

# Tracking for the ILC

Marcel Stanitzki



DESY, 08/10/2013

# Introduction

- Disclaimer
  - I am a “silicon guy”, hence there will be a certain focus on silicon trackers
- This talk should serve as an introduction
  - Overview on relevant issues
  - Neither encyclopaedic nor complete
- Goal
  - Understand the issues and “what people talk about”
  - Get you interested in tracking detectors

# Roadmap

**Basics**

**Tracking  
Detectors**

**Readout  
&  
Digitization**

**Track  
Recon-  
struction**





# Tracking -What is it ?



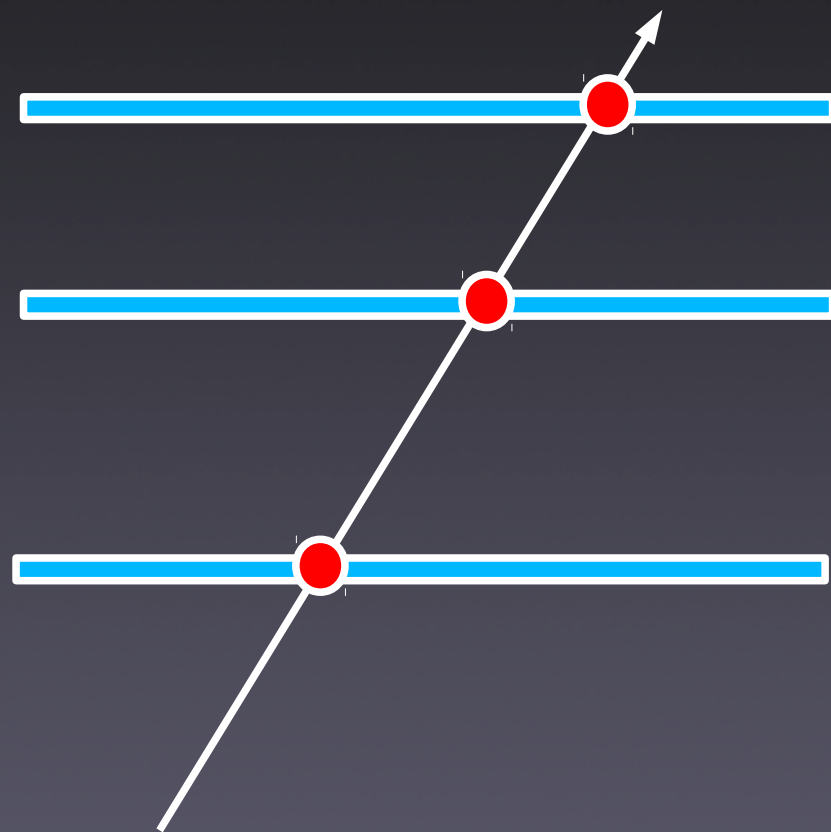
## **Tracking:**

to follow or pursue the track, traces, or footprints of.

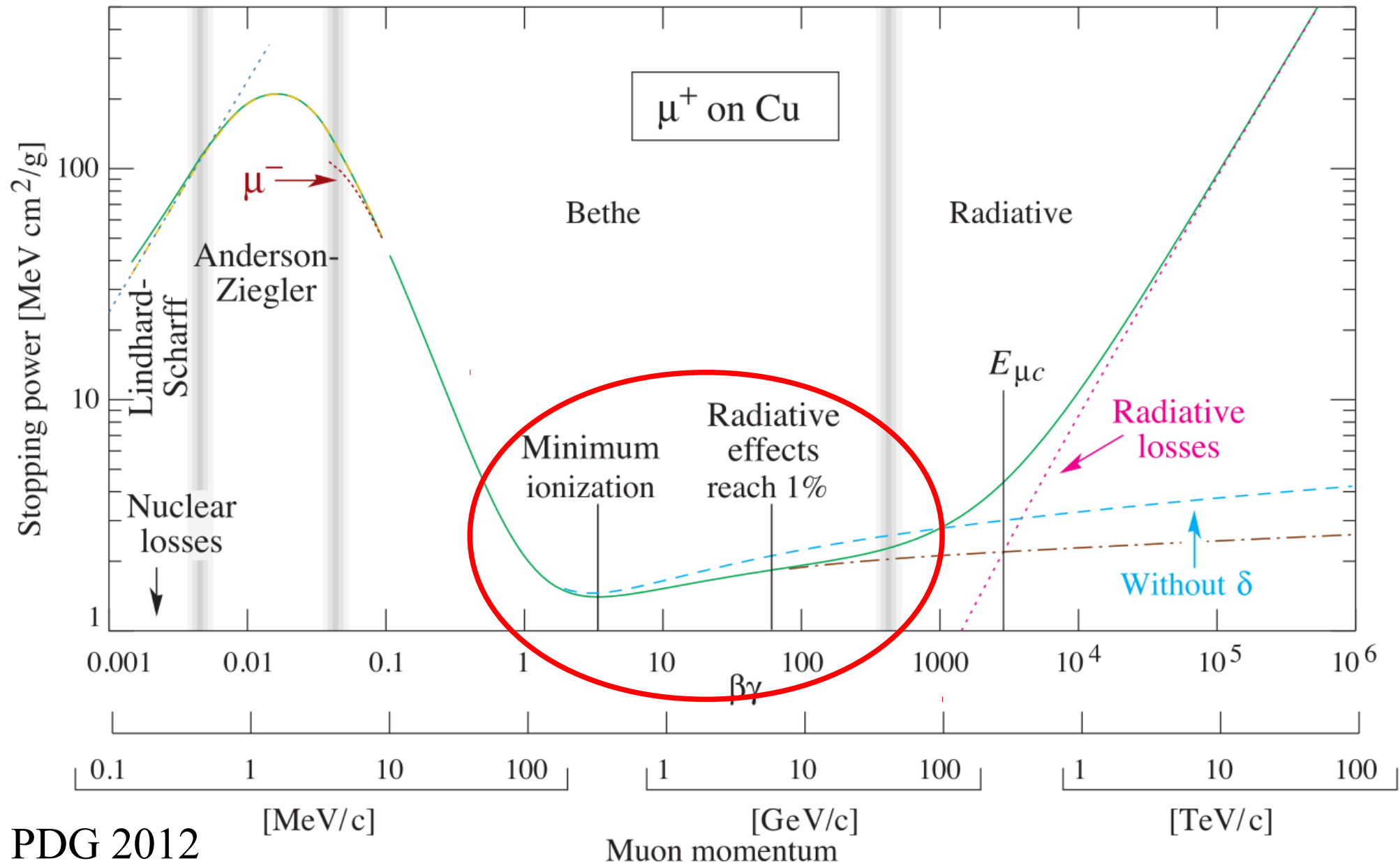


# Basic idea

- Reconstruct the charged particle's trajectory through the detector
  - Obtain several position measurements
- Minimal interruption of the track
  - Minimize material
- Adding magnetic field
  - Get particle momentum
  - Charge information



# Particles through matter



# Particles through matter

- We're mostly dealing with minimum ionizing particles
  - Track momenta usually between 1-100 GeV
- Particles traversing thin material layers
  - Small deviations caused by mainly Coulomb-Scattering
  - Deviations depend on Material (Z,A and  $\rho$ )

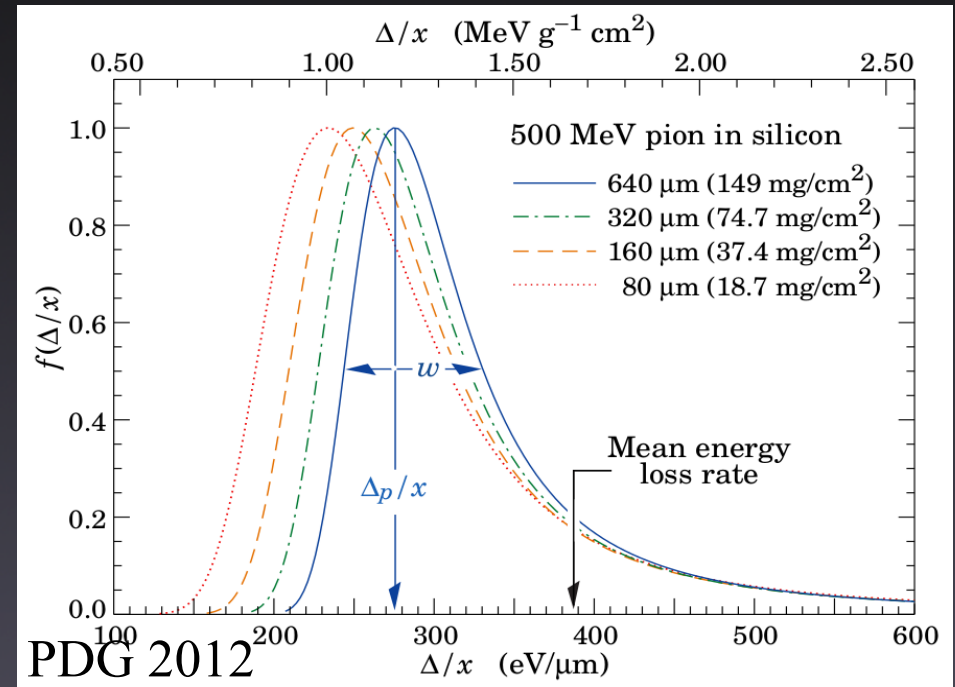
$$\theta_0 = 13.6 \frac{\text{MeV}}{\beta c p} \cdot Z \sqrt{x/X_0} [1 + 0.0038 \ln(x/X_0)]$$

$$X_0 = \frac{716.4A}{Z(Z+1) \cdot \ln(287/\sqrt{Z})} \cdot \frac{1}{\rho}$$



# Modeling the Energy loss

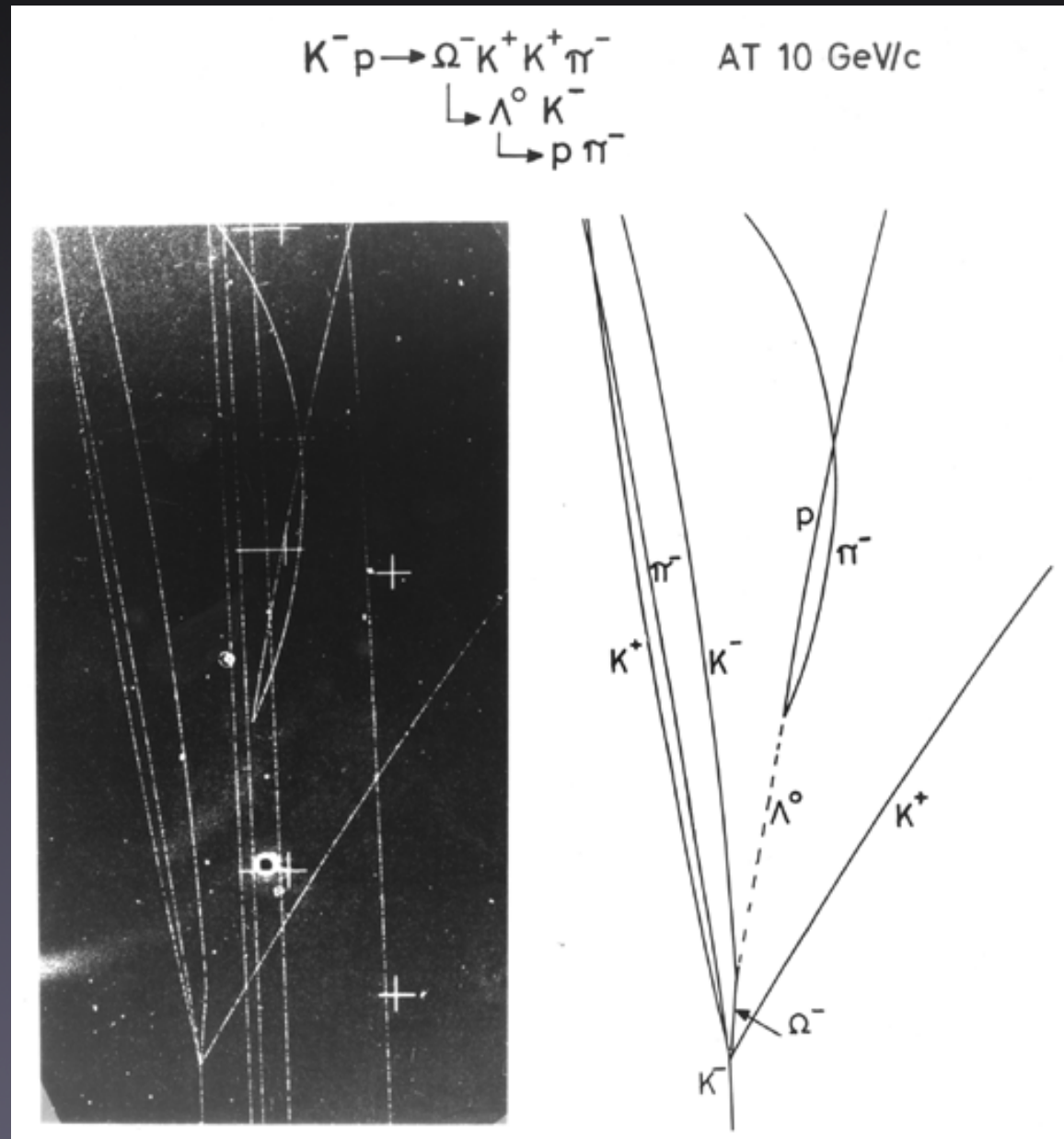
- For single particles
  - Strong fluctuations on the individual particle level
  - Pure Bethe Approach not useful
- Best described by a Landau-Function
  - 90 % of interactions have less than mean energy loss rate
  - But large tail of large energy loss events



## Note:

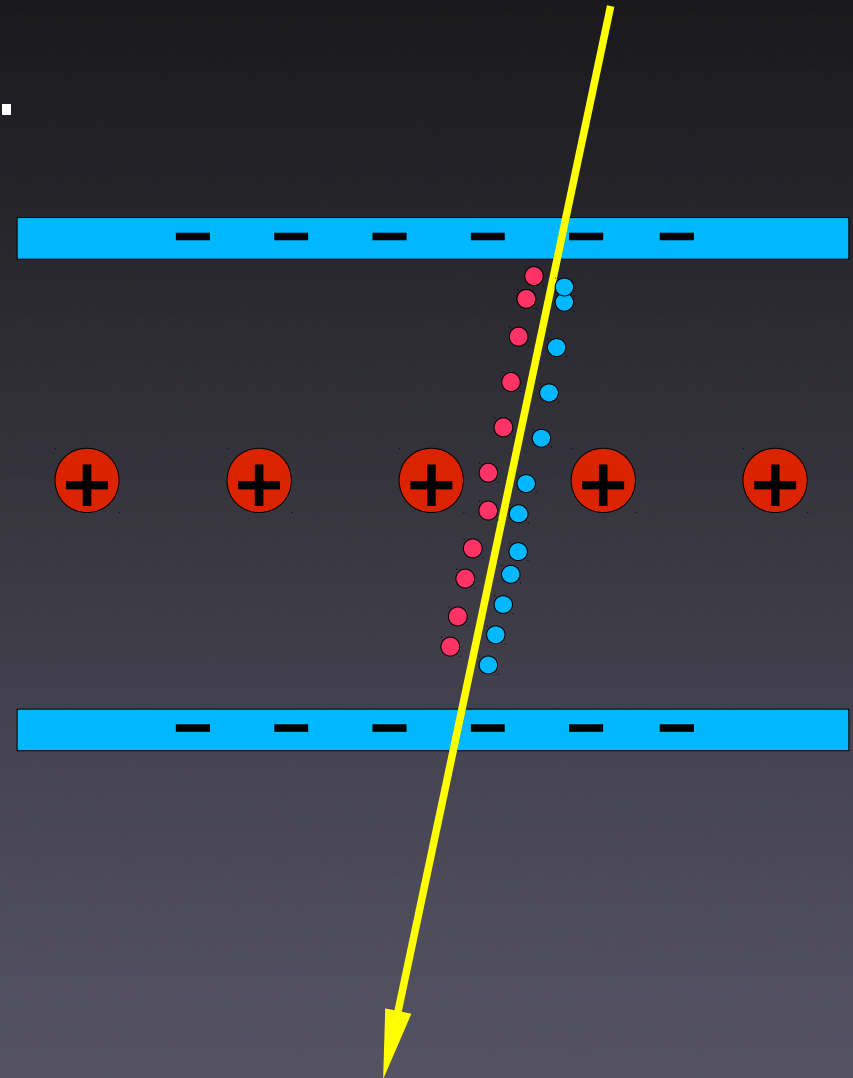
The Landau-Function itself is an approximation for thin tracking layers

