

# Theoretical developments in top-quark physics.



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**LBNL & UC Berkeley**



**QCD@LHC 2013**

**DESY Hamburg, 3 September 2013**

- ## TOP QUARK



Acrylic felt with  
gravel fill for  
maximum mass.

**\$10.49**  
PLUS SHIPPING

**LIGHT HEAVY**

The **PARTICLE ZOO**

No attempt to review latest experimental results, look for them in Gonzalez-Sevilla's talk and yesterday's parallel session.

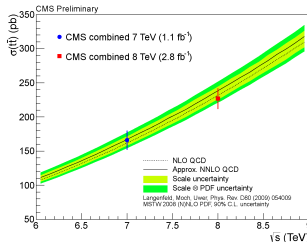
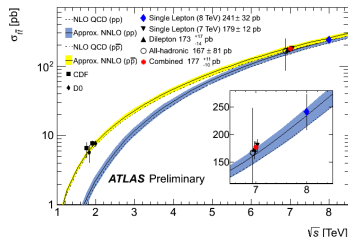
# $t\bar{t}$ pair production

- ▶ Large production cross section at LHC  $\approx 220$  pb at 8 TeV,  $\approx 930$  pb at 14
- ▶ Expected experimental error  $\approx 5\%$
- ▶ NLO long established (25 years)
- ▶ Soft-gluon threshold resummation available up to NNLL
- ▶ NLO+NLL predictions still yield an uncertainty of  $\approx 10\%$
- ▶ Approximate NNLO approaches agree within current exp. uncertainties

Nason, Dawson, Ellis '88-'89, Beenakker et al. '88-'90  
Mangano, Nason, Ridolfi '91

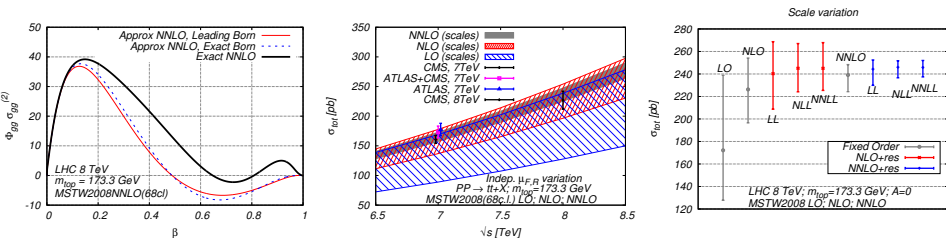
Catani et al. '96, Kidonakis, Sterman '97, Bonciani et al. '98  
Beneke et al. '09, Czakon et al. '09  
Kidonakis '09-'11, Ahrens et al. '10-'11

Aliev et al. '10, Beneke et al. '11  
Ferroglia, Pecjanc, Yang '13



# NNLO $t\bar{t}$ pair production

- ▶ Complete NNLO results available for total x-sec. Baernreuther, Czakon, Fiedler, Mitov '12-'13
- ▶ Uses sector-decomposition-improved FKS subtraction for IR singularities
- ▶ Comparable theoretical and experimental uncer. for total cross sections
- ▶ Challenges approximate NNLO results in all production channels see Fiedler's talk



- ▶ Inclusion of NNLL resummation reduces scale var. uncertainty to 3%
- ▶ Other theoretical unc. of similar size: PDF  $\approx 3 - 5\%$ ,  $\alpha_s \approx 1.5\%$ ,  $m_t \approx 3\%$
- ▶ Allows for an extraction of  $m_t^{\text{pole}}$  and  $\alpha_s(m_Z)$  at NNLO see exp. talks
- ▶ Differential distributions feasible, albeit computationally challenging!

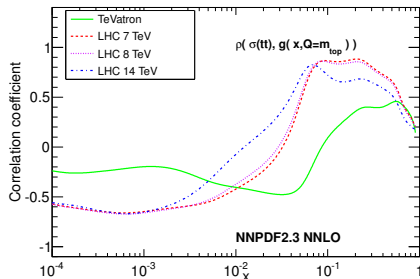
# NNLO $t\bar{t}$ pair production: constraining gluon PDF

- ▶ Top pair x-sec. at LHC highly correlated to gluon PDF in  $0.1 \lesssim x \lesssim 0.5$  range
- ▶ Including 5 Tevatron and LHC results for  $t\bar{t}$  x-sec. into PDF fits

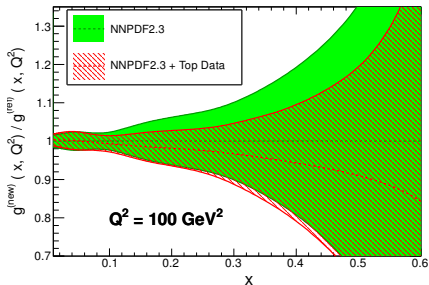
Czakon, Mangano, Mitov, Rojo '13

- Reduces uncertainty on gluon PDF
- Reduces total PDF uncertainty on predictions for  $gg$  driven processes

