

# The NMSSM with F-theory unified boundary conditions

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In collaboration with:

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# A history of tension

Fine Tuning

$$m_h \approx 125 - 126 \text{ GeV}$$

$$\text{SUSY : } m_h \leq 130 \text{ GeV}$$

$\mu$  problem

It is supersymmetric.

Order of SUSY-breaking soft terms

# A history of tension

NMSSM

Maniatis, Ellwanger, Hugonie, Teixeira (2010)

$$W_{\text{NMSSM}} = W_{\text{Yuk}} + \lambda S H_u H_d + \frac{\kappa}{3} S^3$$

$$V_{\text{soft}}^S = m_{H_u}^2 |H_u|^2 + m_{H_d}^2 |H_d|^2 + m_S^2 |S|^2 + \left( \lambda A_\lambda S H_u H_d + \frac{\kappa}{3} A_\kappa S^3 + h.c. \right)$$

$$m_h^2 \simeq m_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta + \delta(m_h^2)$$

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$$m_h^2 \simeq m_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta + \delta(m_h^2)$$

UNIVERSALITY

# A history of love

- SU(5) unified theory
- Origin of SUSY-breaking
- Universality

Modulus dominance SUSY-breaking in F-theory SU(5) GUTs

L.A., Cerdeño, Ibáñez (2008–2012)



$$m_{\tilde{f}}^2 = \frac{1}{2}|M|^2$$

$$m_H^2 = \frac{1}{2}|M|^2(1 - \frac{3}{2}\rho_H)$$

$$A = -\frac{1}{2}M(3 - \rho_H)$$

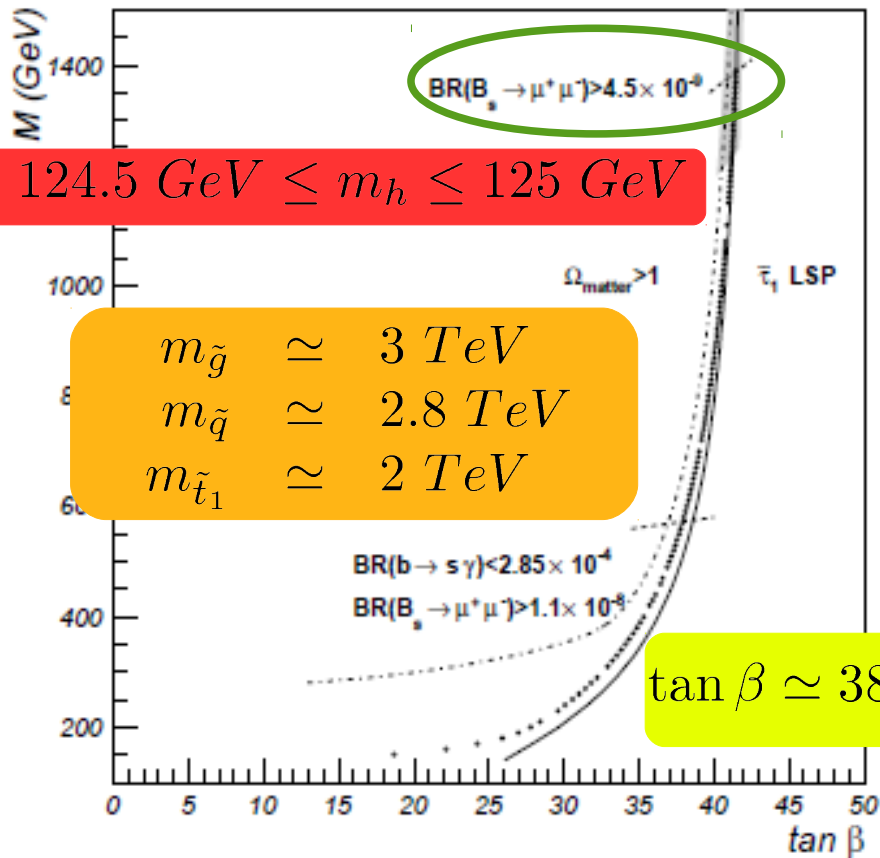
$$B = -M(1 - \rho_H)$$

# A possible history of love

- SU(5) unified theory
- Origin of SUSY-breaking
- Universality

Modulus dominance SUSY-breaking in F-theory SU(5) GUTs

L.A., Cerdeño, Ibañez (2008–2012)

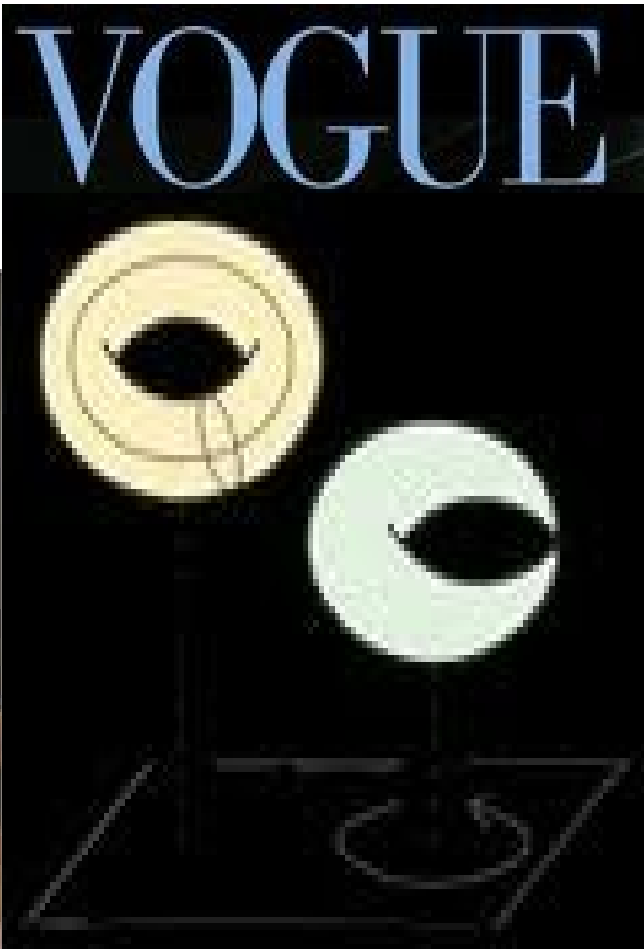
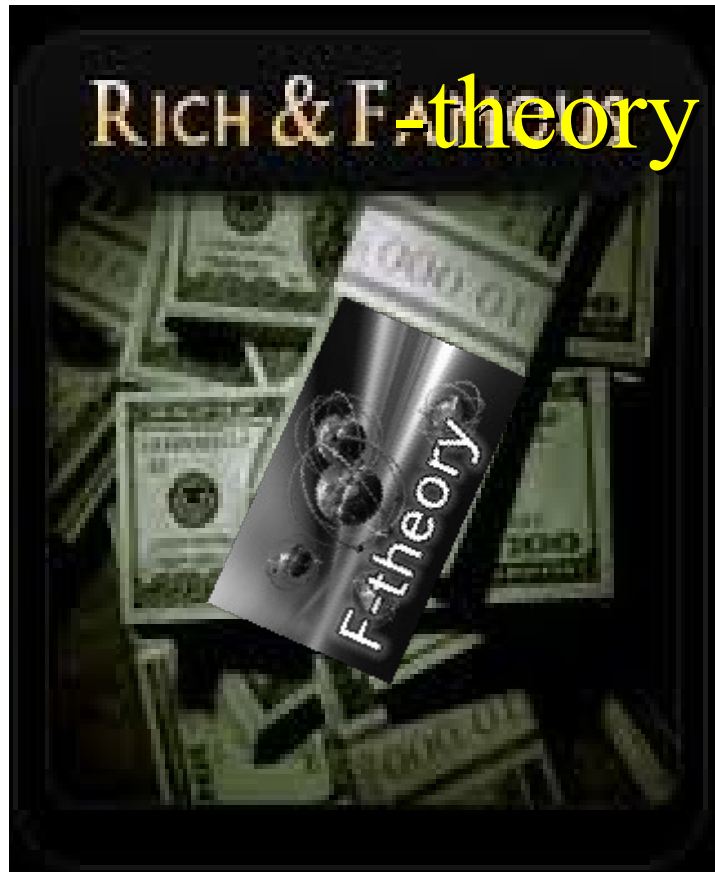


VERY PREDICTIVE !!

Modulus dominated

CNMSSM ??

# F-theory



# F-theory

- $SL(2, \mathbb{Z})$  in Type IIB

F1-string

$SL(2, \mathbb{R})$

D1-brane

$$\tau \rightarrow \frac{a\tau + b}{c\tau + d}, \quad \begin{pmatrix} B_2 \\ C_2 \end{pmatrix} \rightarrow \begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} B_2 \\ C_2 \end{pmatrix}$$

$$\tau = C_0 + ie^{-\phi} = C_0 + \frac{i}{g_s}$$

Schwarz (1996)



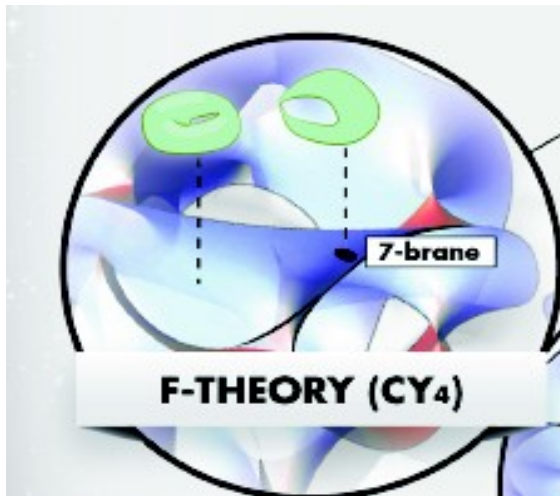
# F-theory crash course

- $SL(2, \mathbb{Z})$  in Type IIB



# F-theory crash course

- $SL(2, Z)$  in Type IIB
- Geometric meaning: elliptic fibrations



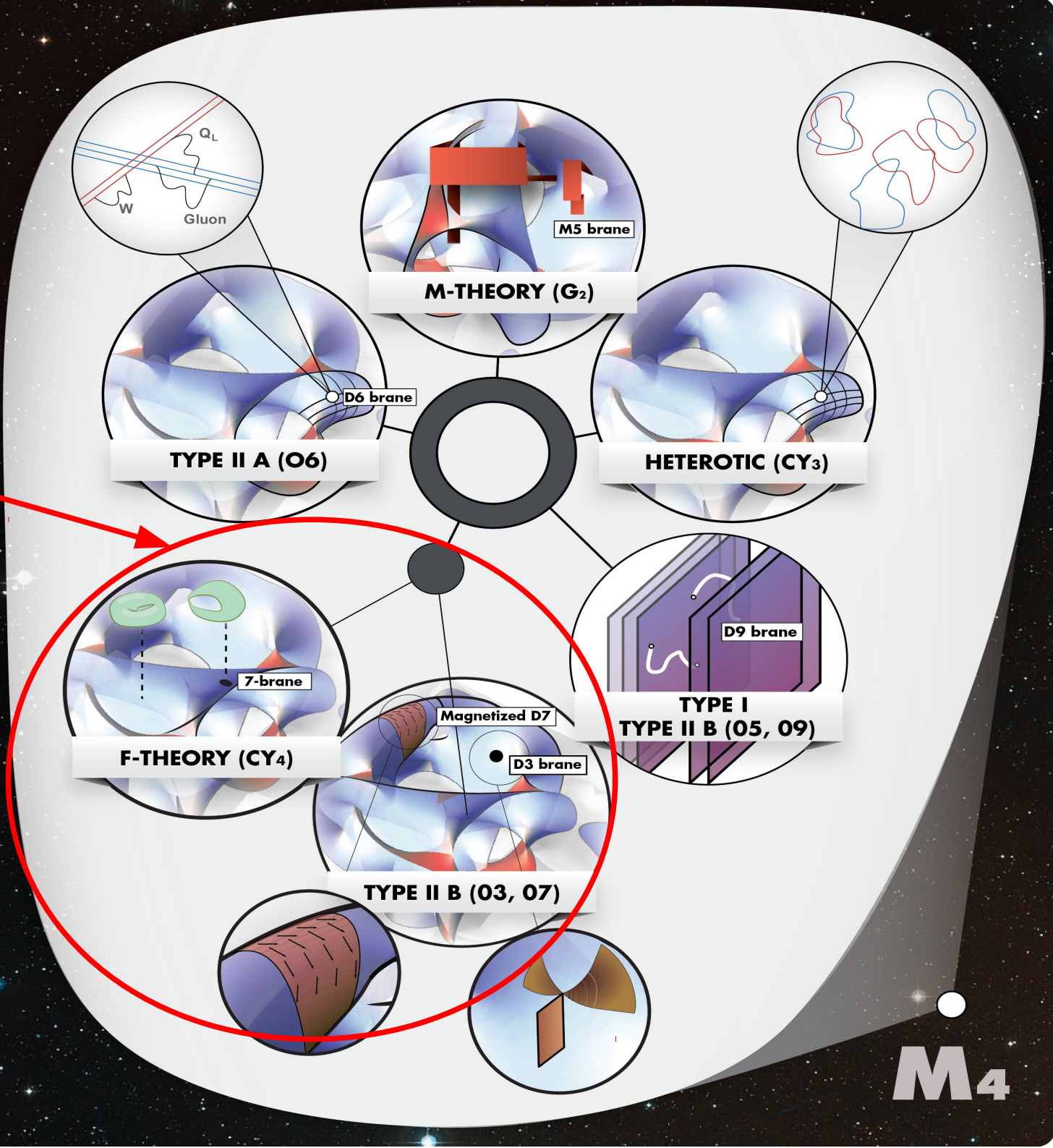
$$\begin{array}{ccc} \mathbf{T}^2 & \rightarrow & \mathbf{CY}_4 \\ & & \downarrow \\ & & \mathbf{B}_3 \end{array}$$

