

Construction and Status of a Semi-Digital Hadronic Calorimeter

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in behalf of **CALICE**-SDHCAL group CIEMAT, Ghent U., IPNL, LAL, LAPP, LLR, Tsinghua U., Tunis, UCL

Title:IN2P3Filaire-Q Creator:Adobe Illust CreationDate:1/28/2



ECFA R&D Panel DESY, 05/11/2012



- The SDHCAL concept
- Technological prototype construction
- Readout & reconstruction
- Test Beam Preliminary Results for GRPC
- Simulation studies
- A word about μ-Megas
- Perspectives and Conclusion

Semi-Digital HCAL Concept

Ultra-granular HCAL can provide a powerful tool for the **PFA** leading to an excellent Jet energy resolution.

It is based on two points:

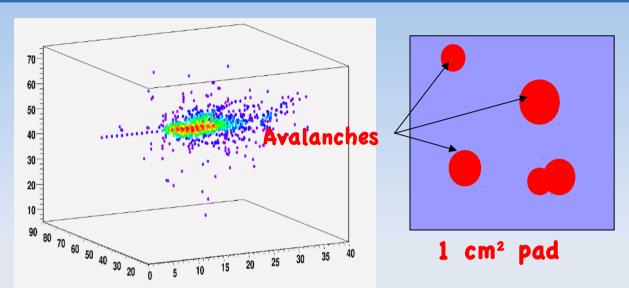
1- Gaseous Detector

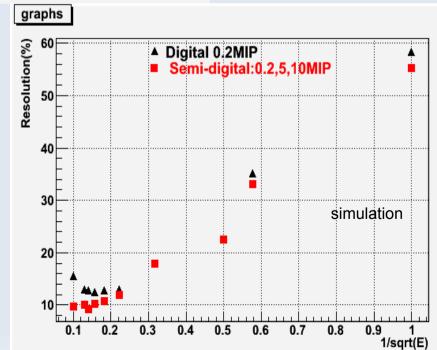
Gaseous detectors like **GRPC** are homogenous, cost-effective, and allow high longitudinal and transverse segmentation.
(MicroMegas was considered as an option)

2- Embedded electronics Readout

A simple binary readout leads to a very good energy resolution
However, at high energy the shower core is very dense and saturation shows up

→ 2-bit readout improves on energy resolution at energies> 30 GeV





SDHCAL technological prototype

SDHCAL is one of the two HCAL options of the **ILD** project.

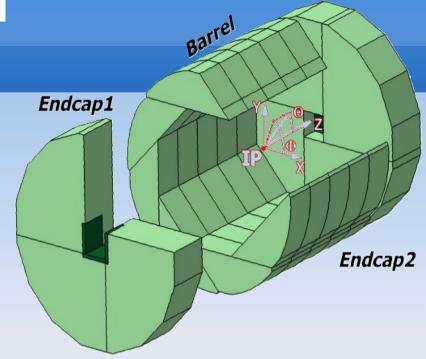
It was proposed with a genuine mechanical structure with no projective cracks and no dead zone between the Barrel and the Endcaps since services are on the periphery

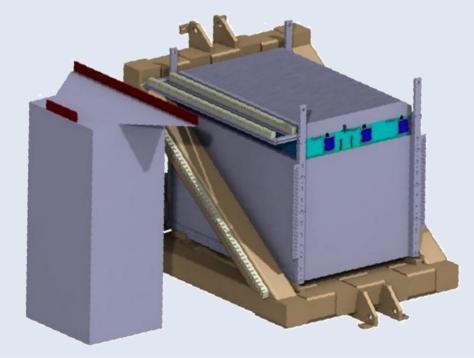
Challenges

- homogeneity for large surfaces
- Thickness of only few mms
- Services from one side
- Embedded power-cycled electronics
- Self-supporting mechanical structure

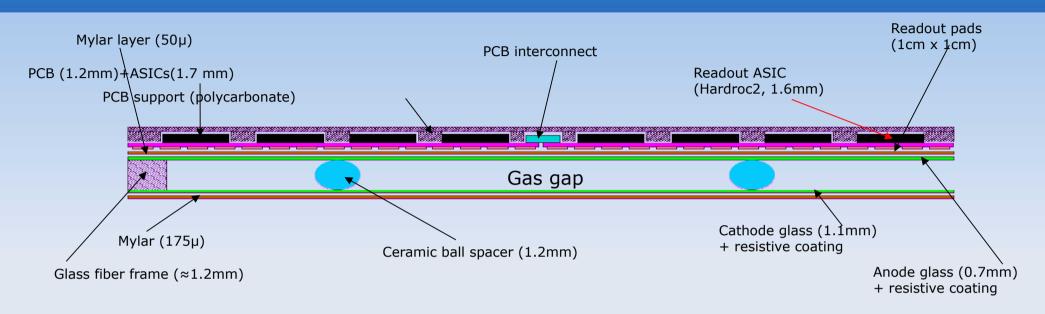
Technological prototype

A prototype with 48 GRPC of 1m² and stainless steel absorber corresponding to 6 $\lambda_{\rm I}$ was conceived as a demonstrator





Structure of an active layer of the SDHCAL



Large GRPC R&D

- Negligible dead zone (tiny ceramic spacers)
- ✓ Efficient gas distribution system (channeling gas inlet and outlet)
- √ Homogenous resistive coating (special paint mixture, silk screen print)



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Electronics readout system R&D

ASICs: HARDROC2

64 channels

Trigger less mode

Memory depth: 127 events

3 thresholds

Range: 10 fC-15 pC

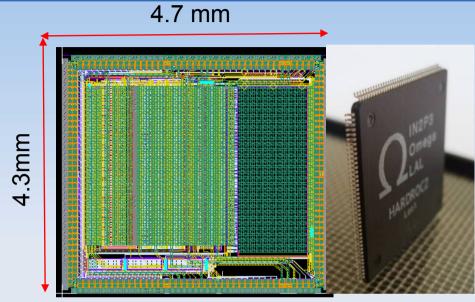
Gain correction → uniformity

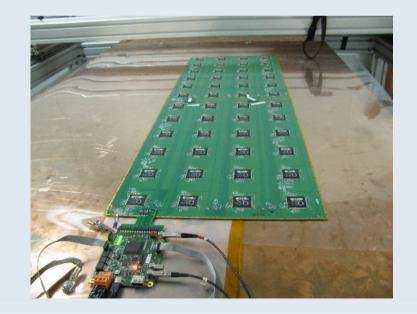
Power-Pulsed (7.5 μW in case of ILC duty cycle)

Printed Circuit Boards (PCB) were designed to reduce the x-talk with 8-layer structure and buried vias.

Tiny connectors were used to connect the PCB two by two so the 24X2 ASIC are daisy-chained.

DAQ board (DIF) was developed to transmit fast commands and data to/from ASICs.





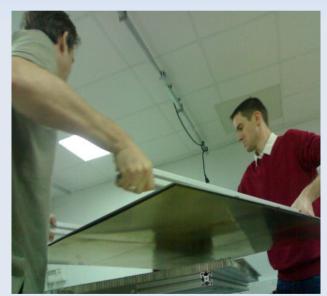
Cassette R&D

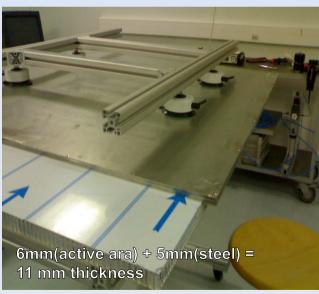
Cassettes were conceived

- ✓ To provide a robust structure.
- ✓ To maintain good contact between the readout electronics and the GRPC.
- ✓ To be part of the absorber.
- ✓ It allows to replace detectors and electronics boards easily.





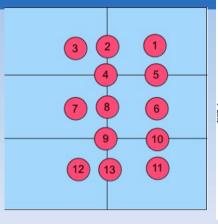


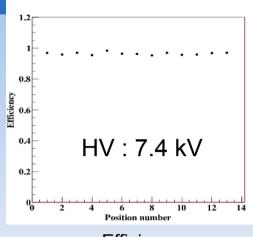


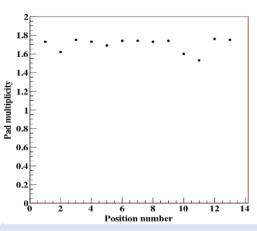
The cassettes are built of no-magnetic stainless steel walls 2.5 mm thick each \rightarrow Total cassette thickness = 6mm (active layer)+5 mm (steel) = 11 mm

The homogeneity of the detector and its readout electronics were studied









Beam spot position

Efficiency

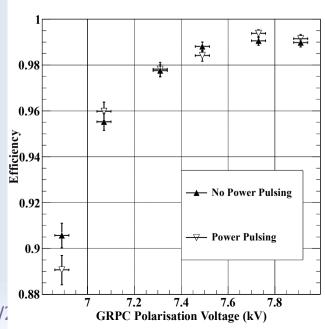
Multiplicity

Power-Pulsing mode was tested in a magnetic field of 3 Tesla



The Power-Pulsing mode was applied on a GRPC in a 3 Tesla field at H2-CERN (2ms every 10 ms)
No effect on the detector performance

ILC duty cycle: 1ms (BC) every 200 ms



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High-Rate GRPC (option)

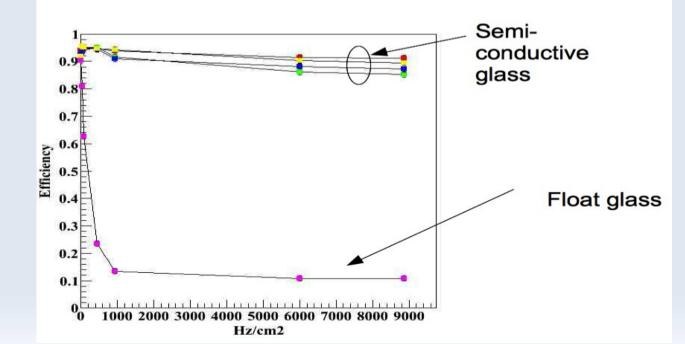
High-Rate GRPC may be needed in the very forward region

- ✓ Semi-conductive glass (10¹⁰ Ω.cm) produced by our collaborators from Tsinghua University was used to build few chambers.
- √4 chambers were tested
 at DESY as well as standard
 GRPC (float glass)

Performance is found to be excellent at high rate for GRPCs with the semiconductive glass and can be used in the very forward region if the rate > 100 Hz/cm²



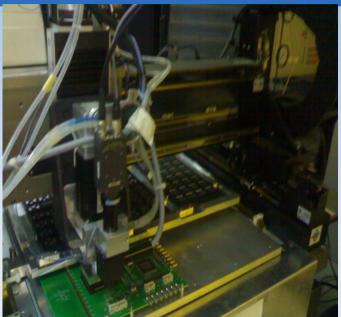


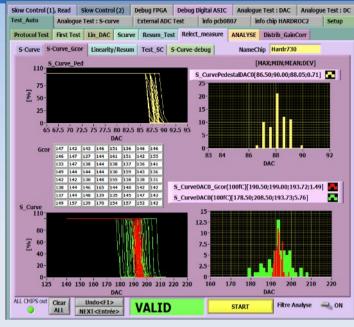


SDHCAL prototype construction

- √ 10500 ASIC were tested and calibrated using a dedicated robot(93% layout)
- √ 310 PCBs were produced, cabled and tested according to strict quality control rules

- ✓ self-supporting mechanical structure was conceived and built.
- √ 51 stainless steel 15mm
 thick plates with planarity
 <250 µm were machined
 and tested
 </p>