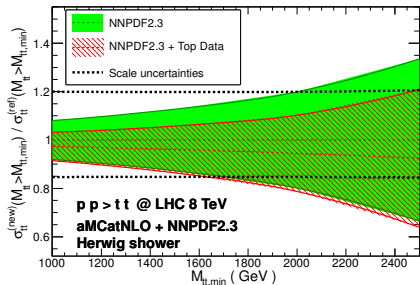
Correlation between PDFs and Cross-Section



Ratio to NNPDF2.3 NNLO,  $\alpha_s = 0.118$



Ratio to NNPDF2.3 NNLO

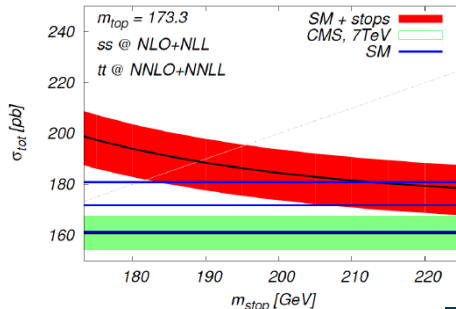
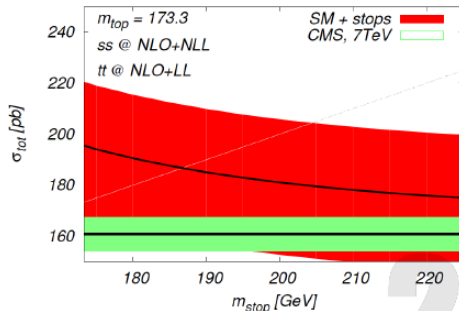
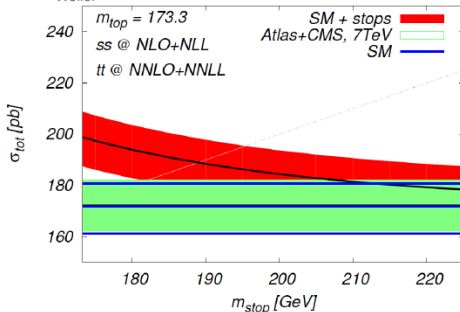


# NNLO $t\bar{t}$ pair production : effects on new physics searches

- ▶ Light third generation squarks compatible with naturalness. Stealth stops  $m_{\tilde{t}} \lesssim 220$  GeV not yet ruled out
- ▶ Identical signatures to  $t\bar{t}$ . Stop contamination  $\approx 15\%$  for identical mass.
- ▶ Preliminary results by A. Mitov. Top pairs @ NNLO required, NLO uncertainties just too big!
- ▶ Assumes identical stop-top acceptances. More detailed analysis ongoing work

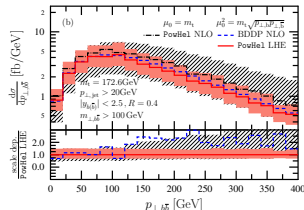
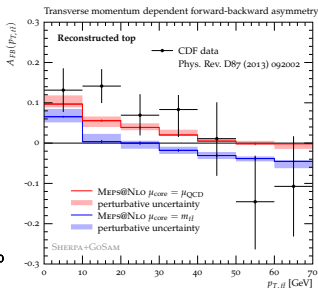
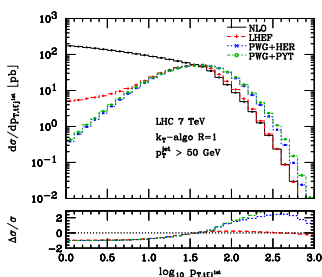
Czakon, Mitov, Papucci, Ruderman,

Weiler



# Monte Carlo for $t\bar{t}$ pair and $t\bar{t}$ + jets

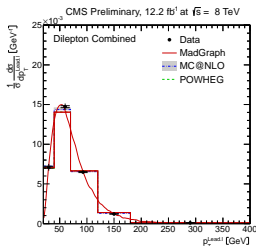
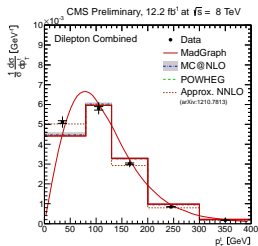
- Fully differential calculation of  $t\bar{t}$  + up to 2 jets, also  $t\bar{t}b\bar{b}$  Dittmaier, P. Uwer, S. Weinzierl '07  
Bevilacqua et al. '08-'11
- NLO production + NLO top decay with full spin correlations in zero width approx.  
Also finite  $\Gamma_t$  and interference effects  $W+W-b\bar{b}$  Melnikov, Scharf, Schulze '09-'11, Campbell, Ellis '12  
Bredenstein et al. '09-'12
- Interference and finite-width effects small on inclusive quantities, but greatly affects tails of distribution (important for mass extraction).
- NLO matched to parton showers POWHEG, POWHEL, aMC@NLO, GOSAM+SHERPA:  $t\bar{t}, t\bar{t} + 1\text{jet}$  and merged sample,  $t\bar{t}b\bar{b}$  Frixione, Nason, Ridolfi '08, SA, Moch, Uwer '11  
Garzelli, Kardos, Papadopoulos, Trocsanyi '11-'13  
Frederix, Frixione '12, Hoeche et al. '13



