

# Monte Carlo Methods

in Natural Sciences, Engineering and Economics

19-21 February 2013

DESY Hamburg

## Uncertainty quantification and going beyond the independent-particle approximation

*What's hot and new in a mature field*

*Monte Carlo for particle transport in particle/nuclear/astro/medical/etc. physics*

Maria Grazia Pia

Paolo Saracco

*INFN Genova, Italy*

**Implicit throughout this talk**

**Monte Carlo**

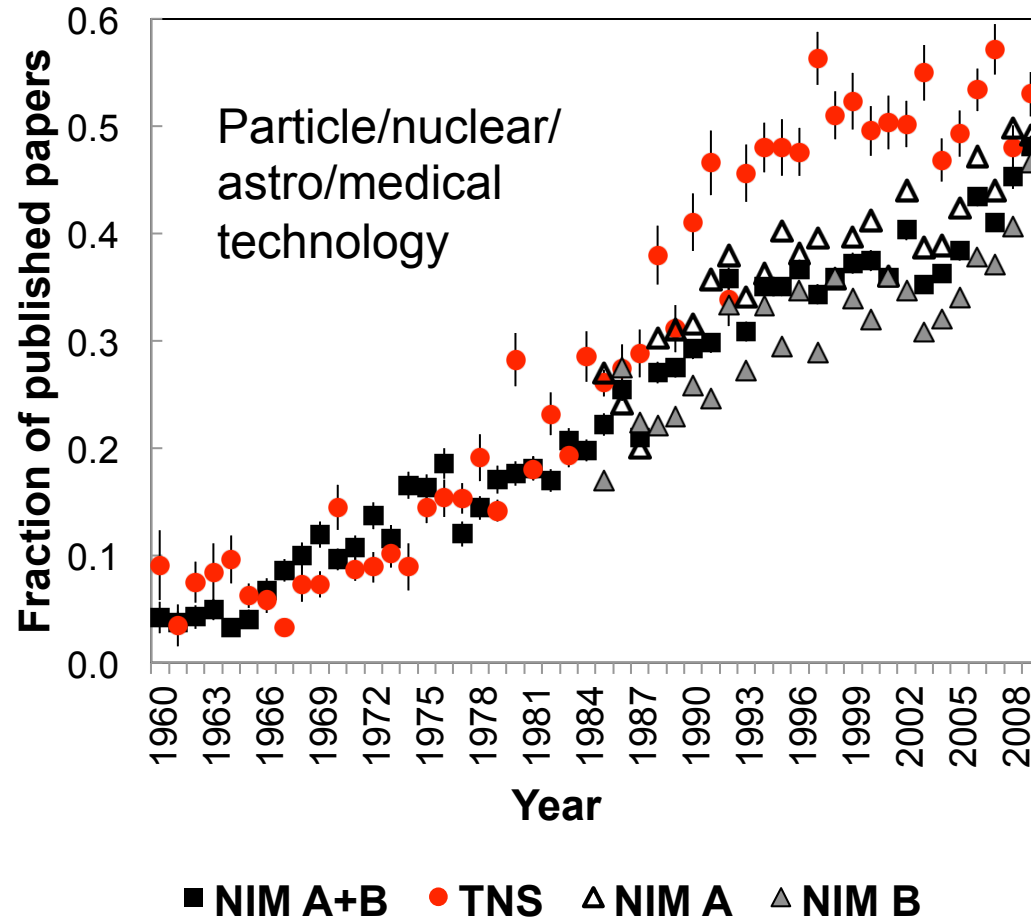


**Monte Carlo for particle transport  
in matter**

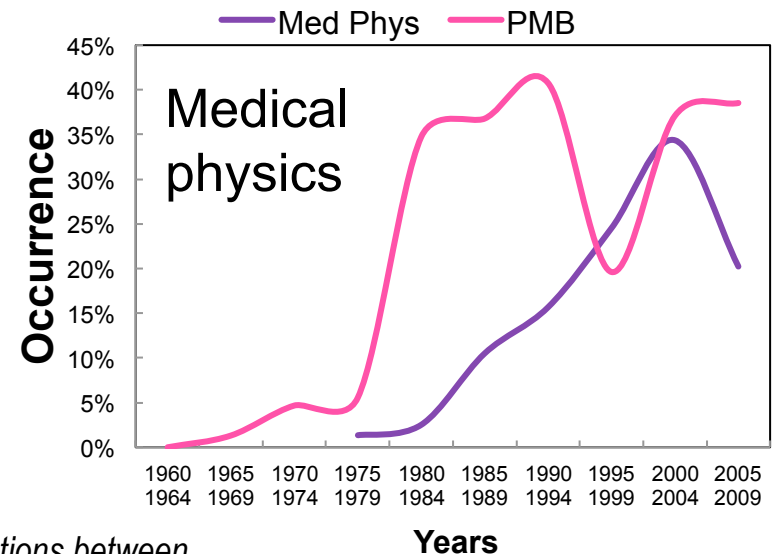
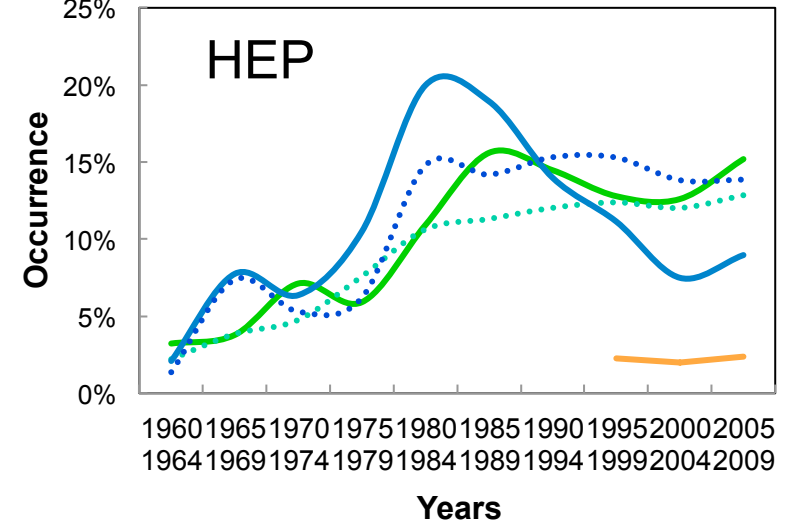
# Monte Carlo in journals

1960-2009

Fraction of papers mentioning  
**Monte Carlo or simulation**



— Phys Rev D    ···· Phys Rev Lett    — Nucl Phys B  
···· Phys Lett B    — APJ



M.G. Pia, T. Basaglia, Z.W. Bell, P.V. Dressendorfer, *The butterfly effect: Correlations between modeling in nuclear-particle physics and socioeconomic factors*, Proc. IEEE NSS 2010

# Nuclear Science & Technology Instruments & Instrumentation

604059 publications

J. P. Biersack, L. L. Haggmark,

**A Monte-Carlo computer-program for the transport of energetic ions in amorphous targets**

*NIM*, vol. 174, no. 1-2, pp. 257-269, 1980

Times Cited: **3661**

S. Agostinelli et al.,

**GEANT4 - a simulation toolkit**

*NIM A*, vol. 506, no. 3, pp. 250-303, 2003

Times Cited: **3640**

L. R. Doolittle,

**Algorithms for the rapid simulation of Rutherford backscattering spectra**

*NIM B*, vol. 9, no. 3, pp. 344-351, 1985

Times Cited: **2095**

*Thomson-Reuters, ISI Web of Science*

*Updated 15 February 2013*

# Physics, Particles & Fields

256905 publications

A. H. Guth,

**Inflationary universe - a possible solution to the horizon and flatness problems**

*Phys. Rev. D*, vol. 23, no. 2, pp. 347-356, 1981

Times Cited: **4,157**

Particle Data Group

**Review of particle physics**

*J. Phys. G*, vol. 33, no. 1 Special Issue, 2006

Times Cited: **3,661**

S. Agostinelli et al.,

**GEANT4 - a simulation toolkit**

*NIM A*, vol. 506, no. 3, pp. 250-303, 2003

Times Cited: **3640**

**Most cited CERN paper**  
(excluding *Rev. Part. Phys.*)

*Thomson-Reuters, ISI Web of Science*  
*Updated 15 February 2013*



An international collaboration of ~ 100 physicists,  
engineers and computer scientists

Laboratories, national institutes and universities

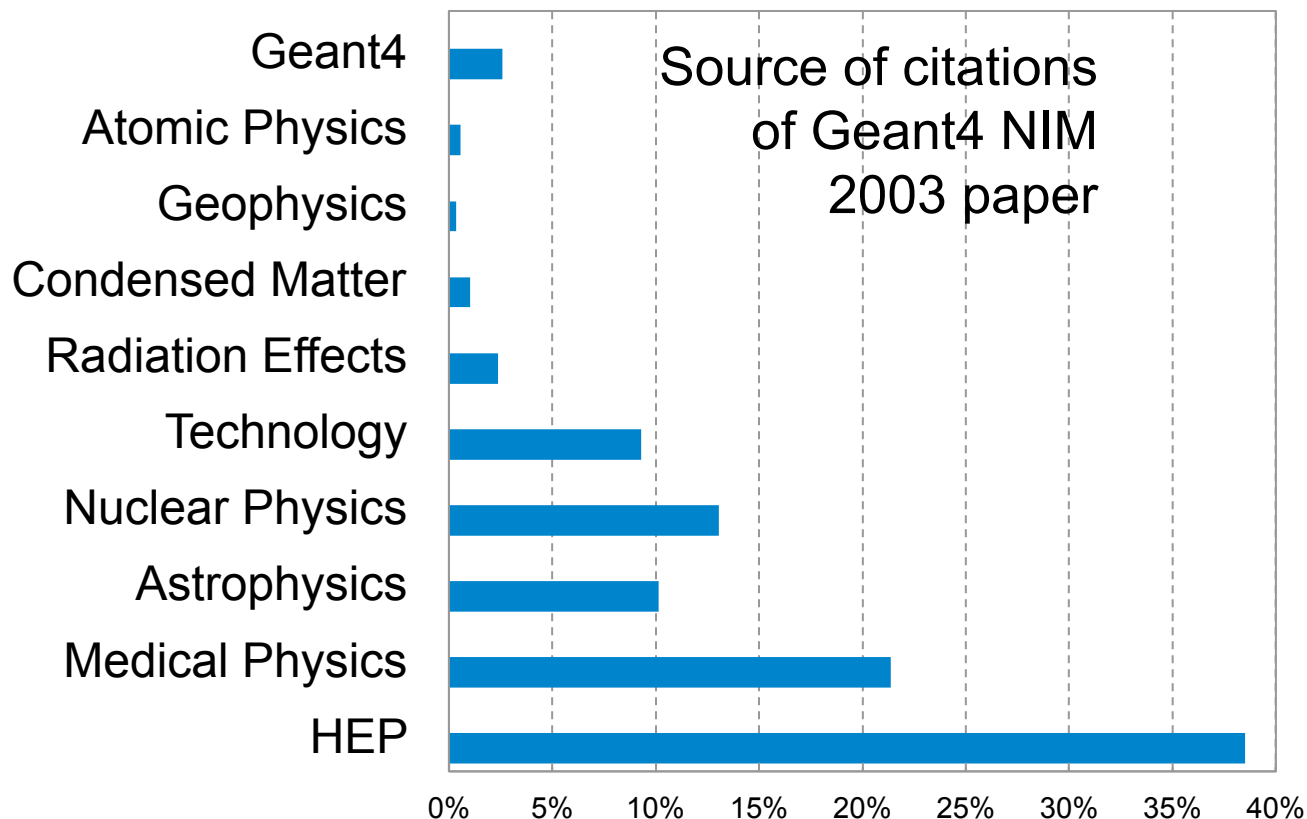
- 1994-1998 RD44 (CERN): R&D phase
- 1<sup>st</sup> public release: 15 December 1998
- 1-2 new versions/year

