

GPGPU projects in Wuppertal

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Thijs Cornelissen, Sebastian Fleischmann, Peter Maettig, Manuel Neumann

Bergische Universität Wuppertal

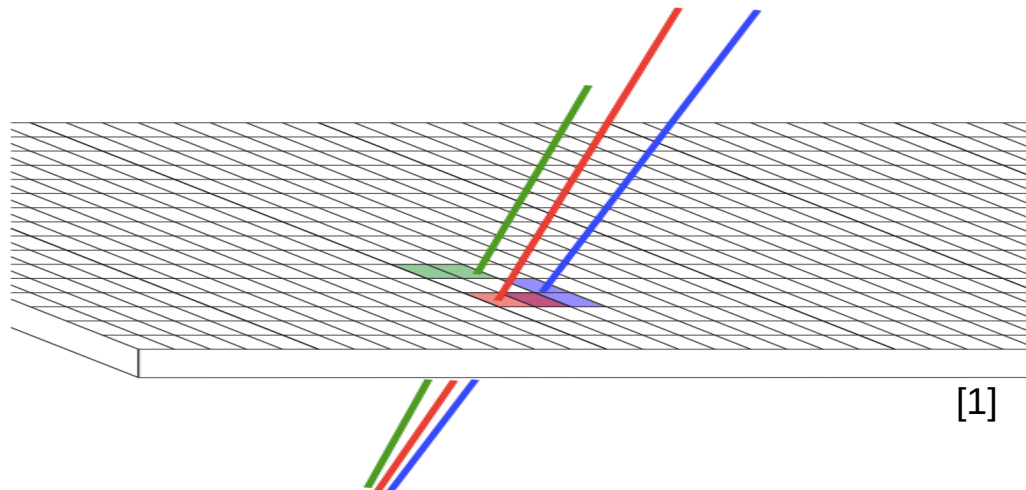


Projects for GPGPU processing

- Overall goal: Gain experience in parallelisation of algorithms in ATLAS offline reconstruction
- **1st Project:** Cluster splitting with neural networks
 - NN implementation in Toolkit for Multivariate data Analysis ([TMVA](#), [0]) on GPUs
 - Collaboration with FH Niederrhein (P. Ueberholz)
 - Preparation of measured data as input for track reconstruction
- **2nd Project:** Track fitting
 - Collaboration with FH Muenster (N. Wulff)
 - Fit track seeds to measurements
 - Multi Track Fitter
 - Kalman filter
 - Global X^2 fitter

1st Project: Cluster Splitting using neural networks

- Close by particles leave charge clusters in pixel detector that may overlap
- Previous cluster seeking method did not solve the issue of accidentally merged clusters
- Merged clusters will reduce tracking performance
 - Too many shared measurements will lead to rejection of tracks
 - Resolution decreases due to less precise reconstructed objects
- New approach uses charge distribution to split clusters according to estimated track count
- A neural networks calculates probability that a cluster is caused by multiple particles

