

A portal extension of SM with an unbroken dark $U(1)$

(based on “arXiv: 1303.4280” with Seungwon Baek and Pyungwon Ko)

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Planck 2013, May 21 (2013), Bonn, Germany

Why is the DM stable?

- Stability is guaranteed by a symmetry.

e.g: Z_2 , R-parity, Topology

- A global symmetry is broken by gravitational effects, allowing interactions like

$$-\mathcal{L}_{\text{int}} = \begin{cases} \lambda \frac{\phi}{M_{\text{P}}} F_{\mu\nu} F^{\mu\nu} & \text{for boson} \\ \lambda \frac{1}{M_{\text{P}}} \bar{\psi} \gamma^\mu D_\mu \ell_{Li} H^\dagger & \text{for fermion} \end{cases}$$

Observation requires [M.Ackermann et al. (LAT Collaboration), PRD 86, 022002 (2012)]

$$\tau_{\text{DM}} \gtrsim 10^{26-30} \text{sec} \Rightarrow \begin{cases} m_\phi \lesssim \mathcal{O}(10) \text{keV} \\ m_\psi \lesssim \mathcal{O}(1) \text{GeV} \end{cases}$$

- Weak scale DM requires a local symmetry.

Discrete or continuous?

- Discrete symmetry

- The symmetry may be originated from a **spontaneously broken** continuous symmetry (e.g: local Z_2 -symmetry).
- Dark matter should have **nothing to do with the symmetry breaking**.
- It should be the **lightest odd** particle.

- Continuous symmetry

- It may be from a large gauge group in a UV theory (e.g: $SO(32)$ or $E_8 \times E_8' \rightarrow SU(3)_c \times SU(2)_L \times U(1)_Y \times G_{DS}?$).
- Dark matter should be the **lightest charged** particle.

Unbroken local $U(1)_X$

- **DM self-interaction**

It may solve some puzzles of the collisionless CDM.

- core/cusp problem:

simulated cusp of DM density profile contrary to the cored one found in the observed LSB galaxies and dSphs

- “too big to fail” problem:

simulated high internal density concentration of the subhalos in the MW-sized halos contrary to the observed brightest MW satellites

- **Massless dark photon**

Contributes to the radiation energy in addition to the one from SM.

$$N_{\text{eff}}^{\text{obs}} = 3.30 \pm 0.27 \text{ at } 68\% \text{ (cf., } N_{\text{eff}}^{\text{SM}} = 3.04)$$

⇒ Fractional contribution of dark photon is still allowed.

SM-DM communication

- Kinetic mixing

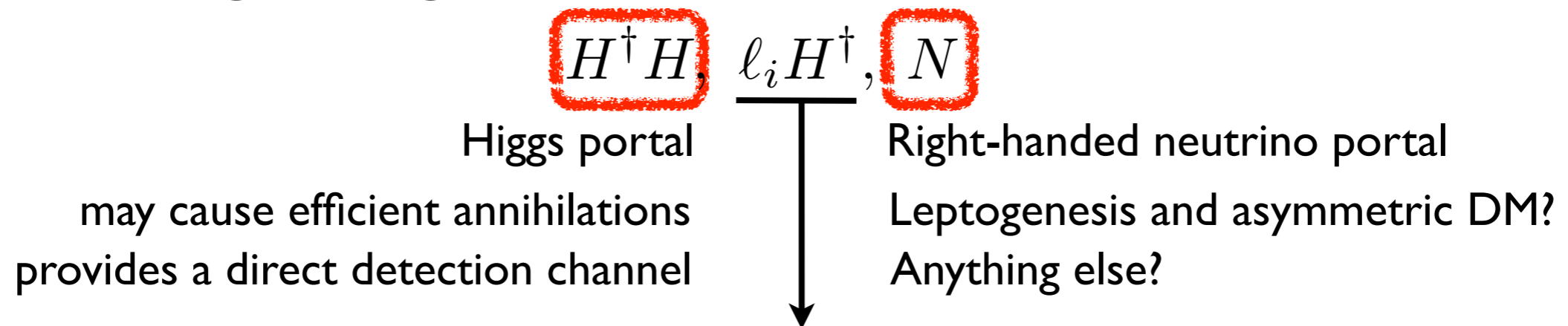
There could be the kinetic mixing between $U(1)_X$ and $U(1)_Y$ of the SM.

⇒ DM becomes **mini-charged** under the electromagnetic interaction.

$$\mathcal{L} \supset -\frac{1}{2} \sin \epsilon X_{\mu\nu} B^{\mu\nu} \quad \Rightarrow \quad q_{\text{em}} = -q_X \frac{g_X}{e} \cos W \tan \epsilon$$

⇒ This opens a direct detection channel.

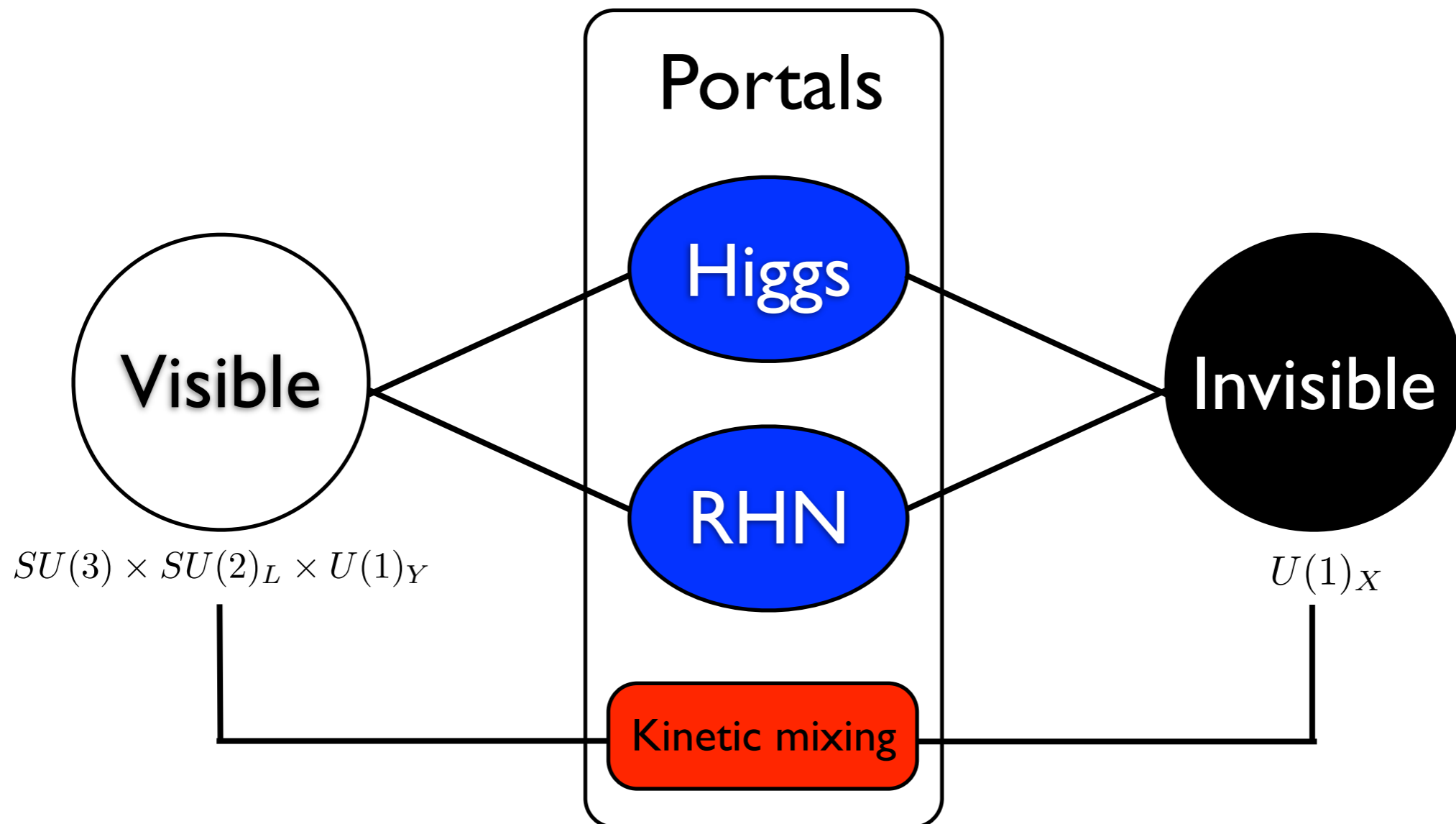
- Gauge-singlets



does not allow renormalizable interactions for a gauge-charged DM

A minimal(?) model

- The structure of the model



- Symmetry

$$SU(3) \times SU(2)_L \times U(1)_Y \times U(1)_X$$

(SM is neutral under $U(1)_X$)

[See also A. Falkowski, J.T. Ruderman & T. Volansky, JHEP1105.016]