Open source  
Freely downloadable  
No limitations on use

# Who uses Geant4?

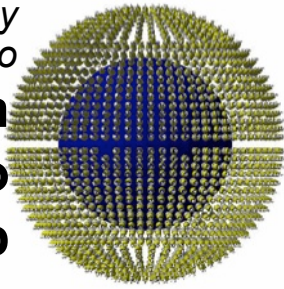
Some degree of subjectivity  
in the classification:

- journal scope
- manual inspection

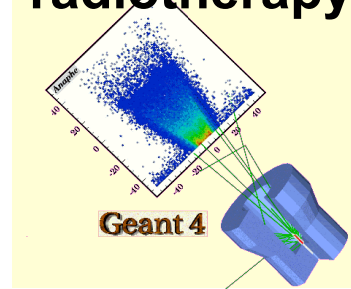


**Update: end 2009** *Roughly similar distribution in recent scientometric data*

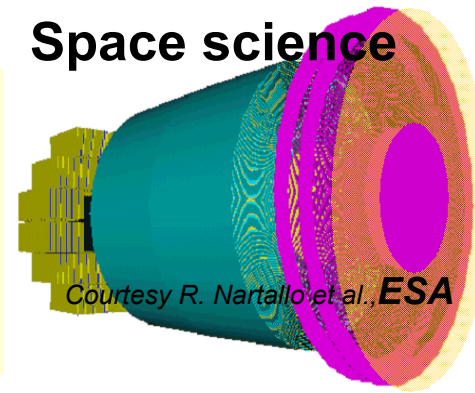
Courtesy  
Borexino  
**Gran  
Sasso  
lab**



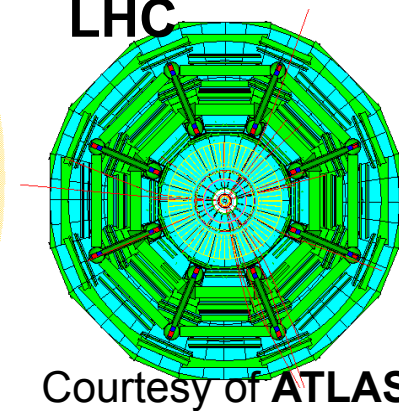
**Oncological  
radiotherapy**



**Space science**



**LHC**



## Simulation in HEP/nuclear/astro experiments

- Fundamental in various domains and phases of an experiment
  - design of the experimental set-up
  - evaluation and definition of the potential physics output of the project
  - evaluation of potential risks to the project
  - development and optimisation of reconstruction and physics analysis software
  - contribution to the calculation and validation of physics results
- Simulation of the passage of particles through matter
  - other kinds of simulation components, such as *physics event generators*, *electronics response* generation, etc.
  - often the simulation of a complex experiment consists of several of these components interfaced to one another



# Basic ingredients

- Modeling the experiment: **geometry + materials**
- **Tracking** particles through matter
- Interaction of particles with matter: **physics** models
- Modeling the detector response
- Run and event control
- Interface to primary event generators
- Accessory utilities (*random number generators, PDG particle data etc.*)
- Visualisation of the set-up, tracks and hits
- User interface
- Persistency

- DPM
- EA-MC
- FLUKA
- GEM
- HERMES
- LAHET
- MCBEND MCU
- MF3D
- NMTC
- MONK
- MORSE
- RTS&T-2000
- SCALE
- TRAX
- VMC++

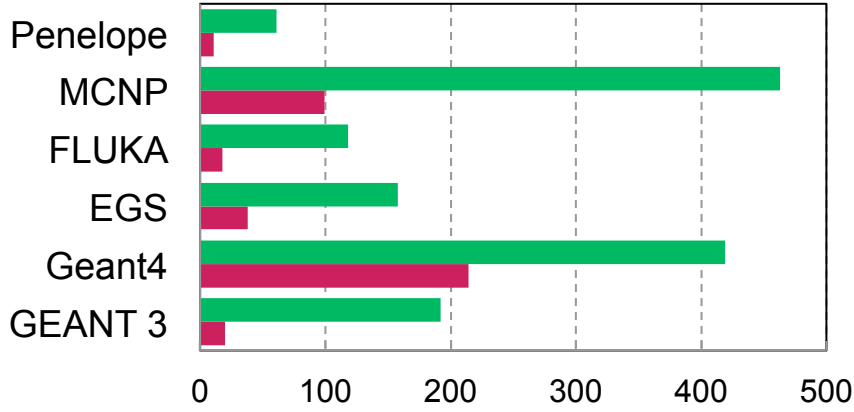
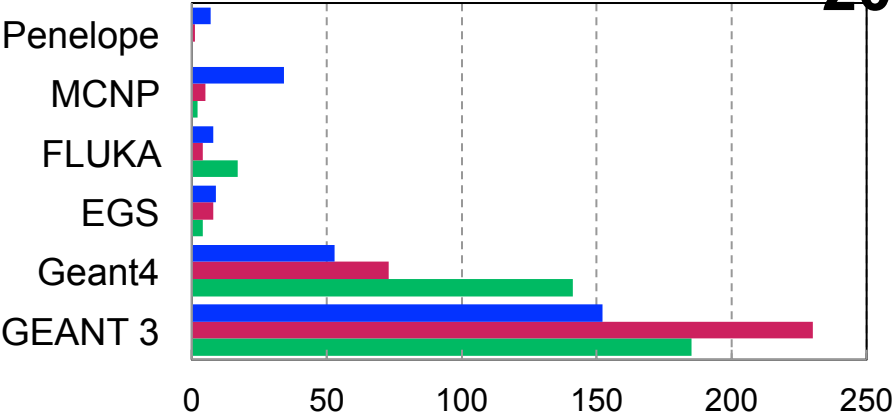
# The zoo

*Many codes not publicly distributed*

- EGS4, EGS5, EGSnrc
- GEANT 3, Geant4
- MARS
- MCNP, MCNPX, A3MCNP, MCNP-DSP, MCNP4B
- MVP, MVP-BURN
- Penelope
- Peregrine
- Tripoli-3, Tripoli-3 A, Tripoli-4

...and I probably forgot some more

## 2004-2008

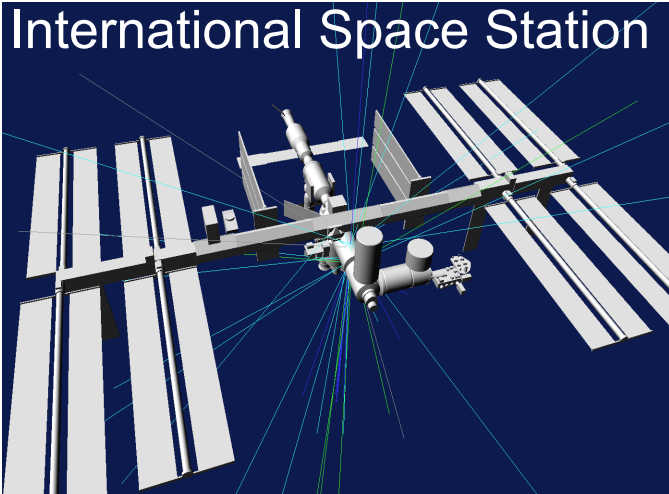


■ Phys. Rev. C ■ Phys. Rev. Lett. ■ Phys. Rev. D

■ NIM ■ TNS

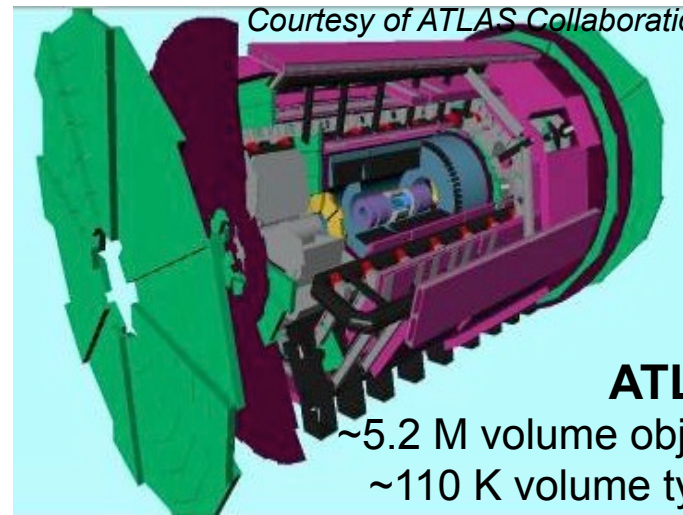
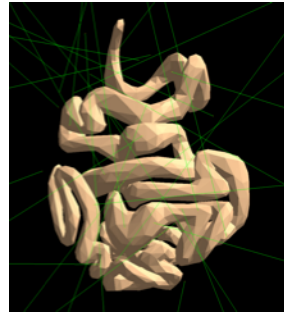
# Geometry

Courtesy T. Ersmark, KTH Stockholm



Courtesy HUREL, Hanyang Univ.

**Intestine**

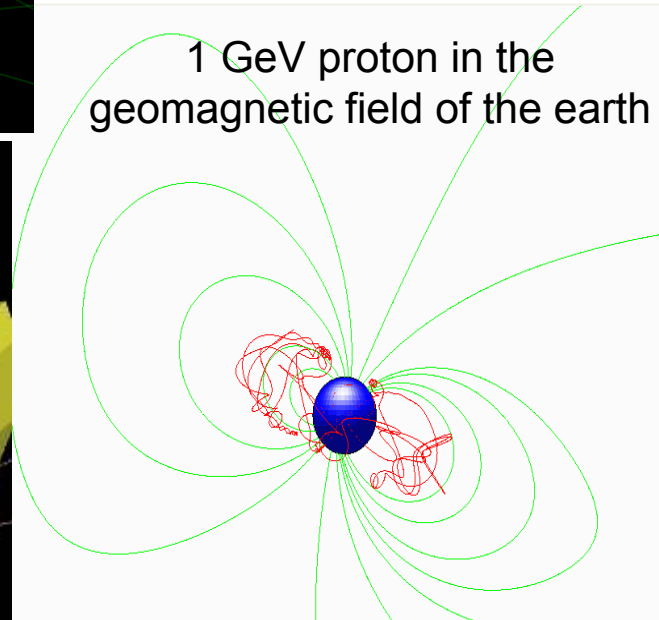


**ATLAS**

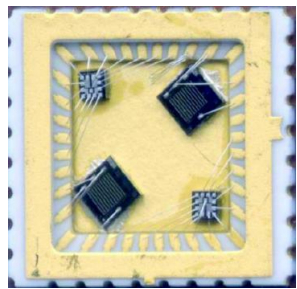
~5.2 M volume objects  
~110 K volume types

**Electric and magnetic fields**

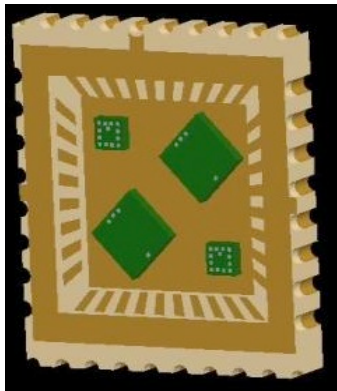
1 GeV proton in the geomagnetic field of the earth