- Reminder: NLO merging is a tricky business! Fixed order  $O(\alpha_s)$  does not automatically mean “next-to-leading accuracy” right. Higher-order logs might spoil it.

# Resummation

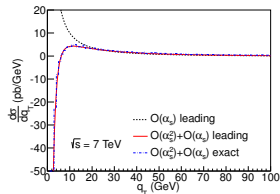
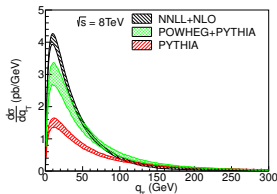
- ▶ MonteCarlos seems to have some problems with reconstructed tops. Better with decay products.
- ▶ Approx. NNLO results based on NNLL 1PI resummation seems in good agreement



- ▶ What about  $p_{T,t\bar{t}}$ ?  
CSS formalism good for Drell-Yan, Higgs,  $VV$ . Not so good with colored objects.  
 $k_T$ -factorization breaks down explicitly in di-jet.

- ▶ New framework for  $q_T$  resummation based on SCET presented for  $t\bar{t}$  Zhu, Li, Shao, Yang '13

- ▶ Based on Becher, Neubert, Wilhelm '12 with transverse soft function matrix. Use TMD pdf matched to ordinary pdf via beam functions and NP input. Resummation up to NNLL performed. Potential for alternative complete NNLO





# Fully exclusive NNLO top-quark decay

- ▶ Previous NNLO decay rate via optical theorem
  - ▶ Now 2 fully differential calculations available
- 1) IR subtractions via PS slicing and subtraction à la

Key idea:  $d\sigma_{NNLO}^X|_{q_T \neq 0} \equiv d\sigma_{NLO}^{X+j}|_{q_T \neq 0} +$   
singular behaviour at  $q_T \rightarrow 0$  known from resum.

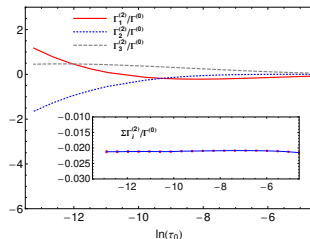
$$\Gamma_t^{NNLO} = \int_0^{\tau_0} d\tau \frac{d\Gamma_t}{d\tau} + \int_{\tau_0}^{\tau_{\max}} d\tau \frac{d\Gamma_t}{d\tau}$$

- $\tau < \tau_0$  exact results from SCET factorization
- $\tau > \tau_0$  exact results from NLO  $t \rightarrow bW^+j$

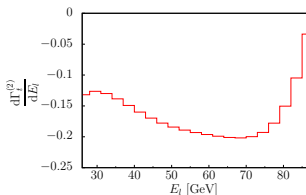
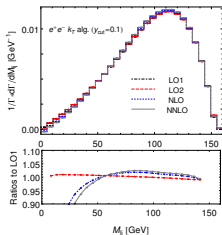
Czarnecki, Melnikov '99, Chetyrkin et al. '99

Gao, Li, Zhu '12, Brucherseifer, Caola, Melnikov '13

Catani, Grazzini '08



- 2) Sector-decomposition improved FKS subtraction.



- ▶ Everything now available for NWA prod.+decay@NNLO

# Electroweak effects and Sudakov logs

- Inclusive NLO EW corrections small  $\lesssim 1.5\%$

Beenakker et al. Hollik et al. '07, Kuhn et al. '07-'13

- But sizeable  $\gtrsim 10\%$  effects from EW Sudakov

$$\log\left(\frac{\alpha}{\sin^2\theta_W}\right)^n \log^{m \leq 2n}\left(\frac{s}{M_{W,Z}^2}\right) \text{ on}$$

high-energy tail of  $d\sigma/dM_{t\bar{t}}$  Manohar, Trott '12

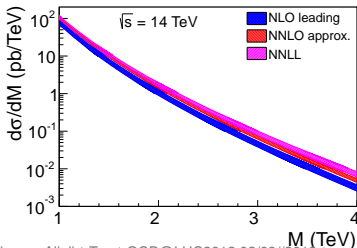
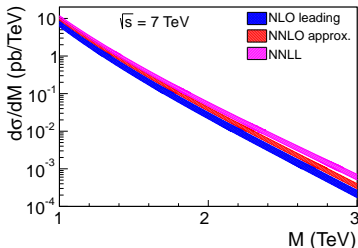
- Unlike QCD ones, don't cancel for inclusive quantities, because partonic processes are not EW singlets.

