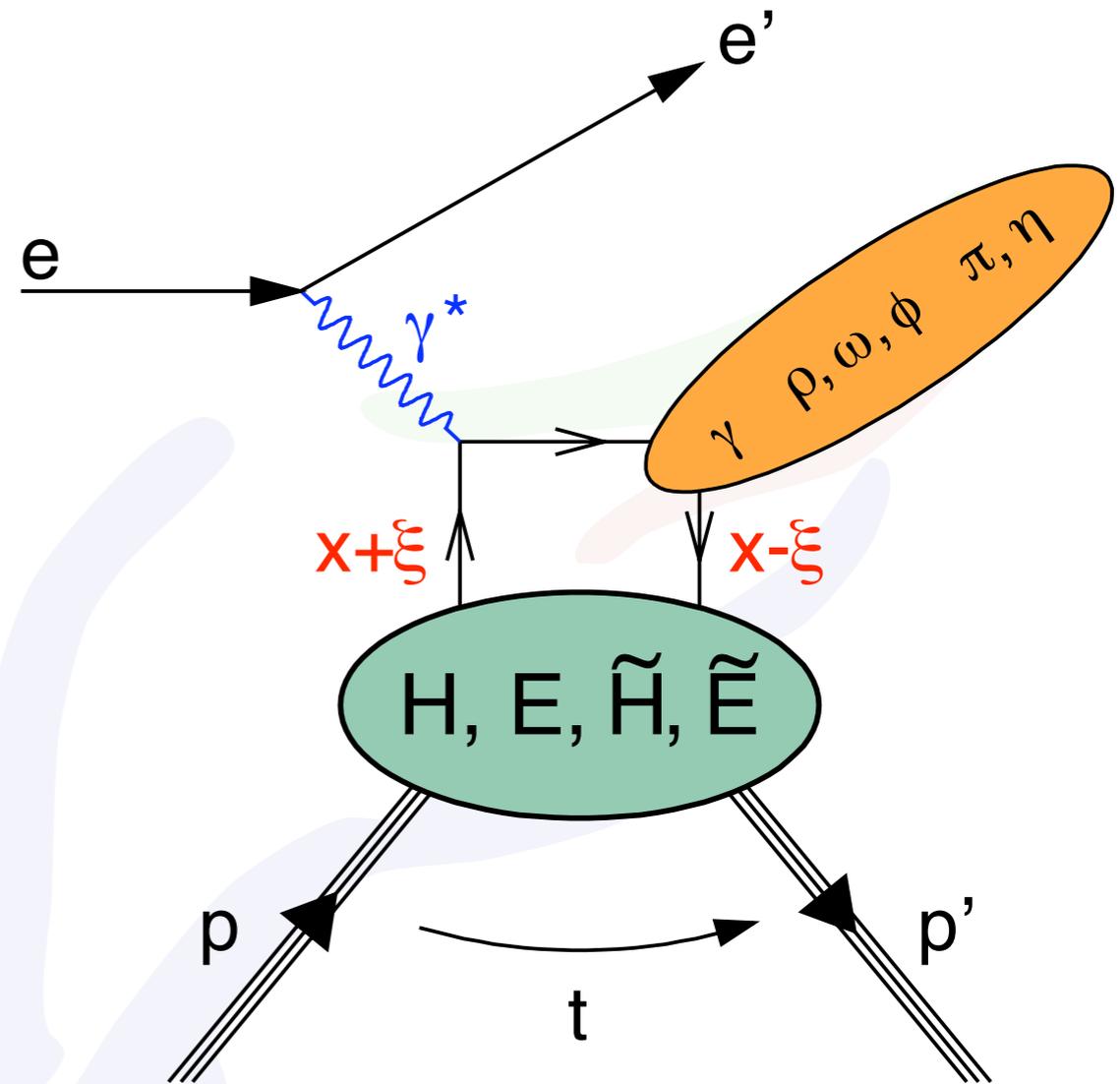
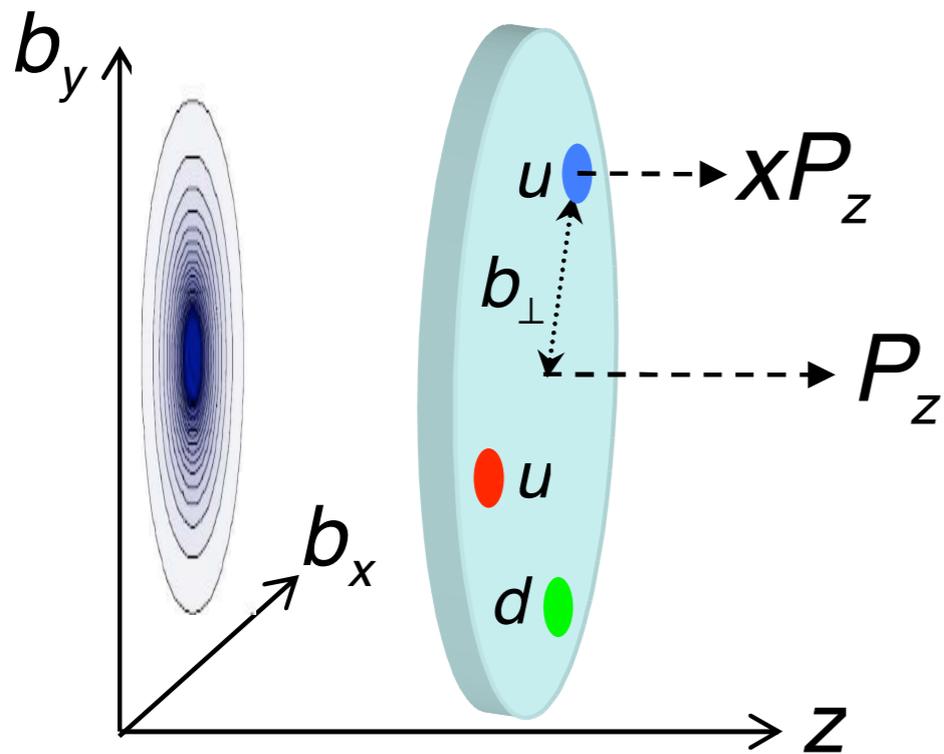
Probing GPDs in Exclusive Reactions



	no quark helicity flip	quark helicity flip
no nucleon helicity flip	H	\tilde{H}
nucleon helicity flip	E	\tilde{E}

(+ 4 more chiral-odd functions)

Probing GPDs in Exclusive Reactions



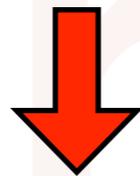
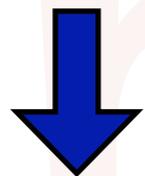
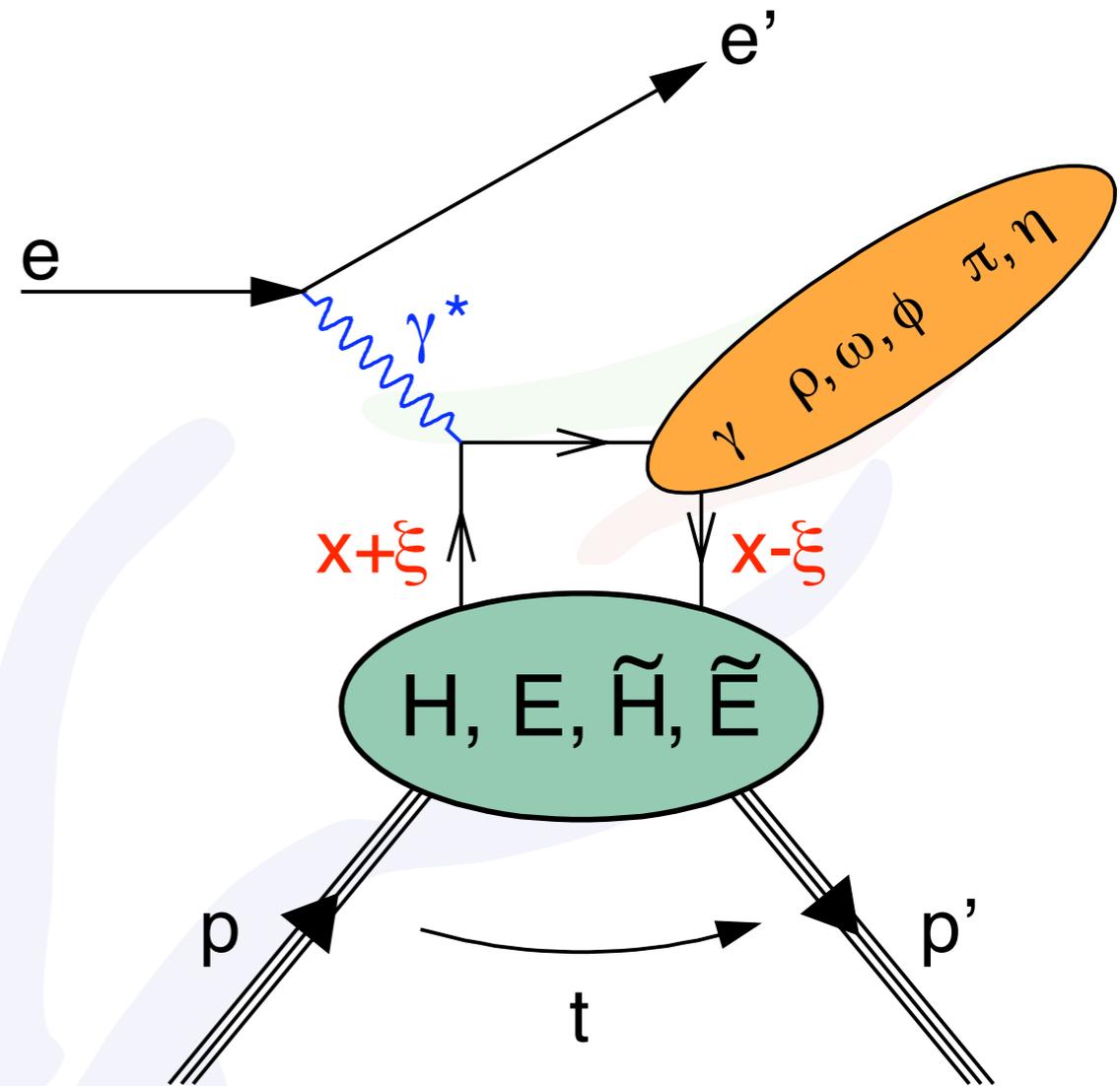
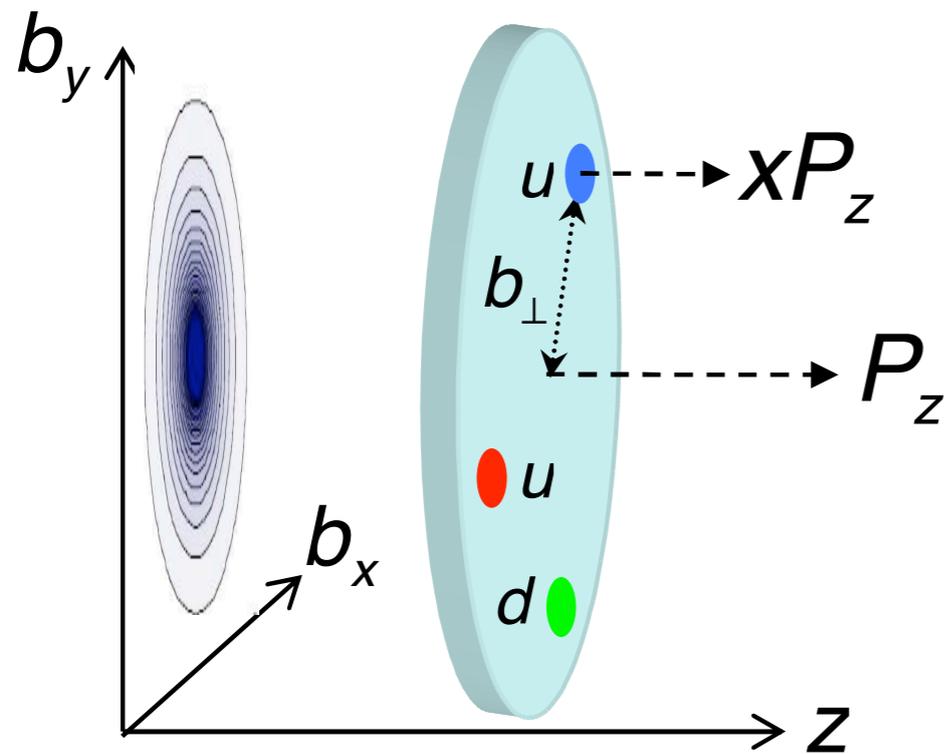
$$\int dx H^q(x, \xi, t) = F_1^q(t)$$

$$\int dx E^q(x, \xi, t) = F_2^q(t)$$

	no quark helicity flip	quark helicity flip
no nucleon helicity flip	H	\tilde{H}
nucleon helicity flip	E	\tilde{E}

(+ 4 more chiral-odd functions)

Probing GPDs in Exclusive Reactions



$$\int dx H^q(x, \xi, t) = F_1^q(t)$$

$$\int dx E^q(x, \xi, t) = F_2^q(t)$$

$$H^q(x, \xi = 0, t = 0) = q(x)$$

$$\tilde{H}^q(x, \xi = 0, t = 0) = \Delta q(x)$$

	no quark helicity flip	quark helicity flip
no nucleon helicity flip	H	\tilde{H}
nucleon helicity flip	E	\tilde{E}

(+ 4 more chiral-odd functions)

Probing GPDs in Exclusive Reactions

Ji relation (1996)

$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx x (H_q(x, \xi, t) + E_q(x, \xi, t))$$