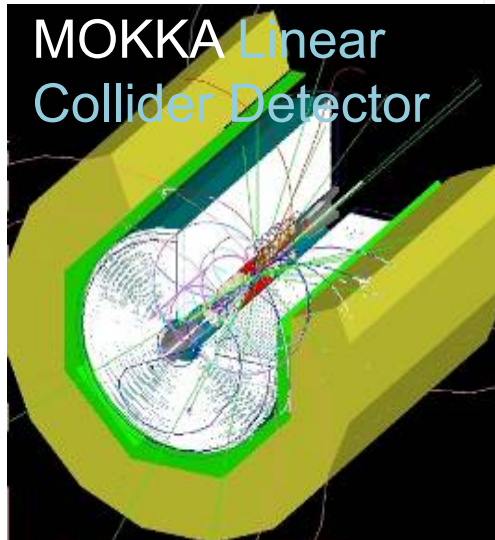
Courtesy L. Desorgher, Univ. Bern



RADMON, CERN



Maria Grazia Pia, INFN Genova



# Geant4 electromagnetic physics

- electrons and positrons
- photons (*including optical photons*)
- muons
- charged hadrons
- ions

Multiple models for the same process:

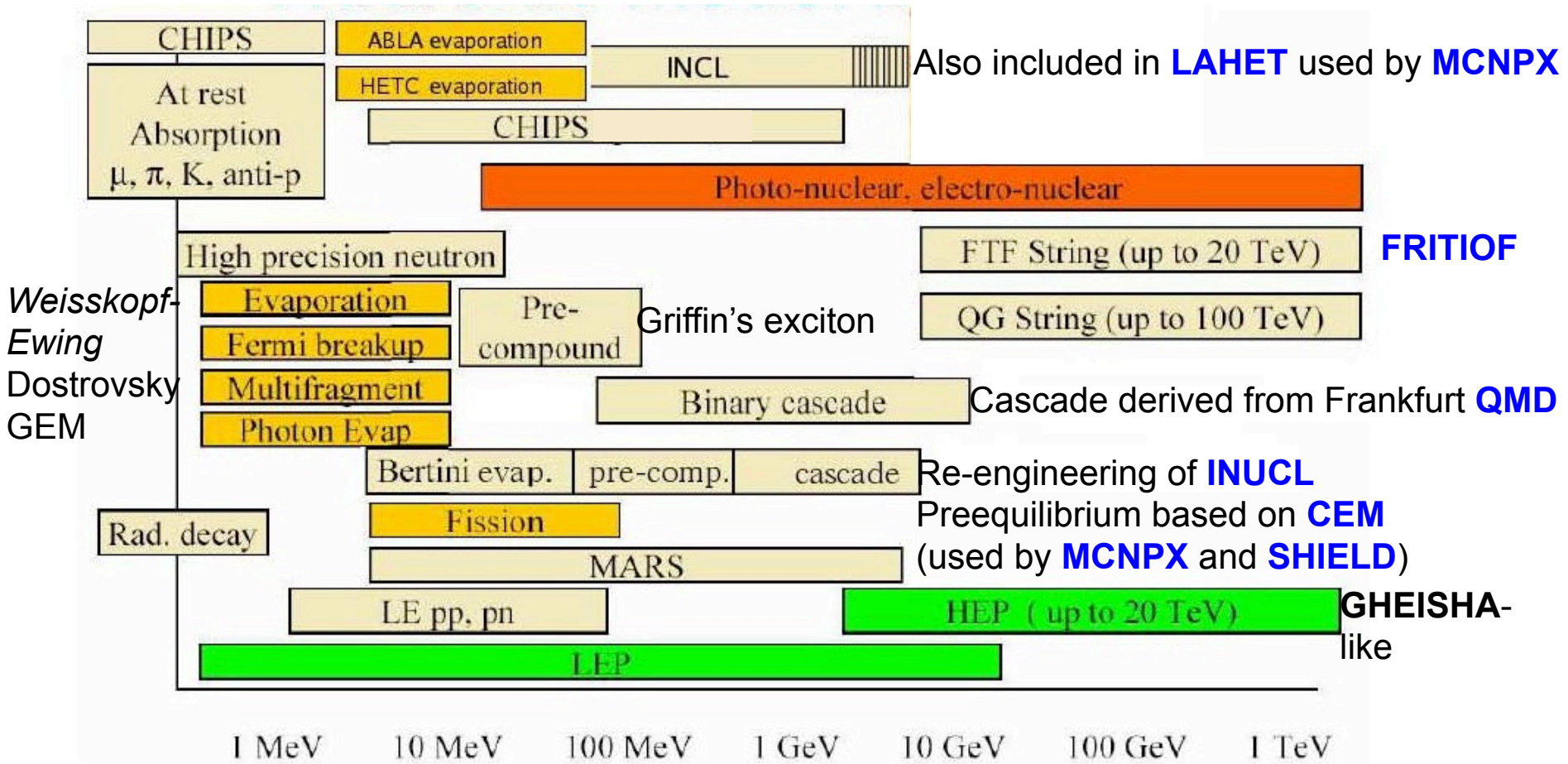
- Standard
- Based on EADL-EEDL-EPDL data libraries
- Penelope-like
- + some variants, e.g. polarised photons

Multiple scattering  
Bremsstrahlung  
Ionisation  
Annihilation  
Photoelectric effect  
Compton scattering  
Rayleigh scattering  
 $\gamma$  conversion  
Synchrotron radiation  
Transition radiation  
Cherenkov  
Refraction  
Reflection  
Absorption  
Scintillation  
Fluorescence  
Auger electron emission

**...sometimes nominally different models are actually identical**

# Geant4 hadronic inelastic model inventory

- Data-driven
- Parameterised
- Theory-driven



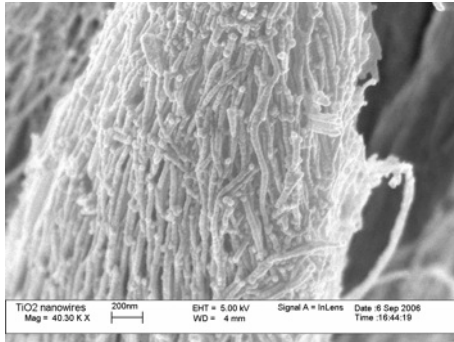
Many physics models are the same across different codes!

# A mature Monte Carlo code

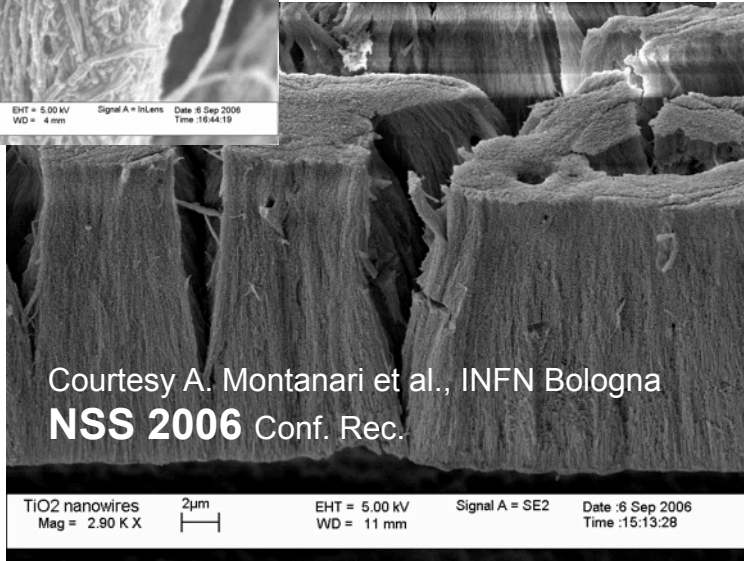
- Successfully used in many, multi-disciplinary experimental applications
- Cited by many relevant publications
  - e.g. Higgs boson discovery
- Ongoing improvements and refinements
  - Similar evolution also in other Monte Carlo codes
- Adaptation to evolving computing technologies
  - e.g. multithreading

**Anything new and hot in the field?**

# The world changes...

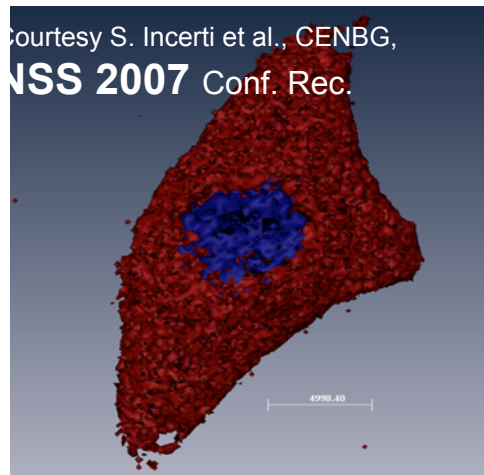
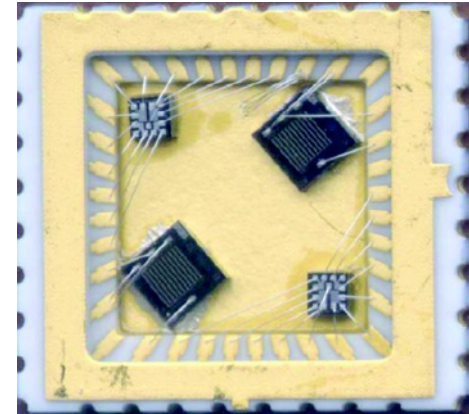


TiO<sub>2</sub> nanowires

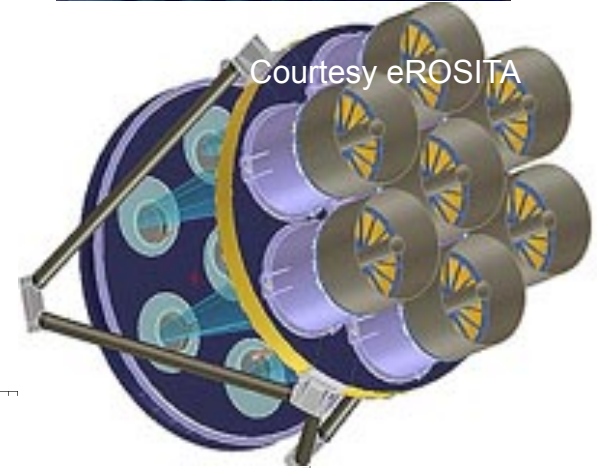


Courtesy A. Montanari et al., INFN Bologna  
**NSS 2006** Conf. Rec.

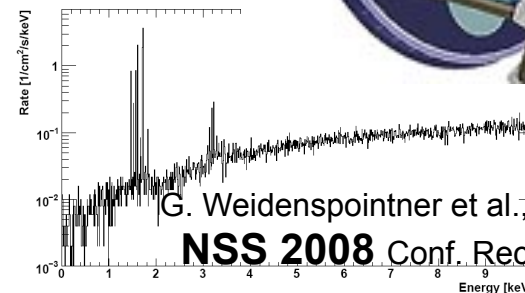
Courtesy RADMON (M. Moll et al.)  
Team, CERN,  
**NSS 2006** Conf. Rec.



Courtesy S. Incerti et al., CENBG,  
**NSS 2007** Conf. Rec.