Type IIB with  $\tau = \tau(z)$

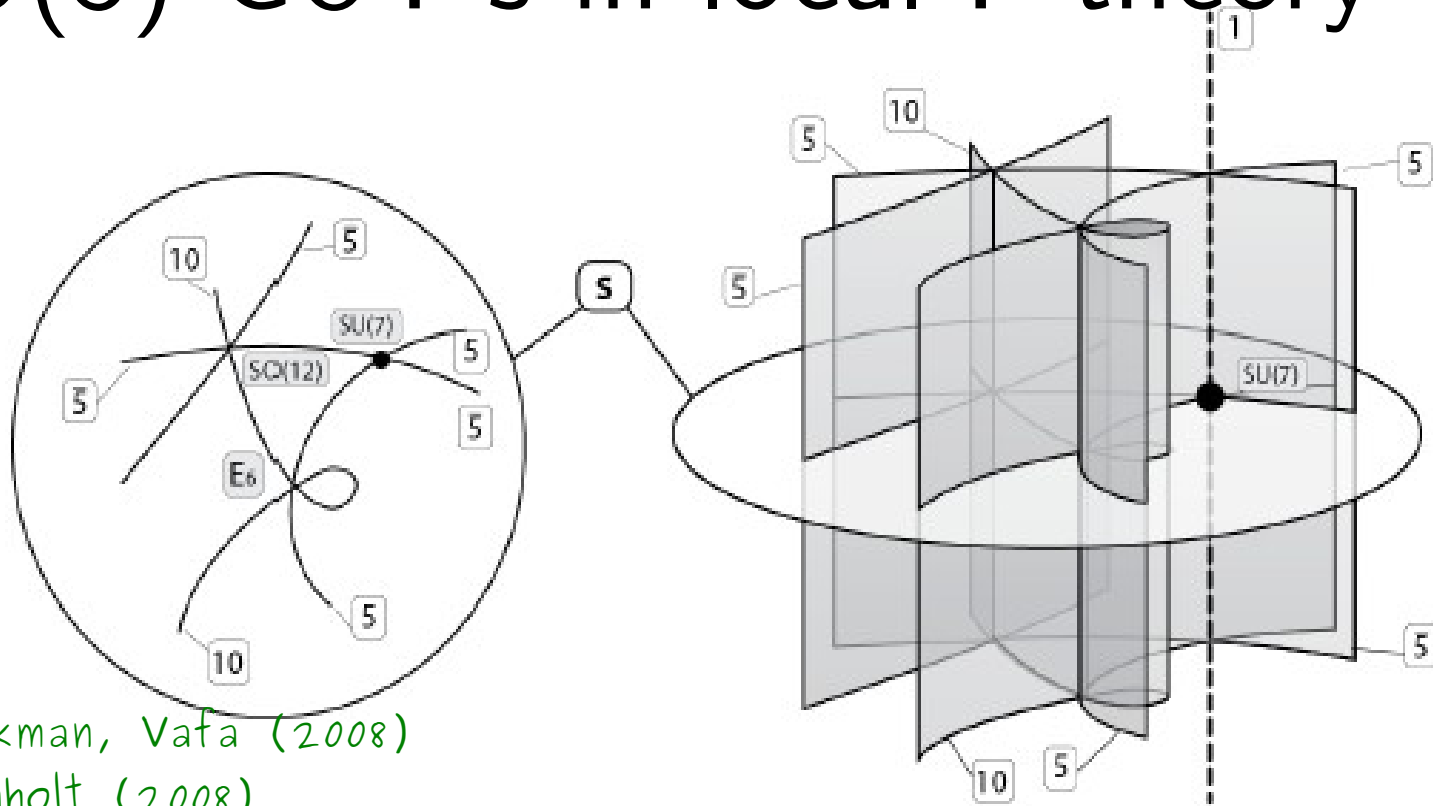
Beasley, Heckman, Vafa (2008)  
Donagi, Wijnholt (2008)

Vafa (1996), Morrison, Vafa (1996)

You are here



# SU(5) GUT's in local F-theory



Beasley, Heckman, Vafa (2008)

Donagi, Wijnholt (2008)

$$SO(12) \rightarrow SU(5) \times U(1) \times U(1)'$$

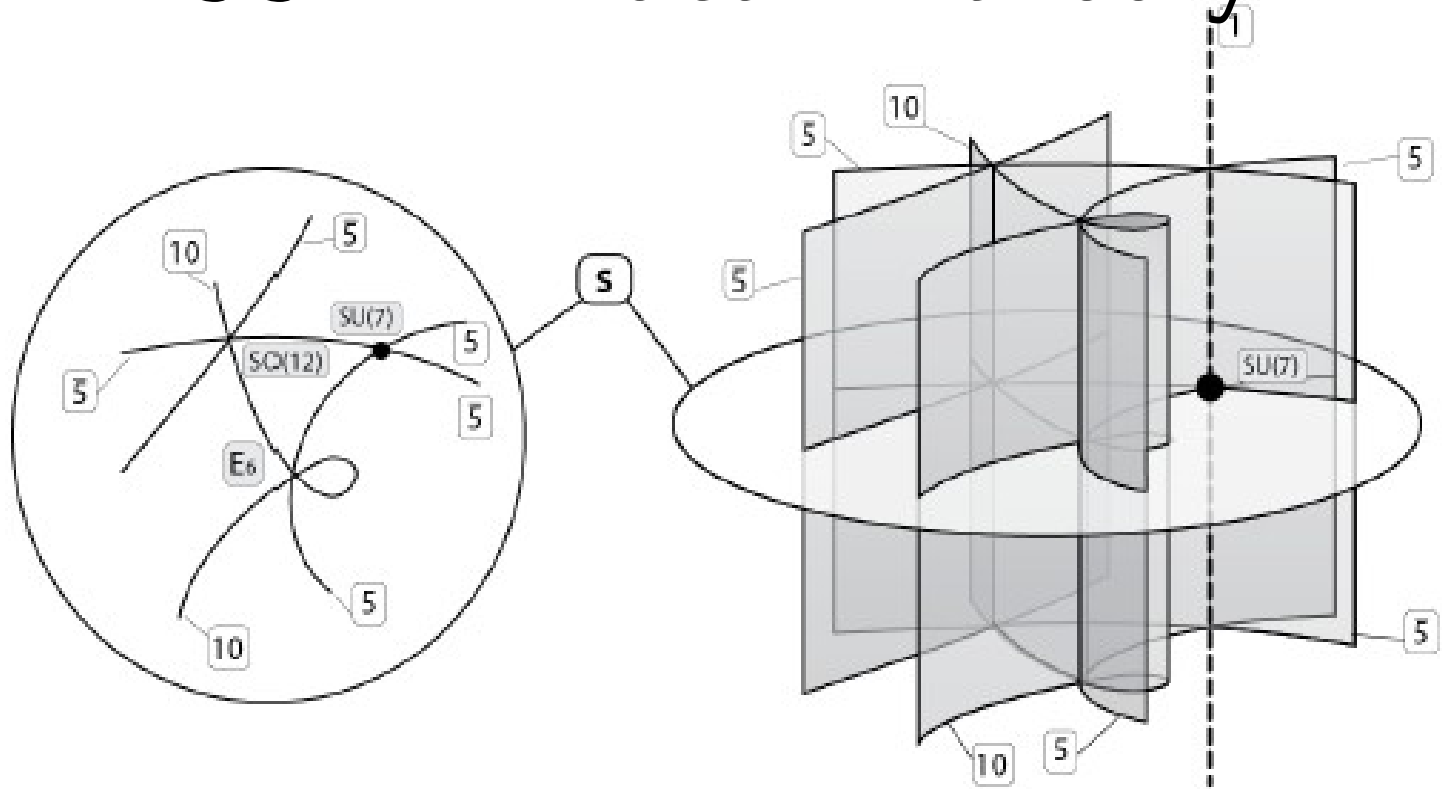
$$66 \rightarrow \text{Adjoint} + [(\mathbf{10}, 4, 0) + (\bar{\mathbf{5}}, -2, 2) + (\bar{\mathbf{5}}, -2, 2) + c.c.]$$

$$E_6 \rightarrow SU(5) \times U(1) \times U(1)'$$

$$78 \rightarrow \text{Adjoint} + [(\mathbf{10}, -1, -3) + (\mathbf{10}, 4, 0) + (\mathbf{5}, -3, 3) + (\mathbf{1}, 5, 3) + c.c.]$$

$$W_{\text{NMSSM}} = W_{\text{Yuk}} + \lambda S H_u H_d + \frac{\kappa}{3} S^3$$

# NMSSM in local F-theory



$SU(7) \rightarrow SU(5) \times U(1)^2$  L.A., Camara, Cerdeno, Ibanez, Valenzuela (2012)

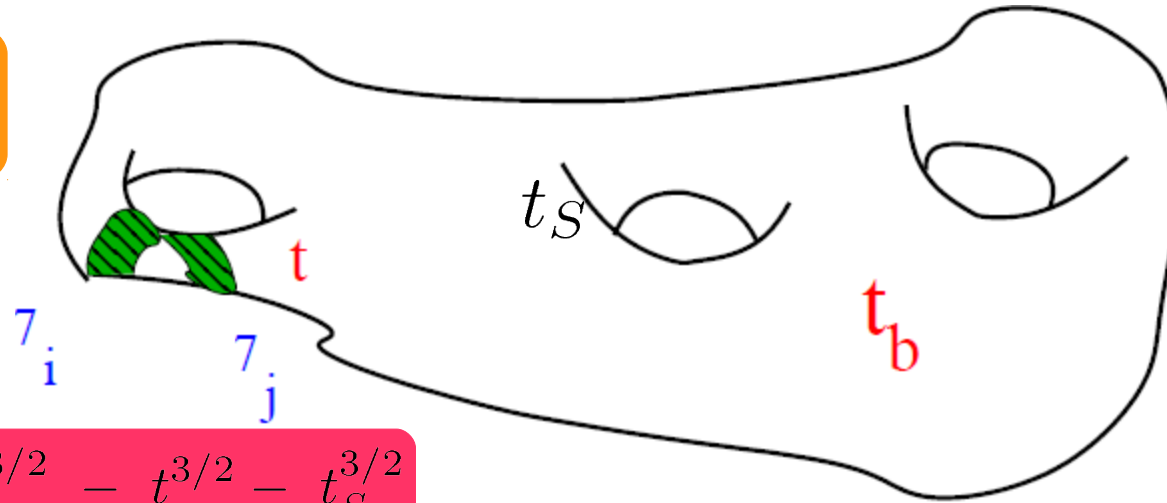
$48 \rightarrow 24 + \mathbf{1}_{(0,0)} + \mathbf{1}_{(0,0)} + [\mathbf{5}_{(0,-1)} + \mathbf{1}_{(-1,1)} + \mathbf{\bar{5}}_{(1,0)} + \text{c.c.}]$

$$W_{\text{NMSSM}} = W_{\text{Yuk}} + \lambda S H_u H_d + \frac{\kappa}{3} S^3$$

Instantons

# T-modulus dominated NMSSM

$$t, t_S \ll t_b$$



$$\text{Vol}[\text{CY}] = t_b^{3/2} - t^{3/2} - t_S^{3/2}$$

- Kähler metrics

$$K_\alpha = \frac{t^{(1-\xi_\alpha)}}{t_b}$$



$$K_{\bar{5},10} = \frac{t^{1/2}}{t_b}, \quad K_S = \frac{t_S^{1/2}}{t_b}$$

Conlon, Cremades, Quevedo (2007)  
L.A., Cerdeño, Ibañez (2008)

