

$$\operatorname{Res}_{s=1} E^{\star}(s; \tau) = \frac{1}{2}$$