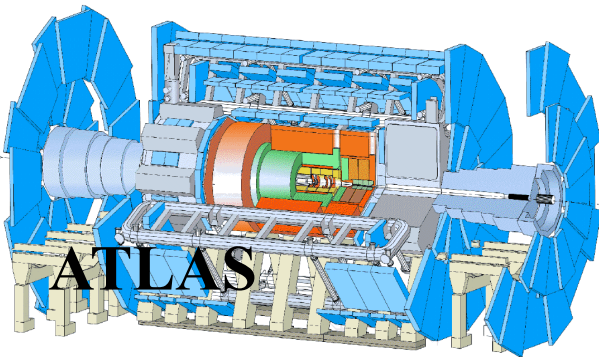
Courtesy eROSITA



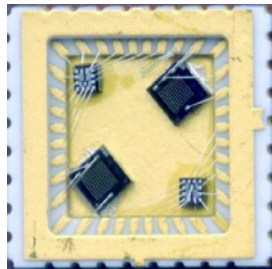
# Two worlds...

## Condensed-random-walk **OR** “discrete” régime

Characterizing choice in a Monte Carlo system



RADMON

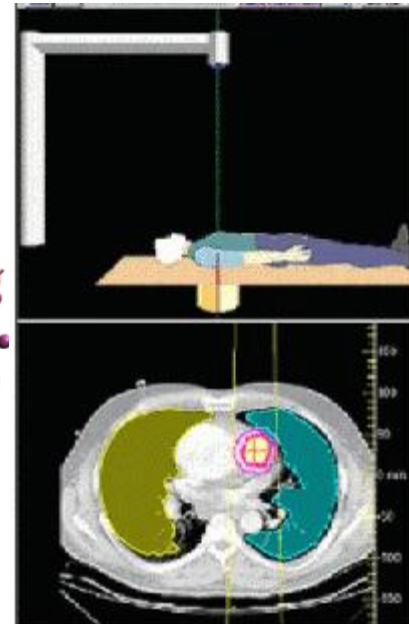
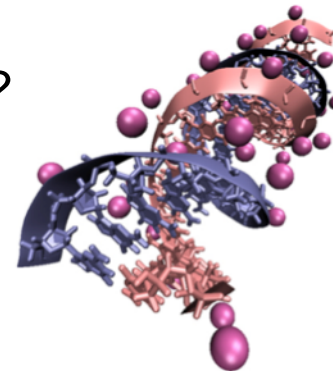


How does one estimate radiation effects on components exposed to LHC + detector environment?

And what about **nanotechnology**-based detectors for HEP?  
And tracking in a **gaseous detector**?

And **plasma** facing material in a fusion reactor?

How does one relate **dosimetry** to  
**radiation biology**?





## Simulation at small scale

Transport very low energy particles ( $\sim$ eV scale)

Physics models  
Experimental data

- ➔ Drop the condensed history scheme
- ➔ Move beyond the independent particle approximation

## Multi-scale simulation

Nano- and macro-scale in the same environment  
Condensed and discrete schemes

*...it is not just a matter of if-then-else*

*Source of inconsistency even in conventional scenarios (e.g. PIXE)*

# Independent particle approximation

Particles interact with atoms

Molecules?  
Solids?

Each electron is considered to move **independently** in the **average field** of the  $Z - 1$  other electrons plus the nucleus

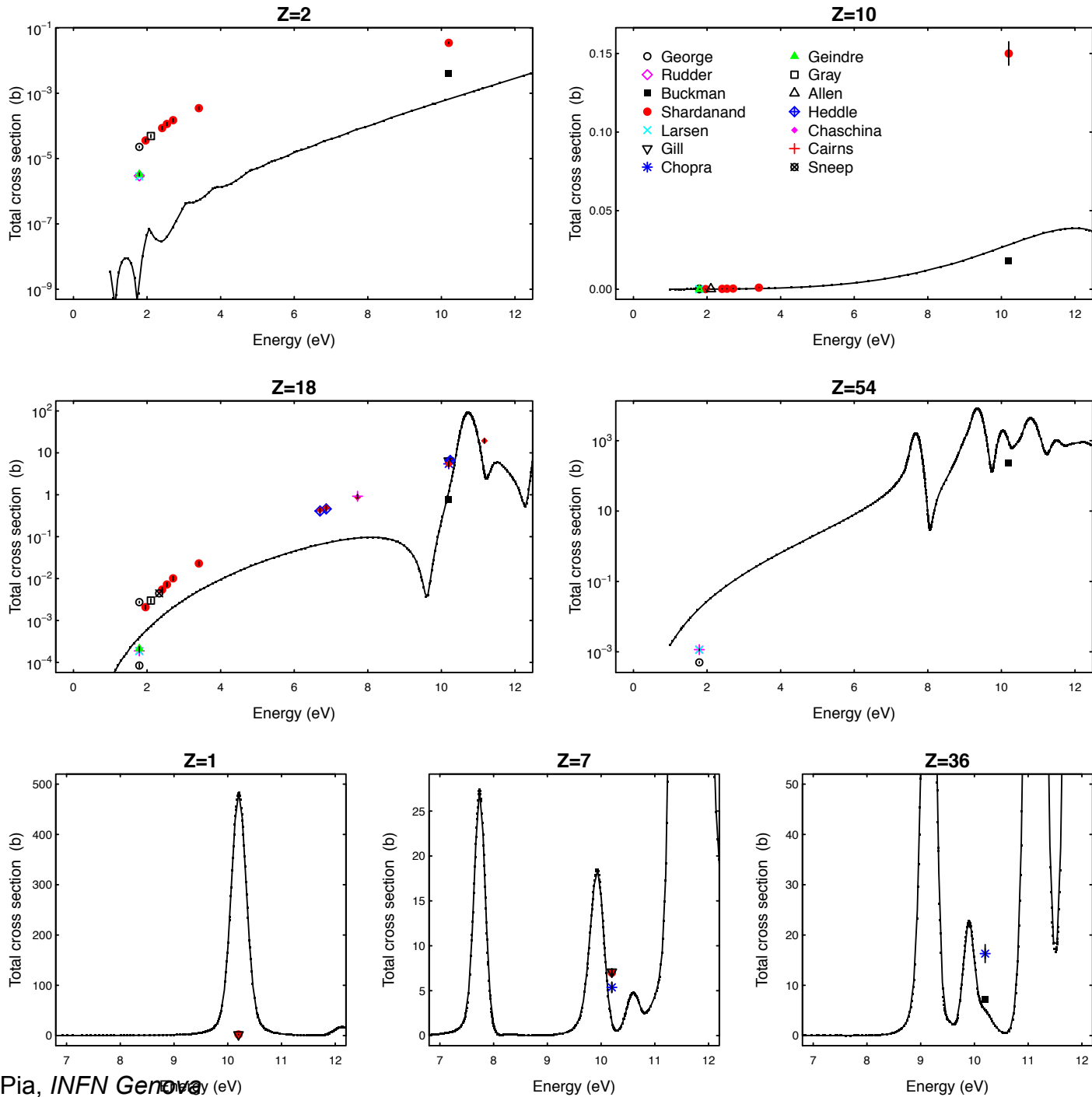
Central-field  
approximation

the distribution of the  $Z - 1$  other electrons is spherically symmetric around the nucleus

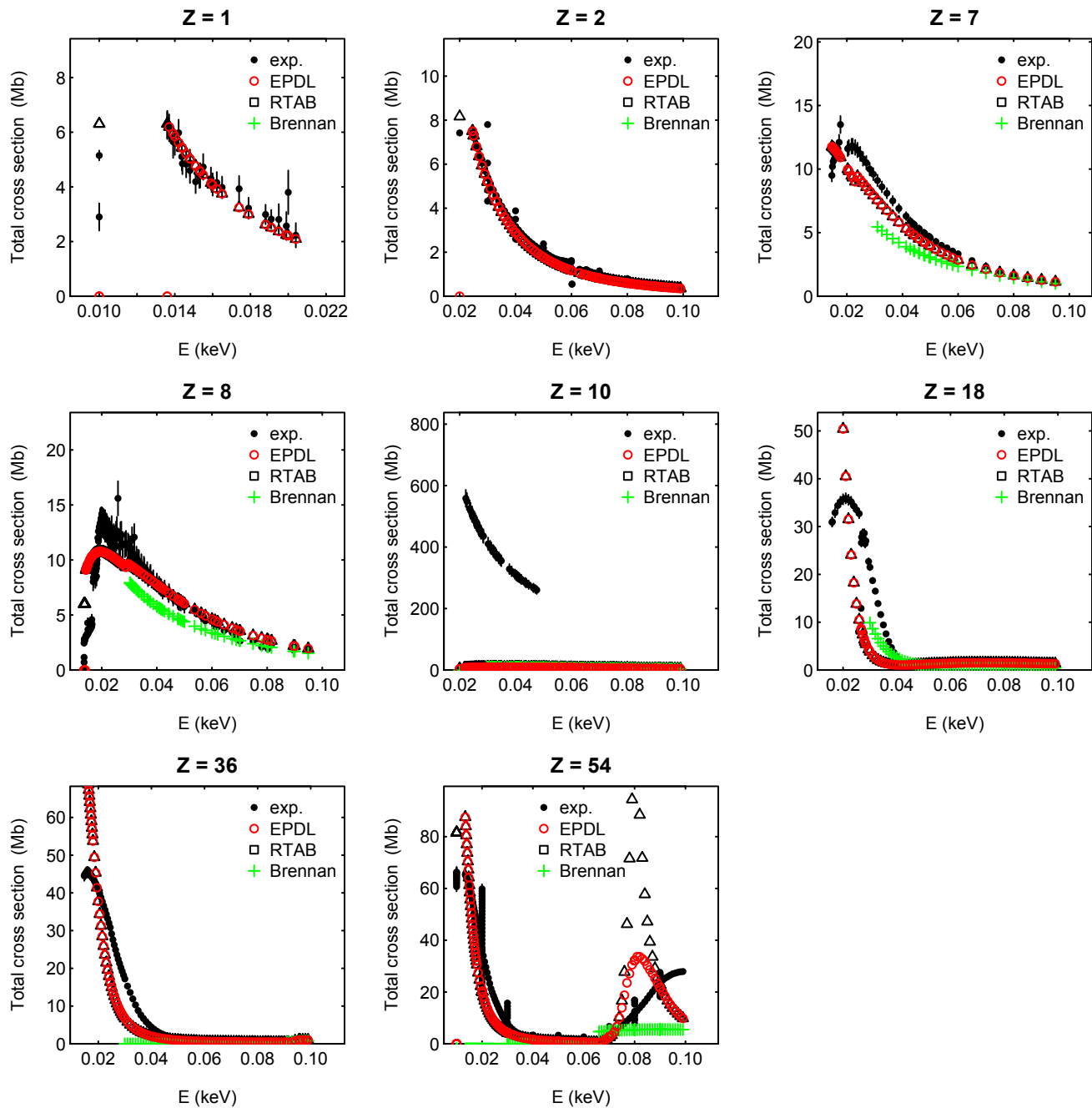
(Dirac) **Hartree-Fock calculations** are at the basis of the physics models used in Monte Carlo particle transport