Prototype integration







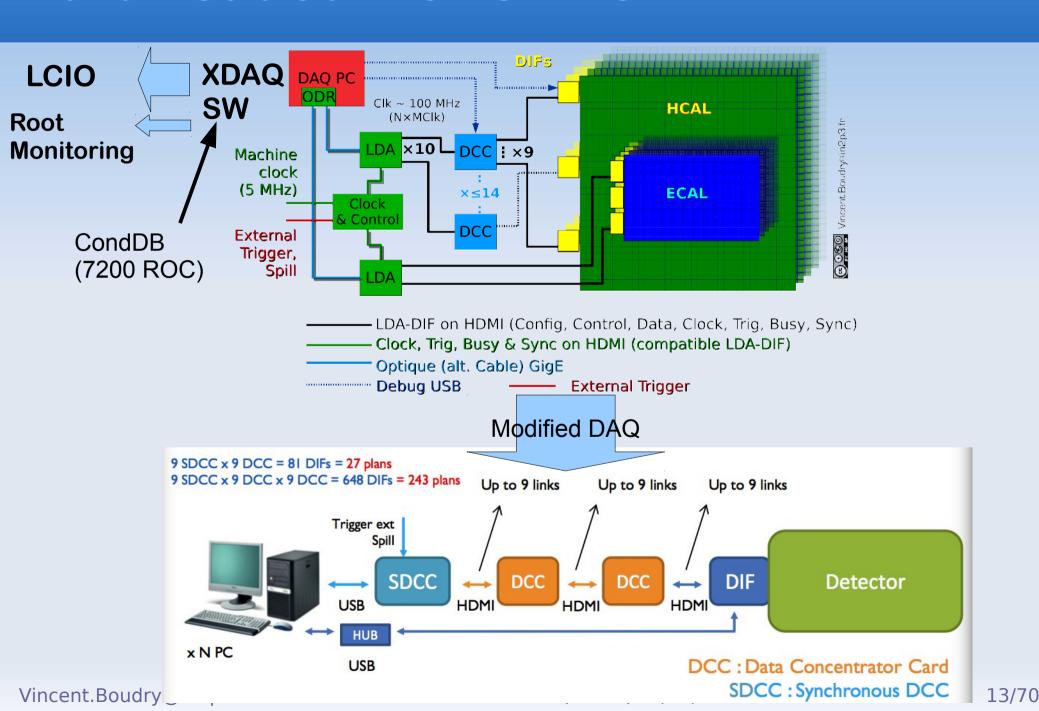


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DAQ

Data readout for SDHCAL



Data taking

- Trigger-less mode: record events until memory is full, then data transfer and restart.
- Power-Pulsed mode : According to the time spill structure
 - ► (N×400 ms (PS)*, 10s (SPS) every 45 s)

Physics events are built as follows: 3 consecutive BC (200ns) around a peak with Nhit/BC>7 # hits 10^{3} Based on cosmic studies Hits left by charged particles 10^{2} # hits 10² 10 10 30000 50000 10000 20000 40000 time (\times 200ns) 2100 2200 2300

N is often 1 and sometimes 2-3 spills/cycle

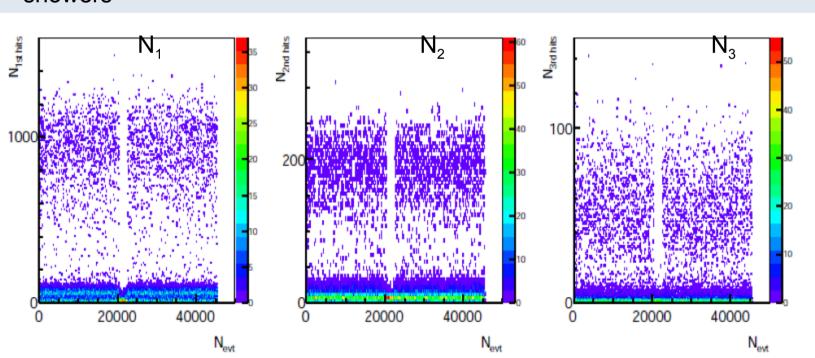
time (\times 200ns)

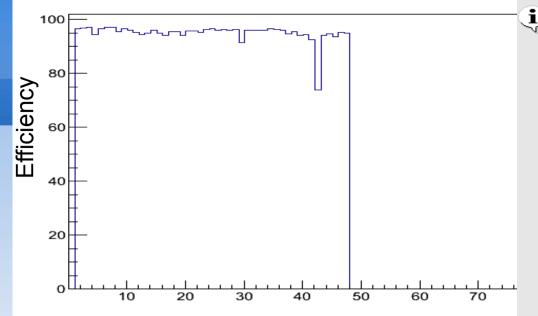
Prototype data acquisition

Online control

During data taking, efficiency and multiplicity are estimated ever now and then using the muon beam, cosmics. This allows to control the detector quality and its stability during the run.

Stability of the three thresholds is also controlled by the hits distribution hadronic showers



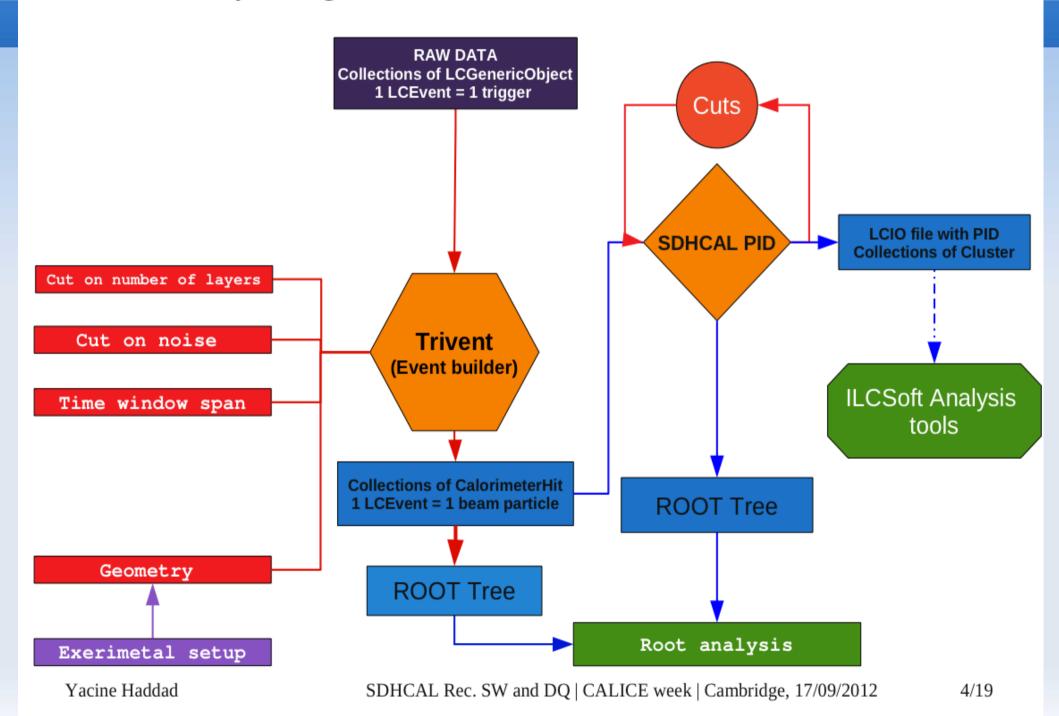


Efficiencies for 43138 |1|298770|288178|96 [2]299923[289999]96 [3]300587[291836]97. [4]302290[285384]94. [5]303182[292831]96. [6]304359[295212]96. [7]303836[295208]97. |8|303234|289097|95 |9|301413|290684|96 |10|299341|287161|9 |11|296713|282710|9 |12|295025|278118|94 |13|292102|277133|9 |14|289232|277629|99 |15|287725|273191|94 |16|285409|268881|94 [17]283921[271082]9 |18|281189|268578|9 |19|279243|262735|94 [20]276900[265080]95 [21]274932[263257]99 |22|273358|260185|95 [23]271427[261003]9 [24]269284[260190]9 |25|267388|256939|96 |26|265796|255818|96 |27|264488|253723|9 |28|262853|253066|96 [29]260714[238445]91 |30|258935|248365|95 |31|257347|247229|96 |32|256354|246290|96 |33|255078|244701|95 |34|253576|244776|96 |35|252403|243090|96 |36|251564|241647|96 |37|250462|237246|94

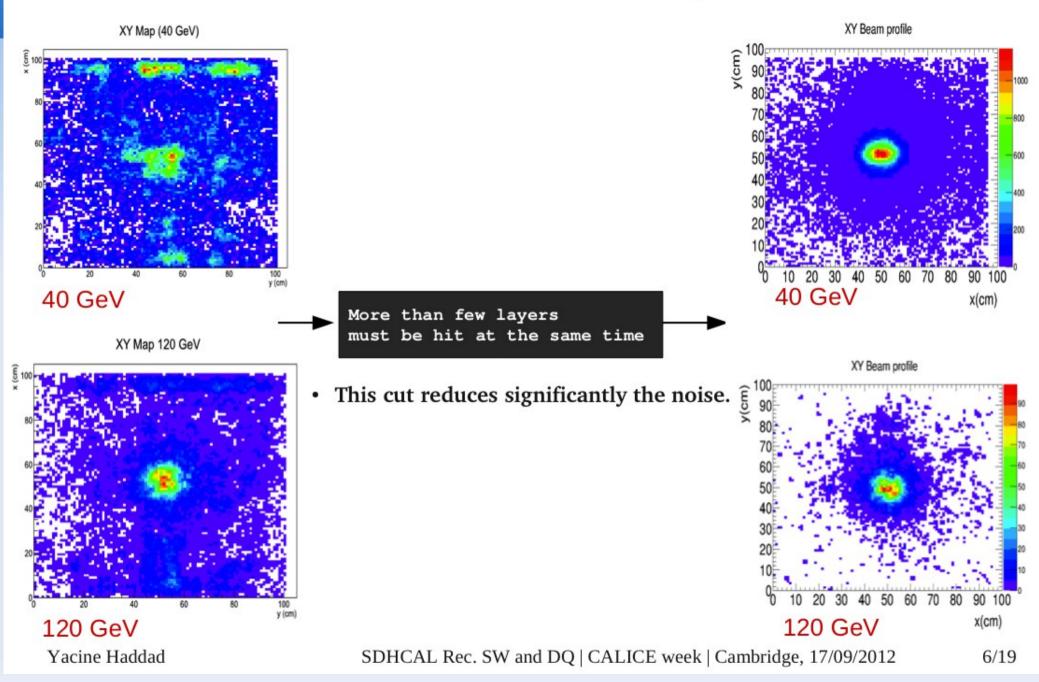
|38|249468|237927|99 |39|248213|233770|99 |40|252447|238044|99 |41|251368|232604|99 |42|249871|184524|73 |43|247550|232840|99 |44|245550|232342|94

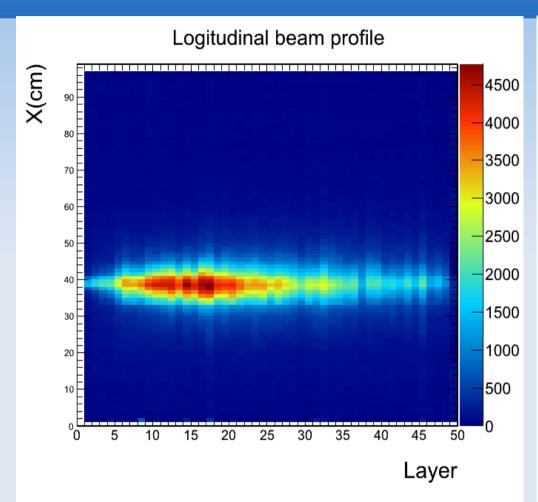
|45||243090||227223||93 |46||240189||228552||95 |47||237527||225465||94

