

$$ds^2 = \frac{dr^2}{r^2 f} + r^2 (-f dt^2 + d\vec{x}^2)$$