

The Scale-Invariant NMSSM and the 126 GeV Higgs Boson

Michael A. Schmidt

University of Melbourne – CoEPP

22nd May 2013

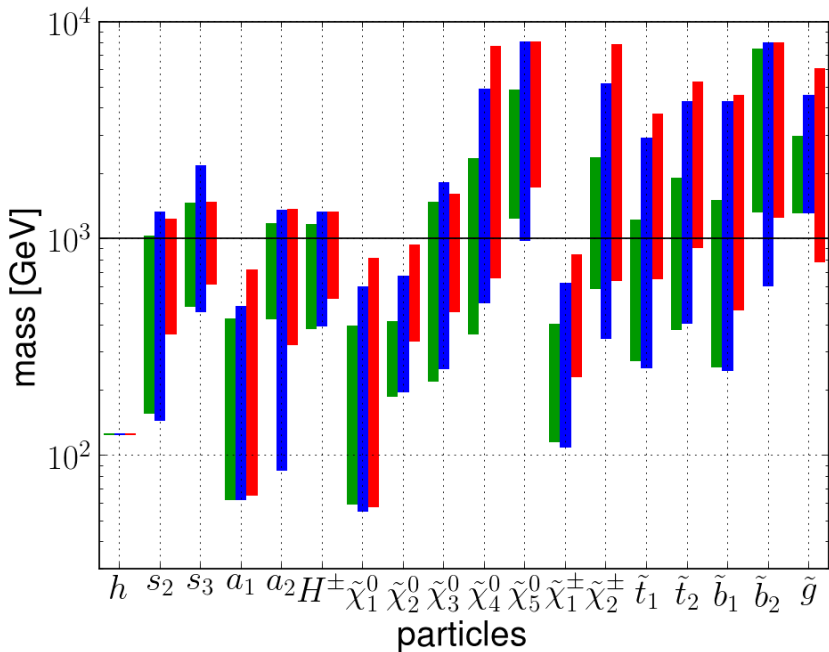
in collaboration with
T. Gherghetta, B. v. Harling, A. Medina
JHEP 1302 (2013) 032 (1212.5243 [hep-ph])



THE UNIVERSITY OF
MELBOURNE



CoEPP
ARC Centre of Excellence for
Particle Physics at the Terascale



Outline

- 1 Introduction
- 2 Naturalness in the Scale-Invariant NMSSM
- 3 Phenomenology
- 4 Conclusions

Outline

1 Introduction

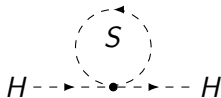
2 Naturalness in the Scale-Invariant NMSSM

3 Phenomenology

4 Conclusions

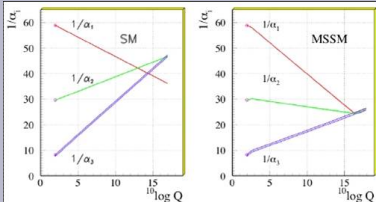
Low-energy Supersymmetry

Solution to hierarchy problem

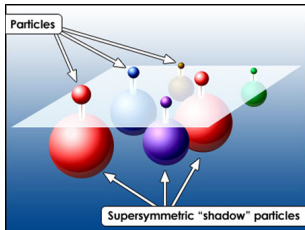
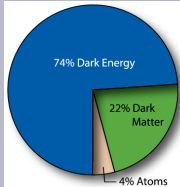


$$\Delta m_H^2 \propto \frac{\lambda_S}{16\pi^2} m_S^2$$

Gauge coupling unification



DM candidate

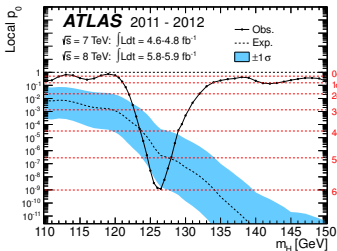


Higgs mass prediction

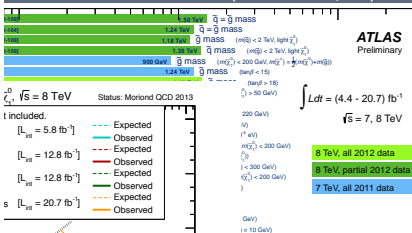
At tree level

$$m_{h^0} < m_Z |\cos 2\beta|$$

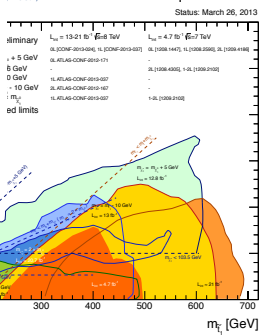
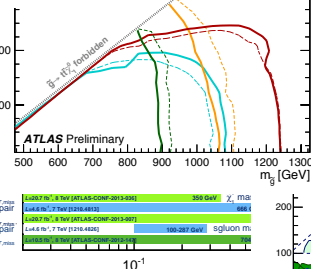
After 8TeV LHC: (C)MSSM and Co.



JSY Searches* - 95% CL Lower Limits (Status: March 26, 2013)