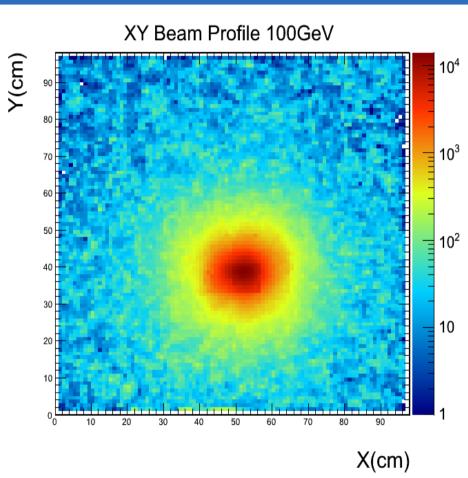
Summary Diagram of SDHCAL Data Reconstruction



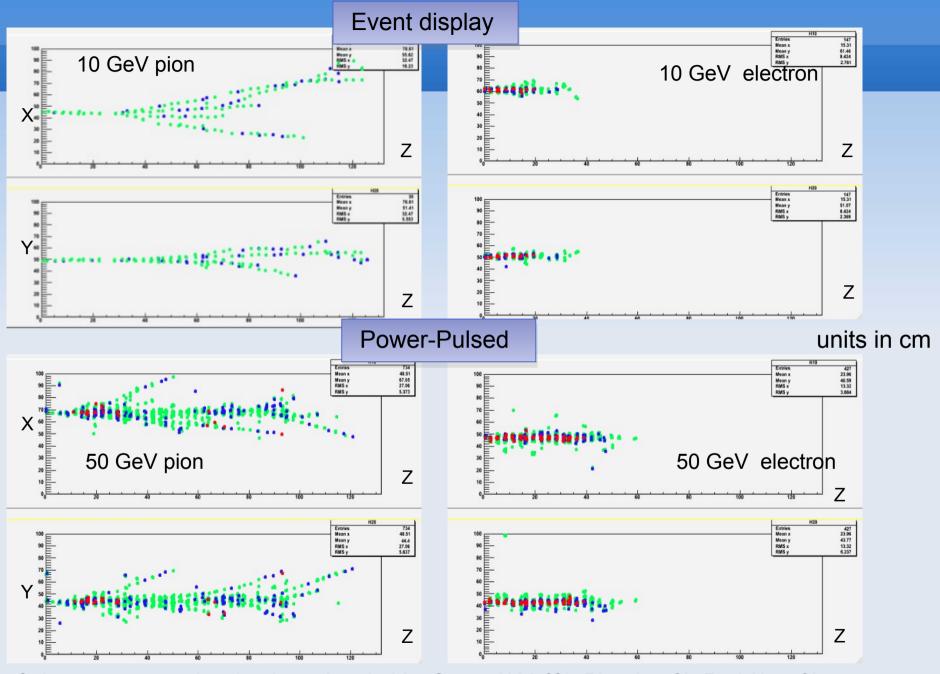
Number of fired layer cut





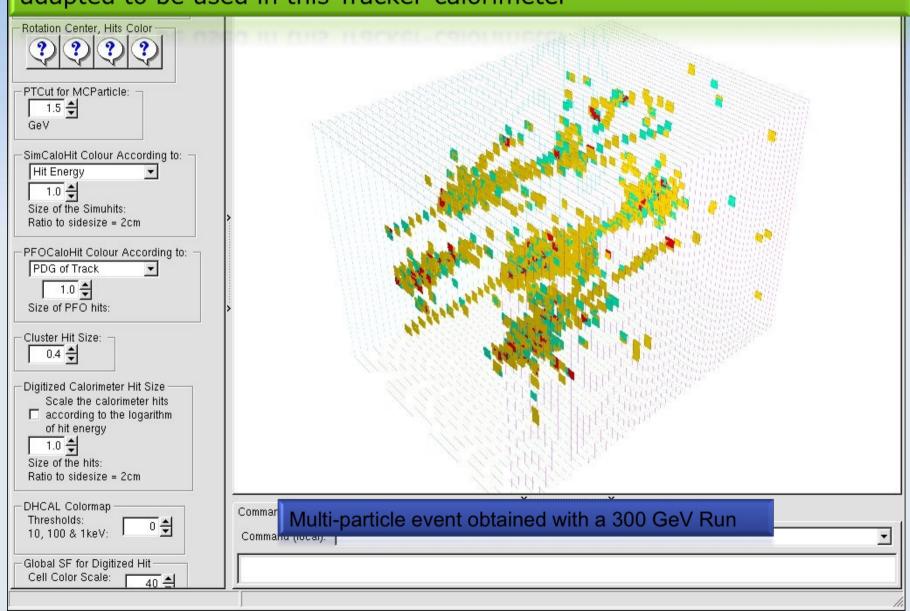


100 GeV pions



Colours correspond to the three thresholds: Green (100 fC), Blue (5 pC), Red (15 pC) Raw data, no treatment except time hit clustering

- √The SDHCAL granularity will allow to separate easily close-by hadronic showers.
- √ Hough Transform and Minimum Spanning Tree algorithms are being adapted to be used in this Tracker-calorimeter



Test beam results

FOREWORDS

- Results from August and May runs
- Raw performances of the Semi-Digital HCAL, 1 m³ based on 1×1 cm² GRPC
 - response to single beam particles
 - Uncalibrated (cell-wise or sensor-wise) calorimeter sensors
 - Not a Particle Flow performances estimation

Data driven analysis

- no use the Ebeam knowledge
- MC needs tuning to data (on going)
- esp. particle ID.
- Mainly results from 1 integrated analysis
 - rush effort of the SDHCAL group and CALICE referee's to validate results
 → CALICE preliminary tag
 - Not final numbers (but good enough!)

Beam conditions

- Beams of pions, electrons and muons at CERN
 - ▶ 2 weeks in May 2012 @ SPS H2
 - π+: 20, 30, 40, 50, 60, 70, 80 GeV
 - ◆ e-:10, 20, 30, 40, 50, 60 GeV
 - μ dedicated runs...
 - 2 weeks in August (& September) 2012 @ SPS H6
 - π+: 5, 7.5, 10, 15, 20, 25, 30, 40, 50, 60, 70, 80, 90, 100 GeV
 - + few μ dedicated runs
- Beam composition:
 - all runs contain μ's (esp. e-) and cosmics
 - π's runs filtered by 4mm Pb to remove e- (esp. for E≥20 GeV)
 - proton component in HE π's runs (@ E≥20 GeV)
 - δE_{heam}/E ~ 1 %
- Large beam profile
 - ▶ low rates (ϵ \sime at $f \ge 100$ Hz)
 - \blacktriangleright Rate monitored online by μ tracks and π tracks segments
 - ♦ Only run with $f \le 1000$ part/spill ⇔ φ ≤ 100 Hz/cm²

Configuration:

GRPC set-up & response

- gas: TFE 93%, CO₂ 5%, SF₆ 2%
- ► HV = 6.9 kV
- ▶ the average MIP induced charge being around 1.2 pC
- ► Thresholds set at 0.11 pC, 5 pC and 15 pC (0.1; 4; 12.5 mip)

Dead zones:

- ▶ 1/3 slab of plane # 46 dead in May; repaired for August runs
- ▶ 1st 47 planes available during 1st week fo August.
- → 7 ASIC switched off (and not replaced) ↔ 1 ‰ dead zone.

Gains

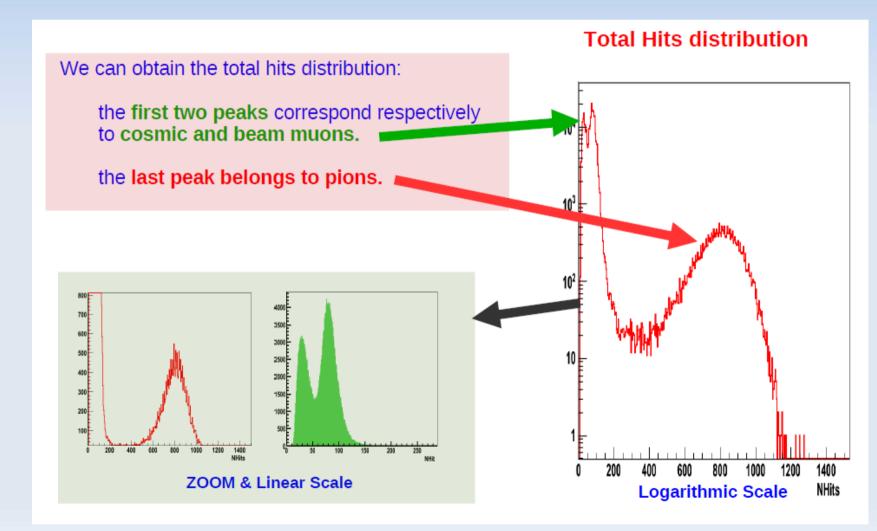
- All set to 1 (no gain corr.) during this data taking
 - (will be done for next period)

Selections & particle ID

Events classification (I)

- Noises
- Muons (from beam and cosmics)
- Pions
- electrons

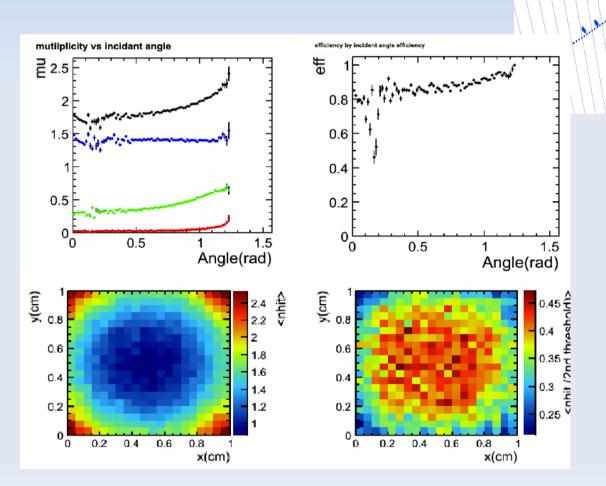
Just the total number of hits is already a good hint.



Efficiency and multiplicity from all muons (cosmics & beam)

■ With muons, one can derive efficiencies and multiplicities per plane, per ASIC, per channel or per area smaller than a cell.

Muons recorded during august test beam.