- These SM effects are unaccounted for in current Monte Carlo (few resums QED coll. logs only)

- Reminder: large  $M_{t\bar{t}}$  region also very sensitive to QCD soft  $1 - M^2/S$  logs. Marked differences for NLO, NNLL and approx. NNLO results ( $m_t \ll M$ ) Ferrogli et al. '13

Bin [GeV]	$\mathcal{R}_t$		$\mathcal{R}_b$		$\mathcal{R}_c$	
[50, 3000]	—	—	0.99	0.99	0.99	0.99
[350, 3000]	0.97	0.97	—	—	—	—
[50, 250]	—	—	0.99	0.99	0.99	0.99
[250, 500]	—	—	1.00	1.00	1.00	1.00
[350, 500]	0.98	0.98	—	—	—	—
[500, 750]	0.97	0.97	0.99	0.99	0.99	0.99
[750, 1000]	0.95	0.95	0.98	0.98	0.98	0.98
[1000, 1500]	0.94	0.94	0.97	0.97	0.96	0.96
[1500, 2000]	0.92	0.92	0.95	0.95	0.95	0.95
[2000, 2500]	0.90	0.91	0.93	0.94	0.93	0.93
[2500, 3000]	0.88	0.89	0.92	0.93	0.92	0.92
[3000, 3500]	0.87	0.88	0.90	0.91	0.91	0.91

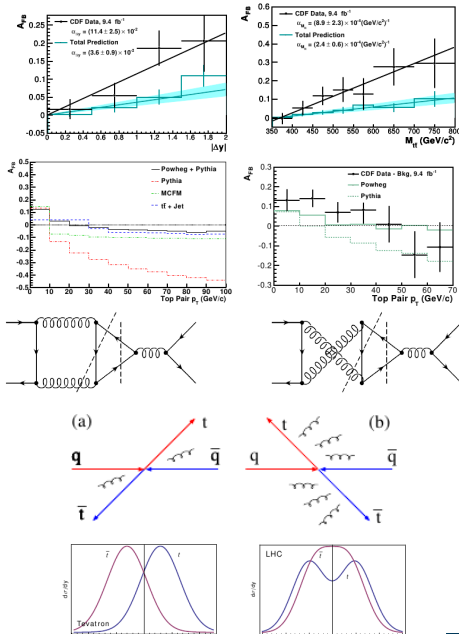
TABLE III: The EWS corrections for heavy quark production at the LHC. The left (right) columns are for  $\sqrt{s} = 7$  (14) TeV.



# $t\bar{t}$ forward-backward and charge asymmetry

Some facts:

- ▶ CDF measured a  $t\bar{t}$  charge (FB) asymmetry  $2 - 3\sigma$  larger than SM
- ▶ Marked dependence on  $\Delta y$ ,  $m_{t\bar{t}}$  and  $p_{T,t\bar{t}}$
- ▶ No contribution from  $gg$ , no from  $q\bar{q}$  at LO.
- ▶ Largest contribution from NLO  $q\bar{q}$  ( $> 0$  from virt.  $< 0$  from reals) Kuhn, Rodrigo '98-'11
- ▶ EW NLO effects calculated. Not small, but not enough Hollik, Pagani '11
- ▶ Coherence effects in parton showers generate supplemental asymmetry Webber, Skands, Winter '12
- ▶ Resummation/merging NLO samples seems to slightly reduce disagreement Li et al. '13, Hoche et al. '13
- ▶ Many BSM models crashed when tried to explain all the features
- ▶ Large difference from TEV to LHC, must include  $y$  cuts of measure charge asym. directly

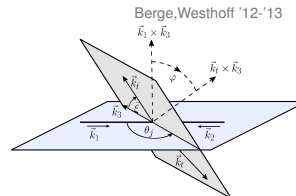


# Asymmetries with a jet handle

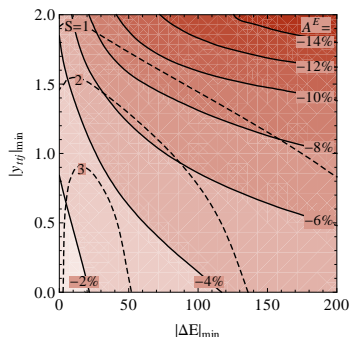
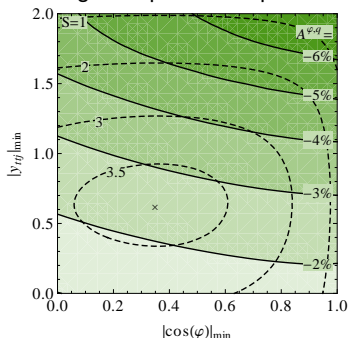
- New observables enhance charge asymmetries at LHC

