

Graduate School 1504 „Mass, Spectra, Symmetry“
Autumn Block Course, September 9-12, 2012, Berlin

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Neutrinos in the Standard Model of Particle Physics

Neutrino oscillations:

experiments with atmospheric,
solar, accelerator and reactor neutrinos

Neutrino masses:

- cosmology and astrophysics
- neutrinoless double β decay
- direct neutrino mass experiments

Neutrino telescopes



Remark: each mass term has to be a scalar ($\bar{\psi}\psi$) and an isospin singlet

Fermion mass terms in the Standard Model by coupling to the Higgs:

$$\mathcal{L} = -f_e (\bar{\nu}_e, \bar{e})_L \begin{pmatrix} \Phi^+ \\ \Phi^0 \end{pmatrix} e_R = -\frac{f_e \cdot v}{\sqrt{2}} \cdot \bar{e}_L e_R =: -m_e \cdot \bar{e}_L e_R \quad (\dots + h.c.)$$


To obtain **massive neutrinos** also such “Dirac mass terms” are in principle possible by introducing right-handed neutrinos.

But it is very “unnatural” to have at least 6 orders smaller Yukawa-couplings to the Higgs !

For neutral Majorana particles more terms are allowed:

$$\begin{aligned} -2\mathcal{L}_\nu &= m_D \left(\bar{\nu}_L \nu_R + \overline{(\nu_R)^c} (\nu_L)^c \right) + m_{LL} \bar{\nu}_L (\nu_L)^c + m_{RR} \overline{(\nu_R)^c} \nu_R + h.c. \\ &= \left(\bar{\nu}_L \overline{(\nu_R)^c} \right) \begin{pmatrix} m_{LL} & m_D \\ m_D & m_{RR} \end{pmatrix} \begin{pmatrix} (\nu_L)^c \\ \nu_R \end{pmatrix} + h.c. \\ &= \left(\bar{\nu}_L \overline{(\nu_R)^c} \right) \mathcal{M} \begin{pmatrix} (\nu_L)^c \\ \nu_R \end{pmatrix} + h.c. \end{aligned}$$

lepton number violating $\Delta L=2$



The matrix \mathcal{M} can be diagonalized

⇒ 2 Majorana neutrino mass states m_1, m_2

Seesaw mechanism

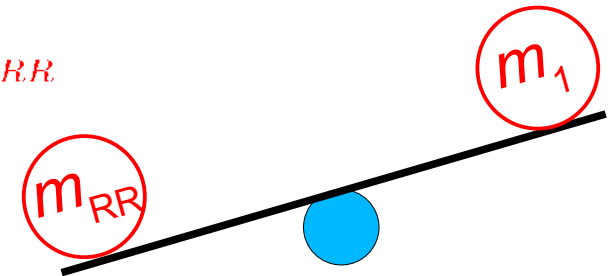
Assume $m_{LL} \approx 0$ (otherwise we will get a problem with e_L mass terms, since it appears within the $(\nu_e, e)_L$ isospin doublet)

and $m_{RR} \gg m_D$

$$-2\mathcal{L}_\nu = \begin{pmatrix} \overline{\nu_L} & \overline{(\nu_R)^c} \end{pmatrix} \begin{pmatrix} 0 & m_D \\ m_D & m_{RR} \end{pmatrix} \begin{pmatrix} (\nu_L)^c \\ \nu_R \end{pmatrix} + h.c.$$

$$\Rightarrow m_1 \approx m_D^2/m_{RR} \quad m_2 \approx m_{RR}$$

Seesaw effect: if m_{RR} gets big, then m_1 gets small



Is such a mass term realistic ?

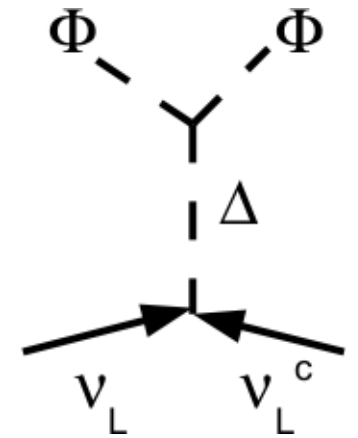
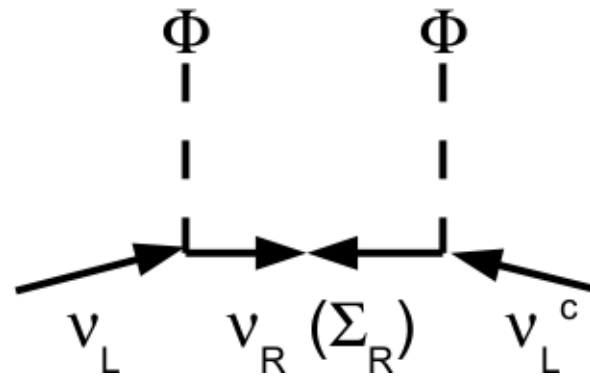
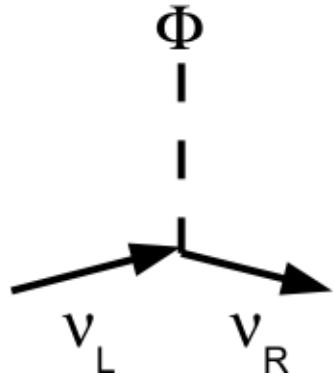
Since $(\nu_L)^c \nu_L$ is a SU(2) triplet, the most simple possible form is:

$$\mathcal{L}_{eJJ} = G/M \cdot \overline{\Phi^c} \Phi (\nu_L, e_L)^c (\nu_L, e_L)$$

where M is an effective mass of an effective field theory, in which the heavy neutrinos $N = \nu_R$ are integrated out.

Expect M on a very large scale, e.g. $M \approx M_{GUT}$

\Rightarrow Seesaw mechanism allows to address large scale M of new physics



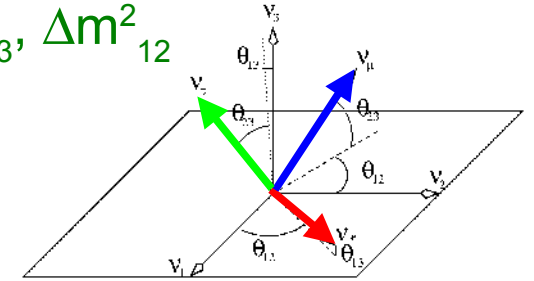
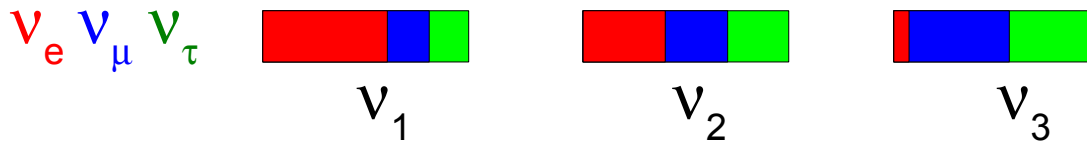
a) Realisation with Higgs doublet Φ like all other fermions
 → very small Yukawa couplings

b) right-handed heavy Majorana neutrinos ν_R (seesaw I)
 or right-handed fermionic triplett Σ_R (seesaw III)

c) Higgs-triplet ξ (no -right-handed neutrinos needed !) (seesaw II)

Need for the absolute ν mass determination

Results of recent oscillation experiments: Θ_{23} , Θ_{12} , Θ_{13} , Δm^2_{23} , Δm^2_{12}



degenerated masses

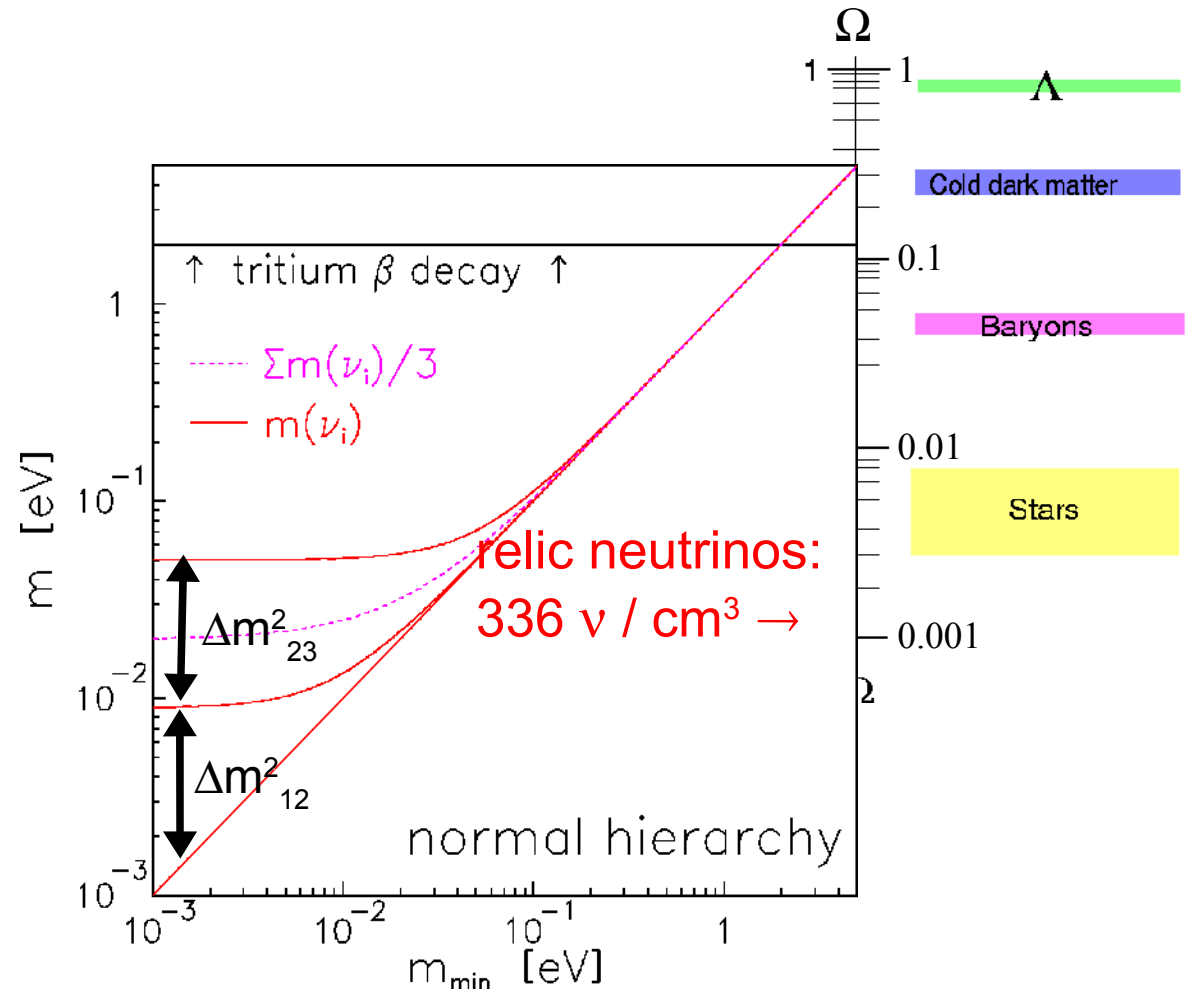
cosmological relevant

e.g. seesaw mechanism type 2

hierarchical masses

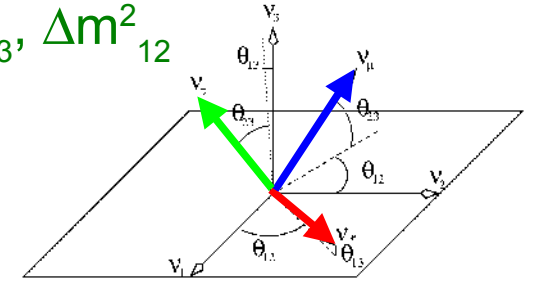
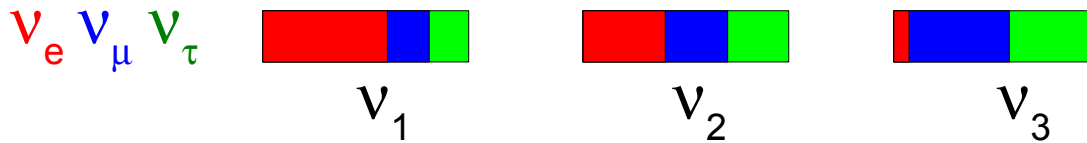
e.g. seesaw mechanism type 1

explains smallness of masses, but not large (maximal) mixing



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degenerated masses

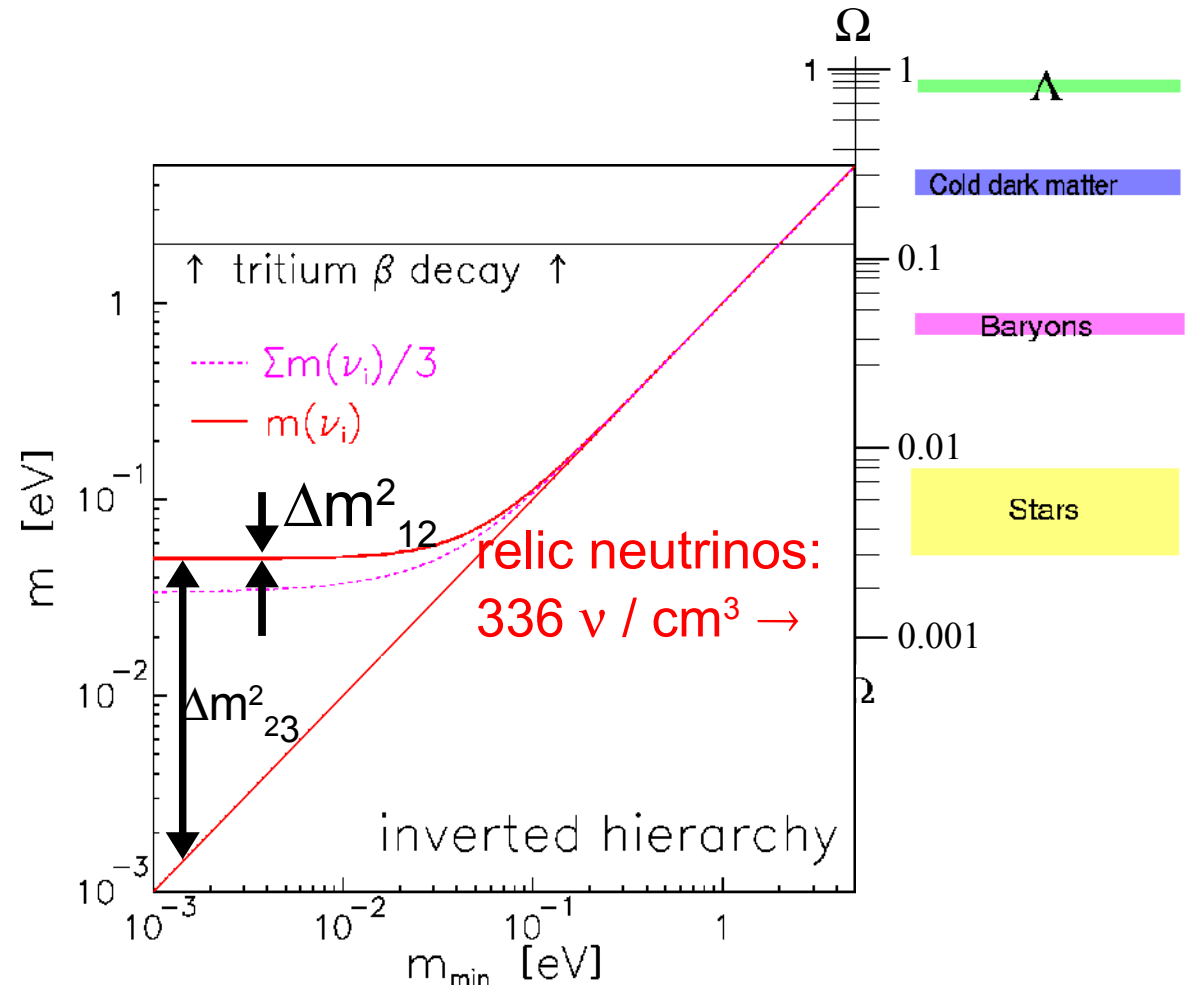
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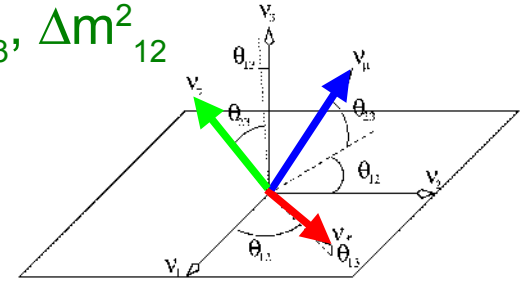
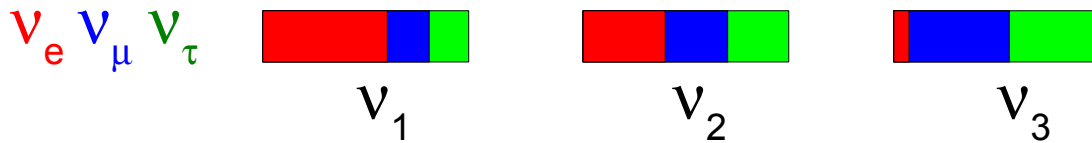
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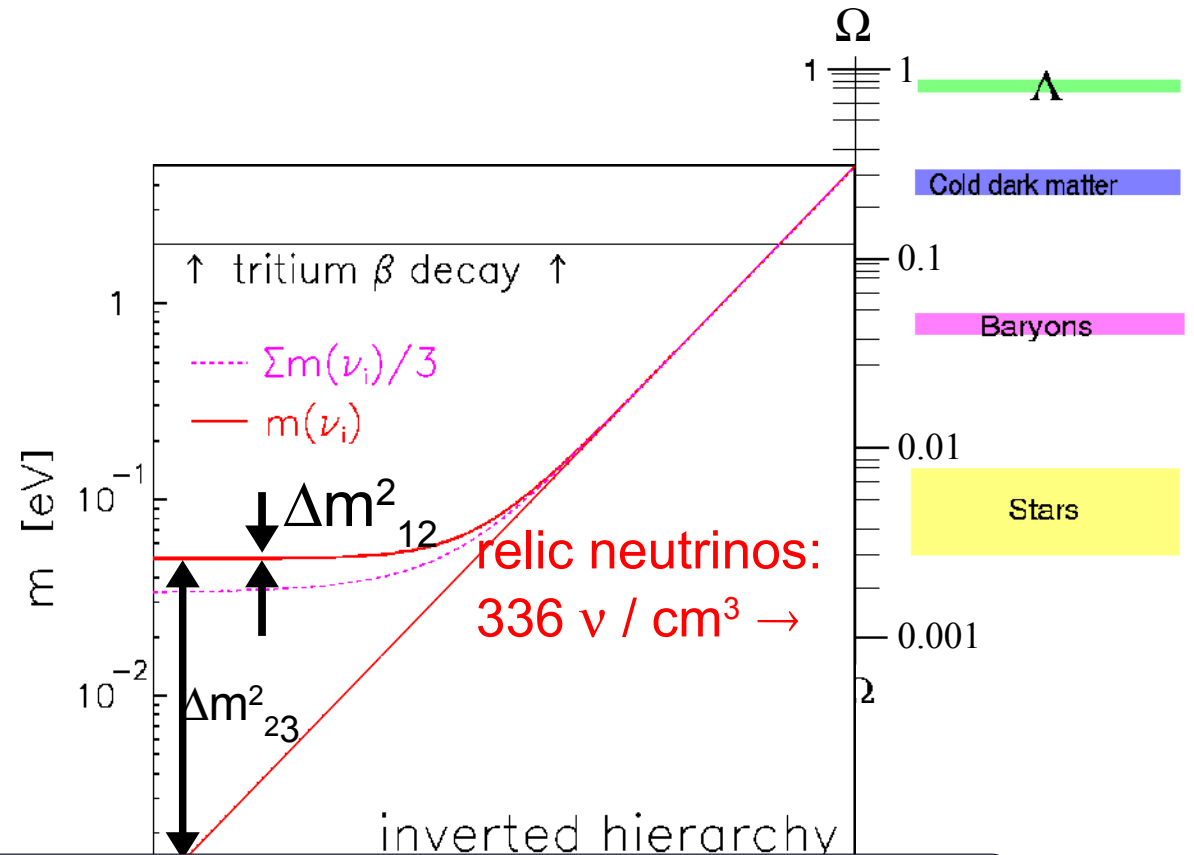
Need for the absolute ν mass determination

Results of recent oscillation experiments: Θ_{23} , Θ_{12} , Θ_{13} , Δm^2_{23} , Δm^2_{12}



degenerated masses
cosmological relevant
e.g. seesaw mechanism type 2

hierarchical masses
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explains smallness of masses,
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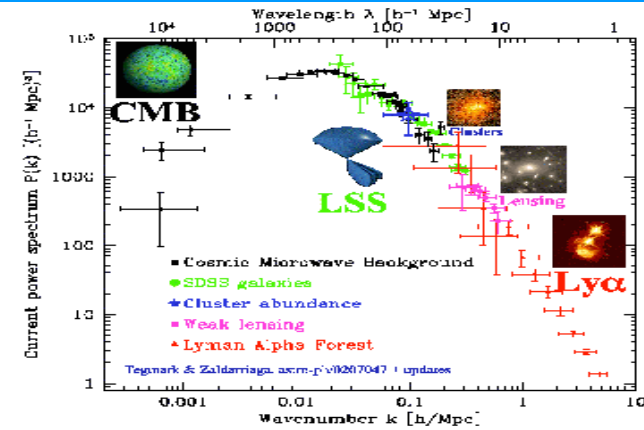


Need neutrino mass from non-oscillation method !