- Gauge kinetic function

$$f = T$$

L.A., Camara, Cerdeño, Ibañez, Valenzuela (2012)

# T-modulus dominated NMSSM

- Assuming  $F_{t_b} \gg F_t \gg F_{t_s}$  (easily obtained in **LVS**)

Conlon, Quevedo, Cicoli, Balasubramanian (2005–2011)

- MSSM-like** soft terms

$$\rho_H \simeq \alpha_G^{1/2} \simeq 0.2$$

L.A., Cerdeño, Ibañez (2012)

$$\begin{aligned} M &= \frac{F_t}{t} \\ m_H^2 &= \frac{|M|^2}{2} \left(1 - \frac{3}{2}\rho_H\right) \\ m_{5,10}^2 &= \frac{|M|^2}{2} \\ A &= -\frac{1}{2}M(3 - \rho_H) \end{aligned}$$

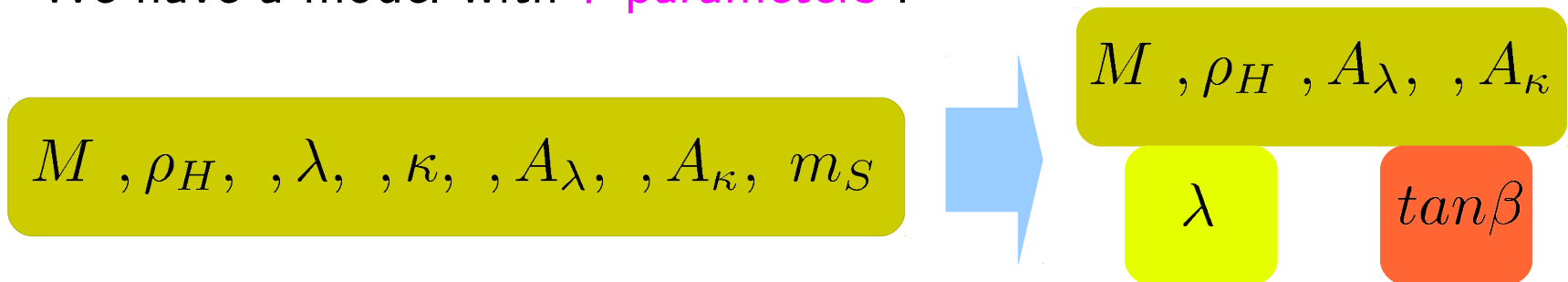
- Singlet-like** soft terms

$$A_\lambda = -M(1 - \rho_H), \quad A_\kappa = m_S^2 = 0$$

L.A., Camara, Cerdeño, Ibañez, Valenzuela (2012)

# T-modulus dominated NMSSM

- We **don't impose** the singlet-like boundary conditions
- We have a model with **7 parameters** :



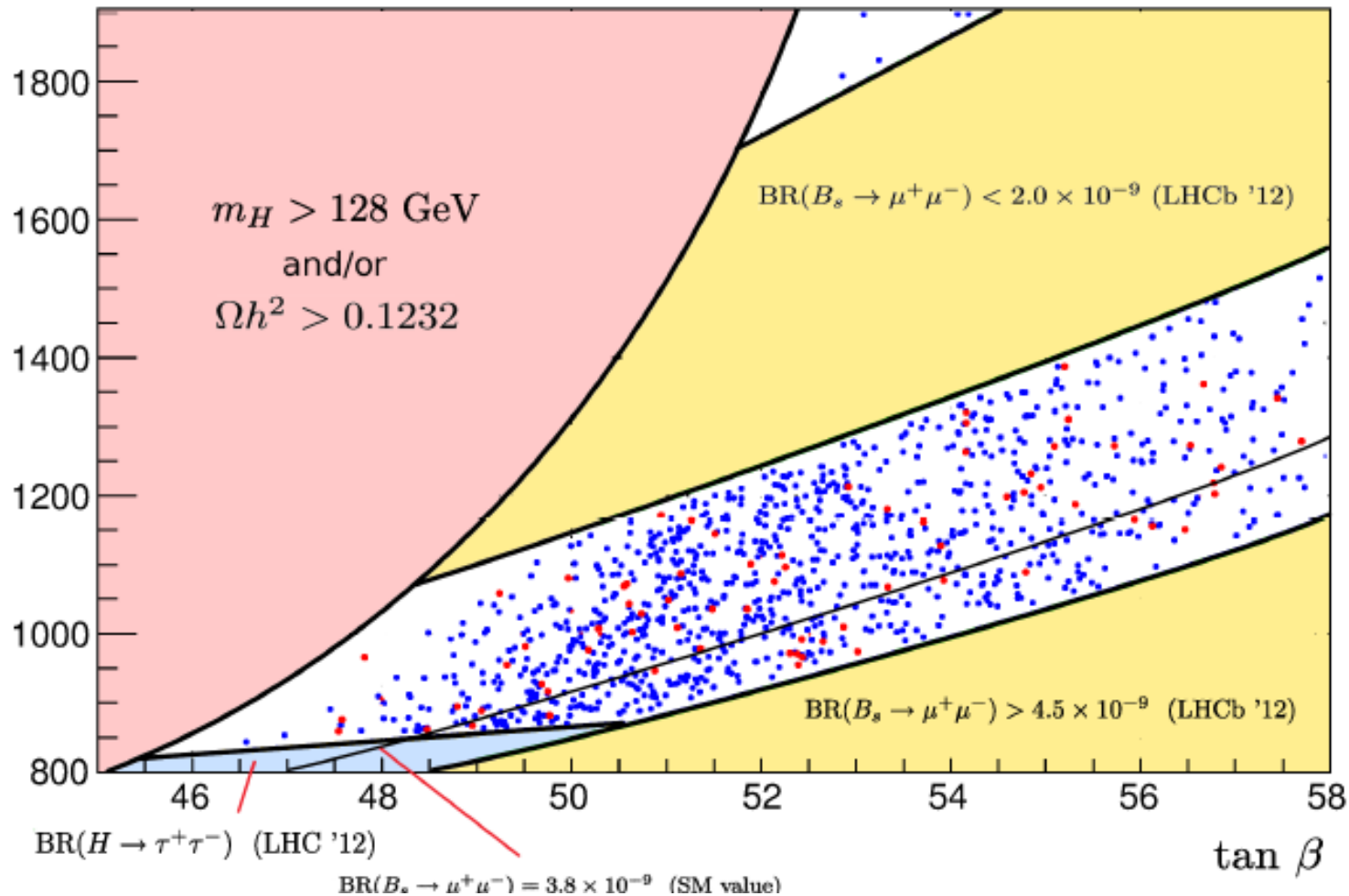
- We perform a large scan using `NMSSMTools`, imposing:
  - EWSB, Ellwanger, Gunion, Hugonie (2004)
  - Reduced cross sections for **Higgs decays** (ATLAS and CMS results)
  - **Flavor** observables (LHCb results)
  - **Dark matter** relic density using `micrOMEGAS` (WMAP results)  
Belanger, Boudejma, Pukhov, Semenov (2011)



# T-modulus dominated NMSSM

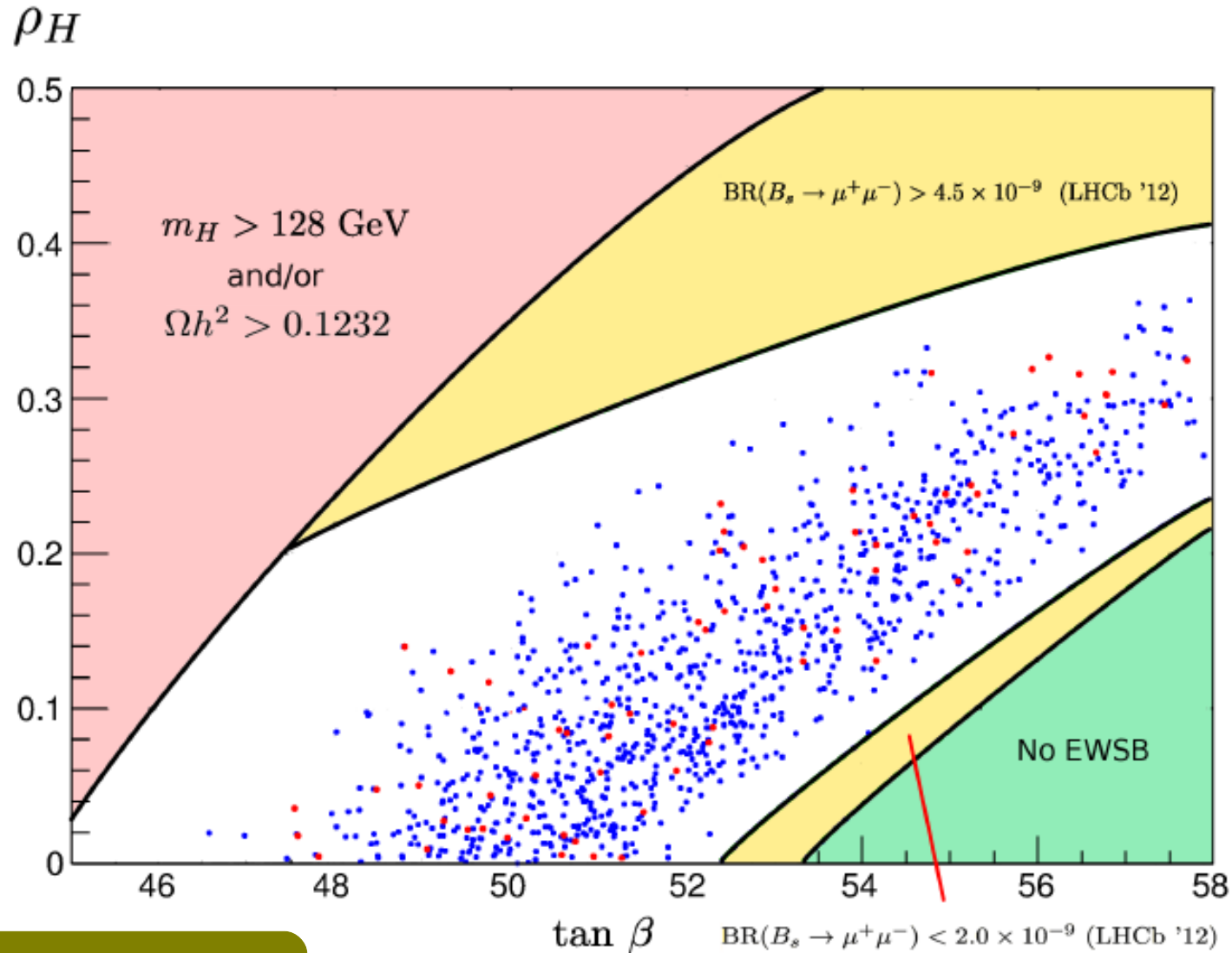
$$A_\lambda < 0, A_\kappa \leq 0 \text{ and } \lambda \geq 0$$

$M$  (GeV)



L.A., Camara, Cerdeño, Ibañez, Valenzuela (2012)