- Lagrangian

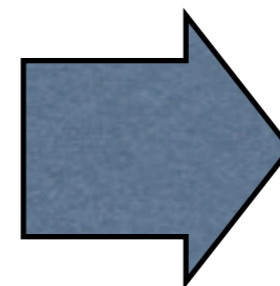
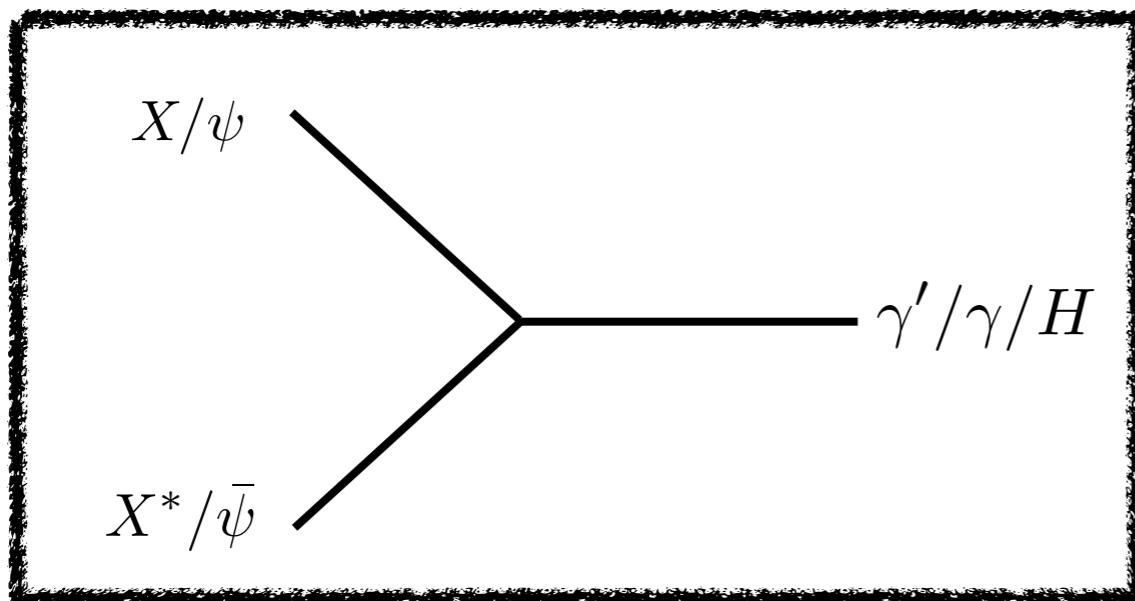
$$\begin{aligned} \mathcal{L} &= \mathcal{L}_{\text{Kinetic}} + \mathcal{L}_{\text{H-portal}} + \mathcal{L}_{\text{RHN-portal}} + \mathcal{L}_{\text{DS}} \\ \mathcal{L}_{\text{Kinetic}} &= i\bar{\psi}\gamma^\mu D_\mu\psi + |D_\mu X|^2 - \frac{1}{4}X_{\mu\nu}X^{\mu\nu} - \frac{1}{2}\sin\epsilon X_{\mu\nu}B^{\mu\nu} \\ -\mathcal{L}_{\text{H-portal}} &= \frac{1}{2}\lambda_{HX}|X|^2 H^\dagger H \\ -\mathcal{L}_{\text{RHN-portal}} &= \frac{1}{2}M_i N_{Ri}^{\bar{C}} N_{Ri} + [Y_\nu^{ij} N_{Ri}^{\bar{C}} \ell_{Lj} H^\dagger + \lambda^i N_{Ri}^{\bar{C}} \psi X^\dagger + \text{H.c.}] \\ -\mathcal{L}_{\text{DS}} &= m_\psi \bar{\psi}\psi + m_X^2 |X|^2 + \frac{1}{4}\lambda_X |X|^4 \end{aligned}$$

$$(q_L, q_X) : N = (1, 0), \psi = (1, 1), X = (0, 1)$$

● Interaction vertices of dark particles (X, ψ)

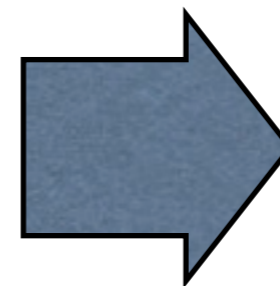
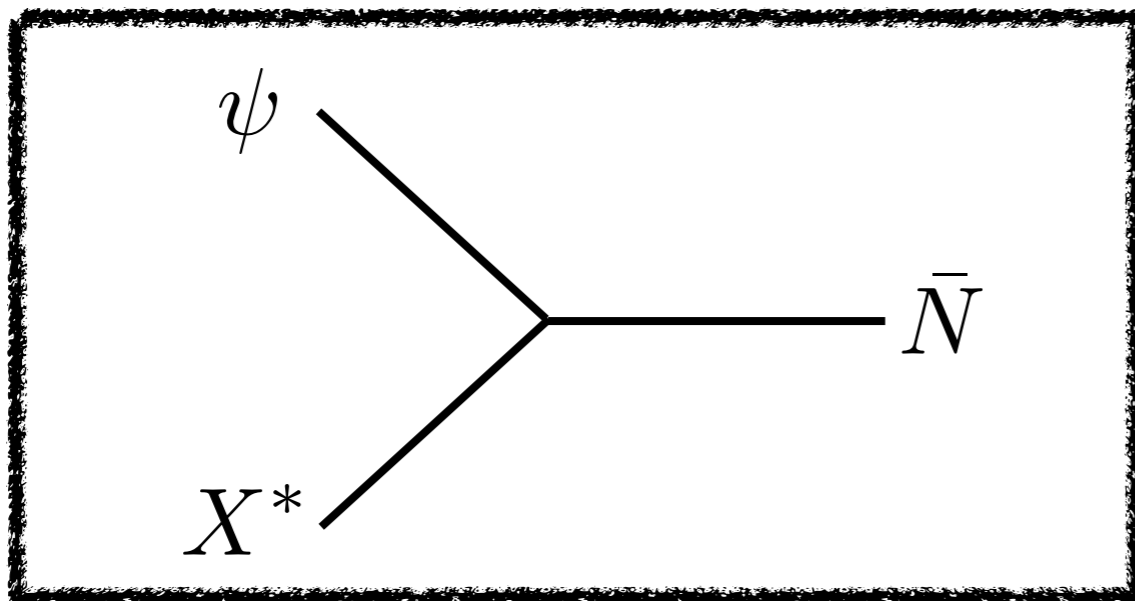
Kinetic term diagonalization:
$$\begin{pmatrix} \hat{B}^\mu \\ \hat{X}^\mu \end{pmatrix} = \begin{pmatrix} 1/\cos\epsilon & 0 \\ -\tan\epsilon & 1 \end{pmatrix} \begin{pmatrix} B^\mu \\ X^\mu \end{pmatrix}$$

$\Rightarrow \mathcal{L}_{\text{DS-SM}} = g_X q_X t_\epsilon \bar{\psi} \gamma^\mu \psi (c_W A_\mu - s_W Z_\mu) + |[\partial_\mu - ig_X q_X t_\epsilon (c_W A_\mu - s_W Z_\mu)] X|^2$



Annihilation
or
scattering

(\Rightarrow Relic density, direct/indirect searches)



Decay of ψ or X

(\Rightarrow Lepto/darkogenesis?)