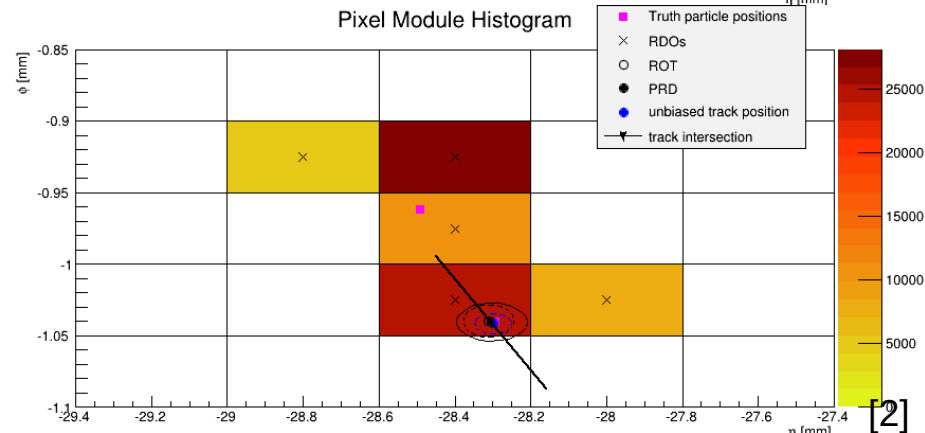
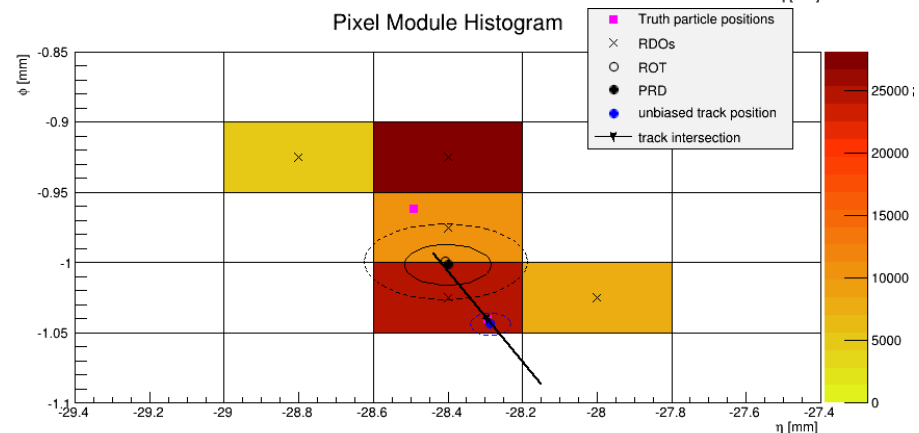
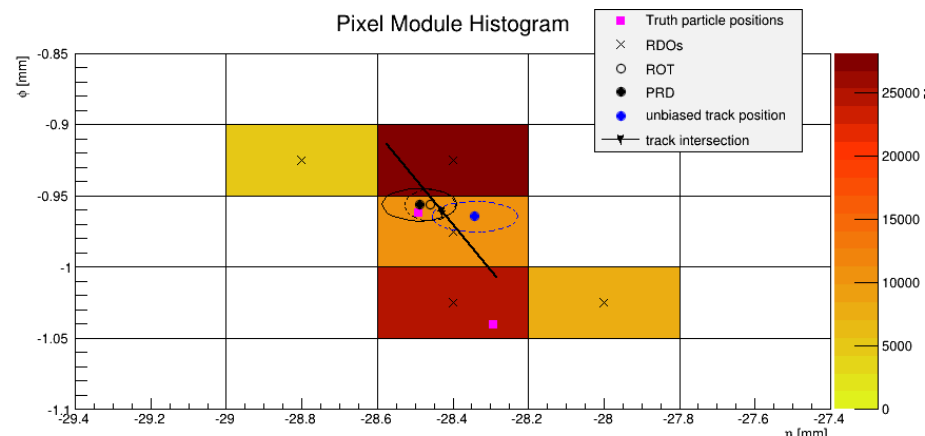
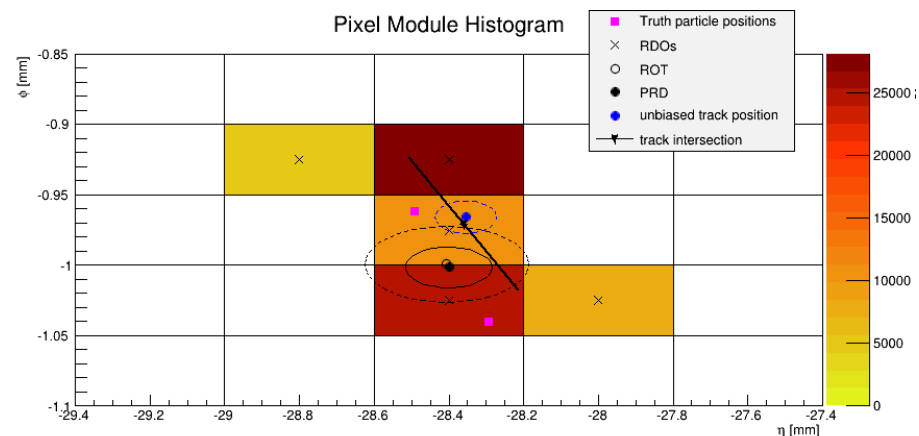


New cluster splitting

- Uses charge information of single pixels in cluster
 - Estimate number of passing tracks of cluster
 - “ position of each track
 - “ uncertainty of measurement
- Inputs:
 - 7x7 pixel information centred using charge weights
 - Longitudinal length of pixel cell
 - Estimated track direction (angle to surface normal)
- Multi Layer Perceptron (MLP) with
 - 3 output nodes (1 for each number of tracks)
 - about 60 input variables
- Try to use GPUs for network training
 - Parallelise weight calculation
 - Train different networks in parallel
 - Starting from GPU-based (CUDA) MLP implementation in TMVA from Edinburgh [\[SOURCE\]](#)
 - Extension to multiple output nodes
 - Rewrite in OpenCL

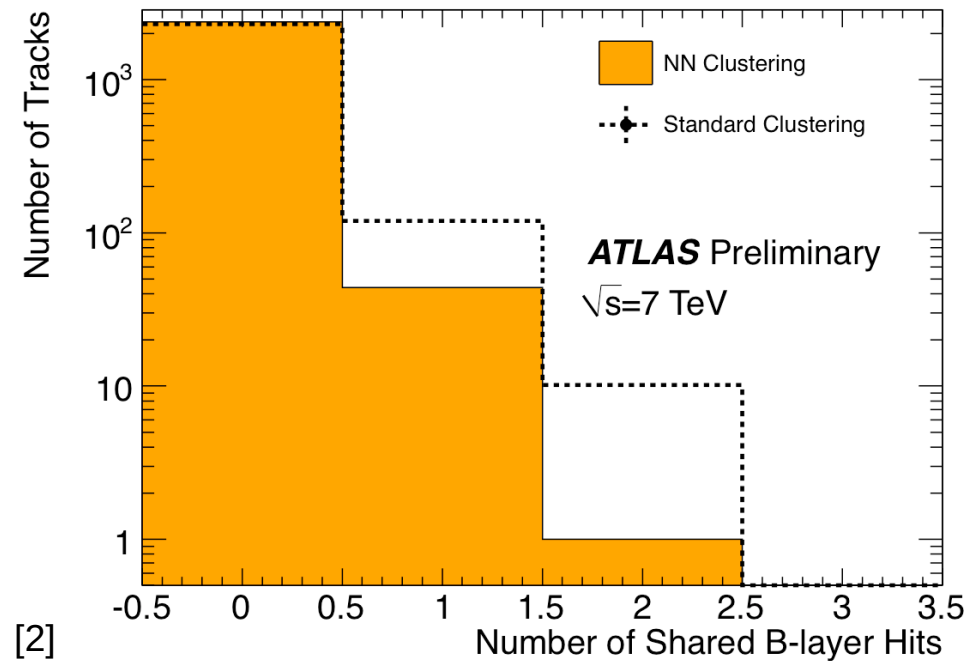
Cluster splitting performance (I)