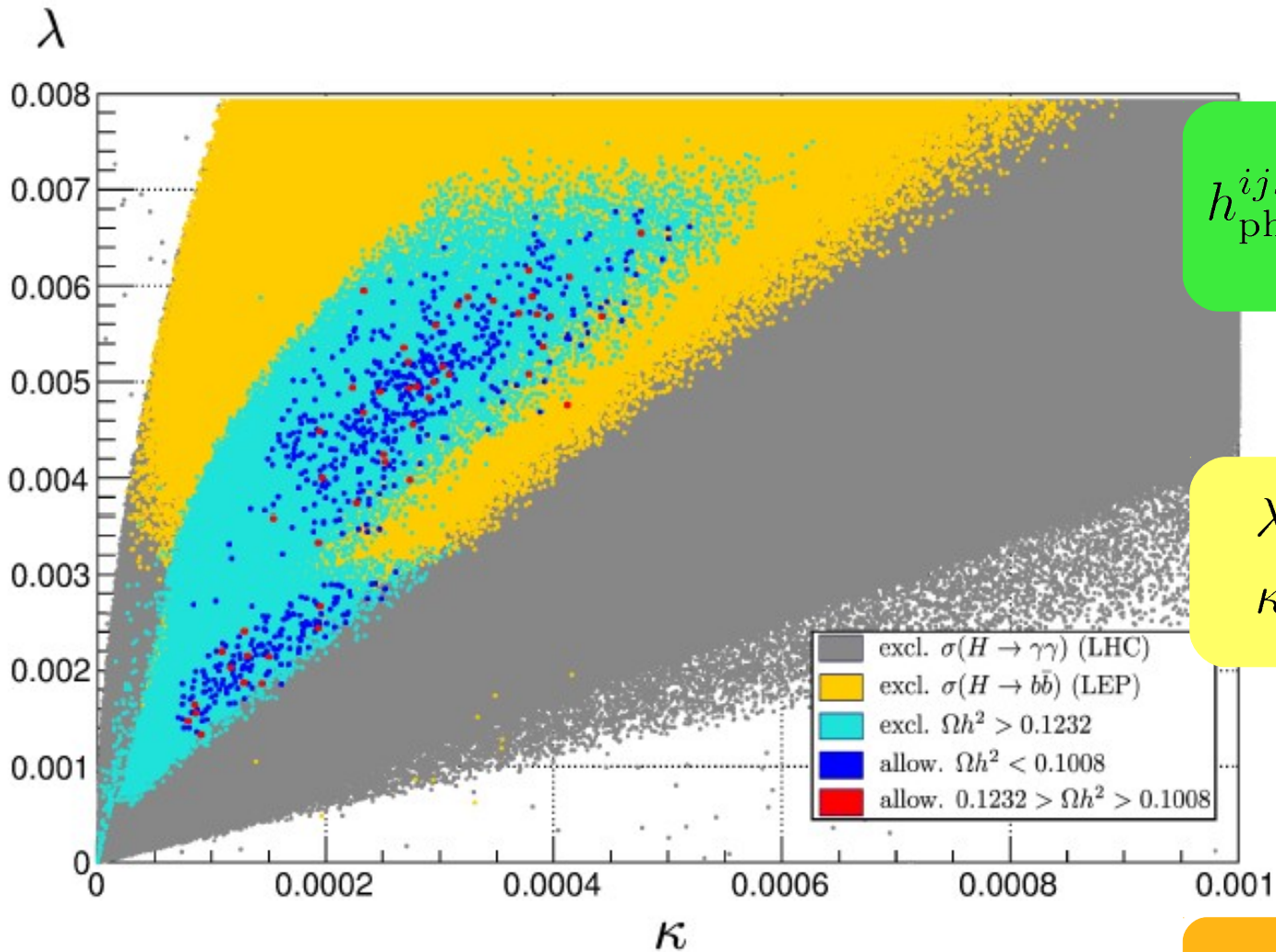
# T-modulus dominated NMSSM



$$\rho_H \simeq \alpha_G^{1/2} \simeq 0.2$$

L.A., Camara, Cerdeño, Ibañez, Valenzuela (2012)

# T-modulus dominated NMSSM



$$h_{\text{phys}}^{ijk} = \frac{h_0^{ijk}}{(K_i K_j K_k)^{1/2}} e^{K/2}$$



$$\lambda_{\text{phys}} = \lambda_0 t^{-1/2} t_S^{-1/4}$$

$$\kappa_{\text{phys}} = \kappa_0 t_S^{-3/4}$$

$$t_S \simeq t = \alpha_G^{-1} \simeq 24$$



$$\lambda_{\text{phys}}, \kappa_{\text{phys}} \simeq 9 \times 10^{-2} \lambda_0, \kappa_0$$

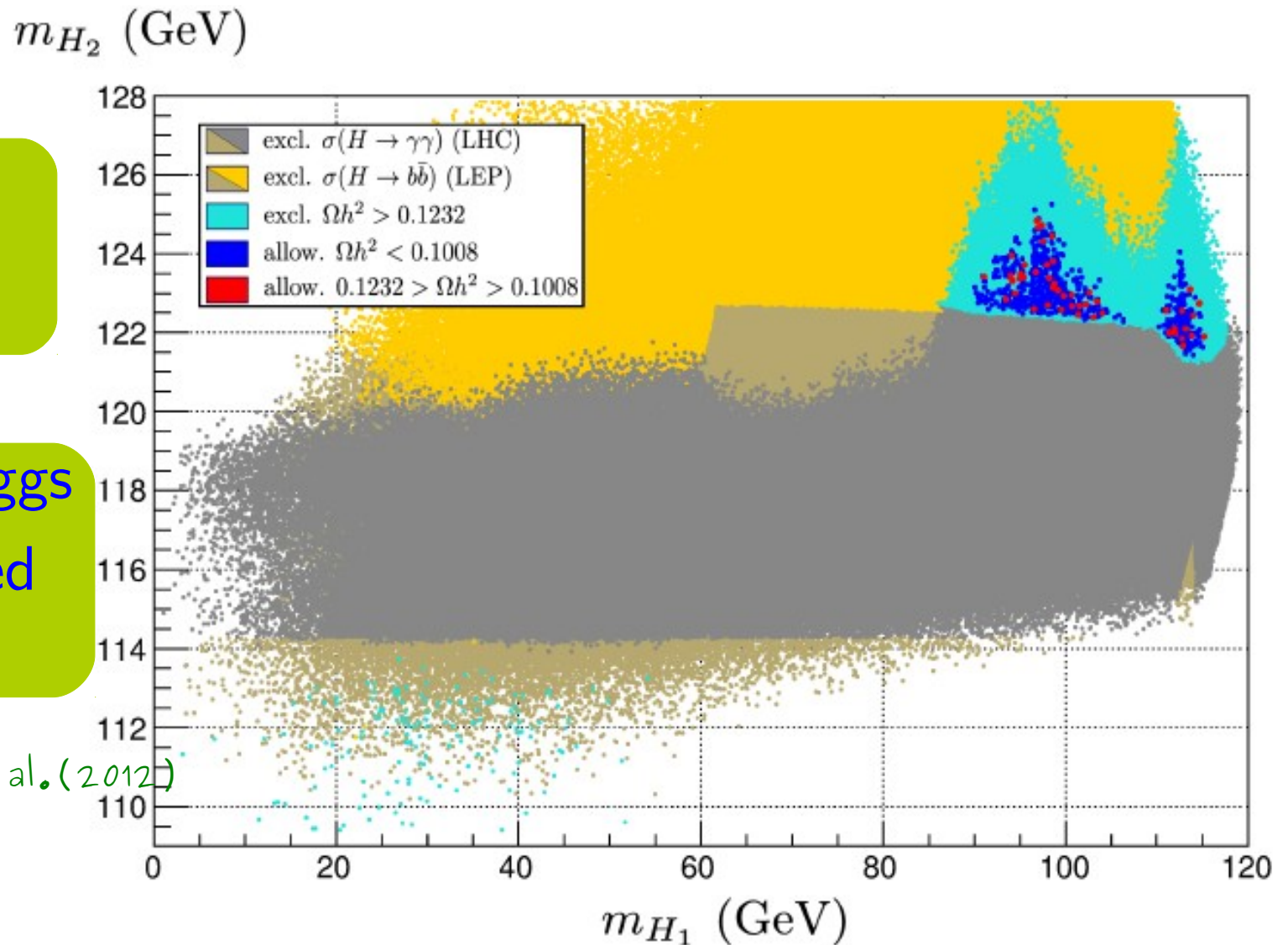
# T-modulus dominated NMSSM

$$m_{H_1} \lesssim 120$$

$$m_{H_2} \gtrsim 122$$

Extra light Higgs  
fairly decoupled  
from SM

Also see Belanger et al. (2012)



L.A., Camara, Cerdeño, Ibañez, Valenzuela (2012)

# T-modulus dominated NMSSM

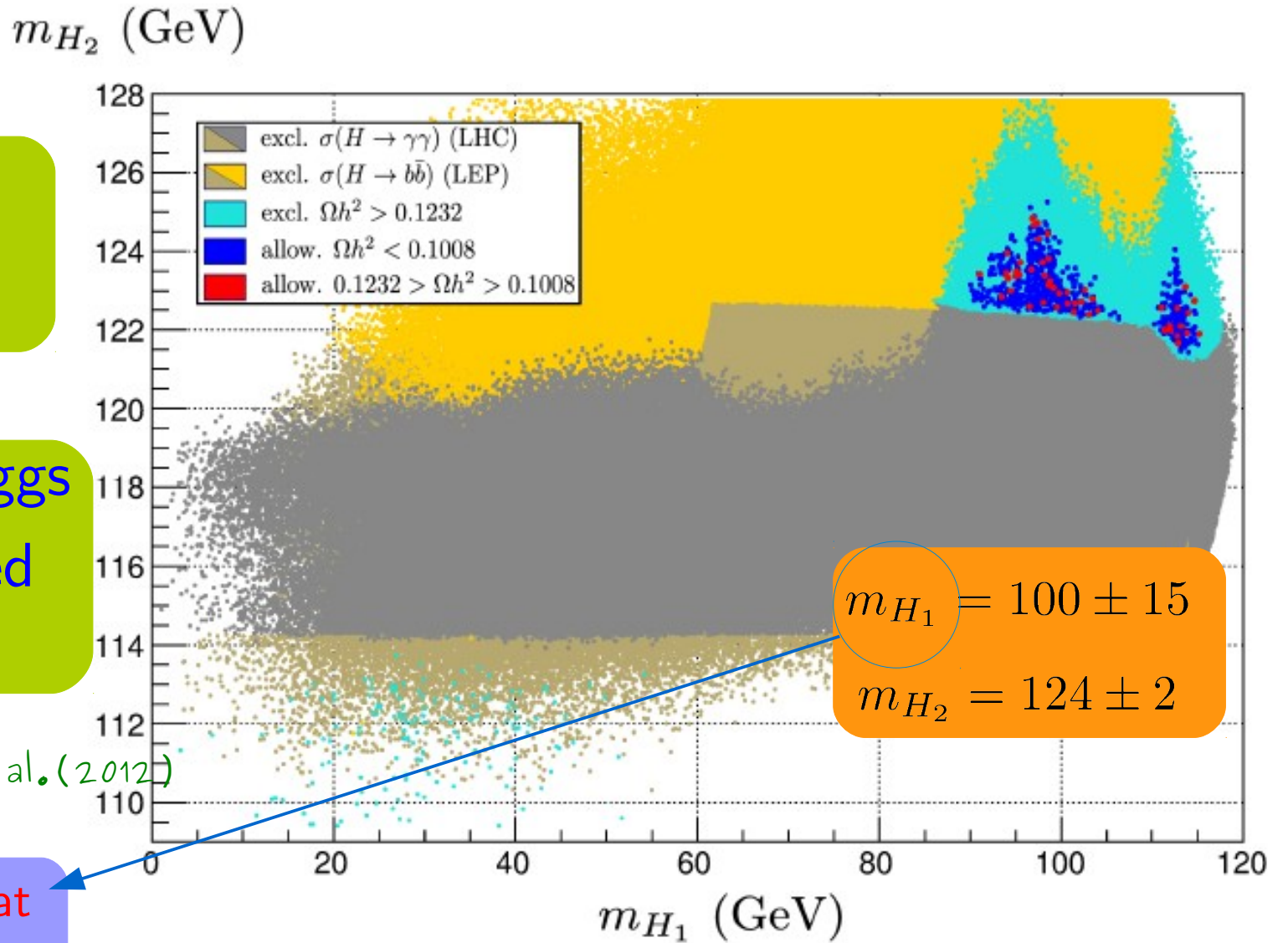
$m_{H_1} \lesssim 120$   
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2 sigma excess at  
 LEP