- 3rd gen direct
 - $\tilde{t} \rightarrow \text{heavy } \tilde{t} \rightarrow \tilde{t} \rightarrow 0 \text{ lep} + 6(2b)\text{-jet}$
 - $\tilde{t} \rightarrow \text{natural GMSB} : Z(-\text{ll}) + b\text{-jet}$
 - $\tilde{t} \rightarrow \tilde{t} \rightarrow \tilde{t} + Z : Z(-\text{ll}) + 1 \text{ lep} + b\text{-jet}$
 - $\tilde{t} \rightarrow \tilde{t} \rightarrow \tilde{t} : \tilde{t} \rightarrow \tilde{t} \rightarrow 2 \text{ lep}$
- EW direct
 - $\tilde{Z} \rightarrow \tilde{Z} \rightarrow W(\nu\nu) : 2 \text{ lep}$
 - $\tilde{Z} \rightarrow \tilde{Z} \rightarrow \nu\nu(\nu\nu) : 2$
 - $\tilde{Z} \rightarrow \tilde{Z} \rightarrow \tilde{t}(\nu\nu) : 3 \text{ lep}$
 - $\tilde{Z} \rightarrow \tilde{Z} \rightarrow W\tilde{Z} \text{ CON} : 3 \text{ lep}$
 - Direct \tilde{Z} pair prod. (AMSB) : lon
 - Stable \tilde{g} , R-hadrons : lon
- Long-lived particles
 - GMSB, stable
 - GMSB, $\tilde{Z} \rightarrow \gamma\tilde{G}$: non-pointing
 - $\tilde{Z} \rightarrow \text{qqq}$ (RPV) : μ + heavy displac
 - LFV : $pp \rightarrow \tilde{W}, \tilde{X}, \tilde{V} \rightarrow \mu\tau + n$
 - LFV : $pp \rightarrow \tilde{W}, \tilde{X}, \tilde{V} \rightarrow \mu\tau + n$
 - Bilinear RPV CMSSM : $1 \text{ lep} + 7 \text{ jet}$
- RPV
 - $\tilde{Z} \rightarrow \tilde{Z} \rightarrow W\tilde{Z} \rightarrow \text{ee}\nu_e\nu_e : 4 \text{ lep}$
 - $\tilde{Z} \rightarrow \tilde{Z} \rightarrow \tilde{t} \rightarrow \text{tt}\nu_e\nu_e : 3 \text{ lep} + 1\tau + E_{\text{miss}}$
 - $\tilde{Z} \rightarrow \tilde{Z} \rightarrow \tilde{t} \rightarrow \text{qqq} : 3\text{-jet resonance pair}$
 - $\tilde{Z} \rightarrow \tilde{Z} \rightarrow \tilde{t} \rightarrow \text{bs} : 2 \text{ SS-lep} + (0\text{-}3b)\text{-jet} + E_{\text{miss}}$
 - Scalar gluon : 2-jet resonance pair
 - WIMP interaction (D5, Dirac $\tilde{\chi}$) : monojet + E_{miss}



*Only a selection of the available mass limits on new states or phenomena shown. All limits quoted are observed minus 1 σ theoretical signal cross section uncertainty.

Fine-tuning in the MSSM

- rely on loop corrections to Higgs mass from (s)top sector

$$m_h^2 = m_Z^2 \cos^2 2\beta \left(1 - \frac{3}{8\pi^2} y_t^2 t \right) + \frac{3}{4\pi^2} y_t^2 \left[\frac{1}{2} X_t + t + \dots \right]$$

with $t = \ln \frac{m_{\text{soft}}^2}{M_t^2}$, $X_t = \frac{2(A_t - \mu \cot \beta)^2}{m_{\text{soft}}^2} \left(1 - \frac{(A_t - \mu \cot \beta)^2}{12m_{\text{soft}}^2} \right)$, $m_{\text{soft}} = \sqrt{m_{\tilde{t}_1} m_{\tilde{t}_2}}$

- Large contribution to $m_{H_u}^2$ from RG evolution in the supersymmetric theory (finite corrections are small compared to RG effects for $\Lambda \gg m_{\text{soft}}$)

$$m_{H_u}^2(m_{\text{soft}}) = m_{H_u}^2(\Lambda) - \frac{3y_t^2}{8\pi^2} \left[m_{Q_3}^2(\Lambda) + m_{u_3}^2(\Lambda) + A_t^2(\Lambda) \right] \ln \left[\frac{\Lambda}{m_{\text{soft}}} \right] + \dots$$

Tree-level minimization conditions

$$m_Z^2 = \frac{m_{H_u}^2 - m_{H_d}^2}{\cos 2\beta} - m_{H_u}^2 - m_{H_d}^2 - 2\mu^2$$

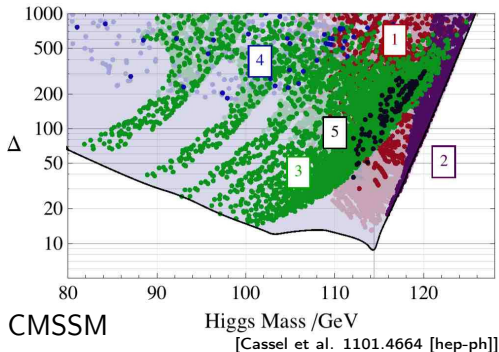
$$0 = \frac{2b}{\sin 2\beta} - m_{H_u}^2 - m_{H_d}^2 - 2\mu^2$$

Fine-tuning in the MSSM 2

Finetuning measure [Barbieri, Giudice (1988)]

$$\Sigma^v = \Delta \equiv \max_{\xi} \left| \frac{\partial \ln v^2}{\partial \ln \xi(\Lambda)} \right|$$

with $\xi = (m_{H_u}^2, m_{H_d}^2, m_{Q_3}^2, m_{u_3}^2, m_{d_3}^2, A_t, A_b, M_1, M_2, M_3)$



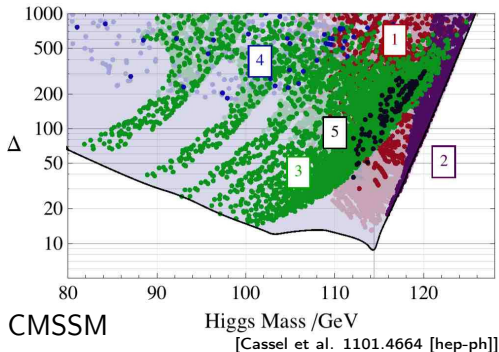
- after LEP: $\Sigma^v \gtrsim 10$,
i.e. 10% fine tuning
- after 8TeV LHC: $\Sigma^v \gtrsim 100$,
i.e. **worse than 1% fine tuning**

Fine-tuning in the MSSM 2

Finetuning measure [Barbieri, Giudice (1988)]

$$\Sigma^v = \Delta \equiv \max_{\xi} \left| \frac{\partial \ln v^2}{\partial \ln \xi(\Lambda)} \right|$$

with $\xi = (m_{H_u}^2, m_{H_d}^2, m_{Q_3}^2, m_{u_3}^2, m_{d_3}^2, A_t, A_b, M_1, M_2, M_3)$