- Compare old (left) to new (right) clustering:
 - Reconstructed objects (black dots at $\Phi=-1$) give intermediate and therefore worse input for track reconstruction
 - New approach separates the hits and with this increases resolution for track reconstruction



Cluster Cluster splitting performance (II)

- Shared measurements in the innermost pixel detector layer
 - Dashed line shows old clustering
 - Orange filled area NN approach
- Clearly the tracks share less hits
 - Results in better track resolution
 - Less tracks will be rejected



[2]

Preliminary results from GPU implementation

- Implementation of the NN that estimates the number of particles (3 outputs nodes)
- Serial CPU only vs. CUDA
- CUDA implementation lacks static input nodes (bias)
- Physical results **not** checked, yet
- Large net: 95604 events
 - 61 input variables
 - 64 neurons and 4160 synapses
 - 3 output nodes
- Small net: 6k events
 - 4 input variables
 - 19 neurons and 45 synapses
 - 1 output node

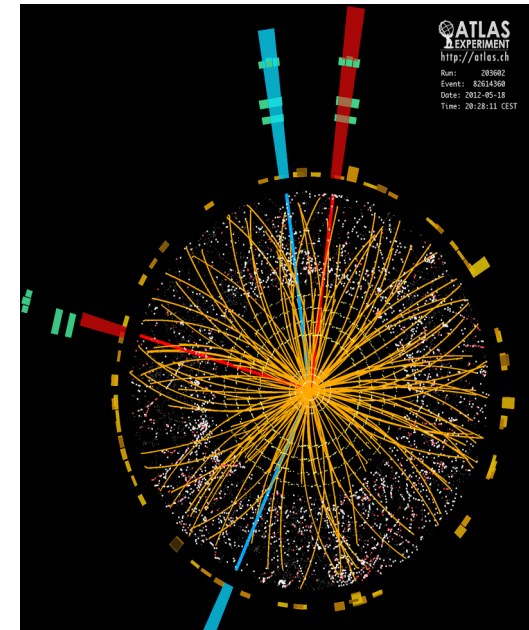
	GeForce GTX 570	Intel Core i7-2600s
Clock rate [GHz]	1.464	2.8 (3.8)
Memory Bandwidth [GB/sec]	152	21
Cores [int]	480	4 (HT)

Training time for different nets

	Large net	Small net
MLP	14.97 h	14.3 s
MLP (CUDA)	24.3 m	87.2 s

2nd Project: Track fitting issues

- Number of tracks $O(1000)$ per event
 - Current framework fits tracks one by one
- Combinatorics in measurement assignment
 - Finding **track seeds**: see talk of J. Mattmann (here I deal only with **fitting of tracks**)
 - Ambiguity solving during fit (shared measurements, duplicate/ghost seeds)
- Track fitting takes around 18 % CPU time of the reconstruction process
 - Needs precise geometry and magnetic field map
 - High fraction for solving ambiguities
 - Standard fitter (GlobalChi2Fitter) deals with matrices of $O(50 \times 50)$



Update track fitting algorithms

● Goals

- reduce computing time
- More efficient usage of current and future hardware
- Improve physics performance in dense track environments (boosted jets)

● Ideas

- Fit many tracks at once
- Algorithm that solve measurement ambiguities intrinsically (see next slides)
- Use vector architectures

● Boundary Conditions

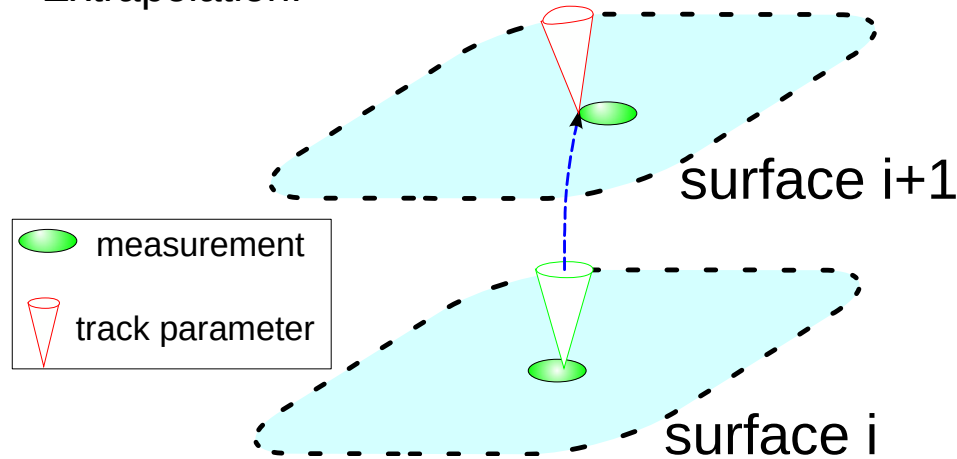
- Track fitting needs precise detector geometry and magnetic field information
- No port of whole reconstruction framework (lack of manpower)