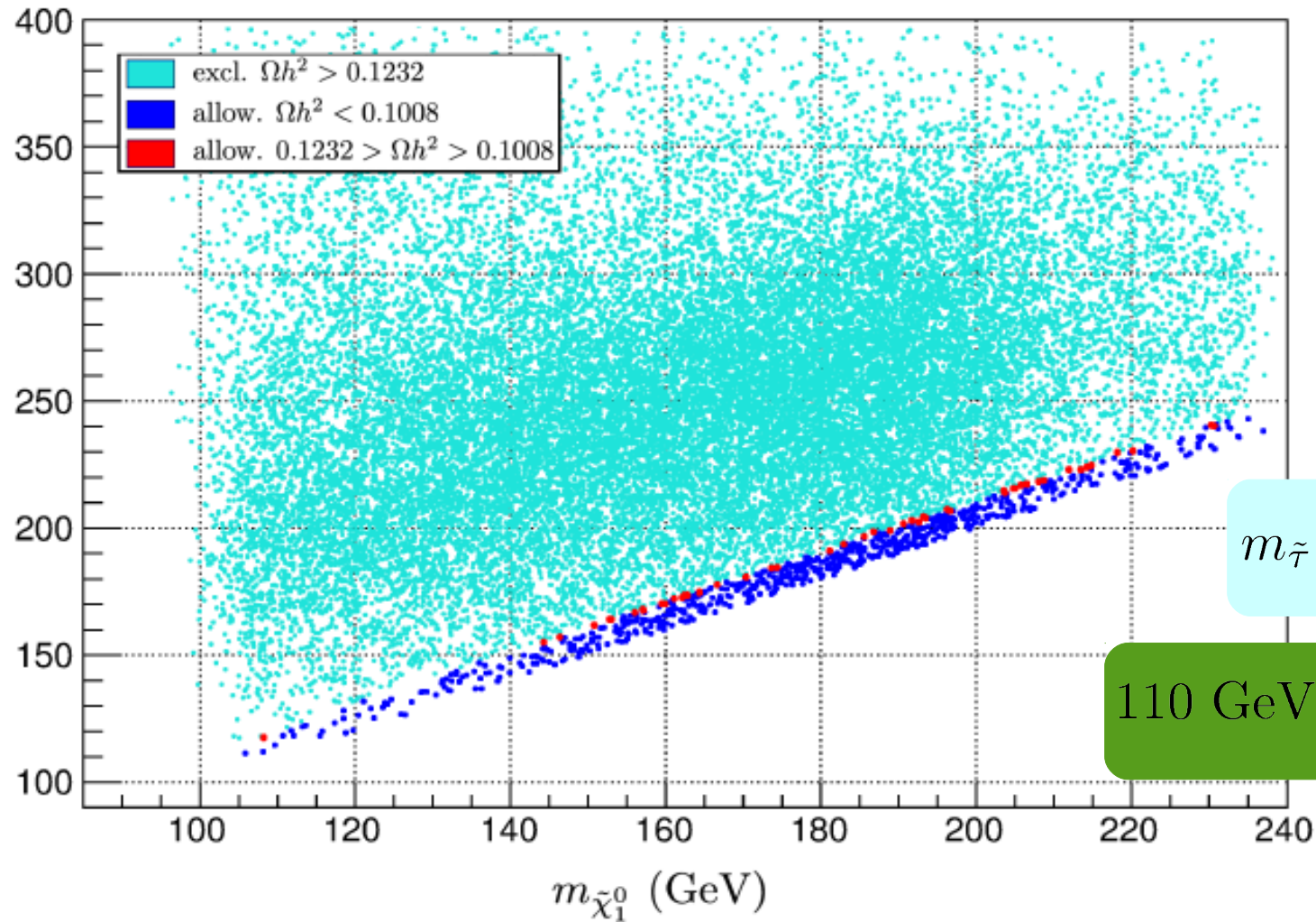
$\mu_{eff} \gtrsim 1$



L.A., Camara, Cerdeño, Ibañez, Valenzuela (2012)

# T-modulus dominated NMSSM

$m_{\tilde{\tau}}$  (GeV)



$$m_{\tilde{\chi}_1^0} \approx 2k v_s$$

$$m_{\tilde{\tau}} - m_{\tilde{\chi}_1^0} \approx 10 \text{ GeV}$$

$$110 \text{ GeV} \lesssim m_{\tilde{\tau}} \lesssim 250 \text{ GeV}$$

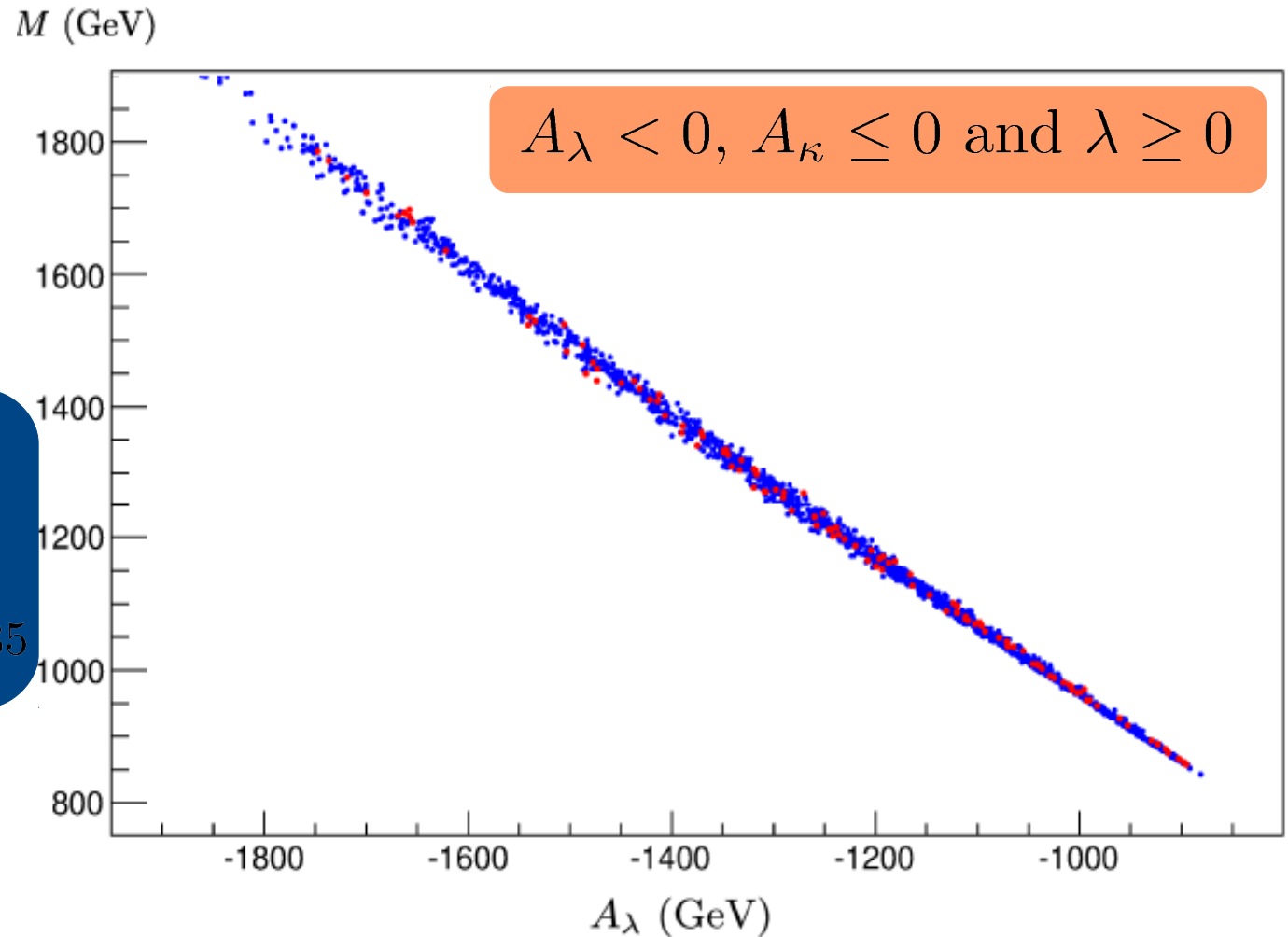
# T-modulus dominated NMSSM

$$A_{\kappa} = m_S^2 = 0$$

$$A_{\lambda} = -M(1 - \rho_H)$$

$$(A_{\kappa}/A) \lesssim 0.3$$

$$-0.015 \lesssim \left(\frac{m_S}{m_{\bar{5},10}}\right)^2 \lesssim 0.035$$



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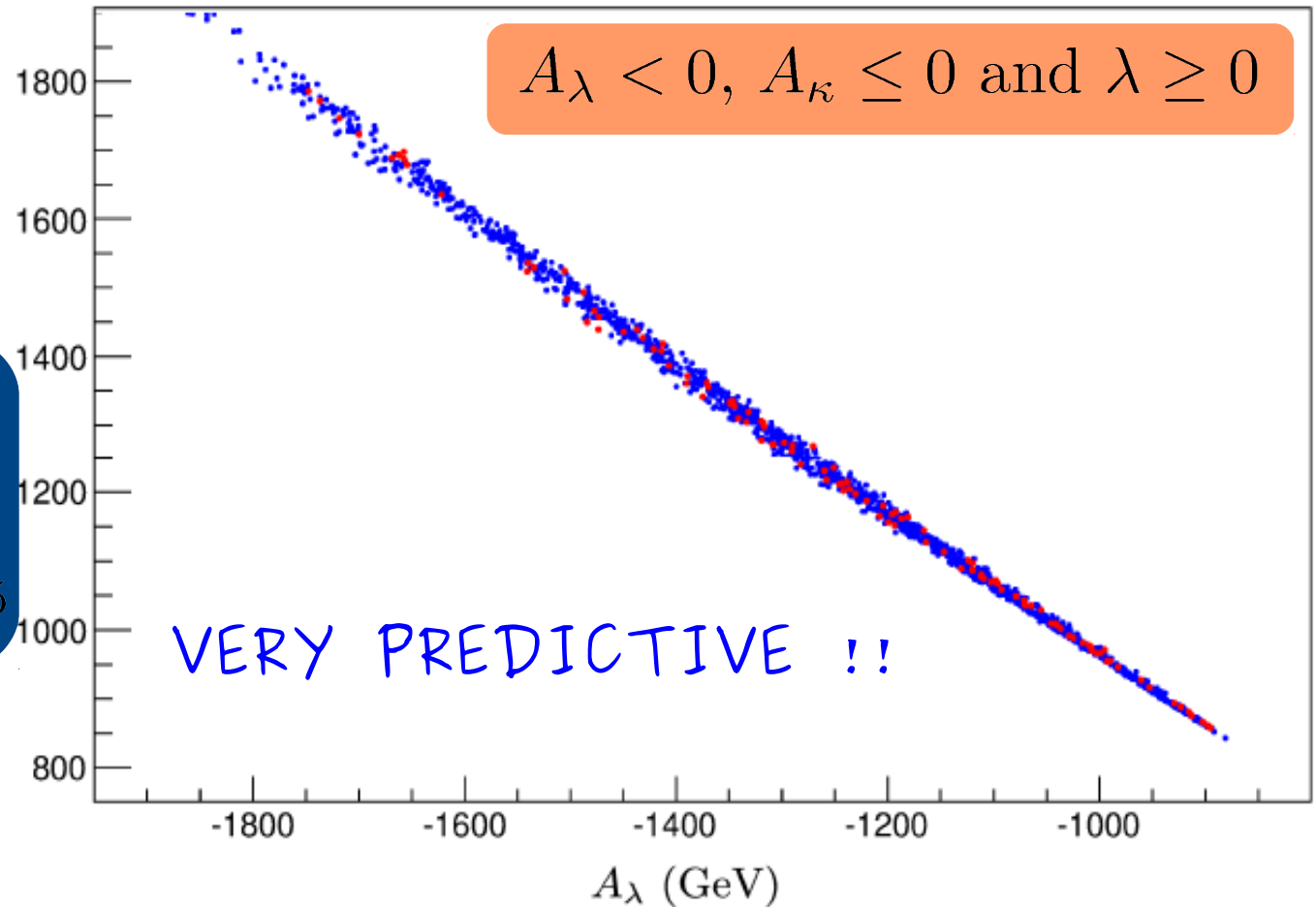
$$-0.015 \lesssim \left(\frac{m_S}{m_{\bar{5},10}}\right)^2 \lesssim 0.035$$

$$M, \rho_H, A_\lambda, A_\kappa$$

$$\lambda$$

$$\tan\beta$$

$M$  (GeV)