Three complementary ways to the absolute neutrino mass scale

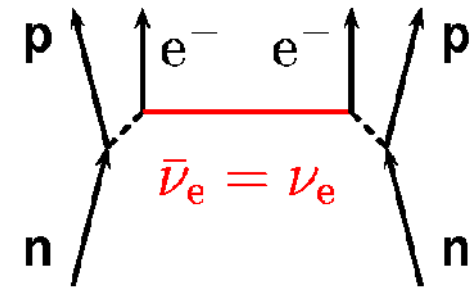
1) Cosmology

very sensitive, but model dependent
compares power at different scales
current sensitivity: $\Sigma m(\nu_i) \approx 0.4 - 1 \text{ eV}$



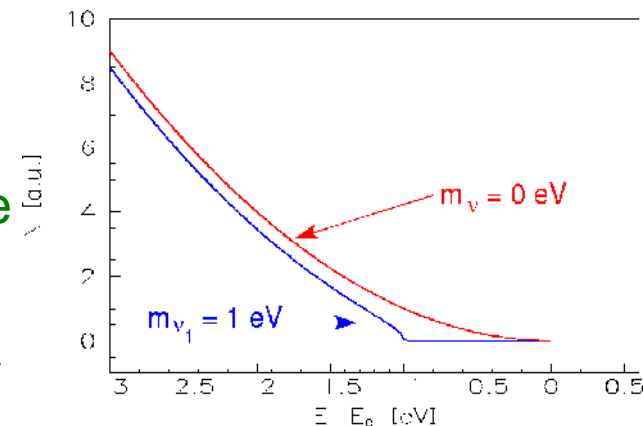
2) Search for $0\nu\beta\beta$

Sensitive to Majorana neutrinos
Evidence for $m_{ee}(\nu) \approx 0.3 \text{ eV}$ (Klapdor-Kleingrothaus et al.)?
New upper limit by EXO-200, GERDA is running

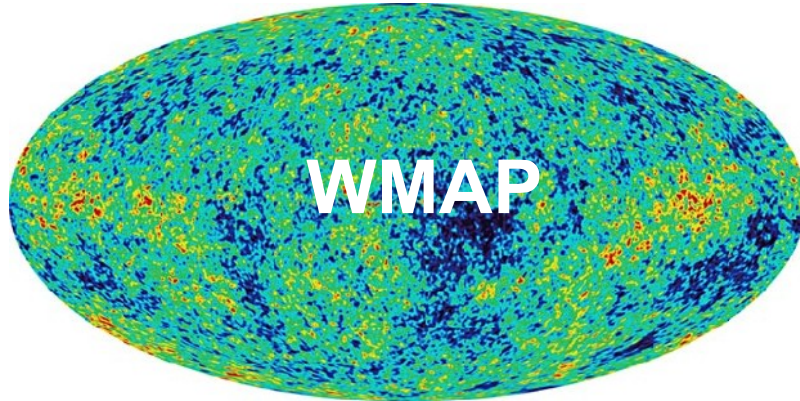


3) Direct neutrino mass determination:

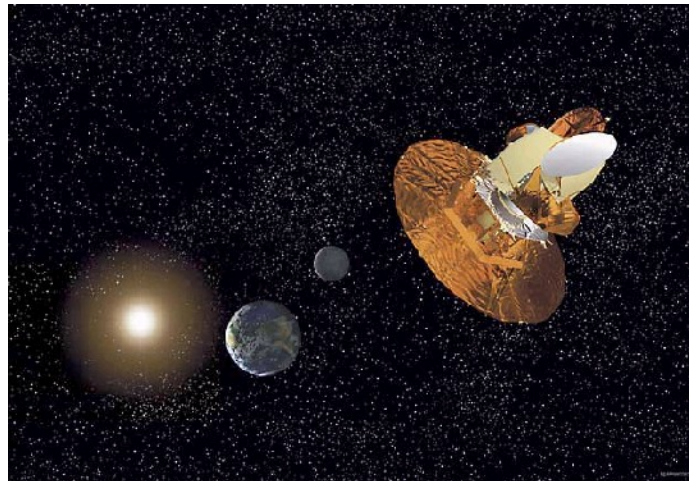
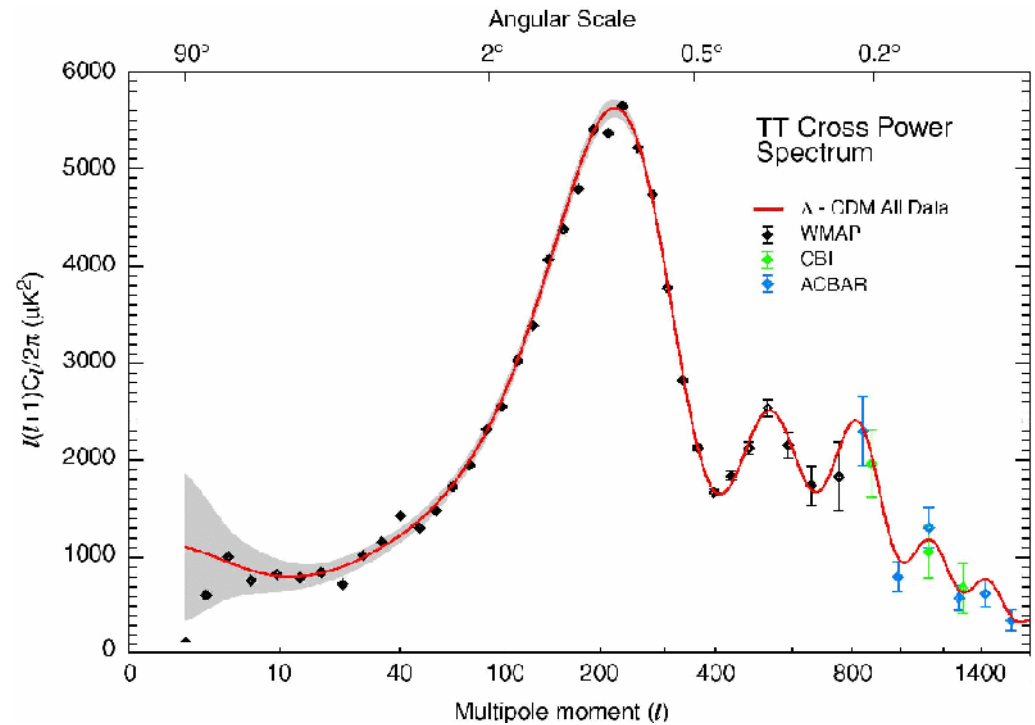
No further assumptions needed. no model dependence
use $E^2 = p^2c^2 + m^2c^4 \Rightarrow m^2(\nu)$ is observable mostly
most sensitive methode: endpoint spectrum of β -decay



Neutrino mass from cosmology

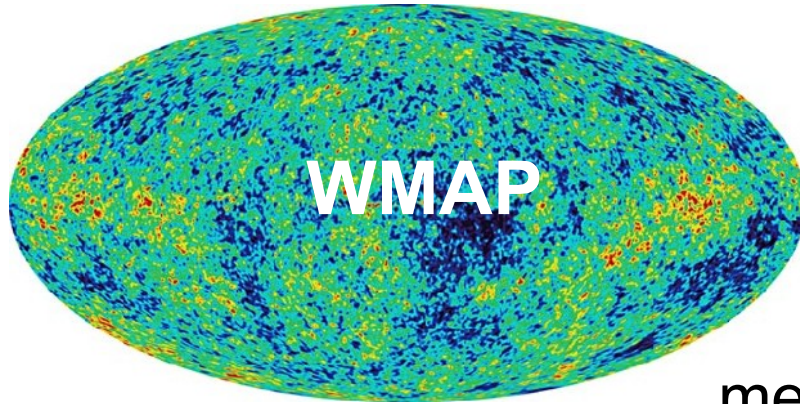


measurement of CMBR
(Cosmic Microwave Background Radiation)



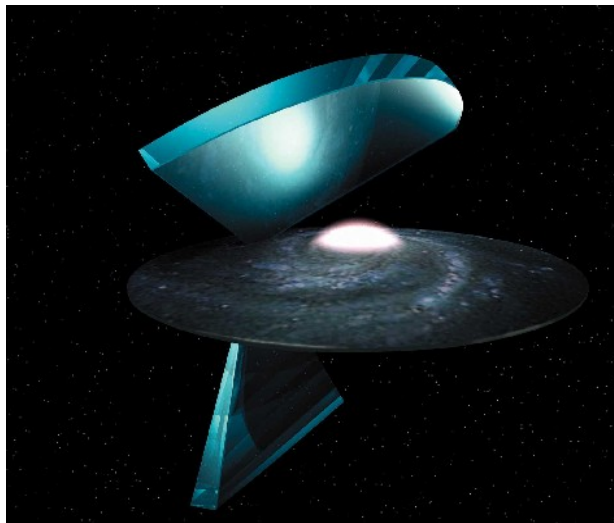
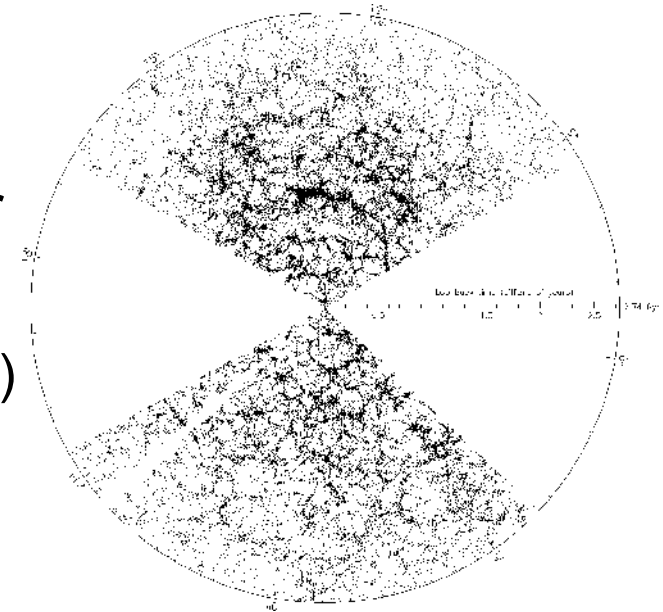
D.N. Spergel et al., astro-ph/0302209

Neutrino mass from cosmology



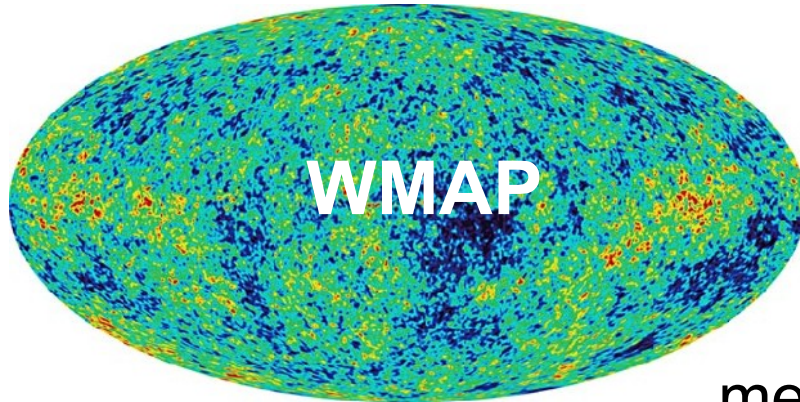
measurement of CMBR
(Cosmic Microwave Background Radiation)

measurement of matter
density distribution
LSS (Large Scale Structure)
2dF, SDSS, ...



2dF: M. Colless et al., MNRAS 328 (2001) 1039
SDSS: M. Tegmark et al., Astrophys.J. 606 (2004) 702-740

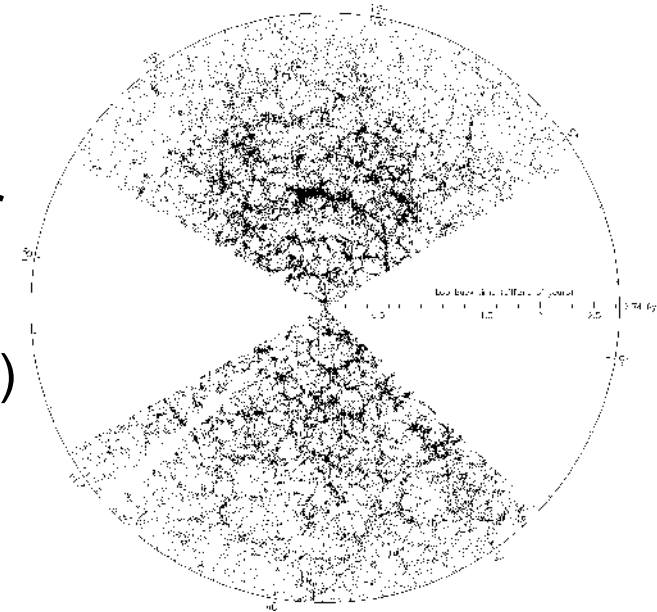
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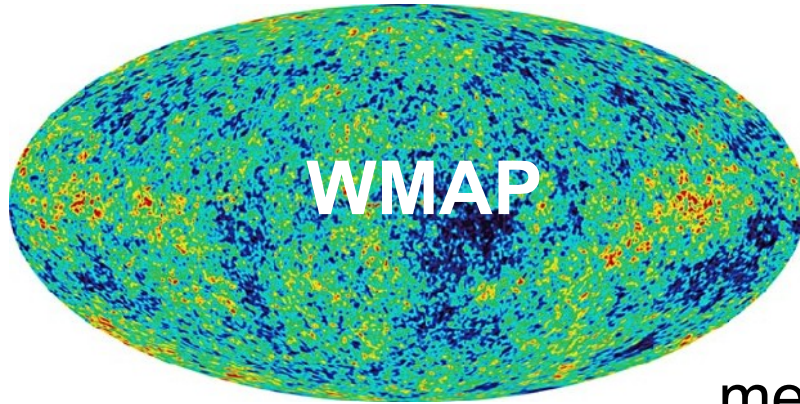


big bang theory:

neutrino density in universe

$$n_{\nu} = 336 / \text{cm}^3$$

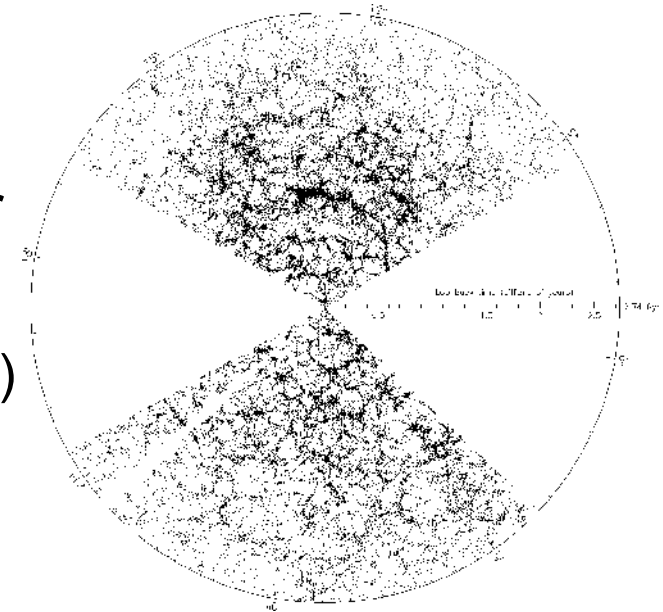
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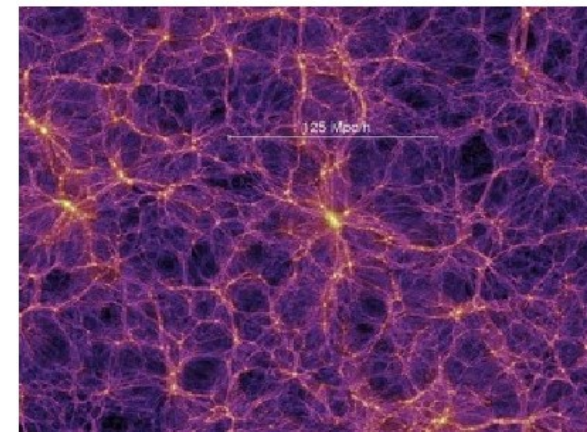
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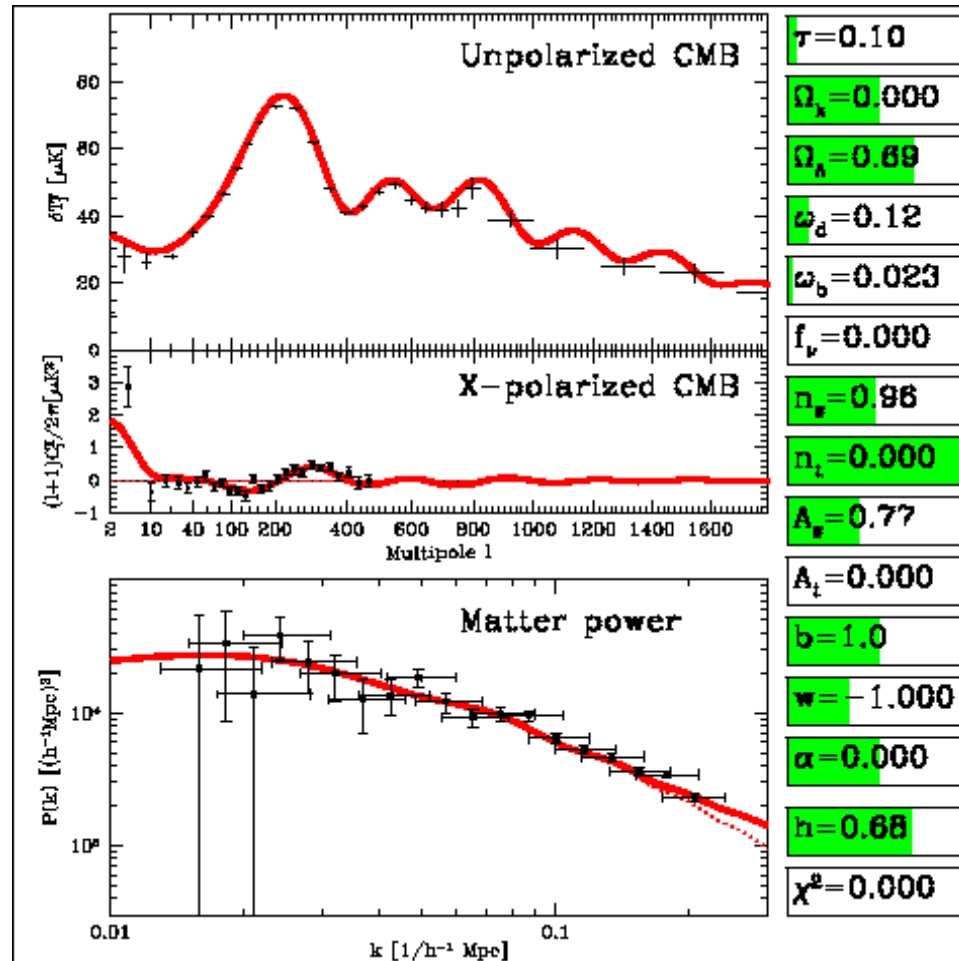
model development

← National Center for SuperComputer Simulations,
<http://cosmicweb.uchicago.edu/sims.html>

Millenium simulation →
<http://www.mpa-garching.mpg.de/galform/presse/>



Fraction of “hot” to “cold” dark matter

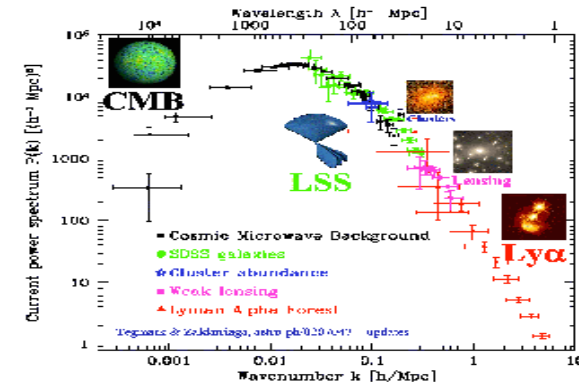


from http://space.mit.edu/home/tegmark/movies_60dpi/fn_movie.gif

E. Komatsu et al. (WMAP, 5 years, arXiv:0803.0547)

$$\Sigma m(\nu_i) < 0.67 \text{ eV}$$

CMB, LSS, SN data, always assuming the cosmological concordance model with cosmological constant $\Lambda = \text{const.}$, no quintessence



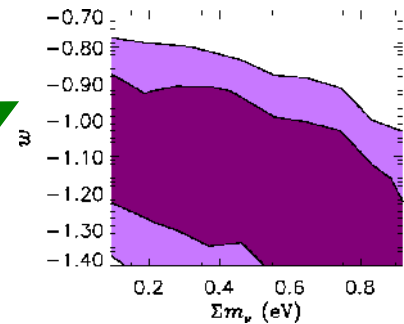
S. Hannestad, Prog. Part. Nucl. Phys. 65 (2010) 185

$$\Sigma m(\nu_i) < 0.5 \text{ eV}$$

using baryon acoustic peaks

Remark: w is correlated to $\Sigma m(\nu_i)$ (arXiv:0709.4152, 0505.551)

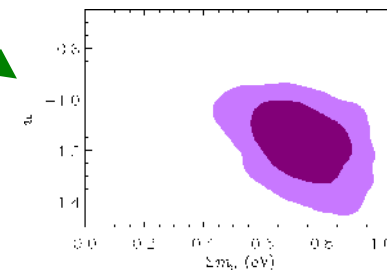
\Rightarrow neutrino mass determination can help dark energy (arXiv0710.1952)