Basic tool: Kalman Filter

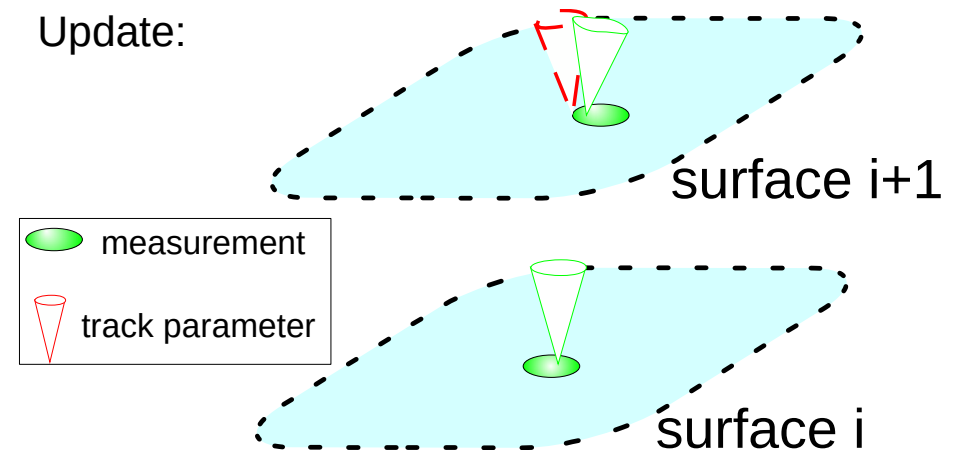
● Procedure

- Extrapolate track parameters to next surface
 - **Combine** track parameters with corresponding measurement
 - Extrapolate updated track parameters to next layers
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- Can be done inside out (fine to coarse detector) and vice versa
 - Iterative approach does not need full geometry information in every step

Extrapolation:



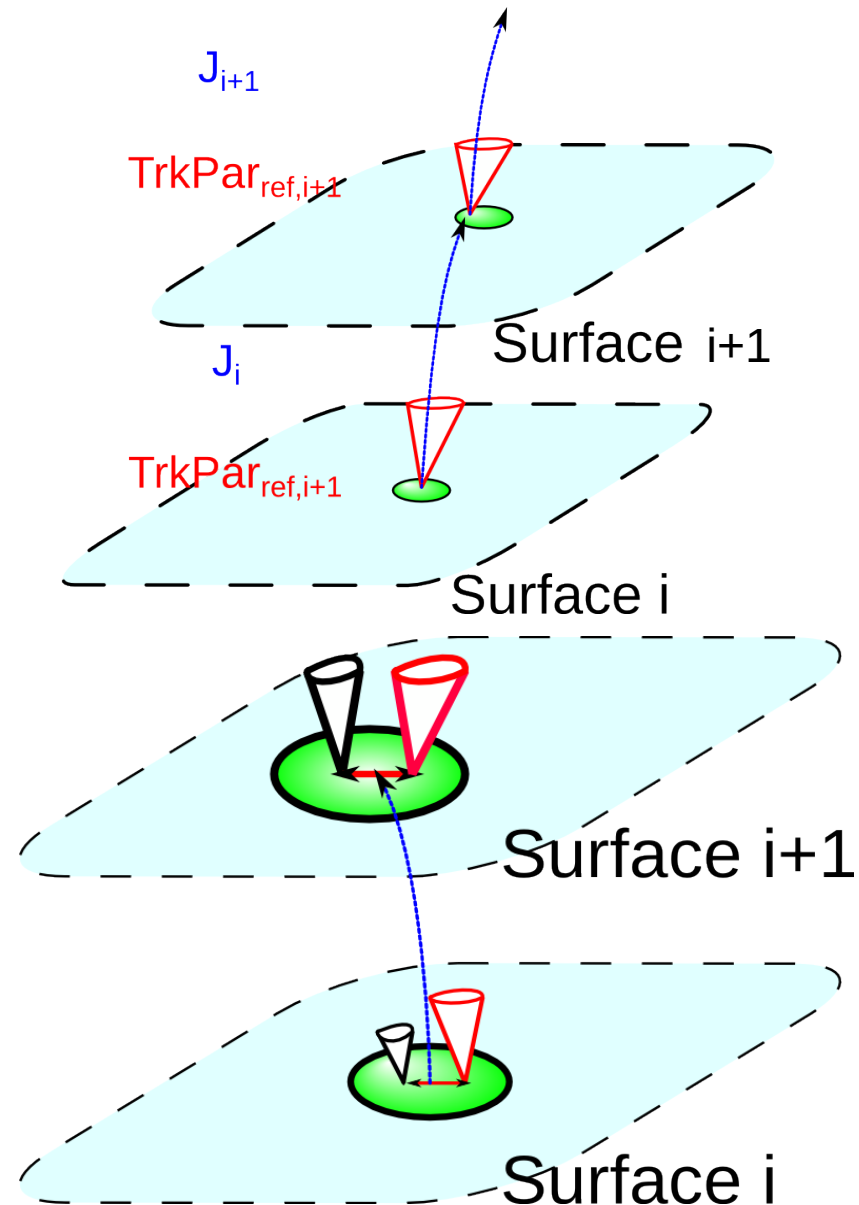
Update:



Reference fit method

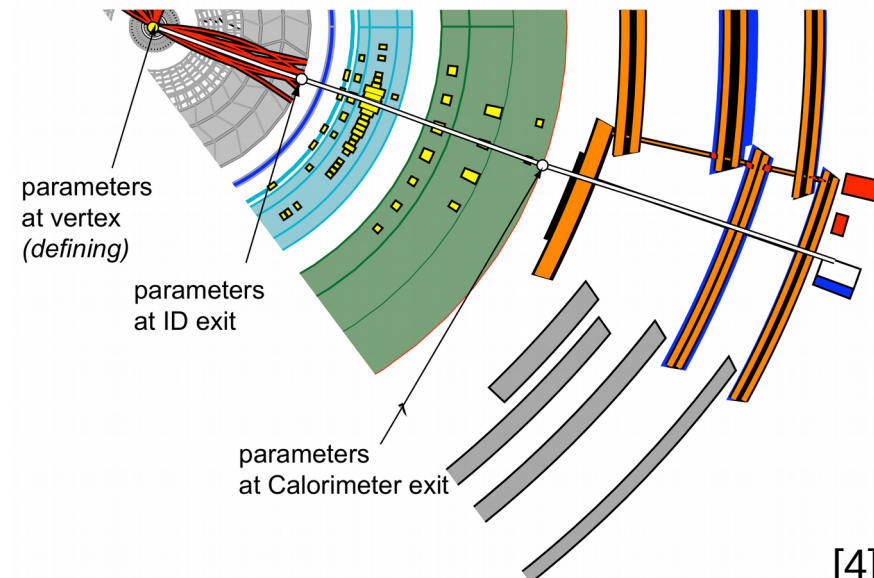
- Extension of the Kalman filter
- Linearisation around seed
- Initialisation:
 - Do a full Kalman fit without including the measurement parameters
 - Store transport Jacobian J matrices and track parameters $\text{TrkPar}_{\text{ref}}$ of this fit
- Fit:
 - Propagate difference of track parameters to measurement with the transport Jacobians

$$\Delta x_{i+1}^{\text{pred}} = J_i \Delta x_i$$
 - Correct prediction with measurement parameters



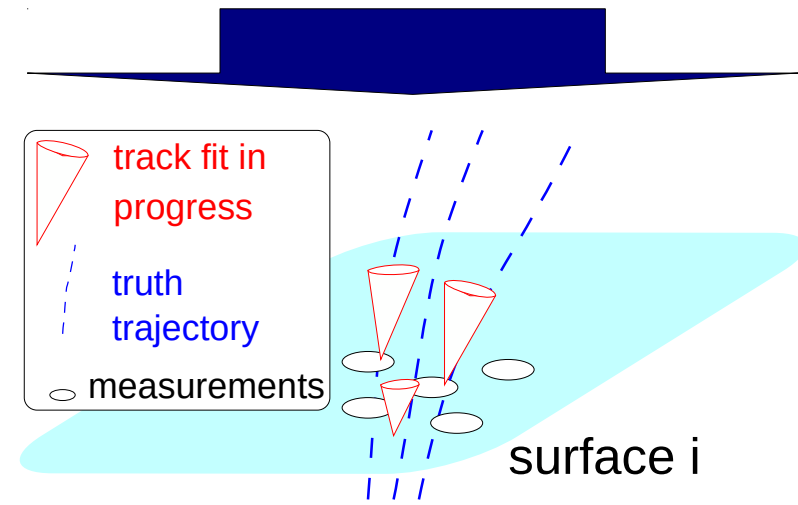
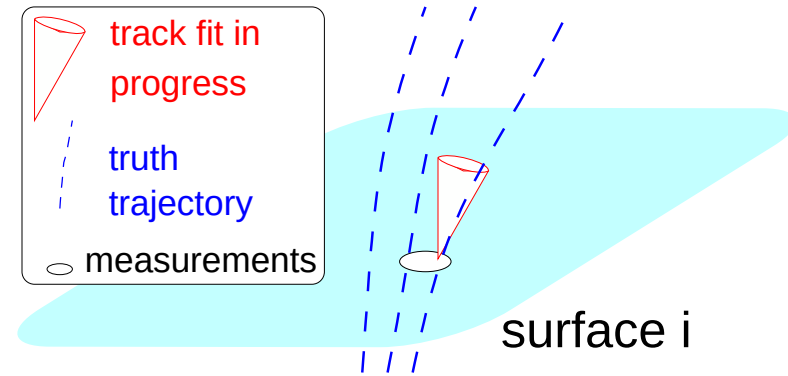
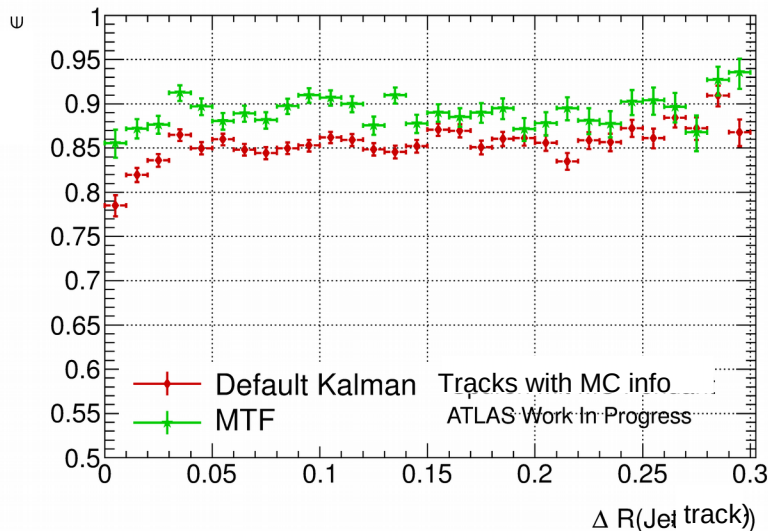
Reasons for the reference fit method

- Higher stability related to numerics and material effects
 - Special w.r.t. detector geometry and features
 - precise (ID) and coarse subsystems (muon spectrometer)
 - magnetic field
- no detector geometry after the first fit iteration needed
 - No database lookup in every iteration
- Matrix operations should be done fast on GPUs and SIMD units
- This allows data parallel (multiple tracks at once) processing