→ Moment of GPD H and E relate directly to the total angular momentum of quarks

↓

$$\int dx H^q(x, \xi, t) = F_1^q(t)$$

$$\int dx E^q(x, \xi, t) = F_2^q(t)$$

↓

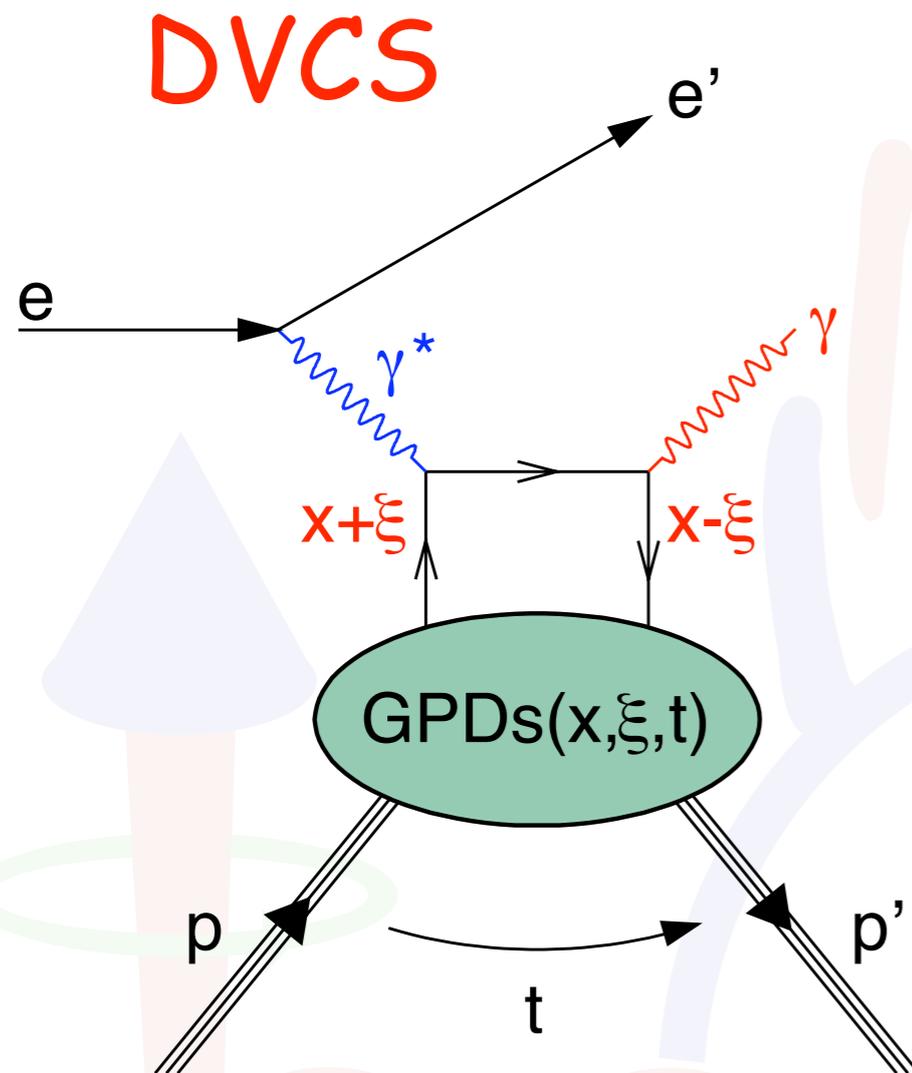
$$H^q(x, \xi = 0, t = 0) = q(x)$$

$$\tilde{H}^q(x, \xi = 0, t = 0) = \Delta q(x)$$

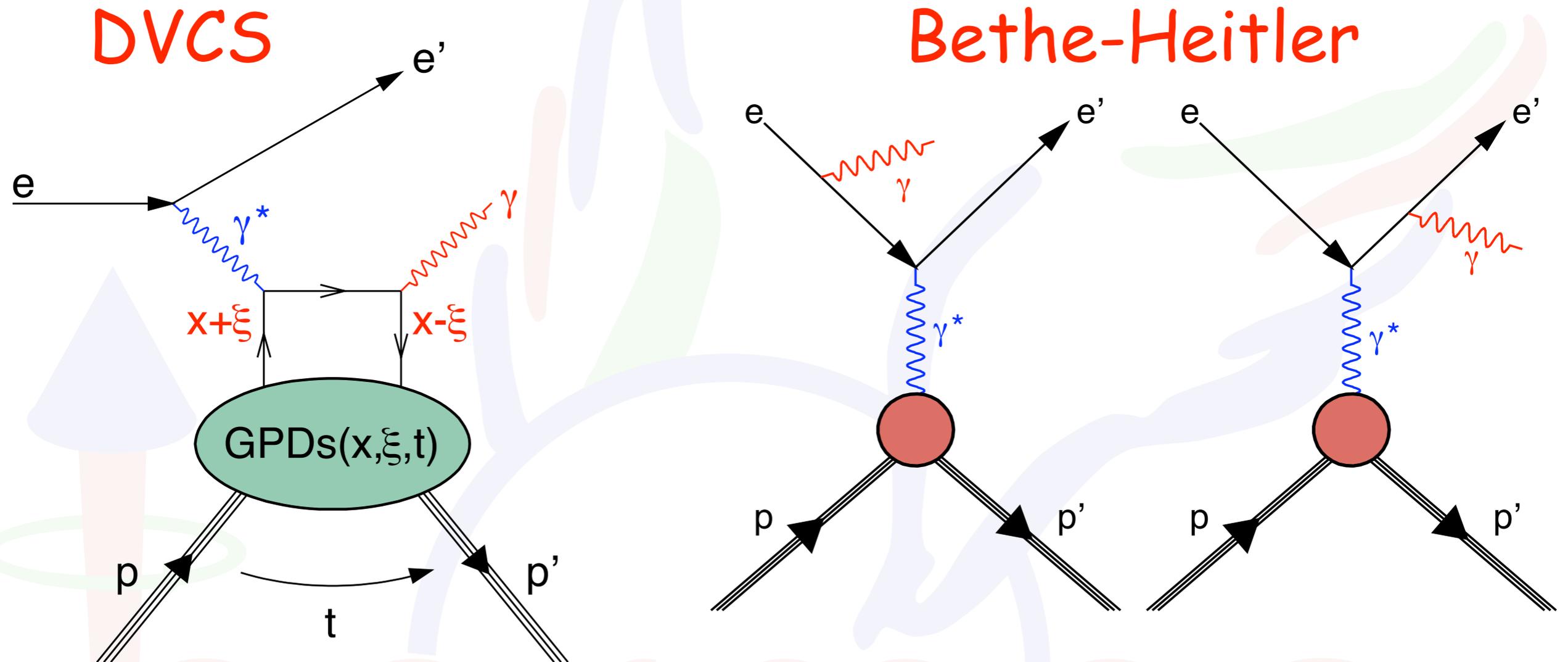
	no quark helicity flip	quark helicity flip
no nucleon helicity flip	H	\tilde{H}
nucleon helicity flip	E	\tilde{E}

(+ 4 more chiral-odd functions)

Real-photon production

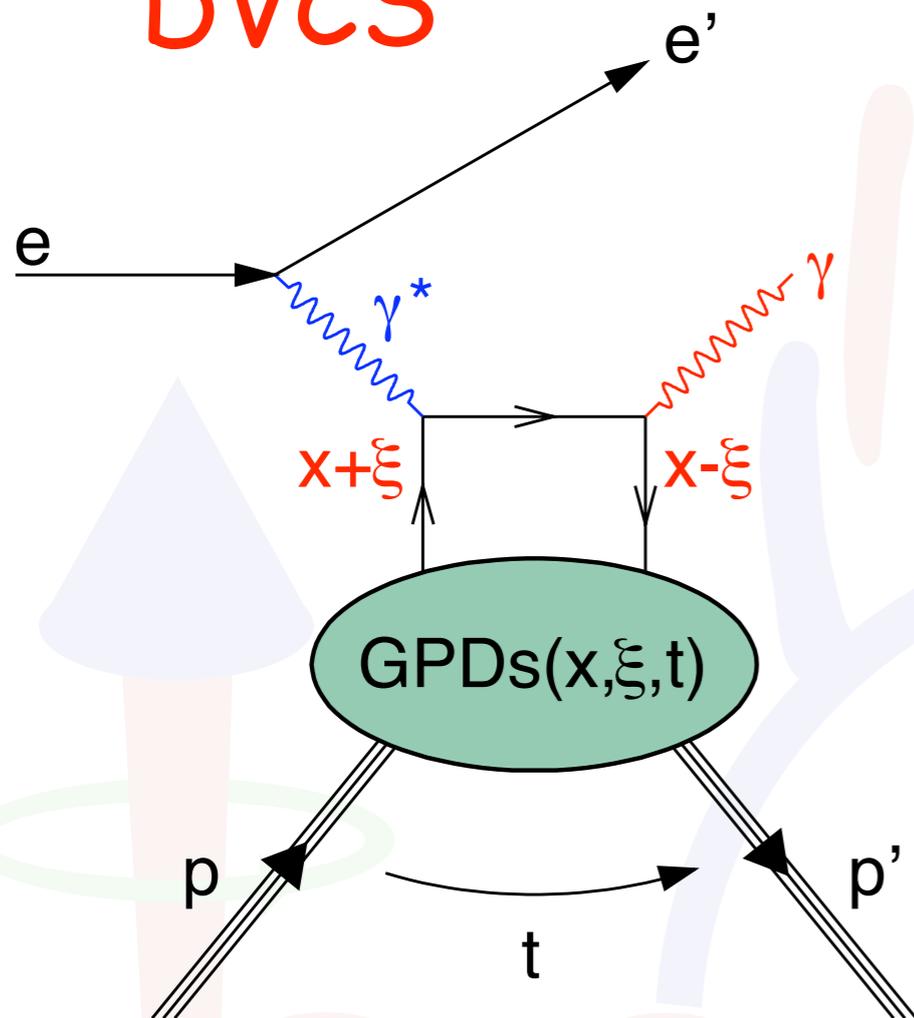


Real-photon production

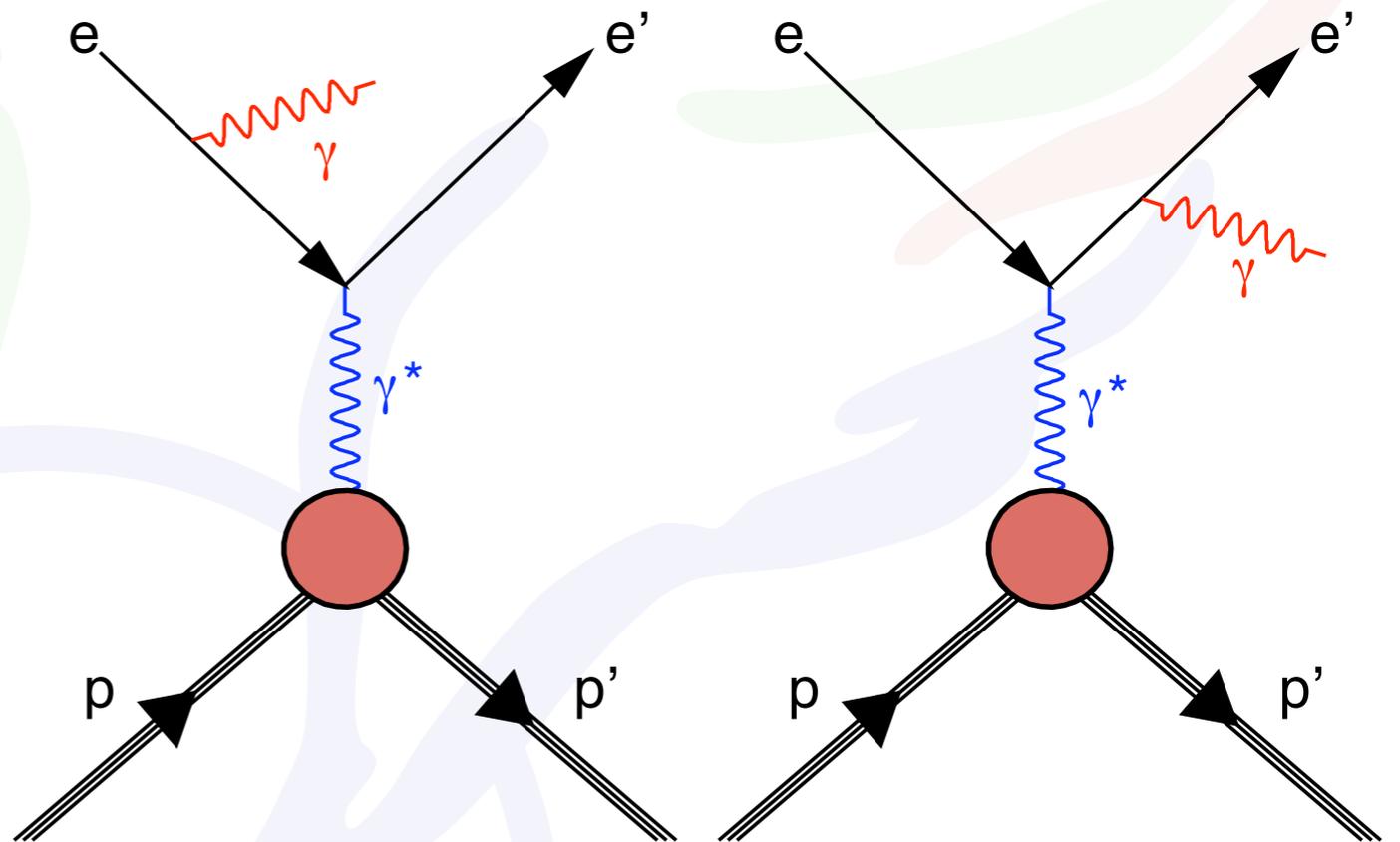


Real-photon production

DVCS



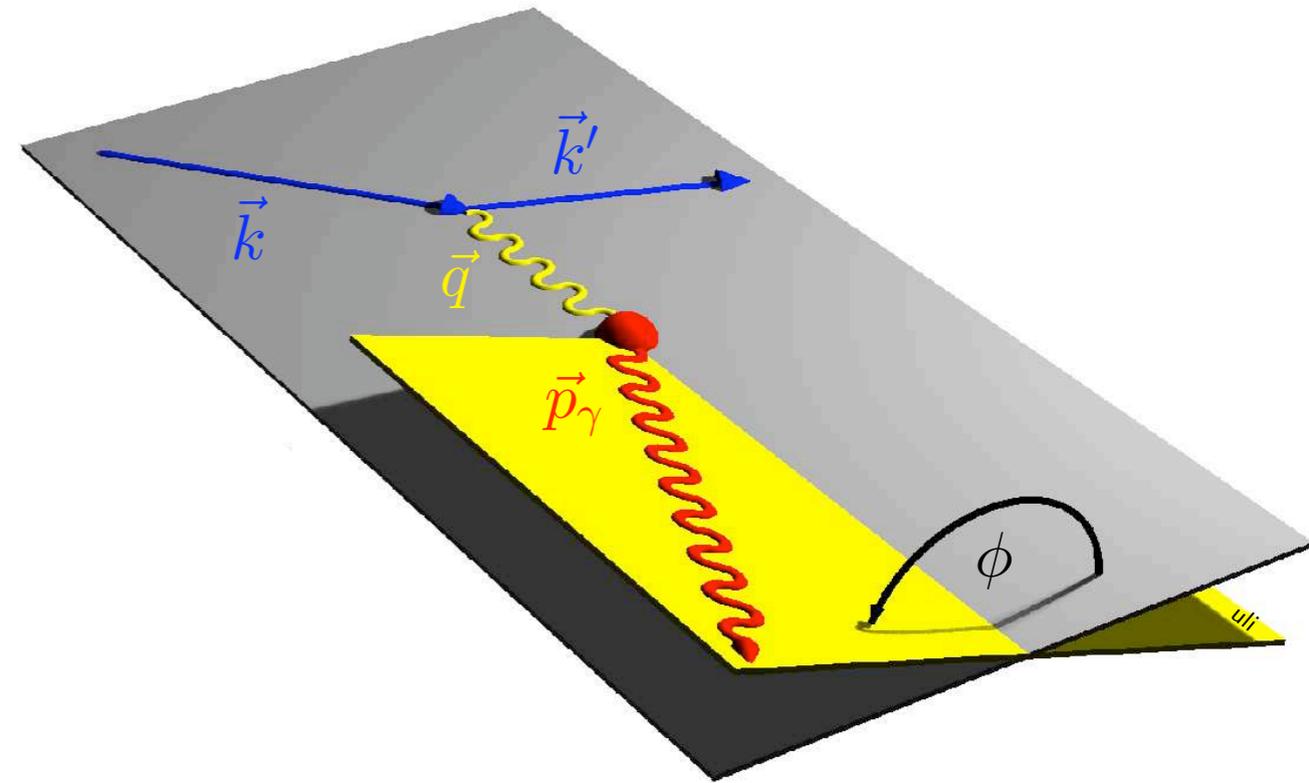
Bethe-Heitler



$$\frac{d^4\sigma}{dQ^2 dx_B dt d\phi} = \frac{y^2}{32(2\pi)^4 \sqrt{1 + \frac{4M^2 x_B^2}{Q^2}}} (|\mathcal{T}_{\text{DVCS}}|^2 + |\mathcal{T}_{\text{BH}}|^2 + \mathcal{I})$$