Ch. Wetterich et al. (e.g. arXiv:0905.0715): avoids bound on $\Sigma m(\nu_i)$

ν coupling to cosmon (quintessence model for dark energy)

leads to growing neutrino mass

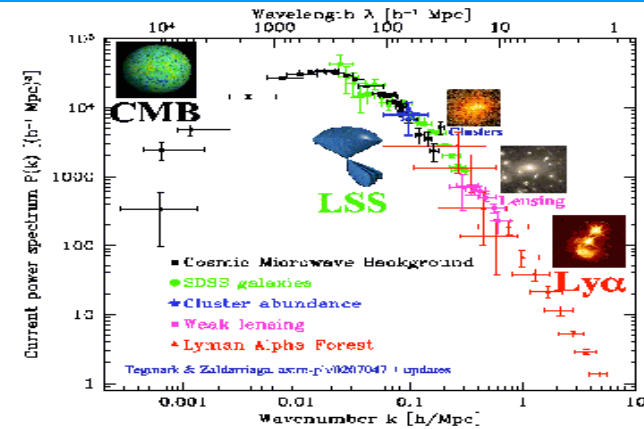


O.E. Bjaelde et al. (astro-ph/0705.2018): ν coupling to scalar field leads to time-varying neutrino mass and connection to dark energy

Three complementary ways to the absolute neutrino mass scale

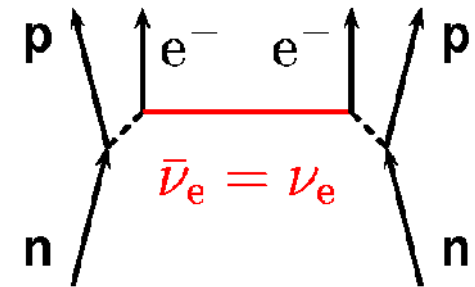
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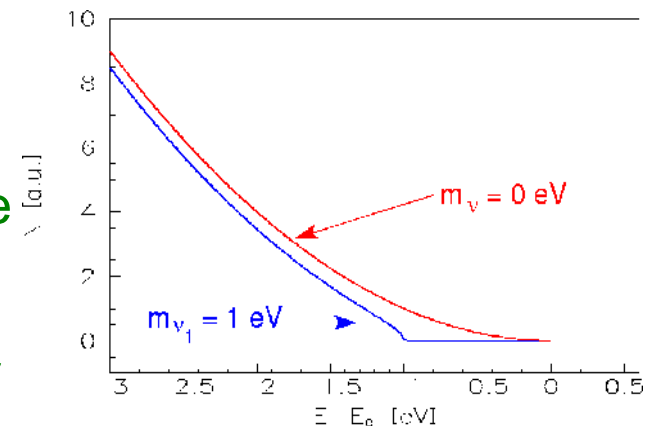
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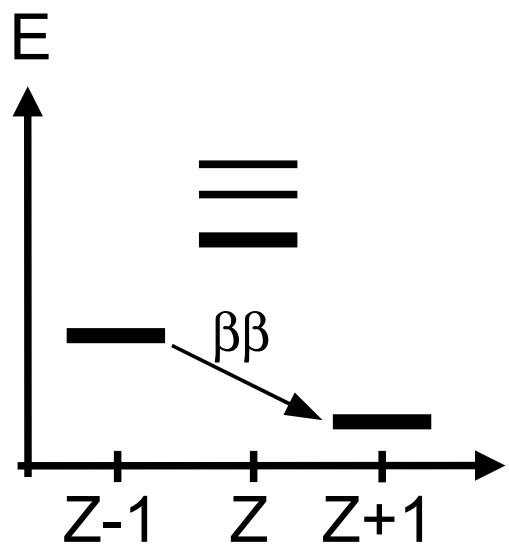


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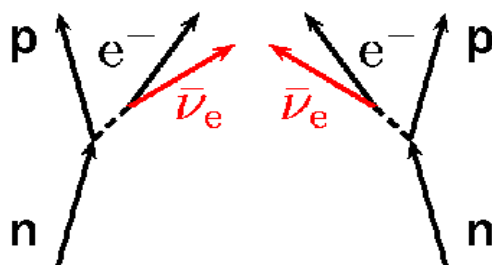
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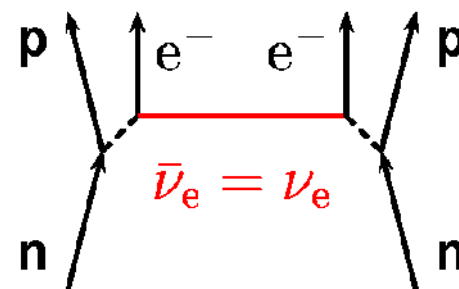
Double β decay



normal ($2\nu\beta\beta$)



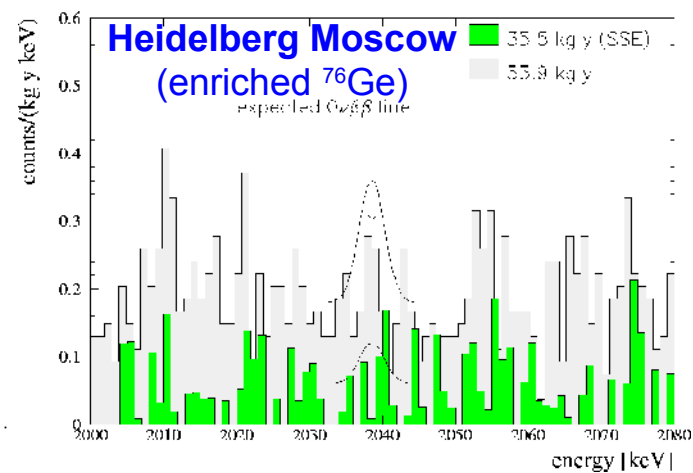
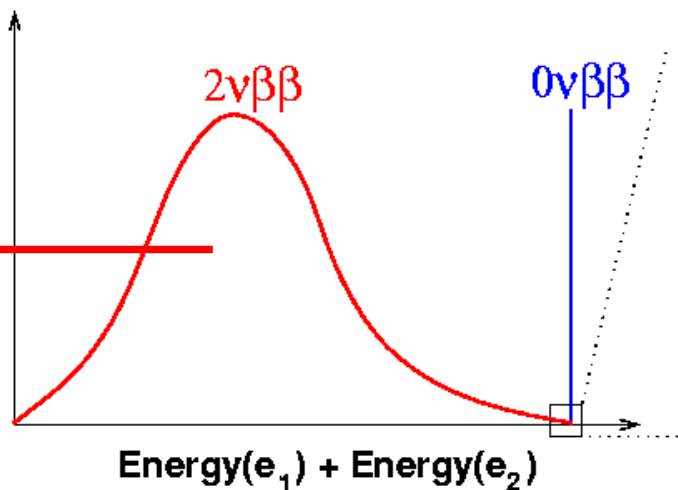
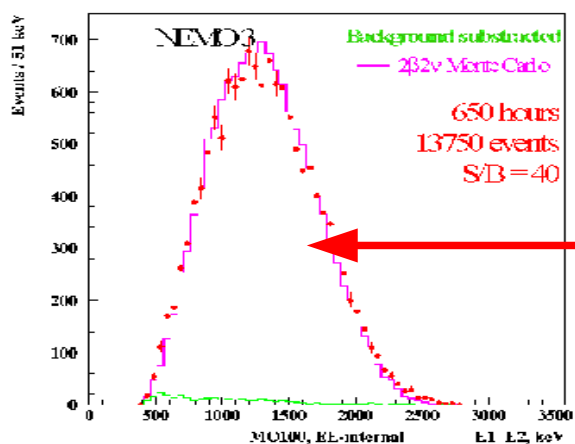
neutrinoless ($0\nu\beta\beta$)



needed: a) $\bar{\nu} = \nu$ (Majorana)

b) helicity flip: $m(\nu) \neq 0$

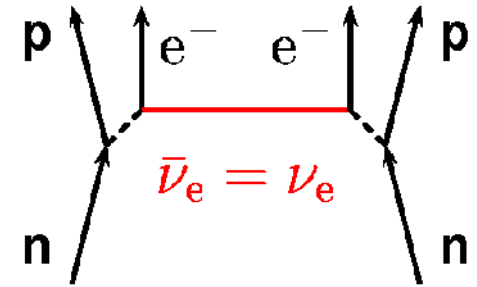
or other new physics



Neutrinoless double β decay: $0\nu\beta\beta$

Weak interaction: left-handed fermions $\Psi_L = (1 - \gamma_5)/2 \Psi$
couple to charge current

$0\nu\beta\beta$: decay rate is proportional to fraction of
positive helicity state within Ψ_L



$$\begin{aligned}
 \Gamma &\sim u_2^+ u_L = W'(\mathcal{H} = +1) \\
 &= \frac{1}{2}(1 - \beta_\nu) \\
 &= \frac{1}{2}\left(1 - \frac{p_\nu c}{E_\nu}\right) = \frac{1}{2}\left(\frac{E_\nu - p_\nu c}{E_\nu}\right) \\
 &= \frac{1}{2} \frac{\sqrt{p_\nu^2 c^2 + m_\nu^2 c^4} - p_\nu c}{E_\nu} \\
 &= \frac{p_\nu c}{2E_\nu} \left(\sqrt{1 + \frac{m_\nu^2 c^2}{p_\nu^2}} - 1 \right) \\
 &\quad \approx \frac{1}{2} \\
 &= \frac{1}{2} \left(1 + \frac{m_\nu^2 c^2}{2p_\nu^2} - 1 \right) \sim m_\nu^2
 \end{aligned}$$

more complete

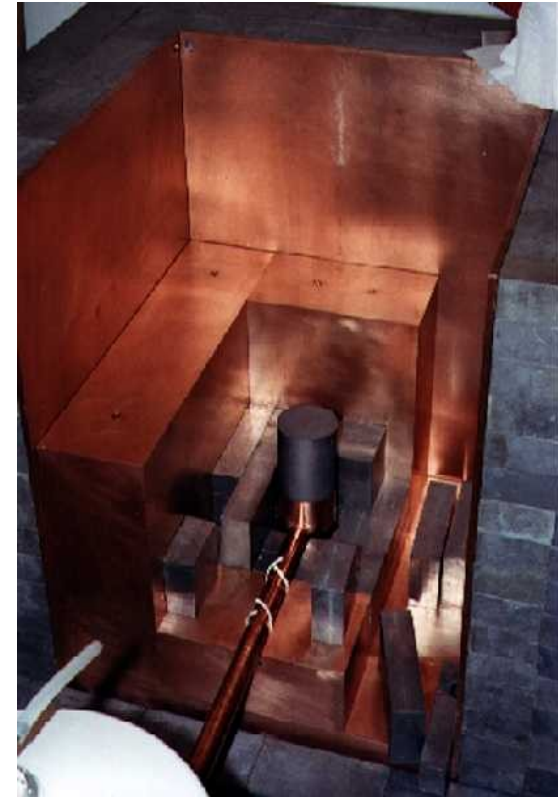
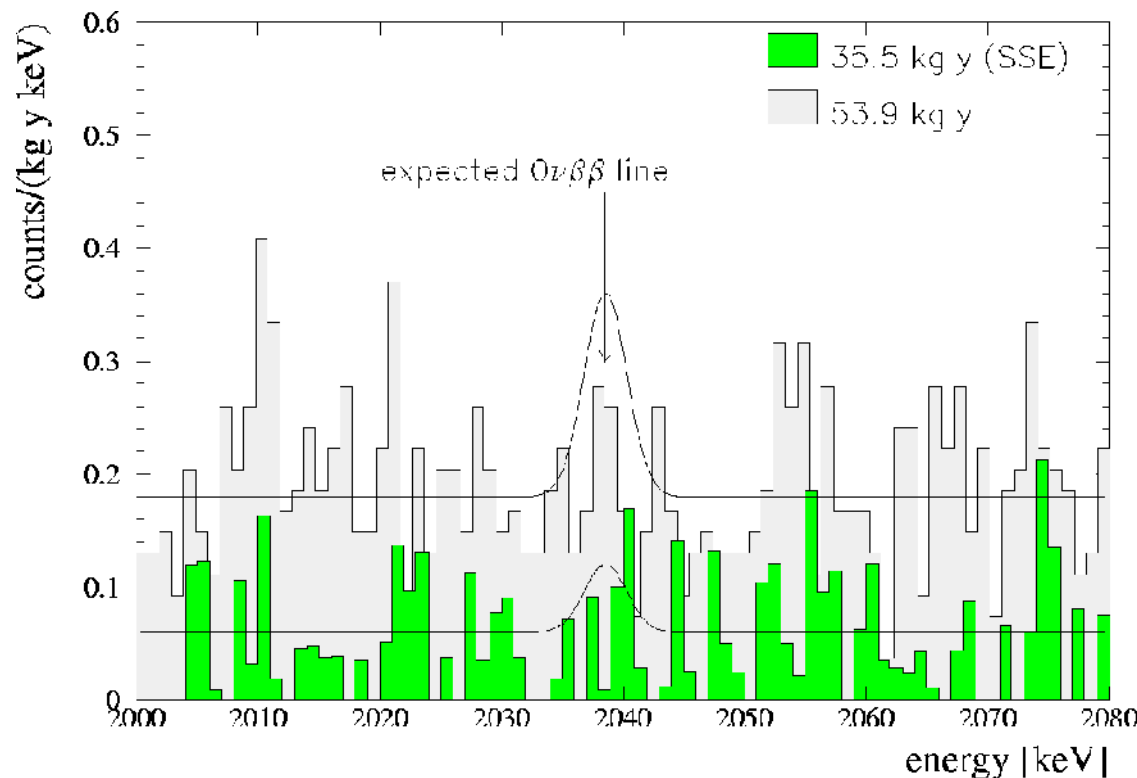
decay rate $\propto m_{ee}^2(\nu)$:

$$m_{ee}(\nu) = \left| \sum |U_{ei}|^2 e^{i\alpha(i)} m(\nu_i) \right|$$

(coherent sum over all neutrino mass eigenstates contributing to the electron neutrino)

\Rightarrow partial cancelation possible

- 5 Ge detectors, 10.9 kg total mass
- enriched ^{76}Ge (86%)
- in the Gran Sasso underground laboratory/italy
- digital puls shape analysis: reduction of background by a factor of 5



up to 2001: $0\nu\beta\beta$ not observed

$$T_{1/2} > 1.9 \cdot 10^{25} \text{ a}$$

$$\Rightarrow m_{ee} < 0.35 \text{ eV (90\% C.L.)}$$

H.V. Klapdor-Kleingrothaus et al.,
Eur. Phys. J. A12 (2001) 147

Evidence for $0\nu\beta\beta$ at Heidelberg Moscow Exp.?

New, data up to 2003: 72 kgy,
with new data selection, new calibration,
new analysis:
assume peaks in [2000,2060] keV,
some of them are known as ^{214}Bi lines

Klapdor-Kleingrothaus et al., PL B586 (2004) 198

⇒ Peak at 2038.1(5) keV (expected: 2039.006(50) keV)

Multi-Gauss. Fit: 4.2σ significance for $0\nu\beta\beta$

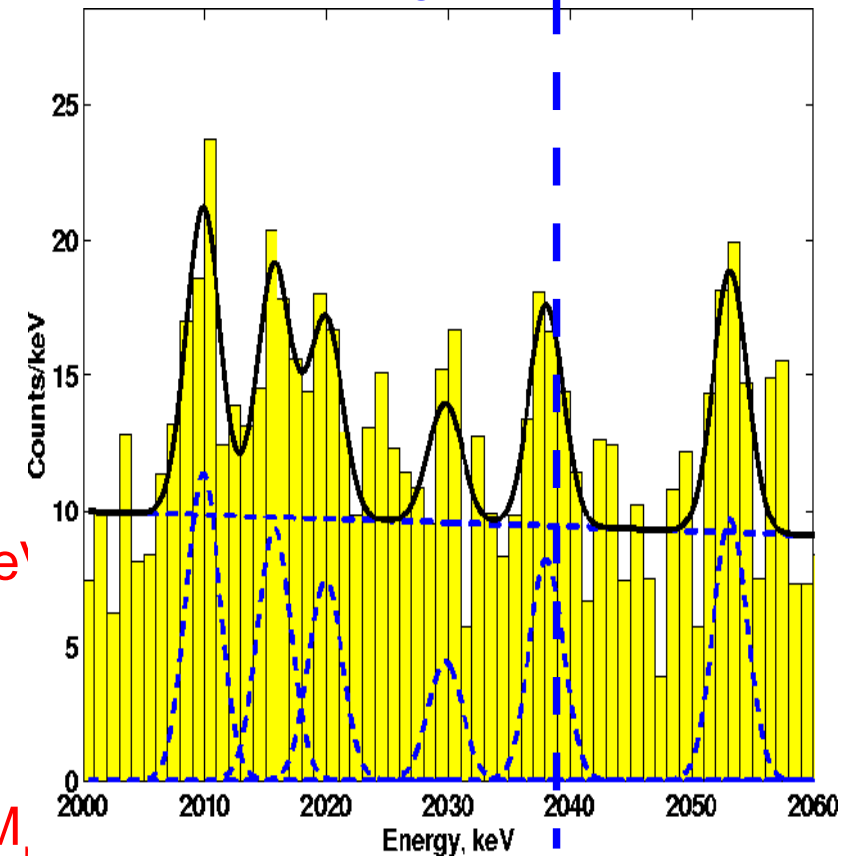
$$T_{1/2}^{0\nu} = (0.34-20.3) 10^{25} \text{ y}$$

⇒ $m_{ee} = 0.1-0.9 \text{ eV}$ (99.7% C.L., incl. uncertainty of $M_{\nu\nu}$)

⇒ Need to be checked by other experiments: NEMO, CUORICINO (CUORE),
EXO, GERDA

⇒ Nuclear matrix elements need to be worked on

expected signal position

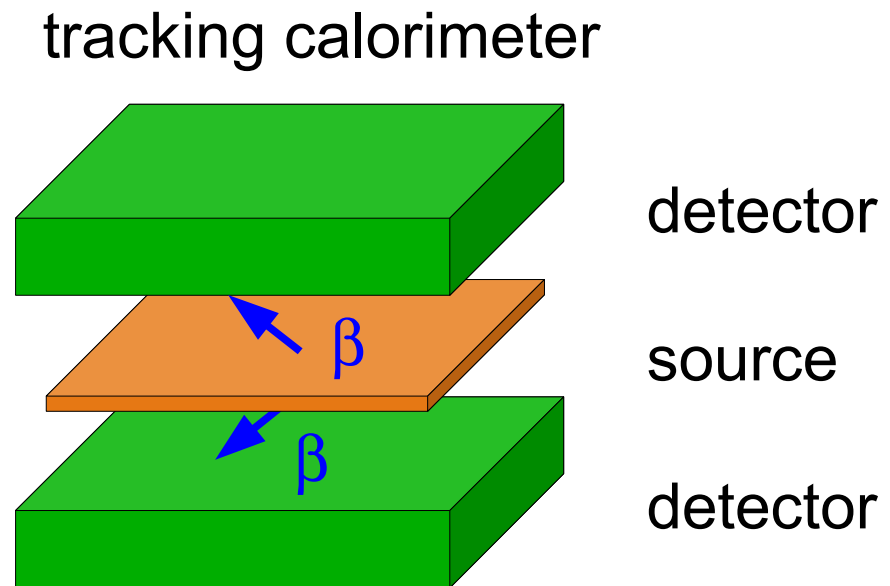
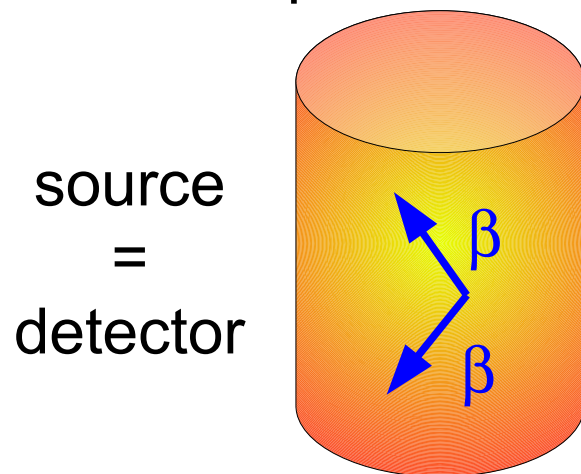


Current and future double β decay experiments

$$m_{ee} \sim (1/\text{enrichment})^{1/2} \cdot (\Delta E \cdot bg/M \cdot t)^{1/4}$$

\Rightarrow mass \rightarrow 1t, high enrichment, very low background bg

2 ways to measure both β -electrons:
 semiconductor,
 cryogenic bolometer
 liquid scintillator

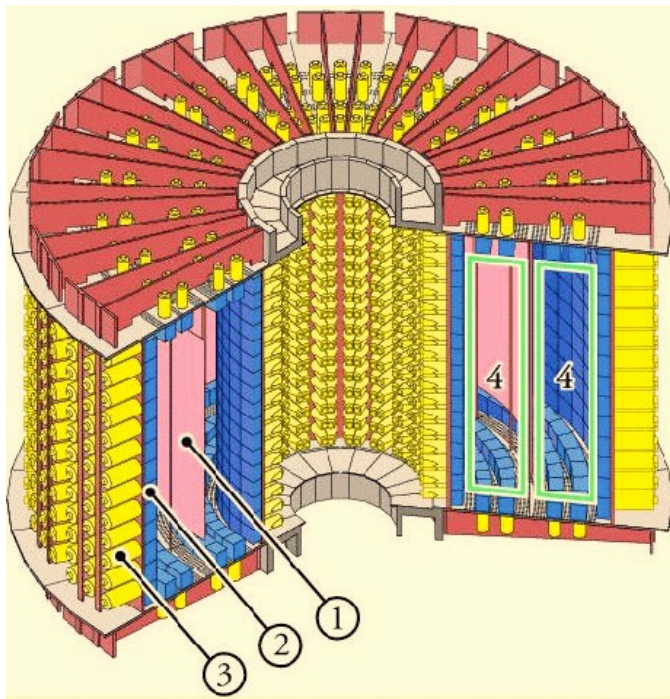


running: CUORICINO
 setting up: GERDA, CUORE, EXO-200
 planned: Majorana, EXO, COBRA, SNO+