$$\frac{d\hat{\sigma}_A(q\bar{q} \rightarrow t\bar{t}j)}{d\varphi d\theta_j dE_t dE_{\bar{t}}} = - [N_1 + \sin^2 \theta_j (N_1^j + \cos^2 \varphi N_1^\varphi)] \cos \varphi \quad \leftarrow \text{Incline Asymmetry}$$

$$+ [\underline{N_2} + \cos^2 \varphi \underline{N_2^\varphi}] \sin \theta_j \cos \theta_j \quad \leftarrow \text{Energy Asymmetry}$$



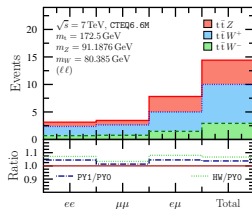
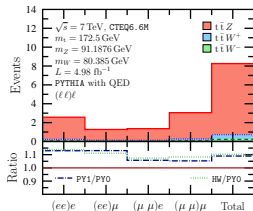
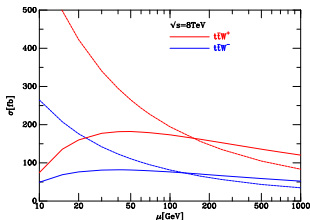
- Incline asymmetry is a refined rapidity asym. ( $\equiv$  at  $y = 0$ ), probes mostly  $q\bar{q}$ . Energy asym. probes only  $qg$ , not yet explored
- Together probe complementary contributions wrt to  $t\bar{t}$



# Top - antitop plus boson associated production

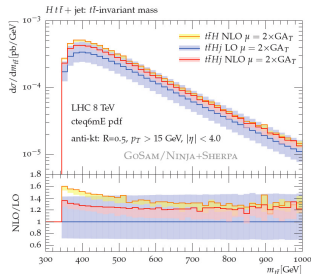
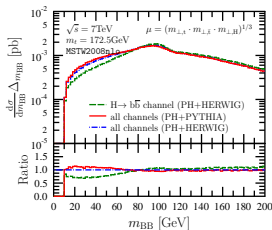
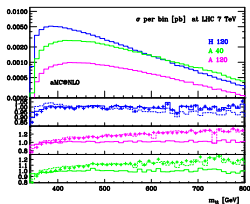
- Vector bosons:  $ttV$   $V = \gamma, W^\pm, Z$

Campbell, Ellis '12, Melnikov et al. '11, Garzelli et al. '11  
Peng-Fei et al. '09, Lazopoulos et al. '08



- (Pseudo-) scalar Higgs  $ttH, ttA$ . probe  $tH$  coupl., NP

Garzelli et al.'11, Frederix et al. '11



- Remarkable new result :  $ttH + 1 \text{ jet}$

Van Deurzen et al. '13  
Simone Alioli

# Single top production

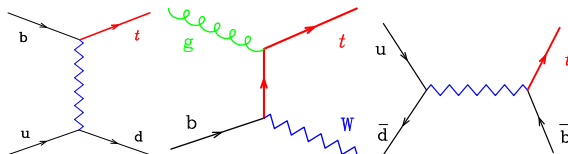
- Three production channels

$$\sigma_{t-ch} \approx 88 \text{ pb},$$

$$\sigma_{Wt} \approx 22 \text{ pb},$$

$$\sigma_{s-ch} \approx 6 \text{ pb}$$

at 8 TeV LHC.

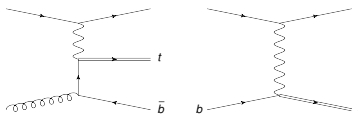


- Allows direct determination of  $V_{tb}$  and probes  $b$  PDF

$t$ -channel

4F:  $b$  from  $g \rightarrow b\bar{b}$

5F:  $b$  inside proton



Harries et al. '02, Campbell, Ellis, Tramontano '04  
 Frixione et al. '05, SA, Nason et al. '09  
 Campbell et al. '09, Schwienhorst et al. '10  
 Frederix, Re, Torrielli '12

- Known at NLO +PS in 4F and 5F schemes, matched to shower in POWHEG and MC@NLO

- Finite-width and non-resonant effects included

Falgari et al. '10-'13, Papanastasiou et al. '13

- NLO Single top production in association with a Z boson  $\sigma_{Zt} \approx 160 \text{ fb}$