Multiplicity & Efficiency vs Angle

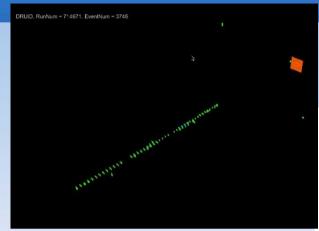
DRUID, RunNum = 714404, EventNum = 4

Efficiency per plane

"folded" in a single cell

⇒ Input to simulation

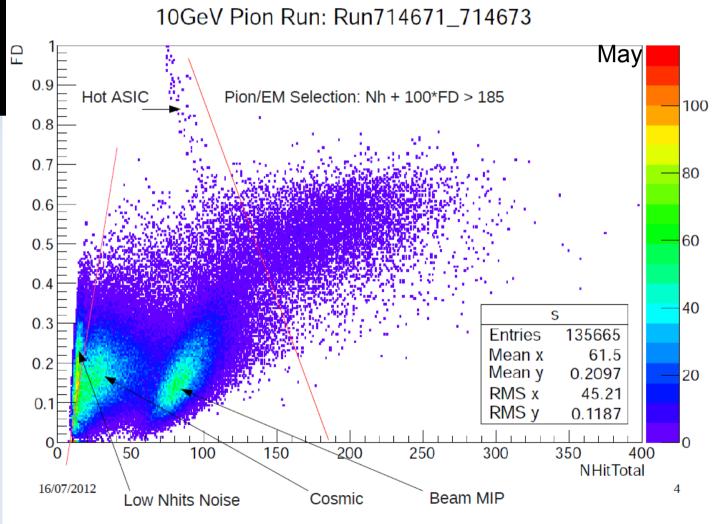
Fractal dimension (FD) versus total number of hits.



$$f(a) = \frac{\ln\left(\frac{N_b}{N_a}\right)}{\ln\left(\frac{a}{b}\right)},$$

$$FD = \langle f(a) \rangle; a > b; \frac{a}{b} \in \mathbb{N}$$

- Can be computed for any thresholds
- •We also use : $\frac{FD}{\ln(Nhi)}$



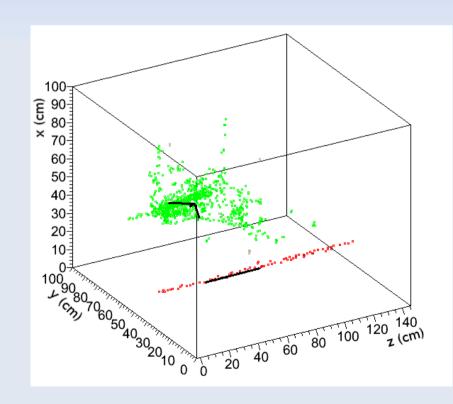
Particle ID variables

Topological:

- Principal Component Analysis (PCA) on all hits or clusters
- ► 3 main \bot axis eigenvalues λ ≡ σ (hits) on axis

$$\lambda_1, \lambda_2, \lambda_3$$
 with $\lambda_1 < \lambda_2 < \lambda_3$

- λ_3 = longitudinal comp.
- Transverse Ratio (λ₁⊕λ₂) / λ₃ → muons vs e, π
- Shower start
 - $ightharpoonup \lambda_{1p}$, λ_{2p} idem to λ_1 , λ_2 restricted to 1 plane
 - ▶ 1st interaction plane (FIP) =
 - $\star \lambda_{1p} \oplus \lambda_{2p} > 1.5 cm$
 - \bullet $N_{hit}^{plane} > 5$



Particle ID (cont'd)

Density

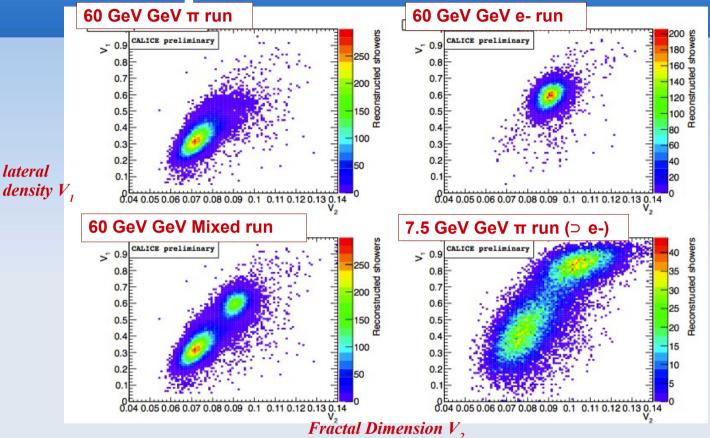
- $ightharpoonup V_1 = (\sum_{layers} N_{25}^{layer}) / N_{hits}$
 - N₂₅ layer = N_{hits} in 5×5 around barycenter in 1 layer
- $ightharpoonup V_2 = FD_{3D} / In(N_{hits})$
 - Fractal dimension: $FD_{3D} = \frac{1}{|I|} \sum_{n \in I} \frac{\ln(N_{\text{hit}}/N_{\text{cube}}(n))}{\ln(n)}$

 $N_{\text{cube}}(n) \equiv \text{number of cube in } I = \{2,3,4,6,8,12,16\}$

Clustering:

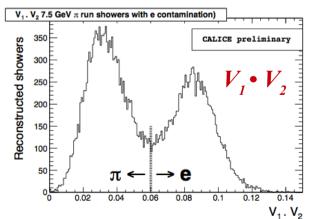
- removal of isolated hits and tagging of overlapping events
- ► MST à la charm-II using $D_{\alpha,\beta} = \left| \text{plane}_{\alpha} \text{plane}_{\beta} \right| + 2 \times (\left| I_{\alpha} I_{\beta} \right| + \left| J_{\alpha} J_{\beta} \right|)$
 - $N_{hits} > 25$; $\lambda_3 > 4.5$ cm; $\lambda_2 / \lambda_3 > 0.01$.

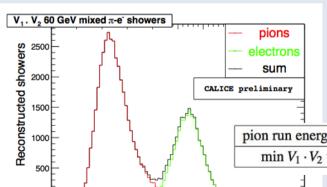
e/π separation



- Operation on clusters
- Negligeable loss of π's @ HE
- few % e- residual contamination @ LE

10% variation of cut ⇒ Systematics





0.02 0.03 0.04 0.05 0.06

Variation of cut with E_{beam}

pion run energy (GeV)	5	7.5-15	20	30-40	50-60	70-80
min $V_1 \cdot V_2$ value	0.065	0.06	0.055	0.05	0.045	0.04

0.07 0.08

Leakage reduction; Statistics of π 's

- FP # < 4.
 - removes cosmics (lateral entrance)
- First Interaction Plane (FIP) # < 15
 - removal of late interacting hadrons.
- The last shower plane (LP) # < 42
- or Nhit(last 7 planes) / Nhit(first 30 planes) < 0.15

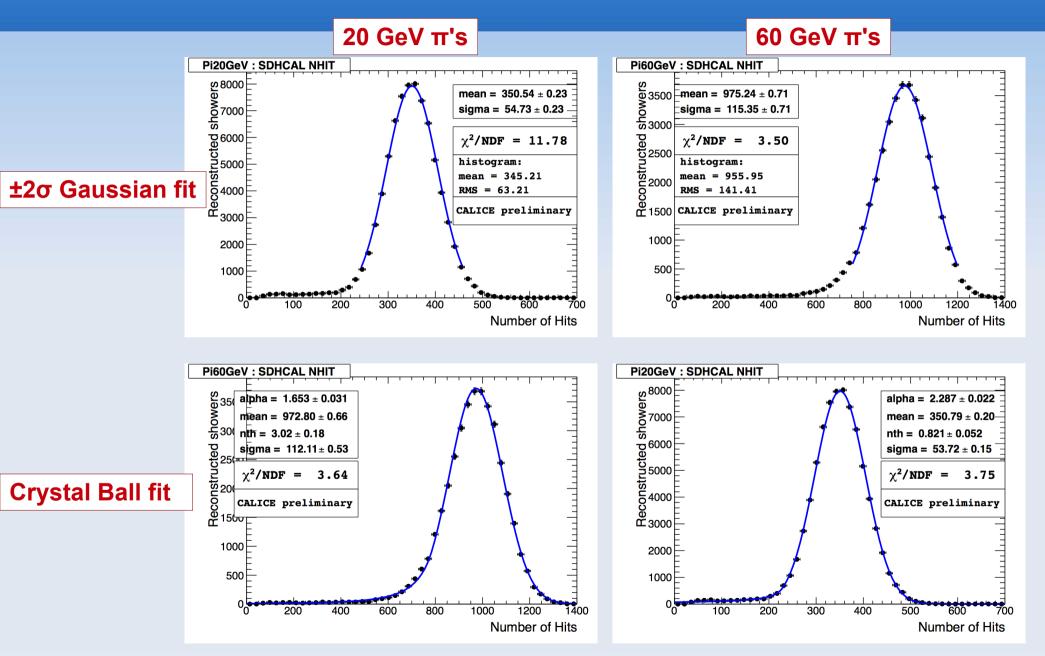
- The first (last) plane (FP, LP) of the reconstructed shower
 - containing a hit:
 - ▶ could be ≠ from interaction plane

After all Selection

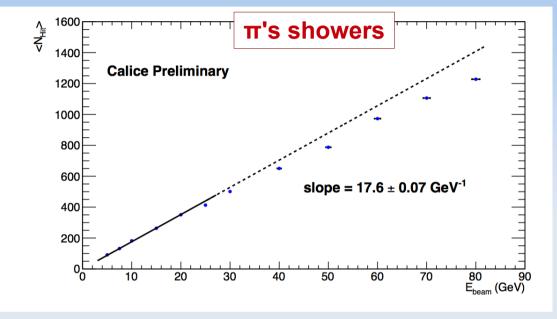
Energy [GeV]	Number of		
	π's events		
5	9504		
7.5	15074		
10	20406		
15	33405		
20	78391		
25	59495		
30	53179		
40	48720		
50	76566		
60	38917		
70	30893		
80	32964		

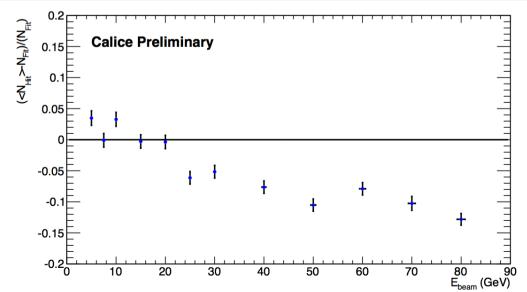
Results

Raw number of hits (binary HCAL)



Nhit response (binary HCAL)





- Saturation observed for E_{heam} ≥ 30 GeV
- Offset (~4 hits) compatible with noise over 3 clock cycles
- Fit by quadratic function:

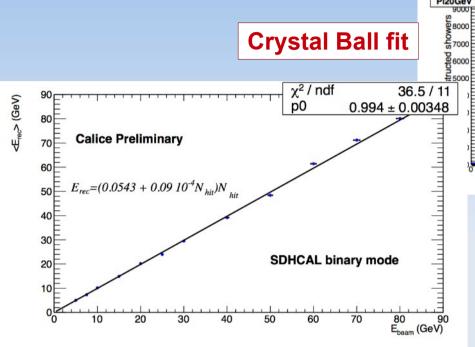
$$E = (C + D \bullet Nhit) Nhit$$

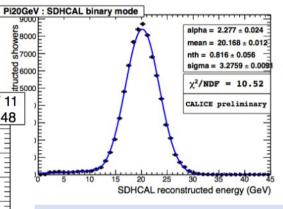
yields:

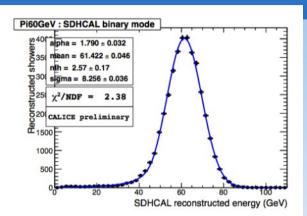
C = 54.3 MeV

D = 0.009 MeV

Linearised response (event by event)



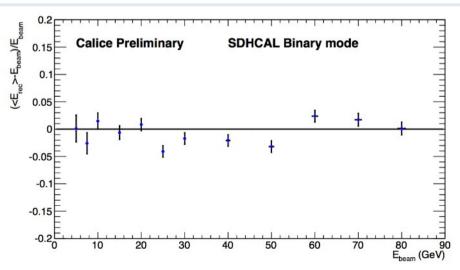


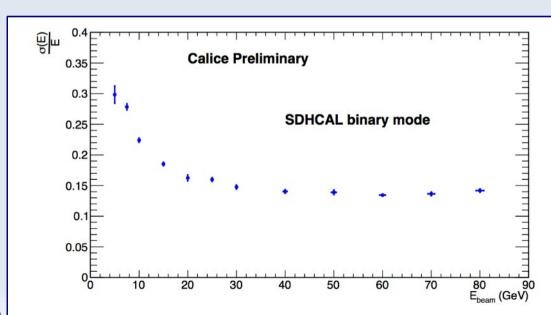


Width (Gauss, CB) $\rightarrow \sigma(E)/E$

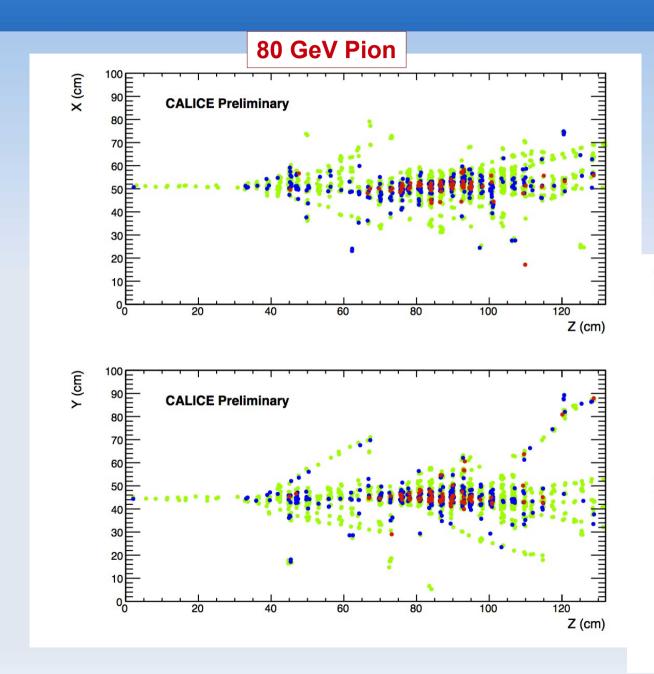
Err = Stat ⊕ δ(Gauss, CB fit)

⊕ cut var +10%



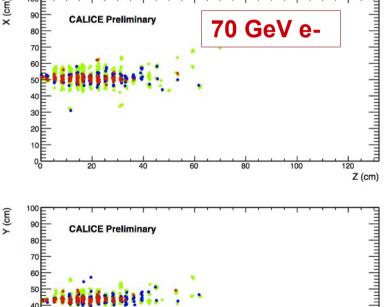


SDHCAL response (multi-thr.)