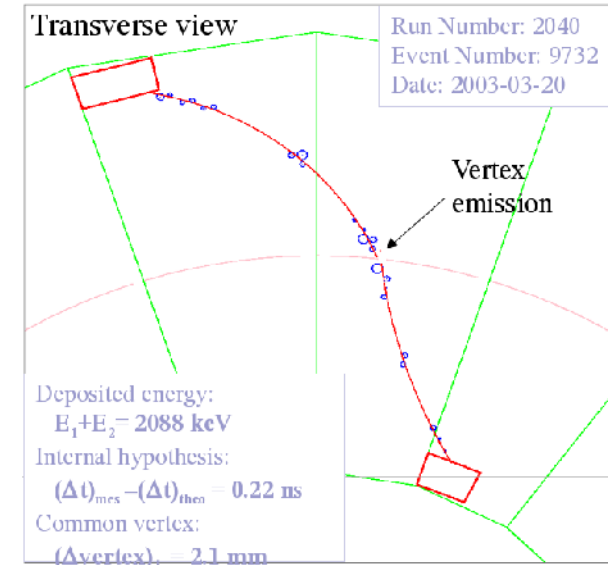
running: NEMO-3
 setting up: SuperNEMO
 ..planned: MOON

Searching for $0\nu\beta\beta$: NEMO3

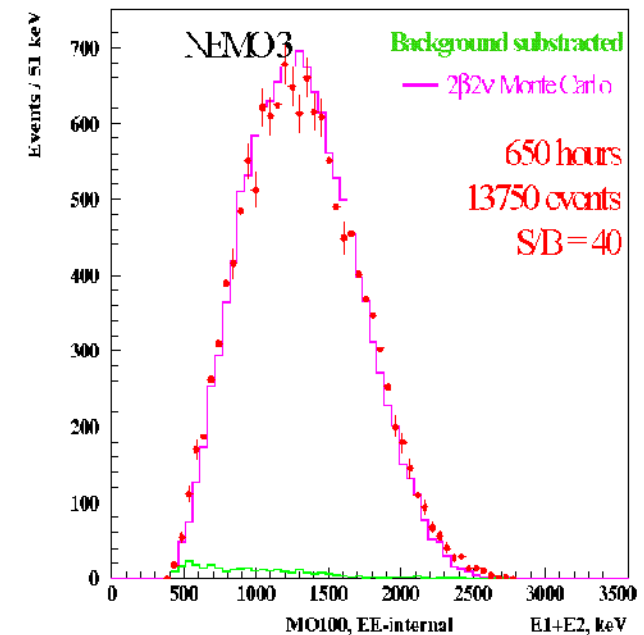
NEMO3: tracking calorimeter
(\rightarrow SuperNEMO with enr. ^{82}Se)



$2\nu\beta\beta$ of ^{100}Mo

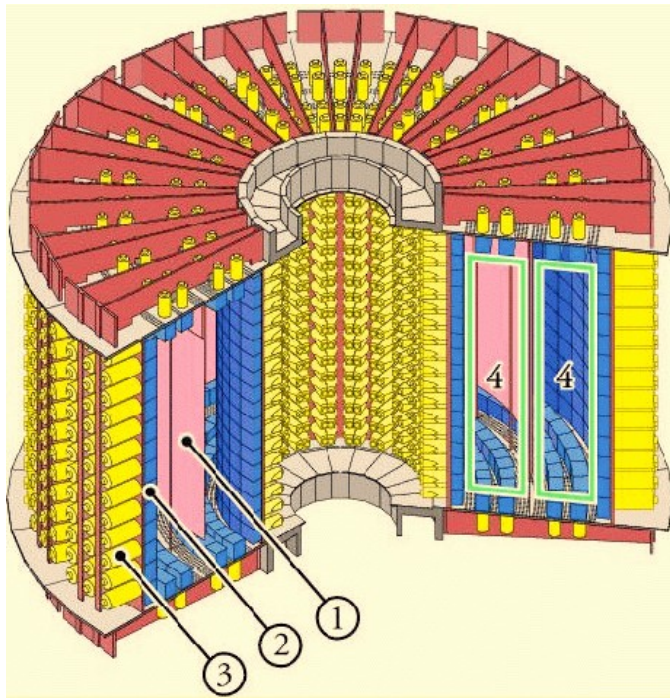


from Ruben Saakyan, DBD06



Searching for $0\nu\beta\beta$: NEMO3 → SuperNEMO

NEMO3: tracking calorimeter
with several isotopes
(finished Jan 2011)

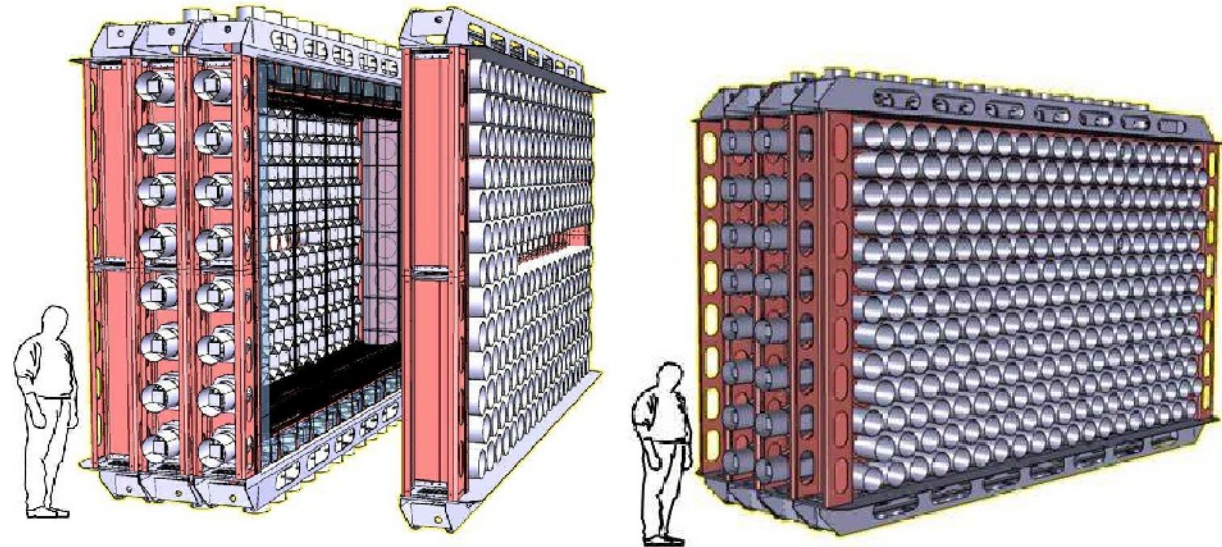


$$^{100}\text{Mo}: T_{1/2} (0\nu\beta\beta) > 1.1 \times 10^{24} \text{ y}$$

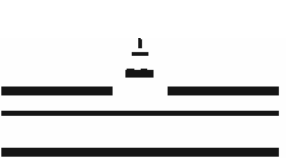
$$\Rightarrow m_{ee} < (0.45 - 0.93) \text{ eV}$$

F Mauger, TAUP09

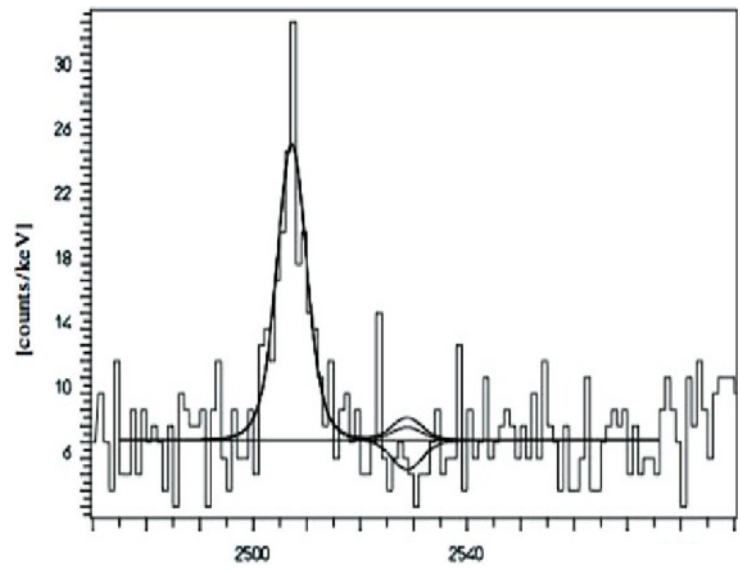
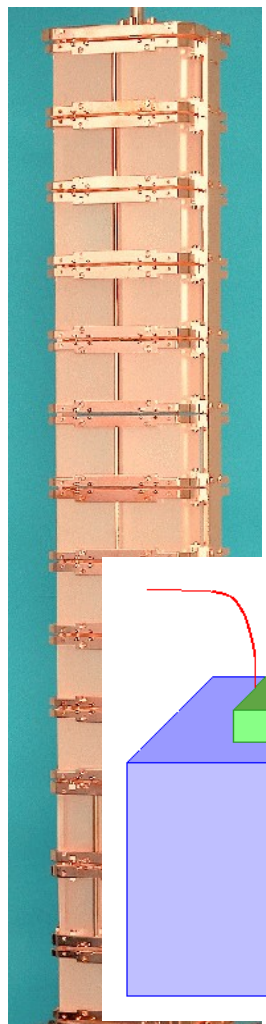
SuperNEMO:
tracking calorimeter modules
enriched ^{82}Se , ^{150}Nd



$$\text{expect sensitivity: } T_{1/2} (0\nu\beta\beta) > 10^{26}$$



Searching for $0\nu\beta\beta$: TeO_2 cryobolometers: CUORICINO \rightarrow CUORE



CUORICINO:

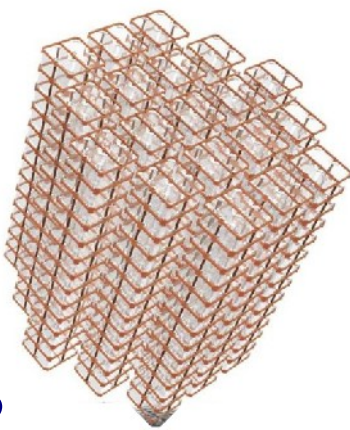
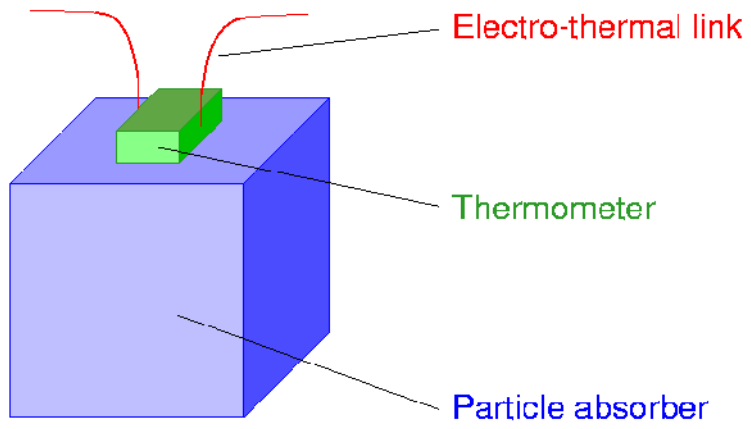
$^{130}\text{Te}: T_{1/2} > 3 \cdot 10^{24} \text{ y}$
 $\Rightarrow m_{ee} < 0.19 - 0.68 \text{ eV}$

PRC 78 (2008) 35502

In 5 years of live running time

Background [c/keV/kg/y]	ΔE_{FWHM} [keV]	$\tau_{1/2}^{0\nu}$ [y] @ 68% C.L.	m_{ee} [meV]			
			R(QRPA) ¹	pn(QRPA) ²	ISM ³	IBM-2 ⁴
0.01	5	2.1×10^{26}	35 ÷ 66	41 ÷ 67	65 ÷ 82	41
0.001	5	6.5×10^{26}	20 ÷ 38	23 ÷ 38	37 ÷ 47	23

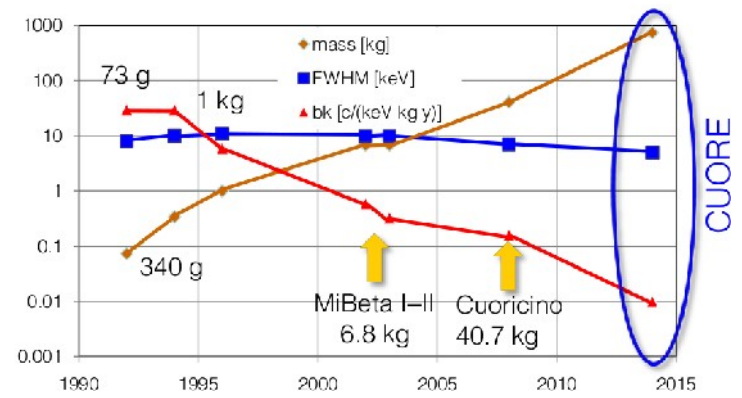
- 1 Šimkovic et al., PRC 77 (2008) 045503
- 2 Civitarese et al., JoP:Conference series 173 (2009) 012012
- 3 Menéndez et al., NPA 818 (2009) 139
- 4 Barea and Iachello, PRC 79 (2009) 044301

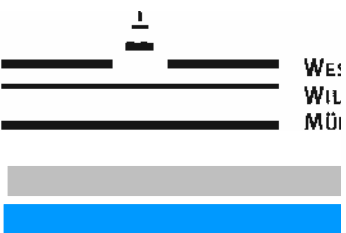


starting:

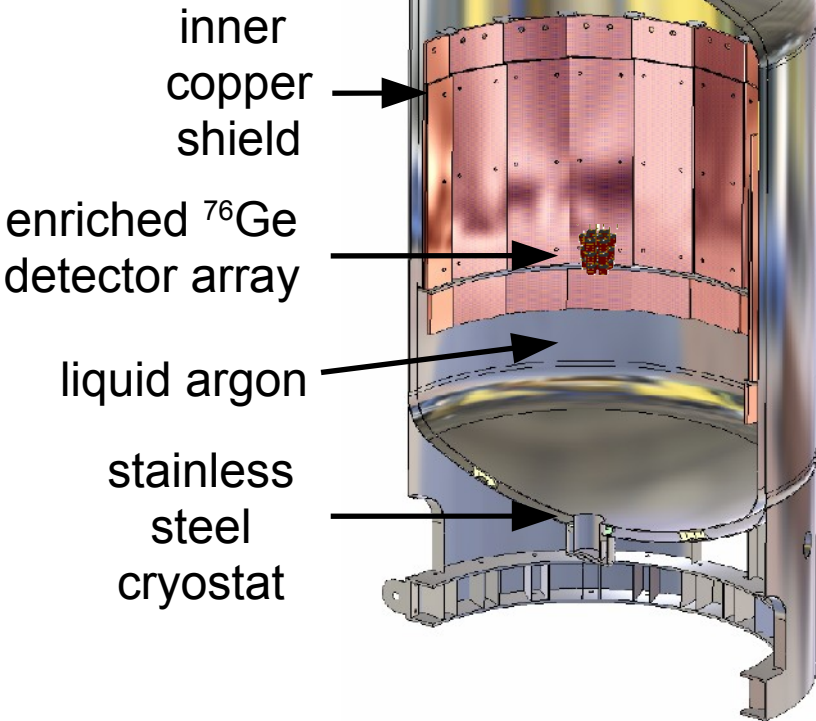
CUORE: 741 kg TeO_2

CUORE-0 will start in 2012





The GERDA experiment



New background reduction methods:

- naked Germanium detectors in noble liquid
- phase 2: point contact detectors p-type (BEGe) to identify multi-side events
- maybe use scintillation of LAr shield as veto

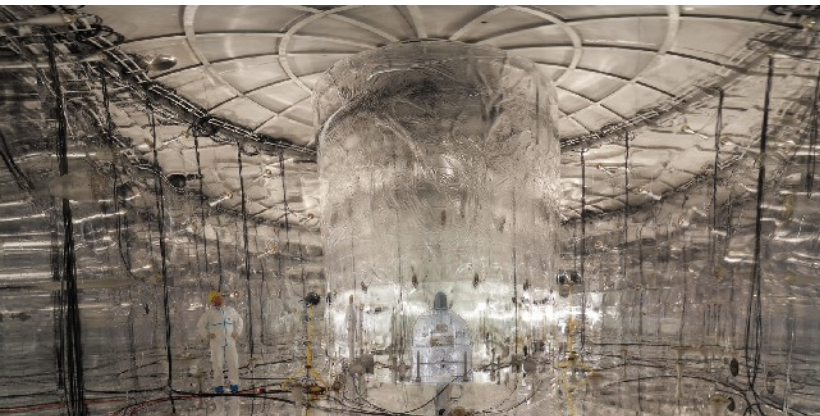
Phases of GERDA:

Phase 1: reuse old det. (Hd-Moscow, IGEX (18 kg))

*1st test string with 3 non-enriched detectors
problem $^{42}\text{Ar} \rightarrow ^{42}\text{K} \rightarrow ^{42}\text{Ca}$, seems to be solved
since Oct 2011: 8 enriched detectors (14.6 kg)
3 natural detectors (7.6 kg)*

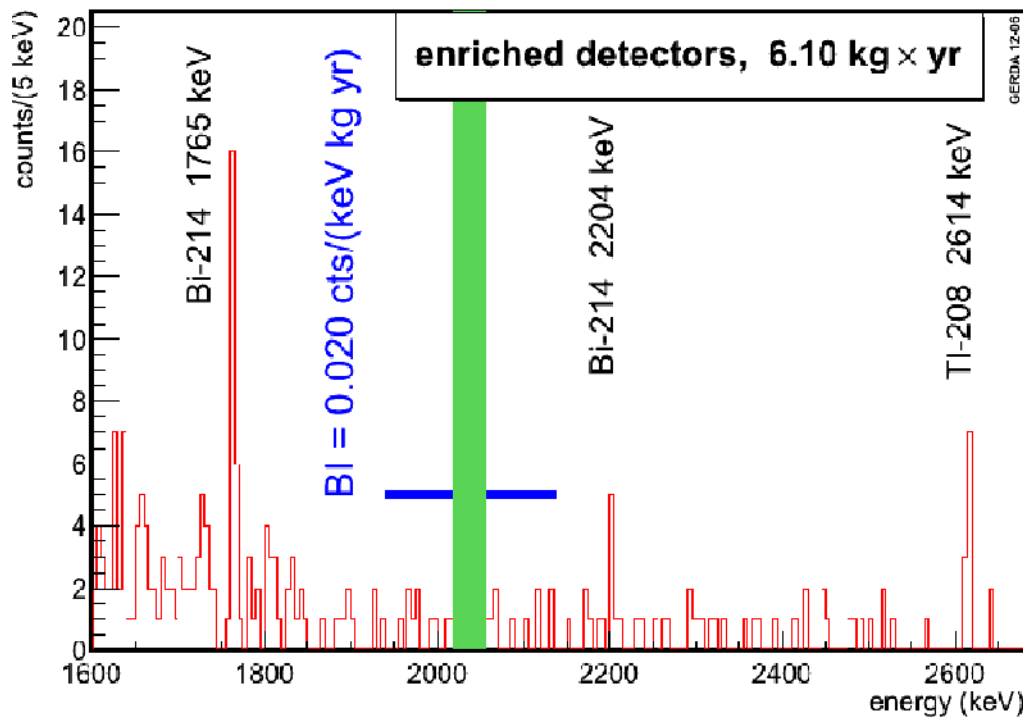
Phase 2: new enriched BEGe detectors (+18 kg)
expect start installing 1st BEGes in 2012

Opt. phase: many detectors (with MAJORANA, 500 kg)



The GERDA experiment

The GERDA background index (BI)



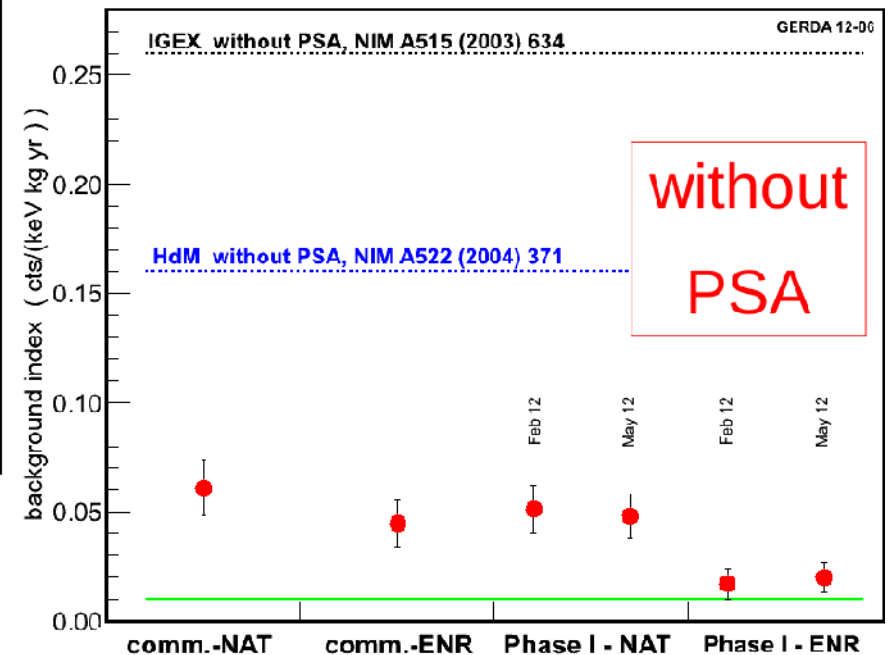
window: $200 - 40 = 160$ keV

$$BI = 0.020 +0.006 -0.004 \text{ cts/ (keV kg yr)} \quad [68\% \text{ coverage}]$$

duty factor: usually 95% ;