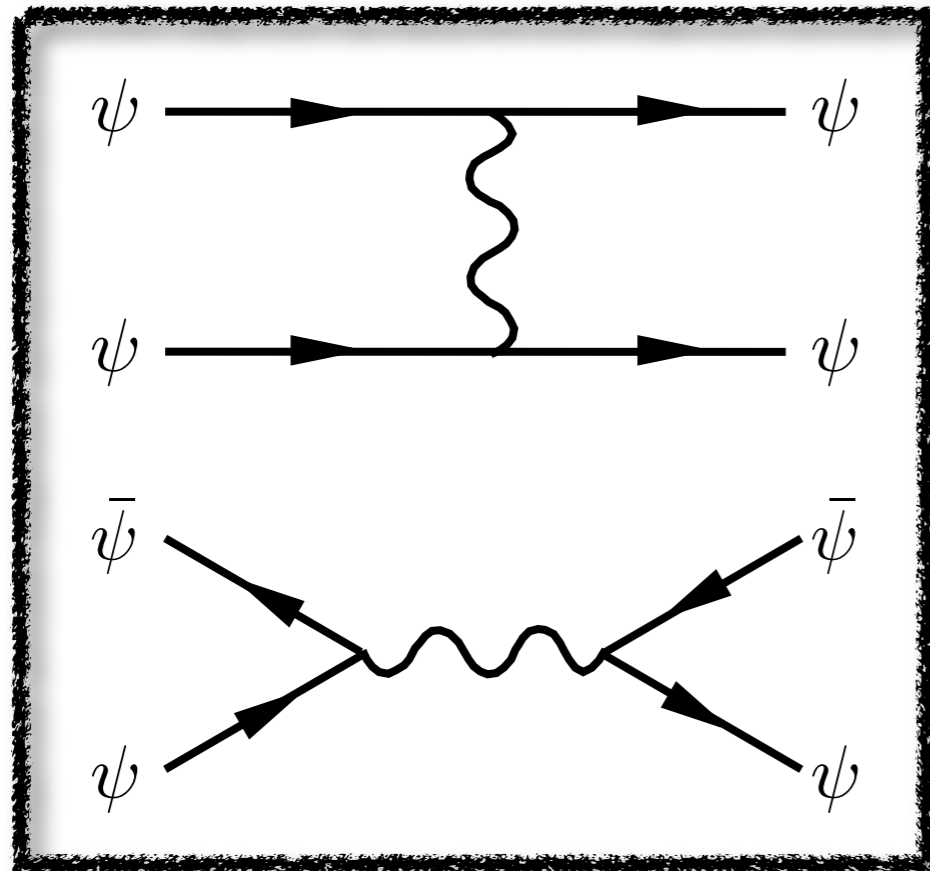
Constraints

Our model can address

- * Some small scale puzzles of CDM (Dark matter self-interaction) (α_X, m_X)
- * CDM relic density (Unbroken dark $U(1)_X$) ($\lambda, \lambda_{hx}, m_X,$)
- * Vacuum stability of Higgs potential (Positive scalar loop correction) (λ_{hx})
- * Direct detection (Photon and Higgs exchange)(ϵ, λ_{hx})
- * Dark radiation (Massless photon)(α_X)
- * Lepto/darkogenesis (Asymmetric origin of dark matter) (Y_ν, λ, M_I, m_X)
- * Inflation (Higgs inflation type) (λ_{hx}, λ_X)

In other words, the model is highly constrained.

● Constraints on dark gauge coupling

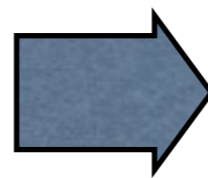


$$\Rightarrow \sigma_T \sim \frac{16\pi\alpha_X^2}{m_{X(\psi)}^2} \frac{1}{v^4} \ln \left[\frac{m_{X(\psi)}^2 v^3}{\sqrt{4\pi\rho_{X(\psi)}\alpha_X^3}} \right]$$

From inner structure and kinematics of dwarf galaxies,

$$\sigma_T^{\max} / m_{\text{dm}} \lesssim 35 \text{ cm}^2 / \text{g}$$

[Vogelsberger, Zavala and Leeb, 1201.5892]



$$\alpha_X \lesssim 5 \times 10^{-5} \left(\frac{m_{X(\psi)}}{300\text{GeV}} \right)^{3/2}$$

If stable, $\Omega_\psi \sim 10^4 \left(\frac{300\text{GeV}}{m_\psi} \right)$. It is too much for CDM relic density at present.

Therefore, Ψ should be able to decay $\Rightarrow m_\Psi > m_X$

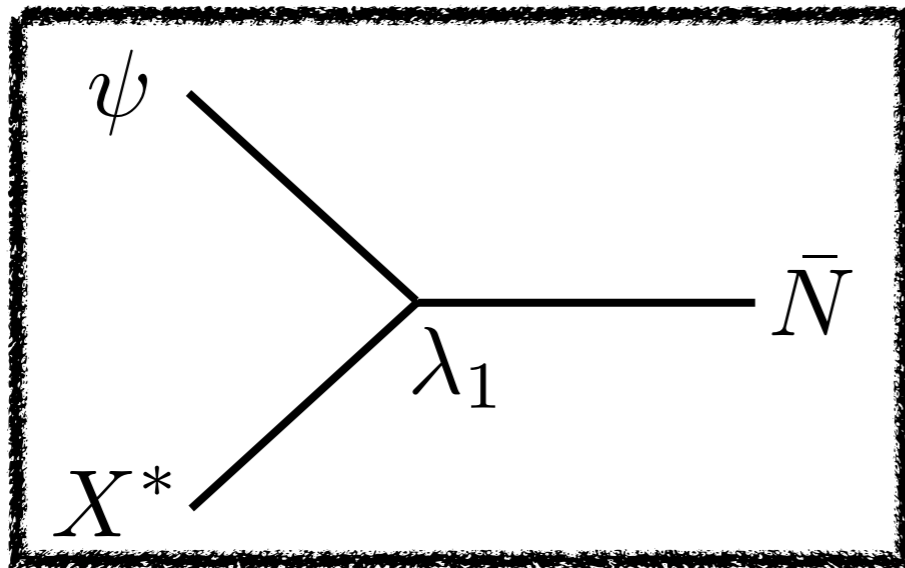
“X” is responsible for the present CDM relic density.

For α_X close to its upper bound, X - X^* can explain some puzzles of collisionless CDM:

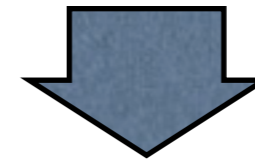
(i) cored profile of dwarf galaxies.

(ii) low concentration of LSB galaxies and dwarf galaxies. [Vogelsberger, Zavala and Leeb, 1201.5892]

- CDM relic density



The late-time decay of ψ



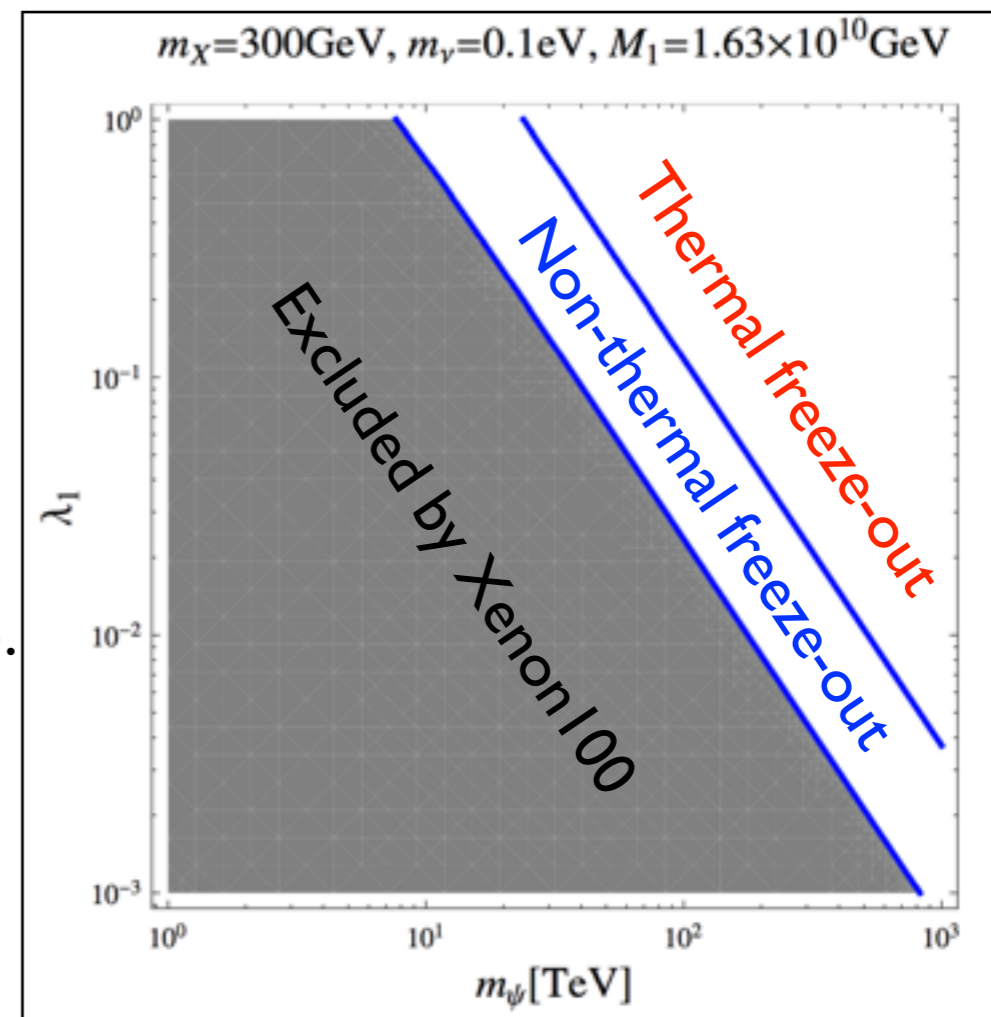
(Non-) thermal freeze-out of X via Higgs portal

$$\lambda_1^2 \simeq 58.5 \left(\frac{0.1 \text{ eV}}{\tilde{m}_\nu} \right) \left(\frac{M_1}{10^9 \text{ GeV}} \right) \left(\frac{1 \text{ TeV}}{m_\psi} \right) \left(1 - \frac{m_X^2}{m_\psi^2} \right)^{-2} \left[1 + \frac{1}{48\pi^2} \left(\frac{m_\psi}{v_H} \right)^2 \right]^{-1} \left(\frac{m_X}{300 \text{ GeV}} \right)^2 \left(\frac{\langle \sigma v \rangle_{\text{ann}}^{\text{th}}}{\langle \sigma v \rangle_{\text{ann,d}}^X} \right)^2$$

* Relic density constrains λ_1 .

* X forms a symmetric DM

(although it might be asymmetric before ψ decays).



