

# Gauge Coupling Unification

## Constraints on String-derived Models



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1106.3082  
1106.5422

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# Nucleon Decay

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- Proton lifetime  $\tau_p \gtrsim 10^{34}$  years [1203.4030 [HEP-EX] SUPER KAMIOKANDE ]
- $B$  and  $L$  global symmetries in SM
- $\tau_p$  indicates cutoff  $\gtrsim 10^{16}$  GeV
- SUSY induces dimension-4 & -5 operators
- Suppressed/forbidden
  - R-symmetries [e.g. 1102.3595 [HEP-PH] RABY, RATZ, ROSS *et al*]
  - Gauged  $B - L$  [e.g. 1207.0507 [HEP-PH] BASSO, STAUB *et al*]
  - $B$  and  $L$  gauge groups [e.g. 1304.0576 [HEP-PH] WISE, PEREZ, DUERR]

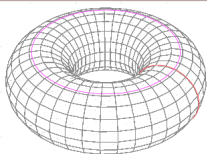
## Viability of $U(1)$

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- Dimension-4, -5, -6 proton decay mediating operators forbidden
- Seesaw mechanism for light neutrinos
- Yukawa couplings to EW Higgs doublets
- Family Universal
- Anomaly Free

# Free Fermionic Formulation

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- Fermion Phases

$$f \longrightarrow -e^{i\pi\alpha(f)} f, \quad \alpha(f) \in (-1, 1]$$

- ABK Rules
- Generalized GSO Projections
- $U(1)$  charges

$$Q(f) = \frac{1}{2}\alpha(f) + F(f)$$

- Corresponds to  $Z_2 \times Z_2$  orbifold

[e.g. HEP-TH/0403272 FARAGGI, DONAGI]

# Model Construction

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- NAHE set of basis vectors:  $\{\mathbf{1}, \mathbf{S}, \mathbf{b}_1, \mathbf{b}_2, \mathbf{b}_3\}$ 
  - $SO(10) \times SO(6)_{1,2,3} \times E_8$
  - 48 generations
  - $\mathcal{N} = 1$  SUSY
- Add  $\{\alpha, \beta, \gamma\}$ 
  - Preserves  $\mathcal{N} = 1$  SUSY
  - 3 generations
  - GG: subgroup  $\times U(1)^n \times$  hidden subgroup

## $SO(10)$ Breaking

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$$\begin{aligned} b \{ \bar{\psi}^{1, \dots, 5} \} &= \{ 11100 \} \\ &+ \\ b \{ \bar{\psi}^{1, \dots, 5} \} &= \left\{ \frac{1}{2} \frac{1}{2} \frac{1}{2} 00 \right\} \end{aligned}$$

$$\implies \mathbf{SU(3)}_C \times \mathbf{U(1)}_C \times \mathbf{SU(2)}_L \times \mathbf{SU(2)}_R$$

[HEP-PH/0006331 CLEAVER, FARAGGI, SAVAGE ]

## Why LRS?

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- $U(1)$  combination

$$U(1)_\zeta = U(1)_1 + U(1)_2 + U(1)_3$$

- $U(1)$  charges

$$Q_\zeta(Q_L; L_L; Q_R; L_R) = \pm \frac{1}{2}$$

- For  $SO(10) \times U(1)_\zeta \subset E_6$ :

$$\mathbf{27} \rightarrow \mathbf{16}_{\pm\frac{1}{2}} + \mathbf{10}_{\mp 1} + \mathbf{1}_{\pm 2}$$

- For  $SO(10) \times U(1)_\zeta \not\subset E_6$ :

$$\mathbf{27} \not\rightarrow \underbrace{\mathbf{16}_{\pm\frac{1}{2}}}_{\mathbf{8}_{\frac{1}{2}} + \mathbf{8}_{-\frac{1}{2}}} + \mathbf{10}_{\mp 1} + \mathbf{1}_{\pm 2}$$

## Spectra Highlights

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- $SU(2)_{L/R}$  doublets cancel gauge anomalies ( $\not\subset E_6$  only)
- Heavy Higgs' break  $SU(2)_R$  at intermediate scale,  $M_R$
- Singlets  $\rightarrow$  Extended seesaw mechanism

For  $\subset E_6$  already in **27**

- Colour triplets  $\rightarrow$  Gauge coupling unification



# Gauge Coupling Unification

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- Heterotic String scale  $\rightarrow M_S \sim 5 \cdot 10^{17}$  GeV
- MSSM GUT scale  $\rightarrow M_{GUT} \sim 2 \cdot 10^{16}$  GeV
- Resolution?