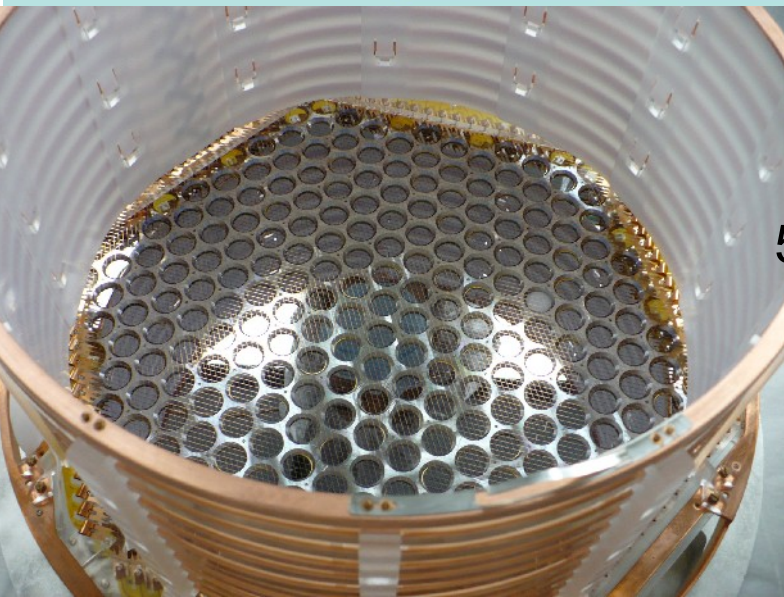
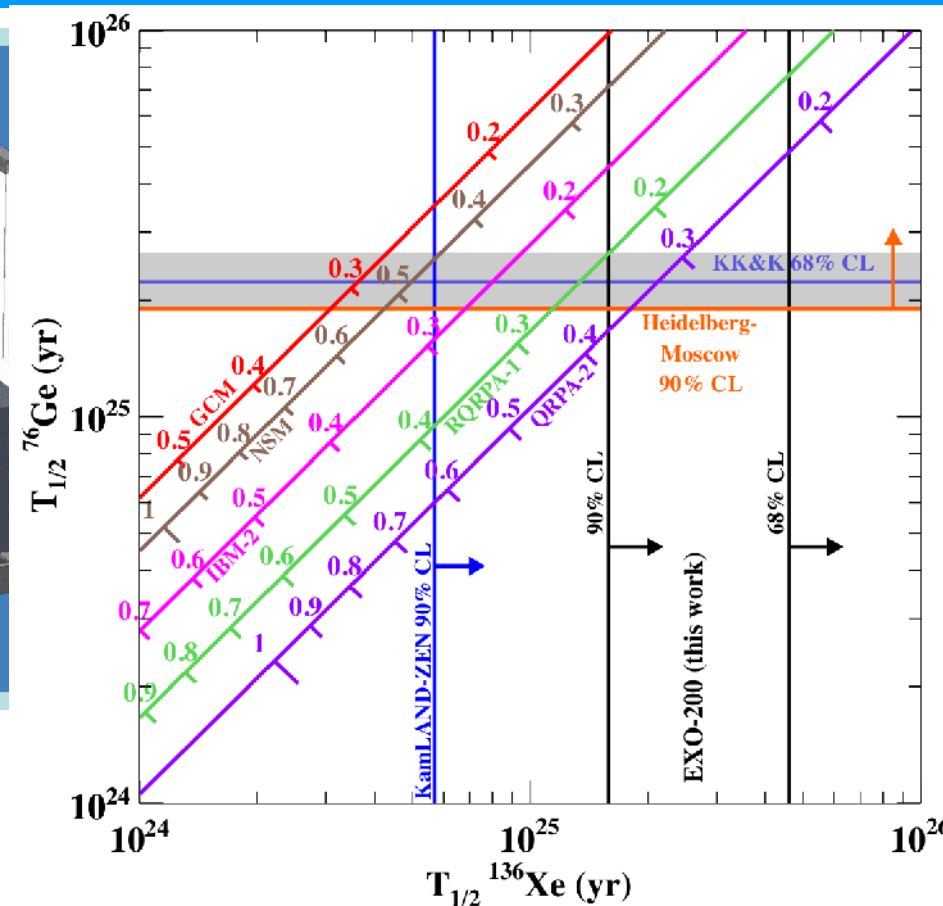
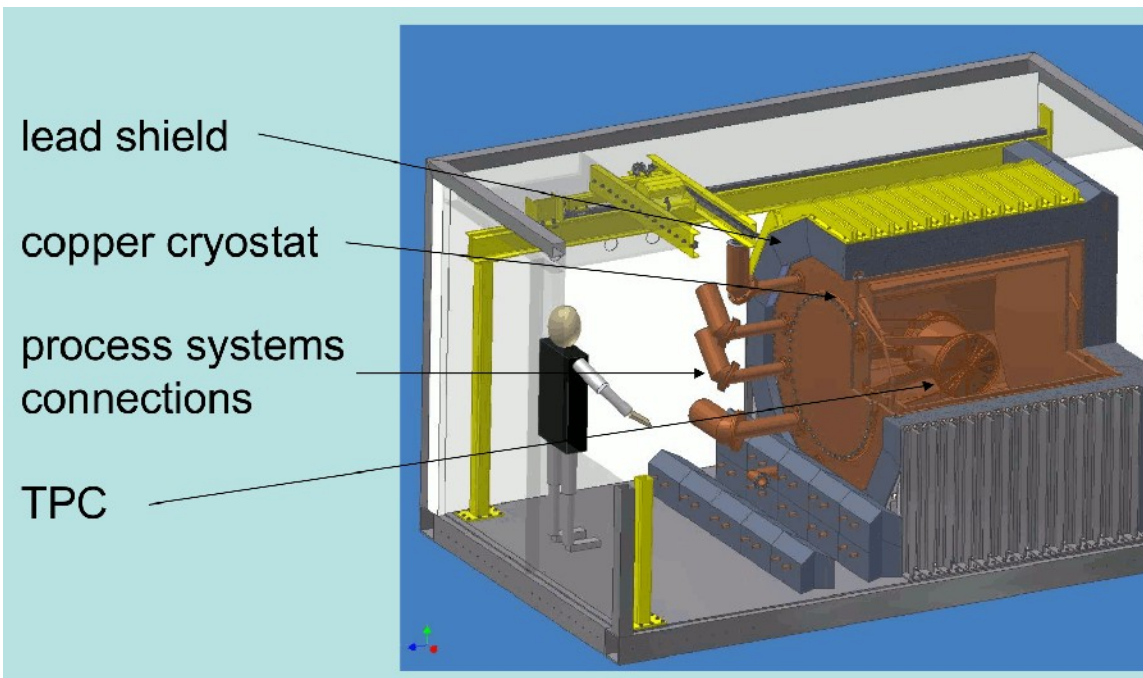
one run not used for physics analysis because of temperature instabilities (overall duty cycle 80%)

from P. Grabmayr's talk at Neutrino 2012



Running since 2011: EXO 200

200 kg enriched ^{136}Xe at WIPP/New Mexico



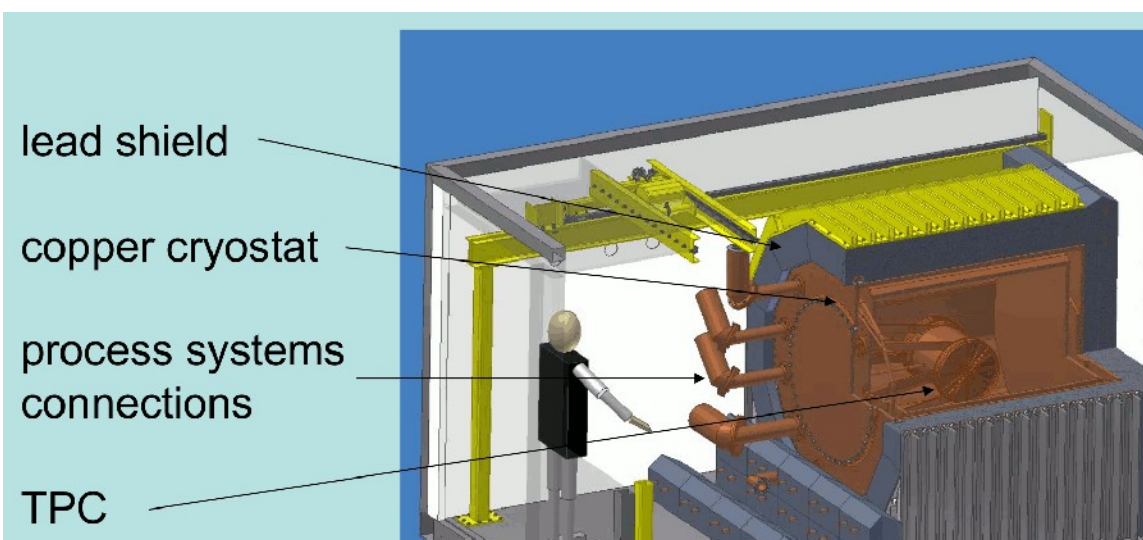
5 events observed, 7.5 background events expected

$T_{1/2}^{0\nu\beta\beta} > 1.6 \cdot 10^{25} \text{ yr}$
 $\langle m_{\beta\beta} \rangle < 140\text{--}380 \text{ meV}$
(90% C.L.)

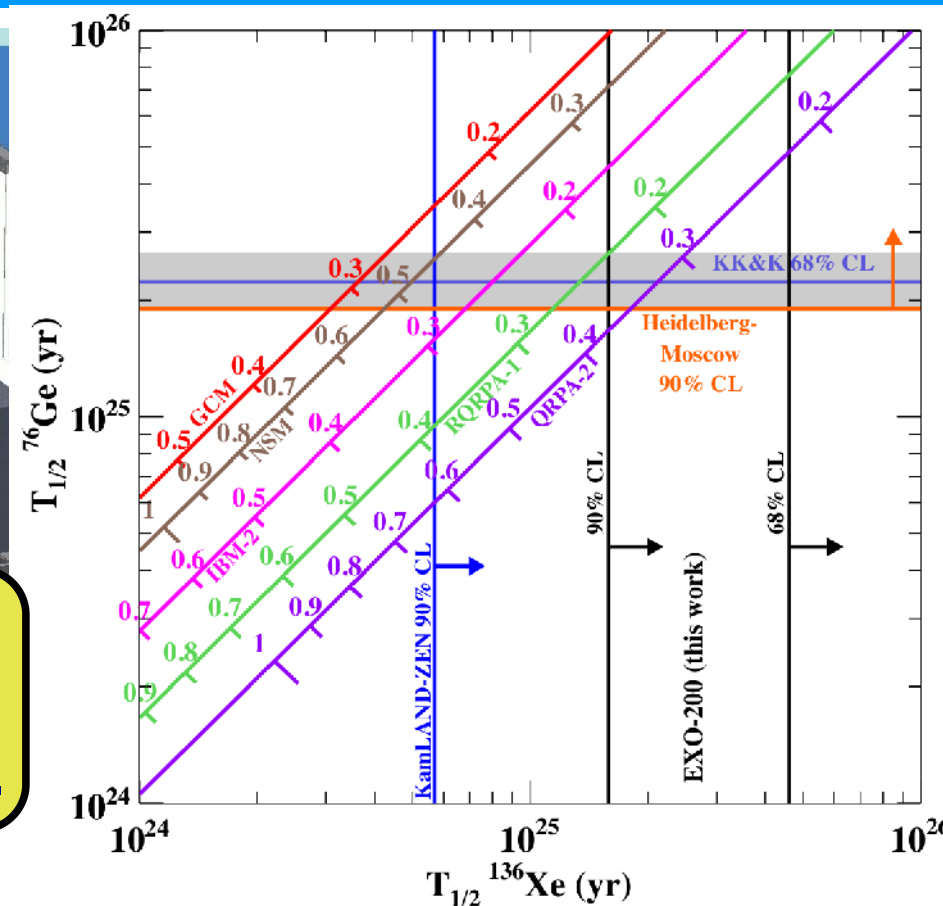
arXiv:1205.5608 – Subm. to PRL

Running since 2011: EXO 200

200 kg enriched ^{136}Xe at WIPP/New Mexico



running: KamLAND-Zen
building: SNO+
prototyping: Majorana, Cobra, ..



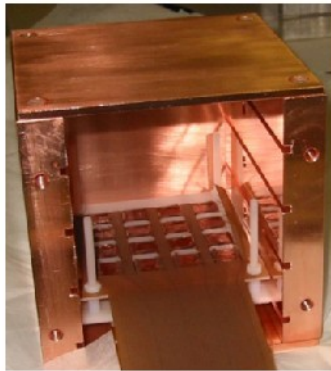
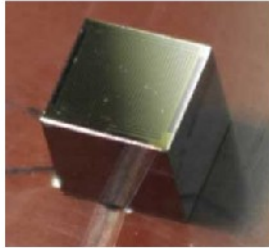
5 events observed, 7.5 background events expected

$T_{1/2}^{0\nu\beta\beta} > 1.6 \cdot 10^{25} \text{ yr}$
 $\langle m_{\beta\beta} \rangle < 140\text{--}380 \text{ meV}$
(90% C.L.)

arXiv:1205.5608 – Subm. to PRL

R&D study: COBRA

CnZnTe detectors at room temperature



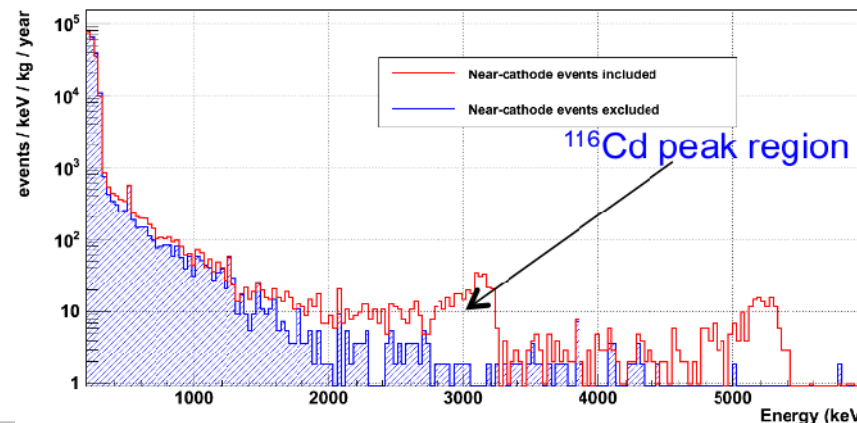
- Source = detector
- Focus on ^{116}Cd
- Semiconductor (Good energy resolution, clean)
- Room temperature
- Modular design (Coincidences)
- Tracking/Pixelisation („Solid state TPC“)

K. Zuber, Phys. Lett. B 519,1 (2001)

Current spectrum (black), **12.73 kg*days**

Background at 2813 keV about 1 ct/keV/kg/yr

PSA very successful



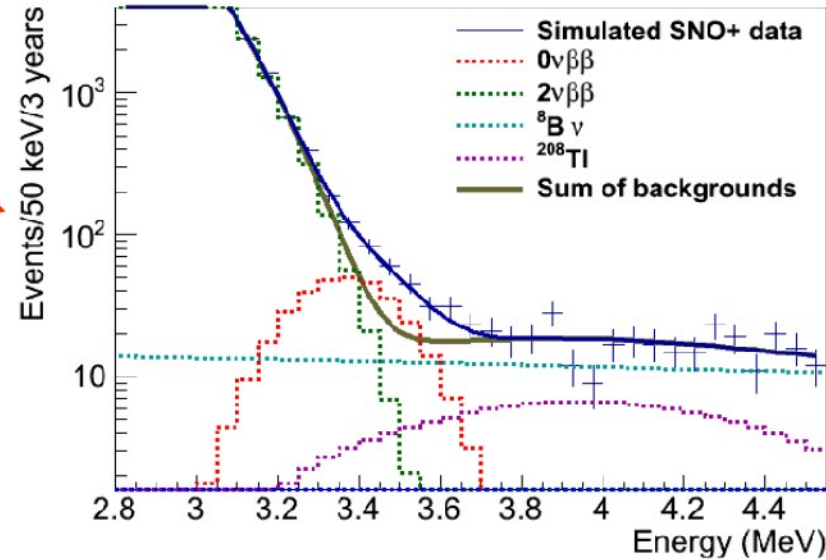


hold-down net installed

^{nat}Nd salt dissolved in liquid scintillator

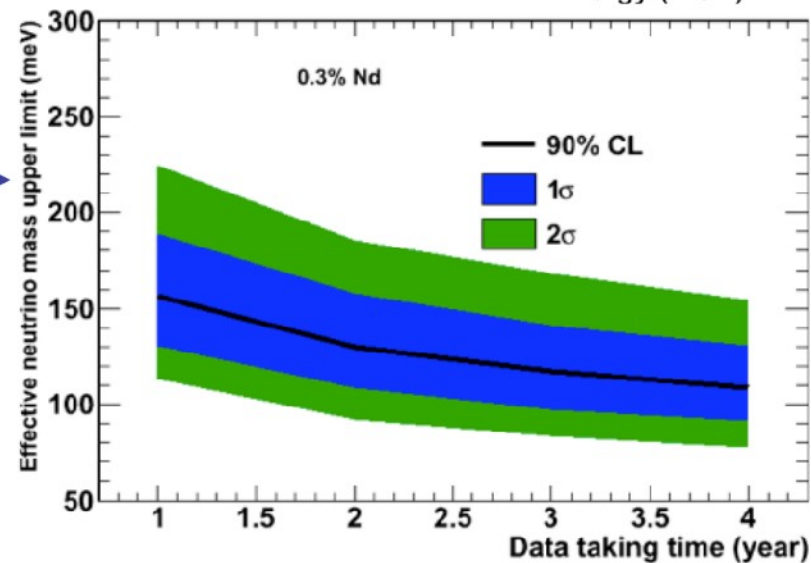
$\beta\beta$ -decay signal for 0.3% Nd-loaded scintillator

- signal at the level of Klapdor [Phys. Lett. B 586 (2004) 198]
- 2.4 live-years data simulated
- ^{214}Bi tagged and removed with $^{214}\text{Bi-Po}$
- ^{208}Tl constrained with $^{212}\text{Bi-Po}$ delayed coincidence
- $t_{1/2}$ 3 min alpha tag of ^{208}Tl rejects 90%



Neutrino mass sensitivity for 0.3% Nd loading (44 kg of ^{150}Nd)

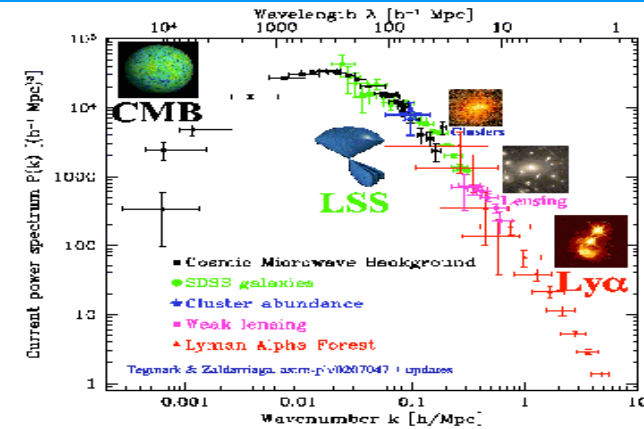
- IBM-2 [Phys. Rev. C 79 (2009) 044301] NME values were used (includes deformation)
- radioactivity backgrounds at the levels achieved by Borexino



Three complementary ways to the absolute neutrino mass scale

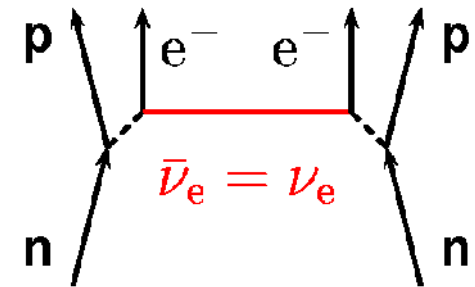
1) Cosmology

very sensitive, but model dependent
compares power at different scales
current sensitivity: $\Sigma m(\nu_i) \approx 0.4 - 1 \text{ eV}$



2) Search for $0\nu\beta\beta$

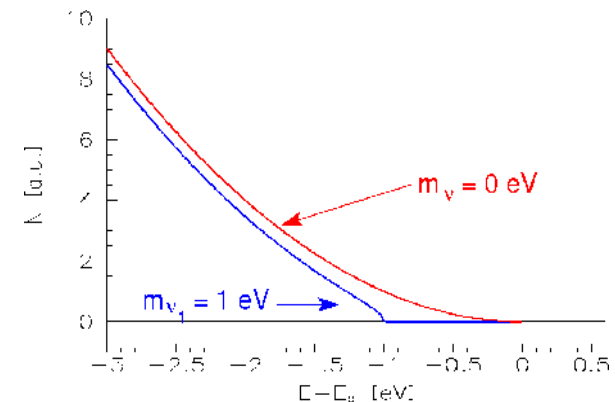
Sensitive to Majorana neutrinos
Evidence for $m_{ee}(\nu) \approx 0.4 \text{ eV}$ (Klapdor-Kleingrothaus et al.)?