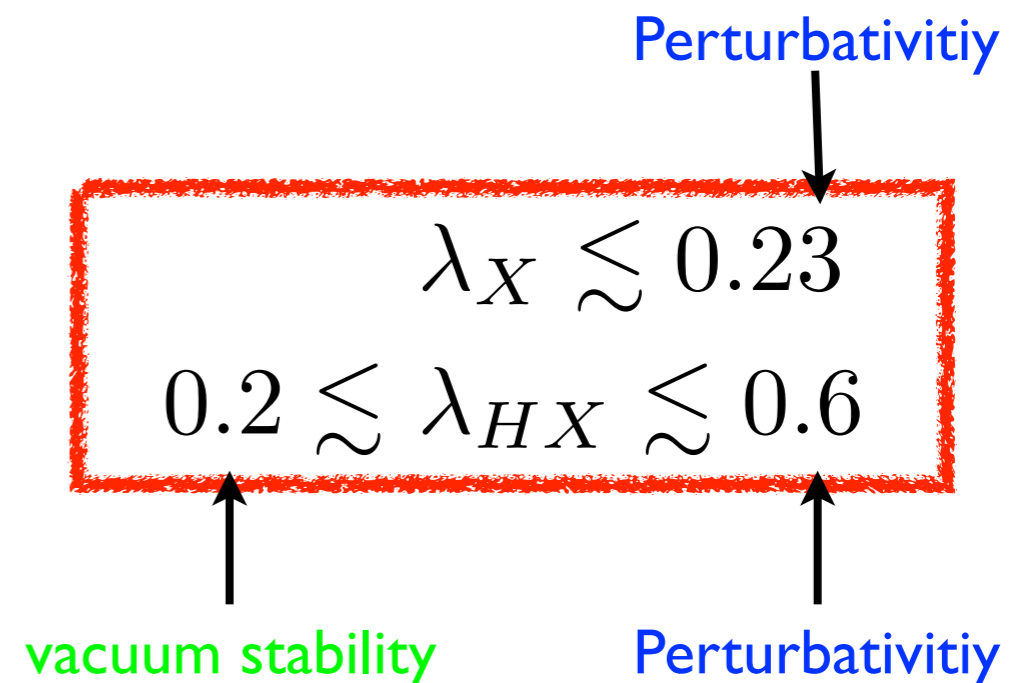
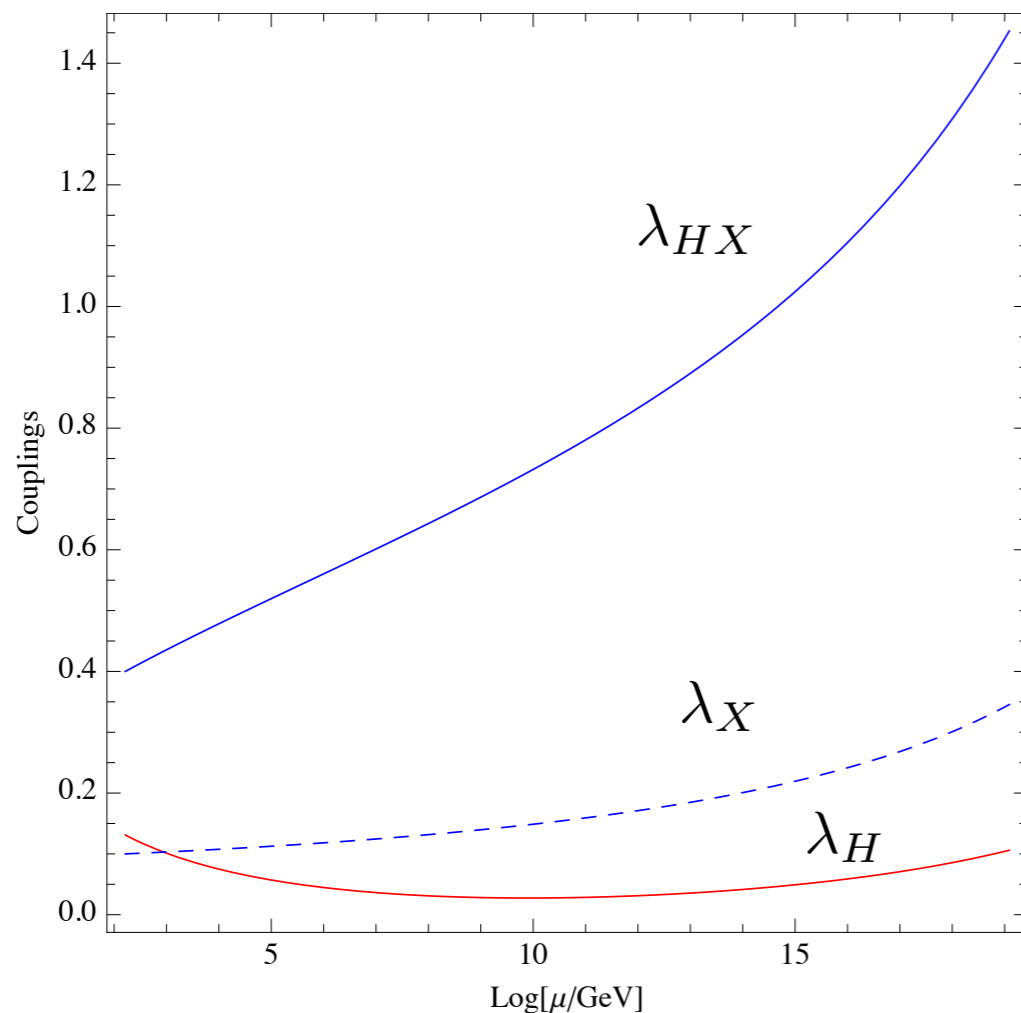
● Vacuum stability (λ_{HX}) [S. Baek, P. Ko, WIP & E. Senaha, JHEP(2012)]

$$\beta_{\lambda_H}^{(1)} = \frac{1}{16\pi^2} \left[24\lambda_H^2 + 12\lambda_H\lambda_t^2 - 6\lambda_t^4 - 3\lambda_H(3g_2^2 + g_1^2) + \frac{3}{8}(2g_2^4 + (g_2^2 + g_1^2)^2) + \frac{1}{2}\lambda_{HS}^2 \right]$$

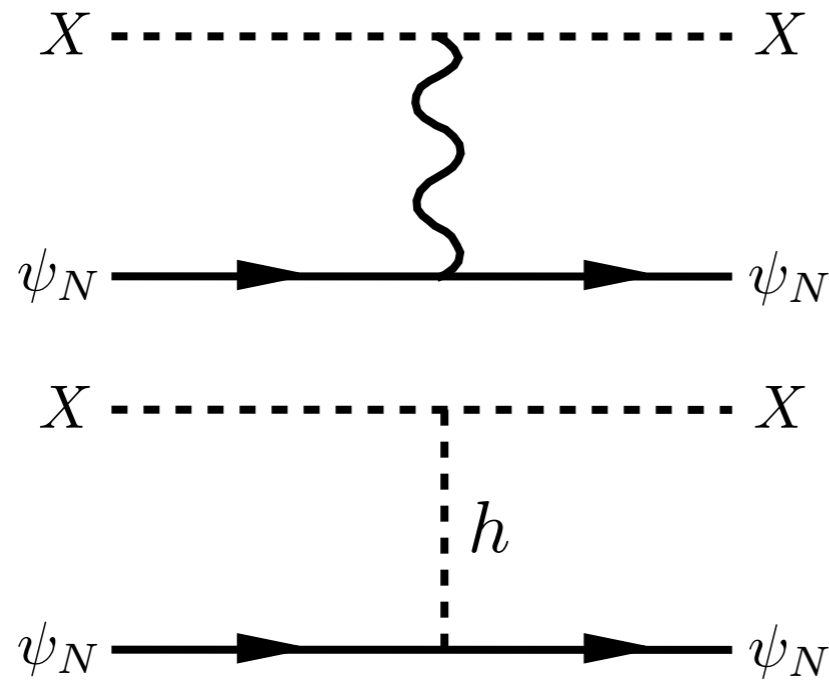
$$\beta_{\lambda_{HS}}^{(1)} = \frac{\lambda_{HS}}{16\pi^2} \left[2(6\lambda_H + 3\lambda_S + 2\lambda_{HS}) - \left(\frac{3}{2}\lambda_H(3g_2^2 + g_1^2) - 6\lambda_t^2 - 4\lambda^2 \right) \right],$$

$$\beta_{\lambda_S}^{(1)} = \frac{1}{16\pi^2} [2\lambda_{HS}^2 + 18\lambda_S^2 + 8\lambda_S\lambda^2 - 8\lambda^4],$$

with $\lambda_{HS} \rightarrow \lambda_{HX}/2$ and $\lambda_S \rightarrow \lambda_X$