# The Bubble Chamber



# Wire chambers

- Bubble Chambers are great...
  - Slow
  - Readout by photographs
- Mid 60's
  - Wire chambers as most basic electronic tracking chambers
- Basic principle
  - HV Wire in gas-filled volume
  - Electrons drift to the closest wires
  - Avalanche effect to amplify charge



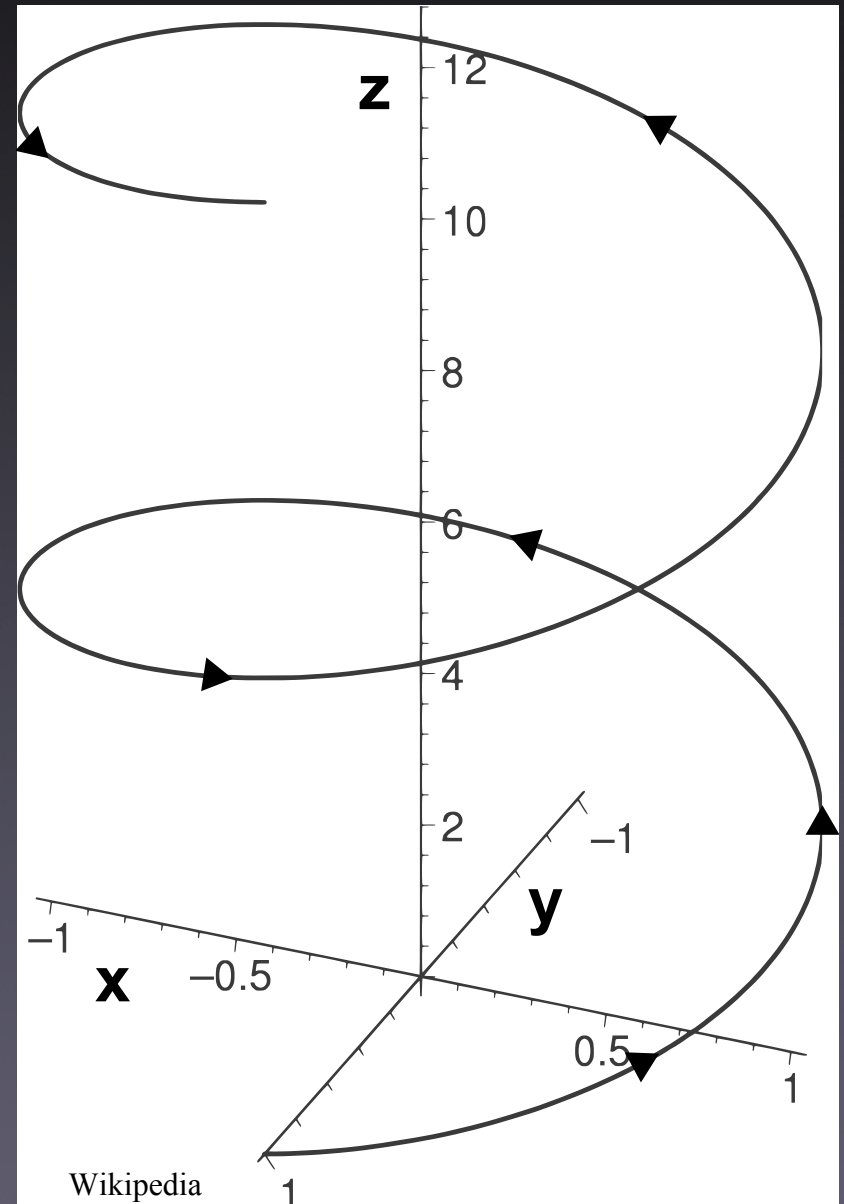


# Particles in a magnetic field

- All driven by the Lorentz Force

$$\vec{F} = q \cdot \vec{v} \times \vec{B}$$

- Particles trajectories follow a helix
  - Arc/Circle in xy
  - Line in z
- Various parametrizations
  - Each experiment has one...

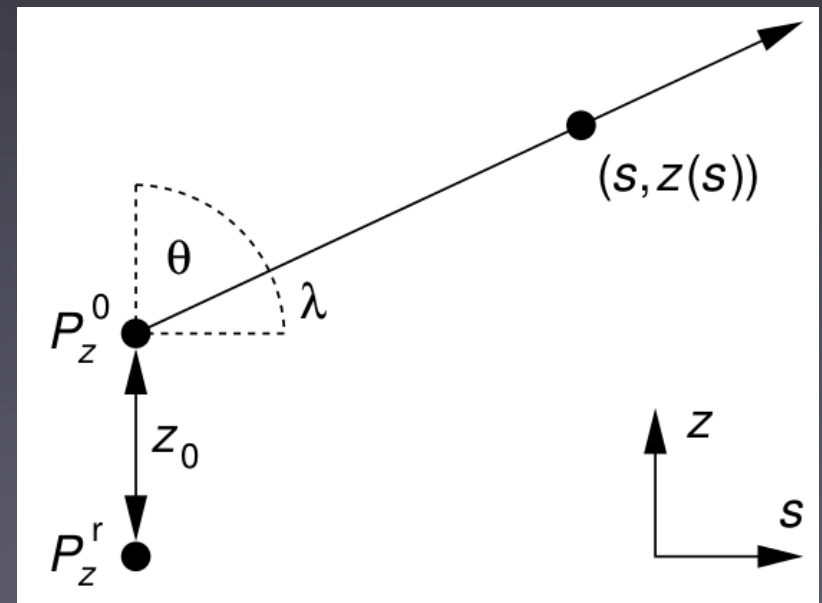
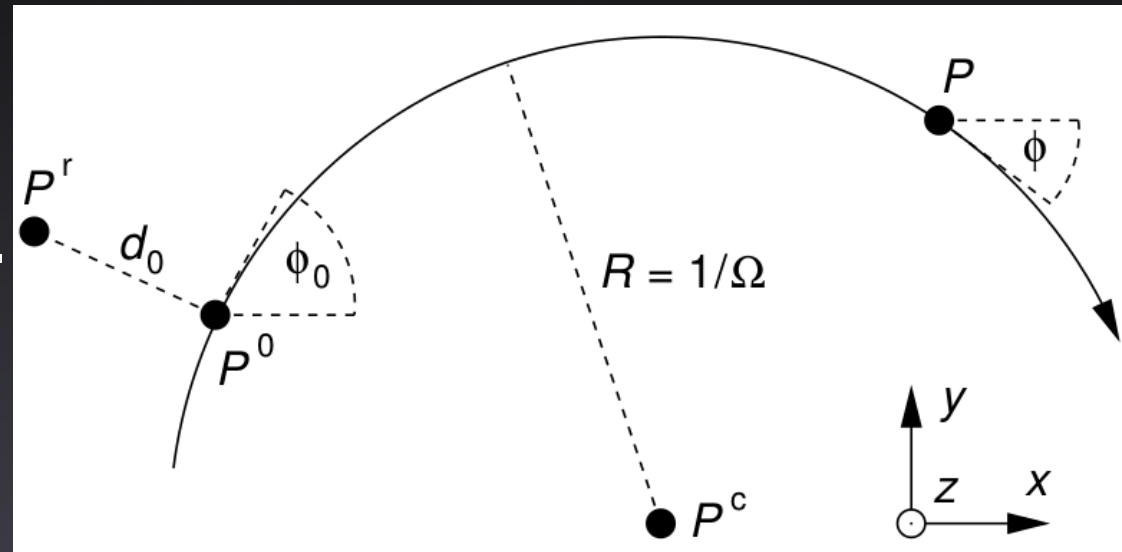


# LCIO Helix Parametrization

- 5 Parameters

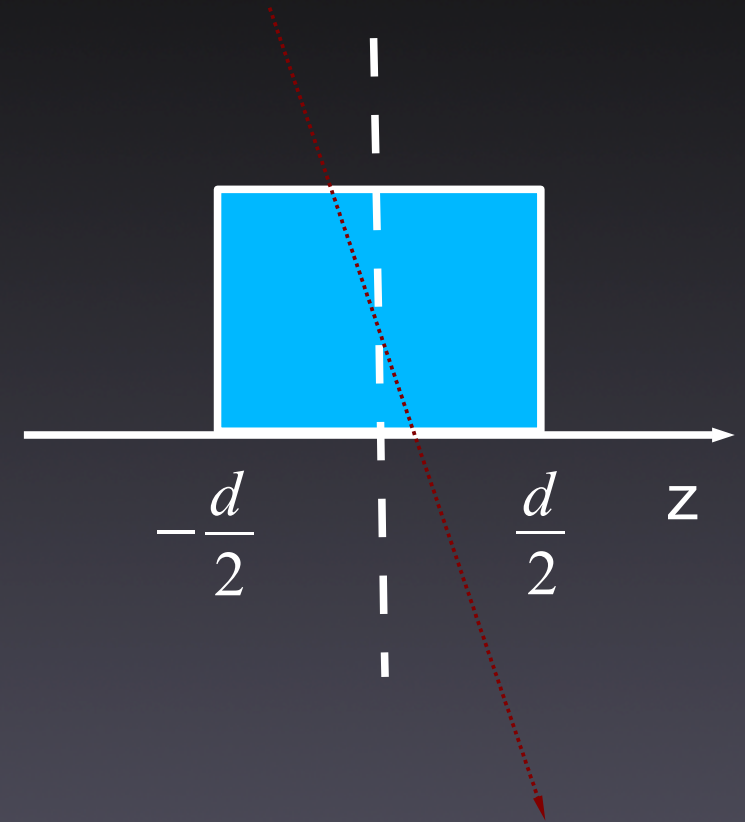
- $\phi_0$  : azimuthal angle of the momentum at the p. c. a.
- $\Omega$  : track curvature
- $d_0$  : signed impact parameter in xy
- $\tan\lambda$  is the slope  $dz/ds$  of the straight line in the sz plane
- $z_0$  : position of the track at the p. c. a.

- See LC-DET 2006-004



# Single Point Resolution

- The figure-of-merit of any tracking detector
- Single Detector element
  - Pitch  $d$
- Track Probability ( $D(z)$  is flat
  - Expectation value is 0 (center)
- Variance is:  $\sigma_z^2 = \int (z - \langle z \rangle)^2 dz / \int D(z) dz \quad \langle z \rangle = 0$



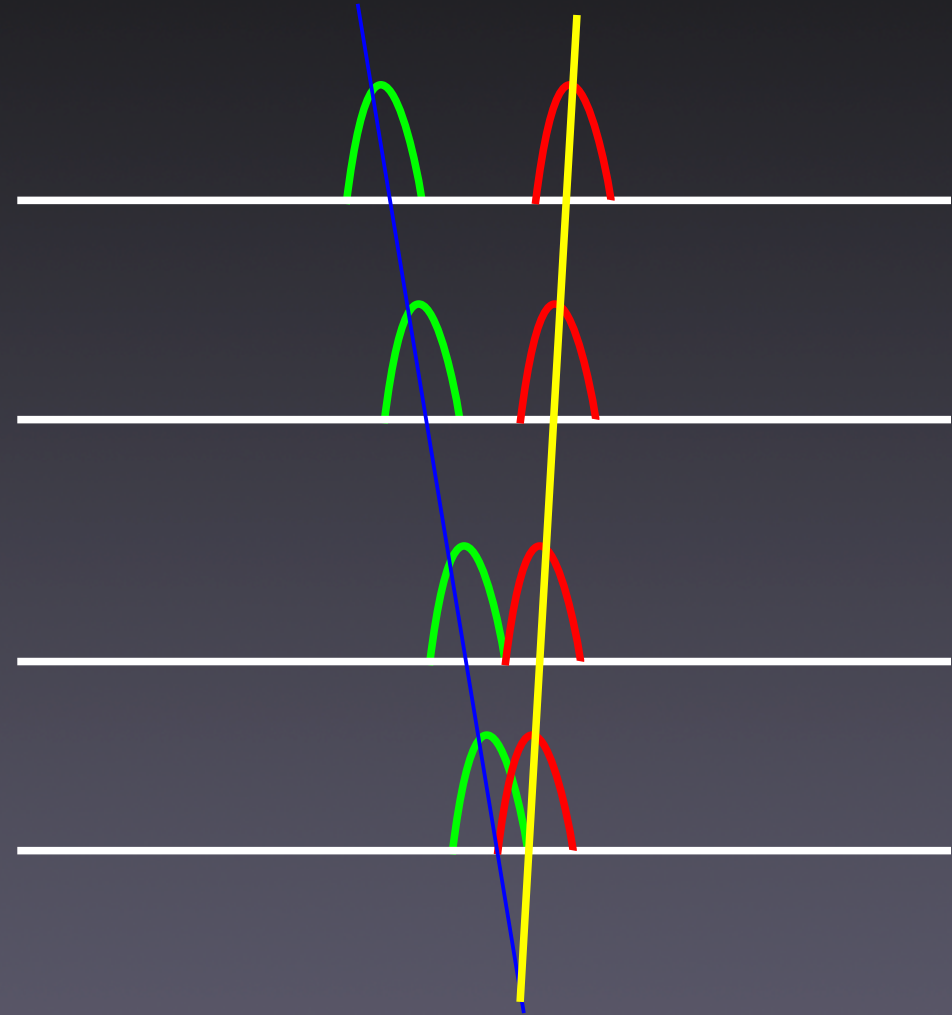
$$\sigma_z^2 = \int_{-\frac{d}{2}}^{+\frac{d}{2}} z^2 dz / d$$

$$\sigma_z^2 = \frac{d}{\sqrt{12}}$$



# Two-Track Separation

- How well can one separate two adjacent tracks
- Driven by single point resolution ( $d/\sqrt{12}$ )
- Important in dense environments
  - e.g. Tracking within Jets
- Improving separation...
  - More granularity
  - Smarter Tracking



# Tracking resolution

- Ultimately Tracking resolution driven by
  - Single Point Resolution
  - Multiple-Scattering
- Hence
  - $\sigma_{Track} = \sqrt{\sigma_{Hit}^2 + \sigma_{MS}^2}$
- Notes
  - Multiple Scattering dominates at low momenta ( $\sim < 10\text{-}20 \text{ GeV}$ )
  - At higher momenta the single-point resolution becomes the limiting factor ( $\sim > 50 \text{ GeV}$ )