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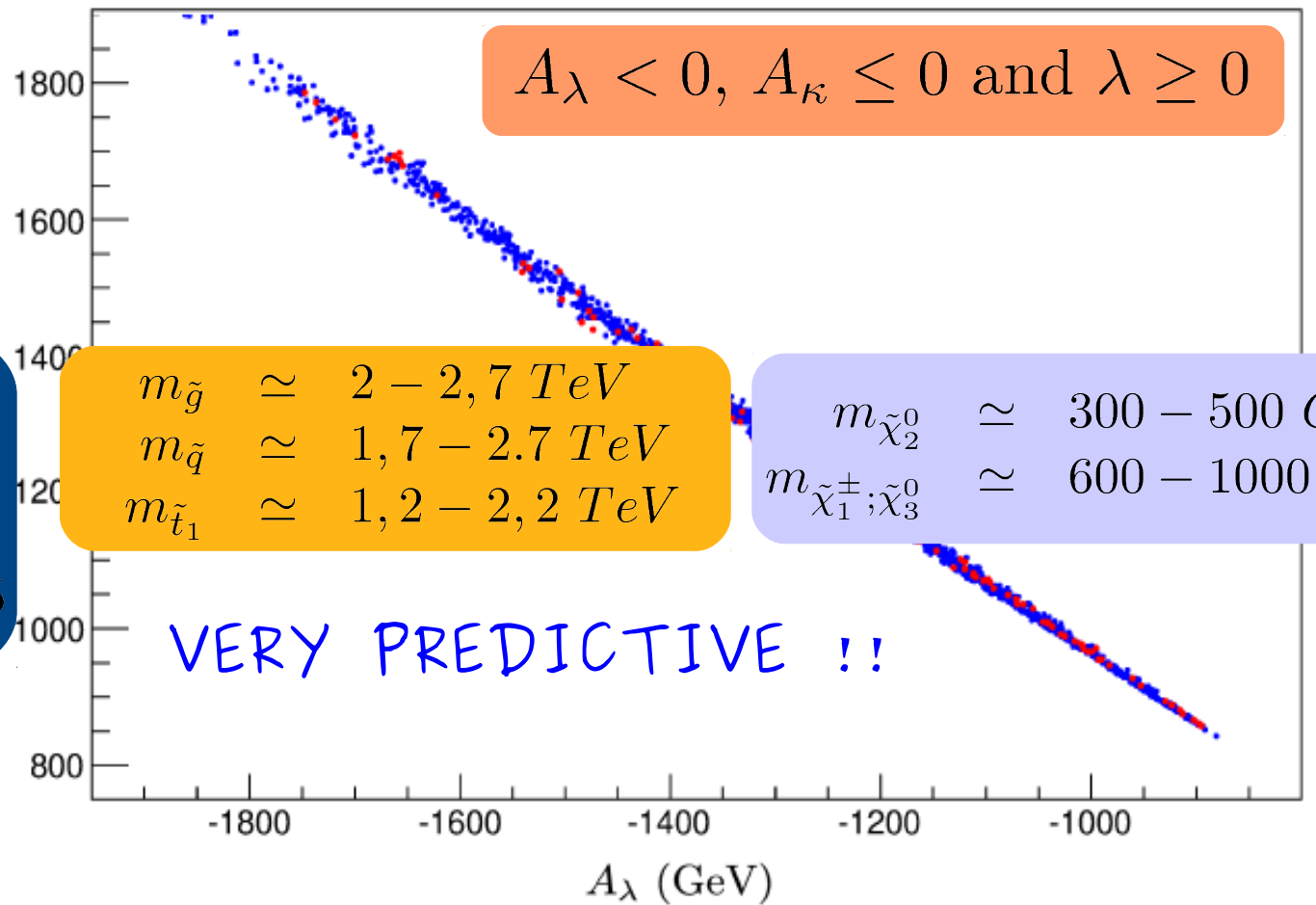
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$M$  (GeV)



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$$M, \rho_H, A_\lambda, A_\kappa$$

$$\lambda$$

$$\tan\beta$$

Multitau signals, hard central jets and missing energy

Ellwaneger, Florent, Zerwas (2011)

$$m_{\tilde{g}} \simeq 2 - 2,7 \text{ TeV}$$

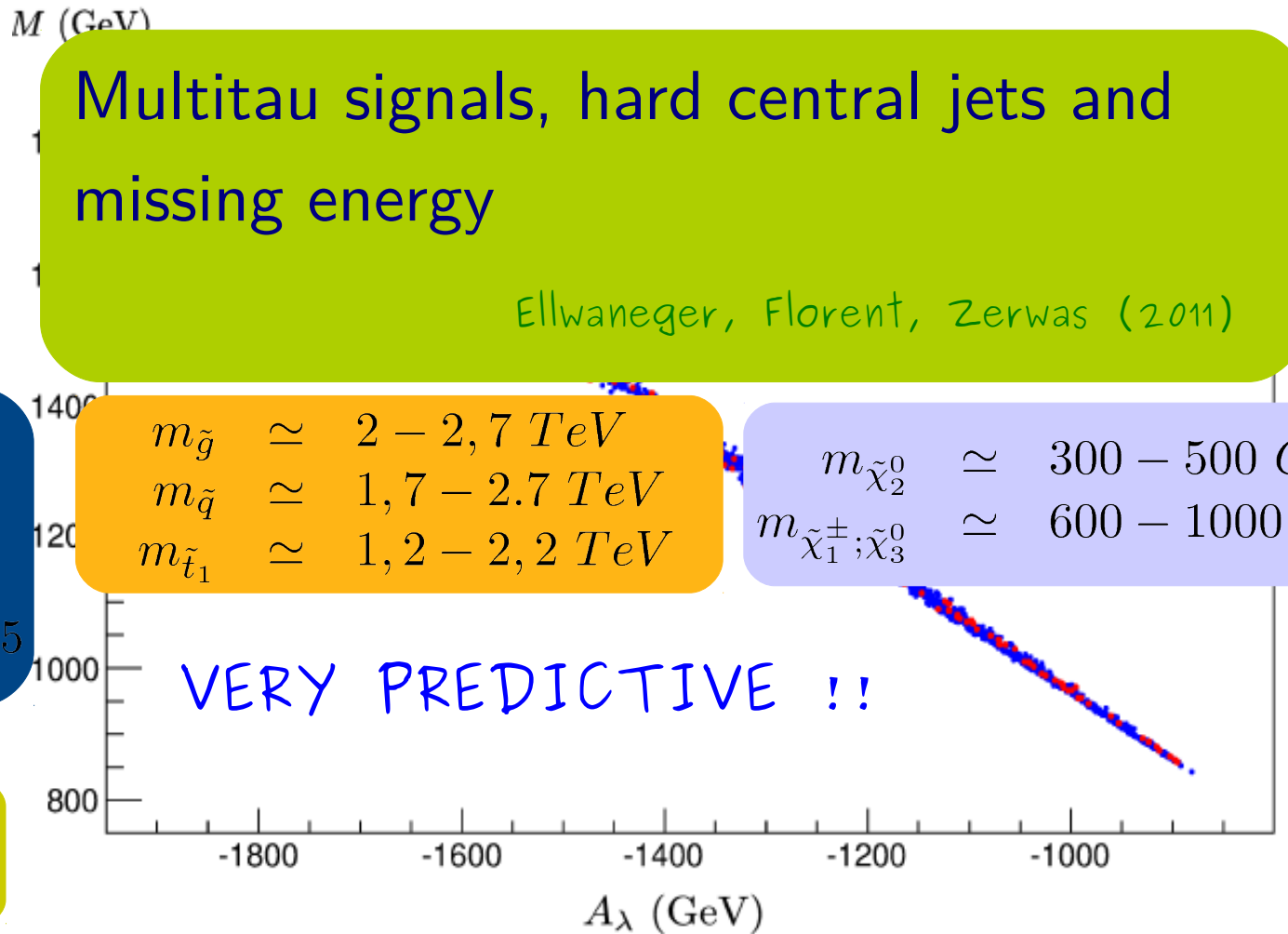
$$m_{\tilde{q}} \simeq 1,7 - 2,7 \text{ TeV}$$

$$m_{\tilde{t}_1} \simeq 1,2 - 2,2 \text{ TeV}$$

$$m_{\tilde{\chi}_2^0} \simeq 300 - 500 \text{ GeV}$$

$$m_{\tilde{\chi}_1^\pm; \tilde{\chi}_3^0} \simeq 600 - 1000 \text{ GeV}$$

VERY PREDICTIVE !!



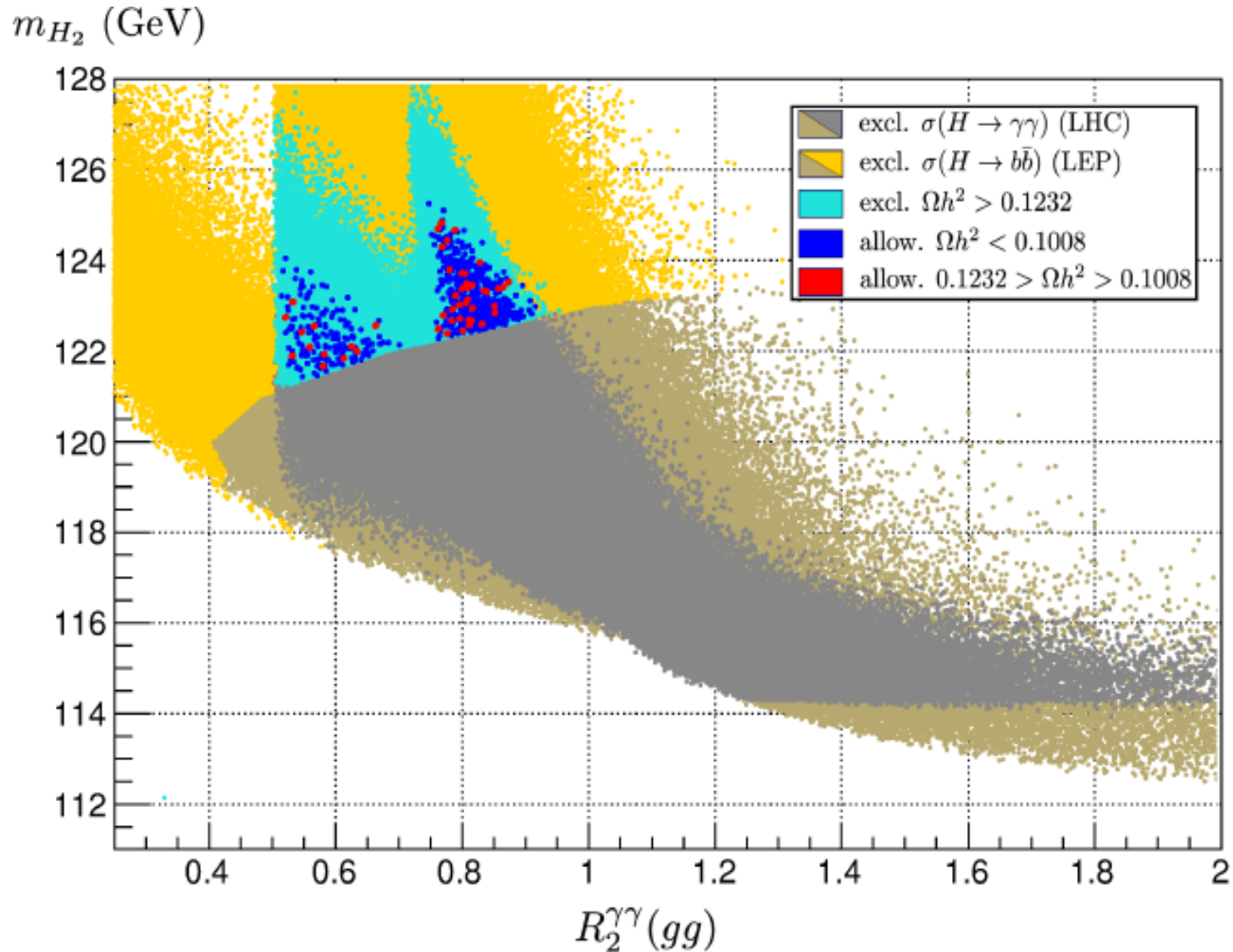
L.A., Camara, Cerdeño, Ibañez, Valenzuela (2012)

# Conclusions

- We have analyzed a **constrained version of the NMSSM** with boundary conditions obtained from the assumption of **modulus dominance SUSY** breaking in **F-theory SU(5) GUT's**.
- Requiring **EWSB**, Dark Matter, Flavor observables, **LEP and LHC limits** we have a **very predictive model**
  - **Small  $\lambda$  and  $\kappa$**  parameters ( $\leq 0,1$ )
  - **Large  $\tan\beta$** .
  - **Singlet dominant  $m_{H1} = 100 \text{ GeV}$**  (LEP excess) and  **$m_{H2} = 125 \text{ GeV}$**
  - **$B \rightarrow \mu\mu$**  satisfies LHCb results and even below the SM value.
  - Dark matter is the **neutralino (singlino)**. Correct relic density thanks to coannihilation with NLSP (stau).
  - **Detectable** at LHC.