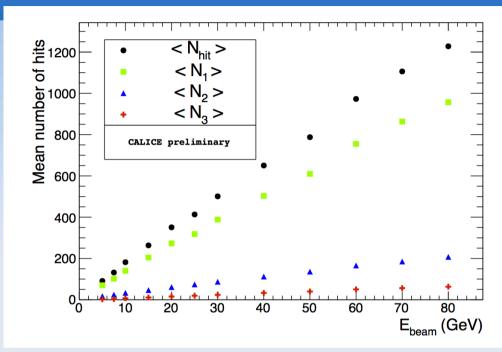
Thresholds set at 114 fC, 5 pC and 15 pC (~ 0.1; 4; 12.5 mip)

 Additional information on shower structure



Z (cm)

SDHCAL response (multi-thr.); Nhits



• Min of χ^2 with

$$\chi^{2} = \sum_{i}^{N} \frac{(E_{true}^{i} - E_{rec}^{i})^{2}}{E_{true}^{i}}$$

over 10, 20, 30, 40, 50 and 60 GeV samples (1/3 of stat.)

- Parametrised as quartic function of Nhit
- Valid for single known particle...

▶
$$N1 = \# \text{ of Hits} \ge \text{thr1}, <\text{thr2}$$

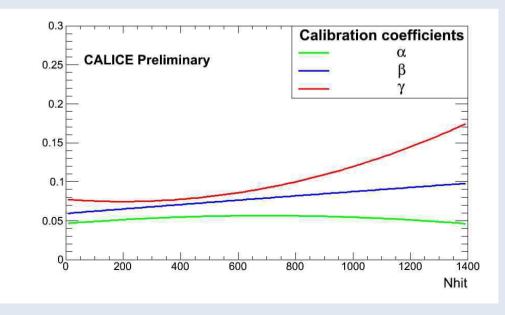
►
$$N2 = \# \text{ hits } \ge \text{thr } 2, < \text{thr} 3$$

►
$$N3 = \# hits \ge thr3$$

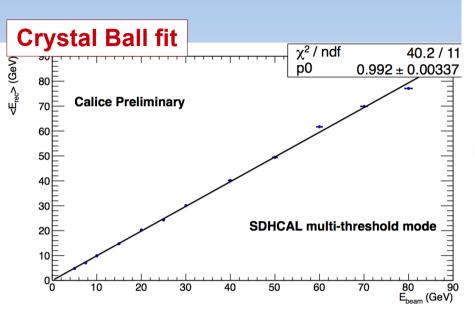
$$Nhit = N1 + N2 + N3$$

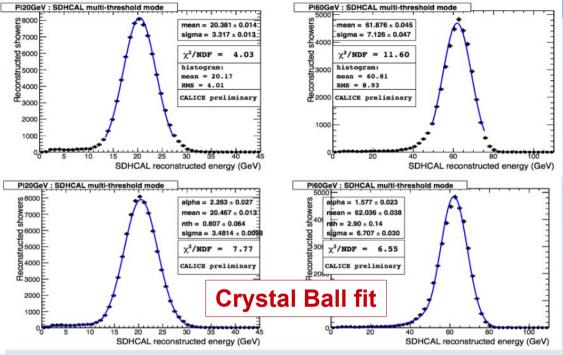
$$E_{rec} = \alpha N1 + \beta N2 + \gamma N3.$$

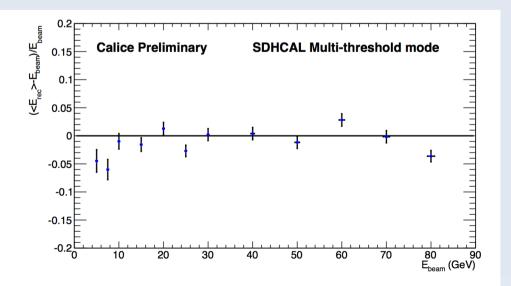
 $\alpha,\beta,\gamma = f(Nhit)$



SDHCAL response

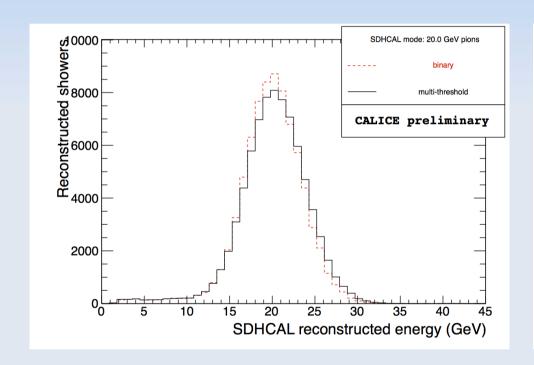


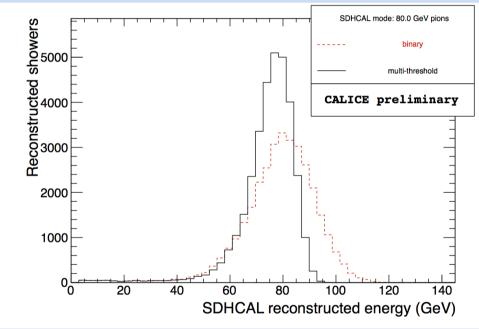




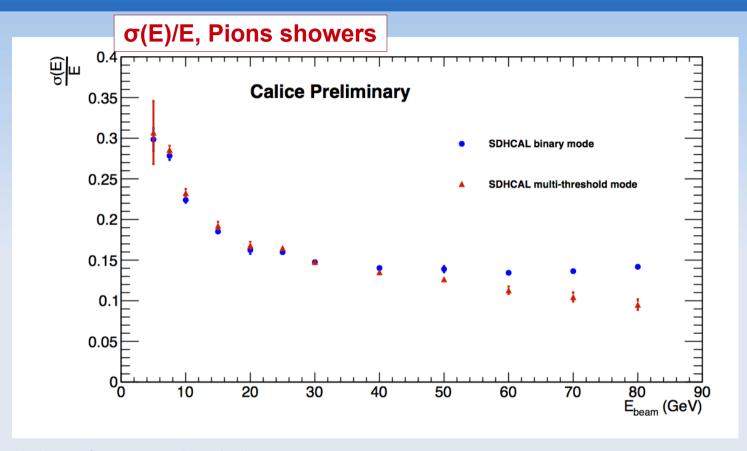
- Linearity ≤ 5% over full range
 - ► Tuning done for E_{heam} ≥ 10 GeV
 - e- contamination @ low E.

SDHCAL: binary vs multi-thr.





SDHCAL binary & multi-thr modes



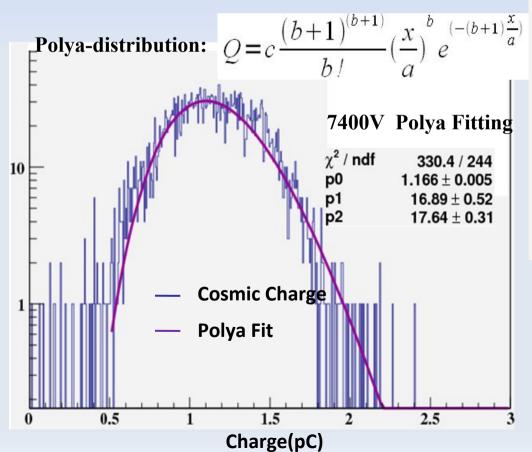
- Raw resolution of untuned calorimeter
 - ▶ SDHCAL
 - ▶ DHCAL
- Single pions, filtered for leakage
- Err = Stat ⊕ δ(Gauss, CB fit) ⊕ cut var ±10%SHCAL

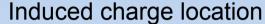
- Visible improvement of resolution for $E\pi \ge 50$ GeV
 - ≥ 10% at 80 GeV.
- Raw performances (no pattern recognition, PFA, ...)

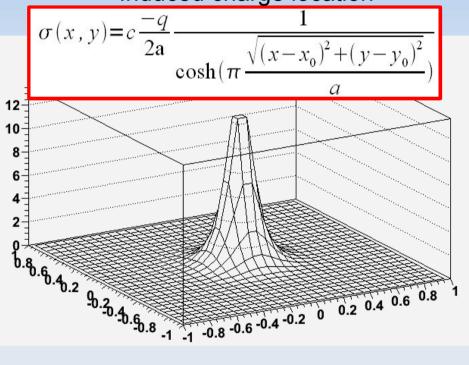
Simulation

Comparison with simulation: Digitisation

- Use standalone GEANT4 application to simulate the prototype.
- Digitisation included in the prototype
 - reproduce ε, μ