## When does it break?

# Photon elastic scattering



# Photoionization



# PARTRAC, OREC, NOREC, LAPPA, MC4V, MC4L, TRION...

- ◆ M. Zaider, D. J. Brenner, W. E. Wilson, "The application of track calculations to radiobiology: I. Monte Carlo simulation of proton tracks", *Radiat. Res.*, vol. 95, pp. 231-247, 1983.
- ◆ H. G. Paretzke, "Radiation track structure theory", in *Kinetics of Non-homogeneous Processes*, Ed. New York: Wiley, 1987, pp. 89-170.
- ◆ W. E. Wilson and H. G. Paretzke, "Calculation of distribution of energy imparted and ionisations by fast protons in nanometer sites", *Radiat. Res.*, vol. 81, pp. 521-537, 1981.
- ◆ A. Ito, "Electron track simulation for microdosimetry", in *Monte Carlo Transport of Electrons and Photons*, Ed. Plenum, 1988, pp. 361-382.
- ◆ S. Uehara, H. Nikjoo, and D. T. Goodhead, "Cross-sections for water vapor for the Monte Carlo electron track structure code from 10 eV to the MeV region", *Phys. Med. Biol.*, vol. 37, pp. 1841-1858, 1992.
- ◆ A. V. Lappa, E. A. Bigildeev, D. S. Burmistrov, and O. N. Vasilyev, "Trion code for radiation action calculations and its application in microdosimetry and radiobiology", *Radiat. Environ. Biophys.*, vol. 32, pp. 1-19, 1993.
- ◆ C. Champion, "Multiple ionization of water by heavy ions: a Monte Carlo approach", *Nucl. Instrum. Meth. B*, vol. 205, pp. 671-676, 2003.
- ◆ W. E. Wilson and H. Nikjoo, "A Monte Carlo code for positive ion track simulation", *Radiat. Environ. Biophys.*, vol. 38, pp. 97-104, 1999.
- ◆ S. Uehara, L. H. Toburen, and H. Nikjoo, "Development of a Monte Carlo track structure code for low-energy protons in water", *Int. J. Radiat. Biol.*, vol. 77, pp. 138-154, 2001.
- ◆ D. Emfietzoglou, G. Papamichael, and M. Moscovitch, "An event-by-event computer simulation of interactions of energetic charged particles and all their secondary electrons in water", *J. Phys. D: Appl. Phys.*, vol. 33, pp. 932-944, 2000.
- ◆ D. Emfietzoglou, G. Papamichael, K. Kostarelos, and M. Moscovitch, "A Monte Carlo track structure code for electrons ( 10 eV-10 keV) and protons ( 0.3-10 MeV) in water: partitioning of energy and collision events", *Phys. Med. Biol.*, vol. 45, pp. 3171-3194, 2000.
- ◆ D. Emfietzoglou, G. Papamichael, and M. Moscovitch, "Charged particle interactions in water: Cross sections and simulations", *Radiat. Phys. Chem.*, vol. 61, pp. 597-598, 2001.
- ◆ M. Terrissol and A. Beaudre, "Simulation of space and time evolution of radiolytic species induced by electrons in water", *Radiat. Prot. Dosim.*, vol. 31, pp. 171-175, 1990.
- ◆ S. M. Pimblott, J. A. LaVerne, A. Mozumder, N. J. B Green, "Structure of electron tracks in water. 1. Distribution of energy deposition events", *J. Phys. Chem.*, vol. 94, pp. 488-495, 1990.
- ◆ R. H. Ritchie et al., "Radiation Interactions and Energy Transport in the Condensed Phase", in *Physical and Chemical Mechanisms in Molecular Radiation Biology*, Ed. Plenum Press, 1991, pp. 99-136.
- ◆ M. Zaider, M. G. Vracko, A. Y. C. Fung, J. L. Fry, "Electron transport in condensed water", *Radiat. Prot. Dosim.*, vol. 52, pp. 139-146, 1994.
- ◆ M.A. Hill, F. A. Smith, "Calculation of initial and primary yields in the radiolysis of water", *Int. J. Appl. Radiat. Isot.*, 43, pp. 265-280, 1994.
- ◆ V. Cobut, Y. Frongillo, J. P. Patau, T. Goulet, M. J. Fraser, and J. P. Jay-Gerin, "Monte Carlo simulation of fast electron and proton tracks in liquid water I. Physical and physicochemical aspects", *Radiat. Phys. Chem.*, vol. 51, pp. 229-243, 1998.
- ◆ V. A. Semenenko et al., "NOREC, a Monte Carlo code for simulating electron tracks in liquid water", *Radiat. Environ. Biophys.*, vol. 42, pp. 213-217, 2003.

# Very-low energy models

1<sup>st</sup> development cycle:  
**Physics of interactions in water down to the eV scale**

IEEE TRANSACTIONS ON NUCLEAR SCIENCE, VOL. 54, NO. 6, DECEMBER 2007

2619

## Geant4 Physics Processes for Microdosimetry Simulation: Design Foundation and Implementation of the First Set of Models

S. Chauvie, Z. Francis, S. Guatelli, S. Incerti, B. Mascialino, P. Moretto, P. Nieminen, and M. G. Pia

## Further developments

*Joint International Conference on Supercomputing in Nuclear Applications and Monte Carlo 2010 (SNA + MC2010)*  
Hitotsubashi Memorial Hall, Tokyo, Japan, October 17-21, 2010

### **Modeling Radiation Chemistry and Biology in the Geant4 Toolkit**

M. Karamitros<sup>1</sup>, A. Mantero<sup>2</sup>, S. Incerti<sup>1\*</sup>, G. Baldacchino<sup>3</sup>, P. Barberet<sup>1</sup>, M. Bernal<sup>4,5</sup>, R. Capra<sup>6</sup>, C. Champion<sup>7</sup>, Z. El Bitar<sup>8</sup>, Z. Francis<sup>9</sup>, W. Friedland<sup>10</sup>, P. Guèye<sup>11</sup>, A. Ivanchenko<sup>1</sup>, V. Ivanchenko<sup>7,12</sup>, H. Kurashige<sup>13</sup>, B. Mascialino<sup>14</sup>, P. Moretto<sup>1</sup>, P. Nieminen<sup>15</sup>, G. Santin<sup>15</sup>, H. Seznec<sup>1</sup>, H. N. Tran<sup>1</sup>, C. Villagrasa<sup>9</sup> and C. Zacharatou<sup>16</sup>

*Physics mostly derived from other “track structure” codes*



Incerti S, Ivanchenko A, Karamitros M, Mantero A, Moretto P, Tran HN, Mascialino B, Champion C, Ivanchenko VN, Bernal MA, Francis Z, Villagrasa C, Baldacchin G, Guèye P, Capra R, Nieminen P, Zacharatou C.

## **Comparison of GEANT4 very low energy cross section models with experimental data in water**

Med. Phys., vol. 37, no. 9, pp. 4692-4708, 2010

Software  
Good software  
Validated software

**1012<sup>TM</sup>**

**IEEE Standard for Software  
Verification and Validation**



# Ionization cross sections for low energy electron transport

Hee Seo, Maria Grazia Pia, Paolo Saracco and Chan Hyeong Kim

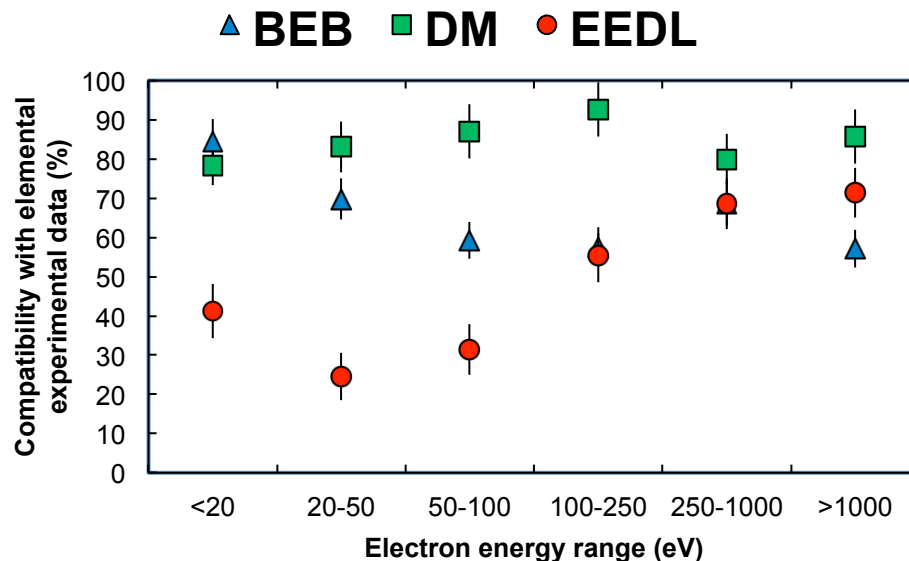
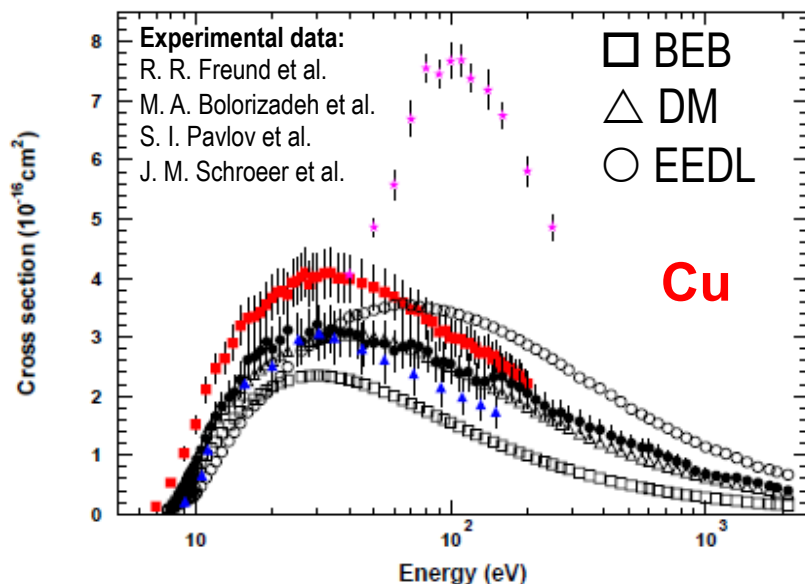
*IEEE Trans. Nucl. Sci., vol. 58, no. 6, pp. 3219–3245, 2011*

## Cross section models

- Binary-Encounter-Bethe (**BEB**)
- Deutsch-Märk (**DM**)
- **EEDL** (*current Geant4 Low Energy*)

## Validation

- 57 elements
- **181** experimental data sets
- statistical data analysis



Percentage of elements for which a model is compatible with experimental data at **95% CL**<sub>24</sub>

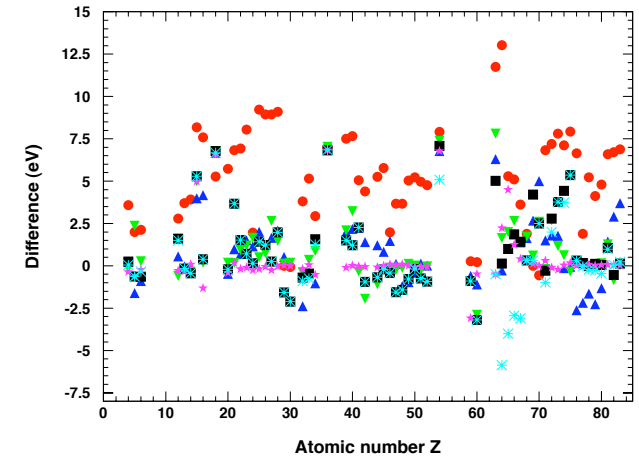
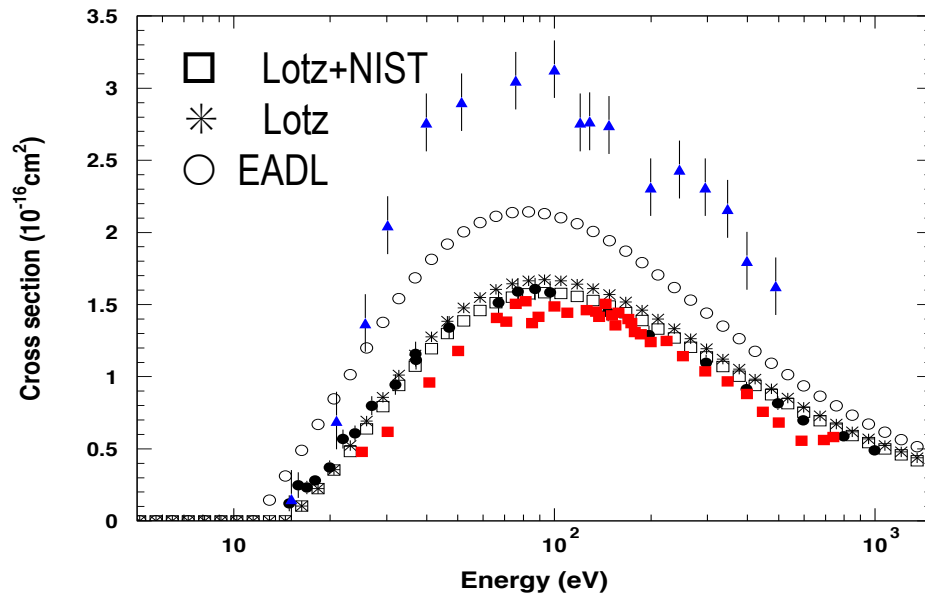