Backup slides

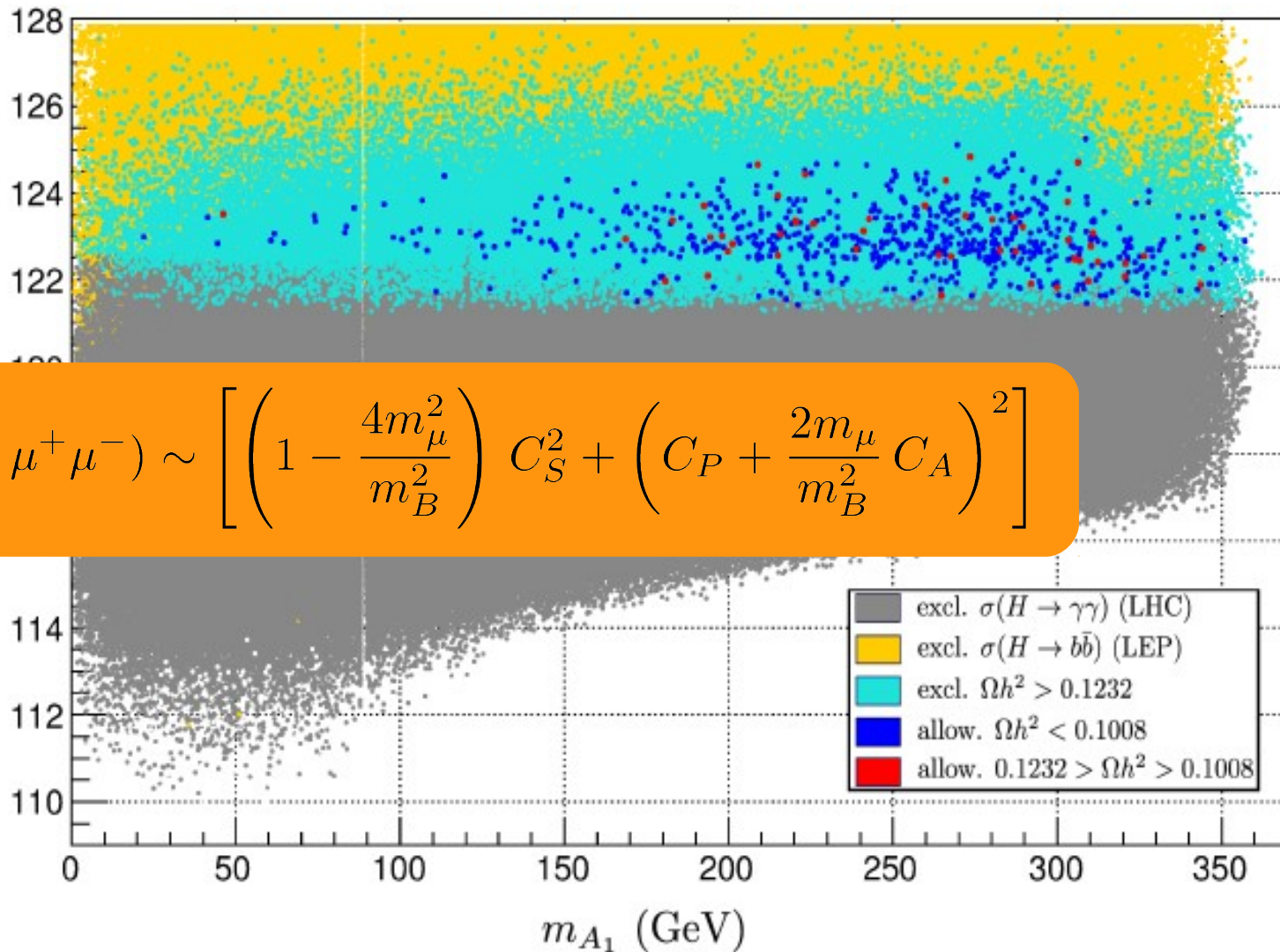
# T-modulus dominated NMSSM



L.A., Camara, Cerdeño, Ibañez, Valenzuela (2012)

# T-modulus dominated NMSSM

$m_{H_2}$  (GeV)



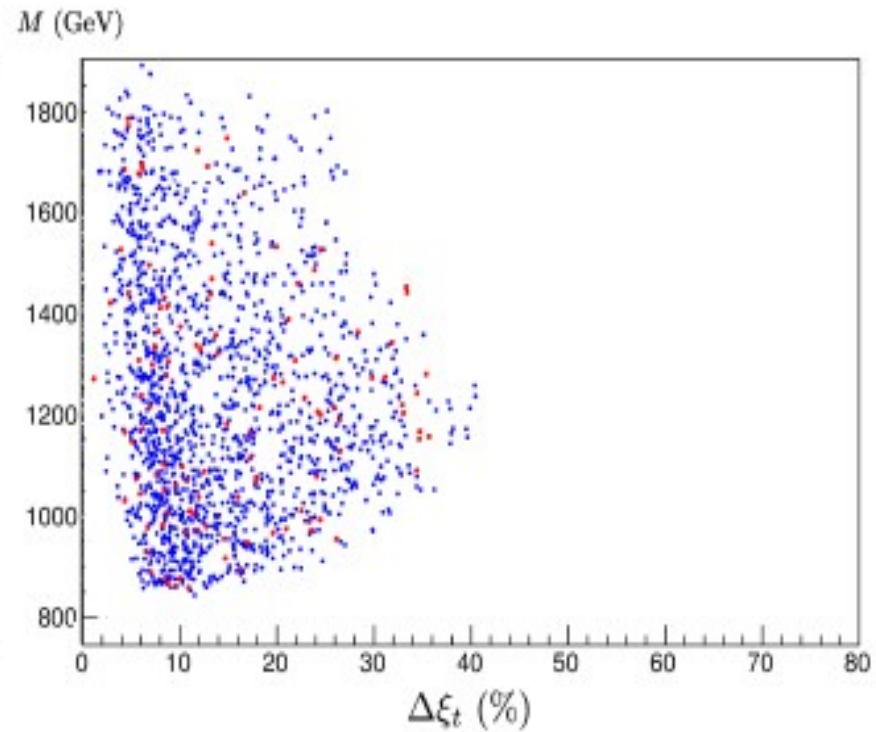
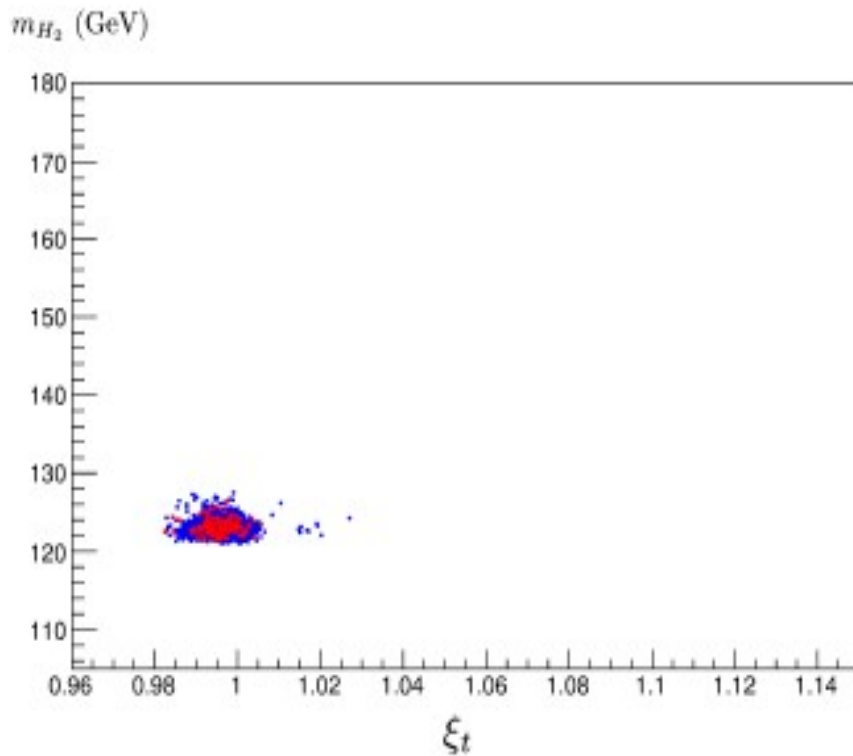
L.A., Camara, Cerdeño, Ibañez, Valenzuela (2012)

# T-modulus dominated NMSSM

$$K_S = \frac{t_S^{1/2} t^{1-\xi_t}}{t_b}$$



$$\begin{aligned} A_\lambda &= -M(2 - \xi_t - \rho_H) \\ A_\kappa &= -3M(1 - \xi_t) \\ m_S^2 &= |M|^2(1 - \xi_t) \end{aligned}$$



# T-modulus dominated NMSSM

| Point | $\bar{g}$ | $\bar{Q}_{R,L}$ | $\bar{t}_{1,2}$ | $\bar{b}_{1,2}$ | $\bar{L}_{R,L}$ | $\bar{\tau}_{1,2}$ | $\bar{\chi}_i^0$               | $\bar{\chi}_i^+$ | $m_{H_i}$             | $m_{A_i}$   | $m_{H^+}$ |
|-------|-----------|-----------------|-----------------|-----------------|-----------------|--------------------|--------------------------------|------------------|-----------------------|-------------|-----------|
| $P_1$ | 1921      | 1758<br>1827    | 1263<br>1558    | 1481<br>1583    | 684<br>827      | 230<br>719         | 213<br>367; 696<br>1238; 1243  | 696<br>1244      | 103<br>172.4<br>1016  | 321<br>1016 | 1019      |
| $P_2$ | 1983      | 1814<br>1886    | 1302<br>1601    | 1521<br>1626    | 708<br>855      | 175<br>735         | 164<br>381; 721<br>1274; 1279  | 721<br>1279      | 98.1<br>173.4<br>1036 | 220<br>1036 | 1040      |
| $P_3$ | 2716      | 1989<br>2069    | 1434<br>1749    | 1673<br>1778    | 782<br>944      | 199<br>807         | 189<br>423; 800<br>1394; 1400  | 800<br>1400      | 96.9<br>174.8<br>1131 | 273<br>1131 | 1134      |
| $P_4$ | 2236      | 2042<br>2125    | 1499<br>1802    | 1718<br>1827    | 804<br>971      | 197<br>831         | 186<br>436; 824<br>1440; 1444  | 824<br>1445      | 97.4<br>174.3<br>1095 | 266<br>1094 | 1098      |
| $P_5$ | 2289      | 2091<br>2175    | 1527<br>1841    | 1762<br>1868    | 825<br>996      | 216<br>851         | 205<br>447; 845<br>1471; 1475  | 845<br>1476      | 97.4<br>174.7<br>1148 | 306<br>1148 | 1151      |
| $P_6$ | 2585      | 2358<br>2455    | 1728<br>2064    | 1986<br>2095    | 939<br>1133     | 178<br>955         | 167<br>513; 967<br>1653; 1657  | 967<br>1657      | 98.5<br>174.4<br>1274 | 223<br>1274 | 1277      |
| $P_7$ | 2663      | 2428<br>2528    | 1809<br>2134    | 2046<br>2161    | 970<br>1169     | 204<br>990         | 193<br>530; 999<br>1712; 1716  | 999<br>1716      | 93.9<br>173.4<br>1227 | 287<br>1227 | 1230      |
| $P_8$ | 2769      | 2525<br>2629    | 1862<br>2207    | 2127<br>2238    | 1011<br>1219    | 164<br>1023        | 153<br>554; 1043<br>1770; 1774 | 1043<br>1774     | 97.9<br>173.7<br>1330 | 192<br>1329 | 1332      |