# Roadmap

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**Readout  
&  
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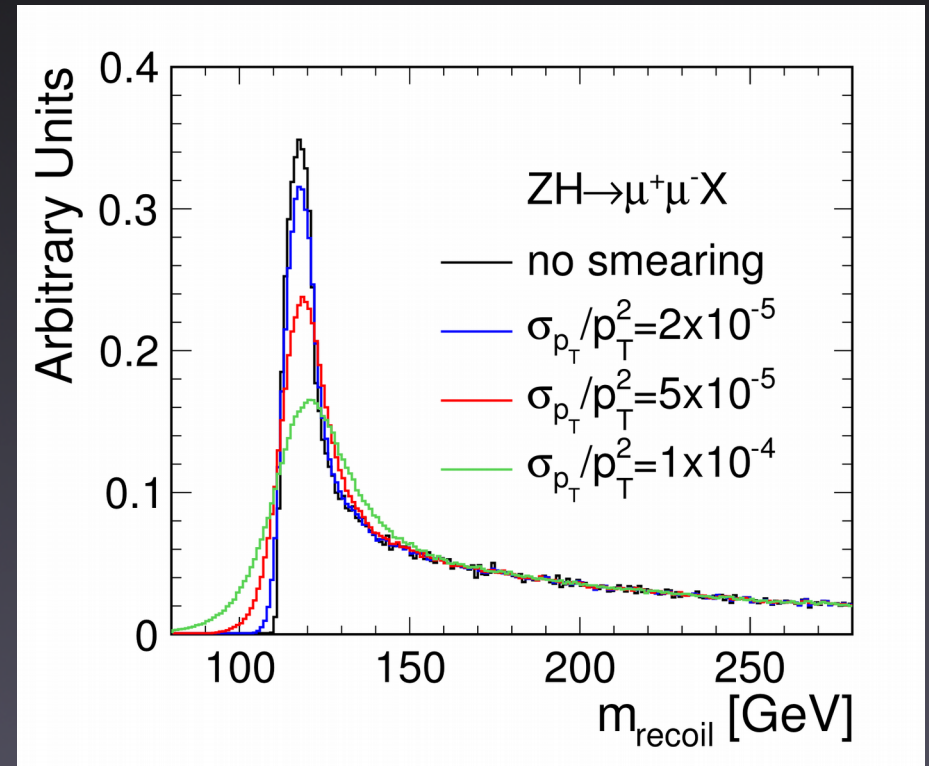
**Track  
Recon-  
struction**





# Tracking at the ILC

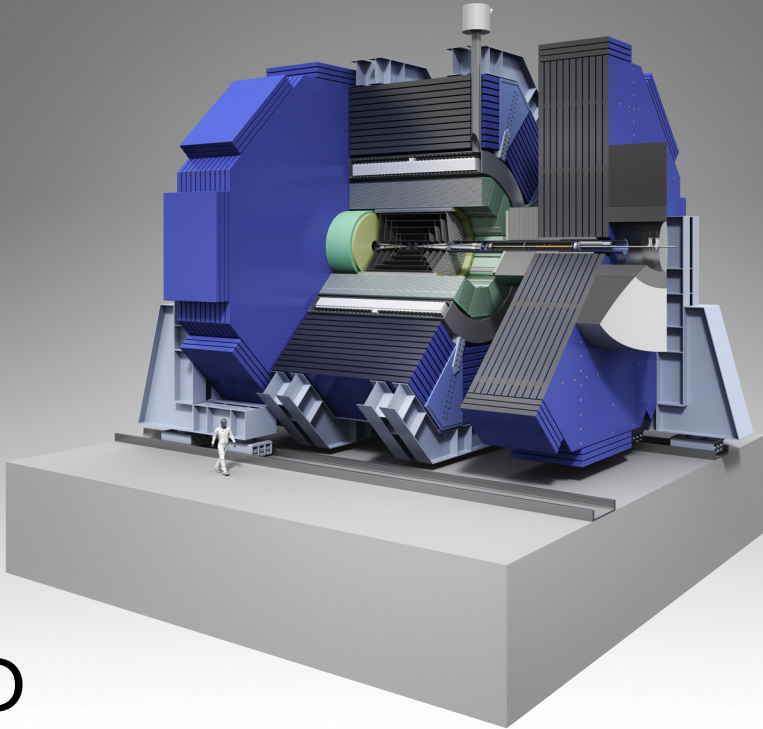
- LC tracking showcase
  - $e^+ e^- \rightarrow ZH \rightarrow \mu^+ \mu^- X$
  - Measuring the Z recoil mass
- Excellent Tracking resolution is key to this measurement
- Trade-off between resolution and required luminosity



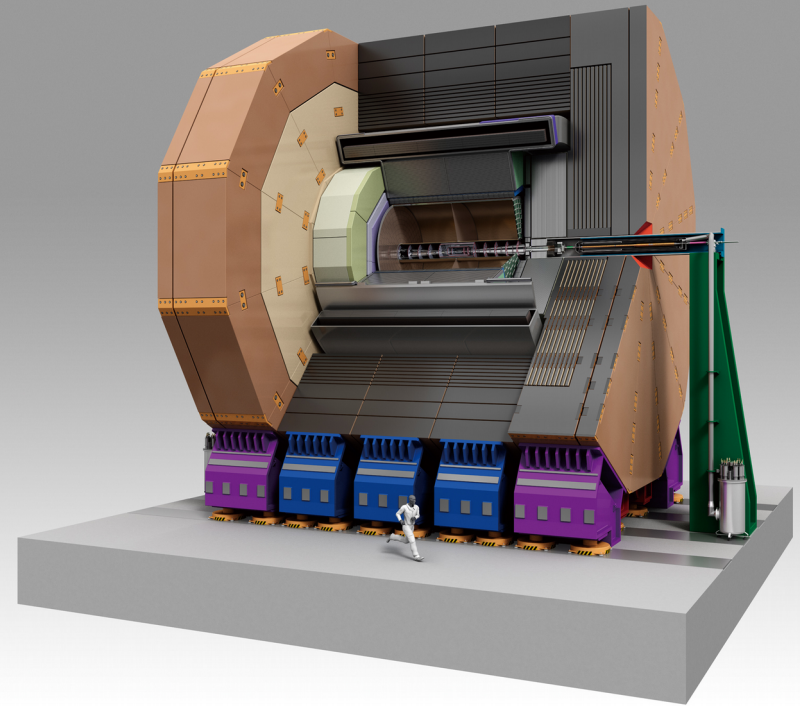
# Tracking at the ILC (II)

- Linear Collider Detectors are build around Particle-Flow paradigm (see Mark's Talk)
- This means combining the tracking and the calorimeter information
  - LC physics is very frequently multi-jet physics
  - Note that in a PFA detector  $\sim 60\%$  of the jet energy is measured using the tracker
- Excellent track resolution and track separation are essential for the PFA reconstruction

# SiD & ILD



SiD



ILD

- SiD

- $r_{\text{Tracker}} = 1.2 \text{ m}$
- $B = 5 \text{ T}$

- ILD

- $r_{\text{Tracker}} = 1.8 \text{ m}$
- $B = 3.5 \text{ T}$

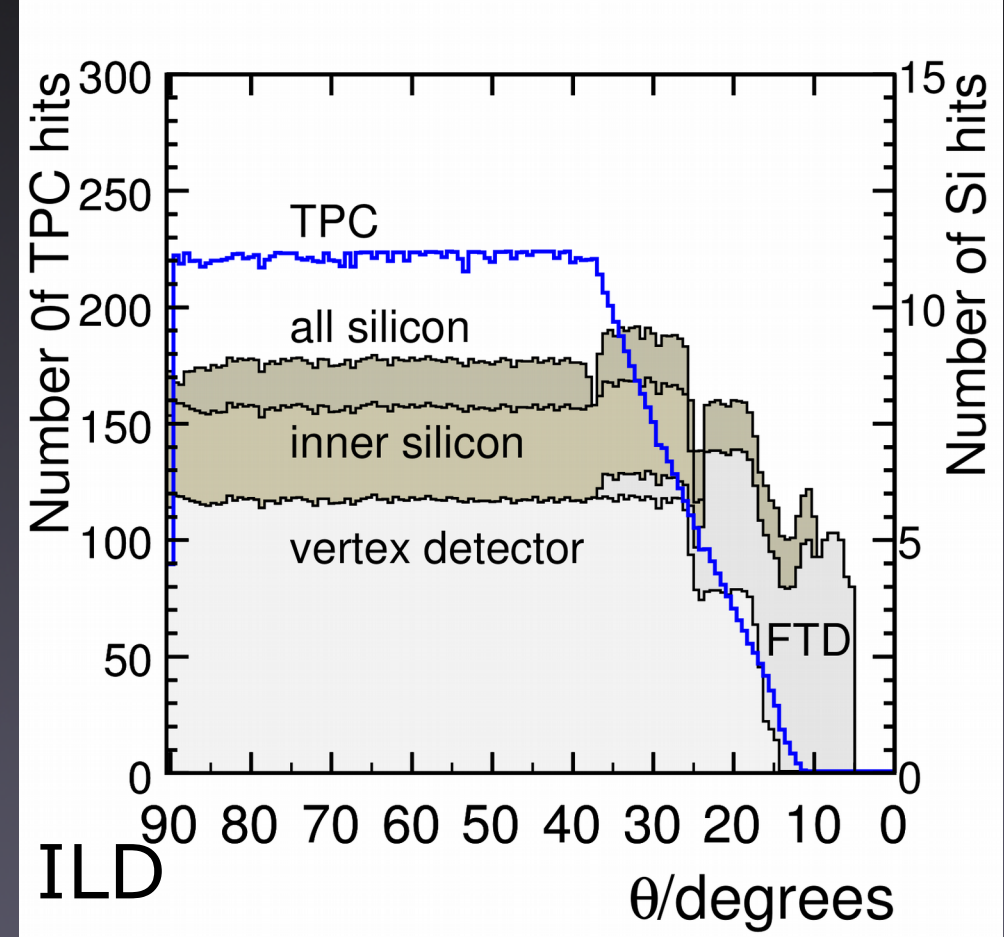
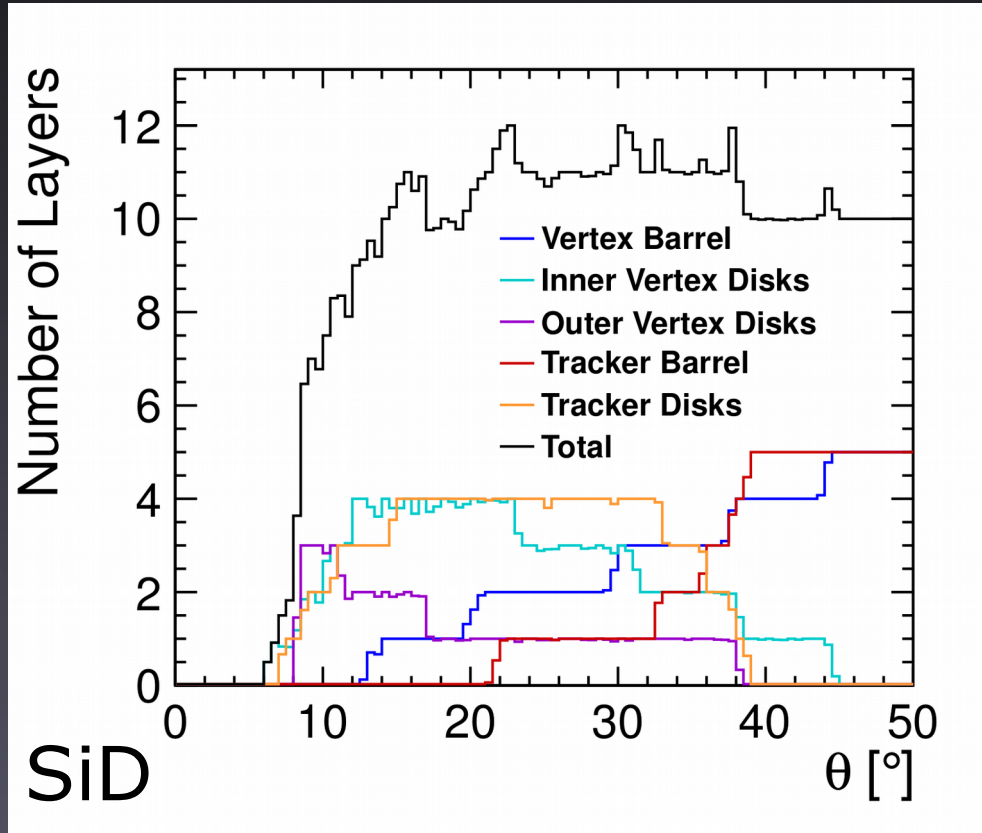


# Two Approaches

- All-silicon Tracking
  - SiD's choice
- Tracking system
  - 5 layer pixel Vertex detector
  - 5 layer Silicon strip tracker
- Few highly precise hits
  - Max 12 hits
- Low material budget
- Concept proven by CMS
- Gaseous Tracking
  - ILD's choice
- Tracking System
  - 3 double layer Vertex detector
  - Intermediate silicon layers
  - TPC
- Max number of hits
  - 228
- High hit redundancy
- Classical approach

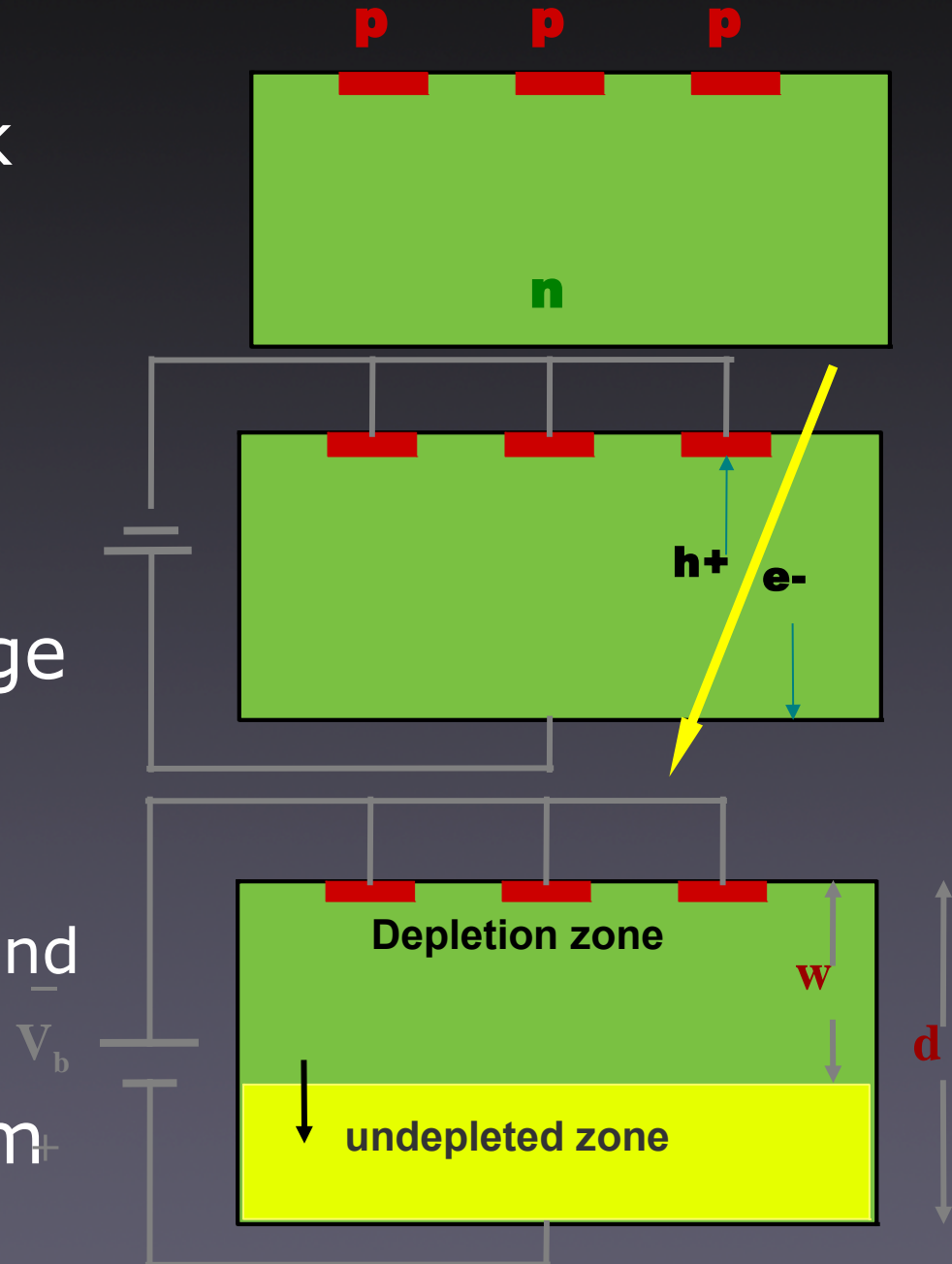


# Available Hits



# Silicon Detector Basics

- Basic building block
  - pn-junction (aka diode)
  - Reverse-bias
  - Fully depleted
- Collecting the charge
  - Either holes or electrons
  - Using charge drift and diffusion
- Thickness  $\sim 300\ \mu\text{m}$