Azimuthal dependences in DVCS/BH

- beam polarization P_B
- beam charge C_B
- here: unpolarized target



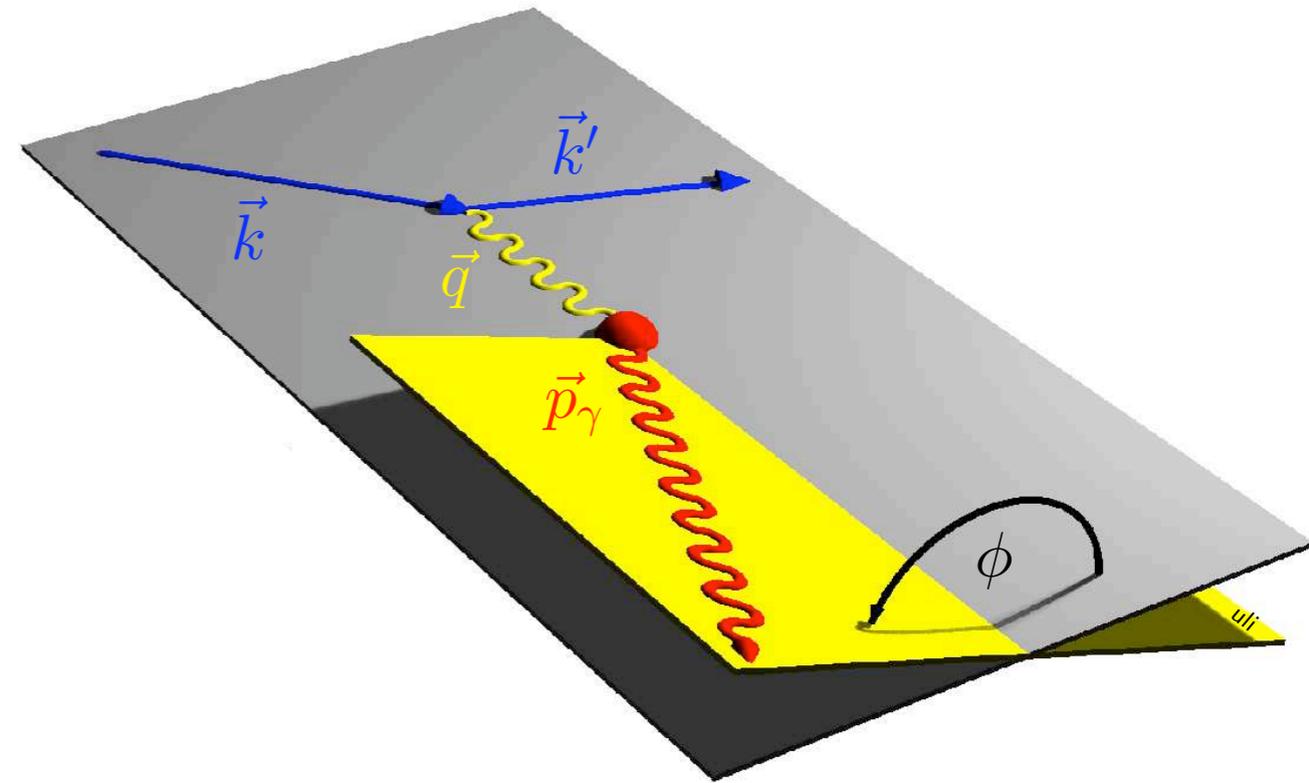
Fourier expansion for ϕ :

$$|\mathcal{T}_{\text{BH}}|^2 = \frac{K_{\text{BH}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \sum_{n=0}^2 c_n^{\text{BH}} \cos(n\phi)$$

calculable in QED
(using FF measurements)

Azimuthal dependences in DVCS/BH

- beam polarization P_B
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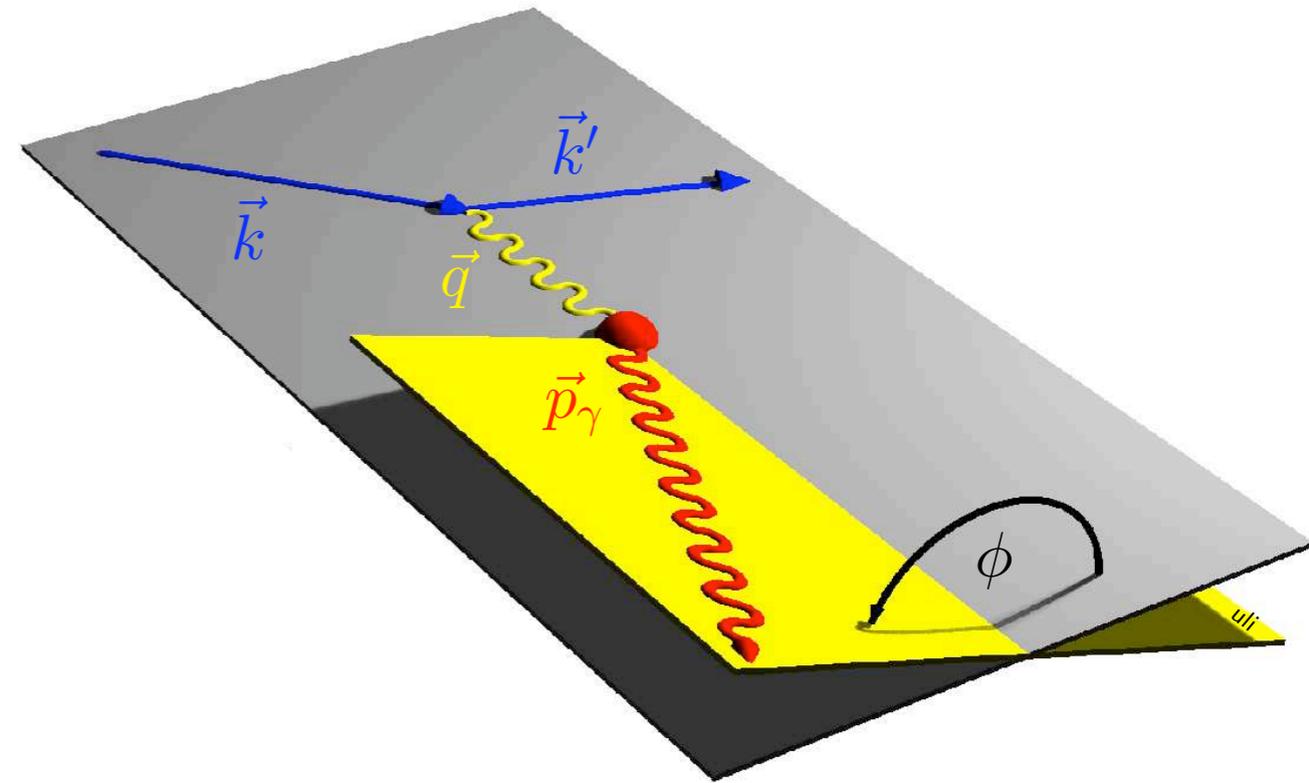
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$$|\mathcal{T}_{\text{DVCS}}|^2 = K_{\text{DVCS}} \left[\sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi) + P_B \sum_{n=1}^1 s_n^{\text{DVCS}} \sin(n\phi) \right]$$

Azimuthal dependences in DVCS/BH

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Fourier expansion for ϕ :

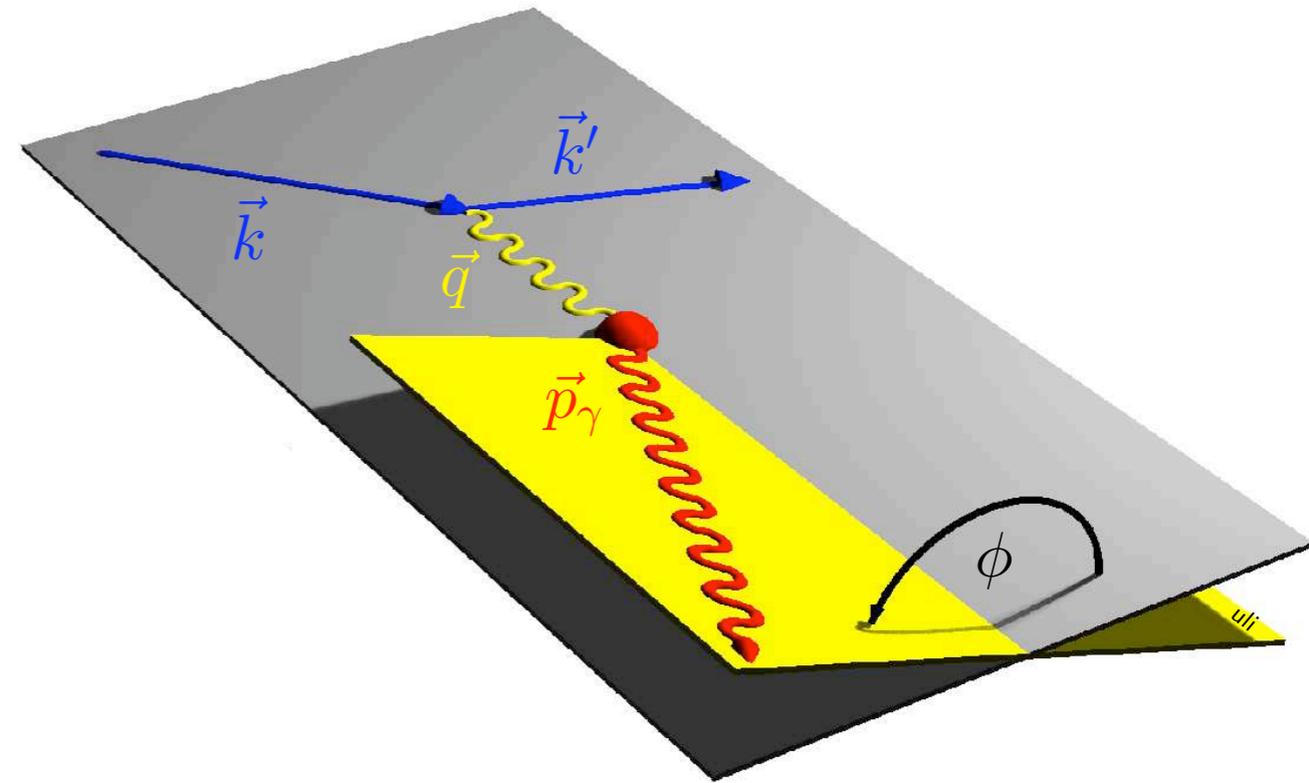
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$$\mathcal{I} = \frac{C_B K_{\mathcal{I}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left[\sum_{n=0}^3 c_n^{\mathcal{I}} \cos(n\phi) + P_B \sum_{n=1}^2 s_n^{\mathcal{I}} \sin(n\phi) \right]$$

Azimuthal dependences in DVCS/BH

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- beam charge C_B
- here: unpolarized target



Fourier expansion for ϕ :

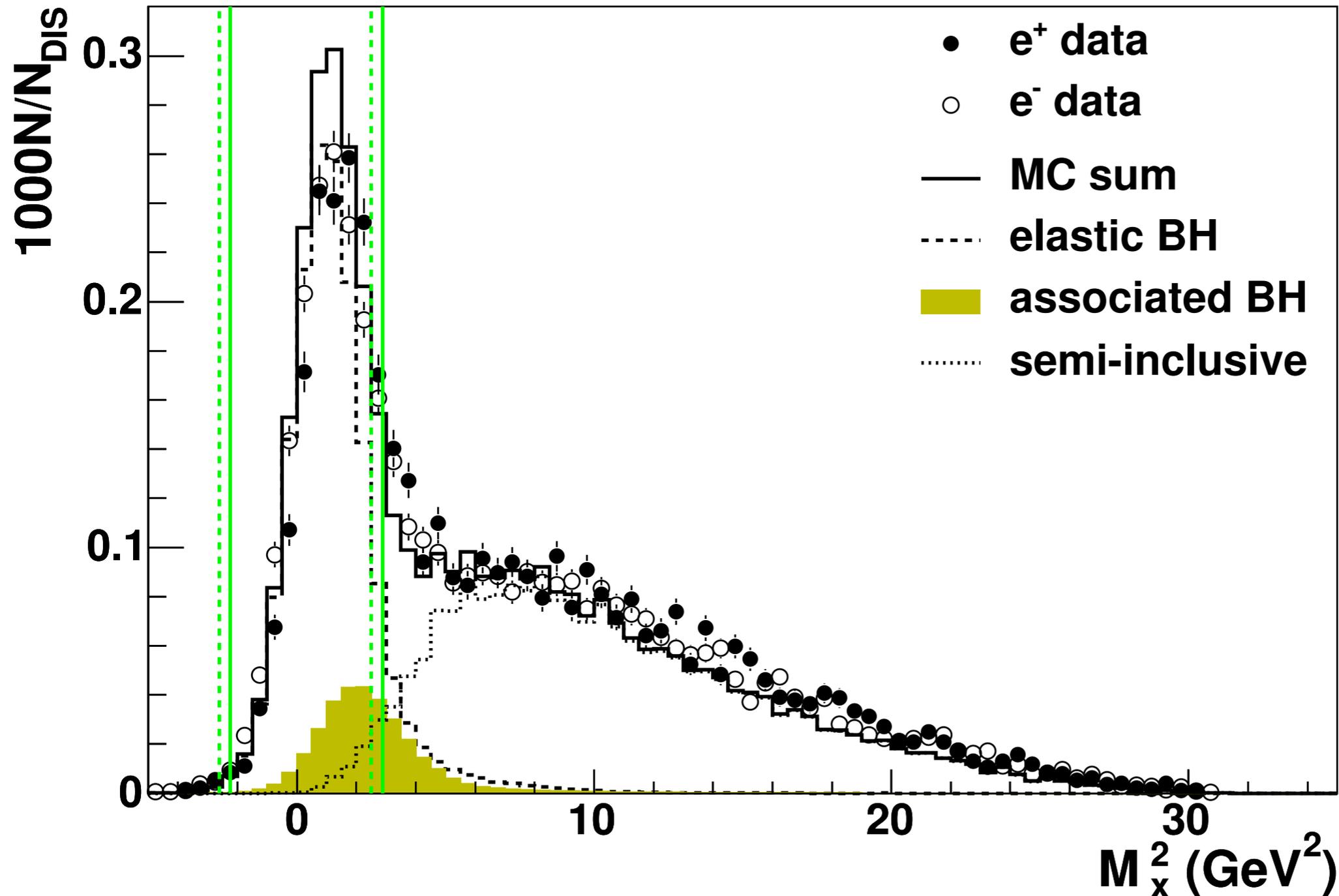
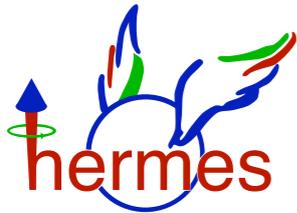
$$|\mathcal{T}_{\text{BH}}|^2 = \frac{K_{\text{BH}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \sum_{n=0}^2 c_n^{\text{BH}} \cos(n\phi)$$

$$|\mathcal{T}_{\text{DVCS}}|^2 = K_{\text{DVCS}} \left[\sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi) + P_B \sum_{n=1}^1 s_n^{\text{DVCS}} \sin(n\phi) \right]$$