# A fresh look at atomic parameters

3246

## Evaluation of Atomic Electron Binding Energies for Monte Carlo Particle Transport

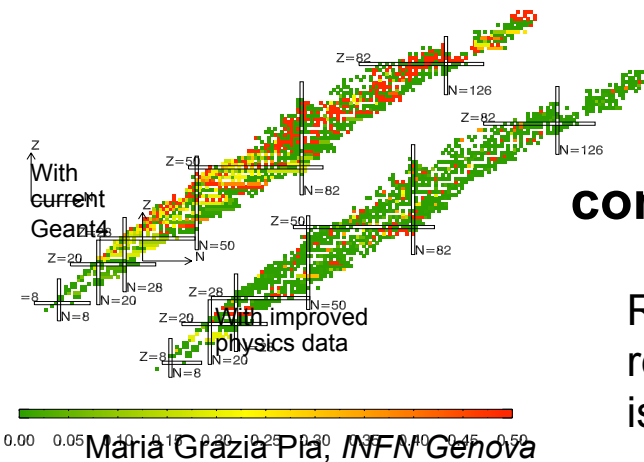
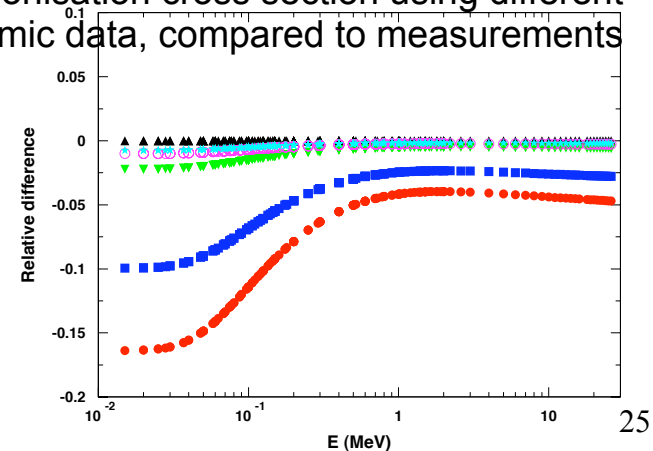
Maria Grazia Pia, Hee Seo, Matej Batic, Marcia Begalli, Chan Hyeong Kim, Lina Quintieri, and Paolo Saracco



Atomic binding energies from various sources compared to experimental data

C, K shell

Proton ionisation cross section using different atomic data, compared to measurements



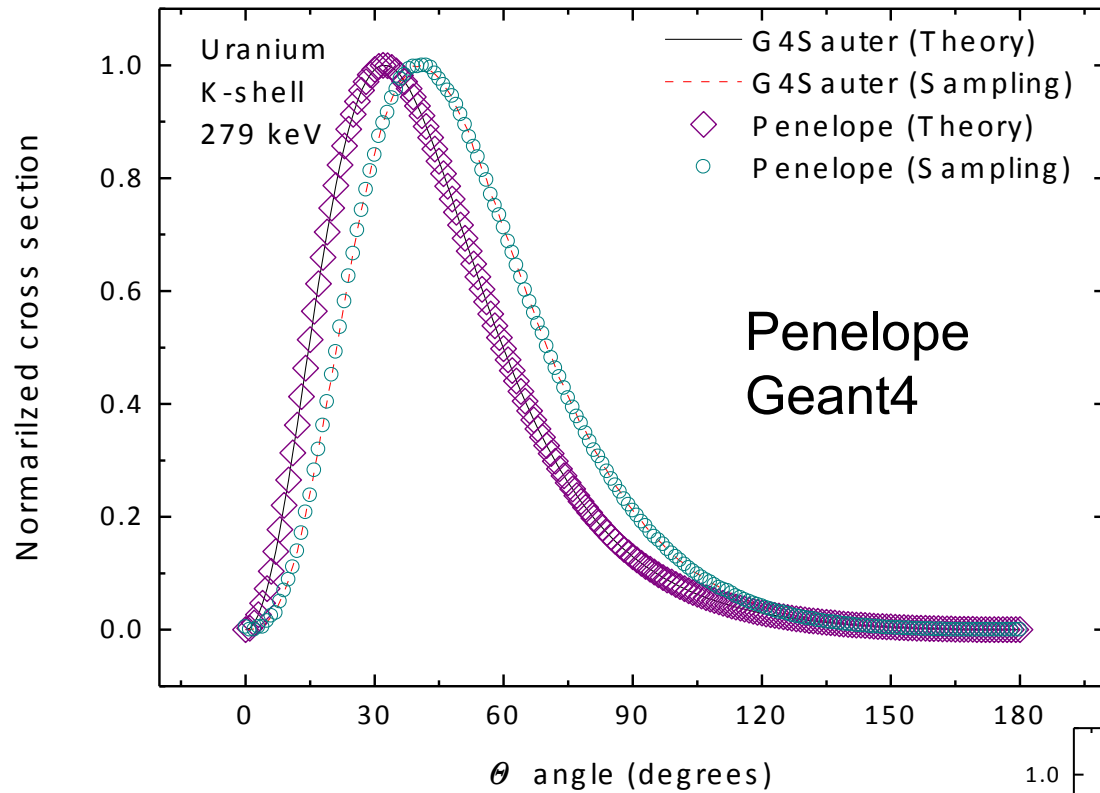
Benefits also in conventional simulations

Radioactive decay: Median relative intensity deviation per isotope for X-ray emission

# How good are Monte Carlo codes?



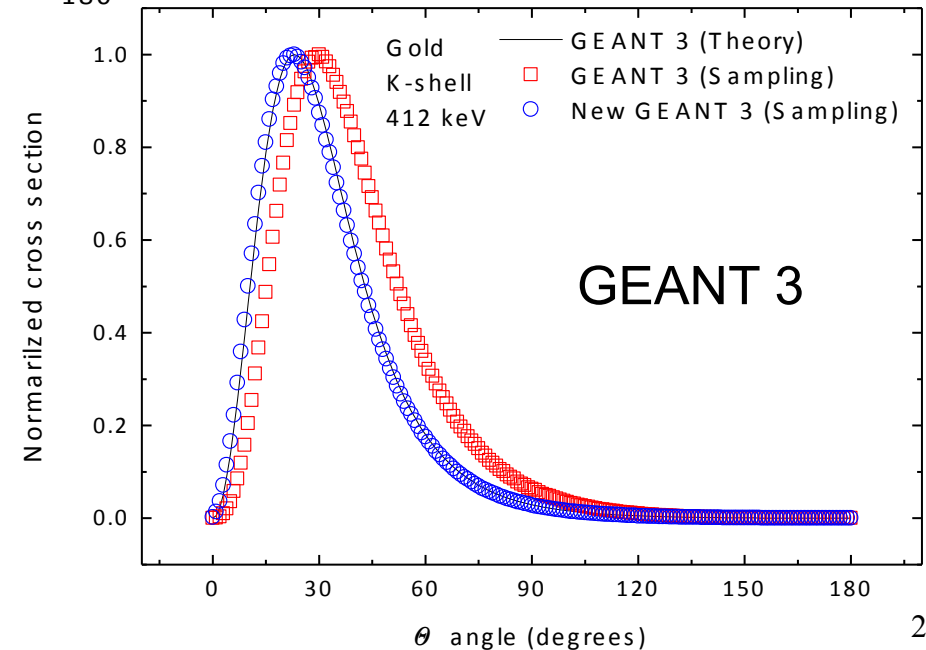
*Hardly any systematic, quantitative validation of the physics models in Monte Carlo codes for particle transport is documented in the literature*



## Photoelectron angular distribution

Error aged for ~30 years  
and propagated across  
different Monte Carlo codes

New, correct sampling  
algorithm reproduces the  
expected theoretical distribution



# Monte Carlo as a predictive instrument

If we know the uncertainties of the “ingredients” of our Monte Carlo code, can we calculate the uncertainties of the observables resulting from the simulation?

**Quantify the uncertainties of the “ingredients”**

**Epistemic uncertainties**

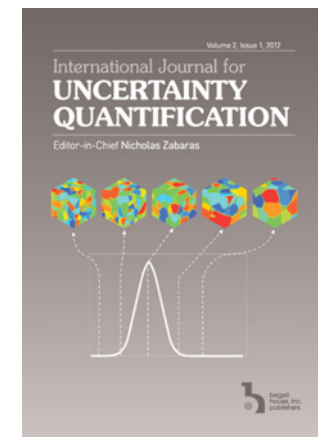
**Propagation of uncertainties into observables**

**Validation** of physics models and parameters

Induced **systematic effects**

Uncertainty Quantification

*Hot topic in deterministic simulation,  
still in its infancy in Monte Carlo simulation*



# Validation of the “ingredients”

594

IEEE TRANSACTIONS ON NUCLEAR SCIENCE, VOL. 54, NO. 3, JUNE 2007

## Validation of Geant4 Atomic Relaxation Against the NIST Physical Reference Data

S. Guatelli, A. Mantero, B. Mascialino, M. G. Pia, and V. Zampichelli

IEEE TRANSACTIONS ON NUCLEAR SCIENCE

## Evaluation of atomic electron binding energies for Monte Carlo particle transport

Maria Grazia Pia, Hee Seo, Matej Batič, Marcia Begalli, Chan Hyeong Kim, Lina Quintieri and Paolo Saracco

3650

IEEE TRANSACTIONS ON NUCLEAR SCIENCE, VOL. 56, NO. 6, DECEMBER 2009

## Validation of K and L Shell Radiative Transition Probability Calculations

Maria Grazia Pia, Paolo Saracco, and Manju Sudhakar

IEEE TRANSACTIONS ON NUCLEAR SCIENCE

## Validation of Proton Ionization Cross Section Generators for Monte Carlo Particle Transport

Matej Batič, Maria Grazia Pia, and Paolo Saracco

3614

IEEE TRANSACTIONS ON NUCLEAR SCIENCE, VOL. 56, NO. 6, DECEMBER 2009

## PIXE Simulation With Geant4

Maria Grazia Pia, Georg Weidenspointner, Mauro Augelli, Lina Quintieri, Paolo Saracco, Manju Sudhakar, and Andreas Zoglauer

IEEE TRANSACTIONS ON NUCLEAR SCIENCE, VOL. 58, NO. 6, DECEMBER 2011

## Ionization Cross Sections for Low Energy Electron Transport

Hee Seo, Maria Grazia Pia, Paolo Saracco, and Chan Hyeong Kim

578

IEEE TRANSACTIONS ON NUCLEAR SCIENCE, VOL. 54, NO. 3, JUNE 2007

## Geant4 Model for the Stopping Power of Low Energy Negatively Charged Hadrons

Stéphane Chauvie, Petteri Nieminen, and Maria Grazia Pia

1636

IEEE TRANSACTIONS ON NUCLEAR SCIENCE, VOL. 59, NO. 4, AUGUST 2012

## Photon Elastic Scattering Simulation: Validation and Improvements to Geant4

Matej Batič, Gabriela Hoff, Maria Grazia Pia, and Paolo Saracco

398

IEEE TRANSACTIONS ON NUCLEAR SCIENCE, VOL. 56, NO. 2, APRIL 2009

## Validation of Geant4 Low Energy Electromagnetic Processes Against Precision Measurements of Electron Energy Deposition

Anton Lechner, Maria Grazia Pia, and Manju Sudhakar

# Computational Science Demands a New Paradigm

Douglass E. Post and Lawrence G. Votta

Maria Grazia Pia, INFN Genova

etc.