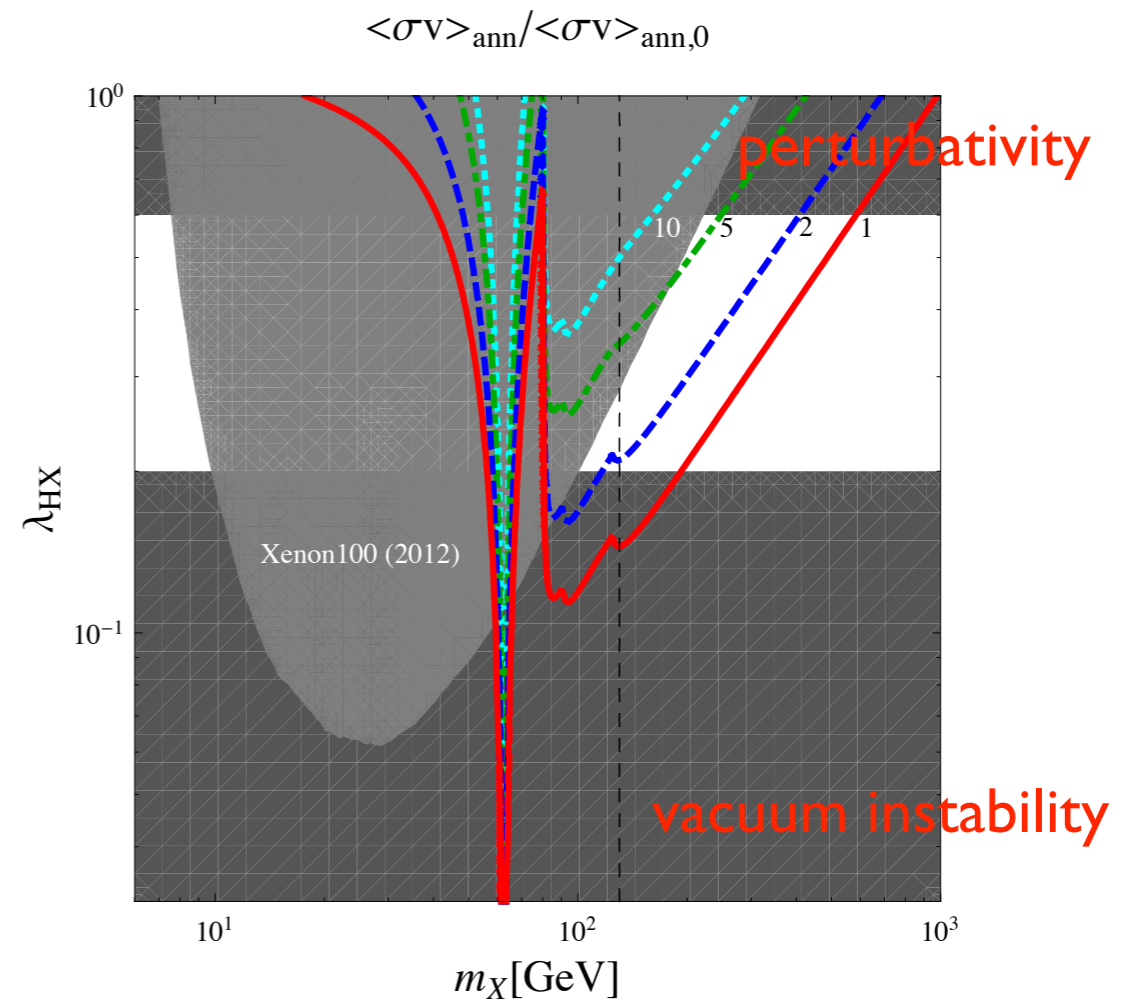
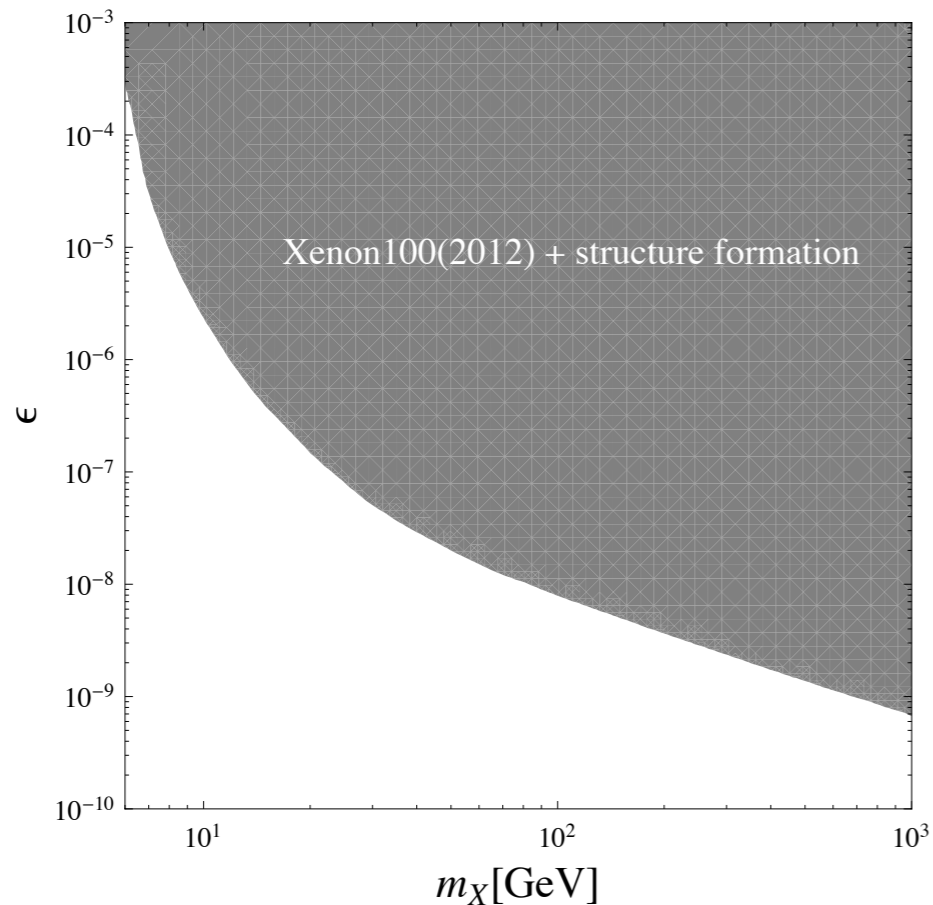


• DM direct search ($\epsilon, \lambda_{hX}, m_X$)



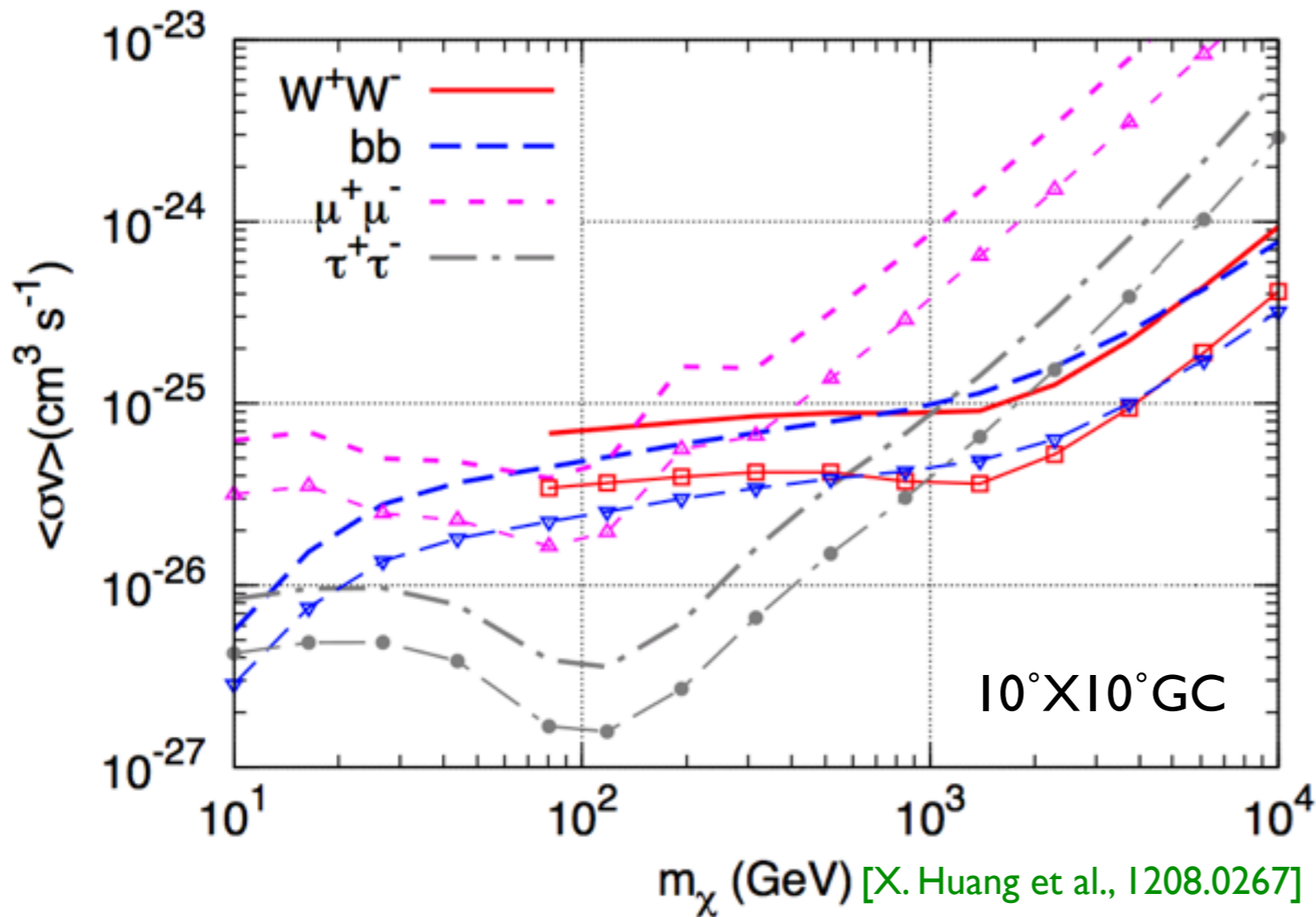
$$\Rightarrow \frac{d\sigma_A}{dE_r} = \frac{2\pi\epsilon_e^2\alpha_{em}^2 Z^2}{m_A E_r^2 v^2} \mathcal{F}_A^2(qr_A)$$

$$\Rightarrow \sigma_{\mathcal{N},h}^{SI} = \frac{\lambda_{HX}^2}{64\pi} \frac{m_r^2 m_{\mathcal{N}}^2}{m_X^2 m_h^4} f_{q,h}^2$$