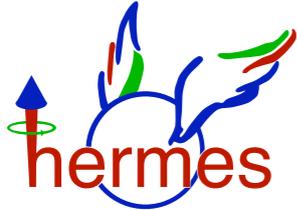
$$\mathcal{I} = \frac{C_B K_{\mathcal{I}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left[\sum_{n=0}^3 c_n^{\mathcal{I}} \cos(n\phi) + P_B \sum_{n=1}^2 s_n^{\mathcal{I}} \sin(n\phi) \right]$$

bilinear ("DVCS") or linear in GPDs

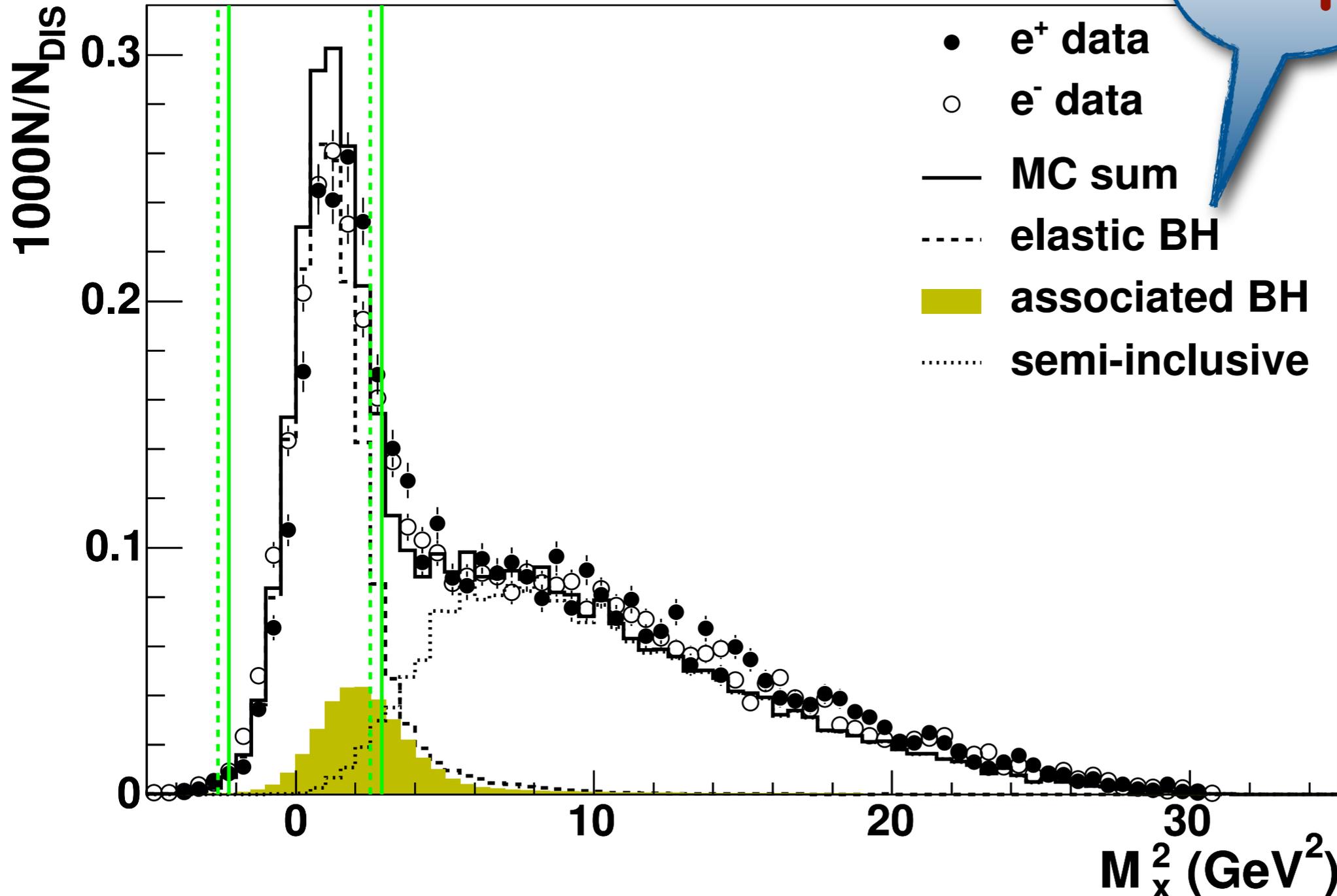
Exclusivity: missing-mass technique



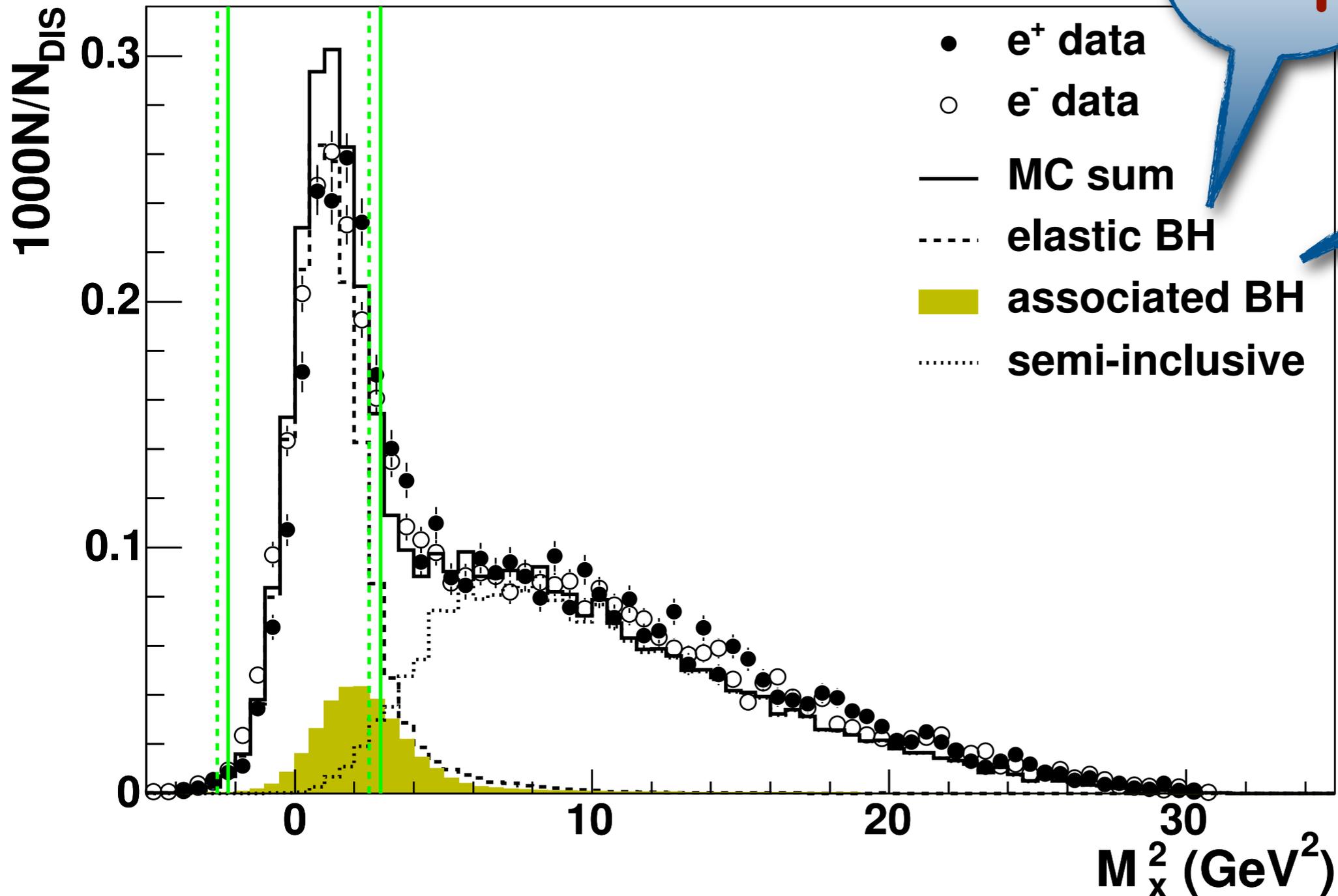
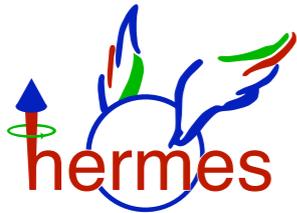
Exclusivity: missing-mass technique



$X=p$



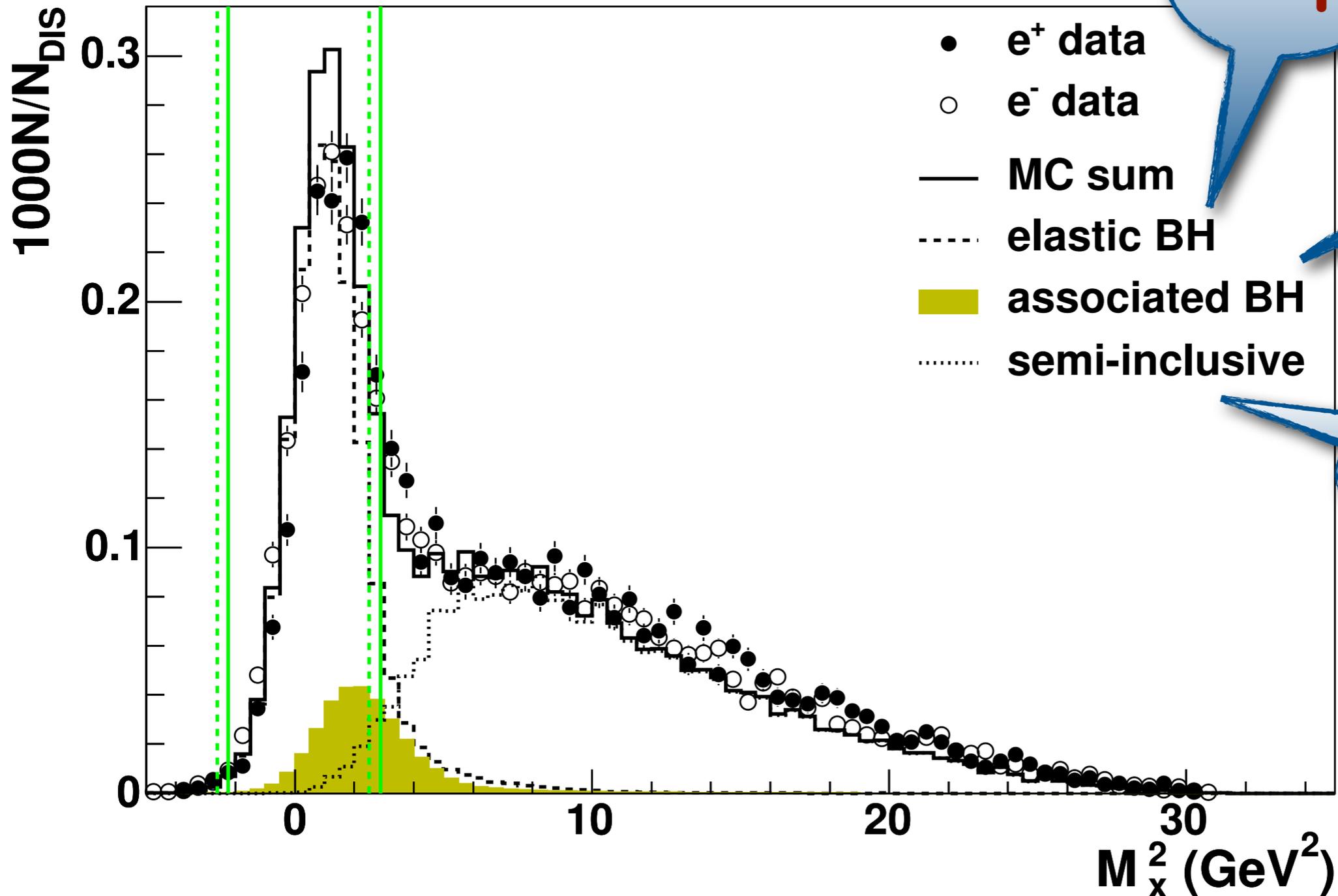
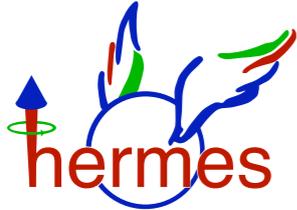
Exclusivity: missing-mass technique