*Physics Today,*  
vol. 58, no. 1, 2005



## Validation of the Geant4 electromagnetic photon cross-sections for elements and compounds

G.A.P. Cirrone<sup>a</sup>, G. Cuttone<sup>a</sup>, F. Di Rosa<sup>a</sup>, L. Pandola<sup>b,\*</sup>, F. Romano<sup>a</sup>, Q. Zhang<sup>a,c,\*\*</sup>

# Comparison to theoretical data libraries NOT validation!

*Joint International Conference on Supercomputing in Nuclear Applications and Monte Carlo 2010 (SNA + MC2010)*  
Hitotsubashi Memorial Hall, Tokyo, Japan, October 17-21, 2010

“After the migration to common design a new **validation** of photon cross sections versus various databases was published <sup>26)</sup> which demonstrated general good agreement with the data for both the Standard and Low-energy models.”

### Recent Improvements in Geant4 Electromagnetic Physics Models and Interfaces

Vladimir IVANCHENKO<sup>1,2,3</sup>, John APOSTOLAKIS<sup>1</sup>, Alexander BAGULYA<sup>4</sup>, Haifa Ben ABDELOUAHED<sup>5</sup>, Rachel BLACK<sup>6</sup>, Alexey BOGDANOV<sup>7</sup>, Helmut BURKHARD<sup>1</sup>, Stéphane CHAUVIE<sup>8</sup>, Pablo CIRRONE<sup>9</sup>, Giacomo CUTTONE<sup>9</sup>, Gerardo DEPAOLA<sup>10</sup>, Francesco Di ROSA<sup>9</sup>, Sabine ELLES<sup>11</sup>, Ziad FRANCIS<sup>12</sup>, Vladimir GRICHINE<sup>1</sup>, Peter GUMPLINGER<sup>13</sup>, Paul GUEYE<sup>8</sup>, Sebastien INCERTI<sup>14</sup>, Anton IVANCHENKO<sup>14</sup>, Jean JACQUEMIER<sup>11</sup>, Anton LECHNER<sup>15</sup>, Francesco LONGO<sup>16</sup>, Omrane KADRI<sup>9</sup>, Nicolas KARAKATSANIS<sup>17</sup>, Mathieu KARAMITROS<sup>14</sup>, Rostislav KOKOULDN<sup>7</sup>, Hisaya KURASHIGE<sup>18</sup>, Michel MAIRE<sup>11,19</sup>, Alfonso MANTERO<sup>20</sup>, Barbara MASCIALINO<sup>21</sup>, Jakub MOSCICKI<sup>1</sup>, Luciano PANDOLA<sup>22</sup>, Joseph PERL<sup>23</sup>, Ivan PETROVIC<sup>9</sup>, Aleksandra RISTIC-FIRA<sup>9</sup>, Francesco ROMANO<sup>9</sup>, Giorgio RUSSO<sup>9</sup>, Giovanni SANTINI<sup>24</sup>, Andreas SCHAELOCKE<sup>25</sup>, Toshiyuki TOSHITO<sup>26</sup>, Hoang TRAN<sup>14</sup>, Laszlo URBAN<sup>27</sup>, Tomohiro YAMASHITA<sup>27</sup> and Christina ZACHARATOU<sup>28</sup>



# Validation is holistic

One must validate the entire calculation system

Including:

- User
- Computer system
- Problem setup
- Running
- Results analysis



An inexperienced user can easily get wrong answers out of a good code in a valid régime



Columbia Space Shuttle accident, 2003

# Epistemic uncertainties

Epistemic uncertainties originate from **lack of knowledge**

Relatively scarce attention so far in Monte Carlo simulation  
Studies in deterministic simulation (*especially for critical applications*)

**Possible sources** in Monte Carlo simulation

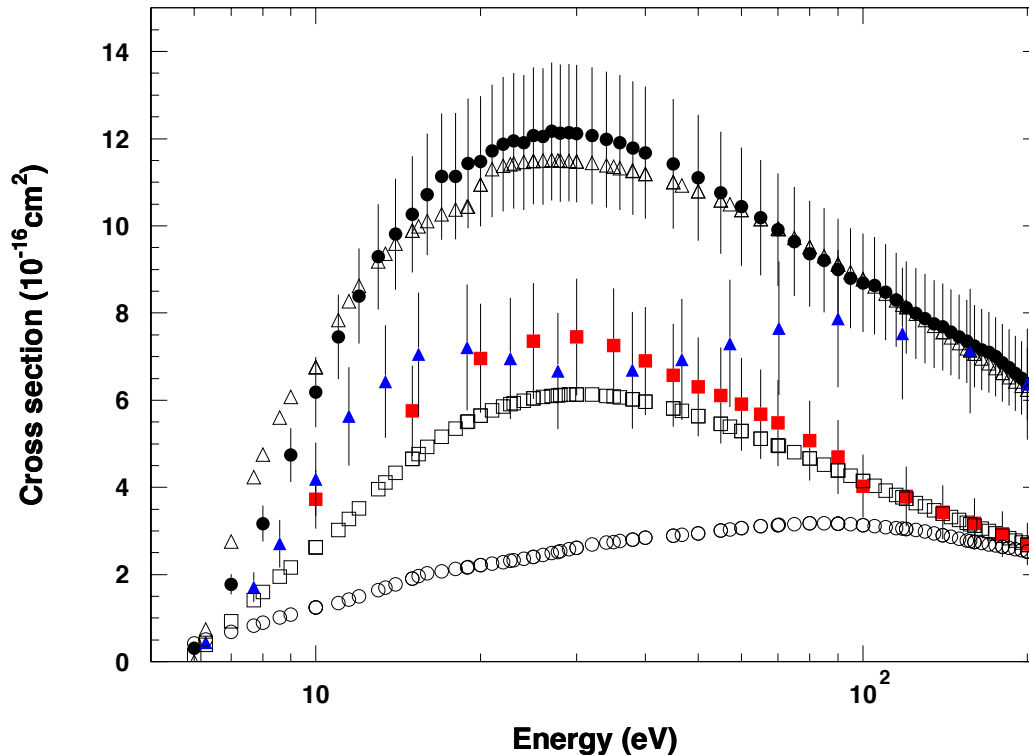
- incomplete understanding of fundamental (physics) processes, or practical inability to treat them thoroughly
- non-existent or conflicting experimental data for a (physical) parameter or model
- applying a (physics) model beyond the experimental conditions in which its validity has been demonstrated

Epistemic uncertainties affect the **reliability** of simulation results

**Can we quantify them?**



# Which one is right?



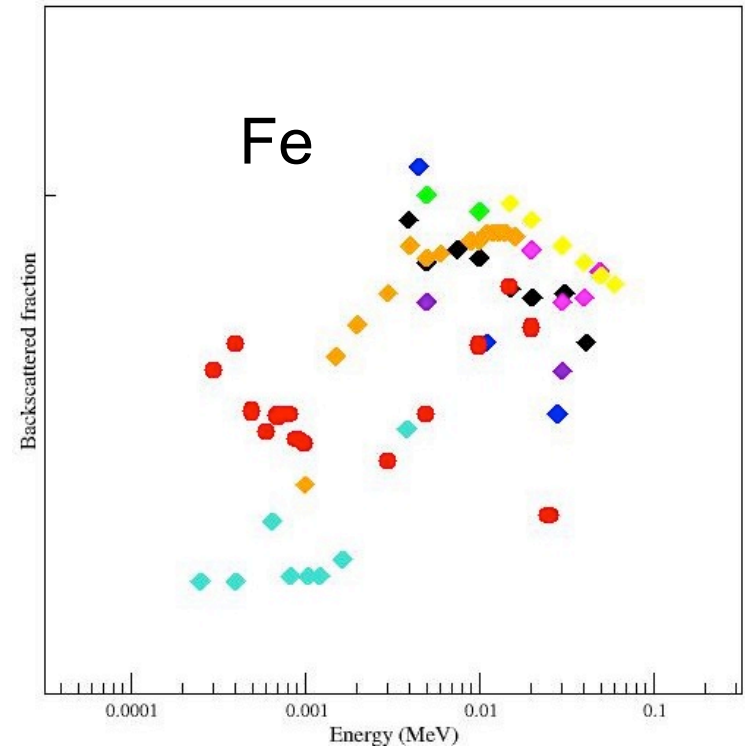
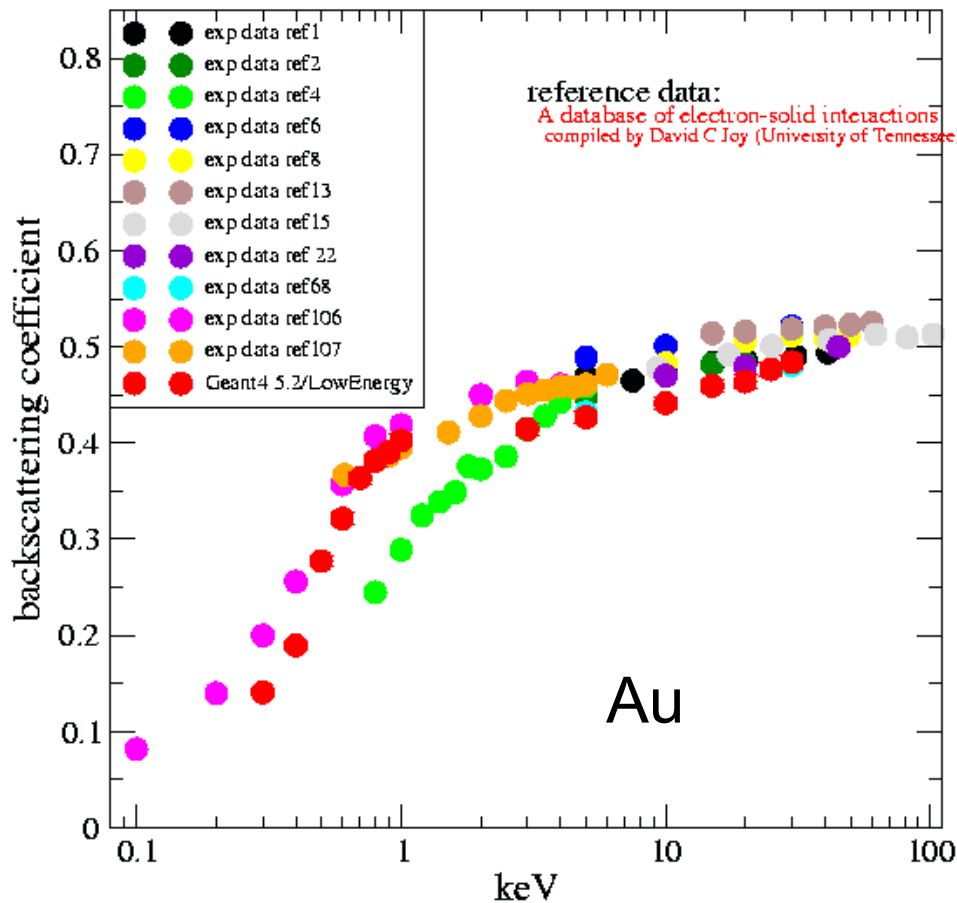
Often an answer can be found only through a **statistical analysis** over a **large sample** of simulated and experimental data (*and would be a result with a given CL, rather than black & white*)