3) Direct neutrino mass determination:

No further assumptions needed, use $E^2 = p^2c^2 + m^2c^4 \Rightarrow m^2(\nu)$ is observable mostly

- **Time-of-flight measurements** (ν from supernova)
SN1987a (large Magellan cloud) $\Rightarrow m(\nu_e) < 5.7 \text{ eV}$
- **Kinematics of weak decays**
measure charged decay prod., E-, p-conservation
 β -decay searches for $m(\nu_e)$ - tritium β spectrometers
- ^{187}Re bolometers

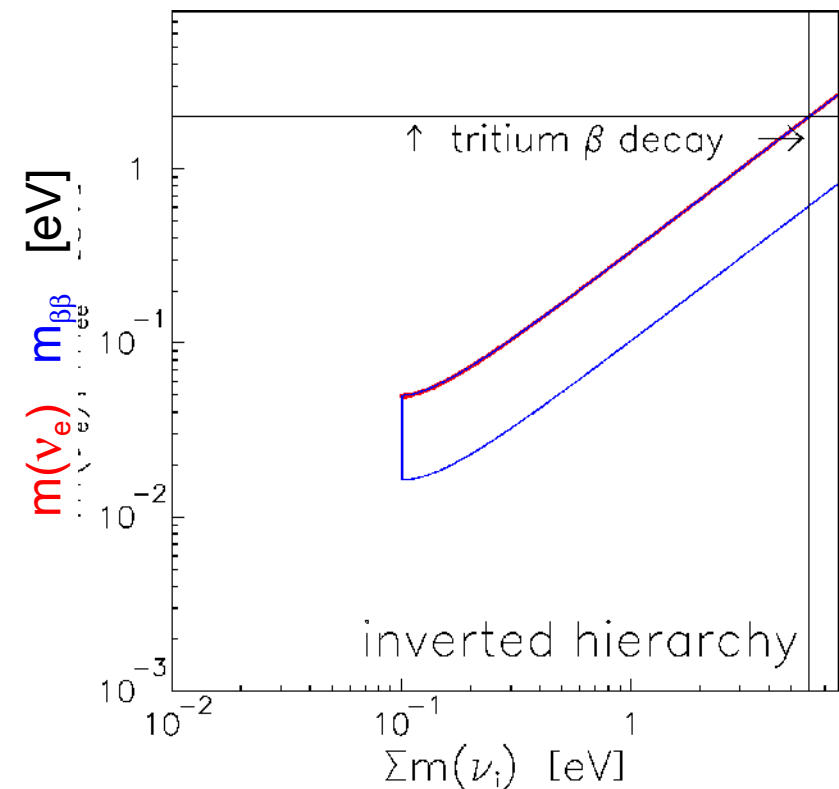
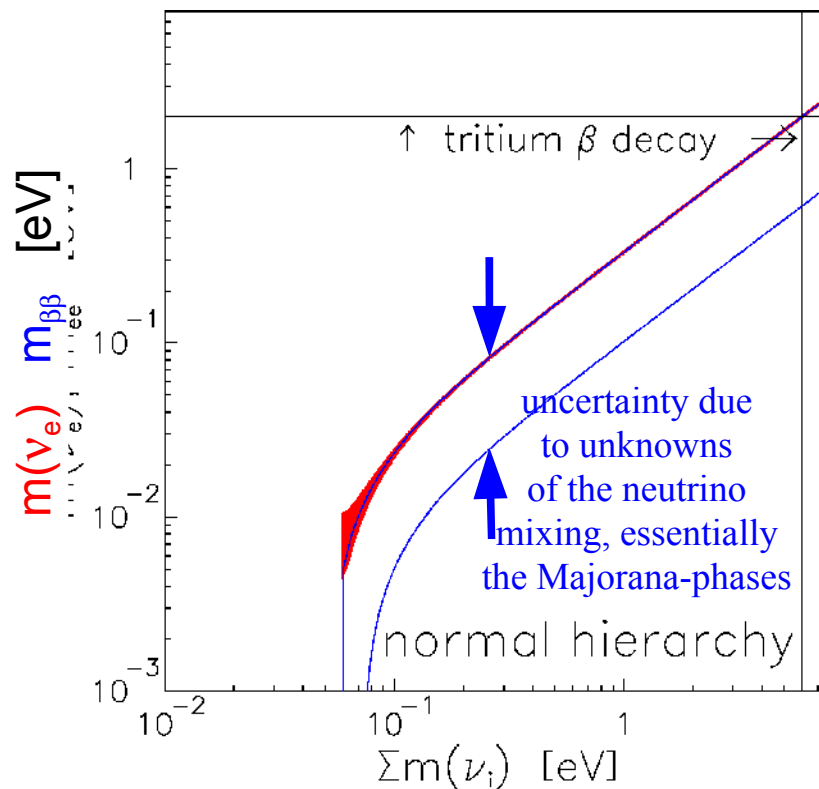


Comparison of the different approaches to the neutrino mass

Direct kinematic measurement: $m^2(\nu_e) = \sum |U_{ei}|^2 m^2(\nu_i)$ (incoherent)

Neutrinoless double β decay: $m_{\beta\beta}(\nu) = |\sum |U_{ei}|^2 e^{i\alpha(i)} m(\nu_i)|$ (coherent)

if no other particle is exchanged (e.g. R-violating SUSY)
problems with uncertainty of nuclear matrix elements



\Rightarrow absolute scale/cosmological relevant neutrino mass in the lab by single β decay

Neutrino mass from supernovae (time-of-flight)

Only one SN detected in ν 's: SN1987a

Simple dependence for sharp ν emission
in time:

$$\Delta t = \frac{L}{c} - \frac{L}{\beta_\nu} = L - \frac{L}{1 - \frac{m_\nu^2}{2E_\nu^2}}$$

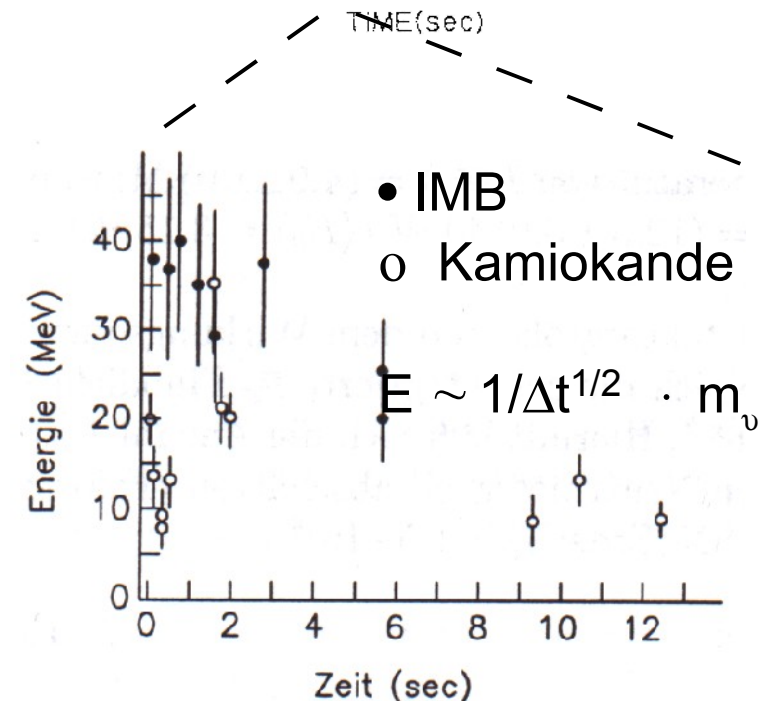
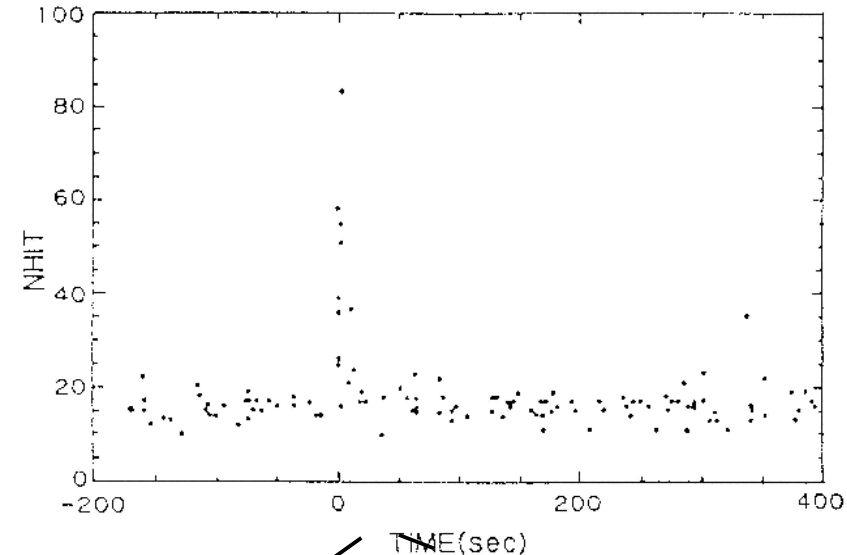
$$\approx L - L \cdot \left(1 + \frac{m_\nu^2}{2E_\nu^2}\right) = -L \cdot \frac{m_\nu^2}{2E_\nu^2}$$

with:

$$m^2 = E^2 - p^2 = E^2(1 - \beta^2)$$

$$= E^2(1 + \beta)(1 - \beta) \approx 2E^2(1 - \beta)$$

$$\Rightarrow \beta = 1 - \frac{m^2}{2E^2}$$



Neutrino mass from supernovae (time-of-flight)

Only one SN detected in ν 's: SN1987a

No energy versus time dependence visible

→ only upper limit on neutrino mass

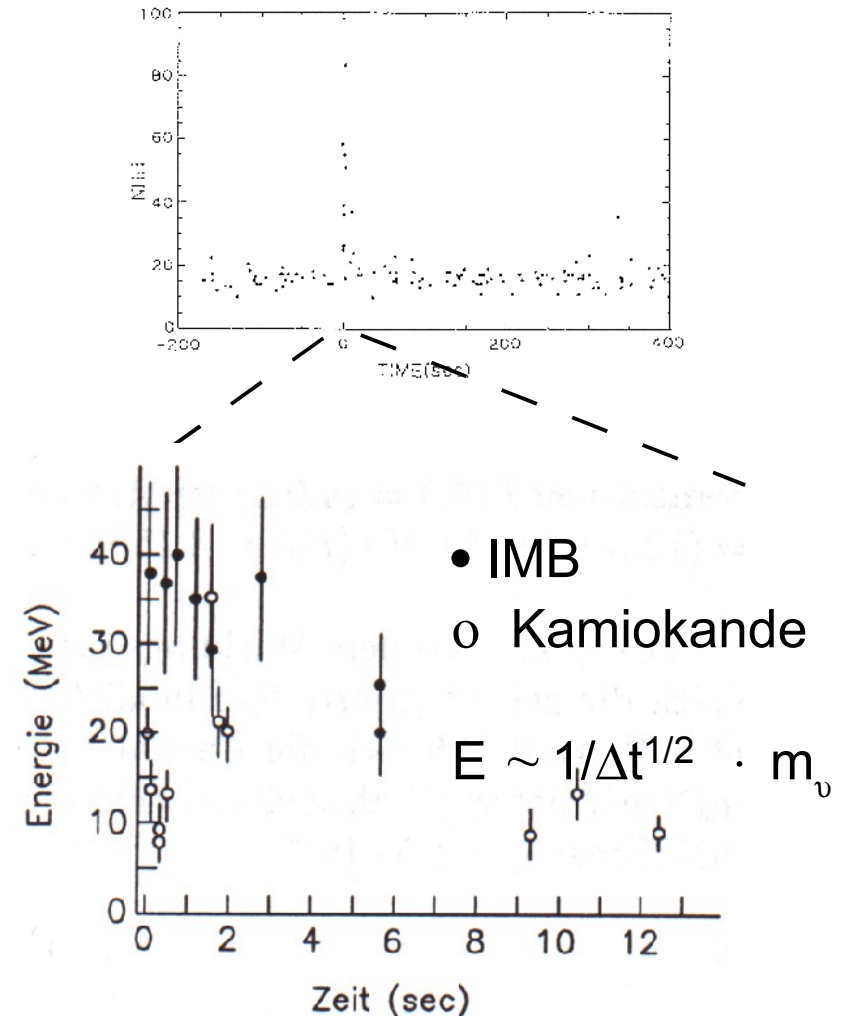
Results depends on underlying SN model, e.g.:

$m(\nu_e) < 5.7 \text{ eV}$

T.J. Loredo et al., PRD65 (2002) 063002

$m(\nu_e) < 5.8 \text{ eV}$

G. Pagliarola, F. Rossi-Torres and F. Vissani,
Astropart. Phys. 33 (2010) 287

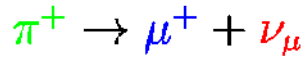


BUT

- galactic SN only about every 40 years

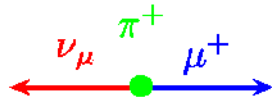
- not sensitive below 1eV (uncertainty of neutrino emission time spectrum)

Determination of „ $m(\nu_\mu)$ “ what does $m(\nu_\mu)$ mean ?



(Two body decay)

Decay at rest:



$$|\vec{p}_\nu| = |\vec{p}_\mu|$$

$$m_\pi = E_\nu + E_\mu$$

$$\rightarrow m_\nu^2 = m_\pi^2 + m_\mu^2 - 2 \cdot m_\pi \cdot \sqrt{m_\mu^2 + p_\mu^2}$$

3 different Experiments:

Values from PDG2000

Pionic atoms:

$$m_\pi = 139.570180(350) \text{ MeV}$$

Myonium:

$$m_\mu = 105.658357(5) \text{ MeV}$$

Magnetic spektrometer (PSI):

$$p_\mu = 29.791998(110) \text{ MeV}$$

$$\rightarrow m(\nu_\mu) < 170 \text{ keV}/c^2 \quad (95\% \text{ c.l.}) \quad (\text{K. Assamagan et al.,}$$

Phys. Rev. D53 (1996) 6065)

$$\text{PDG2000: } m(\nu_\mu) < 190 \text{ keV}/c^2 \quad (95\% \text{ c.l.})$$

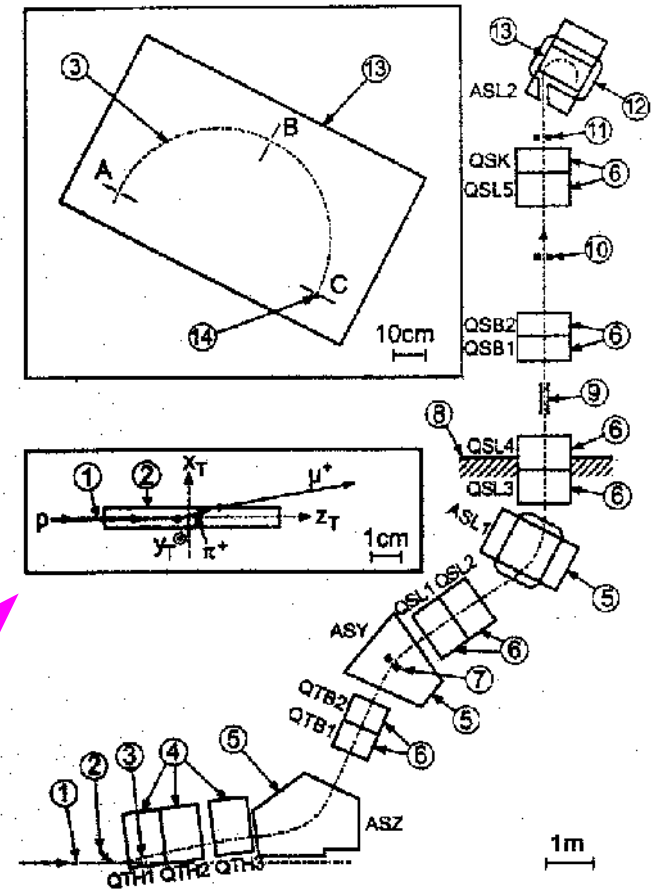
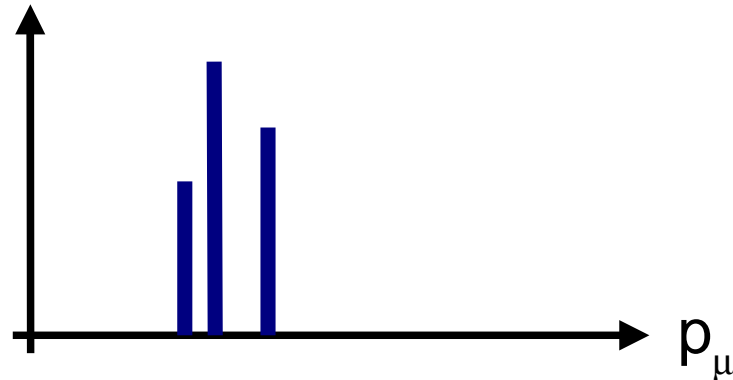


FIG. 1. Experimental setup. (1) Central trajectory of 590 MeV proton beam; (2) graphite target; (3) central trajectory of muon beam; (4) half-quadrupole magnets; (5) dipole magnets; (6) quadrupole magnets; (7) collimator defining the beam momentum acceptance; (8) concrete shielding of proton channel; (9) crossed-field particle separator; (10) lead collimator; (11) normally open movable collimator system (normally open); (12) magnetic spectrometer; (13) pole of spectrometer; (14) muon detectors (silicon microstrip and single surface-barrier detectors); A, B, C: copper collimators.

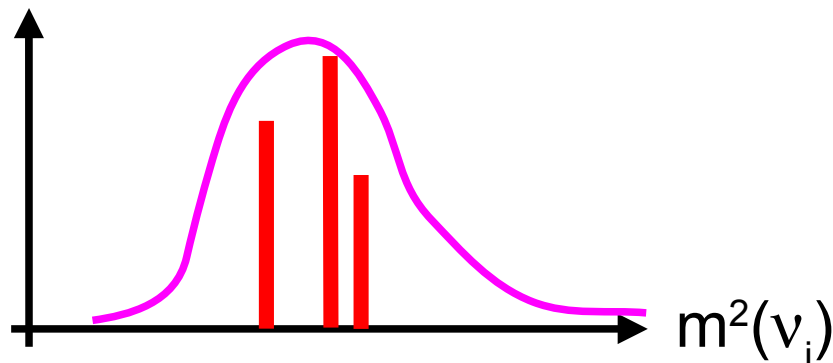
Different neutrino mass states ν_i

⇒ Measure different muon momenta p_μ with probability $|U_{\mu i}|^2$



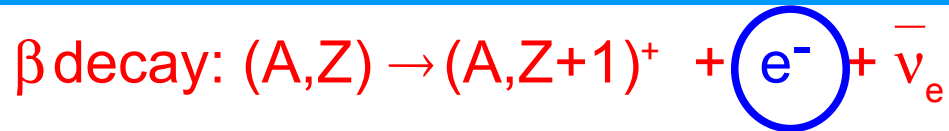
$$m_\nu^2 = m_\mu^2 + m_\pi^2 - 2m_\pi (m_\mu^2 + p_\mu^2)^{1/2}$$

⇒ 3 different neutrino masses $m^2(\nu_i)$ with probability $|U_{\mu i}|^2$



if different mass states can experimentally not be resolved:
 ⇒ $m^2(\nu_\mu) := \sum_i \cdot |U_{\mu i}|^2 \cdot m^2(\nu_i)$

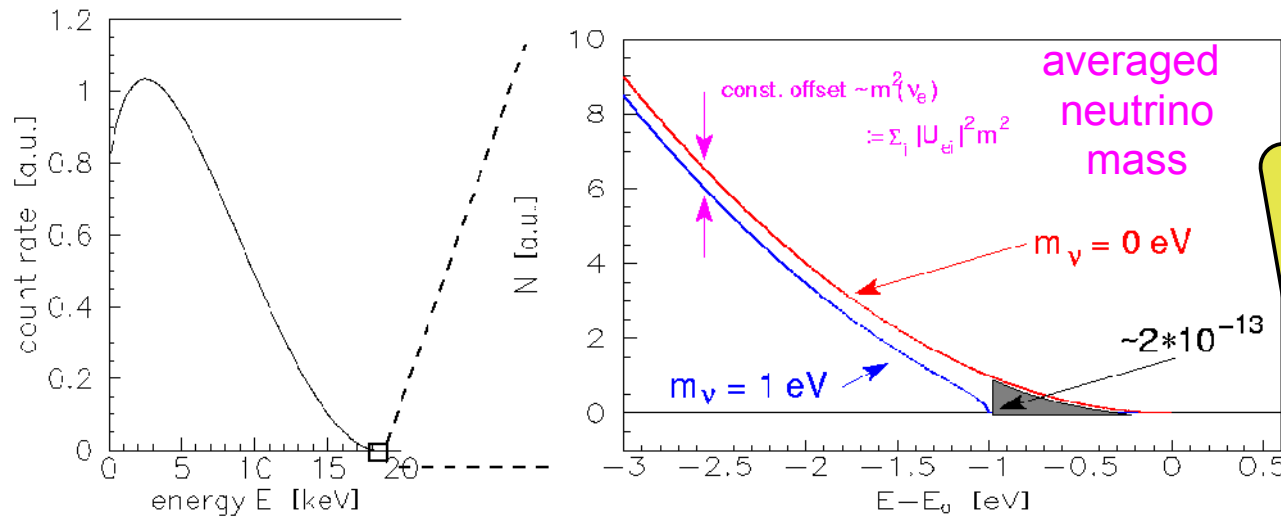
Direct determination of $m(\nu_e)$ from β decay



β electron energy spectrum:

$$dN/dE = K F(E,Z) \rho E_{\text{tot}} (E_0 - E_e) \sum |U_{ei}|^2 \sqrt{(E_0 - E_e)^2 - m(\nu_i)^2}$$

(modified by electronic final states, recoil corrections, radiative corrections)



E.W. Otten & C. Weinheimer
Rep. Prog. Phys.
71 (2008) 086201

Need: low endpoint energy \Rightarrow Tritium ^3H , (^{187}Re)
 very high energy resolution &
 very high luminosity &
 very low background \Rightarrow MAC-E-Filter
 (or bolometer for ^{187}Re)