$X=p$

$X=\Delta^+$

Exclusivity: missing-mass technique

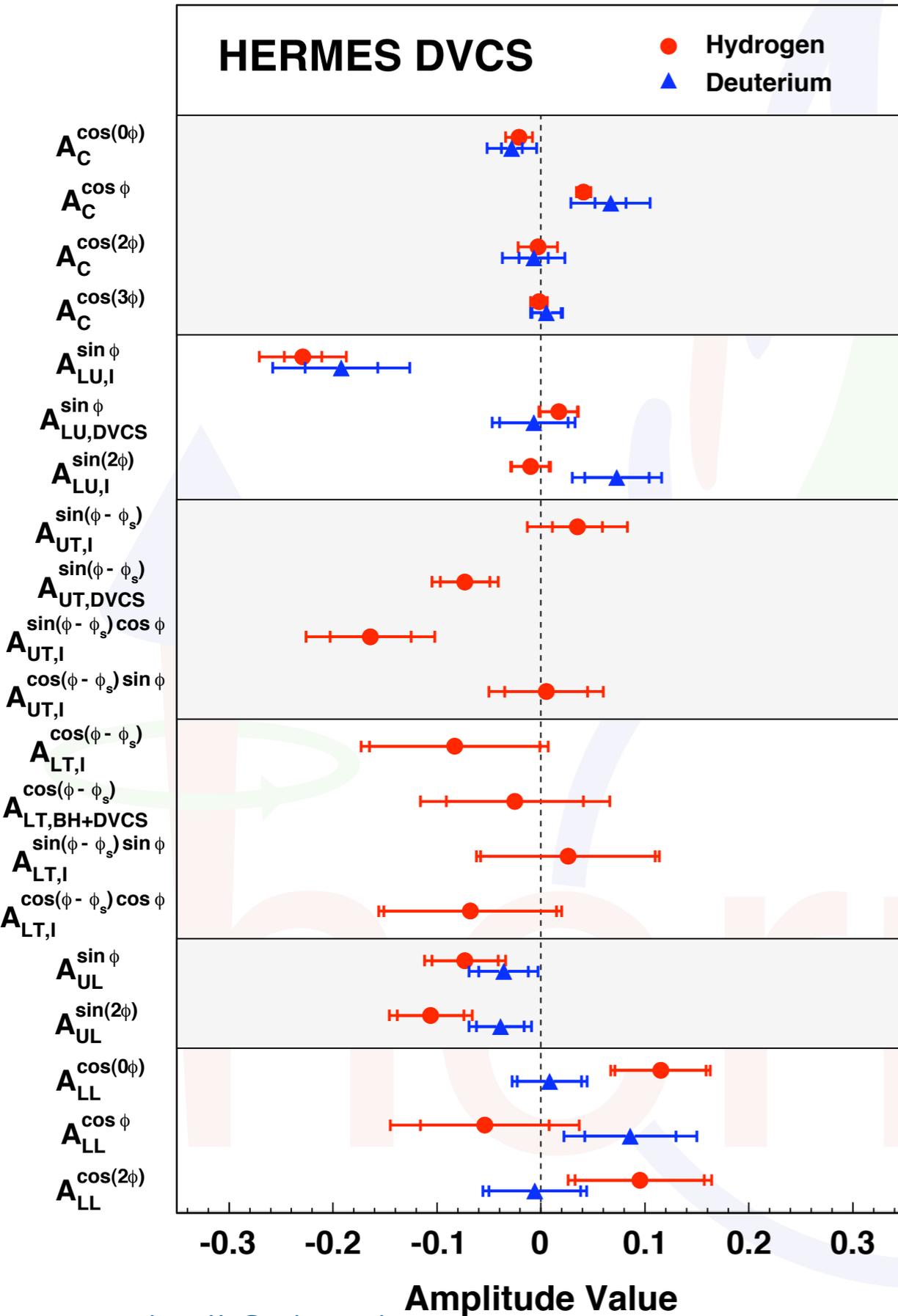


$X=p$

$X=\Delta^+$

$X=\pi^0 + \dots$

A wealth of azimuthal amplitudes



Beam-charge asymmetry:

PRD 75 (2007) 011103

GPD H

NPB 829 (2010) 1

JHEP 11 (2009) 083

Beam-helicity asymmetry:

PRC 81 (2010) 035202

GPD H

PRL 87 (2001) 182001

Transverse target spin asymmetries:

GPD E from proton target

JHEP 06 (2008) 066

PLB 704 (2011) 15

Longitudinal target spin asymmetry:

GPD \tilde{H}

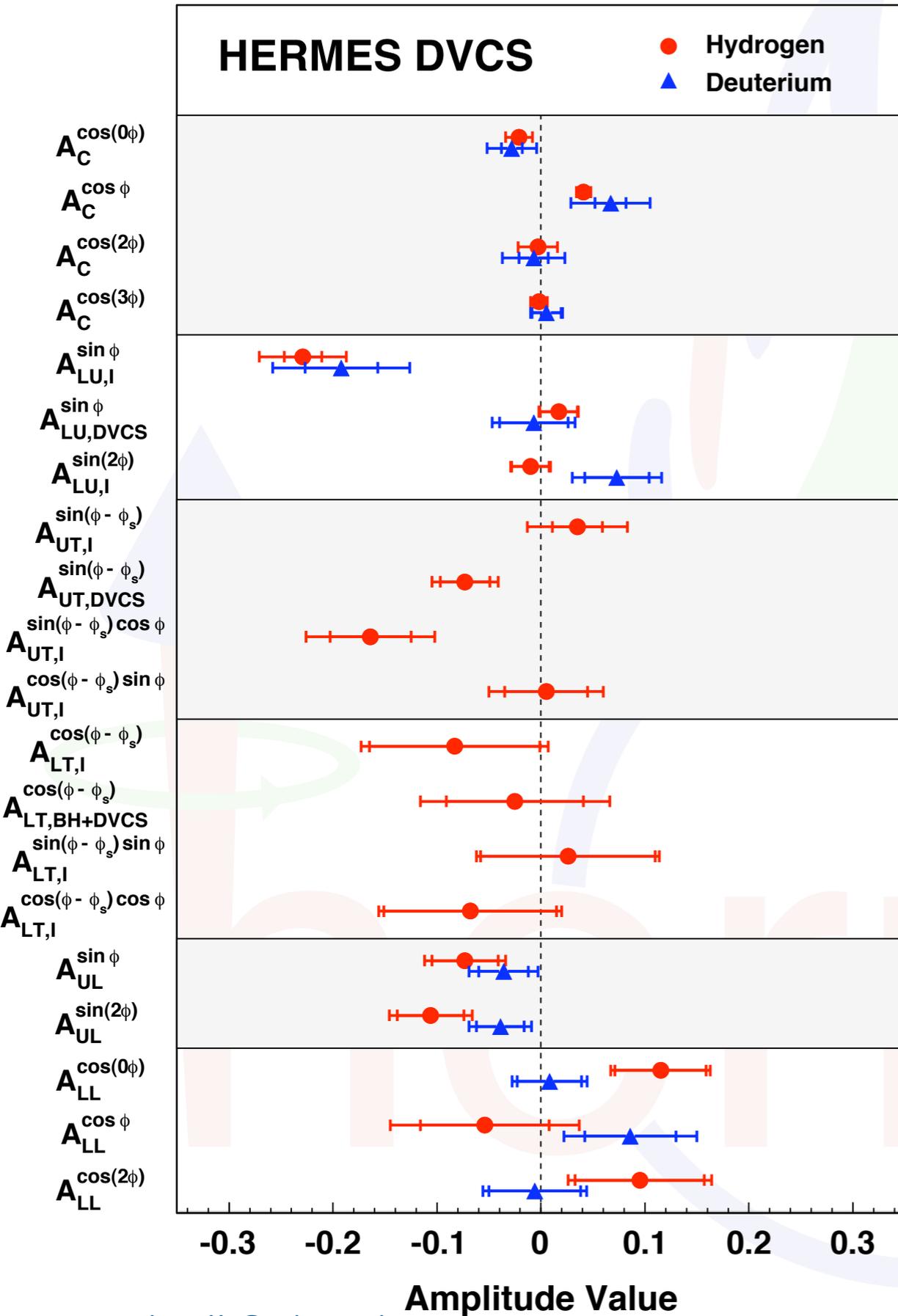
JHEP 06 (2010) 019

Double-spin asymmetry:

GPD \tilde{H}

NPB 842 (2011) 265

A wealth of azimuthal amplitudes



Beam-charge asymmetry:

PRD 75 (2007) 011103

GPD H

NPB 829 (2010) 1

JHEP 11 (2009) 083

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JHEP 06 (2010) 019

Double-spin asymmetry:

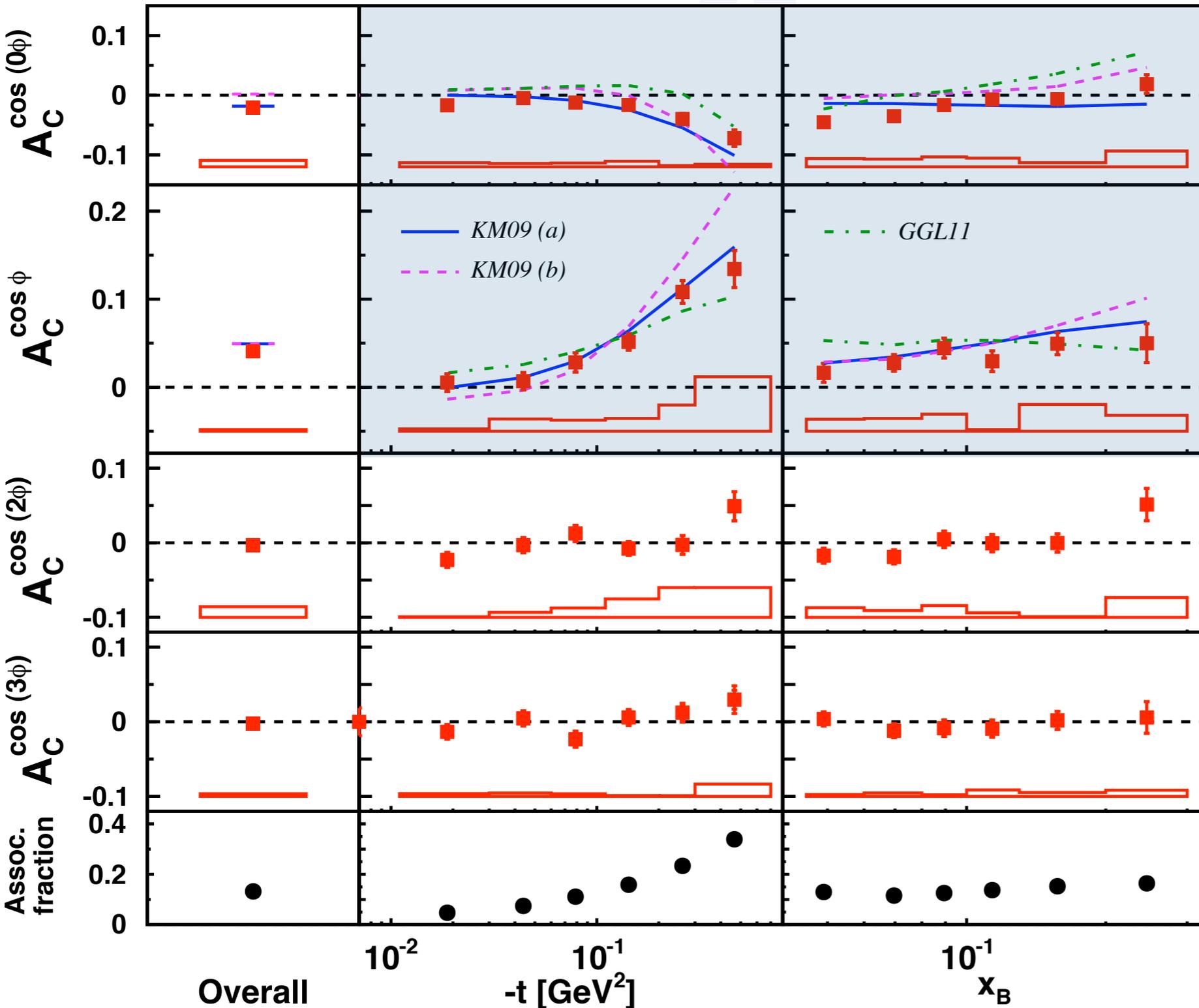
GPD \tilde{H}

NPB 842 (2011) 265

complete data set!

Beam-charge asymmetry

[Airapetian et al., accept. by JHEP; arXiv:1203.6287]



constant term:

$$\propto -A_C^{\cos \phi}$$

$$\propto \text{Re}[F_1 \mathcal{H}]$$

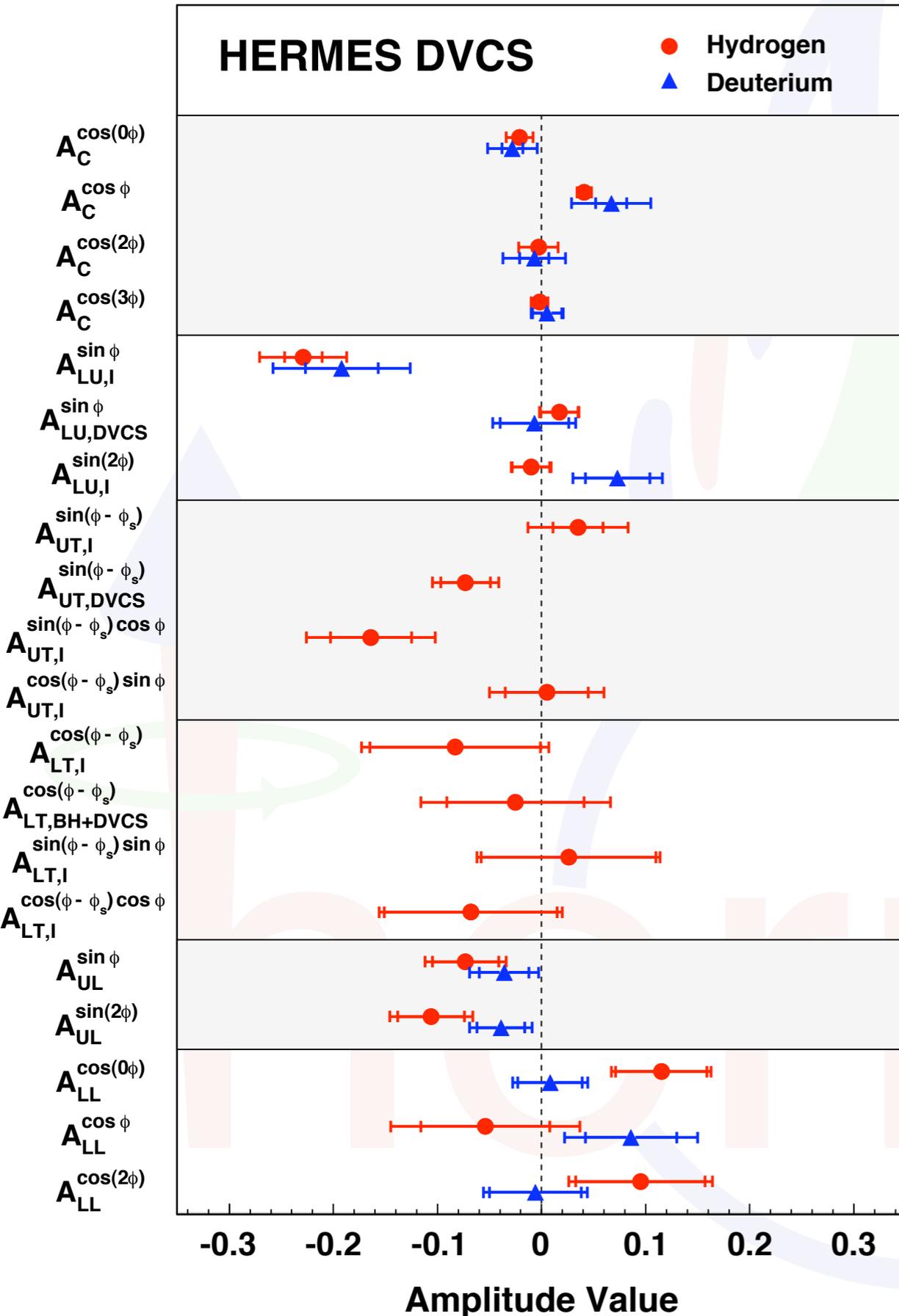
[higher twist]

[gluon leading twist]

Resonant fraction:



A wealth of azimuthal amplitudes



Beam-charge asymmetry:

GPD H

PRD 75 (2007) 011103

NPB 829 (2010) 1

JHEP 11 (2009) 083

PRC 81 (2010) 035202

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PLB 704 (2011) 15

Longitudinal target spin asymmetry:

GPD \tilde{H}

JHEP 06 (2010) 019

Double-spin asymmetry:

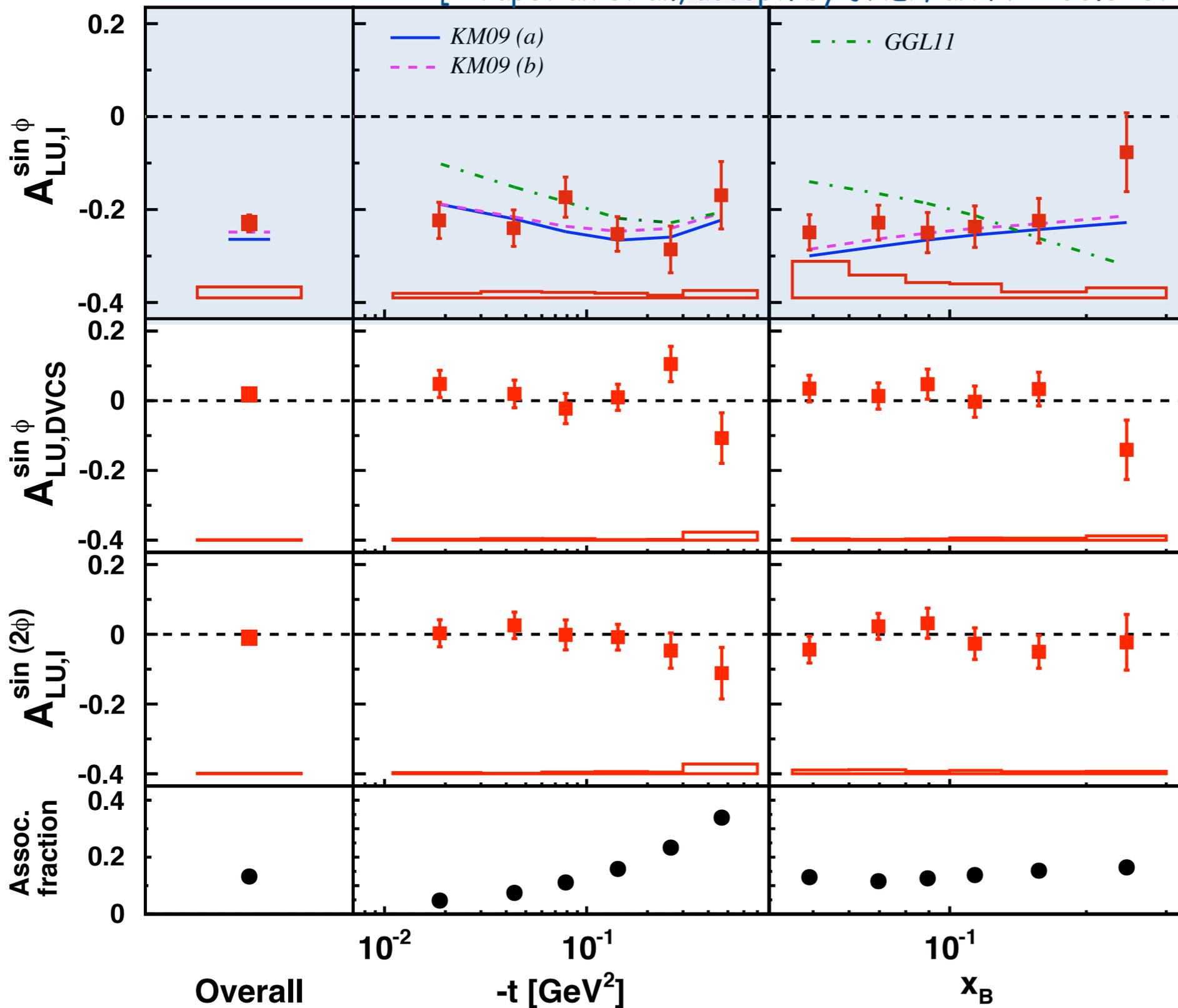
GPD \tilde{H}

NPB 842 (2011) 265

complete data set!

Beam-spin asymmetry

[Airapetian et al., accept. by JHEP; arXiv:1203.6287]



$\propto \text{Im}[F_1 \mathcal{H}]$

[higher twist]

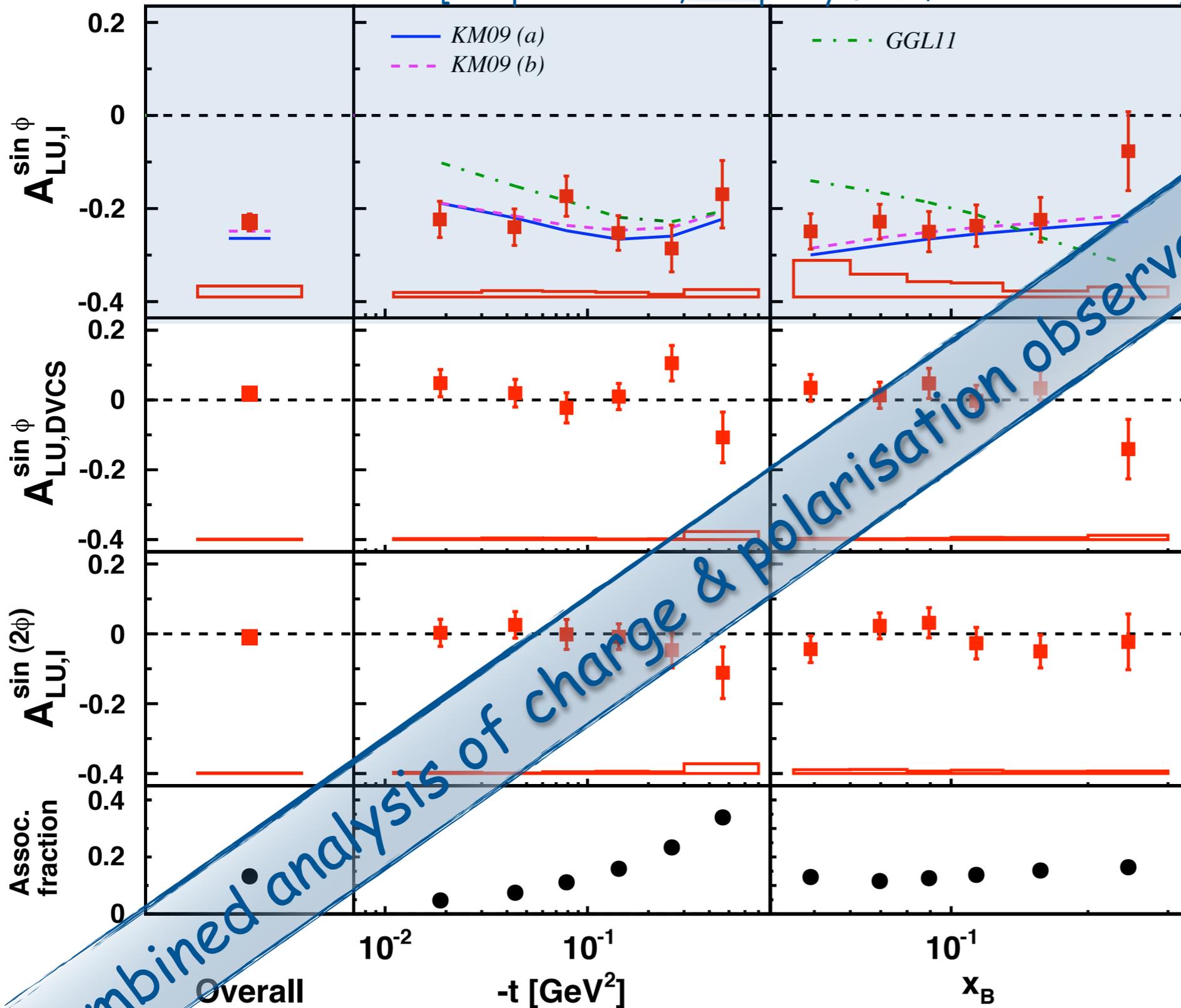
Resonant fraction:



complete data set!

Beam-spin asymmetry

[Airapetian et al., accept. by JHEP; arXiv:1203.6287]



combined analysis of charge & polarisation observables unique to HERA!

$\alpha \text{Im}[F_1 \mathcal{H}]$

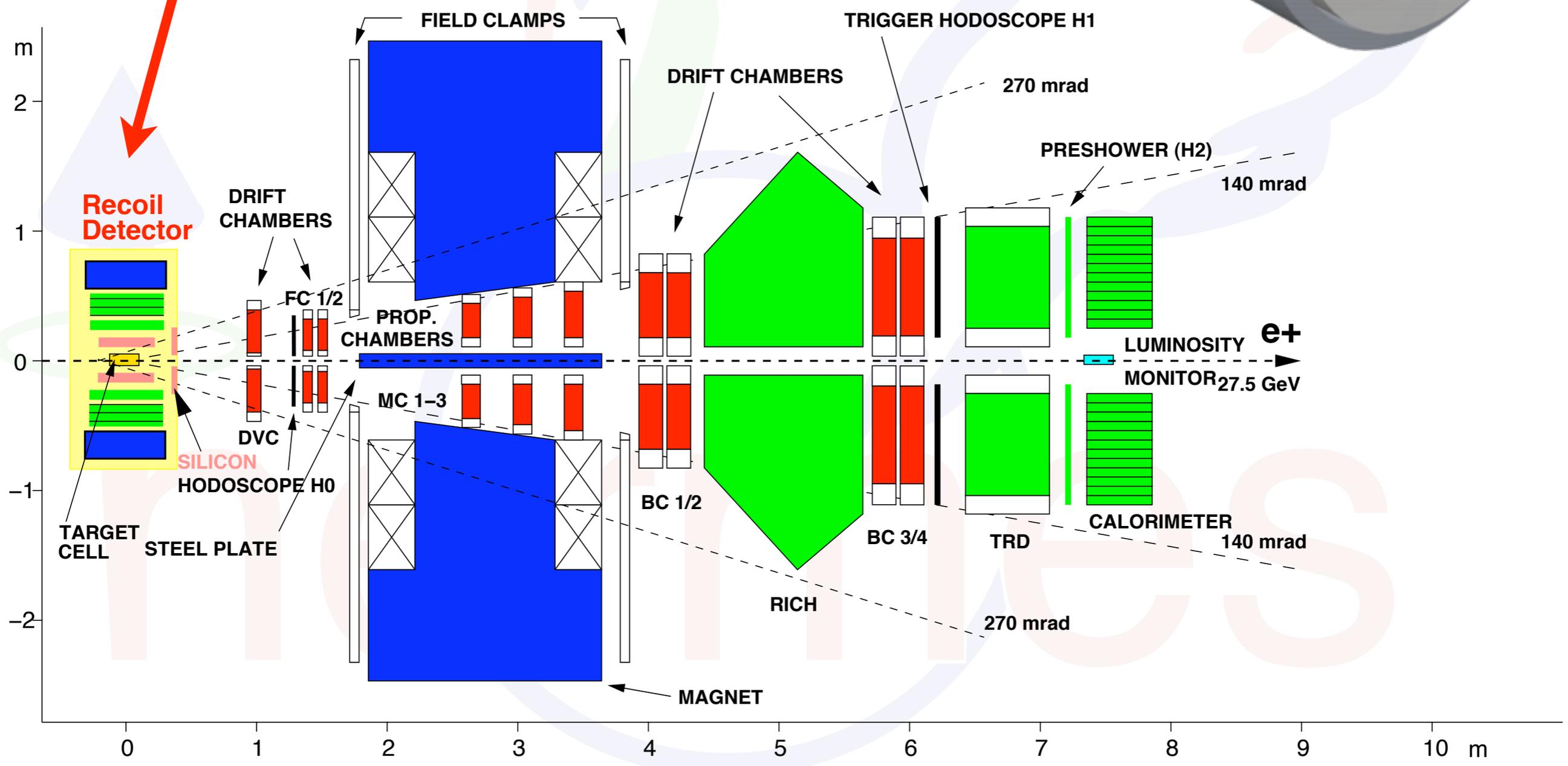
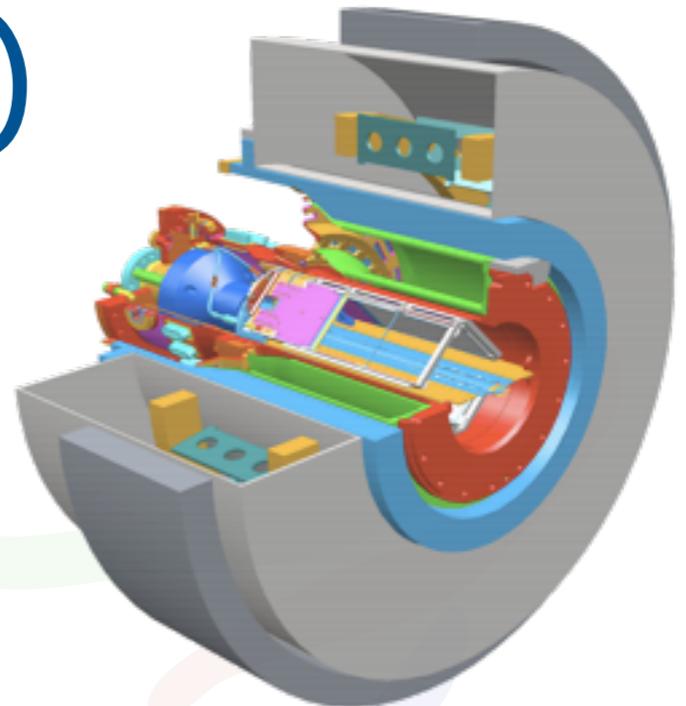
[higher twist]