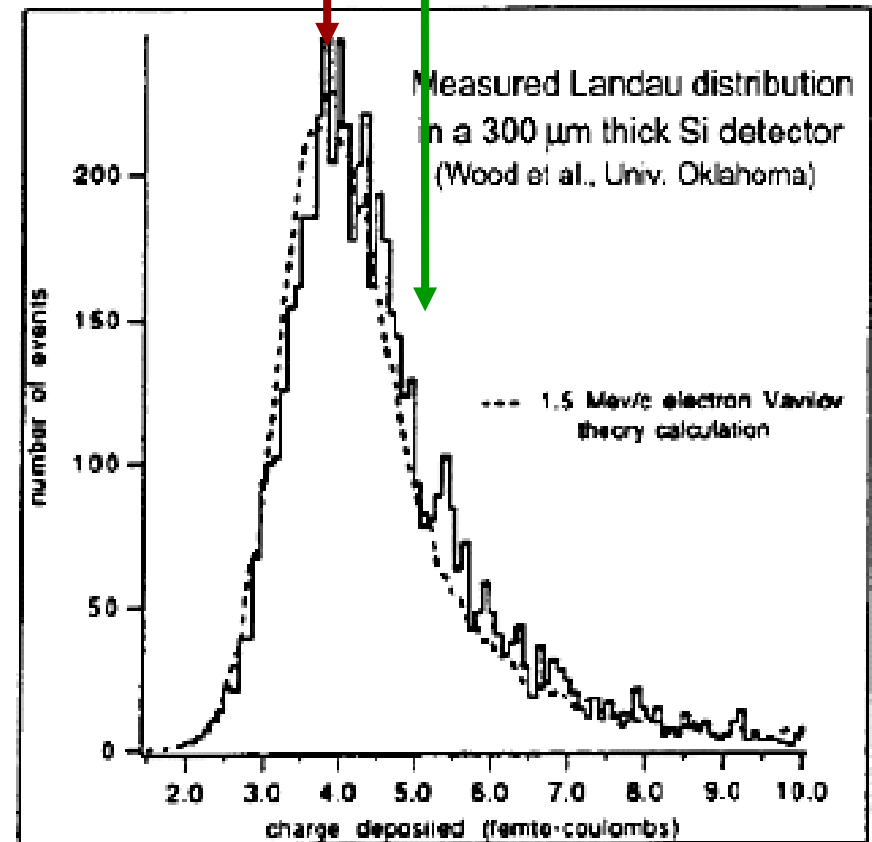


# The collected Charge

- Assuming Minimum Ionizing Particle (MIP)
- Mean Energy loss
  - $dE/dx_{Si} = 3.88 \text{ MeV/cm}$ ,  
for  $300 \mu\text{m}$  thick =  $116 \text{ keV}$
- Most Probable Loss ( $0.7$  mean) =  $81 \text{ keV}$ 
  - $3.6 \text{ eV}$  needed to make  $e^-$ - $h$  pair
  - $22500 \text{ e}^-$  produced

Most probable charge  $\approx 0.7 \sim$  mean

Mean charge



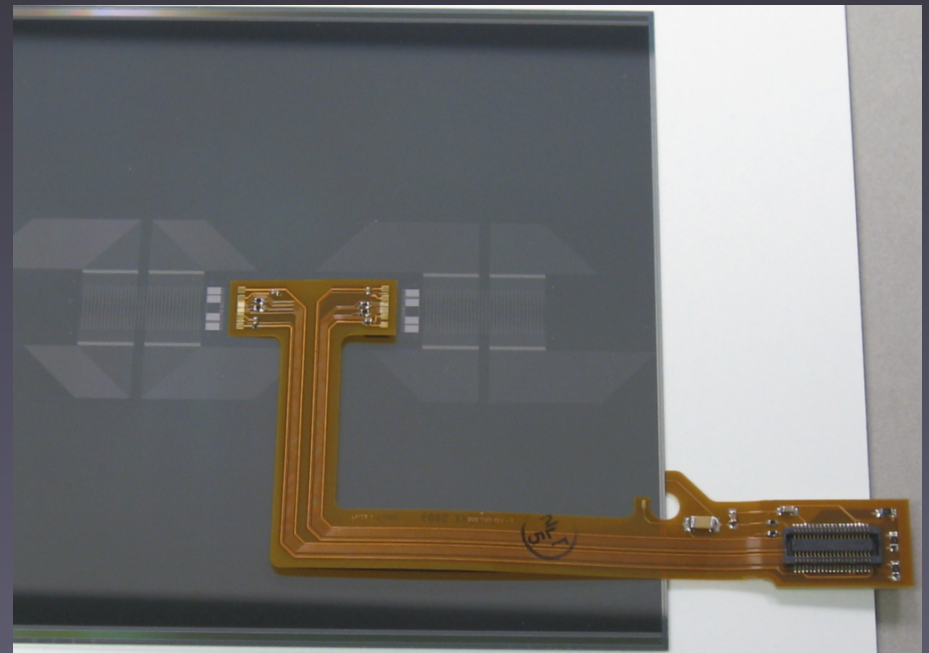
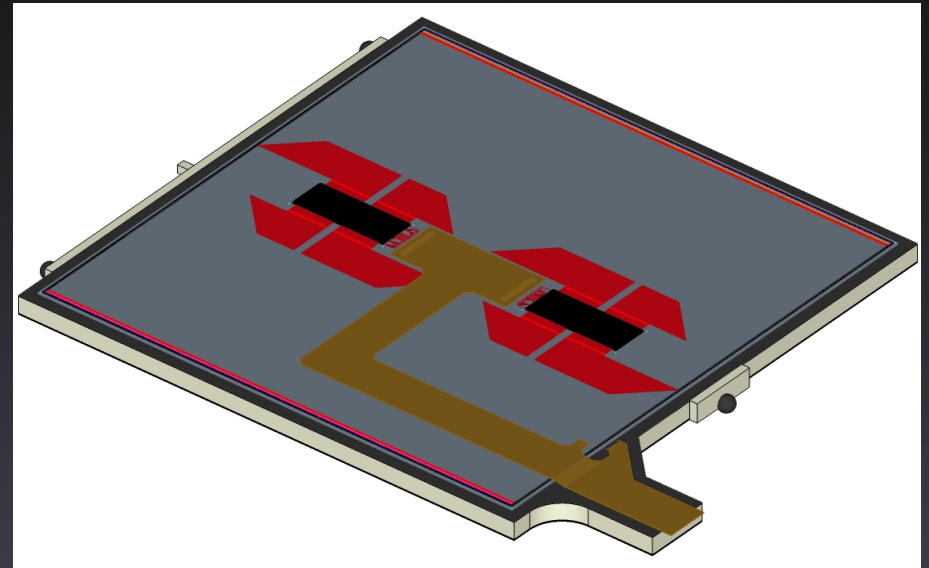
# Strips, Strixels, Pixels

- Silicon detectors come in various flavors
- Silicon Strips
  - Small pitch strips ( $\sim 50\text{-}75\ \mu\text{m}$ ),  $\sim$  several cm long
  - Gives a 2D hit (usually in  $r\phi$ )
  - Z information is weak (cm level)
- Silicon Pixels
  - Can be as small as  $10\times 10\ \mu\text{m}$
  - Real 3D hits
- Strixels
  - Basically very short strips



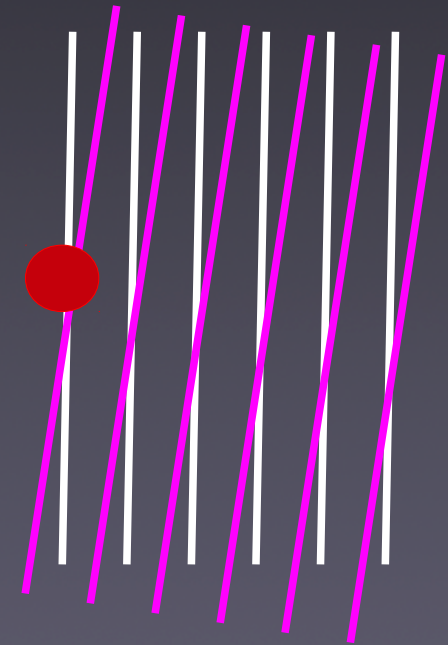
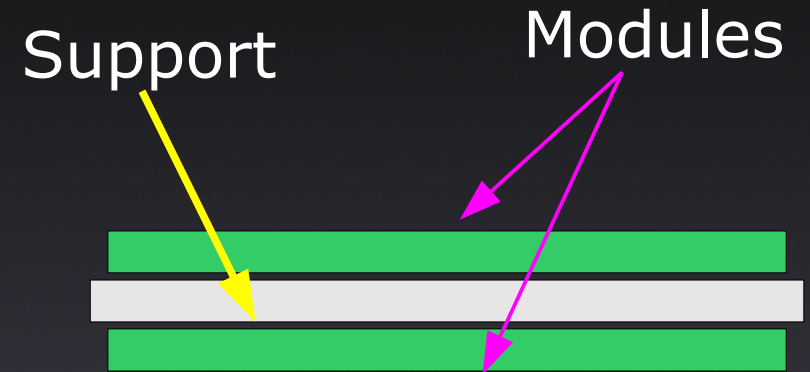
# From Sensor to Module

- The module is the tracker building block
- A typical Module consists of
  - The sensor itself
  - Interconnects
  - Readout ASIC
  - Power and data cables
  - Mechanical support structures



# Double-Sided Strip Modules

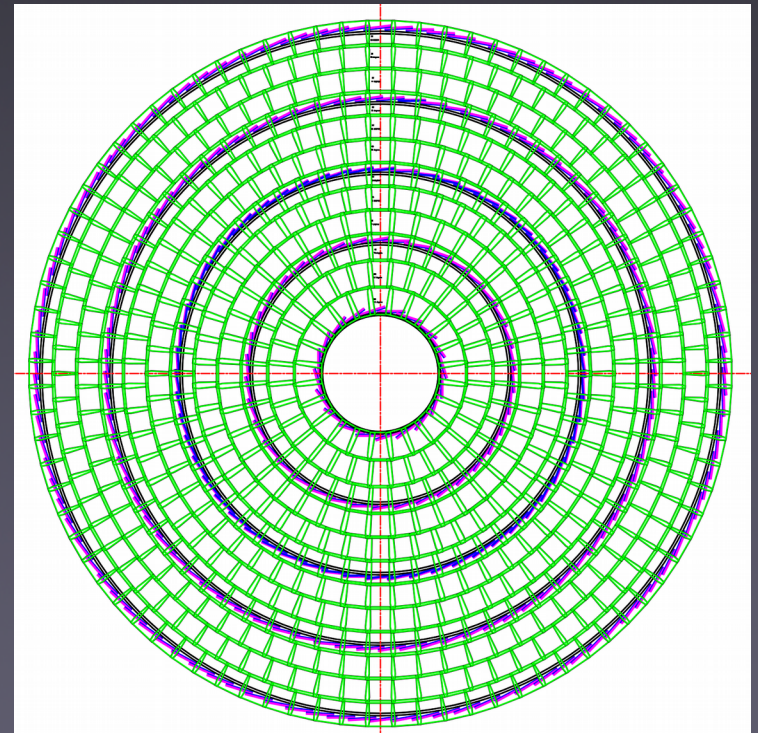
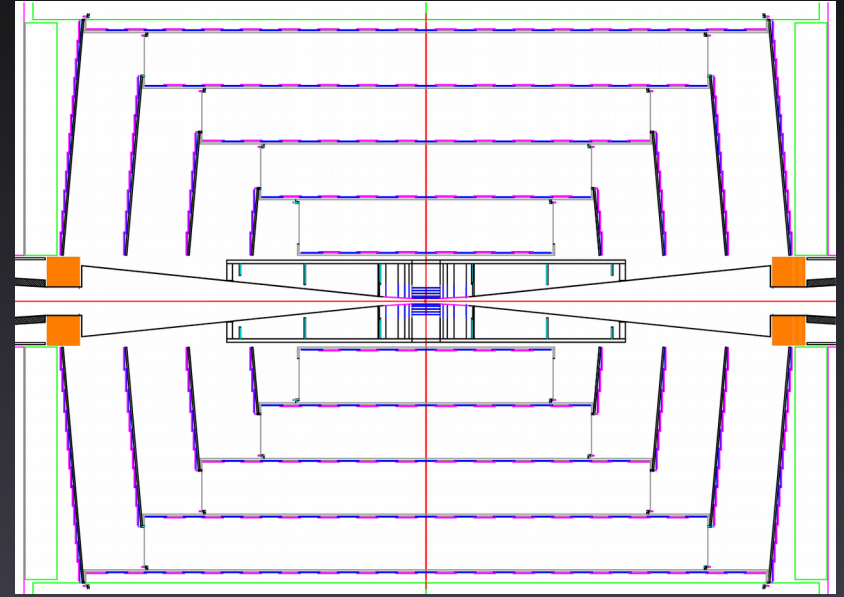
- Everyone likes 3D Hits
  - But pixels are expensive
- Idea
  - Strip modules that deliver  $\sim$  3D Hits
- Today
  - Sandwich of two strip modules
  - Either 90 degree (rare)
  - Small angle stereo





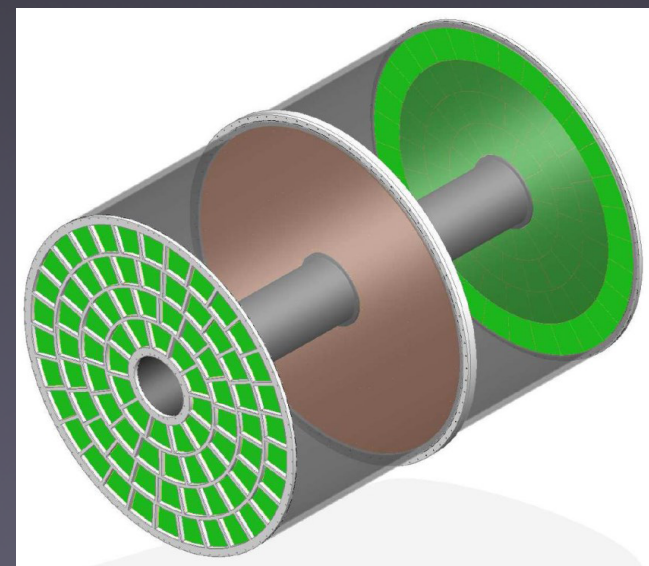
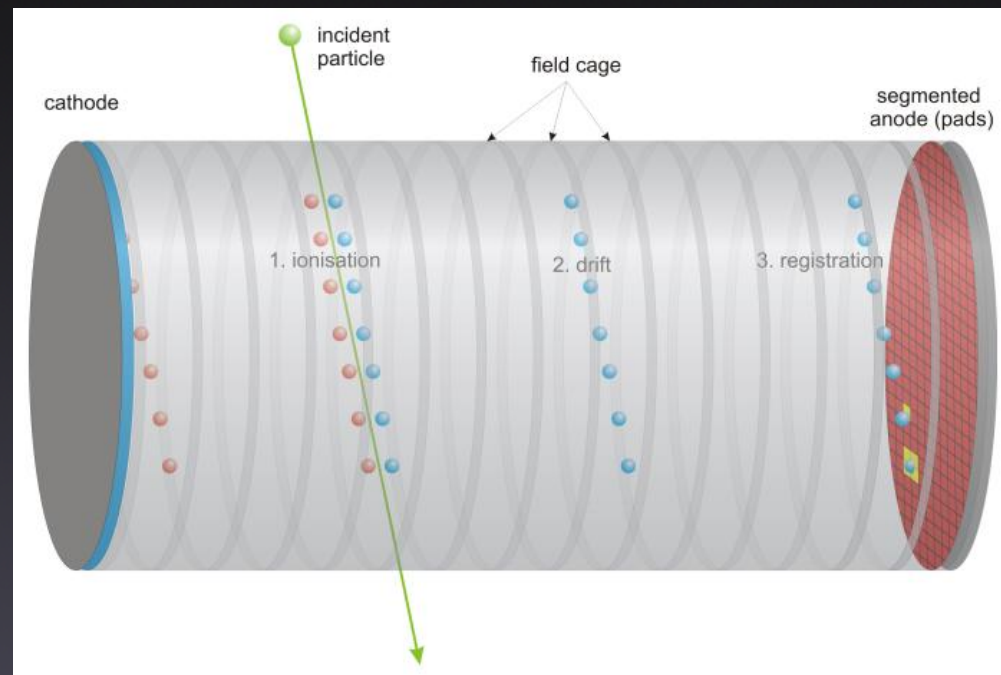
# The SiD Tracker