- Empty symbols: simulation models
- Filled symbols: experimental data

# The main problem of validation: experimental data!

backscattering for e-

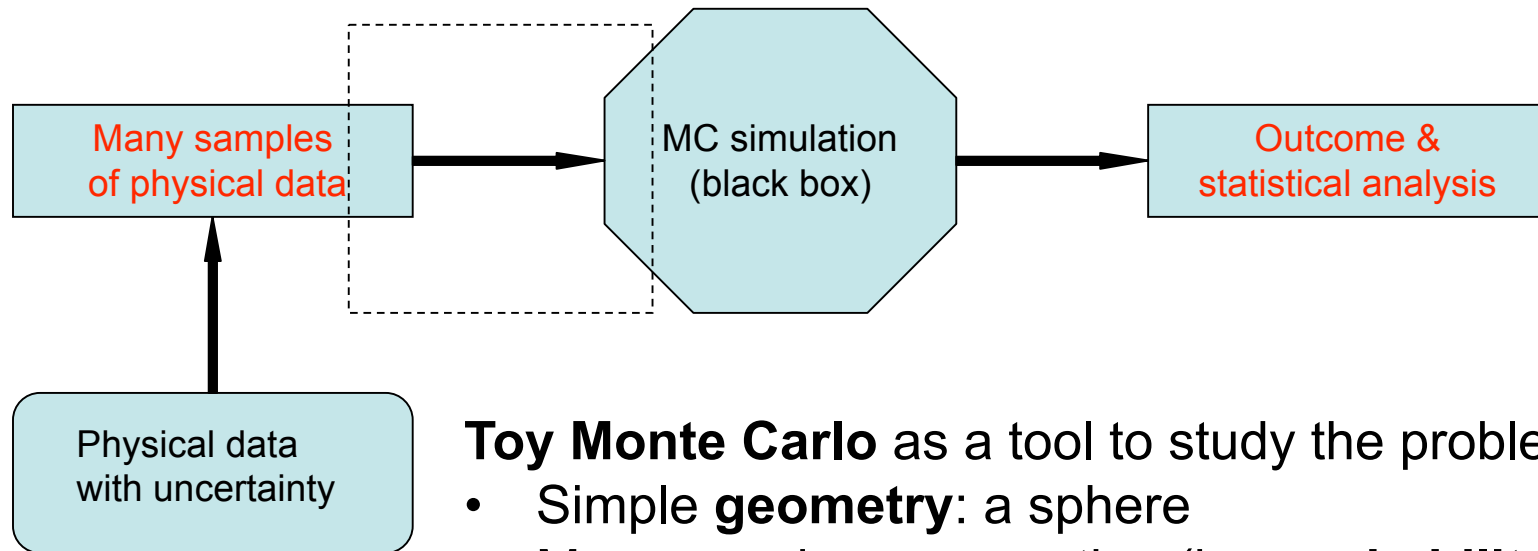
e- energy range: 0.1 keV -> 102. keV



Experimental data often exhibit large differences!

First steps to establish a

# theoretical ground of Uncertainty Quantification

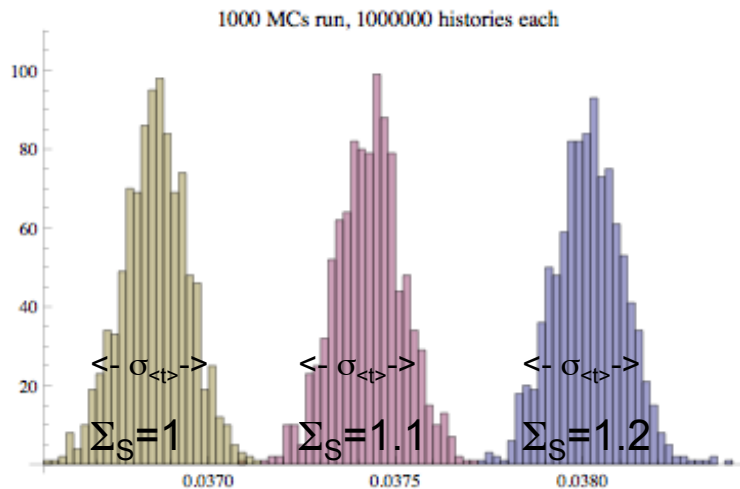


**Toy Monte Carlo** as a tool to study the problem

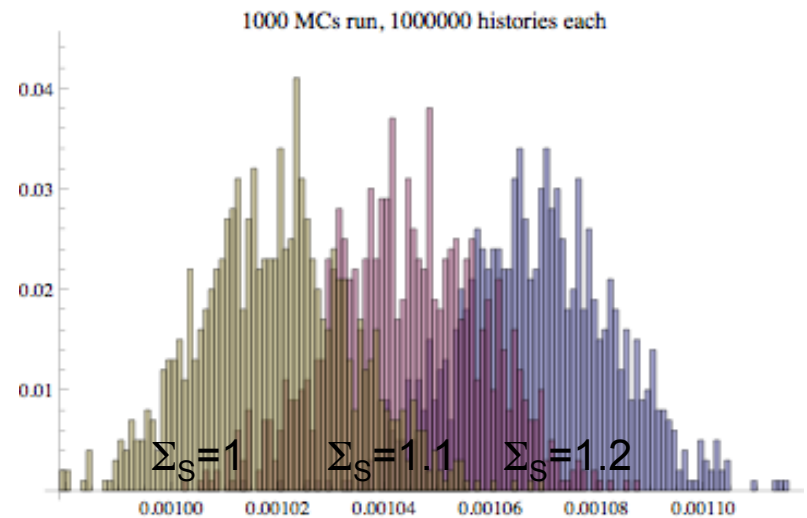
- Simple **geometry**: a sphere
- Macroscopic cross section (i.e. **probability**) for each process: scattering, absorption...
- **Tallies** (e.g. particle flux) in various positions

**How do uncertainties in the cross section affect the tally?**

We vary the “ingredients”, e.g. the scattering cross section  $\Sigma_S$   
 We observe the effect on the tally



Tally near the source:  
 higher statistics



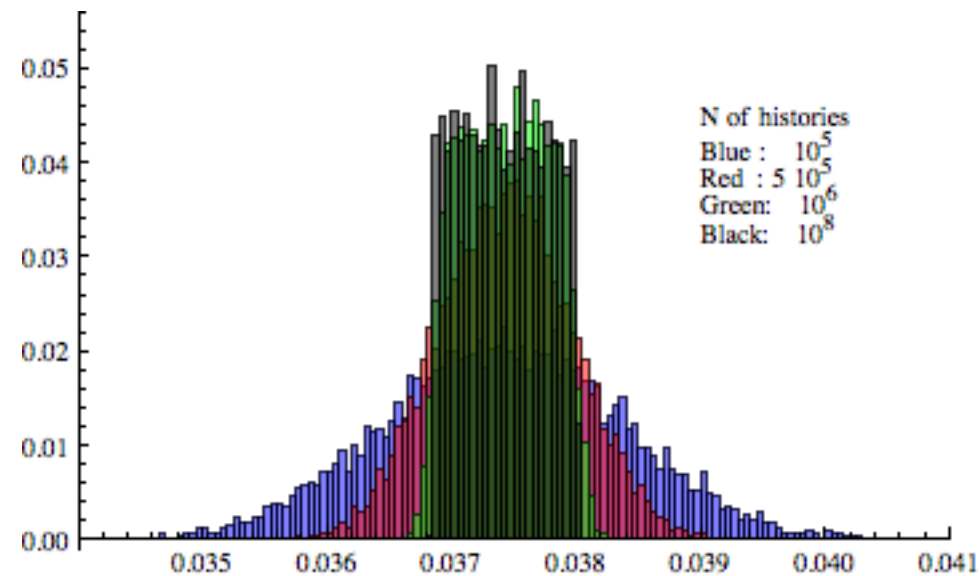
Tally far from source:  
 lower statistics

The Central Limit Theorem ensures that we can reduce the widths by increasing the number of histories in each Monte Carlo run:

$$\sigma_{\langle t \rangle} \cong \sigma_t / \sqrt{N}$$

For instance, here  $\Sigma_S$  varies continuously with a flat distribution in a given interval  $1.0 < \Sigma_S < 1.2$

We observe the effect on the tally



If the number of histories  $N$  is “small”, the outcome may be confused with a gaussian distribution

As the number of histories in each MC increases, the outcome becomes closer and closer to a flat distribution (*the same form we assumed for the variability of the ingredient*)

**MC simulation transfers the original form of the uncertainty into the final outcome, adding some statistical “noise”**

This stems from the identity:

$$\lim_{\sigma \rightarrow 0} \sqrt{\frac{1}{2\pi\sigma^2}} \int_{-\infty}^{\infty} p(x_0) \exp\left[-\frac{(x-x_0)^2}{2\sigma^2}\right] dx_0 = p(x)$$

The statistical “noise” can be reduced in principle arbitrarily by increasing the number of histories

If we run many N-histories MCs varying the parameter(s)  $\Sigma_S$  in some interval with probability  $f(\Sigma_S)$ , the final distribution of the tally will be

$$G(x) = \int_{-\infty}^{+\infty} f(\Sigma_S) \exp\left[-\frac{(x - x_0(\Sigma_S))^2}{2\sigma^2_{x_0} / N}\right] \sqrt{\frac{N}{2\pi\sigma^2_{x_0}}} d\Sigma_S$$

exact mean  
value of the tally

(invertible)  
function  $x_0(\Sigma_S)$

original value of  
the “ingredient”

This assumption relies on the interpretation of the simulation as a surrogate for the solution of **Boltzman transport equation**

In the limit of infinite histories

$$G(x) = K \left| \frac{d\Sigma_S(x)}{dx} \right| f(\Sigma_S^{-1}(x))$$

If the range of variability of  $\Sigma_S$  is sufficiently small,  
 $x(\Sigma_S)$  can be approximated by a linear relation



the final distribution of tallies has the same form of the original uncertainty

$$\Sigma_{\min} \leq \Sigma_S \leq \Sigma_{\max}$$



$$X_{\min} \leq X \leq X_{\max}$$

# Ongoing activity

Further work in progress

*two papers in preparation*

Deal with { many ingredients  
many observables

Define **best practices**  
to quantify uncertainties of a simulation

Experimental application use cases

...along with Geant4 physics validation

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- Andreas Zoglauer



Maria Grazia Pia, *INFN Genova*



# Thank you, Thomas!

*post workshop...*

Commonality across different disciplines

**Uncertainty Quantification**  
Epistemic uncertainties

Cross-disciplinary cooperation?

**Beyond the IPA**  
Physics calculations

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<http://www.nss-mic.org/2013/>

Seoul, 27 October – 2 November 2013

Abstracts: 13 May 2013

IEEE Nuclear Science Symposium  
Contributions concerning Monte Carlo methods  
are welcome!

IEEE Transactions on Nuclear Science

Nuclear, particle physics, astrophysics,  
space science, medical physics,  
photon science etc.