- after LEP: $\Sigma^v \gtrsim 10$,
i.e. 10% fine tuning
- after 8TeV LHC: $\Sigma^v \gtrsim 100$,
i.e. worse than 1% fine tuning







New tree-level contributions to the Higgs mass

- additional D -term contributions
- additional F -term contributions

→ e.g. in the NMSSM: additional gauge singlet S

Outline

1 Introduction

2 Naturalness in the Scale-Invariant NMSSM

3 Phenomenology

4 Conclusions

NMSSM

Superpotential

$$W_{NMSSM} = \lambda S H_d H_u + \frac{\kappa}{3} S^3$$

Soft breaking terms

$$V_{\text{soft}} = m_{H_d}^2 |H_d|^2 + m_{H_u}^2 |H_u|^2 + m_S^2 |S|^2 - (a_\lambda S H_d H_u + \frac{a_\kappa}{3} S^3 + h.c.)$$

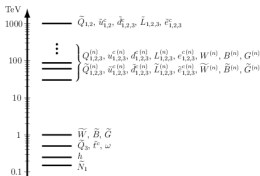
Bound on lightest Higgs mass m_h

$$m_h^2 \leq m_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta \rightarrow \begin{cases} m_Z^2 \cos^2 2\beta & \text{large } \tan \beta \\ \lambda^2 v^2 \sin^2 2\beta & \text{small } \tan \beta \end{cases}$$

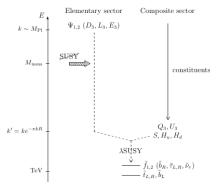
- No gain for large $\tan \beta$ compared to MSSM \rightarrow **small $\tan \beta$**
- \rightarrow **relatively large $\lambda \gtrsim 0.7$** or additional stop loop contribution
- \rightarrow **Landau pole below GUT scale**

Large λ : Landau pole below GUT scale

- Additional vector-like $5 + \bar{5}$ SU(5) multiplets delay Landau pole [Mazip, Munoz-Tapia, Pomarol (1998); Barbieri et al. (2007); Barbieri et al. (2013)]
 - Strong-coupling effects might even correct for 3% discrepancy in unification [Hardy, March-Russell, Unwin (1207.1435)]
 - **New physics at $\Lambda \sim 10$ TeV** (λ SUSY [Barbieri, Hall, Nomura, Rychkov (2006)])
- e.g. Fat Higgs [Harnik, Kribs, Larson, Murayama (2003)]
 [Chang, Kilic, Mahbubani (2004); Delgado, Tait; Birkedal, Chacko, Nomura (2004)]
- e.g. within extra dimensional models



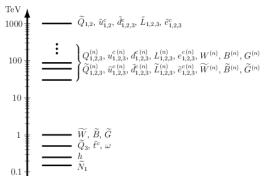
[Gherghetta, v.Harling, Setzer (2011)]



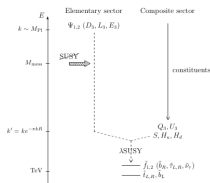
[Larsen, Nomura, Roberts (2012)]

Large λ : Landau pole below GUT scale

- Additional vector-like $5 + \bar{5}$ SU(5) multiplets delay Landau pole [Mazip, Munoz-Tapia, Pomarol (1998); Barbieri et al. (2007); Barbieri et al. (2013)]
 - Strong-coupling effects might even correct for 3% discrepancy in unification [Hardy, March-Russell, Unwin (1207.1435)]
 - **New physics at $\Lambda \sim 10$ TeV** (λ SUSY [Barbieri, Hall, Nomura, Rychkov (2006)])
- e.g. Fat Higgs [Harnik, Kribs, Larson, Murayama (2003)]
 [Chang, Kilic, Mahbubani (2004); Delgado, Tait; Birkedal, Chacko, Nomura (2004)]
- e.g. within extra dimensional models



[Gherghetta, v.Harling, Setzer (2011)]



[Larsen, Nomura, Roberts (2012)]

- Our assumptions: couple first two generations of particles as well as third generation of sleptons

EW symmetry breaking

MSSM minimization conditions

$$m_Z^2 = \frac{m_{H_u}^2 - m_{H_d}^2}{\cos 2\beta} - m_{H_u}^2 - m_{H_d}^2 - 2\mu^2$$
$$0 = m_A^2 - m_{H_u}^2 - m_{H_d}^2 - 2\mu^2$$

We obtain the following minimization conditions in the NMSSM [$\mu \equiv \lambda v_S$ and $m_A^2 \equiv \frac{2(a_\lambda + \lambda \kappa v_S)v_S}{\sin 2\beta}$]

$$m_Z^2 = \frac{m_{H_u}^2 - m_{H_d}^2}{\cos 2\beta} - m_{H_u}^2 - m_{H_d}^2 - 2\lambda^2 v_S^2$$
$$\lambda^2 v^2 = \frac{2(a_\lambda + \lambda \kappa v_S)v_S}{\sin 2\beta} - m_{H_u}^2 - m_{H_d}^2 - 2\lambda^2 v_S^2$$
$$m_S^2 = \lambda \kappa v^2 \sin 2\beta - 2\kappa^2 v_S^2 - \lambda^2 v^2 - \frac{a_\lambda v^2}{2v_S} \sin 2\beta - a_\kappa v_S$$

Beyond tree-level

$$S_{\text{eff}} = \int d^4x \left\{ \sum_{n=0}^{\infty} Z_i^n \partial_\mu \phi_i^\dagger \partial^\mu \phi_i - \sum_{n=0}^{\infty} V_n \right\}$$

The NLO corrections to the potential are given by the Coleman-Weinberg potential

$$V_1 = \frac{1}{64\pi^2} \text{STr} M^4 \left[\ln \left(\frac{M^2}{\mu_r^2} \right) - \frac{3}{2} \right]$$