- All silicon tracker
  - Using silicon micro-strips with Double metal layers
- 5 barrel layers and 4 disks
- Cooling
  - Gas-cooled
- Material budget
  - less than 20 %  $X_0$  in the active area
- Readout using KPiX ASIC
  - Bump-bonded directly to the modules



# Time Projection Chamber

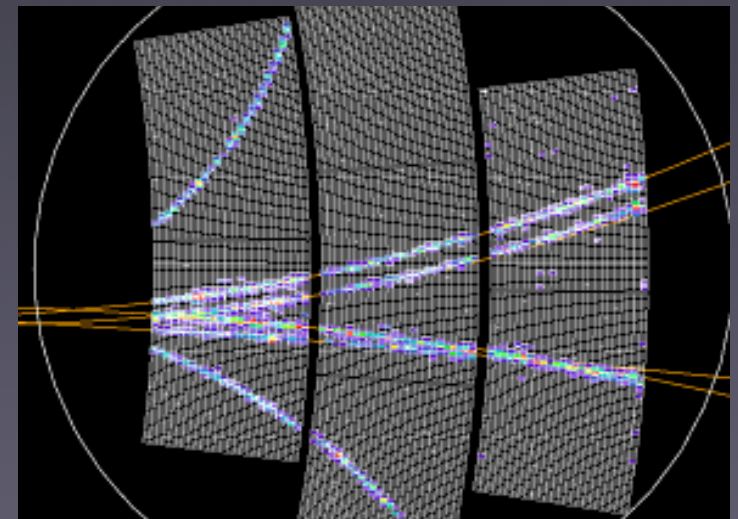
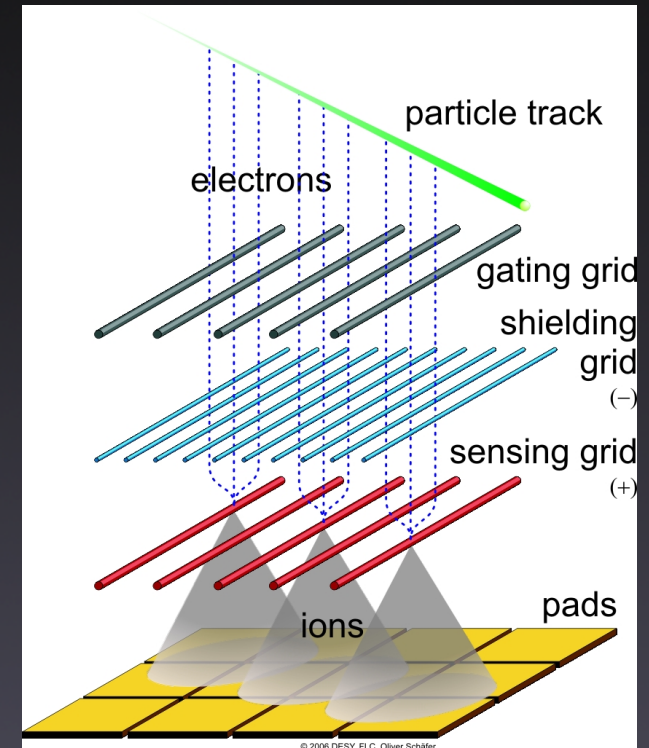
- Invented in the 70's
- Uniform electric field
  - drifts tracks of electrons towards into 2D readout pads at the endplate.
  - The signal amplitudes and arrival times provide 3D information
- Inside solenoid B field
  - Particle momenta can be estimated from the track curvature



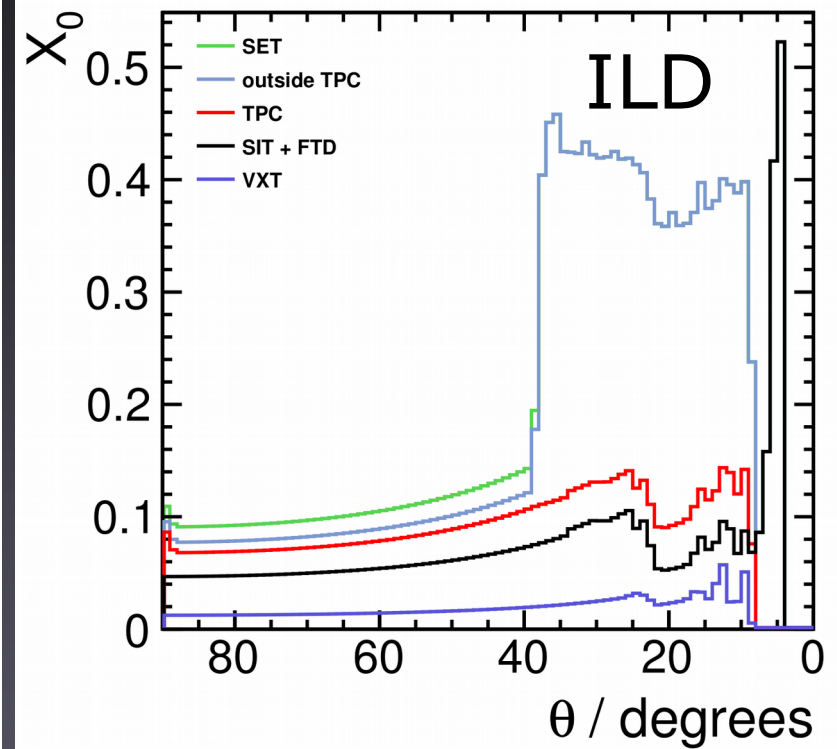
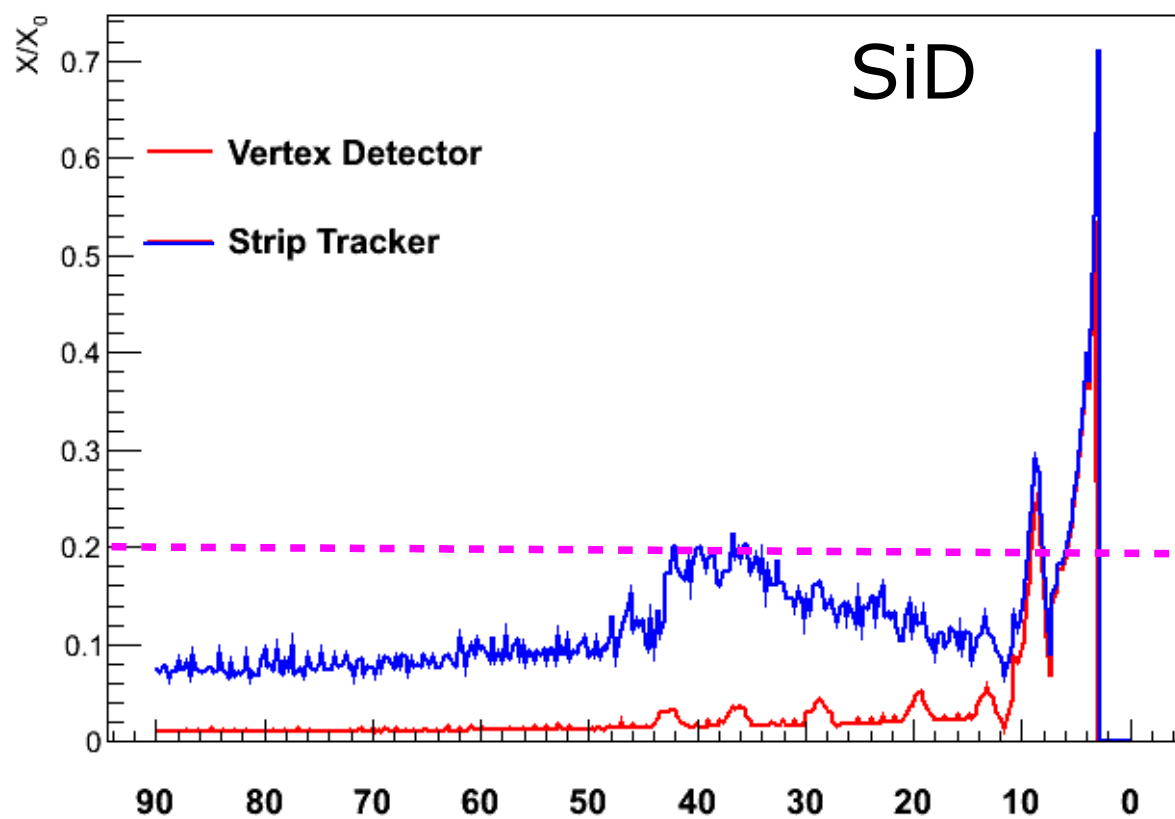


# Endplate

- Drifted charge is amplified at the TPC endplate
- Today:
  - Two main options for gas amplification: GEM or Micromegas
  - Readout pad size  $\sim 1 \times 6 \text{ mm}^2$   $10^6$  pads/endplate
- Readout electronics integrated in the endplate



# Material Budget



Both concepts have very aggressive material budget

# Roadmap

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struction**

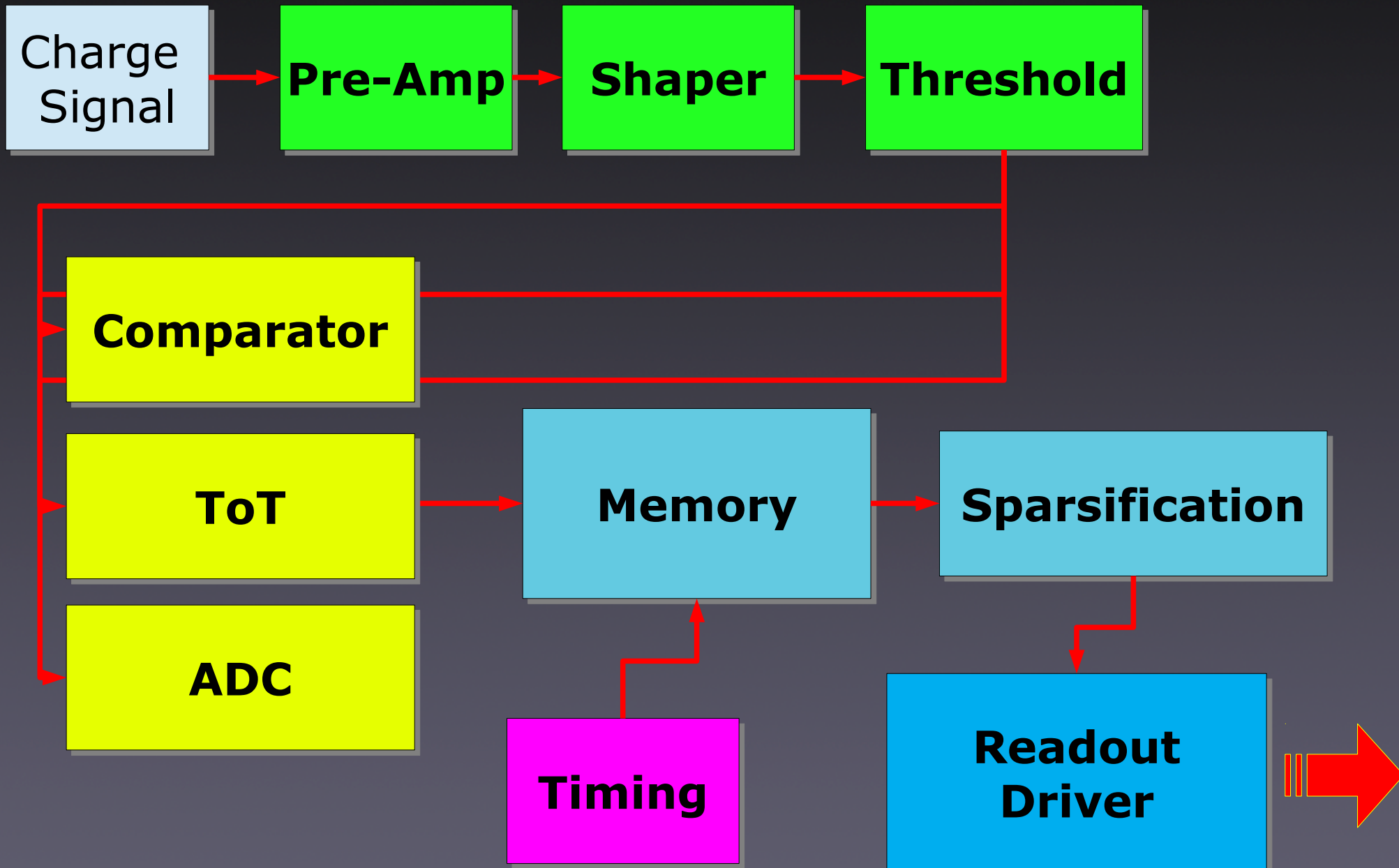


# Readout ASICS

- The Readout ASIC is a key ingredient to an excellent tracker
- The ASIC
  - Amplifies and digitizes the charge
  - Provides timing information
  - Buffering
  - Transfers data to the DAQ
- ASIC are specifically designed for each tracker
  - Industry-level CMOS design
  - Making a good ASIC is an art