● Indirect search (λ_{hX}, m_X)

- DM annihilation via Higgs produces a continuum spectrum of γ -rays
- Fermi-LAT γ -ray search data poses a constraint



In our model,

$$\langle\sigma v\rangle_{XX^\dagger \rightarrow W^+W^-}^{\text{obs}} \lesssim 2 \times 7.4 \times 10^{-26} \text{cm}^3/\text{sec}$$

$$\Rightarrow \langle\sigma v\rangle_{\text{ann}}^X \lesssim \frac{2 \times 7.4 \times 10^{-26} \text{cm}^3/\text{sec}}{\text{Br}(XX^\dagger \rightarrow W^+W^-)}$$

$$\Rightarrow 1 \lesssim \frac{\langle\sigma v\rangle_{\text{ann}}^X}{\langle\sigma v\rangle_{\text{ann}}^{\text{th}}} \lesssim 5$$

* Monochromatic γ -ray spectrum?

$$\langle\sigma v\rangle_{\text{ann}}^{\gamma\gamma} \sim 10^{-4} \langle\sigma v\rangle_{\text{ann}}^X \lesssim 10^{-29} \text{cm}^3/\text{sec}$$

Too weak to be seen!

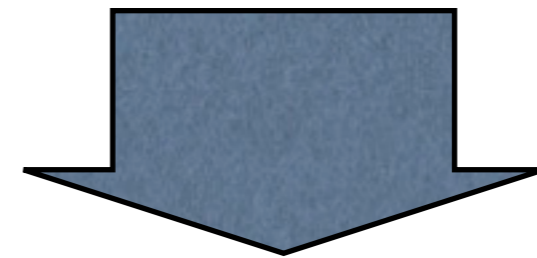
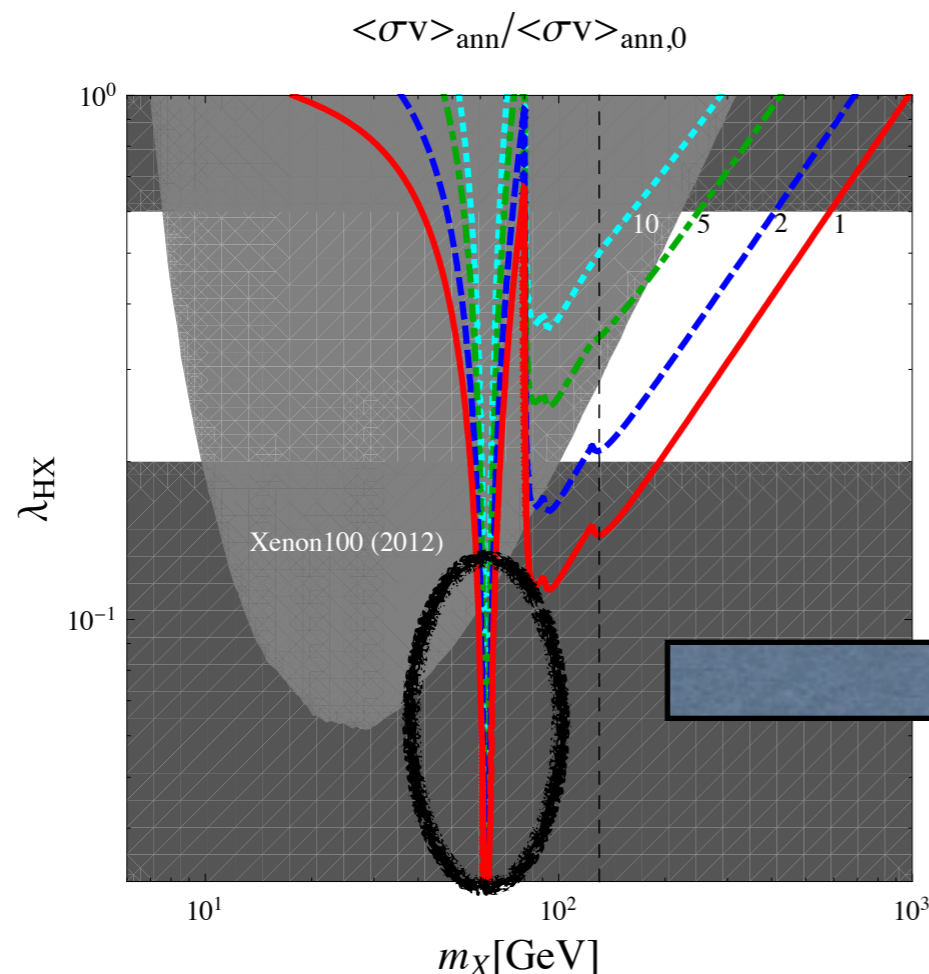
● Collider phenomenology (λ_{hX}, m_X)

Invisible decay rate of Higgs is

$$\Gamma_{h \rightarrow XX^\dagger} = \frac{\lambda_{HX}^2 v^2}{128\pi m_h} \left(1 - \frac{4m_X^2}{m_h^2}\right)^{1/2}$$

SM signal strength at collider is

$$\mu = 1 - \frac{\Gamma_{h \rightarrow XX^\dagger}}{\Gamma_h^{\text{tot}}} \quad \left(\begin{array}{l} \text{cf., } \mu_{\text{ATLAS}} = 1.43 \pm 0.21 \quad \text{for } m_h = 125.5 \text{ GeV} \\ \mu_{\text{CMS}} = 0.8 \pm 0.14 \quad \text{for } m_h = 125.7 \text{ GeV} \end{array} \right)$$



We may need $\text{Br}(h \rightarrow XX^\dagger) \ll \mathcal{O}(10)\%$, i.e.,

$$\lambda_{HX} \ll 0.1$$

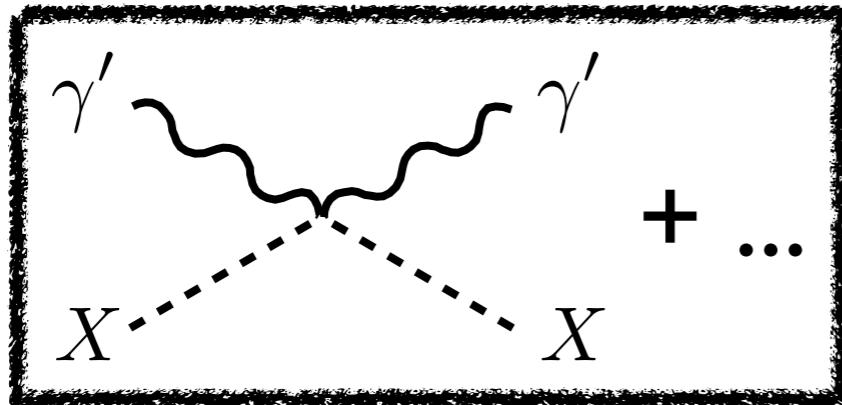
or

$$m_h - 2m_X \lesssim 0.5 \text{ GeV}$$

or kinematically forbidden

- Dark radiation

Decoupling of dark photon



$$\left\{ \begin{array}{l} \Gamma(T_{\gamma'}) = \frac{32\pi^3 \alpha_X^2 T_{\gamma'}^4}{45m_X^3} \Rightarrow T_{\text{dec},\gamma'-X} \gtrsim 16\text{MeV} \\ T_{\text{dec},X-\text{SM}} \sim 1\text{GeV} \Rightarrow T_{\text{dec},\gamma'-\text{SM}} \sim 1\text{GeV} \end{array} \right.$$

of extra relativistic degree of freedom

$$\Delta N_{\text{eff}} = \frac{\rho_{\gamma'}}{\rho_{\nu}} = \frac{g_{\gamma'}}{g_{\nu}} \left(\frac{T_{\gamma,0}}{T_{\nu,0}} \right)^4 \left(\frac{T_{\gamma',\text{dec}}}{T_{\gamma,\text{dec}}} \right)^4 \left(\frac{g_{*S}(T_{\gamma,0})}{g_{*S}(T_{\gamma,\text{dec}})} \right)^{4/3}$$

$$\frac{T_{\nu,0}}{T_{\gamma,0}} = \begin{cases} \left(\frac{4}{11}\right)^{1/3} & \text{for } T_{\text{dec}} \gtrsim 1\text{MeV} \\ 1 & \text{for } T_{\text{dec}} \lesssim 1\text{MeV} \end{cases}$$

