

$$ds^2 = \tilde{r}^{-1} \left(-\tilde{r}^2 dt^2 + \tilde{r}^{-2} d\tilde{r}^2 + \tilde{r}^2 d\vec{x}^2 \right)$$