Campbell, Ellis,

Röntscher '13

- Also NLO  $tZ$  and  $t\gamma$  with FCFN

Zhang, Li, Gao, Zhu '10-'11

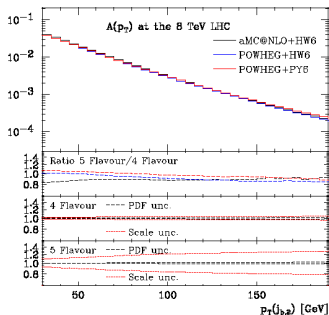
- Resummation to NNLL and approximate NNLO available

Kidonakis '10, Wang, Li, Zhu, Zhang '10

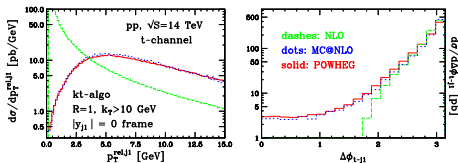
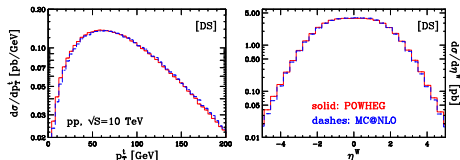


# NLO Monte Carlo for single top production

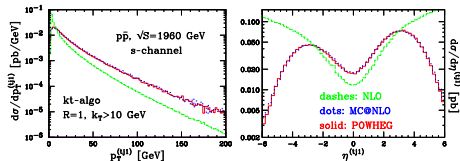
## ► $t$ -channel: 4F vs. 5F scheme



## ► $Wt$ -channel, ambiguities in NLO contribution due to $t\bar{t}$ interference

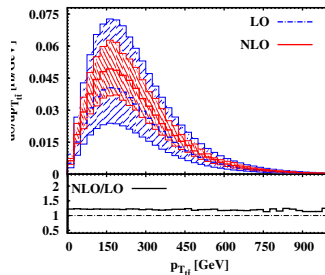
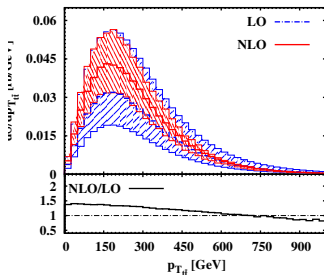
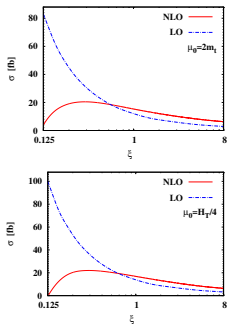


## ► $s$ -channel



# Four tops: $t\bar{t}t\bar{t}$

- ▶ Results recently available. Last one on Les Houches wishlist. Bevilacqua, Worek '12
- ▶ Important background to many NP searches: Heavy Higgs,  $Z'$ , KK, Higgs & Top compositeness, effective 4-tops vtx
- ▶ Small but important x-sec  $\approx 17$  fb at LHC14. Comparable to NP at  $m_{\text{new}} = 1.5$  TeV
- ▶ NLO inc. corrections  $\approx 25\%$ .
- ▶ Multiscale process: fixed  $\mu = 2m_t$  vs. dyn scale  $\mu = H_T/4$  matters for distributions

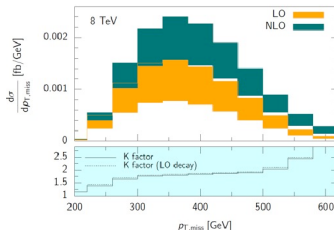
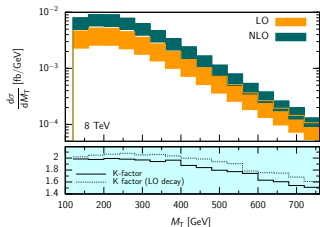




# BSM top partners

- ▶ Top largest contribution to Higgs mass correction. Several BSM models introduces top-partners to tame quadratic divergences.
- ▶ MSSM naturalness prefers light top-partners + heavier colored superpartners.
- ▶ MSSM stops NLO predictions by PROSPINO only give flat  $K$ -factors. This is usually used in searches.
- ▶ NLO calculations for  $t\bar{t} \rightarrow t\bar{t}\chi\bar{\chi} + X$  shows sizeable kinematics dependence. Also fermionic  $T\bar{T} \rightarrow t\bar{t}A_0A_0 + X$  in Little-Higgs with  $T$ -parity