Multi Track Fitter

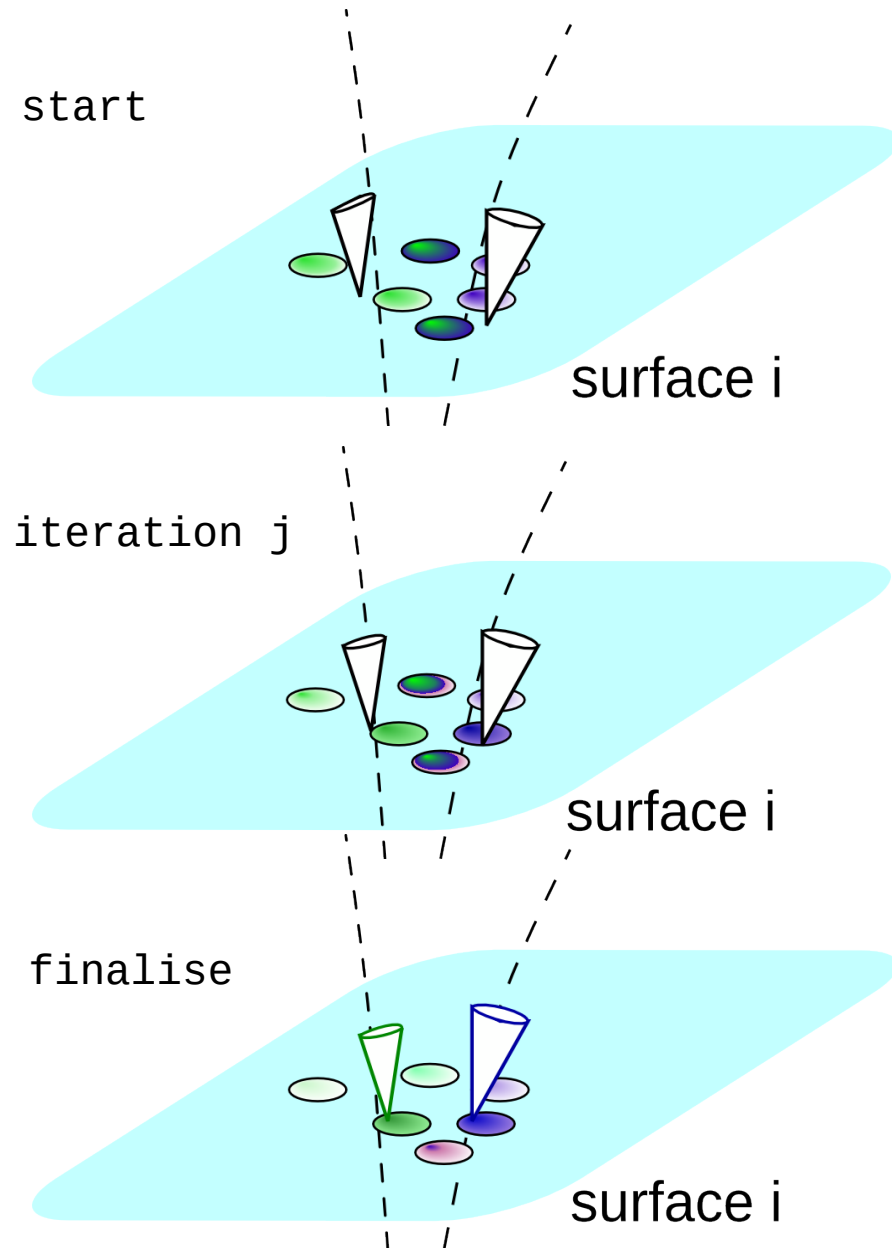
- Based on “adaptive multi track fitting” by A. Strandlie, R. Frühwirth [5]
- Idea:
 - Combine information of multiple track candidates
 - Loose assignment of measurements at the beginning of fit process
 - Inherent ambiguity processing of measurement to track assignment
 - Improve tracking performance inside jets



Multi Track Fitter - Principle

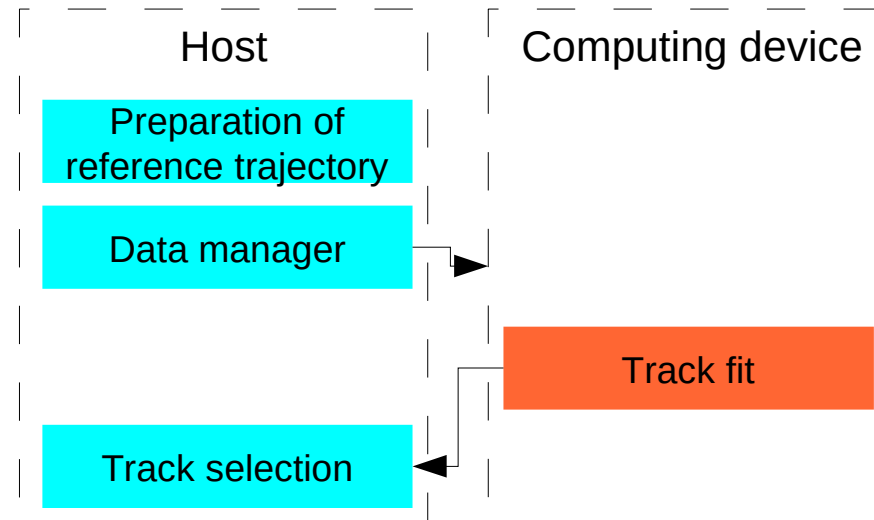
- Extension of the Kalman Filter:

- Assign a weight to every measurement for every considered track
- In every iteration of the MTF:
 - Decrease a temperature parameter that goes into the calculation of the weight (Low values for temperature cause a hard cut off)
 - Proceed with the Kalman filter
- Selection: In the last iteration a single measurement will be assigned to a track



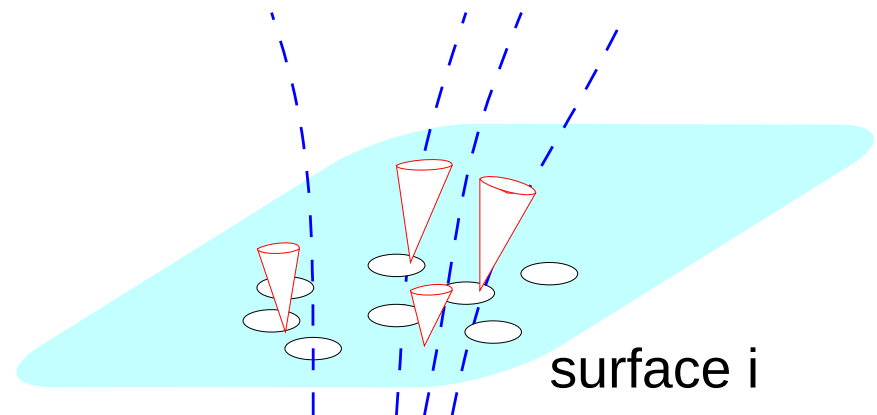
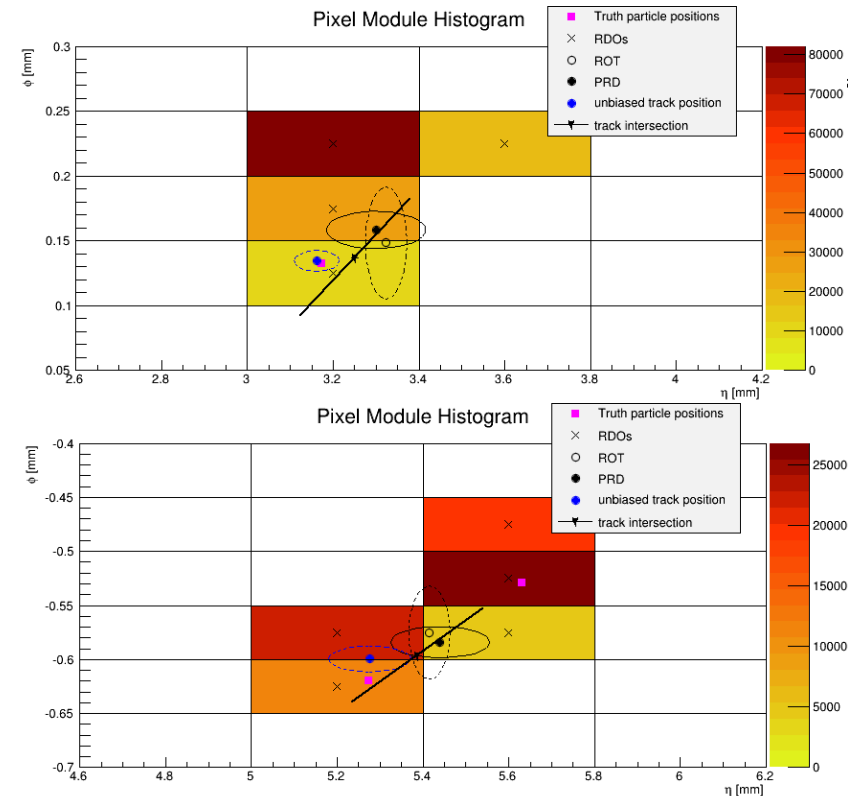
Multi Track Fitter – the whole package

- Use Kalman filter with reference method
- Fill reference trajectory and assignment weights at the beginning
- Transfer trajectories and track seeds to computing device
- Fit predictions to measurements
 - only updates present information
 - Mostly matrix/vector operations (suitable for SIMD/GPU computing units)
- Transfer back to host and do track selection



Summary

- Projects related to track reconstruction ongoing:
 - Neural networks to improve measurement information
 - Track fitter to gain from current (SIMD) and future (GPU) hardware
 - Will speed up fitting
 - Collaboration with FH Niederrhein/Muenster and Wuppertal's department of electrical engineering (CUDA Research Center)
 - Funding for GPU cluster (48 NVIDIA Tesla M2090 Modules) granted, but main user will be dept. of EE



Bibliography

- [0] Acceleration of multivariate analysis techniques in TMVA using GPUs
A. Hoecker, H. McKendrick, J. Therhaag, A. Washbrook
- [1] Neural network based cluster creation in the ATLAS silicon Pixel Detector, Andreazza, A., ATL-PHYS-SLIDE-2013-155, 2013
- [2] Neural network based cluster creation in the ATLAS Pixel Detector, Andreazza, A., ATL-PHYS-PROC-2012-240, 2012
- [3] Track Reconstruction in the ATLAS Experiment – the Deterministic Annealing Filter, Fleischmann, S., 2007
- [4] Artemis School on Calibration and performance of ATLAS detectors / ID reconstruction, Salzburger, A., 2008
- [5] Adaptive multitrack fitting, A. Strandlie, R. Frühwirth, Computer Physics Communications, Volume 133, Issue 1, p. 34-42.