Defining

$$\hat{m}_{H_u}^2 \equiv m_{H_u}^2 + \frac{d}{dv_u^2} V_1, \quad \hat{m}_{H_d}^2 \equiv m_{H_d}^2 + \frac{d}{dv_d^2} V_1, \quad \hat{m}_S^2 \equiv m_S^2 + \frac{d}{dv_S^2} V_1$$

the minimization conditions at NLO can be written as

$$m_Z^2 = \frac{\hat{m}_{H_u}^2 - \hat{m}_{H_d}^2}{\cos 2\beta} - \hat{m}_{H_u}^2 - \hat{m}_{H_d}^2 - 2\lambda^2 v_S^2.$$

$$\lambda^2 v^2 = 2 \frac{(a_\lambda v_S + \lambda \kappa v_S^2)}{\sin 2\beta} - \hat{m}_{H_u}^2 - \hat{m}_{H_d}^2 - 2\lambda^2 v_S^2$$

$$\hat{m}_S^2 = \lambda \kappa v^2 \sin 2\beta - 2\kappa^2 v_S^2 - \lambda^2 v^2 - \frac{a_\lambda v^2}{2v_S} \sin 2\beta - a_\kappa v_S$$

Fine-tuning in the NMSSM

Finetuning measure [Barbieri, Giudice (1988)]

$$\Sigma^v = \max_i \left| \frac{\partial \ln v^2}{\partial \ln \xi_i(\Lambda)} \right|$$

with $\xi_i = (m_{H_u}^2, m_{H_d}^2, m_S^2, \lambda, \kappa, a_\lambda, a_\kappa, m_{Q_3}^2, m_{u_3}^2, m_{d_3}^2, A_t, A_b, M_1, M_2, M_3)$

Finite one-loop corrections alleviate tuning by 10-20% compared to tree-level (cf. [Cassel, Ghilenciu, Ross (2010)])

$$\Sigma^v = \max_i \left| \sum_j \frac{d \ln v^2}{d \ln \xi_j(m_{\text{soft}})} \frac{d \ln \xi_j(m_{\text{soft}})}{d \ln \xi_i(\Lambda)} \right|$$

Fine-tuning in the NMSSM

Finetuning measure [Barbieri, Giudice (1988)]

$$\Sigma^v = \max_i \left| \frac{\partial \ln v^2}{\partial \ln \xi_i(\Lambda)} \right|$$

with $\xi_i = (m_{H_u}^2, m_{H_d}^2, m_S^2, \lambda, \kappa, a_\lambda, a_\kappa, m_{Q_3}^2, m_{u_3}^2, m_{d_3}^2, A_t, A_b, M_1, M_2, M_3)$

Finite one-loop corrections alleviate tuning by 10-20% compared to tree-level (cf. [Cassel, Ghilenciu, Ross (2010)])

$$\Sigma^v = \max_i \left| \sum_j \frac{d \ln v^2}{d \ln \xi_j(m_{\text{soft}})} \frac{d \ln \xi_j(m_{\text{soft}})}{d \ln \xi_i(\Lambda)} \right|$$

For example in the case of $m_{Q_3}^2$ neglecting finite one-loop correction:

$$\left| \frac{d \ln v^2}{d \ln m_{Q_3}^2(\Lambda)} \right| \approx \left| \frac{3y_t^2}{8\pi^2} \frac{m_{Q_3}^2(\Lambda)}{v^2} \ln \left[\frac{\Lambda}{m_{\text{soft}}} \right] \times \frac{dv^2}{dm_{H_u}^2(m_{\text{soft}})} \right| \lesssim \Sigma^v$$

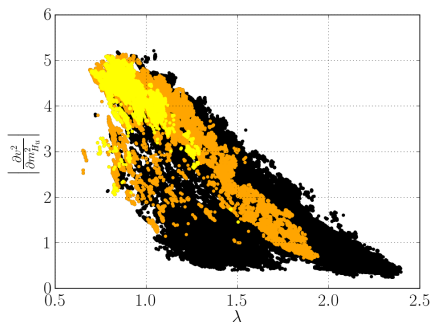
MSSM

$$\frac{dv^2}{dm_{H_u}^2(m_{\text{soft}})} = -2 \frac{v^2}{m_Z^2} + \mathcal{O} \left(\frac{1}{\tan \beta} \right)$$

NMSSM

$$\frac{dv^2}{dm_{H_u}^2(m_{\text{soft}})} = \frac{\kappa}{\lambda^3} \cot 2\beta + \mathcal{O} \left(\frac{1}{\lambda^4} \right)$$

Large λ helps

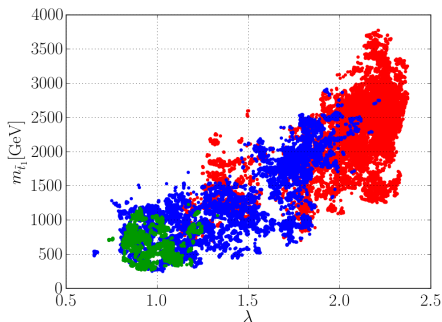
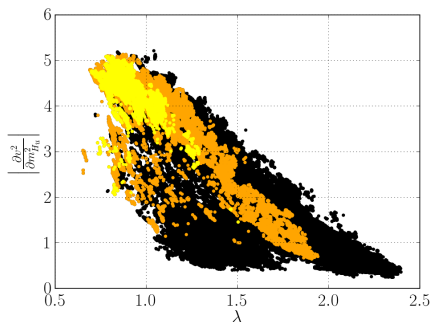


- $\frac{dv^2}{dm_{H_u}^2(m_{\text{soft}})} \sim \frac{\kappa}{\lambda^3} \cot 2\beta$

→ large λ reduces finetuning

- black $\Lambda = 20$ TeV, orange $\Lambda = 100$ TeV, yellow $\Lambda = 1000$ TeV