Schulze,Boughezal '13



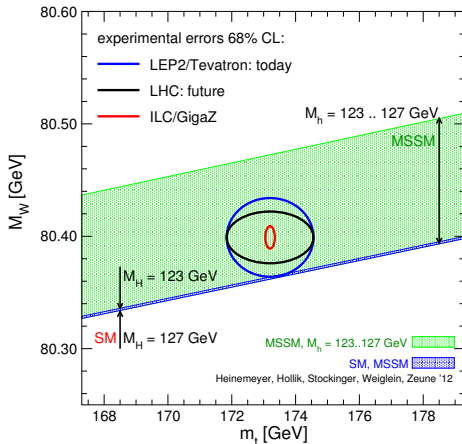
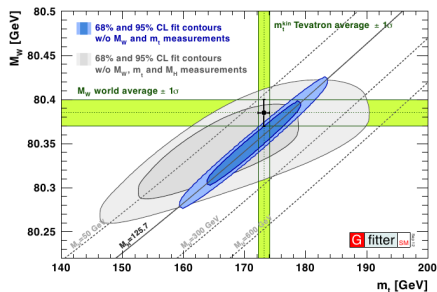
- ▶ NLO+NLL resummation for  $t\bar{t}$  available
- ▶ Approximate NNLO predictions recently
- ▶ NLO+PS not yet available

Beenakker et al. '12-'13

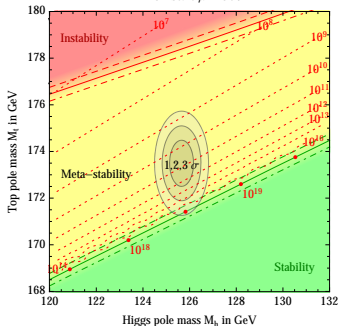
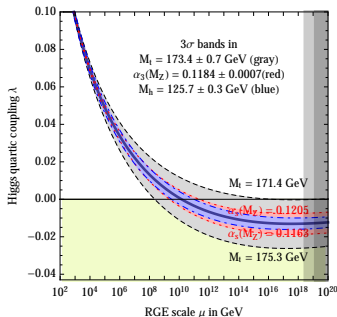
Broggio et al. '13

# Motivations for precise $m_t$ measurements

- ▶ The top is the only quark that decays before hadronization: unique opportunity to study a quasi-free quark.
- ▶ The top sector might play an important role in EWSB
- ▶ Its mass is a fundamental parameter of SM Lagrangian
- ▶ Important parameter in SM (and MSSM) fits, although not limiting factor



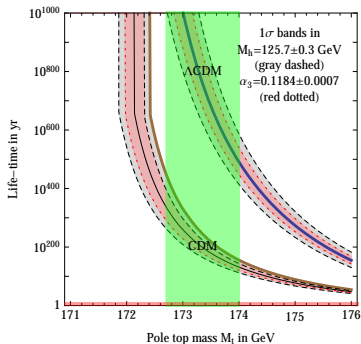
# Motivations for precise $m_t$ measurements



- Sub-GeV accuracy crucial for vacuum (meta-)stability of SM at NNLO and the fate of the universe

Buttazzo et al. '13

DeGrassi et al. '12, Alekhin, Djouadi, Moch '12



- Cosmological Higgs-driven inflation models compatible with Planck data

Bezrukov, Shaposhnikov '07-'08, De Simone, Hertzberg, Wilczek '08

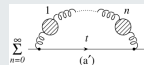
# Theoretical issues in determination of the top-quark mass

- ▶ Confinement = free quarks not observable = no pole in the S-matrix
- ▶ Parameters of the theory measured through their influence on hadronic observables: fit  $\mathcal{O}^{\text{exp}}(\vec{x})$  with  $\mathcal{O}^{\text{th}}(m_t, \vec{x})$  and extract  $m_t$

Which mass are we measuring ? At least NLO required to fix the ren. scheme.

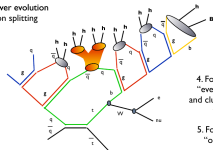
- ▶ Precise value depends on the  $m_t$  definition:  $m_t^{\text{pole}}$ ,  $m_t^{\overline{\text{MS}}}$ , etc.

Which scheme ? Some show better convergence (e.g.  $m_t^{\overline{\text{MS}}}$ ), some ill-defined beyond PT (IR renormalons  $\Delta_{m_t^{\text{pole}}} \propto \Lambda_{QCD}$ )



## ▶ Color reconnections

1. Hard Process
2. Shower evolution
3. Gluon splitting



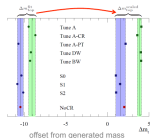
4. Formation of "even" clusters and cluster decay to hadrons
5. Formation of "odd" cluster
6. Decay of "odd" clusters, if large cluster mass, and decays to hadrons

From M. Mangano

## Non-perturbative effects at the LHC

[Skands, Wickens 08]

Simulate top mass measurement using different models/tunes for non-perturbative physics / colour reconnection



different offset for different tunes!

Non-perturbative effects result in uncertainty of the order of 500 MeV

blue: pt-ordered PS  
green: virtually ordered PS

- ▶ Current experimental precision at 0.5% impressive. Theoretical interpretation not so well under control.