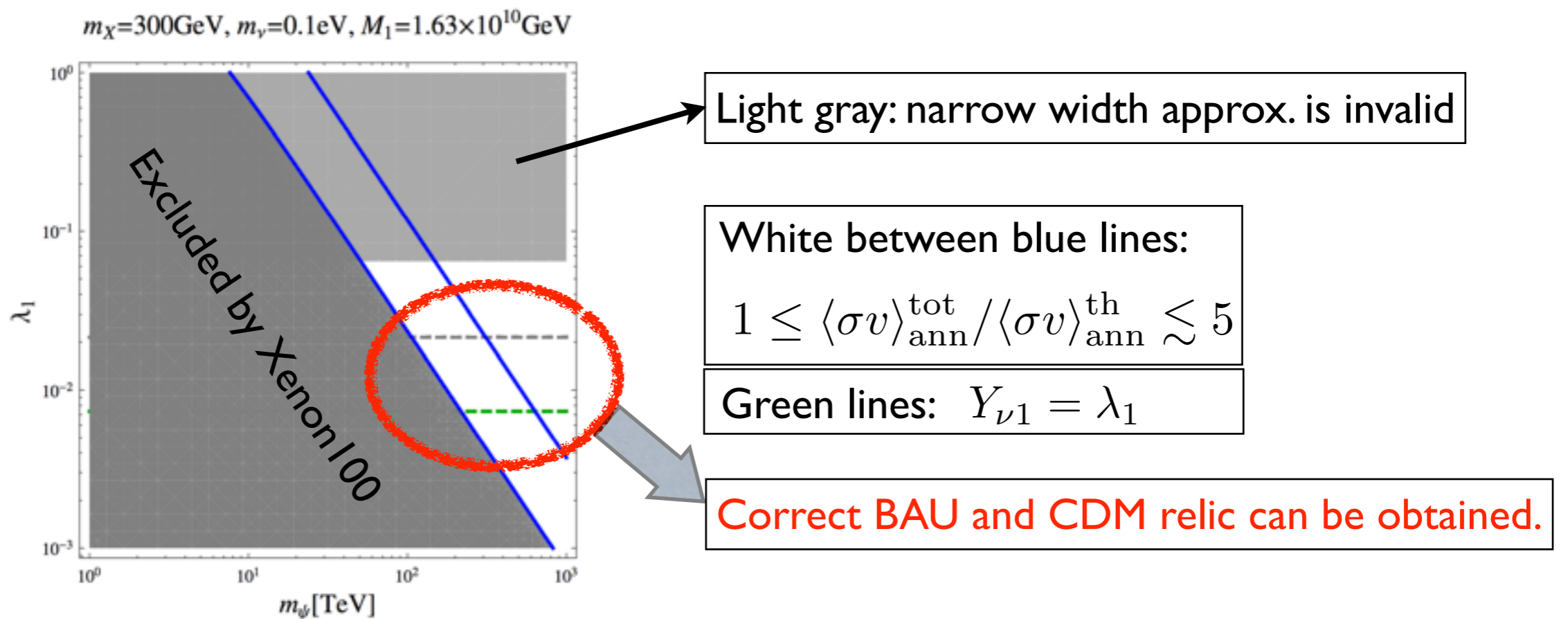
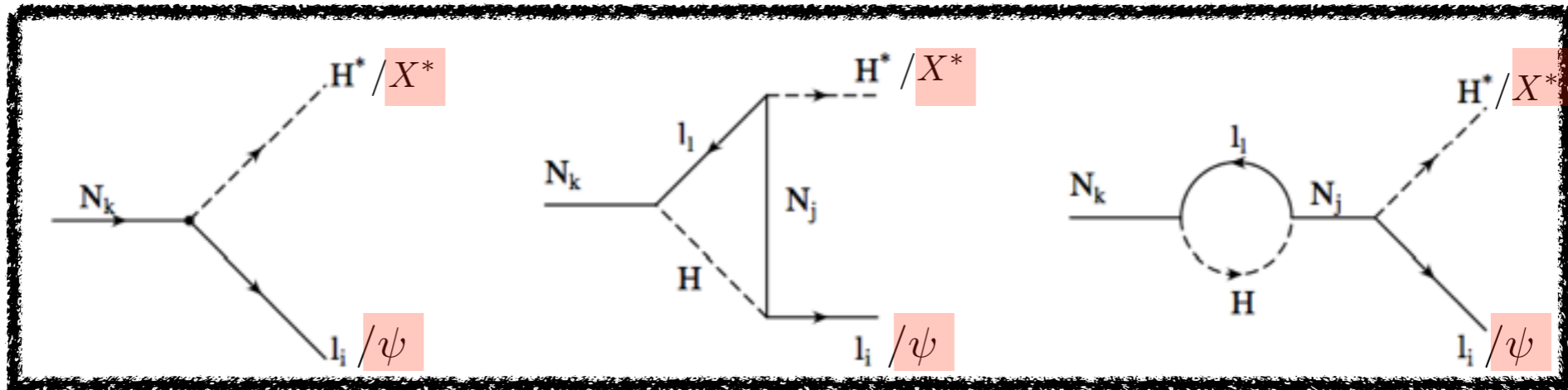
$$\Delta N_{\text{eff}} = 0.474_{-0.45}^{+0.48} \text{ at 95\% CL (Planck+WP+highL+H}_0\text{+BAO)}$$

[Planck Collaboration, arXiv:1303.5076]

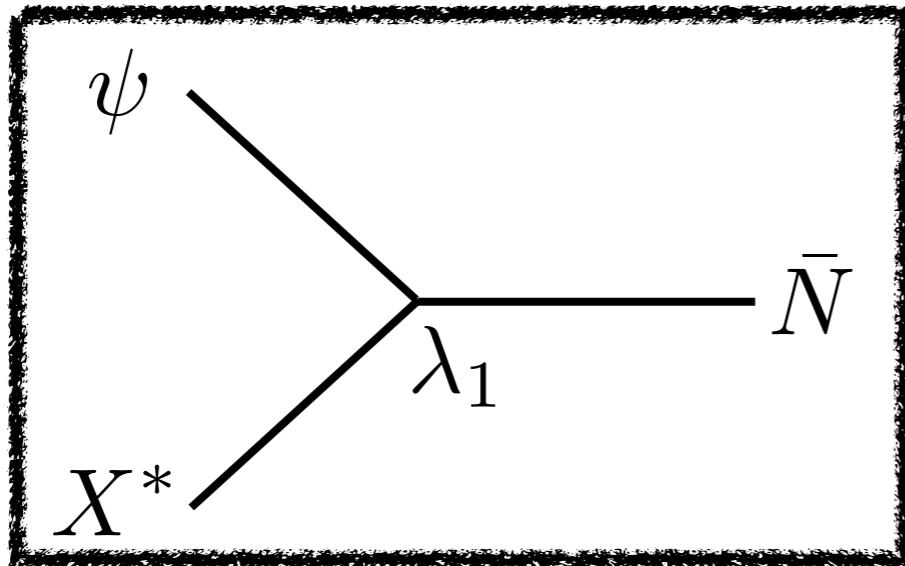
$$T_{\text{dec},\gamma'-\text{SM}} \sim 1\text{GeV} \Rightarrow \Delta N_{\text{eff}} = \frac{2}{2\frac{7}{8}} \left(\frac{11}{4} \right)^{4/3} \left(\frac{g_{*S}(T_{\gamma,0})}{g_{*S}(T_{\text{dec},X_{\mu}})} \right)^{4/3} \sim 0.06$$

Lepto/darkogenesis

- Lepto/darkogenesis from the decay of RHN



- Leptogenesis from the late-time decay of ψ & ψ -bar

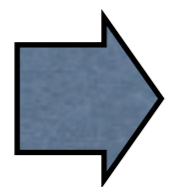


Late-time decay \rightarrow No wash-out!



$$\Delta(Y_{\Delta L}) = 2\epsilon_L Y_\psi(T_{\text{fz}}^\psi)$$

$$Y_\psi(T_{\text{fz}}^\psi) = \frac{3.79 (\sqrt{8\pi})^{-1} g_*^{1/2} / g_* S x_{\text{fz}}^\psi}{m_\psi M_{\text{P}} \langle \sigma v \rangle_{\text{ann}}^\psi} \simeq 0.05 \frac{x_{\text{fz}}^\psi}{\alpha_X^2} \frac{m_\psi}{M_{\text{P}}}$$



$$\frac{\Delta(Y_{\Delta L})}{Y_{\Delta L}} \simeq 2 \times 10^7 \frac{x_{\text{fz}}^\psi}{\alpha_X^2} \frac{m_\psi}{M_{\text{P}}} \frac{M_1 m_\nu^{\text{max}}}{v_H^2} \times \begin{cases} 1 & \text{for } \text{Br}_L \gg \text{Br}_\psi \\ \sqrt{\lambda_2^2 M_1 / \lambda_1^2 M_2} & \text{for } \text{Br}_L \ll \text{Br}_\psi \end{cases}$$

(e.g : $\epsilon_L \sim 10^{-7}$, $\alpha_X \sim 10^{-5}$, $m_\psi \sim 10^3 \text{ TeV} \rightarrow \frac{\Delta(Y_{\Delta L})}{Y_{\Delta L}} \sim 0.3$)

* Late-time decays of **symmetric ψ and ψ -bar** can generate a sizable amount of lepton number asymmetry.