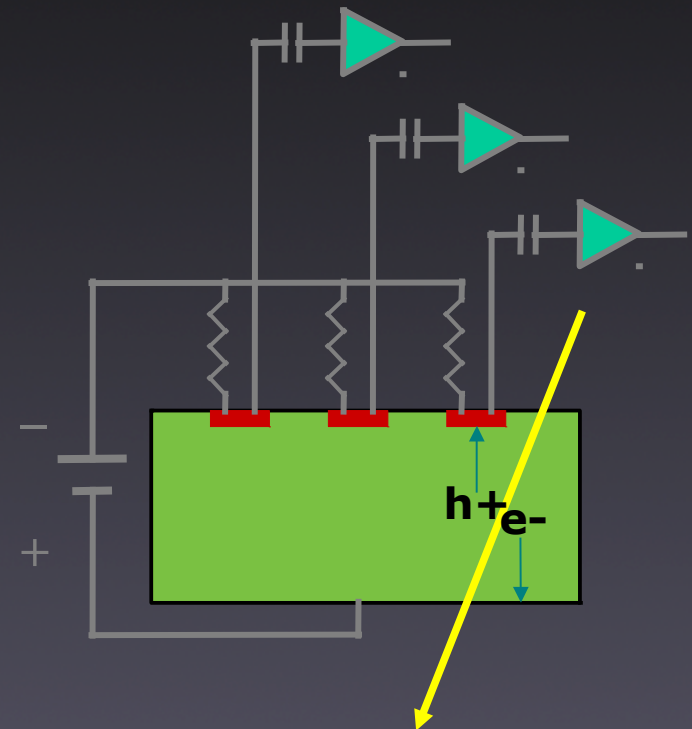


# ASIC building blocks



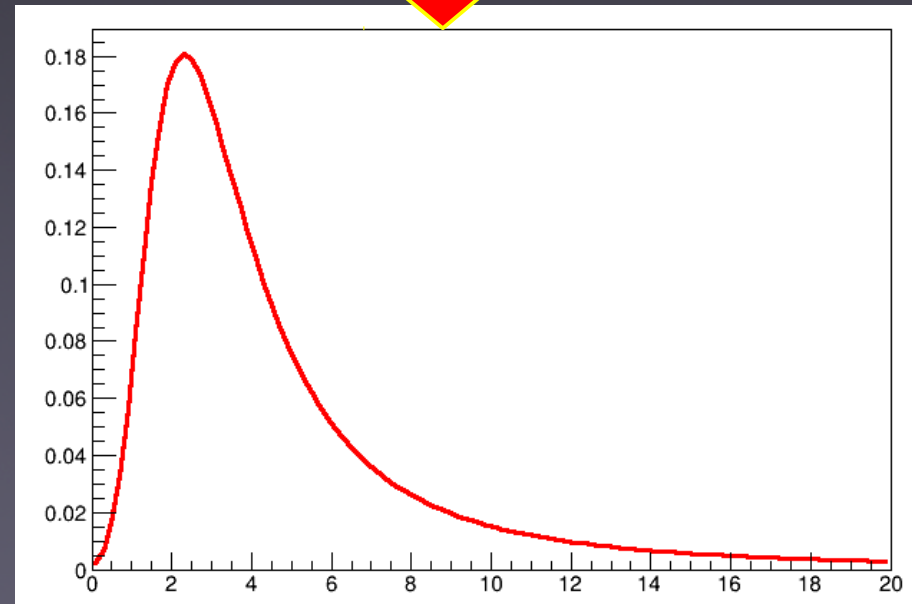
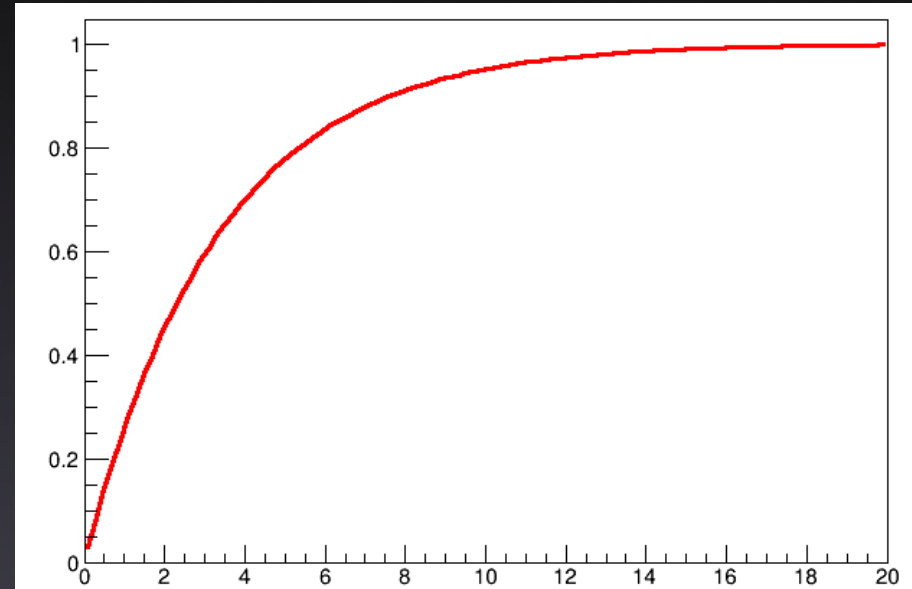
# Readout and Pre-Amp

- isolate strips from each other
  - collect/measure charge on each strip
  - high impedance bias connection (resistor or equivalent)
- Usually AC (capacitive) coupling for input amplifier
  - avoid large DC input from leakage current.
- Both structures are often integrated directly on the silicon sensor
  - Bias resistors via deposition of doped polycrystalline silicon, and
  - capacitors via metal readout lines over the implants but separated by an insulating dielectric layer ( $\text{SiO}_2$ ,  $\text{Si}_3\text{N}_4$ )



# Shaper

- Pre-Amp usual very “simple” and integrating
- Output signal not optimal for digitization
  - No well defined peak
  - No “clear edge” for timing
- Need to apply some level of “shaping” to make a nice pulse
  - Many shaping circuits on the market



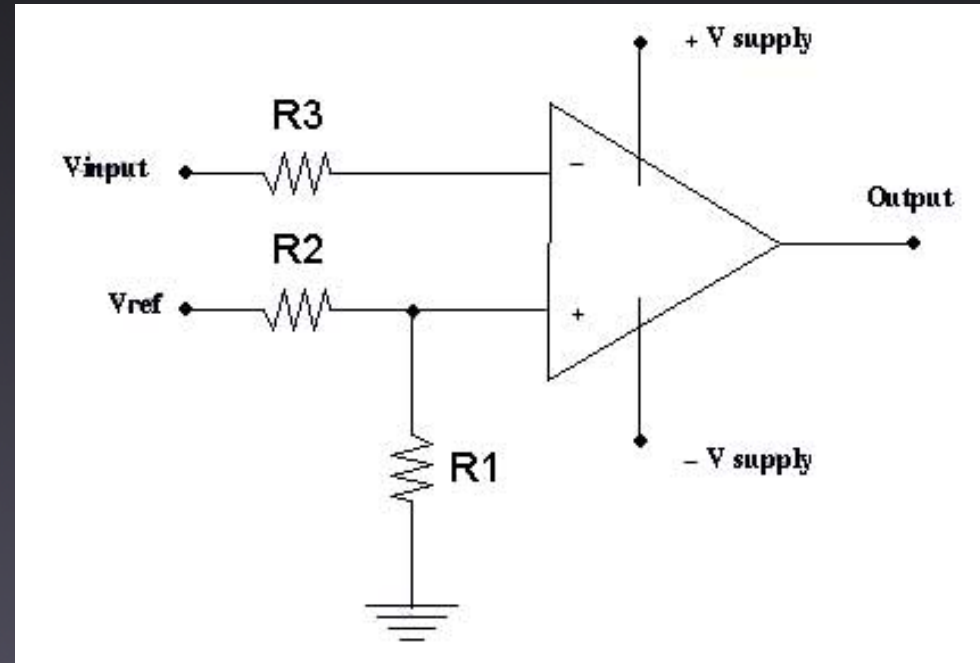
# Thresholding & Digitization

- Now the analog signal is ready for digitization
- However Digitization is costly
  - Time and power
  - Configurable Analog threshold before digitization
- Three basic types of Digitizers
  - Comparators
  - ToT (Time over Threshold)
  - ADC (Analog to Digital Converter)
- Figures of merit
  - Resolution in bits
  - Speed
  - Power consumption



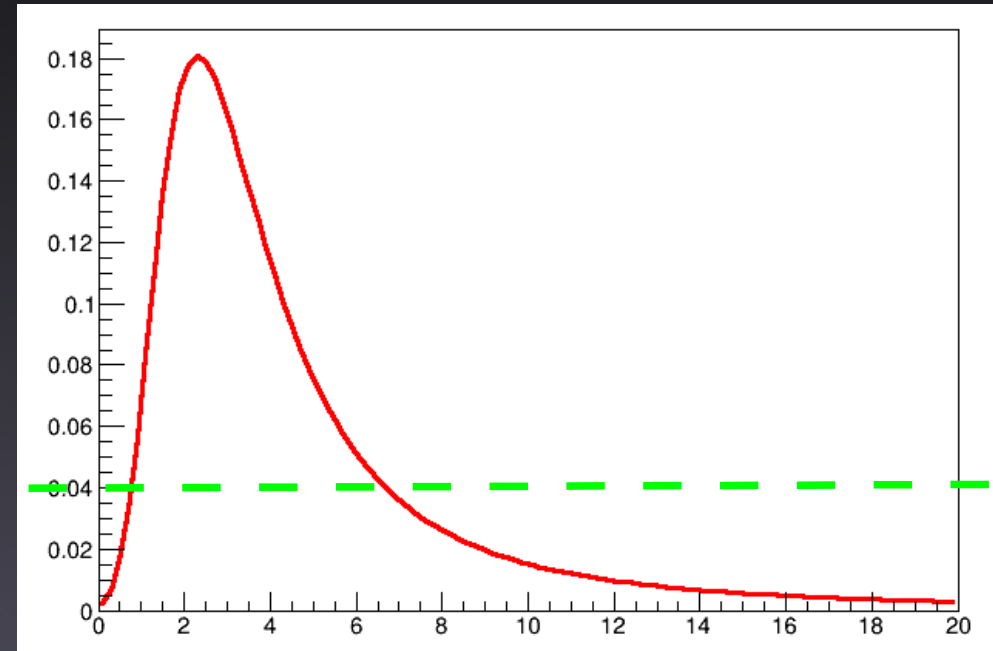
# Comparators

- A Comparator is simplest way to digitize
- Compare  $V_{\text{input}}$  to  $V_{\text{ref}}$ 
  - $V_{\text{input}} > V_{\text{ref}}$     Output=1
  - $V_{\text{input}} < V_{\text{ref}}$     Output=0
- Disadvantage
  - Simple binary information
  - Hit or no hit
- Advantages
  - Simple, fast and low power



# ToT

- This is a simple Counter
- If  $V_{\text{input}} > V_{\text{ref}}$ 
  - Counter starts
- If  $V_{\text{input}} < V_{\text{ref}}$  again
  - Stop counter
- Digitized information
  - Number of counts
- Limited by clock and signal shape



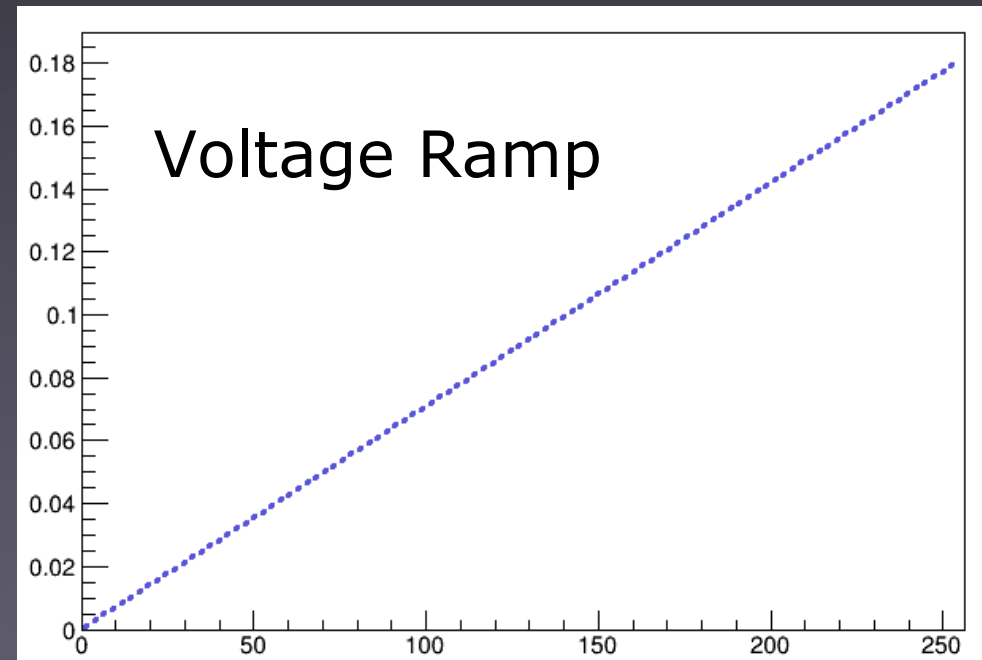
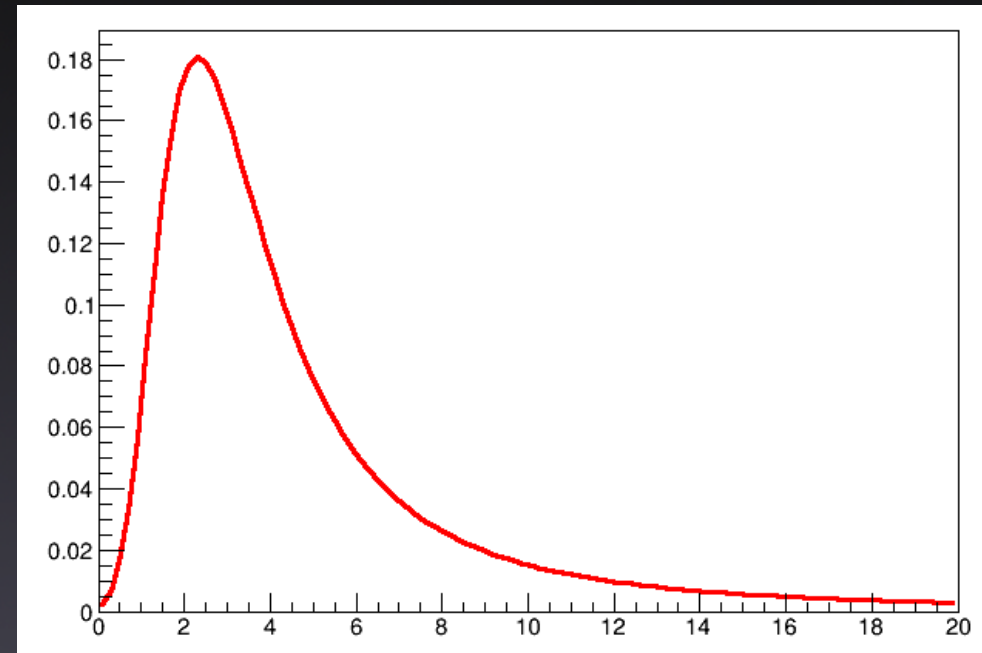
Basic Assumption  
Pulse Width  $\sim$  Pulse Height

# ADC

- ADCs are an art form these days
- Many different circuits and ideas
  - Speed of conversion
  - Resolution
  - Robustness
  - ADC design is popular thesis subject
- I'll focus on two basic types
  - Wilkinson ADC
  - FLASH ADC
- This is by far incomplete

# Wilkinson ADC

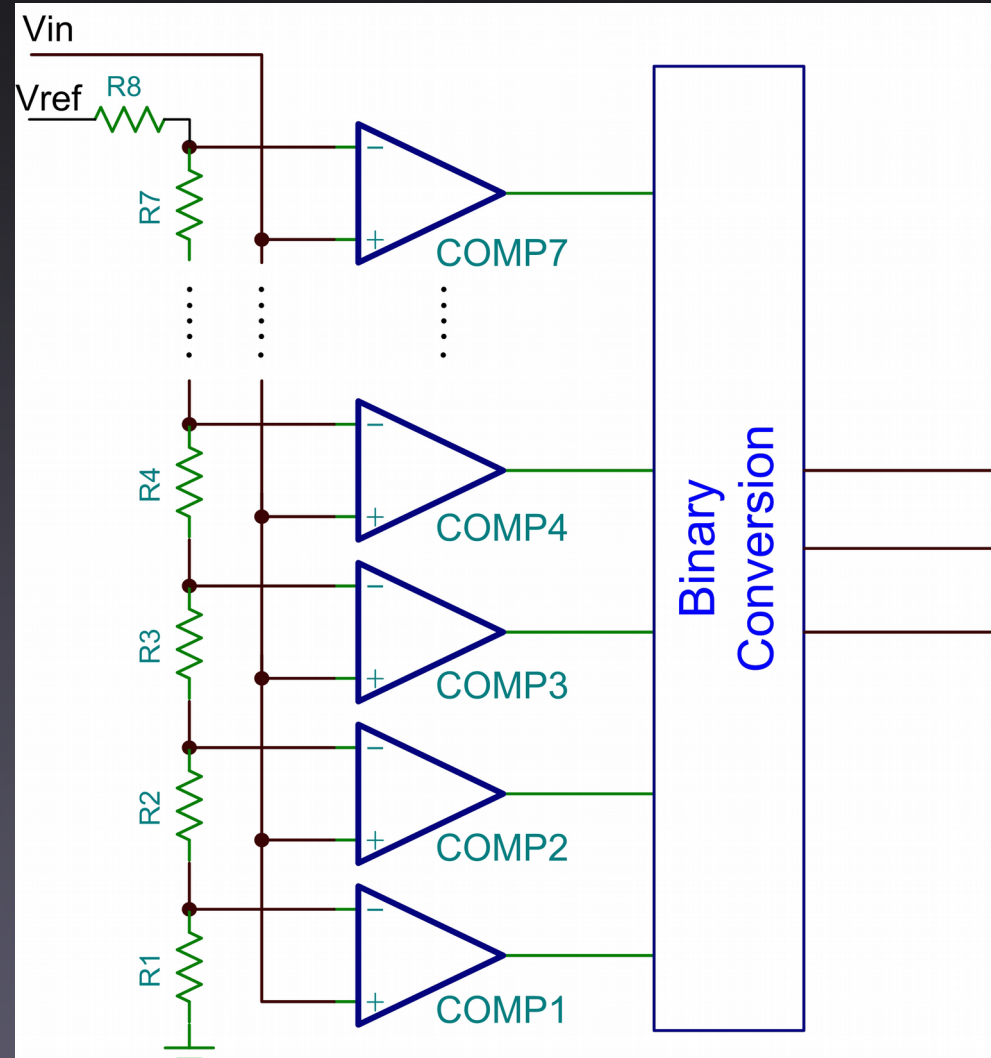
- This is a very simple ADC
- At  $t=0$ 
  - Counter starts
  - ADC generates voltage ramp
- If  $V_{\text{ramp}} = V_{\text{input}}$ 
  - Counter is stopped
  - $N_{\text{counts}}$  is digitized information
- Speed driven by counter clock
  - Slow but low-power