Intermediate mass scales

[HEP-TH/9505046 FARAGGI, DIENES]

## Symmetry Breaking

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$$SO(10) \xrightarrow{M_S} SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_C$$

$$\xrightarrow{M_R} SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)_{Z'}$$

$$\xrightarrow{M_{Z'}} SU(3)_C \times SU(2)_L \times U(1)_Y$$

- Triplets acquire mass at  $M_D$ , SUSY scale  $\rightarrow M_{SUSY}$
- Mass scale hierarchy  $M_S \gtrsim M_R > M_D \gtrsim M_{Z'} \gtrsim M_{SUSY} > M_Z$

## RGEs

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- One-loop RGEs for gauge couplings

$$\frac{4\pi}{\alpha_i(\mu)} = k_i \frac{4\pi}{\alpha_{\text{string}}} + \beta_i \log \frac{M_{\text{string}}^2}{\mu^2} + \Delta_i^{(\text{total})},$$

where  $\Delta_i^{(\text{total})}$  are corrections from I.M and I.G.

- Hypercharge embedding

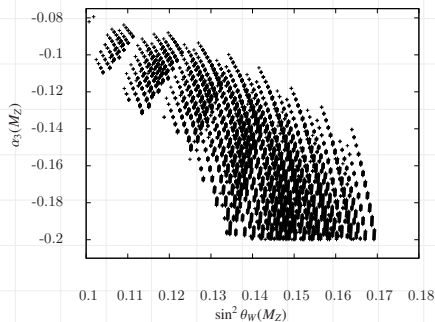
$$\alpha_1^{-1}(M_R) = \alpha_{2R}^{-1}(M_R) + \frac{2}{3}\alpha_{\hat{C}}^{-1}(M_R)$$

- At string unification scale

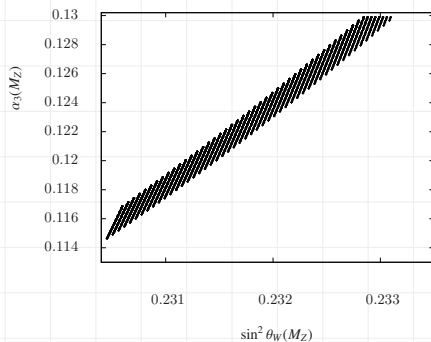
$$\alpha_S \equiv \alpha_3(M_S) = \alpha_2(M_S) = \frac{5}{3}\alpha_Y(M_S)$$

# Analysis

- $SO(10) \times U(1) \not\subset E_6$



- $SO(10) \times U(1) \subset E_6$



## Intermediate Thresholds

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- $\not\subset E_6$ :

$$\delta(\sin^2 \theta_W(M_Z))_{\text{I.T.}} = \frac{1}{2\pi} \frac{k_1 \alpha}{1 + k_1} \left( \frac{12}{5} \log \frac{M_S}{M_R} - \frac{24}{5} \log \frac{M_S}{M_{Z'}} - \frac{2n_D}{5} \log \frac{M_S}{M_D} \right)$$

$$\delta(\alpha_3(M_Z))_{\text{I.T.}} = \frac{1}{2\pi} \left( \frac{3}{2} \log \frac{M_S}{M_R} - 9 \log \frac{M_S}{M_{Z'}} + \frac{3n_D}{4} \log \frac{M_S}{M_D} \right)$$

- $\subset E_6$

$$\delta(\sin^2 \theta_W(M_Z))_{\text{I.T.}} = \frac{1}{2\pi} \frac{k_1 \alpha}{1 + k_1} \left( \frac{12}{5} \log \frac{M_S}{M_R} + \frac{6}{5} \log \frac{M_S}{M_H} - \frac{6}{5} \log \frac{M_S}{M_D} \right)$$

$$\delta(\alpha_3(M_Z))_{\text{I.T.}} = \frac{1}{2\pi} \left( \frac{3}{2} \log \frac{M_S}{M_R} - \frac{9}{4} \log \frac{M_S}{M_H} + \frac{9}{4} \log \frac{M_S}{M_D} \right)$$

# Summary

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- Viable  $U(1)_{Z'}$  from strings
- Problematic GCU when  $SO(10) \times U(1)_\zeta \not\subset E_6$   
Unless Spinor–vector duality realised  
[\[HEP-TH/0611251 FARAGGI, KOUNNAS, RIZOS \]](#)
- $U(1)_\zeta$  desirable candidate
- Can it be embedded in  $E_6$ ?

## An $E_6$ Model

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- $\mathbf{x}$  enhances  $(3_C, 2_L, 2_R, 1_C, 1_\zeta) \rightarrow (4_C, 2_L, 2_R, 1_{\zeta'})$
- Anomaly free as full  $\mathbf{27}$  kept
- $U(1)_{\zeta'}$  rotation of  $U(1)_\zeta$
- **PROTON LIFETIME PRESERVED**