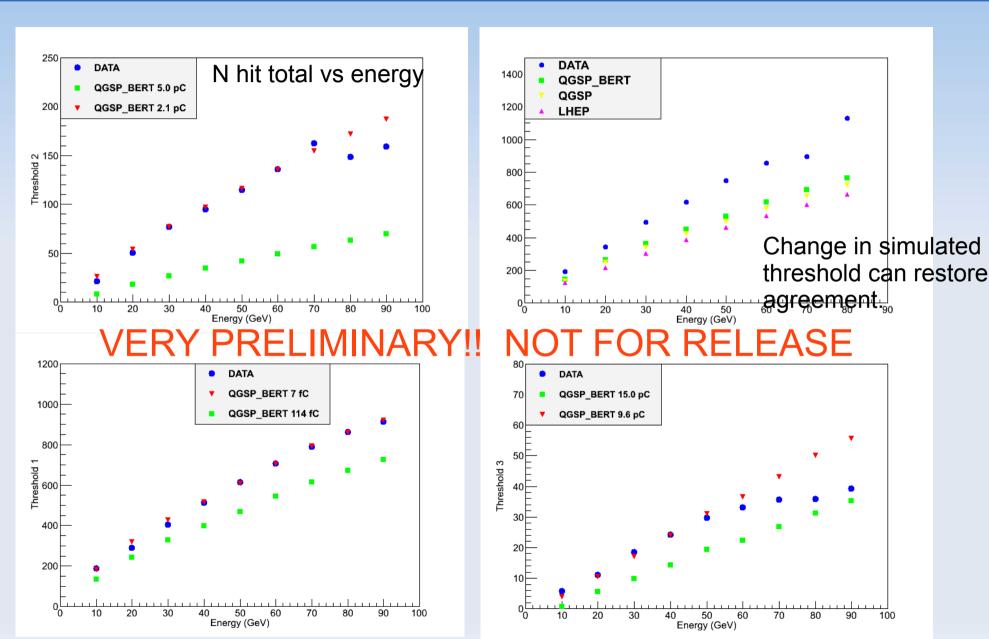




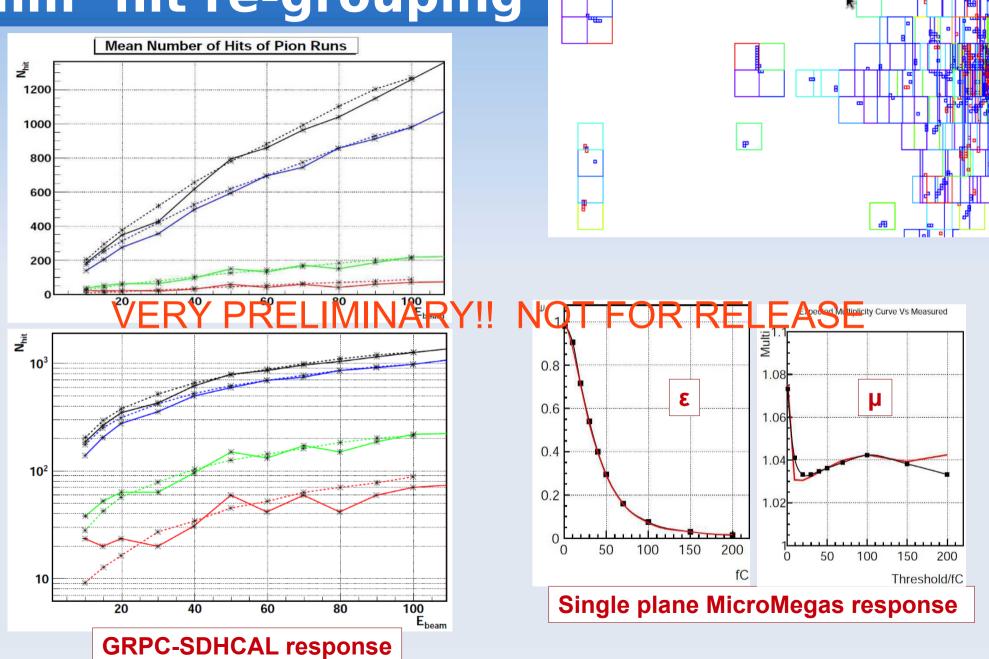
- Two approaches & Marlin modules:
 - Single GEANT hit smearing
 - mm² pseudo cells re-grouped

Comparison with simulation: Hit smearing

Compare GEANT4 physics lists with data



Comparison with simulation: mm² hit re-grouping

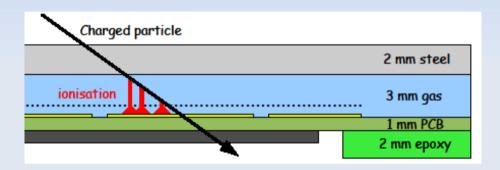


MicroMegas

Micromegas for a 2-bit semi-digital HCAL

Alternative to RPCs operating in the proportional amplification mode

- → No saturation of the avalanche process makes the energy measurement with 3 thresholds more precise
- + High rate capability, basically no ageing and minimal hit multiplicity
- + Operating voltage below 500 V and simple gas mixtures (e.g. Ar/CO₂)



Active Sensor Unit (ASU) of 32x48 cm²

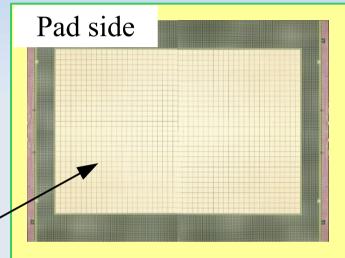
 $1 \text{cm}^2 \text{ pads} + \text{mesh on } 1 \text{ side}$

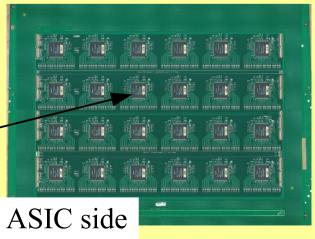
24 MICROROC ASIC + spark protections on other side

MICROROC ASIC (LAPP/LAL Omega)

ILC-like → power pulsing, self-triggering with internal memory

3 thresholds \rightarrow down to 0.25 MIP, up to 100 MIPs





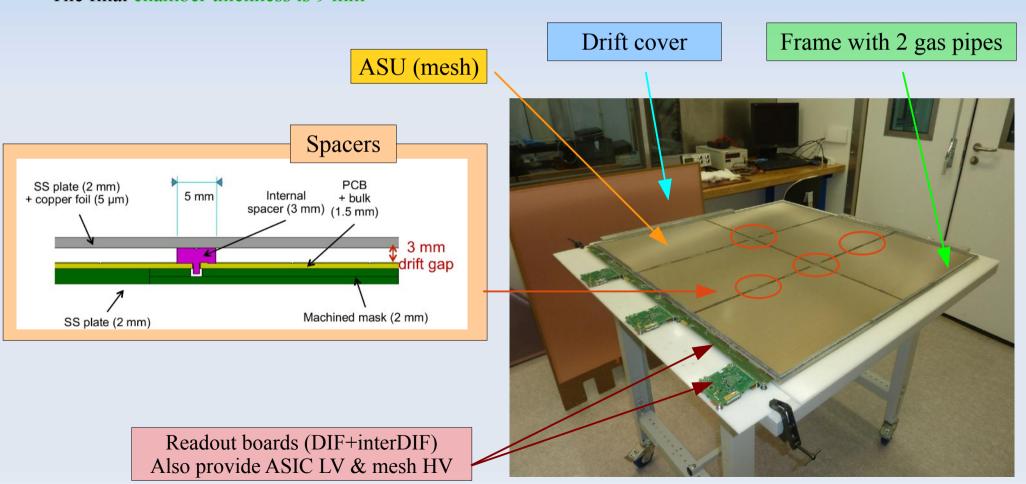
Design of the 1×1 m² chamber

The 1x1 m² chamber consists of 3 slabs of 2 ASUs and some readout boards (DIF + interDIF)

This design introduces <u>very little dead zone (below 2%)</u> and is fully scalable to larger sizes

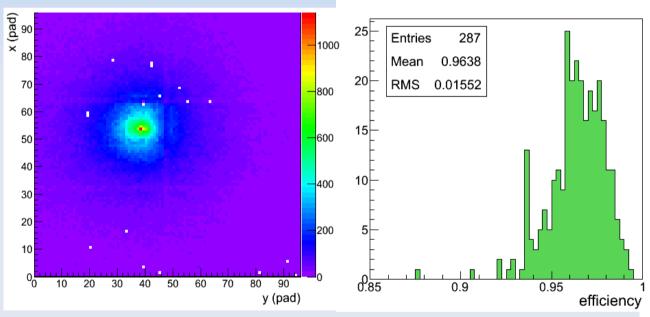
The drift gap is defined by small spacers and a frame

The final chamber thickness is 9 mm



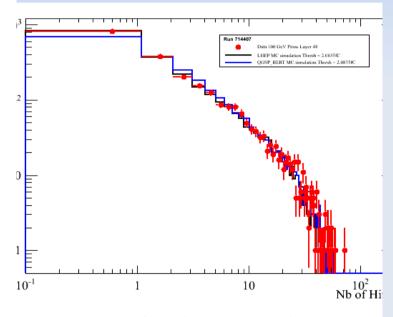
Main performance results

- 1. The XY plot shows a uniform response, no noise and 99.98% working channels
- 2. The average efficiency measured on 2 chambers inside the SDHCAL is $(96 \pm 2 \text{ RMS})$ %
- 3. The number of hit distribution at layer 49/50 of the SDHCAL is well re-produced by simulation



150 GeV/c pions after 1 λ_{int} of Fe XY occupancy for 50 k events

Efficiency to 100 GeV/c muons over 287 regions of 8x8 cm²

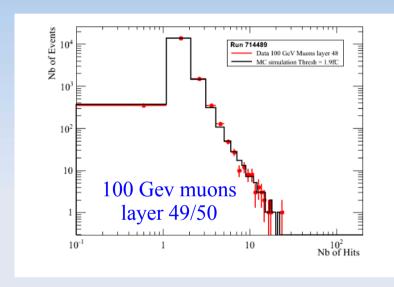


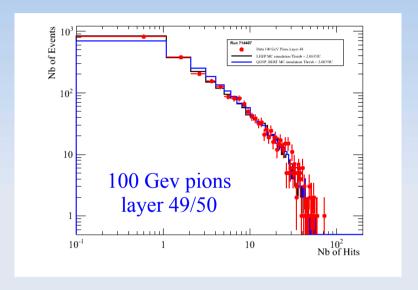
Number of hits from 100 GeV/c pions at layer 49/50 of the CALICE SDHCAL

<u>4 chambers are now ready for test beam</u>, in November, inside the CALICE SDHCAL. In 2013, we will concentrate on the development of <u>spark protections using resistive layers</u>.

Performance inside CALICE/SDHCAL

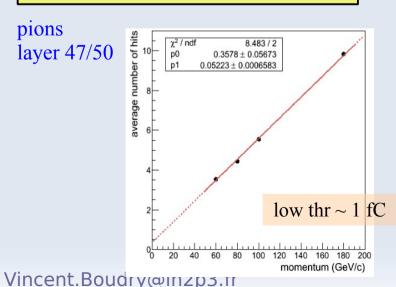
The distributions measured in the Micromegas chambers are well reproduced by MC simulation

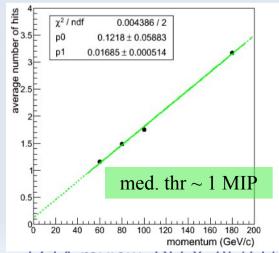


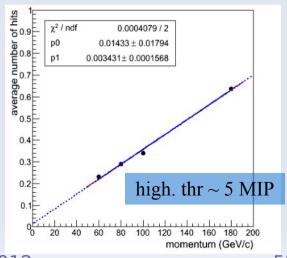


Average Nhit versus pion energy

No saturation at the back of SDHCAL → <u>linear response of 3 thresholds</u>







ECFA review, DESY, 05/11/2012

52/70

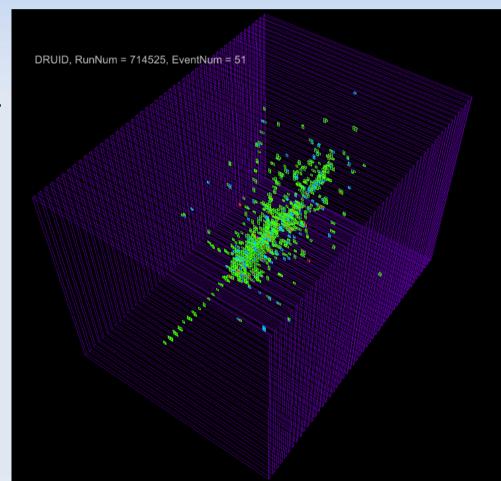
Conclusions & Perspective

- A semi-digital, high granular hadronic calorimeter seems an excellent tool to achieve PFA in the future linear collider experiments.
- The CALICE technological SDHCAL-GRPC prototype was successfully tested with its 48 layers and its 6 λ_1 in different places (SPS, PS)
 - ► Power-Pulsing allows optimal conditions (temperature, noise) and it was the running mode during this year different TB.
 - Excellent data quality was obtained in TB (especially in August with gas installation under our own control) with smooth running conditions (no intervention for the 2week TB period).
- Preliminary results without data treatment (no gain correction, no local calibration, ...) indicate an excellent single particle energy resolution on pions
 - Multi-threshold mode brings significant improvement at Eπ≥50 GeV.
 - Many many studies still to be done
 - ◆ Electron response; thr. scan; PFA disambiguation; pattern recognition; ...
- Comparison with simulation is ongoing and will bring rich information to better understand the hadronic showers.