# FLASH ADC

- Speedwise this is the Ferrari of ADC's
  - Conversion in 1 clock cycle
- Complex with loads of circuitry
  - Power-hungry
  - N bits  $2^n - 1$  Comparators needed
- FLASH ADCs are chosen when speed is essential



# Writing the Data

- After digitization data is transferred to the buffer memory and combine with the timestamp info
- For a tracker
  - 1 % Hit occupancy
- So for 256 channel Readout ASIC
  - A few hits (2-3)
- Remainder of data could be eliminated
  - Digital Threshold and sparsification

# Sparsification

- Example
- Raw data (16 bytes)
  - 00 01 01 09 02 25 03 9F 04 17 05 01 06 00 07 01
- Sparsification (Threshold > 10) (6 bytes)
  - 02 25 03 9F 04 17
- Sparsification reduces bandwidth requirements
  - Smarter chips have even more elaborate sparsifiers
- Every modern chip has some kind of sparsification circuitry
- Depends on applications
  - e.g Calorimeter chips have to deal with very high local occupancies

# Analog vs Binary

- An old discussion
- Binary only stores hit/no hit
  - Hit resolution is limited to  $d/\sqrt{12}$
  - Robust and simple
- Analog also stores the digitized pulse height
  - More information available
  - Can further improve on hit resolution
  - Better detector monitoring
- Many trackers, many opinions
  - ATLAS is binary
  - CMS is analog
  - LC detectors plan to do analog



# Roadmap

**Basics**

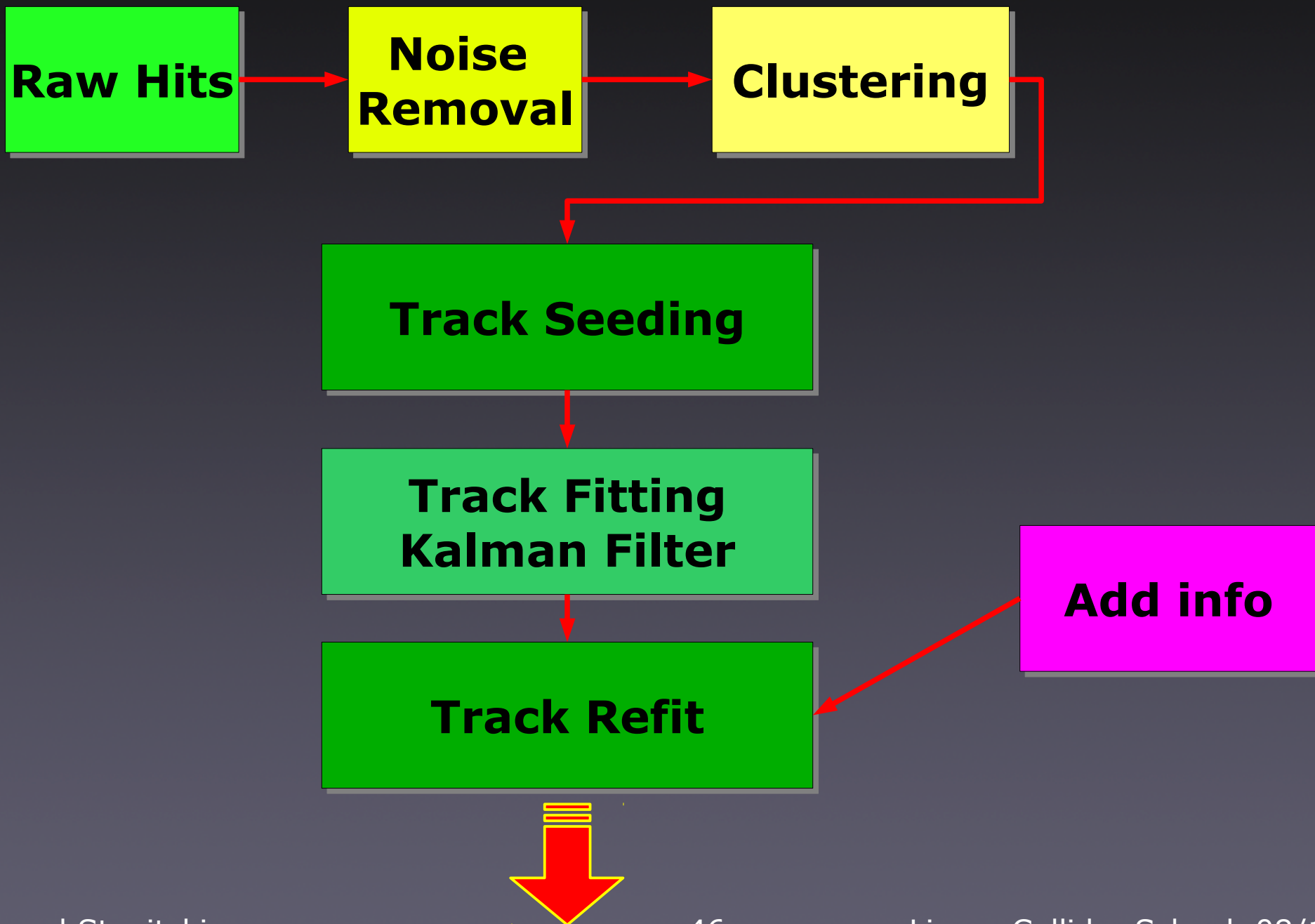
**Tracking  
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# Track reconstruction



# Noise Removal

- In Reality no detector is completely noise-free
- Noise Source
  - Random (Noise floor  $10^{-5}$ ,  $10^6$  channels ...)
  - Hot channels
  - Pick-up Noise (from somewhere else)
- Tracking is an  $\sim n^2$  problem
  - Remove as many noise hits as possible
- Classic approaches
  - Remove all channels with Occupancies  $> O(10) \%$
  - Dedicated Noise runs during no-beam
- After Noise Removal we're ready for the first tracking step

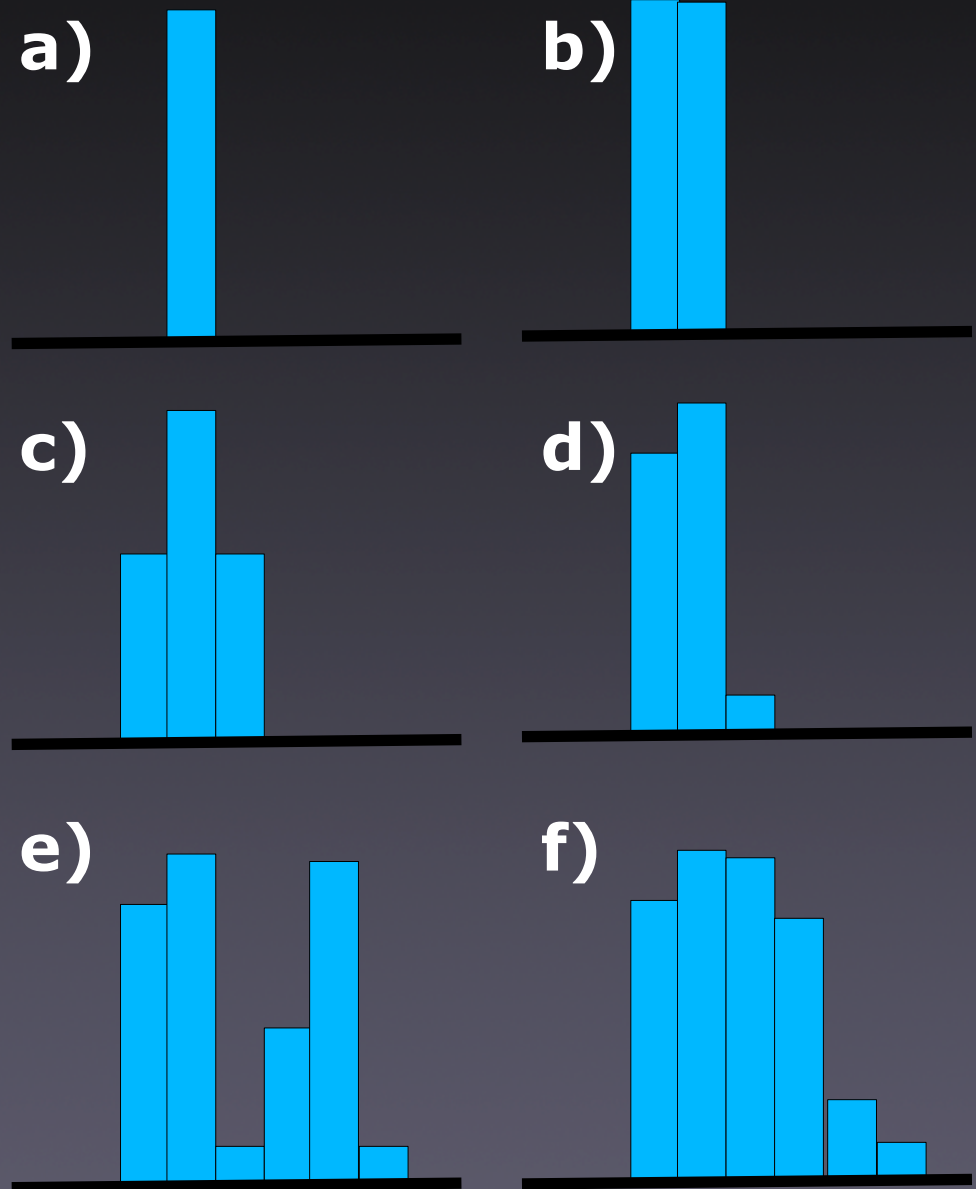
# From Hits to Clusters

- A particle may deposit charge in several strips/pixels causing several hits
  - So not every hit corresponds to a particle
  - So need to reconstruct the particle hit
- Hence Clustering algorithms are used
  - To merge hits belonging to one particle
- Clustering shows one real advantage of analog readout
  - Here the additional information really adds resolution



# Clustering

- Merging
  - Cluster all hits together until there is a channel without a hit
  - Calculate weighted mean for cluster position
- Splitting
  - Occasionally two tracks are very close
  - Hits are merged together
  - Cluster splitting to correct for this behavior
  - This can occasionally be tricky

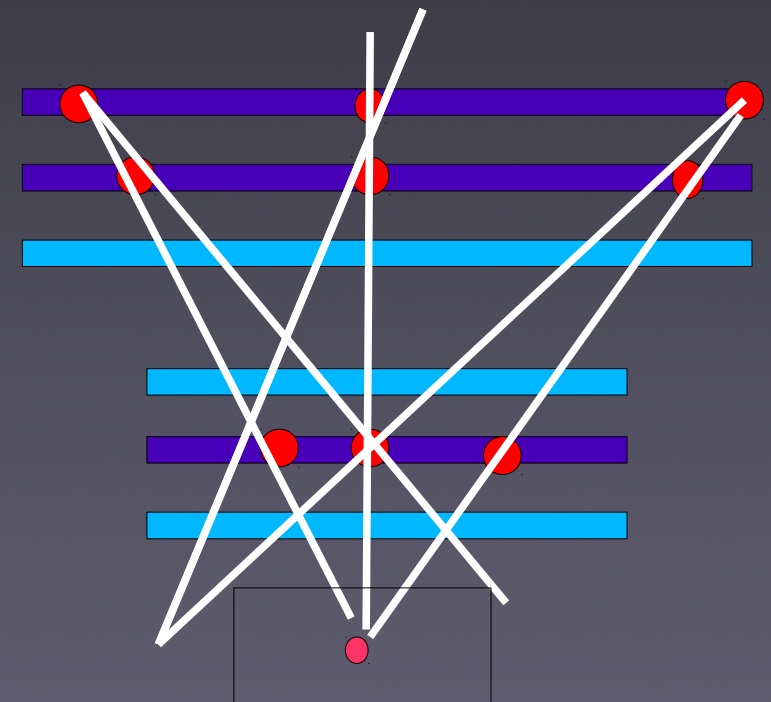
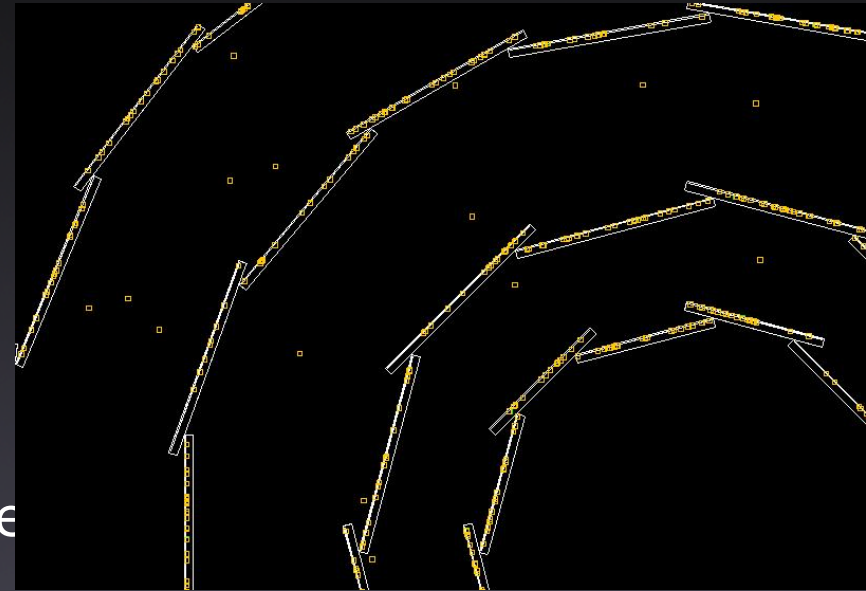


# Tracking Strategies

- A lot in tracking evolves around choosing the right “strategy”
- Outside-In
  - Occupancy is a lot small outside, track from the outside and pick up hits on the way
- Inside-Out
  - Higher granularity in the inner layers, so start from there
- Vertex-Standalone
  - Use only the highly granular vertex detector to find tracks
- Reality
  - All of the above to achieve an optimal tracking performance

# Seeding

- Need to start from somewhere
- Forming Seed tracks
  - Choose e.g. 3 layers
  - Form tracks from all hit triplets
  - Remove tracks that are not even close to the interaction region (z cut)
- These Seed tracks then form the input the next step
- Problem
  - Combinatorial issue, many seed tracks to evaluate
  - Choice of seed layers important