Resonant fraction:

$$ep \rightarrow e\Delta^+\gamma$$

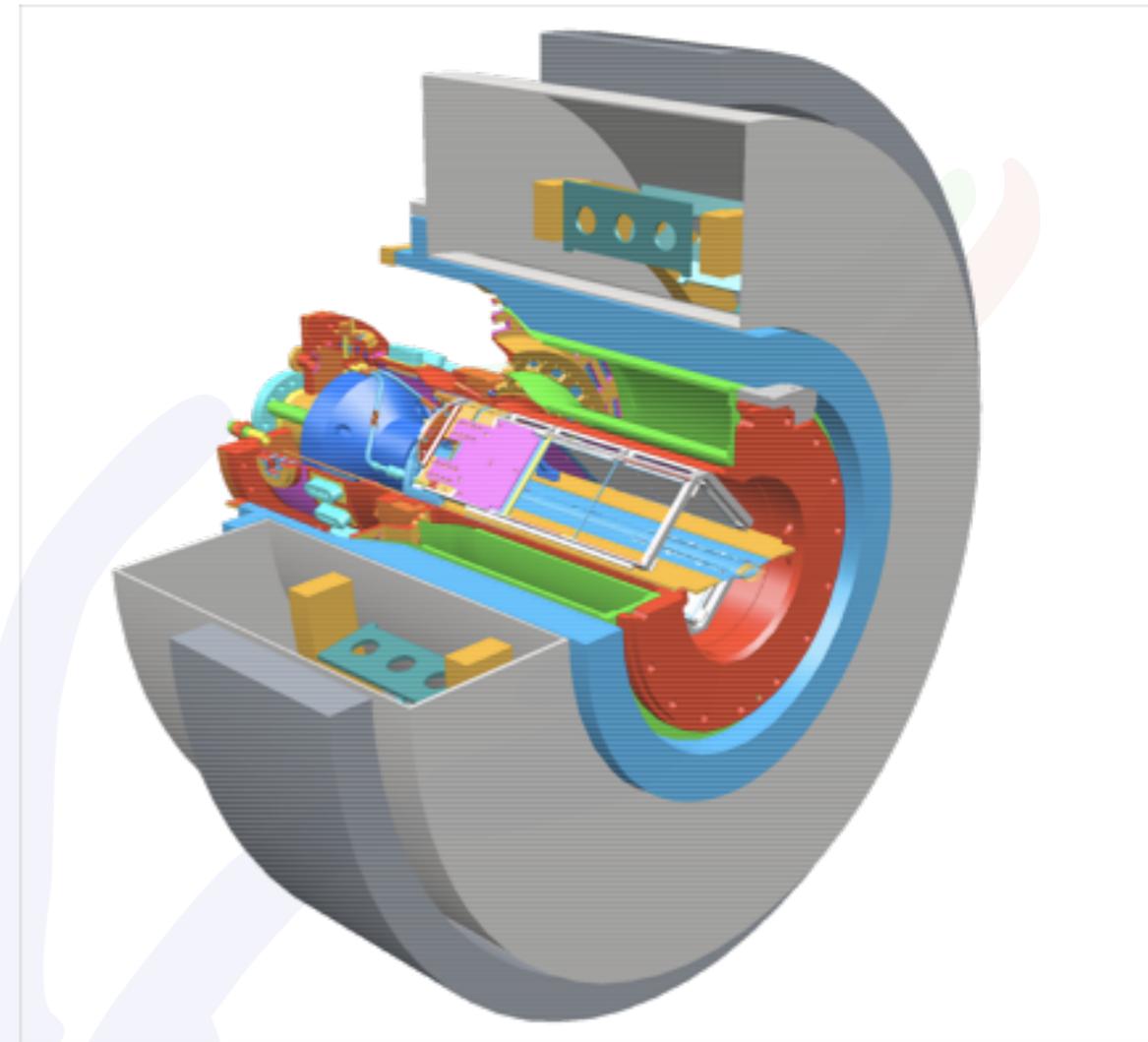
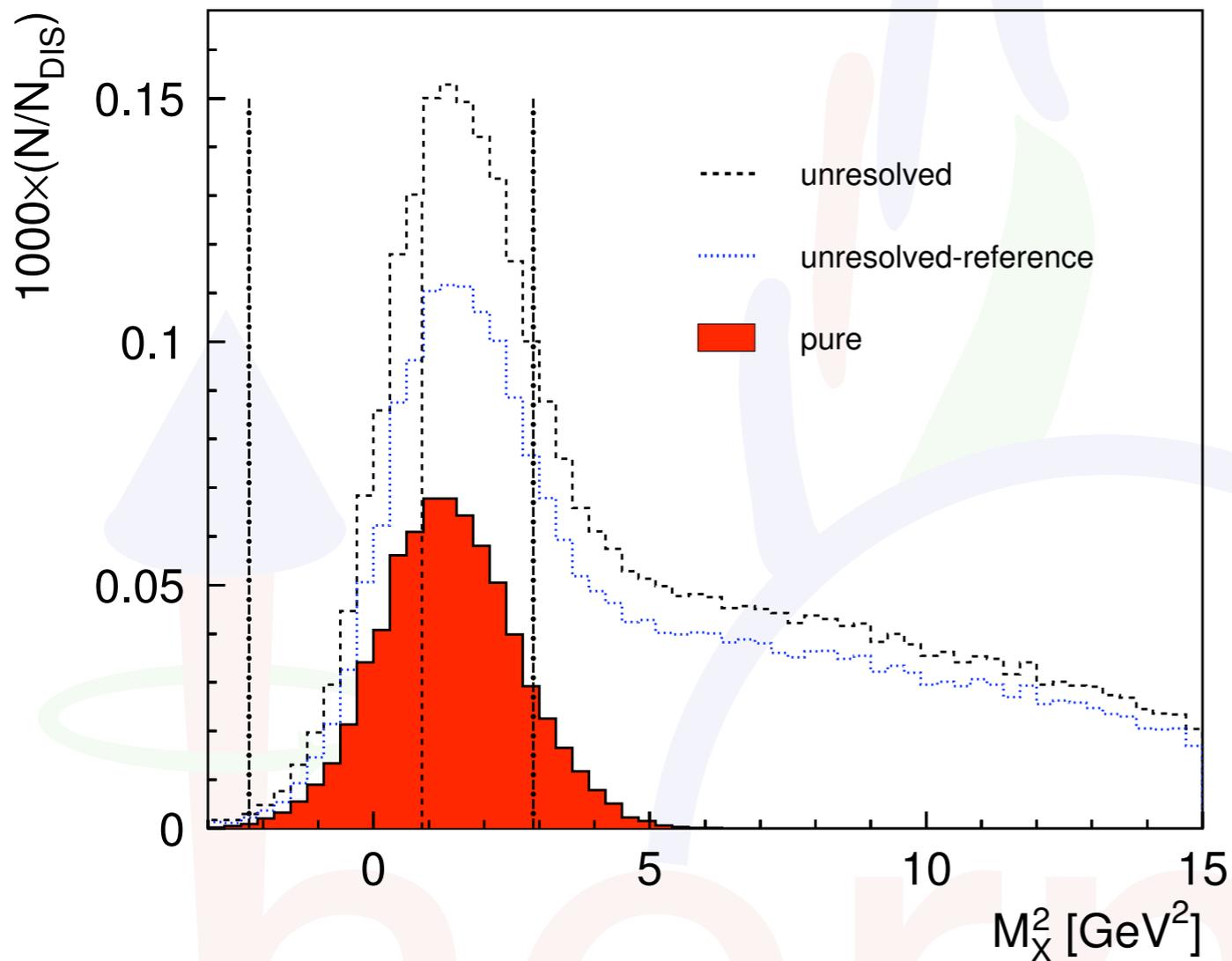
HERMES detector (2006/07)

detection of recoiling proton



HERMES detector (2006/07)

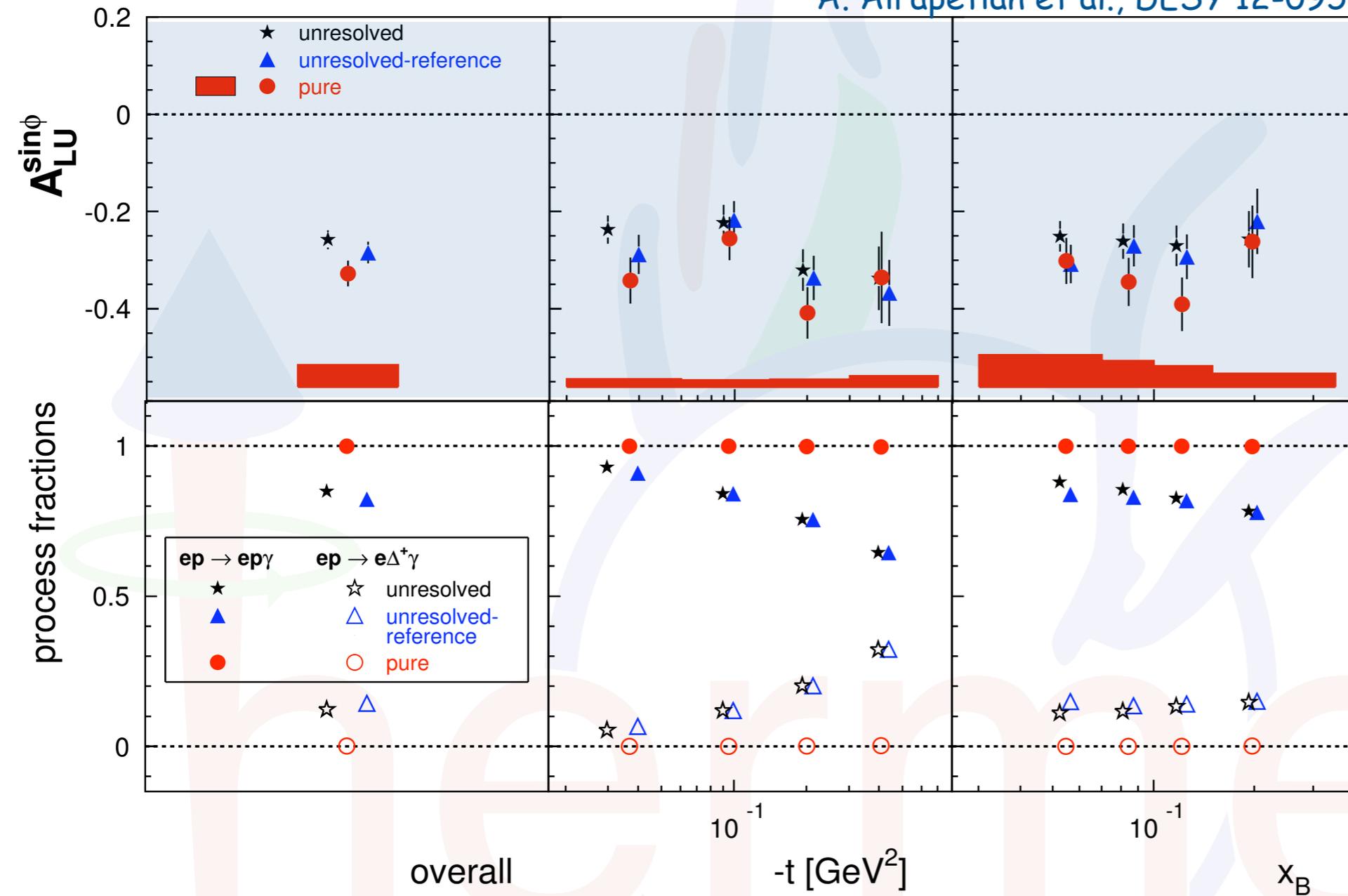
kinematic fitting



- All particles in final state detected → 4 constraints from energy-momentum conservation
- Selection of **pure BH/DVCS** ($ep \rightarrow ep \gamma$) with high efficiency (**~83%**)
- Allows to suppress background from associated and semi-inclusive processes to a negligible level (**<0.2%**)

DVCS with recoil detector

A. Airapetian et al., DESY 12-095

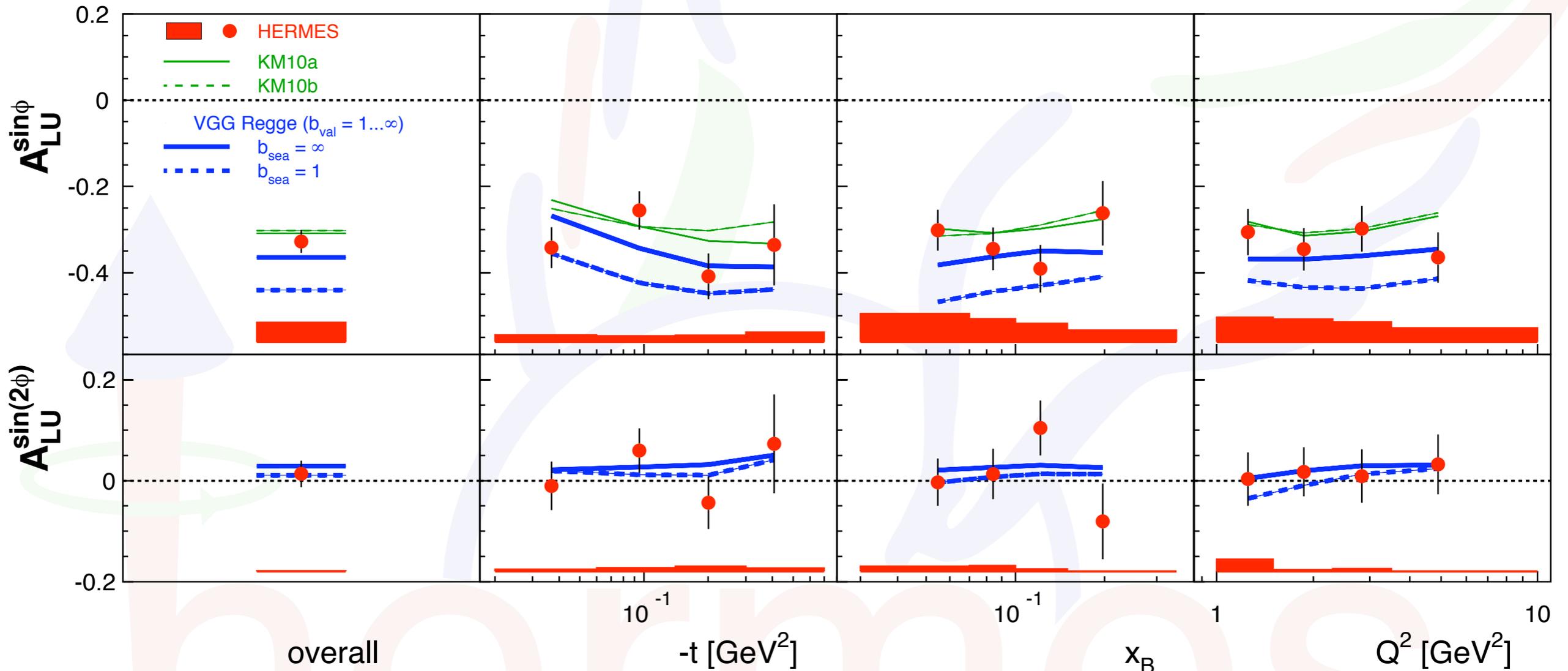


indication of larger amplitudes for pure sample
 (-> assoc. in trad. analysis mainly dilution)