Large λ helps



- $\frac{dv^2}{dm_{H_u}^2(m_{\text{soft}})} \sim \frac{\kappa}{\lambda^3} \cot 2\beta$

→ large λ reduces finetuning

- black $\Lambda = 20$ TeV, orange $\Lambda = 100$ TeV, yellow $\Lambda = 1000$ TeV
- right: $\Sigma^v < 20$: better than 5% VEV tuning
- large λ allows larger stop masses

Large λ hurts

$$m_h^2 \simeq m_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta + \delta m_{h,\text{stop}}^2 + \delta m_{h,S}^2$$

- For large λ : $\lambda v \sin 2\beta > m_h$: cancellation required
 - generally $\delta m_{h,\text{stop}}^2 > 0$
 - partly cancelled by mixing with singlet (cf. [Agashe, Cui, Franceschini (2012)])
 - In our scan, it amounts to at most 40% of $m_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta$
- loop corrections from Higgs-singlet sector lead to required cancellation

Large λ hurts

$$m_h^2 \simeq m_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta + \delta m_{h,\text{stop}}^2 + \delta m_{h,S}^2$$

- For large λ : $\lambda v \sin 2\beta > m_h$: cancellation required
 - generally $\delta m_{h,\text{stop}}^2 > 0$
 - partly cancelled by mixing with singlet (cf. [Agashe, Cui, Franceschini (2012)])
 - In our scan, it amounts to at most 40% of $m_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta$
- loop corrections from Higgs-singlet sector lead to required cancellation

Higgs mass tuning

$$\Sigma^h \equiv \max_{\xi_i} \left| \frac{d \ln m_h^2}{d \ln \xi_i} \right| \approx \max_{\xi_i} \left| \frac{\xi_i}{m_h^2} \frac{d m_{h,\text{tree}}^2}{d \xi_i} \right|$$

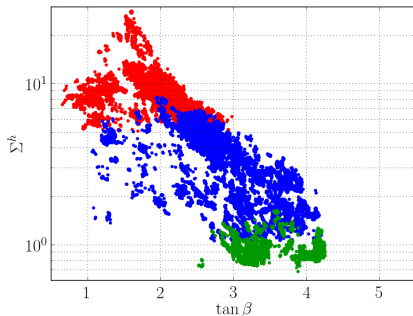
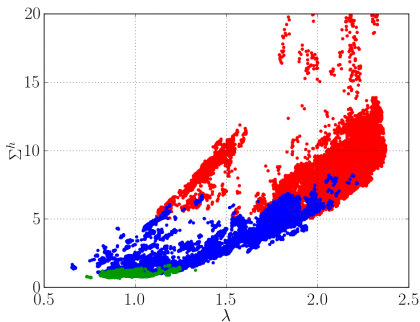
with $\xi_i = (\lambda, \kappa, a_\lambda, a_\kappa, m_{Q_3}^2, m_{u_3}^2, m_{d_3}^2, A_t, A_b, M_1, M_2, M_3)$ and fix $v_{u,d,S}$

Large λ hurts 2

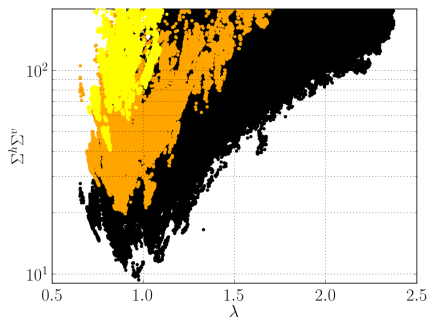
Higgs mass tuning

$$\Sigma^h \equiv \max_{\xi_i} \left| \frac{d \ln m_h^2}{d \ln \xi_i} \right| \approx \max_{\xi_i} \left| \frac{\xi_i}{m_h^2} \frac{dm_{h,\text{tree}}^2}{d\xi_i} \right|$$

with $\xi_i = (\lambda, \kappa, a_\lambda, a_\kappa, m_{Q_3}^2, m_{u_3}^2, m_{d_3}^2, A_t, A_b, M_1, M_2, M_3)$ and fix $v_{u,d,S}$

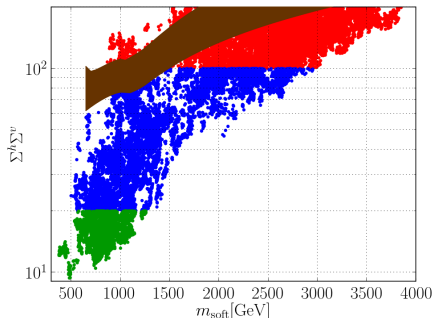
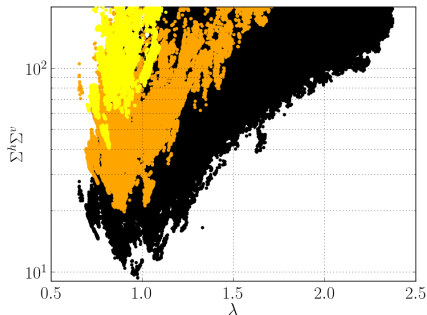


Combined fine-tuning



- In a statistical sense, if two quantities are not correlated, the probability involving both is $P(A \cap B) = P(A) * P(B)$.
- black $\Lambda = 20$ TeV, orange $\Lambda = 100$ TeV, yellow $\Lambda = 1000$ TeV

Combined fine-tuning



- In a statistical sense, if two quantities are not correlated, the probability involving both is $P(A \cap B) = P(A) * P(B)$.
- black $\Lambda = 20$ TeV, orange $\Lambda = 100$ TeV, yellow $\Lambda = 1000$ TeV
- right: $\Sigma^{\nu} < 20$: better than 5% VEV tuning
- green $\Sigma^h\Sigma^{\nu} < 20$, blue $20 < \Sigma^h\Sigma^{\nu} < 100$, red $\Sigma^h\Sigma^{\nu} > 100$
- brown band: MSSM with $\mu = 200$ GeV, $\tan\beta = 20$ and $m_A = 1$ TeV
[generated using FeynHiggs]