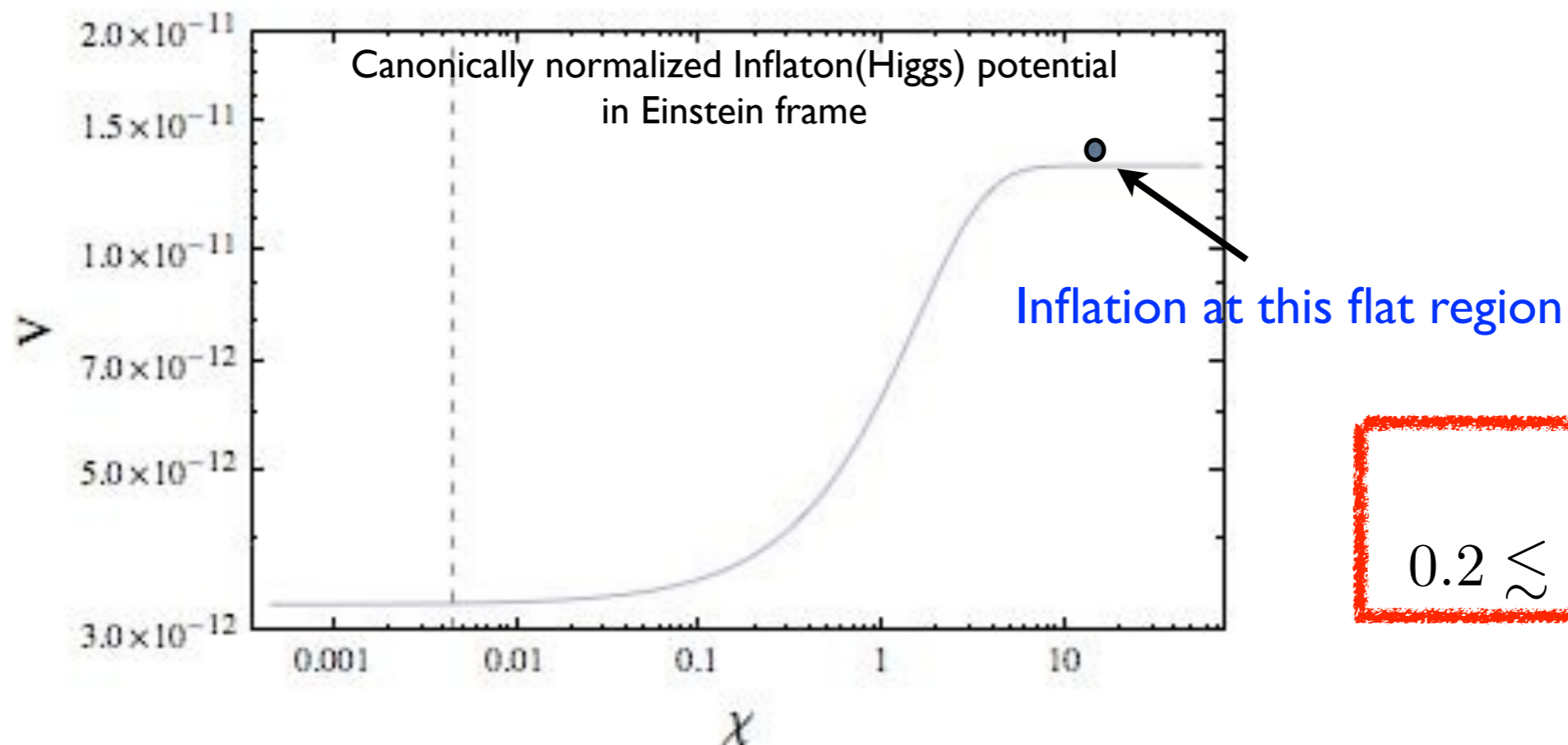
Inflation

- Higgs inflation in Higgs-singlet system

[Lebedev, 1203.0156]

$$\frac{\mathcal{L}_{\text{scalar}}}{\sqrt{-g}} = -\frac{1}{2}M_{\text{P}}^2 R - \frac{1}{2}(\xi_h h^2 + \xi_x x^2) R + \frac{1}{2}(\partial_\mu h)^2 + \frac{1}{2}(\partial_\mu x)^2 - V(h, x)$$

where $\xi_h, \xi_x \gg 1$



$$\lambda_X \lesssim 0.23$$

$$0.2 \lesssim \lambda_{HX} \lesssim 0.6$$

- Summary of main constraints

Small scale structure + CDM

$$\alpha_X \lesssim 4 \times 10^{-5} \left(\frac{m_{\psi(X)}}{300 \text{ GeV}} \right)^{3/2}$$

$$\lambda_1^2 \simeq 58.5 \left(\frac{0.1 \text{ eV}}{\tilde{m}_\nu} \right) \left(\frac{M_1}{10^9 \text{ GeV}} \right) \left(\frac{1 \text{ TeV}}{m_\psi} \right) \left(1 - \frac{m_X^2}{m_\psi^2} \right)^{-2} \left[1 + \frac{1}{48\pi^2} \left(\frac{m_\psi}{v_H} \right)^2 \right]^{-1} \left(\frac{m_X}{300 \text{ GeV}} \right)^2 \left(\frac{\langle \sigma v \rangle_{\text{ann}}^{\text{th}}}{\langle \sigma v \rangle_{\text{ann,d}}^X} \right)^2$$

Vacuum stability + perturbativity

$$\lambda_X \lesssim 0.23$$

$$0.2 \lesssim \lambda_{HX} \lesssim 0.6 \quad \Rightarrow \quad 100 \text{ GeV} \lesssim m_X \lesssim 600 \text{ GeV}$$

Direct search

$$\epsilon \lesssim 10^{-9} - 10^{-4}, \quad 1 \leq \langle \sigma v \rangle_{\text{ann}}^{\text{tot}} / \langle \sigma v \rangle_{\text{ann}}^{\text{th}} \lesssim 5$$

- Variations of the model

Assume the decay of Higgs to DMs is forbidden.

Dark sector fields	$U(1)_X$	Messenger	DM	Extra DR	Signal strength μ_i
$\hat{B}'_{\mu}, X, \psi_X$	Unbroken	$H^\dagger H, \hat{B}'_{\mu\nu} \hat{B}^{\mu\nu}, N_R$	X	~ 0.06	1 ($i = 1$)
\hat{B}'_{μ}, X	Unbroken	$H^\dagger H, \hat{B}'_{\mu\nu} \hat{B}^{\mu\nu}$	X	~ 0.06	1 ($i = 1$)
\hat{B}'_{μ}, ψ_X	Unbroken	$H^\dagger H, \hat{B}'_{\mu\nu} \hat{B}^{\mu\nu} \text{ } \circledast$	ψ_X	~ 0.06	< 1 ($i = 1, 2$)
$\hat{B}'_{\mu}, X, \psi_X, \phi_X$	Broken	$H^\dagger H, \hat{B}'_{\mu\nu} \hat{B}^{\mu\nu}, N_R$	X or ψ_X	~ 0	< 1 ($i = 1, 2$)
$\hat{B}'_{\mu}, X, \phi_X$	Broken	$H^\dagger H, \hat{B}'_{\mu\nu} \hat{B}^{\mu\nu}$	X	~ 0	< 1 ($i = 1, 2$)
\hat{B}'_{μ}, ψ_X	Broken	$H^\dagger H, \hat{B}'_{\mu\nu} \hat{B}^{\mu\nu} \text{ } \circledast$	ψ_X	~ 0	< 1 ($i = 1, 2, 3$)

\circledast = a singlet real scalar

because of mixing in Higgs sector

- * Unbroken $U(1)_X$ allows a sizable contribution to the extra radiation.
- * Broken $U(1)_X$ or the case of fermion dark matter results in “ $\mu_i < 1$ ”.

Summary

- Stability of weak scale dark matter requires a local symmetry.
- The simplest extension of SM with a local $U(1)$ has a unique set of renormalizable interactions.
- The model can address following issues.
 - * Some small scale puzzles of standard CDM scenario
 - * Vacuum stability of Higgs potential
 - * CDM relic density (thermal or non-thermal)
 - * Dark radiation
 - * Lepto/darkogenesis
 - * Inflation (Higgs inflation type)