basically no contamination
 -> clear interpretation

DVCS with recoil detector

A. Airapetian et al., DESY 12-095



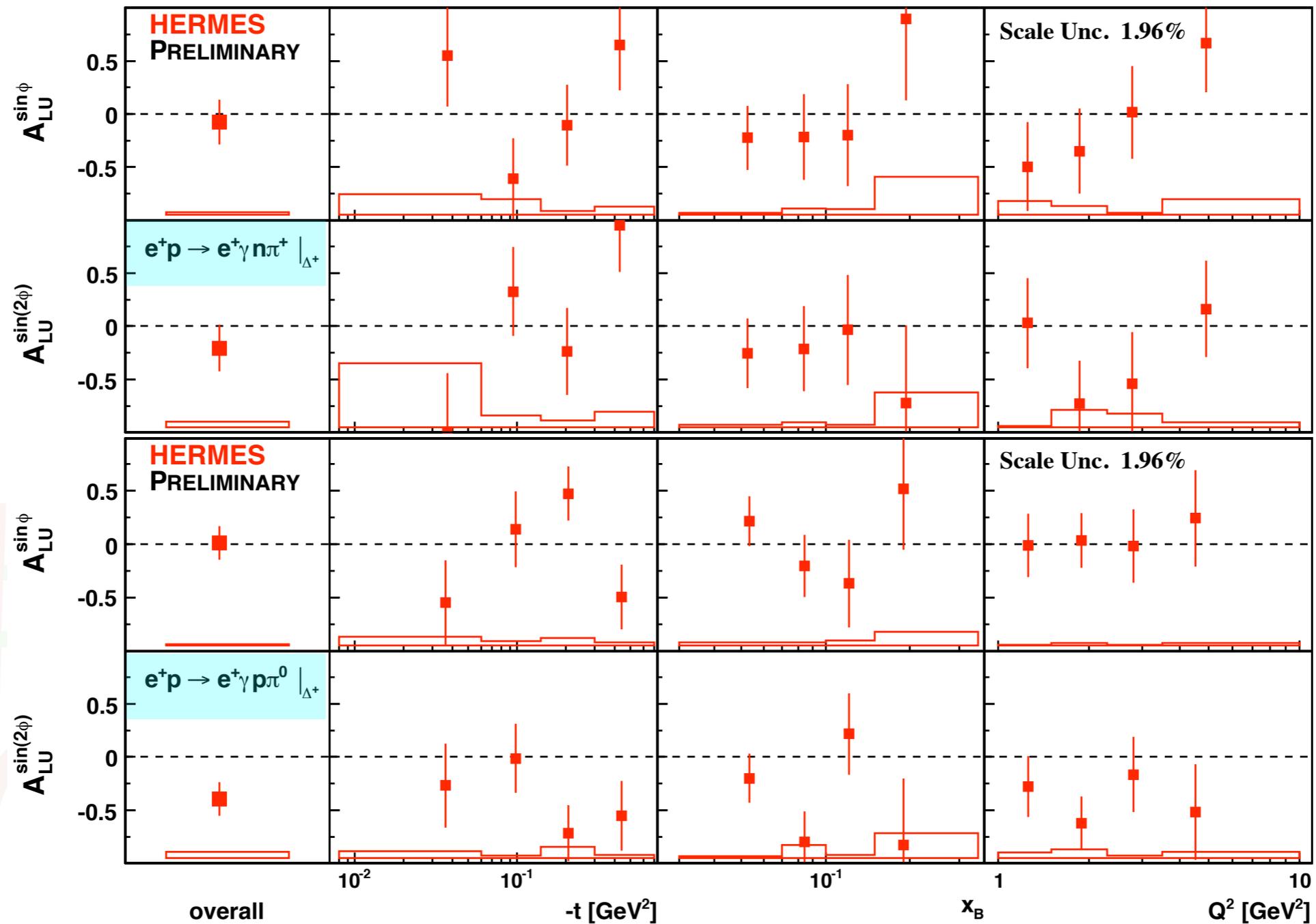
good agreement with models

KM10 - K. Kumericki and D. Müller, Nucl. Phys. B 841 (2010) 1

VGG - M. Vanderhaeghen et al., Phys. Rev. D 60 (1999) 094017

Associated DVCS with recoil detector

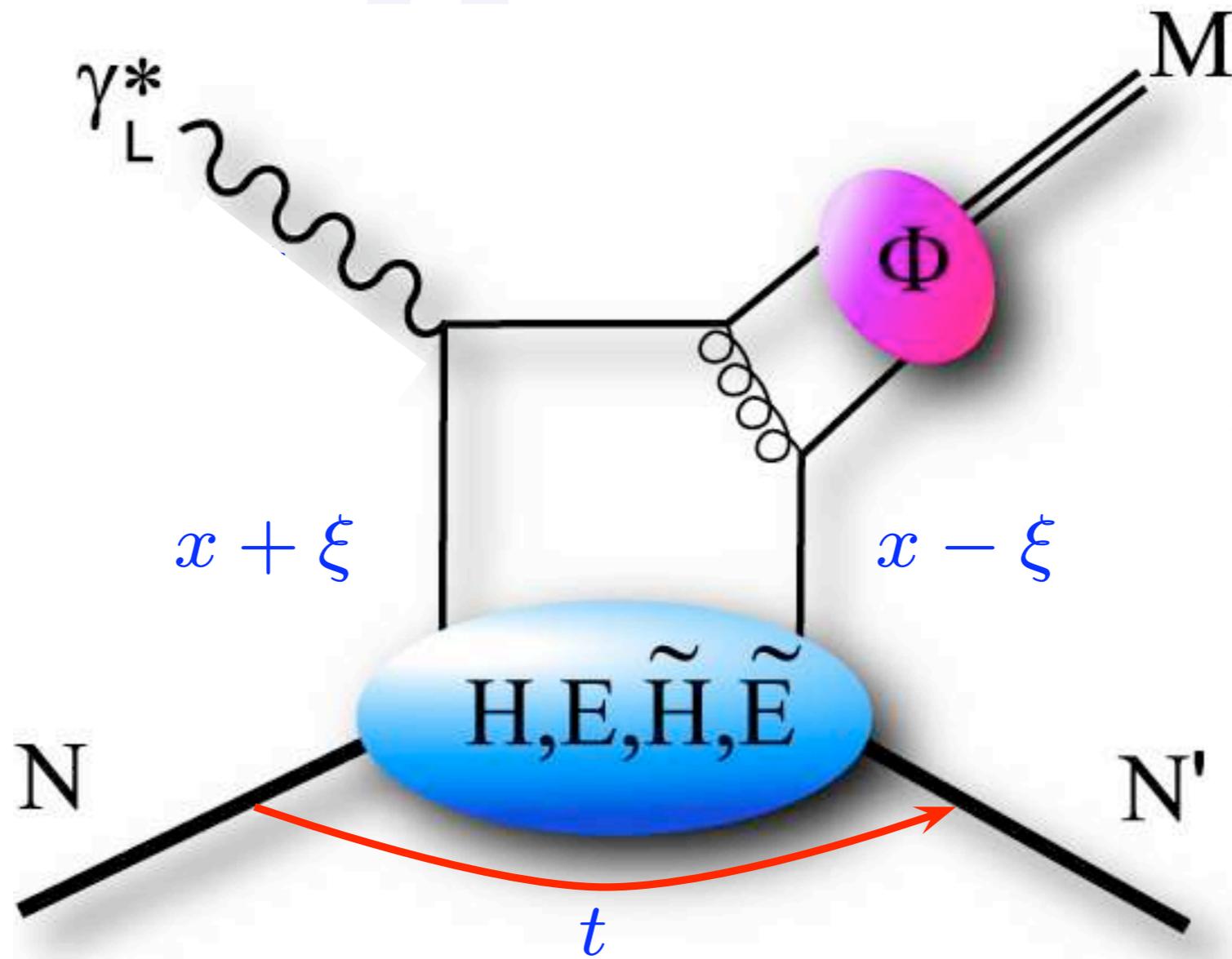
study background process for traditional analyses



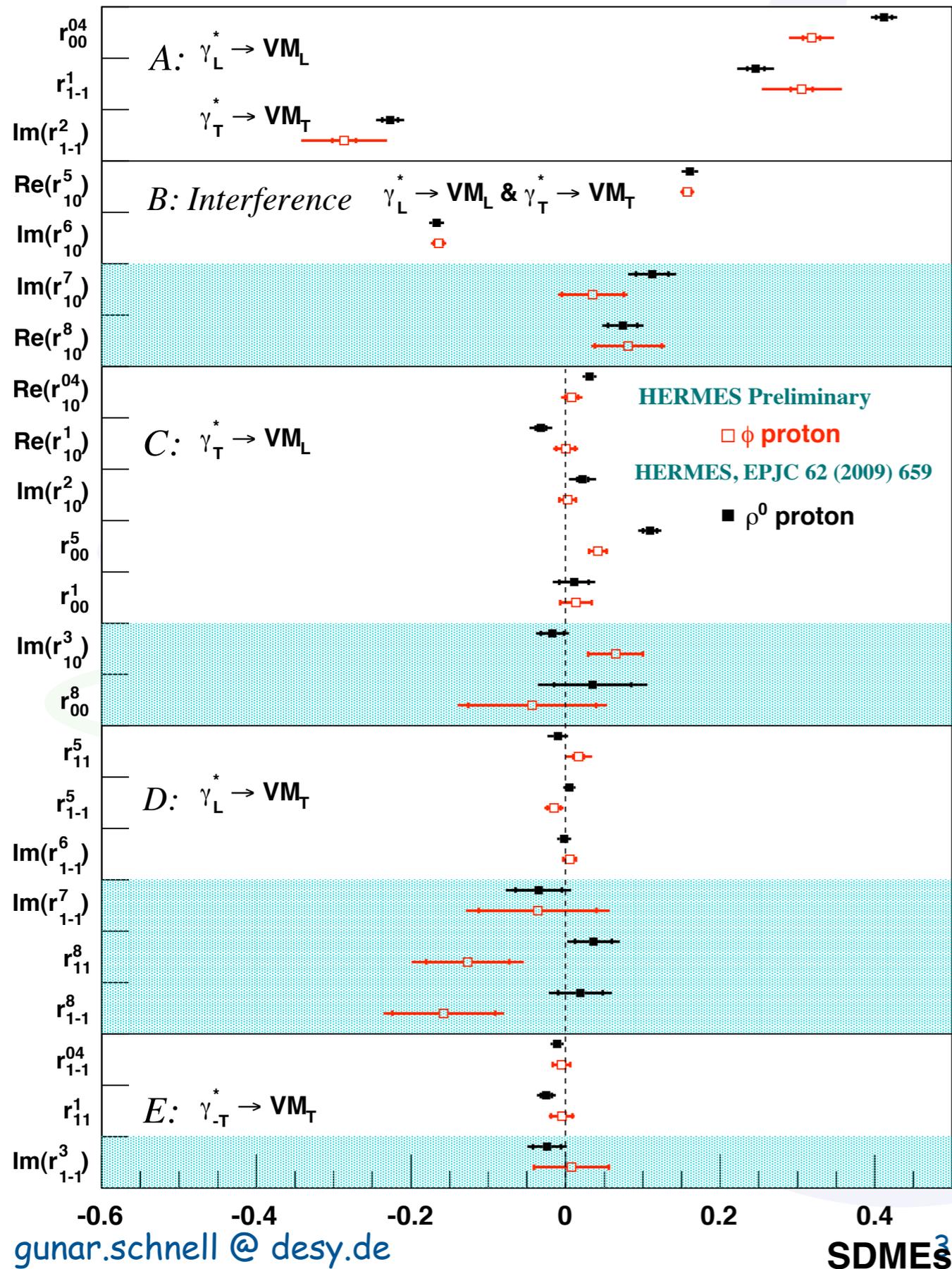
- asymmetry amplitudes consistent with zero

- consistent with pure DVCS results (e.g., dilution in traditional analysis)

Exclusive meson production

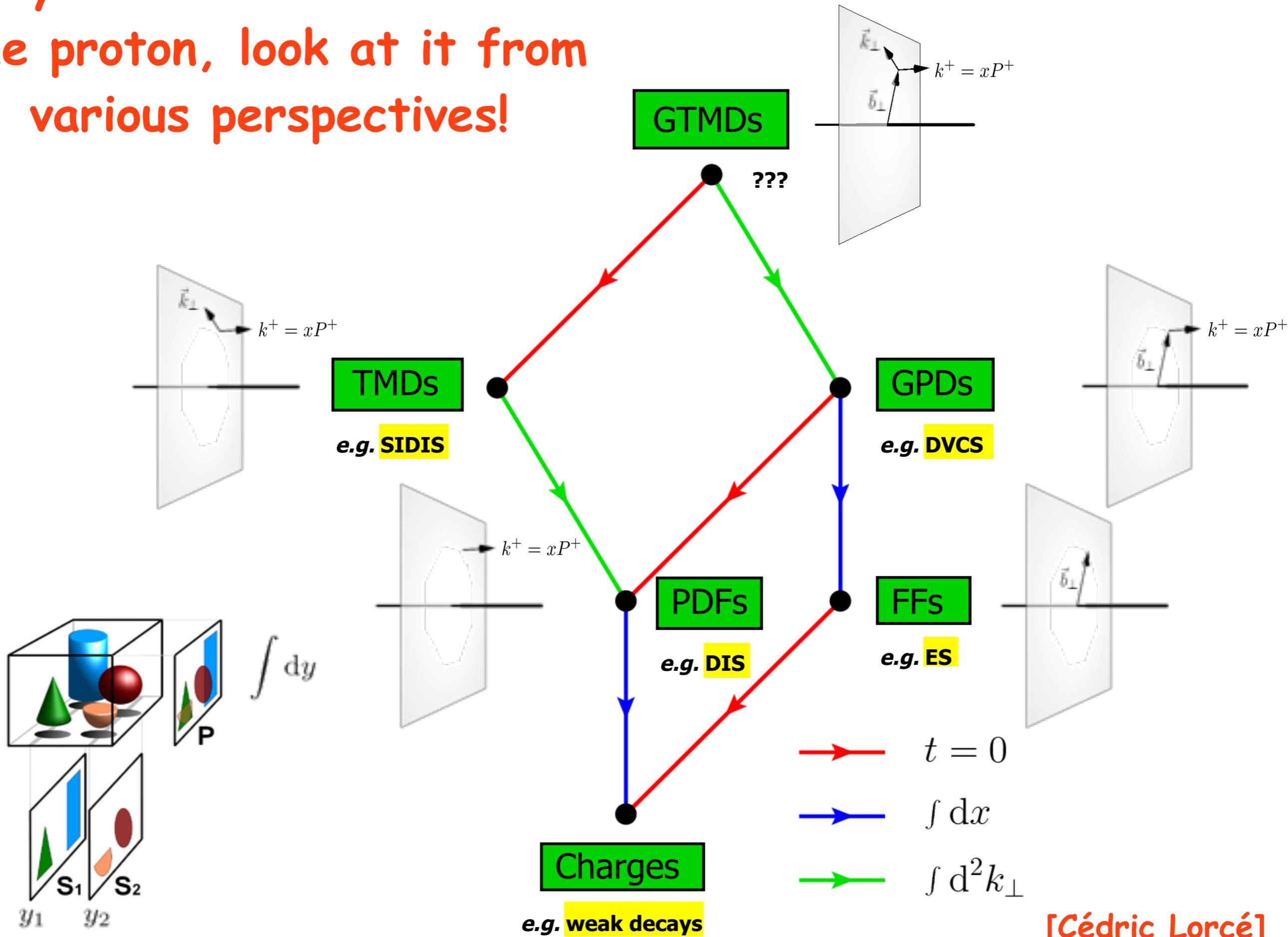


SDMEs for phi production



- (decay) angular distributions reveal helicity transitions
- similar to rho production: helicity-conserving SDMEs dominate
- hardly any violation of SCHC observed for phi

If you want to understand the proton, look at it from various perspectives!



[Cédric Lorcé]