# (Some) top-quark mass measurements at hadron colliders

## ▶ Template method - Ideogram method

✗  $m_t^{MC} = m_t^{\text{pole}}(1 \pm \Delta), \Delta = ? , \text{LO}$

✓ high-precision

## ▶ Matrix element method

✗ LO only, NLO under develop. ✓

✓ high-precision

## ▶ Cross section

✓ theoretically clean, NNLO, finite  $\Gamma_t$

✗ reduced sensitivity, threshold eff. included

## ▶ $J/\psi$ method: $t \rightarrow (b \rightarrow (J/\psi \rightarrow \mu^+ \mu^-) + X) + (W^+ \rightarrow \ell^+ \nu_\ell)$

✓ NLO, small sensitivity to JES unc. and top reco.

✗ finite  $\Gamma_t$ , very-high statistics required

## ▶ Dilepton-specific distributions

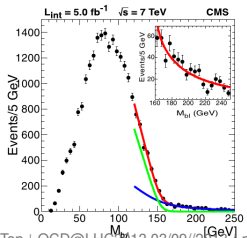
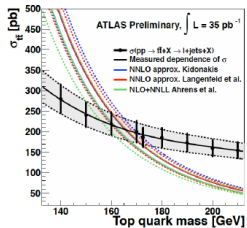
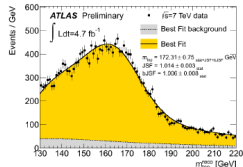
✓ NLO, JES unc., top reco., finite  $\Gamma_t$

✗ reduced sensitivity, high statistics required

## ▶ Kinematic endpoint: $\max(M_{bl})$ and $m_t$ strongly correlated

✓ NLO (but not yet) , small sensitivity to top reco.

✗ strong dep. on JES, finite  $\Gamma_t$

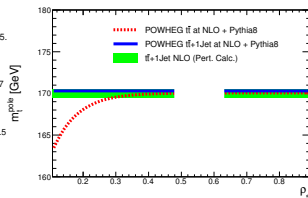
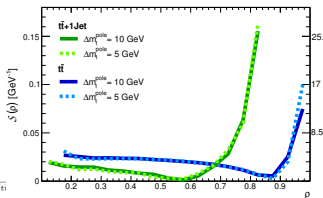
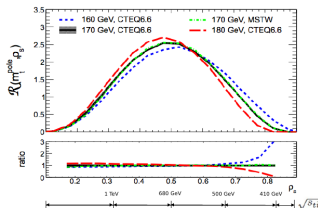


# New proposal: top-mass from jet rates

- ▶ Study  $t\bar{t} + 1\text{-jet}$  events : large rate at the LHC ( $\gtrsim 30\% - 50\%$ ), NLO and NLO+PS available  
SA, Fernandez et al., see A.Irles' talk
- ▶ Experimentally accessible, errors reduced through normalization factor

$$\mathcal{R}(m_t^{\text{pole}}, \rho_s) = \frac{1}{\sigma_{t\bar{t}+1\text{-jet}}} \frac{d\sigma_{t\bar{t}+1\text{-jet}}}{d\rho_s}(m_t^{\text{pole}}, \rho_s), \quad \rho_s = \frac{2m_0}{\sqrt{s_{t\bar{t}j}}}, \quad m_0 = 170 \text{ GeV}$$

- ▶ Theoretically well defined, calculable at NLO, small uncertainties and small NP corrections,  $\overline{\text{MS}}$  mass extraction also feasible from  $\mathcal{R}(m_t^{\overline{\text{MS}}}, \rho_s)$ .



- ▶ Enhanced sensitivity (x5), potential for  $\lesssim 1 \text{ GeV}$  theo+exp combined accuracy. Room for improvement with detector specific tools.
- ▶ Several methods availables for NLO top mass, important to take advantage of all of them, with a look on the theory side.

# Conclusions

- ▶ Total x-sec. for  $t\bar{t}$  production now known at NNLO+NNLL. Theory unc. from scales, pdf,  $\alpha_s$ ,  $m_t$  of small similar size. High-precision test of SM.
- ▶ Lesson learned: precision pays back! Important phenomenology, improve constraints on PDF's and limits on BSM searches.
- ▶ Monte Carlo tools available fares fairly well with current data.
- ▶ Electroweak Sudakov logarithms becomes increasingly important raising energy.
- ▶ Single top also in good shape (NLO+PS, NNLL resum. approx. NNLO). Complete NNLO might not be in the too far future.
- ▶ Various associated production processes known at NLO + PS
- ▶ CDF  $t\bar{t}$  asymmetry discrepancy slightly reduced but still not satisfactorially explained.
- ▶ New observables proposed for the LHC might help shed some light.
- ▶ Top-mass precision  $< 1$  GeV is important and has tremendous consequences ...
- ▶ Theoretically unambiguous top-mass definitions should be used whenever possible

***Thank you for your attention!***