Outline

- 1 Introduction
- 2 Naturalness in the Scale-Invariant NMSSM
- 3 Phenomenology**
- 4 Conclusions

Numerical Scan

- Markov Chain Monte Carlo
- We used a modified version of NMHDECAY, which is part of NMSSMTools 3.2.1, as well as MicrOMEGAs 2.4.5 for DM
- We scanned linearly in 14-dimensional parameter space

$\tan \beta$	$\tan \beta > 0.08$	m_{Q_3}	$\Delta_{\tilde{g}} m_{Q_3} < m_{Q_3} < 5 \text{ TeV}$	M_1	$0 < M_1 < 8 \text{ TeV}$
μ	$ \mu < 1 \text{ TeV}$	m_{u_3}	$\Delta_{\tilde{g}} m_{u_3} < m_{u_3} < 5 \text{ TeV}$	M_2	$0 < M_2 < 8 \text{ TeV}$
λ	$0 < \lambda < 3$	m_{d_3}	$0 < m_{d_3} < 8 \text{ TeV}$	M_3	$0.5 \text{ TeV} < M_3 < 8 \text{ TeV}$
κ	$ \kappa < 2.75$	A_t	$ \Delta_{\tilde{g}} A_t < A_t < 5 \text{ TeV}$	ν	174 GeV
A_λ	$ A_\lambda < 2 \text{ TeV}$	A_b	$ A_b < 8 \text{ TeV}$	Λ	20, 100, 1000 TeV
A_κ	$ A_\kappa < 1 \text{ TeV}$				

- ⇒ We did not sample the full parameter space. Therefore, **there is no statistical interpretation of the scatter plots.**
- Likelihood function: product of Gaussians for the Higgs mass centered at 126 GeV and for the VEV finetuning centered at 0.
 - We impose the hard cuts summarised in the table as well as

$$|\xi(\Lambda) - \xi(m_{\text{soft}})| < |\xi(\Lambda)| \quad \text{for } \xi = m_{Q_3}^2, m_{u_3}^2, m_{d_3}^2, A_t, A_b$$
 similar to "gluino sucks the stop mass up" [Arvanitaki, Craig, Dimopoulos, Villadoro(2012)]
 - **We conservatively impose the collider, EW precision and flavour constraints.**

Electroweak Precision Tests (EWPT)

- impose EWPT at 2σ with $m_{h,ref} = 117$ GeV [PDG(2012)].

$S_0 = -0.04 \pm 0.09$, $T_0 = 0.07 \pm 0.08$ and correlation of 88% at 95% C.L.

Electroweak Precision Tests (EWPT)

- impose EWPT at 2σ with $m_{h,ref} = 117$ GeV [PDG(2012)].
 $S_0 = -0.04 \pm 0.09$, $T_0 = 0.07 \pm 0.08$ and correlation of 88% at 95% C.L.
- Consistent with previous analyses[Barbieri et. al.(2006); Franceschini, Gori (2010)], we find
- Higgs and singlet scalars do not contribute much to S,T
- (3rd gen) squarks: $\tan \beta$ can not be too large unless cancellation
 $\tan \beta \neq 1$ breaks custodial SU(2) \rightarrow contribution to T

Electroweak Precision Tests (EWPT)

- impose EWPT at 2σ with $m_{h,ref} = 117$ GeV [PDG(2012)].
 $S_0 = -0.04 \pm 0.09$, $T_0 = 0.07 \pm 0.08$ and correlation of 88% at 95% C.L.
- Consistent with previous analyses [Barbieri et. al.(2006); Franceschini, Gori (2010)], we find
- Higgs and singlet scalars do not contribute much to S,T
- (3rd gen) squarks: $\tan \beta$ can not be too large unless cancellation
 $\tan \beta \neq 1$ breaks custodial SU(2) \rightarrow contribution to T
- Neutralino/chargino sector imposes strong constraint on λ as well as $\tan \beta$

$$M_{\psi^0} = \begin{pmatrix} M_1 & 0 & -\cos \beta \sin \theta_W m_Z & \sin \beta \sin \theta_W m_Z & 0 \\ \cdot & M_2 & \cos \beta \cos \theta_W m_Z & -\sin \beta \cos \theta_W m_Z & 0 \\ \cdot & \cdot & 0 & -\mu & -\lambda v \sin \beta \\ \cdot & \cdot & -\mu & 0 & -\lambda v \cos \beta \\ \cdot & \cdot & \cdot & \cdot & -2\frac{\kappa}{\lambda} \mu \end{pmatrix}$$

$$M_{\psi^\pm} = \begin{pmatrix} 0 & X^T \\ X & 0 \end{pmatrix} \quad \text{with} \quad X = \begin{pmatrix} M_2 & \sqrt{2} m_W \sin \beta \\ \sqrt{2} m_W \cos \beta & \mu \end{pmatrix}$$

in gauge-basis $\psi^0 = (\tilde{B}, \tilde{W}^3, \tilde{H}_d^0, \tilde{H}_u^0, \tilde{S})$ and $\psi^\pm = (\tilde{W}^\pm, \tilde{H}_u^\pm, \tilde{W}^\mp, \tilde{H}_d^\mp)$

- We find $\tan \beta \lesssim 5$ depending on λ

SUSY searches

Assuming a neutralino LSP, we **conservatively** exclude the following regions:

- gluino search: $\tilde{g} \rightarrow b\bar{b}\tilde{\chi}_1^0$ [ATLAS-CONF-2012-151]

$$m_{\tilde{g}} < 1310 \text{ GeV} \quad \text{if } m_{\tilde{\chi}_1^0} < 650 \text{ GeV}$$

- sbottom search [PDG (2012); CMS-PAS-SUS-12-028; ATLAS-CONF-2012-106]

$$m_{\tilde{b}} < 89 \text{ GeV}$$

$$150 \text{ GeV} < m_{\tilde{b}} < 650 \text{ GeV} \quad \text{if } m_{\tilde{\chi}_1^0} < 230 \text{ GeV}$$

- stop search [PDG(2012); ATLAS (1208.1447, 1208.2590)]

$$m_{\tilde{t}} < 95.7 \text{ GeV}$$

$$220 \text{ GeV} < m_{\tilde{t}} < 500 \text{ GeV} \quad \text{if } m_{\tilde{\chi}_1^0} < 160 \text{ GeV}$$

- chargino search [PDG (2012)]

$$m_{\tilde{\chi}^\pm} < 94 \text{ GeV}$$

The neutralino/chargino searches by ATLAS/CMS did not lead to further constraints.