Backu
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Kalman filter

- Prediction:

$$x_{i+1}^{pred} = F_i x_i$$

$$C_{i+1}^{pred} = F_i C_i F_i^T + Q_i$$

C: covariance,

x: track parameters,

F: model description

Q: material effects

- Update:

$$x_{i+1}^{upd} = x_i C_{i+1}^{upd} \left((C_{i+1}^{pred})^{-1} x_{i+1}^{pred} + H_{i+1}^T V_{i+1}^{-1} m_{i+1} \right)$$

$$(C_{i+1}^{upd})^{-1} = (C_{i+1}^{pred})^{-1} + H_{i+1}^T V_{i+1}^{-1} H_{i+1}$$

$$V = C^{-1},$$

m: measurement parameters,

H: translation between trk/measurment space

Reference method

- Prediction

$$\Delta x_{i+1}^{pred} = J_i \Delta x_i$$

$$\Delta x = x_{\text{trkpar}} - x_{\text{refpar}}$$

$$C_{i+1}^{pred} = J_i C_i^{ref} J_i^T + Q_i$$

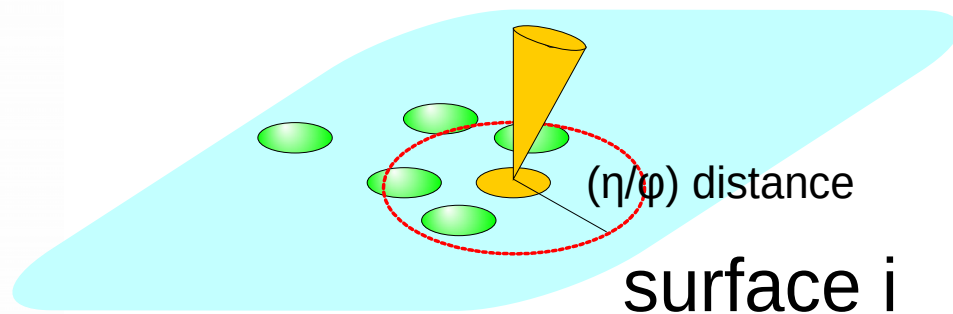
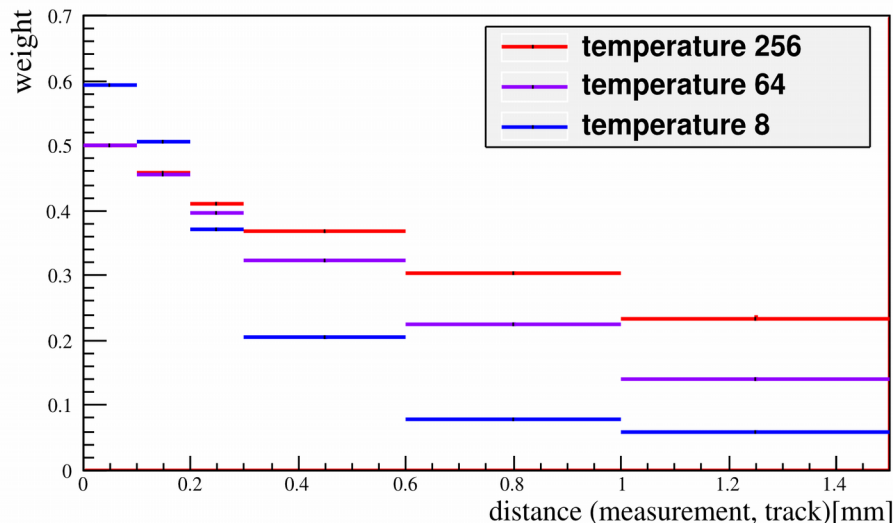
Optimisation

- Goal: Reduce fake rate while hold reconstruction efficiency high
- Problematic parameters of the MTF:
 - Temperature scheme
 - Road width of additional measurements (given by local distance between track and measurements)
 - $\max(\eta/\varphi)$ is the largest value for (η/φ) -distance

$$[T_0, T_1, \dots, T_N]$$

$$distance_{\eta} := \frac{|Trk :: loc \eta - cluster :: loc \eta|}{\sigma_{\eta}}$$

$$distance_{\varphi} := \frac{|Trk :: loc \varphi - cluster :: loc \varphi|}{\sigma_{\varphi}}$$



Proposed competing ROT mean values in the SCT

- New compROT mean:

$$m'_i = \left(p_a \frac{m_{a,x}}{\lambda_{a,1}} + p_b \frac{m_{b,x}}{\lambda_{b,1}} \right) \left(\frac{p_a}{\lambda_{a,1}} + \frac{p_b}{\lambda_{b,1}} \right)^{-1} \quad i \in x, y$$

$$V' = R V'' R^T$$

$$V'' = \begin{pmatrix} \frac{1}{p_a/\lambda_{a,1} + p_b/\lambda_{b,1}} & 0 \\ 0 & \frac{1}{p_a/\lambda_{a,2} + p_b/\lambda_{b,2}} \end{pmatrix}$$

$$R = \begin{pmatrix} \cos(\theta') & -\sin(\theta') \\ \sin(\theta') & \cos(\theta) \end{pmatrix}$$

- θ is the angle between the system of the covariance and the SCT module system

$$\theta = \frac{1}{2} \arctan \left(\frac{2\sigma_{xy}}{\sigma_x^2 - \sigma_y^2} \right)$$

- λ_j are the eigenvalues of the covariance matrices:

$$\lambda_{a,j} = \frac{\text{Tr}(V)}{2} \pm \sqrt{\frac{\text{Tr}(V)^2}{4} - (\sigma_x^2 \sigma_y^2 - \sigma_{xy}^2)}$$