Prospects

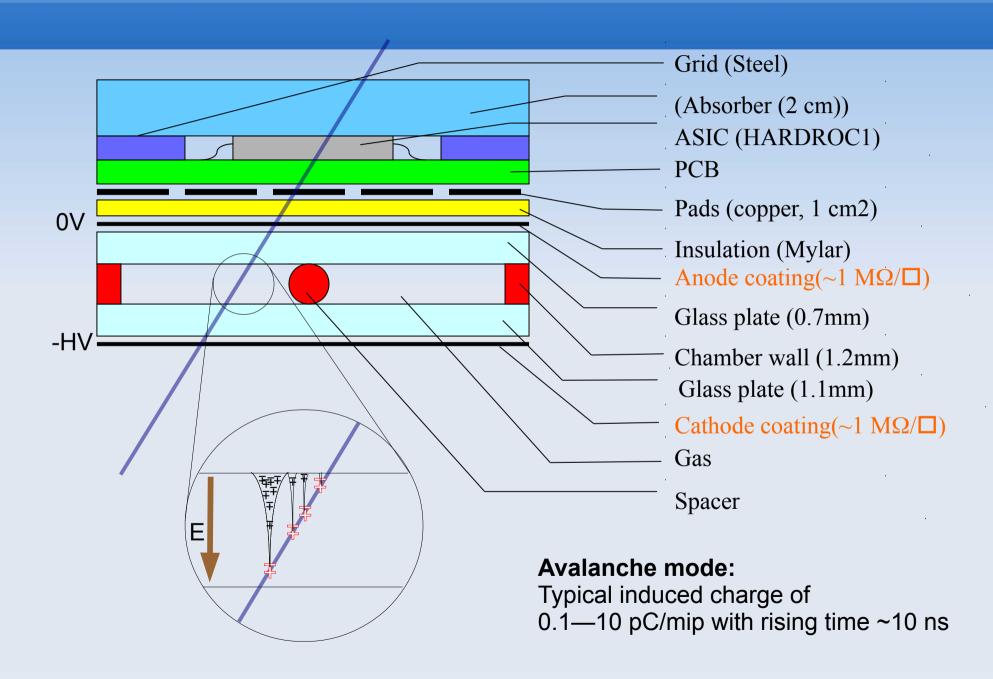
- Prospects50 GRPC will used for the November TB at CERN. Gain correction will be applied. A tail catcher using 4 chambers of MicroMegas will be used
 - ► A week with 4 MicroMegas & 46 GRPC will follow

- Work on very large GRPC 2-3 m² has started and will be completed next year.
 - new ASIC generation (HR3),
 - new PCB
 - improved readout system.

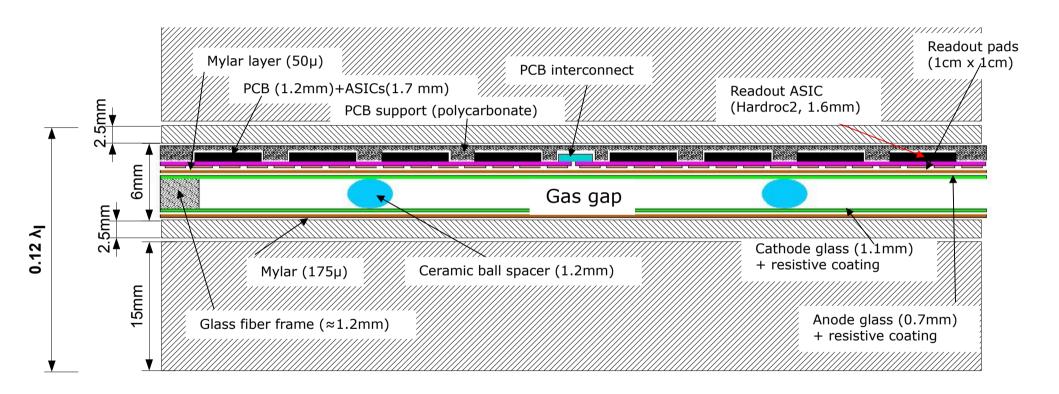


Back up

Glass Resistive Plate Chamber



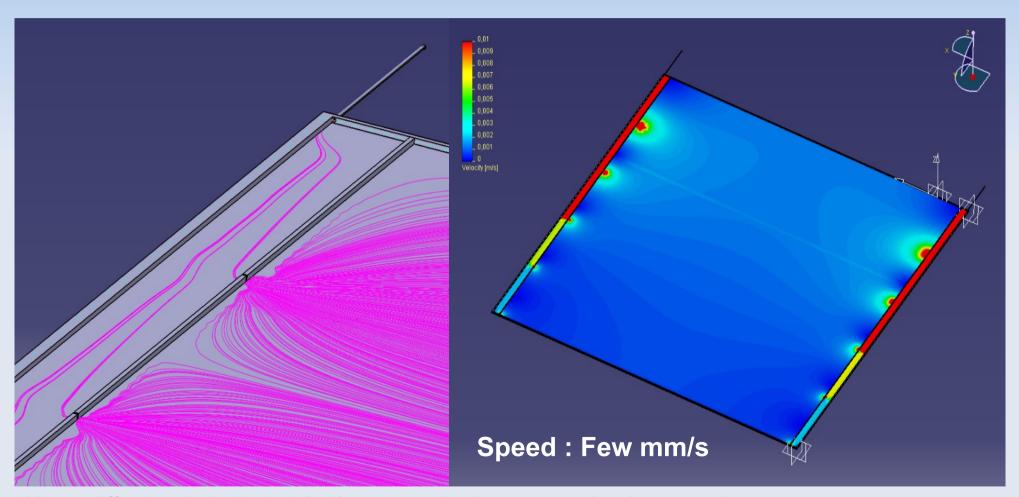
Structure of an active layer of the SDHCAL



50 layers of 0.12 $\lambda_1 = 6 \lambda_1$

Gas distribution system

The services being on one side of the detector, a new gas distribution design is used. It allows to distribute the gas uniformly in the large chamber.

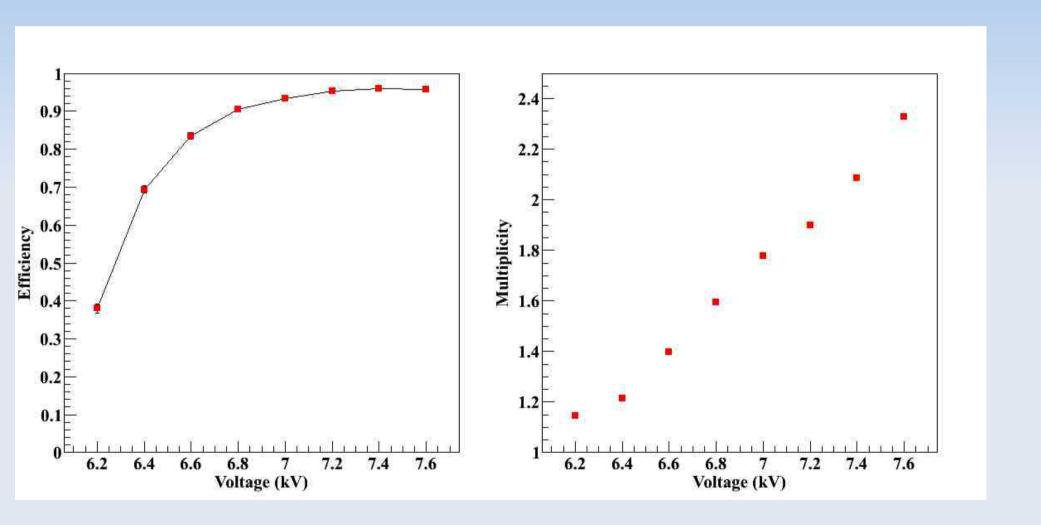


When diffusion is included → Homogeneity is expected to be even better

A test using Kr83m radioactive gas is scheduled to monitor online the gas distribution

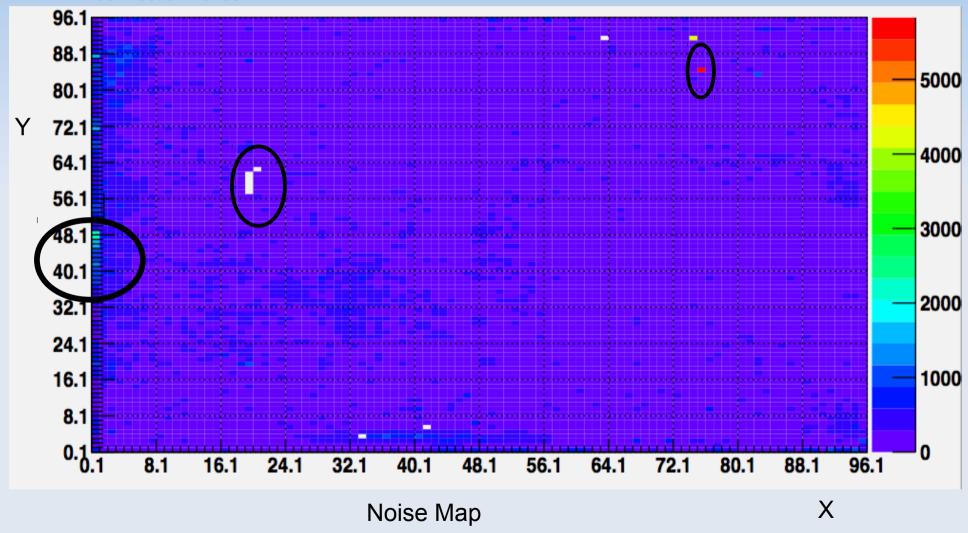


To check that the detectors and electronics are not at the origin of this... A short beam test was organized at PS in November 2011 with 6 detectors taken from the prototype



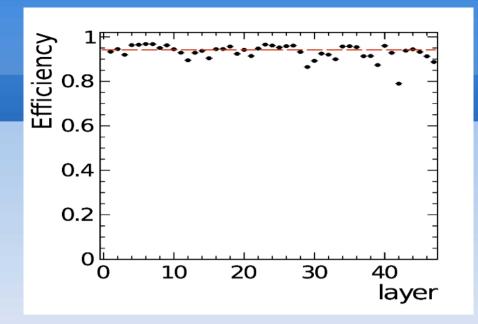
Validation

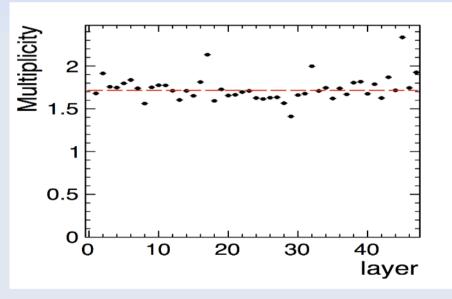
Noise was measured and found to be < 1 Hz/cm² outside the channeling tubes and HV connection zones



μ track selection (monitoring)

- ε, μ estimated from tracks reconstructed from other layers
 - hits are grouped in clusters if sharing an edge
 - ► isolated clusters ($\Delta r_{in \, layer} > 12 \, cm$) dropped
 - ► Tracks reconstructed if remaining N_{lavers} > 7,
 - with at least 1 layer on each side of investigated one (except 1st and last layer)
 - ▶ χ^2 with $\Delta x,y = \text{Span(cm)}$ in $(x,y) / \sqrt{12}$
- Efficiency





Nb tracks with ≥ 1 hit $\delta r \leq 3$ cm from track impact in plane Nb of tracks