Higgs searches

$$R_X \equiv \frac{\sigma(h) \times BR(h \rightarrow X)}{\sigma(h_{\text{SM}}) \times BR(h_{\text{SM}} \rightarrow X)}$$

- Higgs resonance at 126 GeV

[ATLAS (1207.7214), ATLAS-CONF-2012-162; ATLAS-CONF-2012-170; CMS (1207.7235), CMS-HIG-12-045]

$$0.81 < R_{ZZ} < 1.32, \quad 0.74 < R_{WW} < 1.40,$$
$$0 < R_{b\bar{b}} < 1.10, \quad 0.27 < R_{\tau\tau} < 1.15,$$

- Heavy Higgs searches [CMS-PAS-Higgs-11-024, CMS-PAS-Higgs-11-041]

$$\frac{\sigma(s_i) \times BR(s_i \rightarrow ZZ)}{\sigma(h_{\text{SM}}) \times BR(h_{\text{SM}} \rightarrow ZZ)} < 0.09$$
$$\frac{\sigma(s_i) \times BR(s_i \rightarrow WW)}{\sigma(h_{\text{SM}}) \times BR(h_{\text{SM}} \rightarrow WW)} < 0.2$$

- Charged Higgs [PDG(2012)]

$$m_{H^\pm} \gtrsim 79.3 \text{ GeV}$$

Flavour Constraints

We use the following flavour physics constraints

- B -meson mixing [HFAG (1207.1158)]

$$\Delta M_s = (17.719 \pm 0.086) \text{ ps}^{-1}$$

$$\Delta M_d = (0.507 \pm 0.008) \text{ ps}^{-1}$$

- rare B -decays [HFAG (1207.1158)]

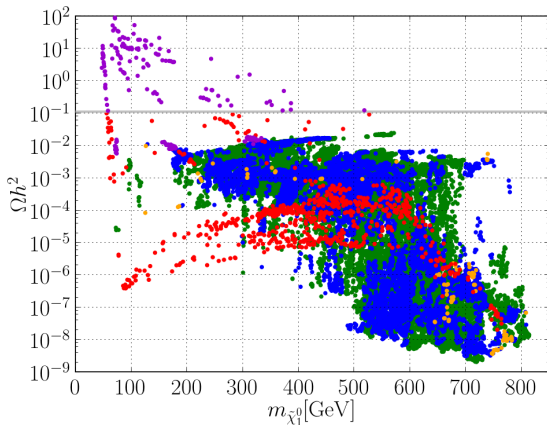
$$\text{Br}(B^+ \rightarrow \tau^+ \nu_\tau) = (1.67 \pm 0.60) \times 10^{-4}$$

$$\text{Br}(B \rightarrow X_s \gamma) = (3.55 \pm 0.48 \pm 0.18) \times 10^{-4}$$

- recently measured rare decay $B_s^0 \rightarrow \mu^+ \mu^-$ [LHCb (1211.2674)]

$$\text{Br}(B_s^0 \rightarrow \mu^+ \mu^-) = 3.2_{-2.4}^{+3.0+1.0}_{-0.6} \times 10^{-9}$$

Dark Matter



- WMAP-7 constraint: $\Omega_{LSP} h^2 < \Omega_{WMAP-7} h^2 = 0.1120 \pm 0.0056$
 - green (singlino), blue (Higgsino), orange (wino), red (bino) DM
 - Purple points overclose the Universe or are excluded by XENON100
- ⇒ but they are viable if the gravitino is the LSP.

Dark Matter 2

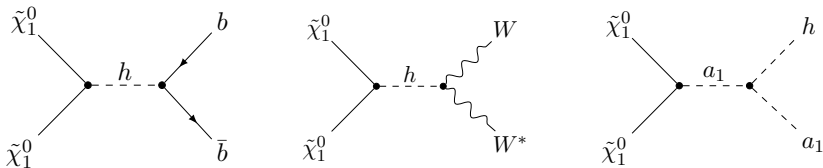
- A mostly Bino with Higgsino admixture is viable DM candidate

• We find:

- lightest chargino mostly Higgsino with $m_{\tilde{\chi}^\pm} \gtrsim 200$ GeV
- charged Higgs $m_{H^\pm} \gtrsim 750$ GeV

⇒ t -channel annihilation via chargino and LSP-chargino coannihilation via charged Higgs are suppressed

- Dominant annihilation channels:



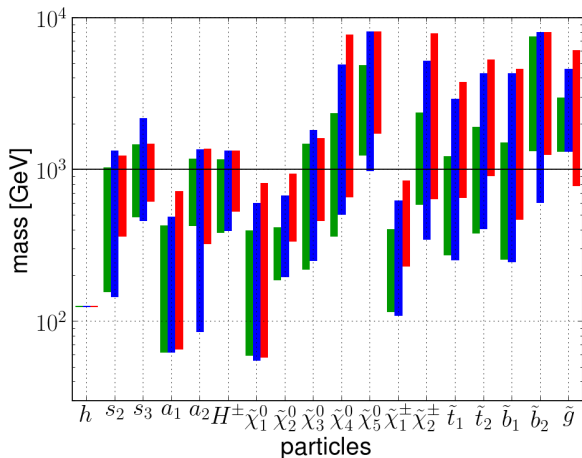
- on resonance for CP even Higgs-mediated annihilation (p -wave)

- s -wave CP odd Higgs-mediated annihilation

- Why did we not find more points, which fit WMAP-7?

