

$$S_{1d} = \int dr \sum_{\alpha} \left(\phi'_{\alpha} - f_{\alpha}(\phi) \right)^2 + \text{total derivative}$$