L.A., Camara, Cerdeño, Ibañez, Valenzuela (2012)



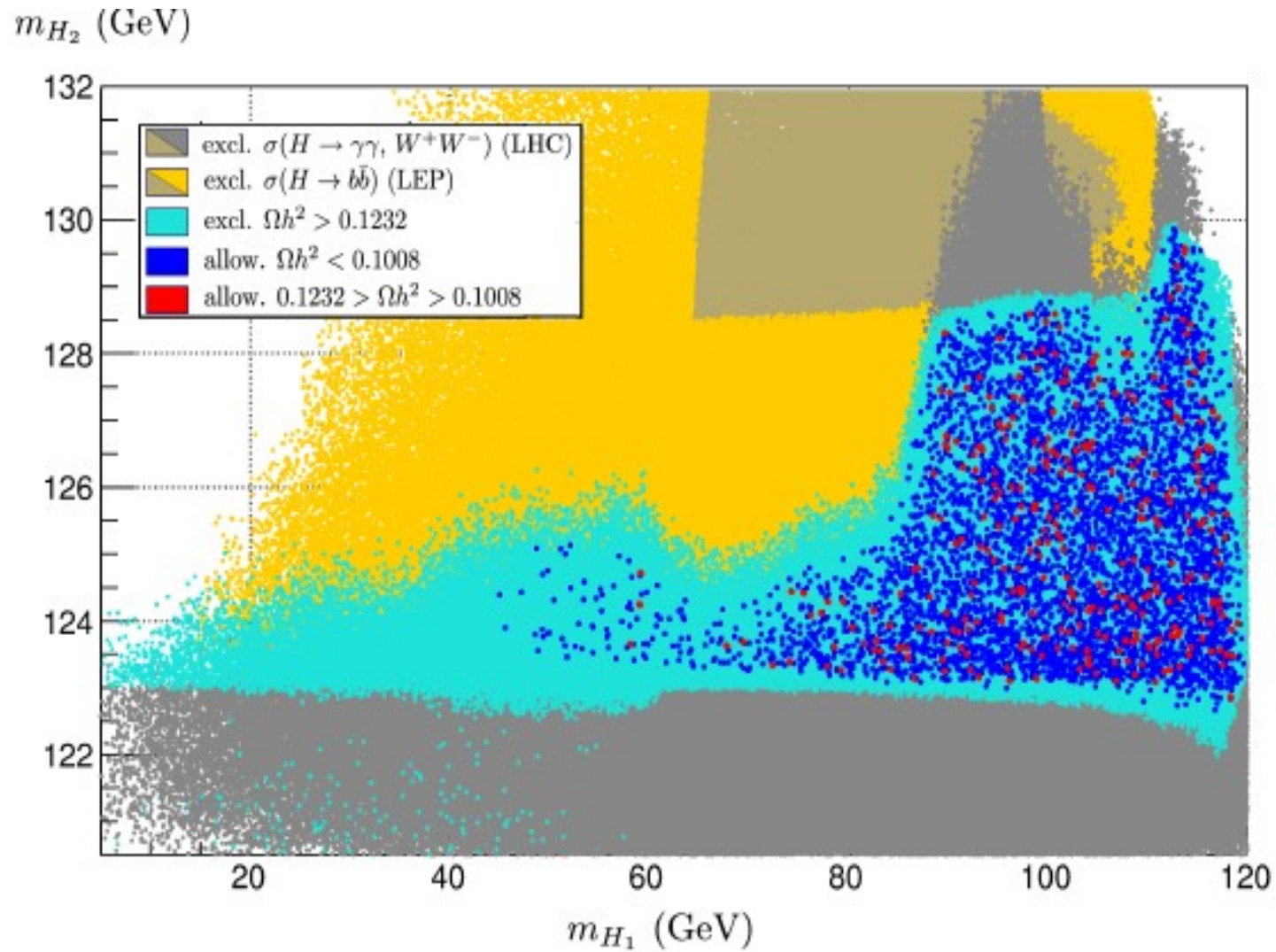
# T-modulus dominated NMSSM

| Point | M      | $\tan \beta$ | $\rho_H$ | $\lambda^{GUT}$     | $\kappa^{GUT}$      | $A_\lambda^{GUT}$ | $A_\kappa^{GUT}$ | $m_S^{GUT}$ |
|-------|--------|--------------|----------|---------------------|---------------------|-------------------|------------------|-------------|
| $P_1$ | 858.2  | 47.5         | 0.035    | $5.2 \cdot 10^{-3}$ | $4.1 \cdot 10^{-4}$ | -895.4            | -319.2           | 105.9       |
| $P_2$ | 888.0  | 49.0         | 0.0092   | $6.5 \cdot 10^{-3}$ | $3.8 \cdot 10^{-4}$ | -922.9            | -195.6           | 50.0        |
| $P_3$ | 981.4  | 49.5         | 0.021    | $6.7 \cdot 10^{-3}$ | $4.1 \cdot 10^{-4}$ | -1015.7           | -262.2           | 82.9        |
| $P_4$ | 1009.9 | 52.9         | 0.195    | $6.4 \cdot 10^{-3}$ | $3.7 \cdot 10^{-4}$ | -1045.7           | -252.7           | 78.5        |
| $P_5$ | 1036.0 | 51.5         | 0.135    | $6.3 \cdot 10^{-3}$ | $3.9 \cdot 10^{-4}$ | -1070.3           | -303.1           | 99.9        |
| $P_6$ | 1180.5 | 53.3         | 0.030    | $5.5 \cdot 10^{-3}$ | $2.5 \cdot 10^{-4}$ | -1204.2           | -198.2           | 50.6        |
| $P_7$ | 1218.5 | 56.8         | 0.30     | $5.7 \cdot 10^{-3}$ | $2.8 \cdot 10^{-4}$ | -1257.9           | -281.6           | 91.9        |
| $P_8$ | 1271.0 | 55.1         | 0.182    | $5.1 \cdot 10^{-3}$ | $1.9 \cdot 10^{-4}$ | -1290.0           | -160.5           | 22.7        |

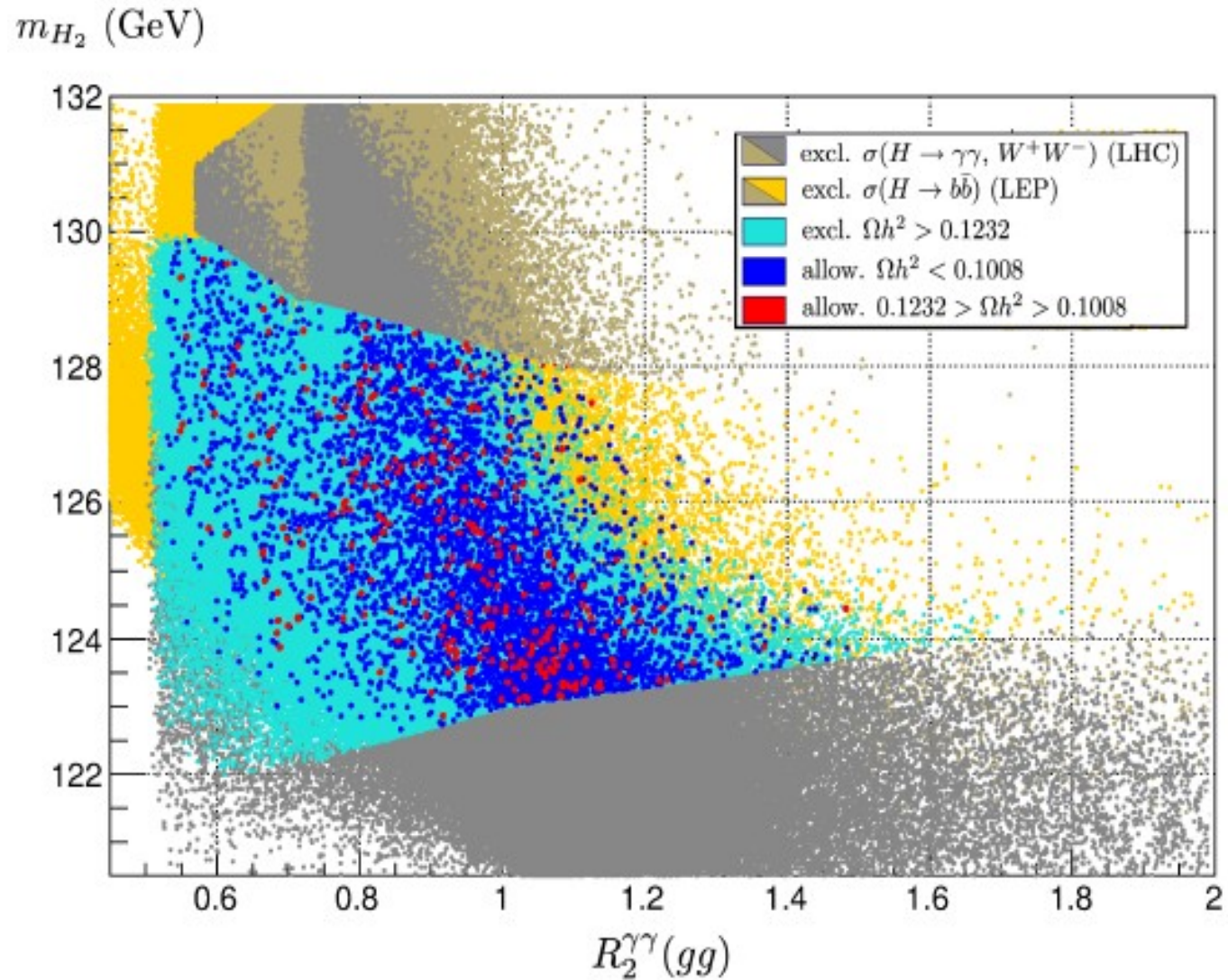
| Point | $\lambda^{SUSY}$    | $\kappa^{SUSY}$     | $A_\lambda^{SUSY}$ | $A_\kappa^{SUSY}$ | $m_S^{SUSY}$ | $\mu_{eff}$ |
|-------|---------------------|---------------------|--------------------|-------------------|--------------|-------------|
| $P_1$ | $4.8 \cdot 10^{-3}$ | $4.1 \cdot 10^{-4}$ | -107.0             | -319.1            | 105.8        | 1243        |
| $P_2$ | $5.9 \cdot 10^{-3}$ | $3.8 \cdot 10^{-4}$ | -84.3              | -195.5            | 49.9         | 1280        |
| $P_3$ | $6.1 \cdot 10^{-3}$ | $4.1 \cdot 10^{-4}$ | -97.2              | -262.2            | 82.8         | 1401        |
| $P_4$ | $5.7 \cdot 10^{-3}$ | $3.7 \cdot 10^{-4}$ | -98.9              | -252.6            | 78.4         | 1447        |
| $P_5$ | $5.7 \cdot 10^{-3}$ | $4.0 \cdot 10^{-4}$ | -107.3             | -303              | 99.9         | 1478        |
| $P_6$ | $4.9 \cdot 10^{-3}$ | $2.5 \cdot 10^{-4}$ | -91.0              | -198.2            | 50.5         | 1662        |
| $P_7$ | $4.9 \cdot 10^{-3}$ | $2.8 \cdot 10^{-4}$ | -107.3             | -281.5            | 91.9         | 1723        |
| $P_8$ | $4.5 \cdot 10^{-3}$ | $1.9 \cdot 10^{-4}$ | -86.0              | -160.5            | 22.5         | 1780        |

L.A., Camara, Cerdeño, Ibañez, Valenzuela (2012)

# 1-loop



# 1-loop



L.A., Camara, Cerdeño, Ibañez, Valenzuela (2012)