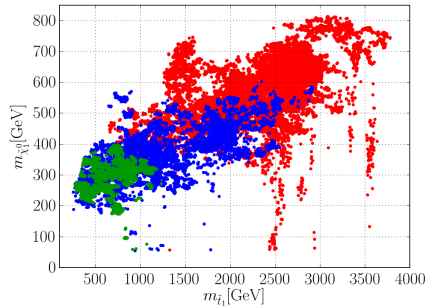
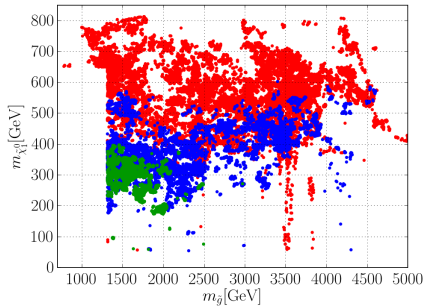
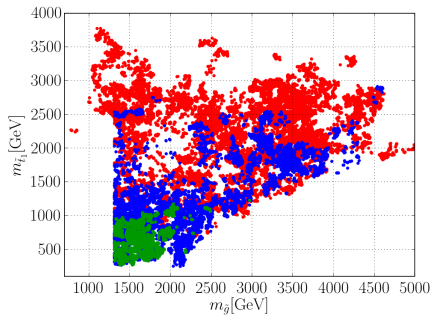
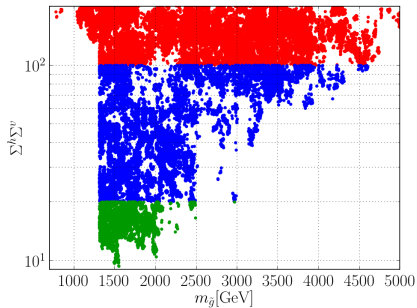
→ scan linearly in parameters → large values are preferred, M_1 generally large

Particle spectrum

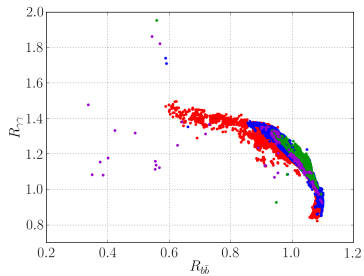
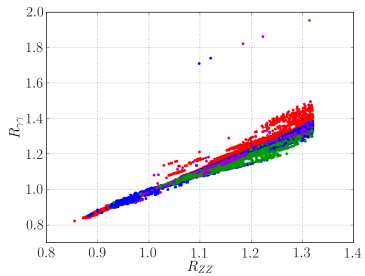


- all colored particles can be above 1 TeV with tuning better than 5%
- but light EW sector required
- due to limits on invisible widths: $m_{a_1} \gtrsim \frac{m_h}{2}$ and $m_{\tilde{\chi}_1^0} \gtrsim \frac{m_Z}{2}$ (or $\frac{m_h}{2}$)

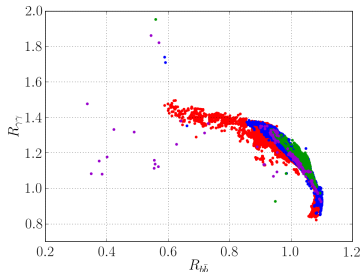
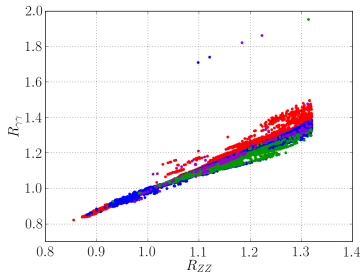
SUSY searches



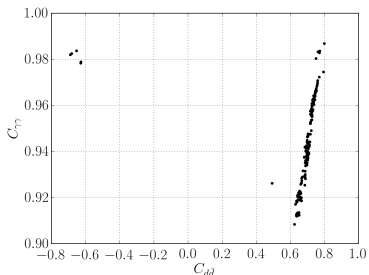
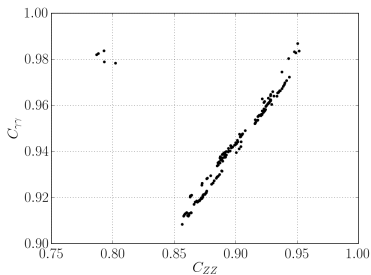
Higgs diphoton rate



Higgs diphoton rate



Require $h \rightarrow \gamma\gamma$ to be within 1σ : $1.40 < R_{\gamma\gamma} < 1.99$



Outline

- 1 Introduction
- 2 Naturalness in the Scale-Invariant NMSSM
- 3 Phenomenology
- 4 Conclusions**

Conclusions

- natural SUSY is not excluded (yet)
 - TeV-scale stop masses allowed with 5% tuning for a cutoff scale of 20 TeV
 - a large value of λ reduces tuning in Higgs VEV, Σ^v
 - but introduces an additional tuning in the Higgs mass, Σ^h
- ⇒ consider combined tuning $\Sigma^v \Sigma^h$

Conclusions

- natural SUSY is not excluded (yet)
 - TeV-scale stop masses allowed with 5% tuning for a cutoff scale of 20 TeV
 - a large value of λ reduces tuning in Higgs VEV, Σ^v
 - but introduces an additional tuning in the Higgs mass, Σ^h
- ⇒ consider combined tuning $\Sigma^v \Sigma^h$

Particle spectrum

We find for the particle spectrum with a combined tuning, $\Sigma^v \Sigma^h$, better than 5(1)% with $\Lambda = 20$ TeV

- lightest stop $m_{\tilde{t}_1} \lesssim 1.2(2.6)$ TeV
 - gluino masses $m_{\tilde{g}} \lesssim 3.0(4.6)$ TeV
 - lightest EW sparticles (charginos/neutralinos) $m_{\tilde{\chi}} \lesssim 400(600)$ GeV
- We have to wait for the 14 TeV LHC