Summary: β -spectrum incl. electronic final states + ν mixing

Including electronic excited final states of excitation energy V_j with probability W_j

$$W_j = |\langle \Psi_0 | \Psi_{f,j} \rangle|^2$$

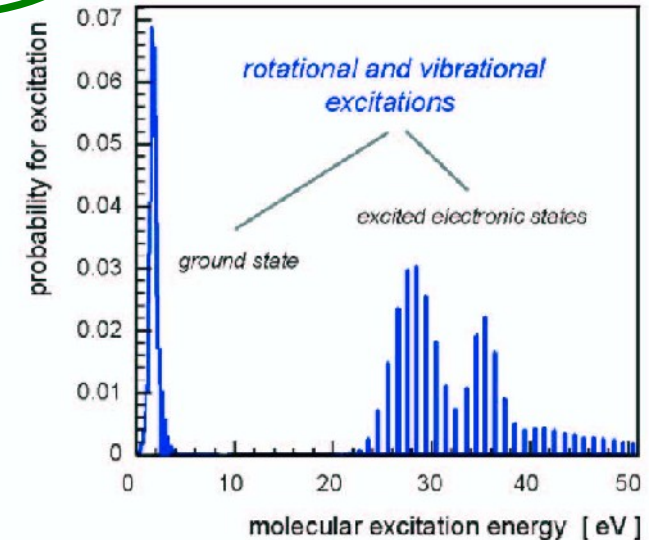
Using $\epsilon_j = E_0 - V_j - E$

$$\frac{d^2 N}{dt dE} = A \cdot F(E, Z + 1) \cdot p \cdot (E + m) \cdot \sum_j W_j \cdot \epsilon_j \cdot \sqrt{\epsilon_j^2 - m^2(\nu_c)} \cdot \Theta(\epsilon_j - m(\nu_c))$$

Final states of T_2 β -decay:

(A. Saenz et al. Phys. Rev. Lett. 84 (2000) 242,
N. Doss et al., Phys. Rev. C73 (2006) 025502)

**⇒ electronic final states
are very important**



**⇒ look at
endpoint region**

Including neutrino mixing

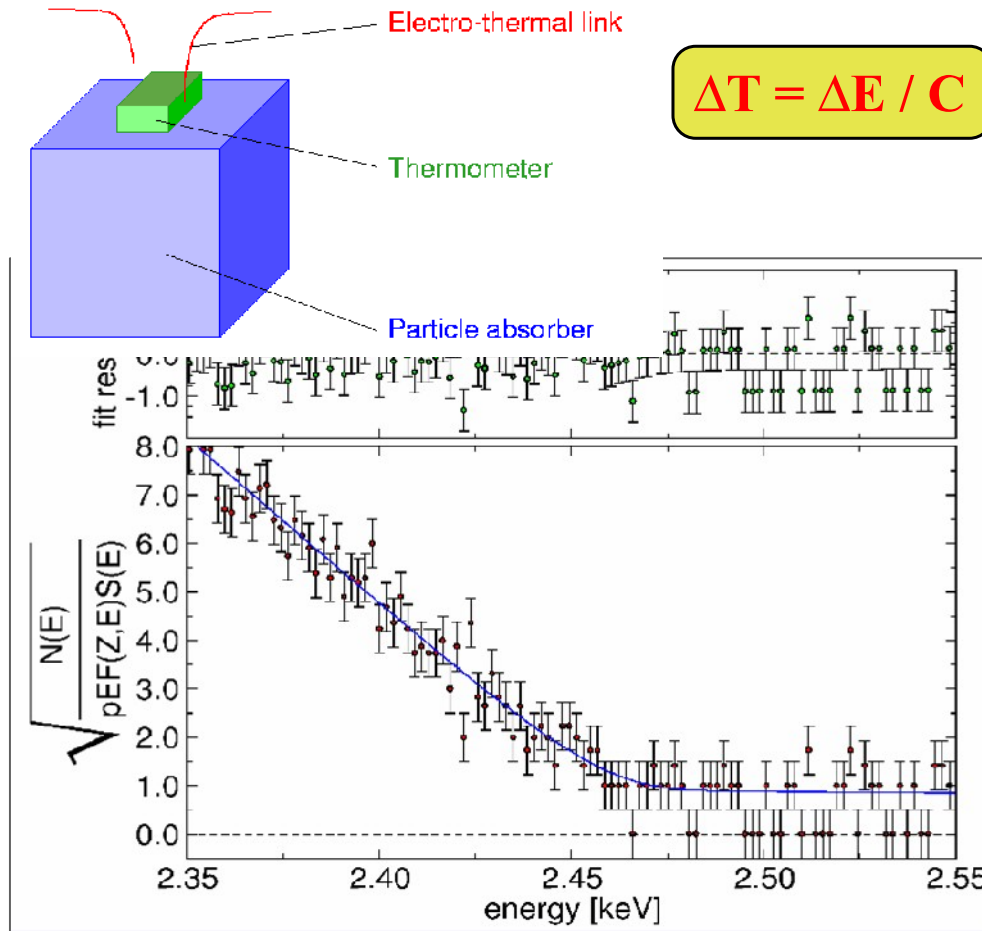
$$\frac{d^2 N}{dt dE} = A \cdot F(E, Z + 1) \cdot p \cdot (E + m) \cdot \sum_j W_j \cdot \epsilon_j \cdot \left(\sum_i |U_{ci}|^2 \sqrt{\epsilon_j^2 - m^2(\nu_i)} \cdot \Theta(\epsilon_j - m(\nu_i)) \right)$$

⇒ "Electron neutrino mass"

$$m^2(\nu_c) := \sum_i |U_{ci}|^2 \cdot m^2(\nu_i)$$

**⇒ the different $m(\nu_i)$
are not important
at present precision**

Cryogenic bolometers with ^{187}Re MIBETA (Milano/Como)



Measures all energy except that of the neutrino

detectors: 10 (AgReO_4)

rate each: 0.13 1/s

energy res.: $\Delta E = 28 \text{ eV}$

pile-up frac.: $1.7 \cdot 10^{-4}$

$$M_\nu^2 = -141 \pm 211_{\text{stat}} \pm 90_{\text{sys}} \text{ eV}^2$$

$$M_\nu < 15.6 \text{ eV (90\% c.l.)}$$

(M. Sisti et al., NIMA520 (2004) 125)

MANU (Genova)

- Re metallic crystal (1.5 mg)
- BEFS observed (F.Gatti et al., Nature 397 (1999) 137)
- sensitivity: $m(\nu) < 26 \text{ eV}$ (F.Gatti, Nucl. Phys. B91 (2001) 293)

MARE neutrino mass project:

^{167}Re beta decay with cryogenic bolometers

Advantages of cryogenic bolometers:

- measures all released energy except that of the neutrino
- no final atomic/molecular states
- no energy losses
- no back-scattering

Challenges of cryogenic bolometers:

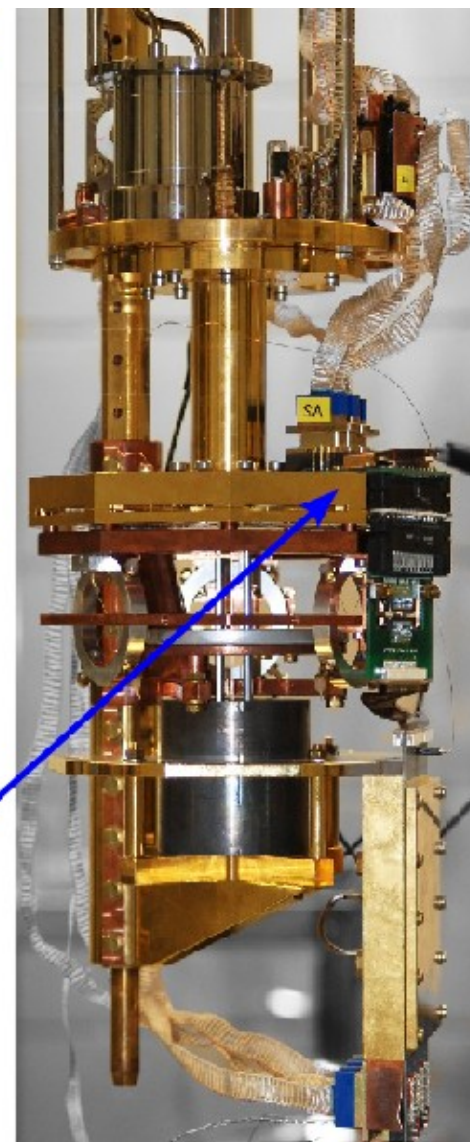
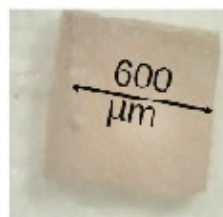
- measures the full spectrum (pile-up)
- need large arrays to get statistics
- understanding spectrum
- still energy losses or trapping possible

MARE-1 @ Milano-Bicocca

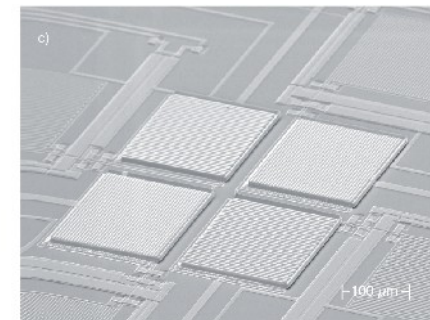
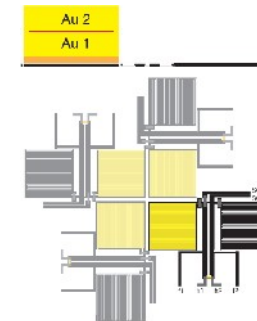
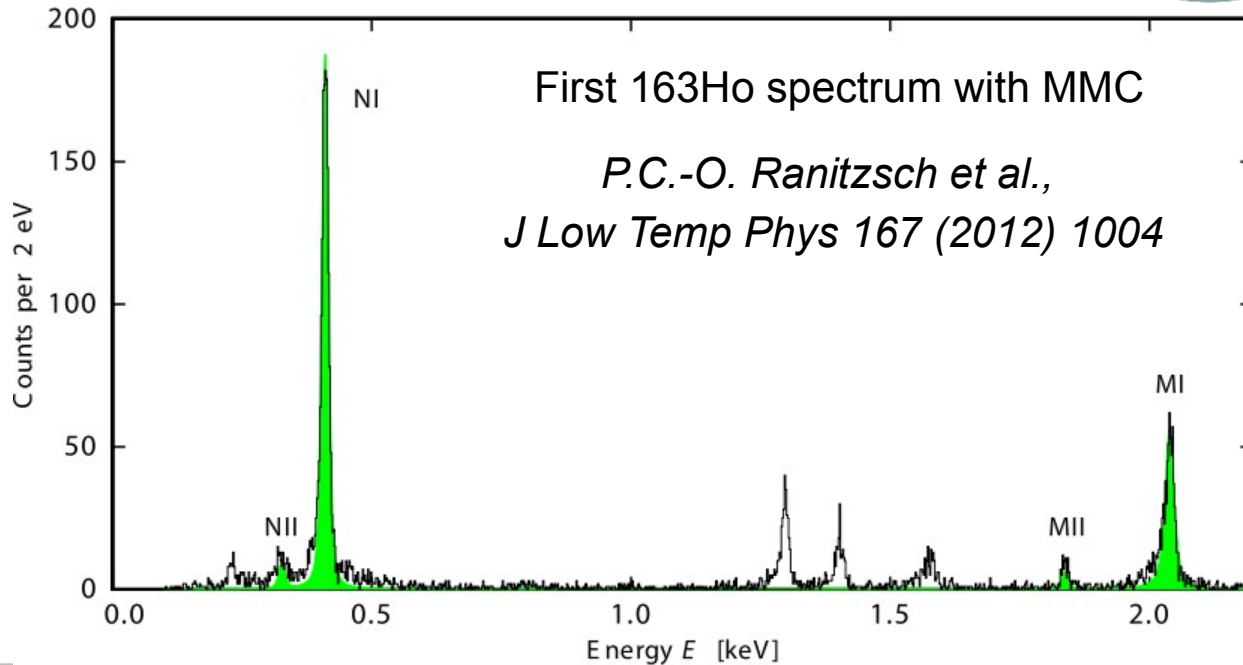
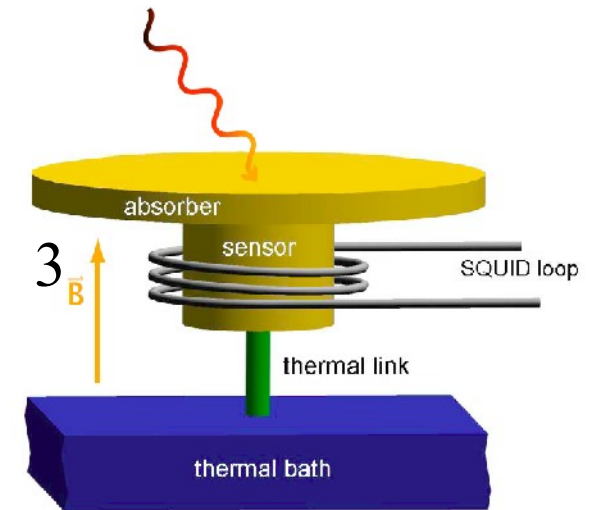
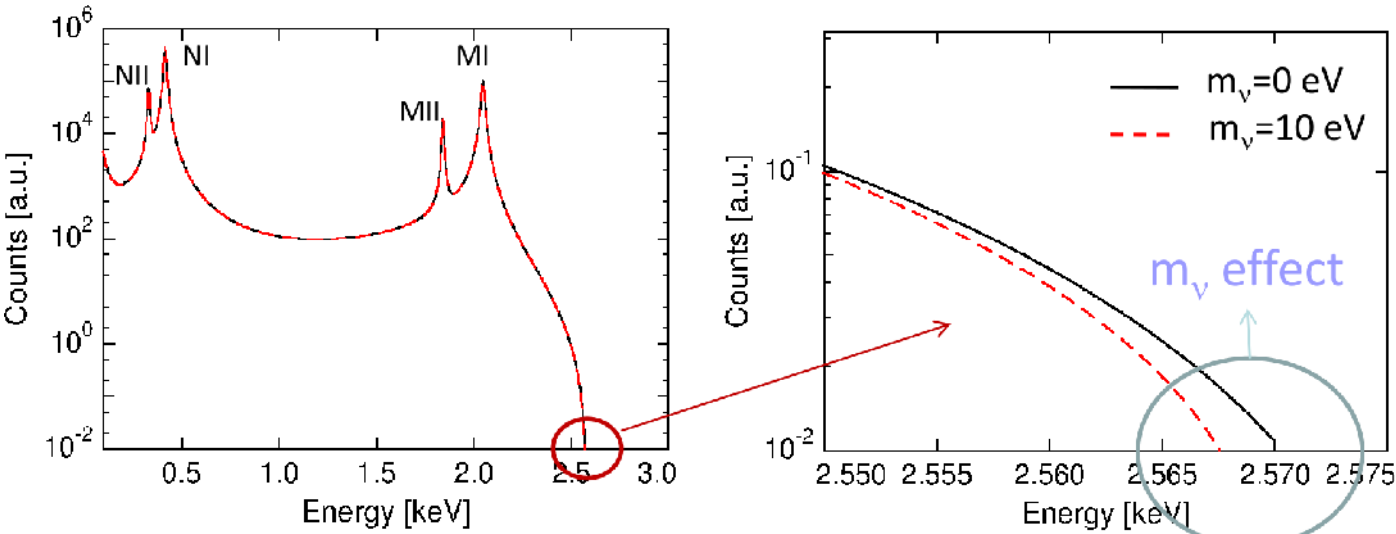
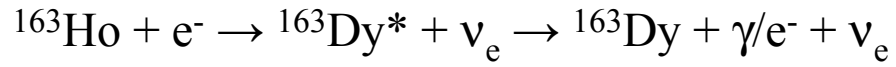
- 6x6 array of Si-implanted thermistors (NASA/GSFC)
- 0.5 mg AgReO_4 crystals
- $\Delta E \approx 30$ eV, $\tau_R \approx 250$ μs
- experimental setup for up to 8 arrays completed
- starting with 72 pixels in 2011
- up to 10^{10} events in 4 years
→ ~ 4 eV sensitivity

MARE-1 @ Genova

- R&D effort for Re single crystals on transition edge sensors (TES)
→ improve rise time to $\sim \mu\text{s}$ and energy resolution to few eV
- large arrays ($\approx 10^3$ pixels) for 10^4 - 10^5 detector experiment
- high bandwidth, multiplexed SQUID readout
- also used with ^{163}Ho loaded absorbers



ECHO neutrino mass project: ^{163}Ho electron capture with metallic magnetic calorimeters

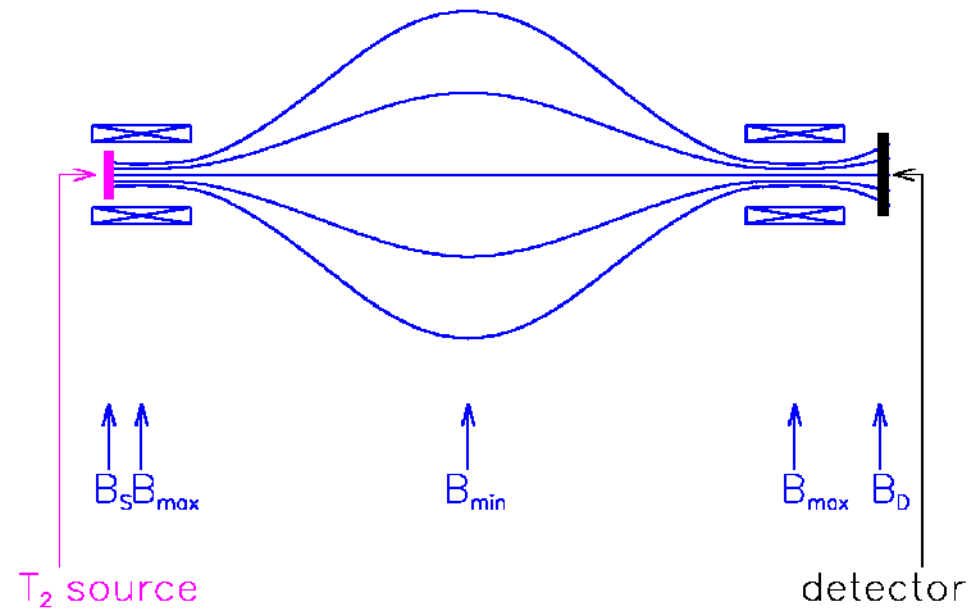


courtesy L. Gastaldo

Principle of the MAC-E-Filter

Magnetic Adiabatic Collimation + Electrostatic Filter
(A. Picard et al., Nucl. Instr. Meth. 63 (1992) 345)

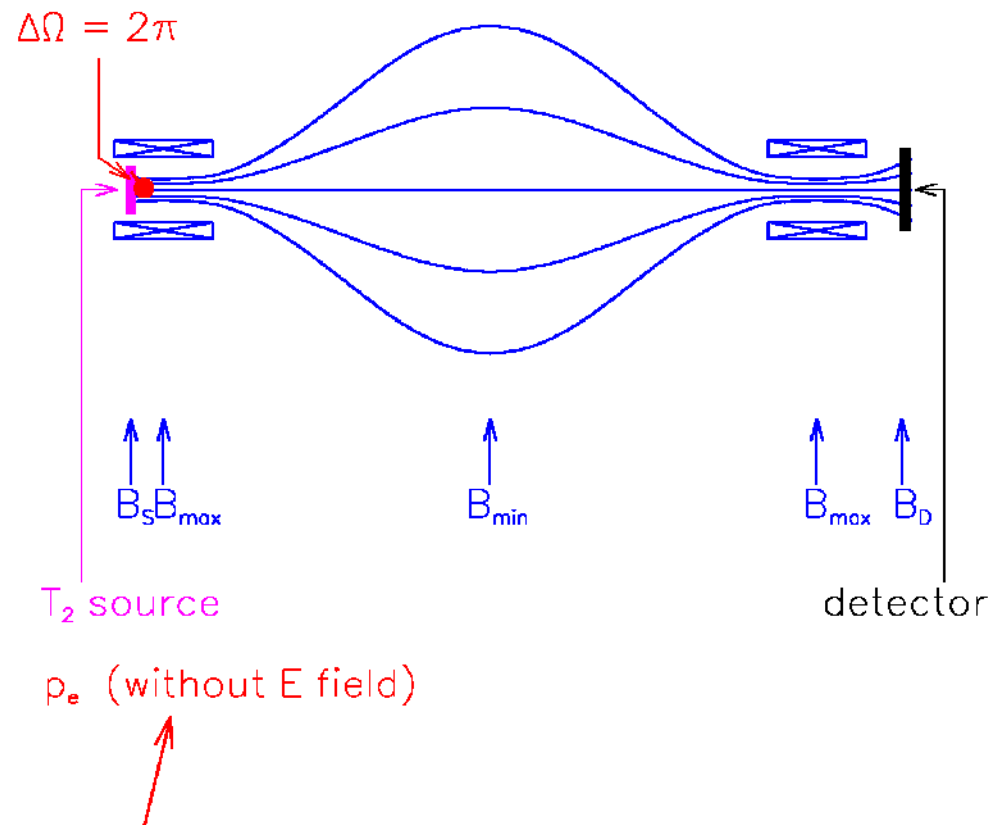
- Two supercond. solenoids compose magnetic guiding field
- Electron source (T_2) in left solenoid



Principle of the MAC-E-Filter

Magnetic Adiabatic Collimation + Electrostatic Filter
 (A. Picard et al., Nucl. Instr. Meth. 63 (1992) 345)