 $\langle Nb | hit in cluster closest to tracks, if any \rangle$

Crystal Ball function

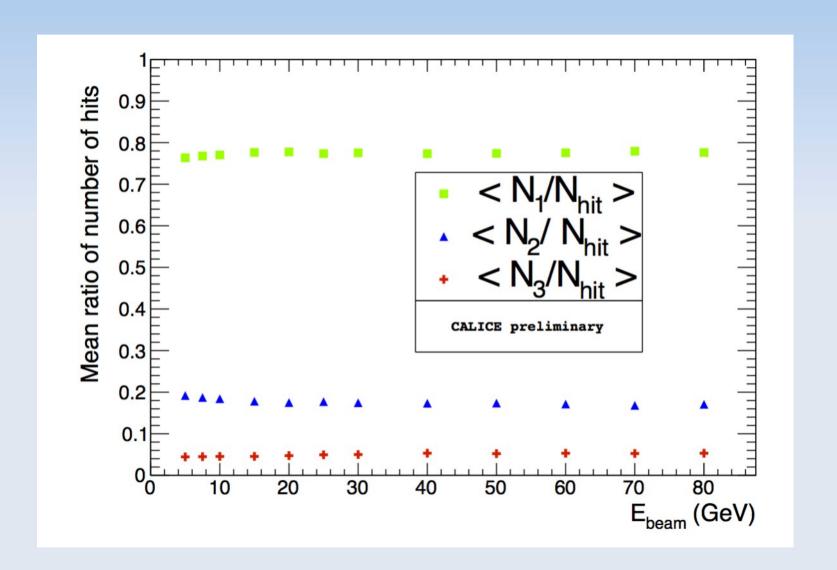
$$f(x; \alpha, nth, \bar{x}, \sigma) = N \cdot \begin{cases} \exp(-\frac{(x-\bar{x})^2}{2\sigma^2}) & \text{for } \frac{x-\bar{x}}{\sigma} > -\alpha \\ A \cdot (B - \frac{x-\bar{x}}{\sigma})^{-nth} & \text{for } \frac{x-\bar{x}}{\sigma} \leq -\alpha \end{cases}$$

where:

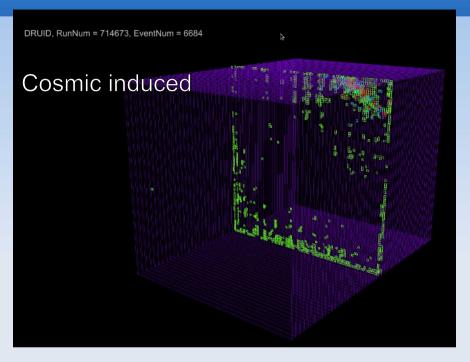
$$A = \left(\frac{nth}{|\alpha|}\right)^{nth} \cdot \exp\left(-\frac{|\alpha|^2}{2}\right)$$

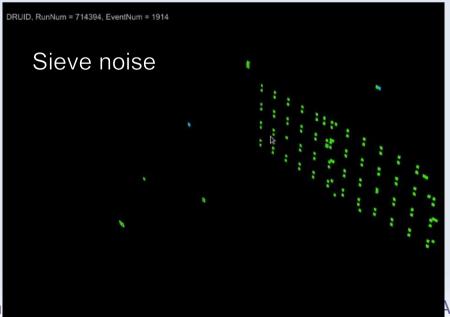
$$B = \frac{nth}{|\alpha|} - |\alpha|$$

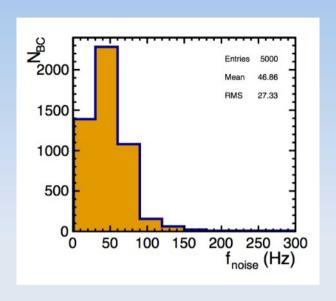
N is a normalization factor.

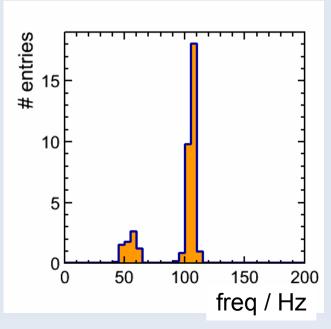


Coherent noise



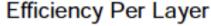




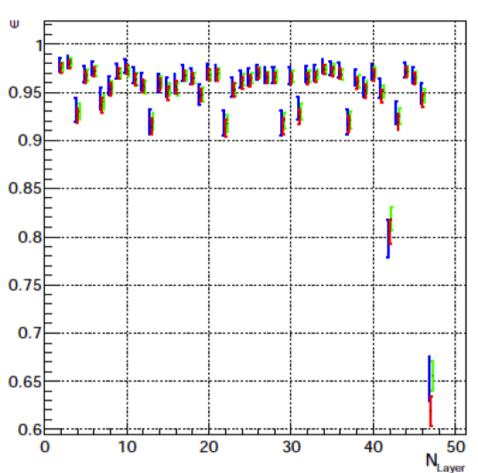


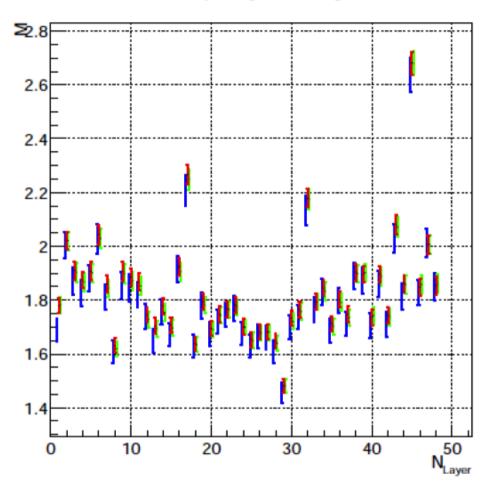
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Efficiency & Multiplicity: Stability



Multiplicity Per Layer





Stable with sensible fluctuation (error bar scaled by 10 times)

15 GeV Pion (714439, 4441): 43797 long beam mip evts

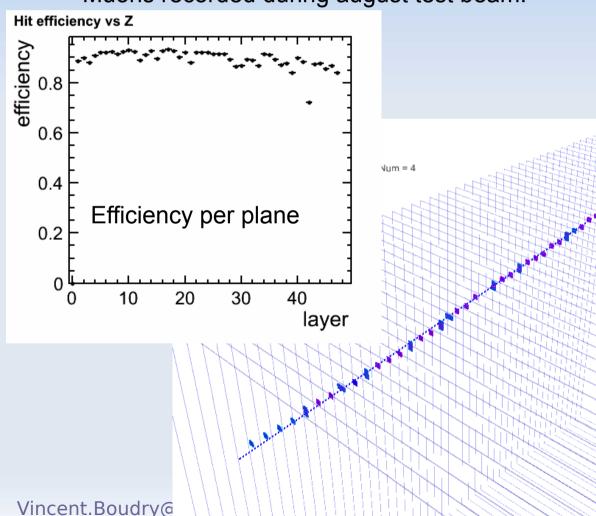
20 GeV Pion (714565, 4573): 103109 evts

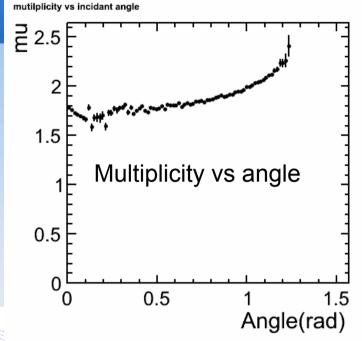
60 GeV Pion (714551, 4552, 4553): 98960 evts

Micro structure of segmented GRPC response... **The company of the company of th

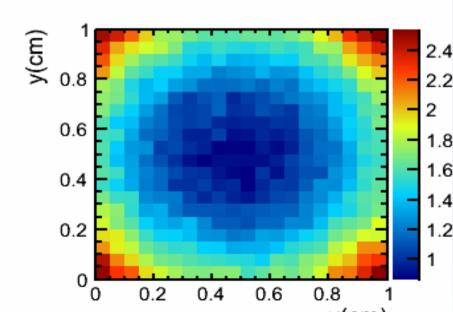
With muons (beam + cosmics), one can derive efficiencies and multiplicities per plane, per ASIC, per channel or per area smaller than a cell.

Muons recorded during august test beam.



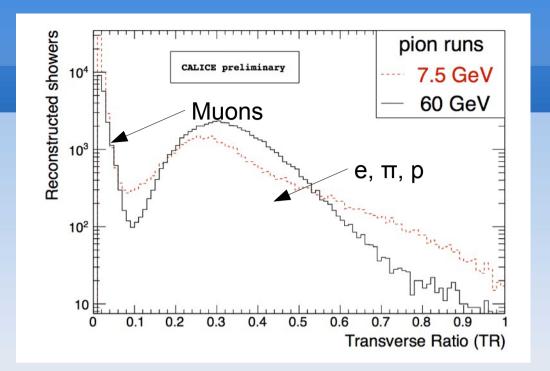


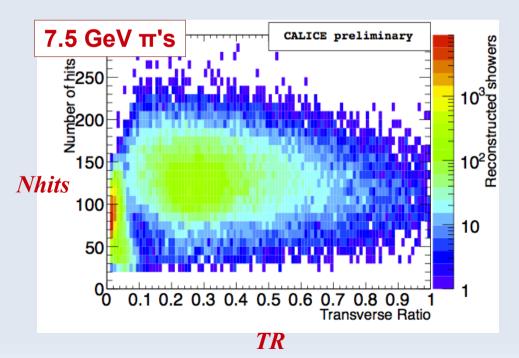
Multiplicity in a cell

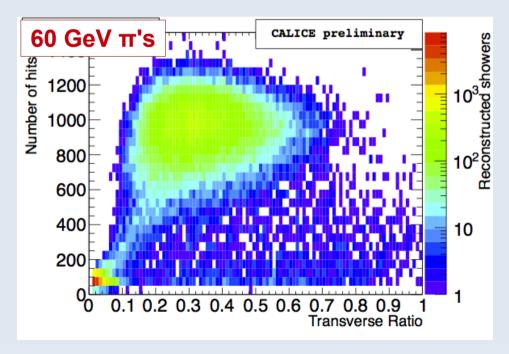


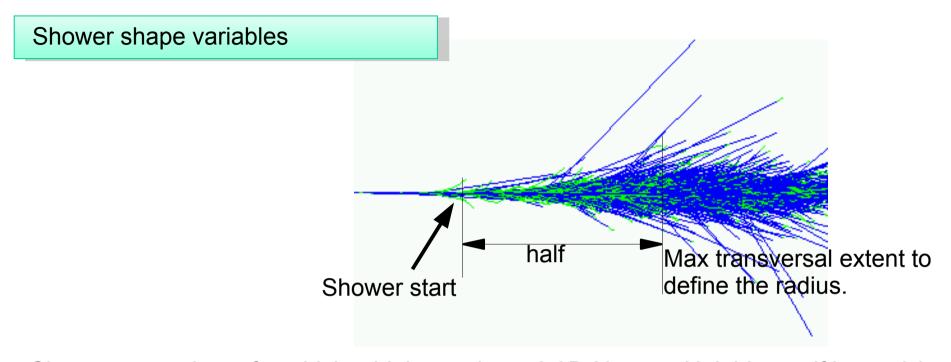
Event selection

- μ rejection:
 - Transverse ratioTR ≥ 0.1 → 98% of μ's









Shower start = layer for which a hit has at least 8 3D-Nearest Neighbours if layer+3 has at least 12 Nearest Neighbours.

Then for each layer, clusterise the hits, removing hits which are at more than 3 rms (spatial distribution) from the center of gravity.

Find the layer which has the biggest spatial rms of the hit distribution. That rms is the radius.

Half is the distance between the shower start layer and the layer that has the biggest spatial rms.