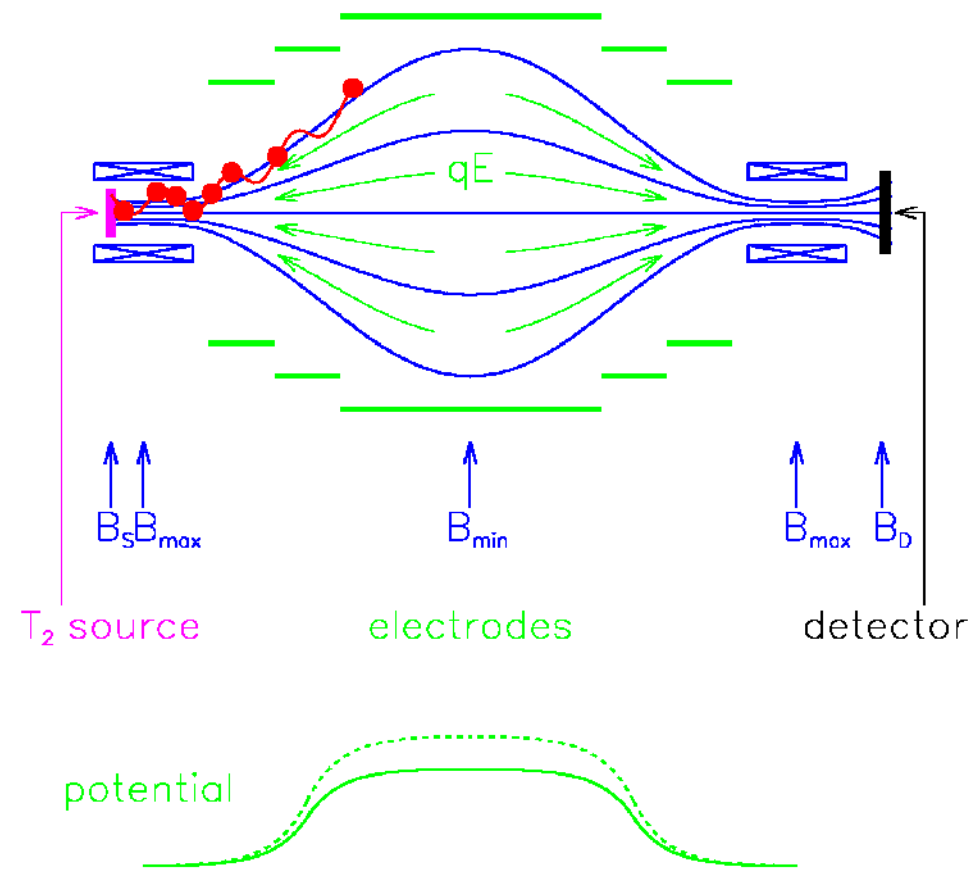
- Two supercond. solenoids compose magnetic guiding field
- Electron source (T_2) in left solenoid
- e^- in forward direction: magnetically guided
- adiabatic transformation: $\mu = E/B = \text{const.}$
 \Rightarrow parallel e^- beam



Principle of the MAC-E-Filter

Magnetic Adiabatic Collimation + Electrostatic Filter
(A. Picard et al., Nucl. Instr. Meth. 63 (1992) 345)

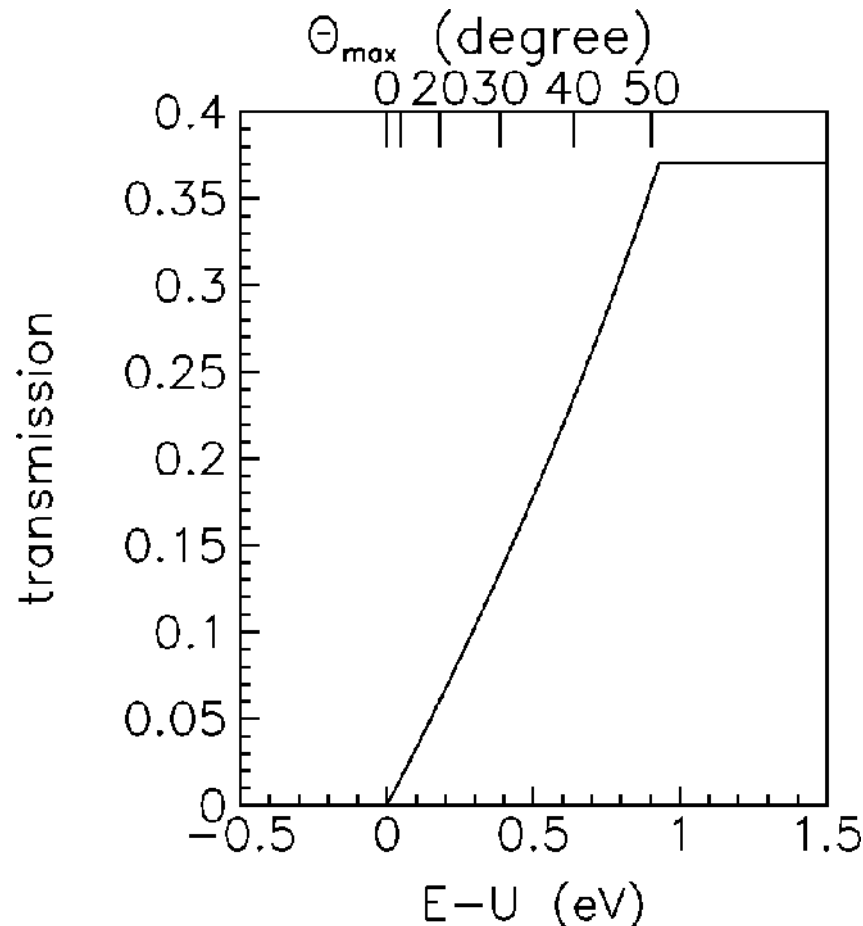
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 \Rightarrow parallel e^- beam
- Energy analysis by electrostat. retarding field
 $\Delta E = EB_{\min}/B_{\max} = EA_{s,\text{eff}}/A_{\text{analyse}} \approx 4.8 \text{ eV (Mainz)} = 0.93 \text{ eV (KATRIN)}$



Principle of the MAC-E-Filter

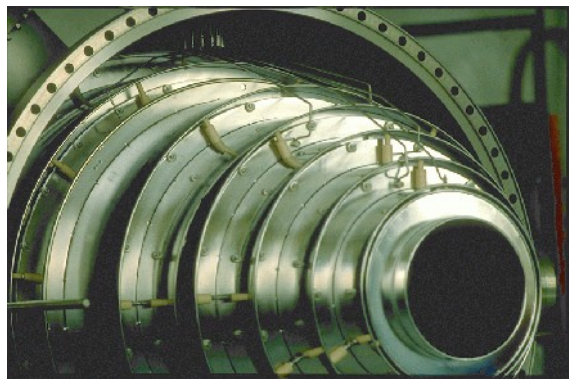
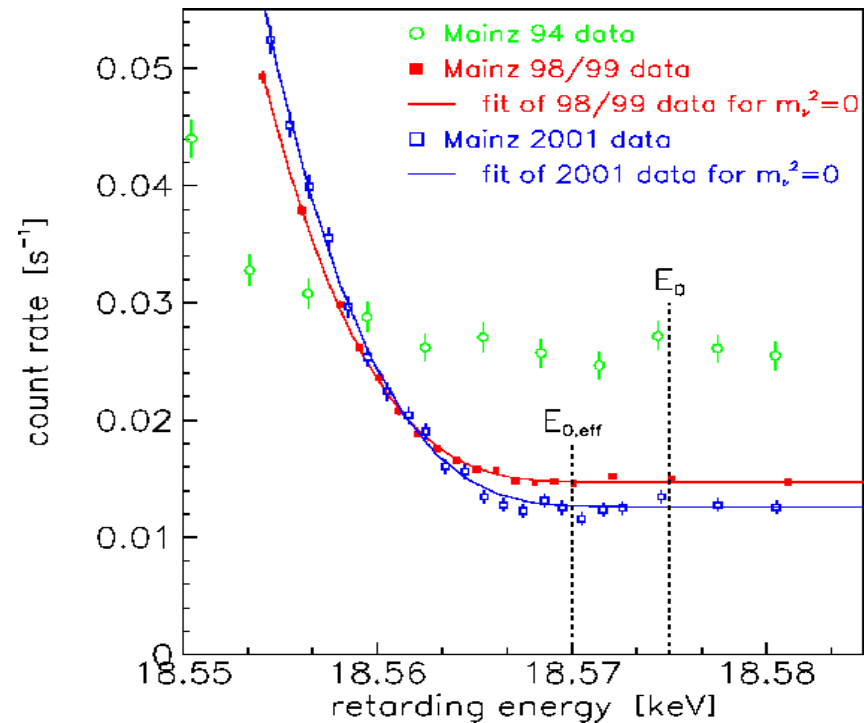
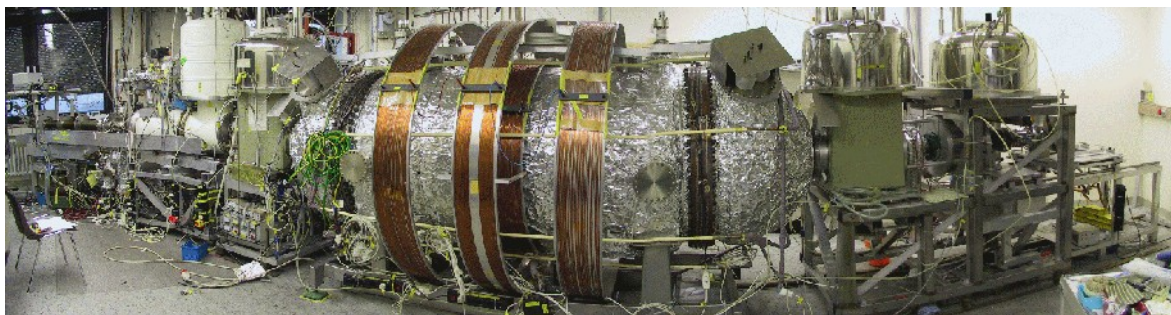
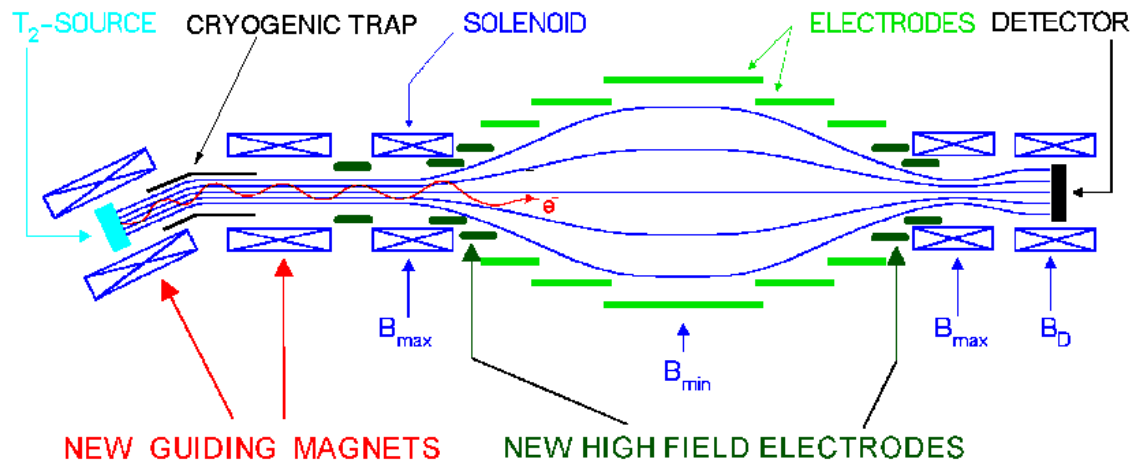
Magnetic Adiabatic Collimation + Electrostatic Filter
(A. Picard et al., Nucl. Instr. Meth. 63 (1992) 345)

⇒ sharp integrating transmission function without tails:



$$\Delta E = E B_{\min} / B_{\max} = E A_{s,\text{eff}} / A_{\text{analyse}} \approx 4.8 \text{ eV (Mainz)} = 0.93 \text{ eV (KATRIN)}$$

The Mainz Neutrino Mass Experiment Phase 2: 1997-2001

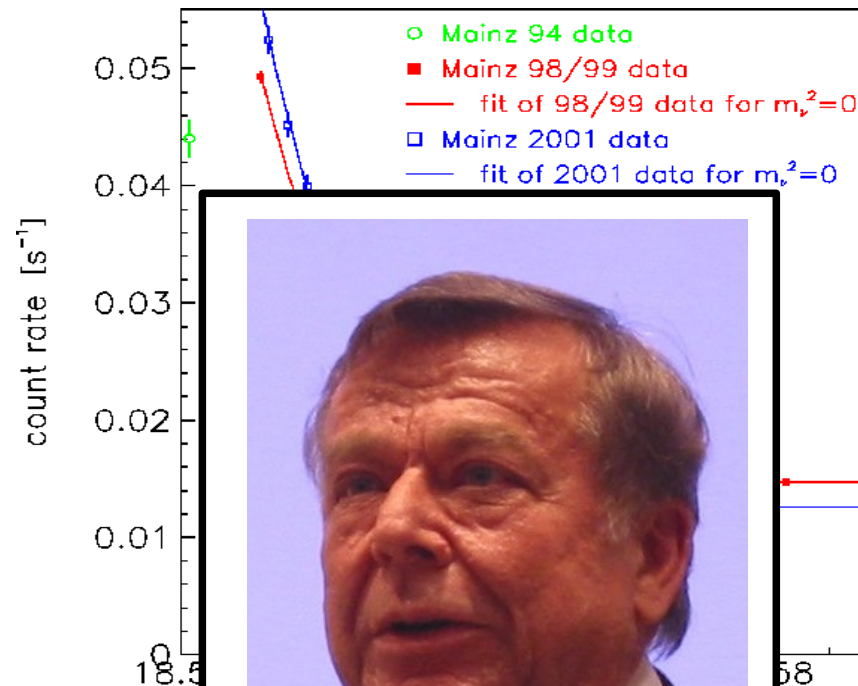
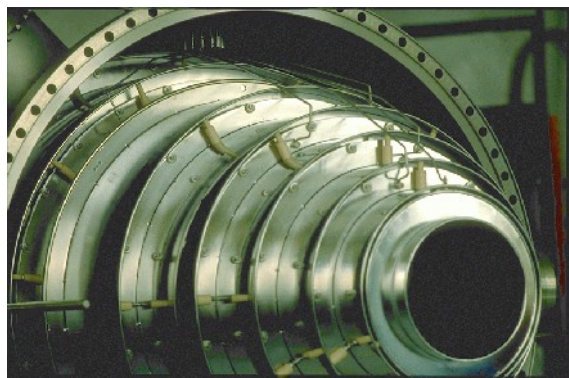
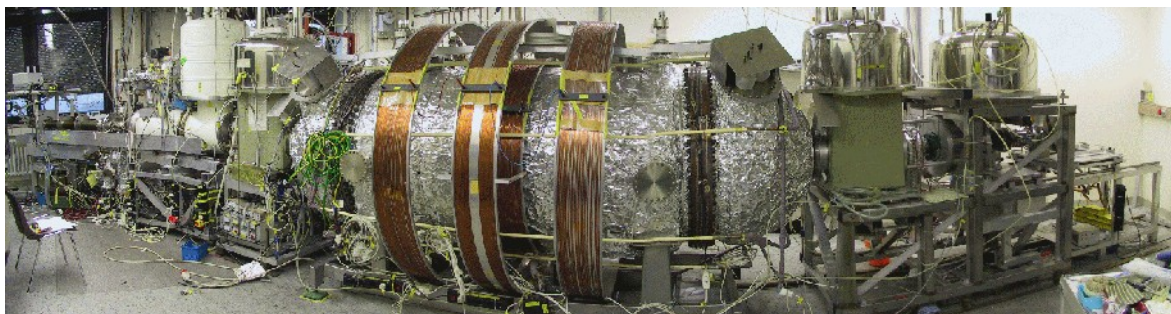
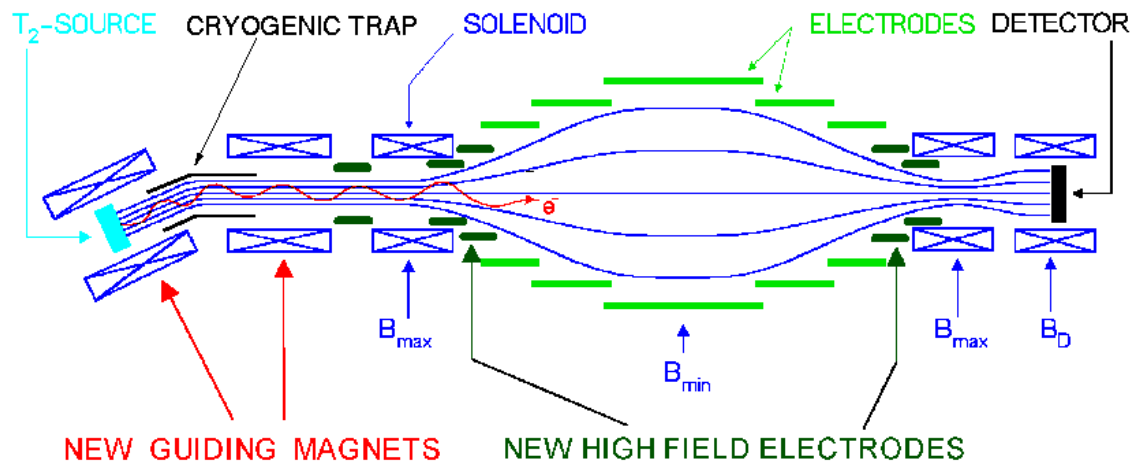


After all critical systematics measured by own experiment
(atomic physics, surface and solid state physics:
inelastic scattering, self-charging, neighbour excitation):

$$m^2(\nu) = -0.6 \pm 2.2 \pm 2.1 \text{ eV}^2 \Rightarrow m(\nu) < 2.3 \text{ eV (95\% C.L.)}$$

C. Kraus et al., Eur. Phys. J. C 40 (2005) 447

The Mainz Neutrino Mass Experiment Phase 2: 1997-2001



Dr. Jochen Bonn

* 7.4.44

+ 27.8.12

After all critical systematics measu
(atomic physics, surface and solid
inelastic scattering, self-chargi

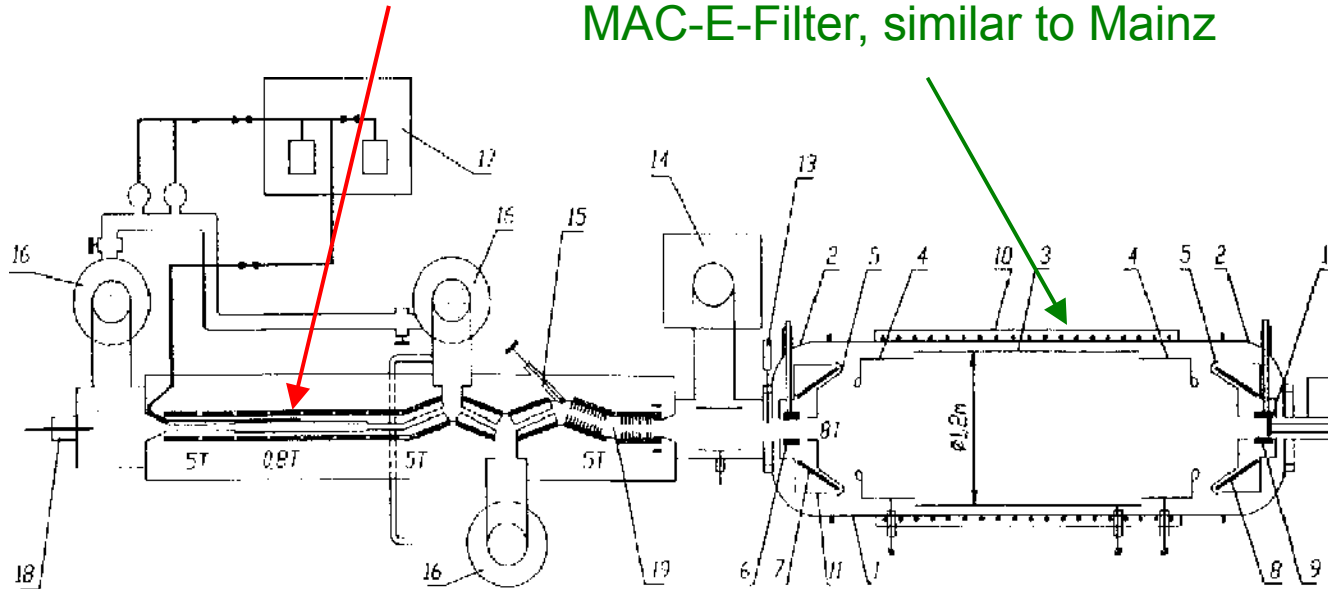
$$m^2(\nu) = -0.6 \pm 2.2 \pm 2.1 \text{ eV}^2 \Rightarrow$$

C. Kraus et al., Eur. Phys. J. C 40 (2005) 447

The Troitsk Neutrino Mass Experiment

windowless gaseous T_2 source, similar to LANL

MAC-E-Filter, similar to Mainz



Luminosity: $L = 0.6 \text{ cm}^2$
($L = \Delta\Omega/2\pi * A_{\text{source}}$)

Energy resolution: $\Delta E = 3.5 \text{ eV}$
3 electrode system in 1.5m
diameter UHV vessel ($p < 10^{-9}$ mbar)



Vladimir
Mikhailovich
Lobashev
1934-2011



Re-analysis of Troitsk data
(better source thickness, better run selection)
Aseev et al, Phys. Rev. D 84, 112003 (2011)
 $m_\beta < 2.2 \text{ eV, 95\% CL}$