# Tracking & Fitting

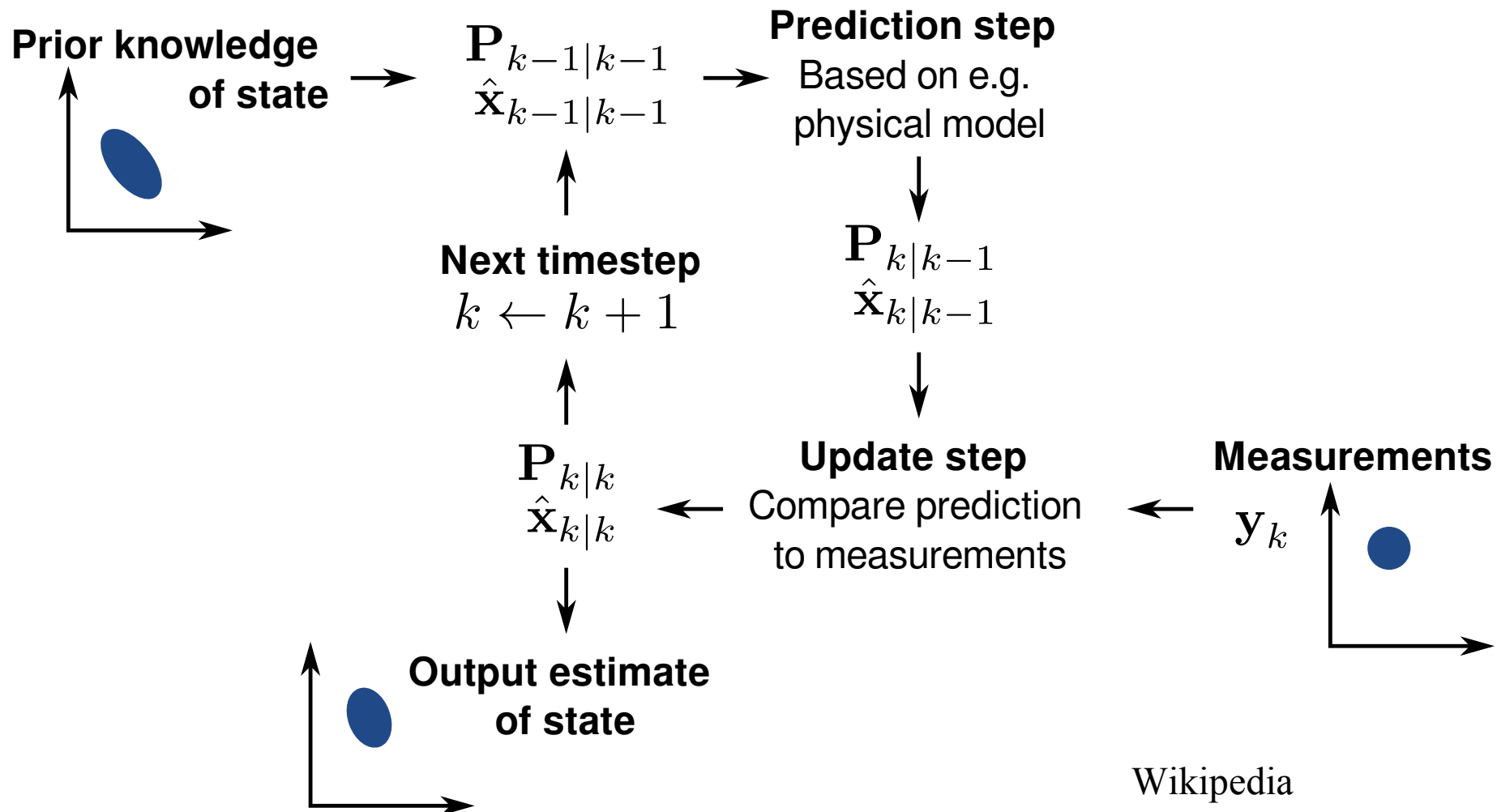
- Take all SeedTracks
- Pick up all hits along seed trajectory
  - Remove tracks with a below minimum number of hits
  - Make a Helix fit
  - Use goodness-of-fit to select good tracks
- Usually several steps
  - “Easy tracks” first
- Then
  - Loopers
  - low momentum tracks
  - tracks that have smaller number of hits
- Kalman Filter (see next slides)
  - Best tool for this, used by most experiments



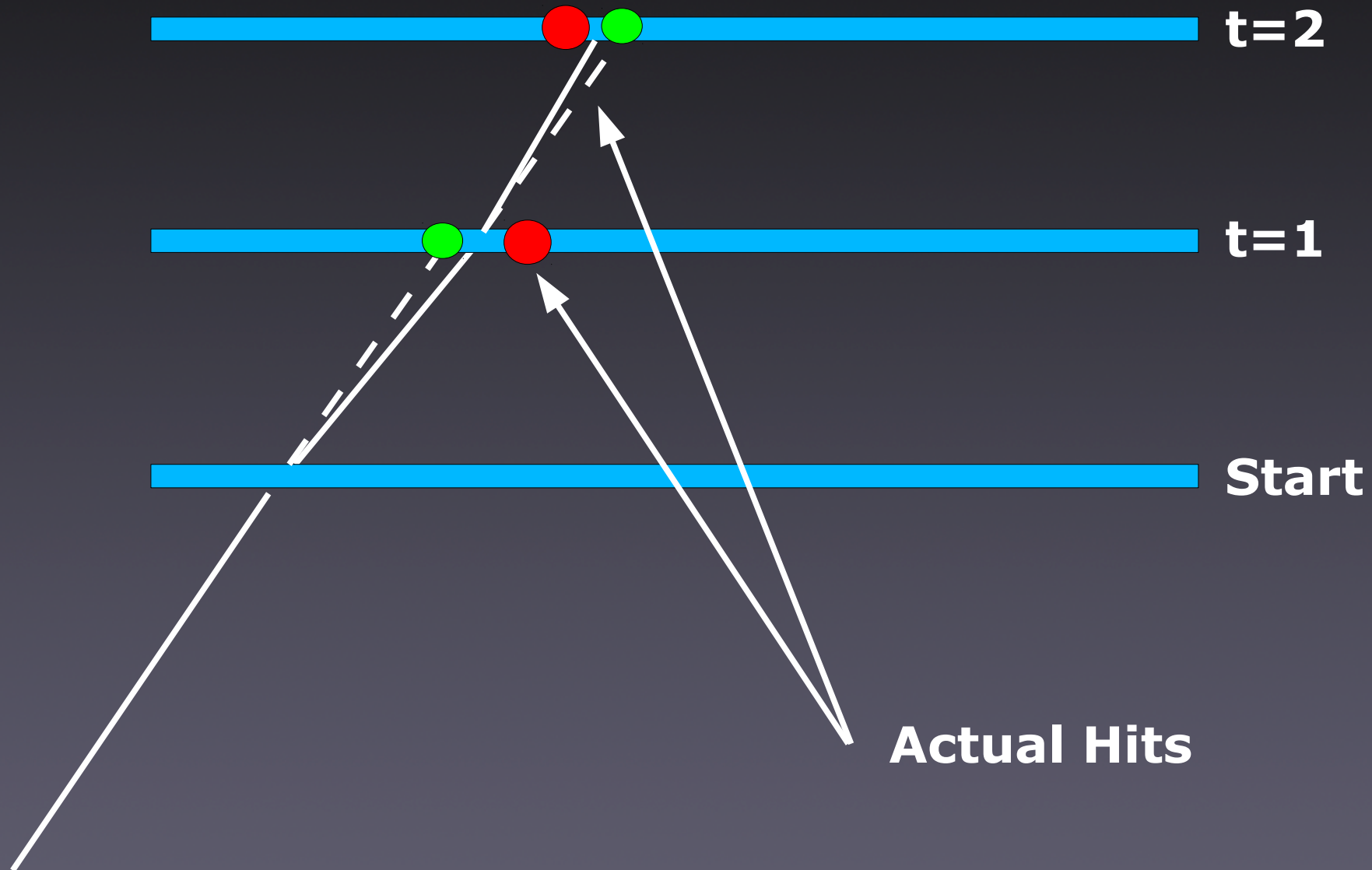
# Kalman Filter

- What is it ?
  - Recursive algorithm using “noisy” input data
  - Statistically optimal estimate of the underlying system state
  - Needs physical propagation model
- Kalman Filters are the tool of choice for tracking objects
  - Particles
  - Airplanes
  - Missiles

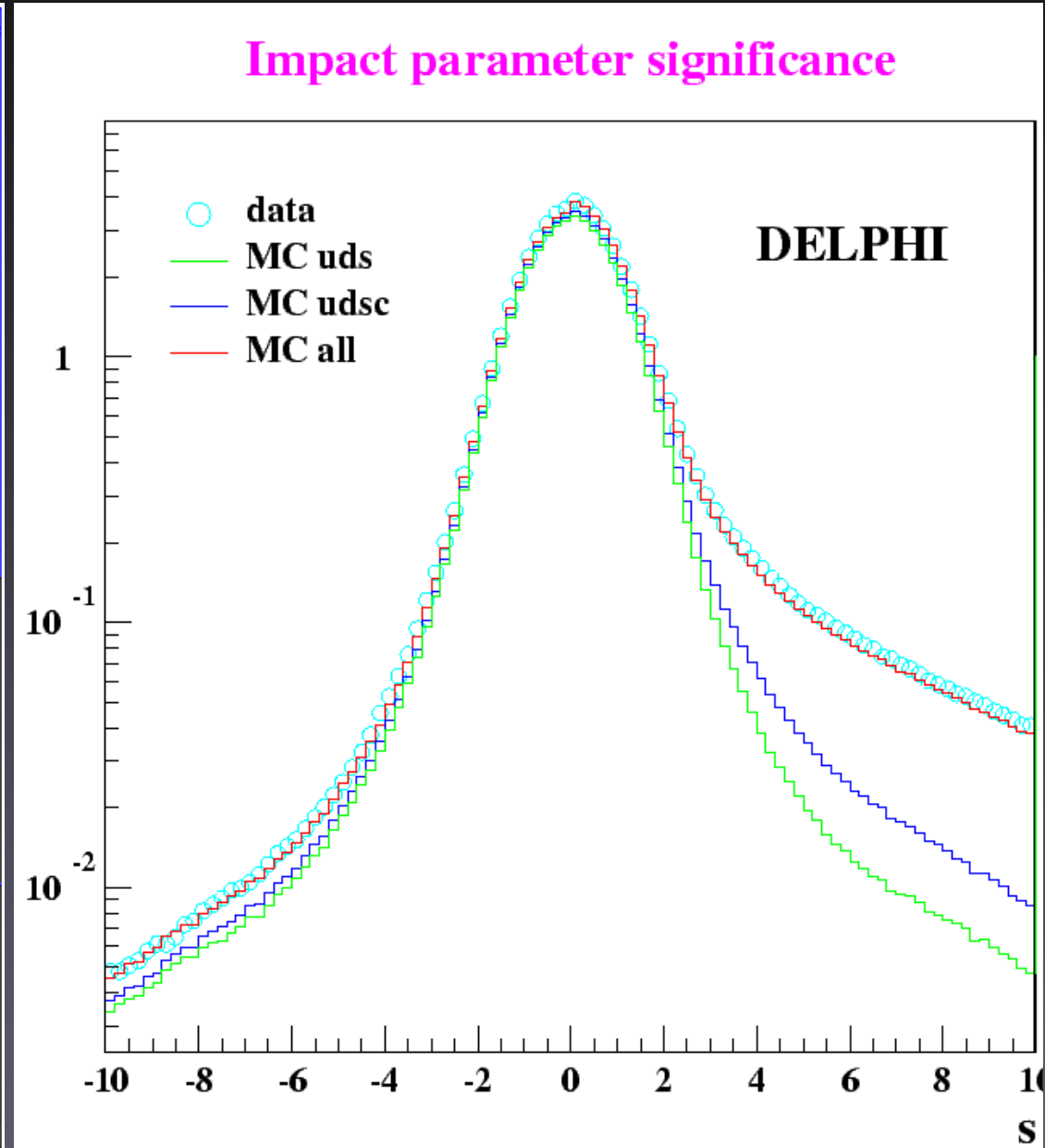
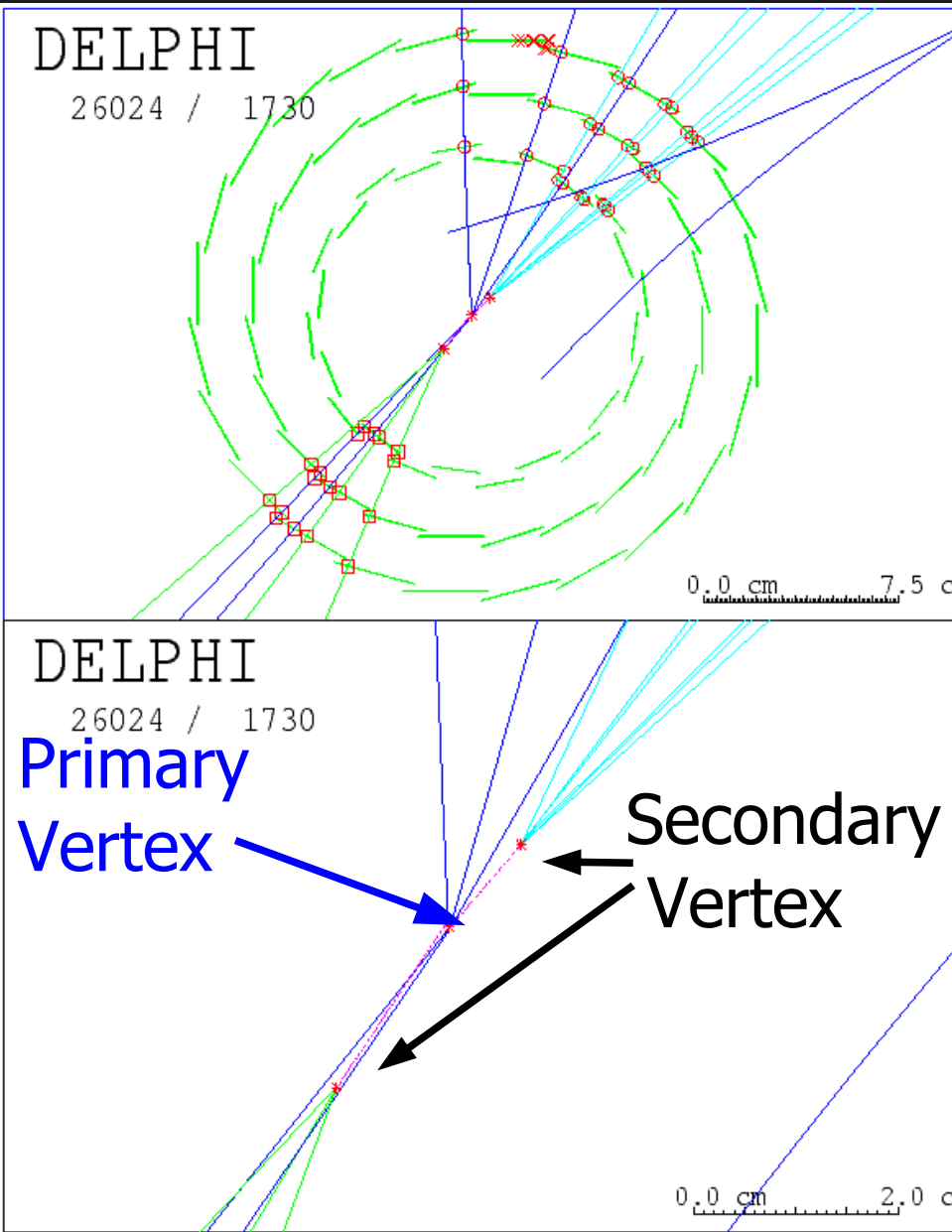
# Kalman filter Sketch



# Tracking Example



# Vertexing



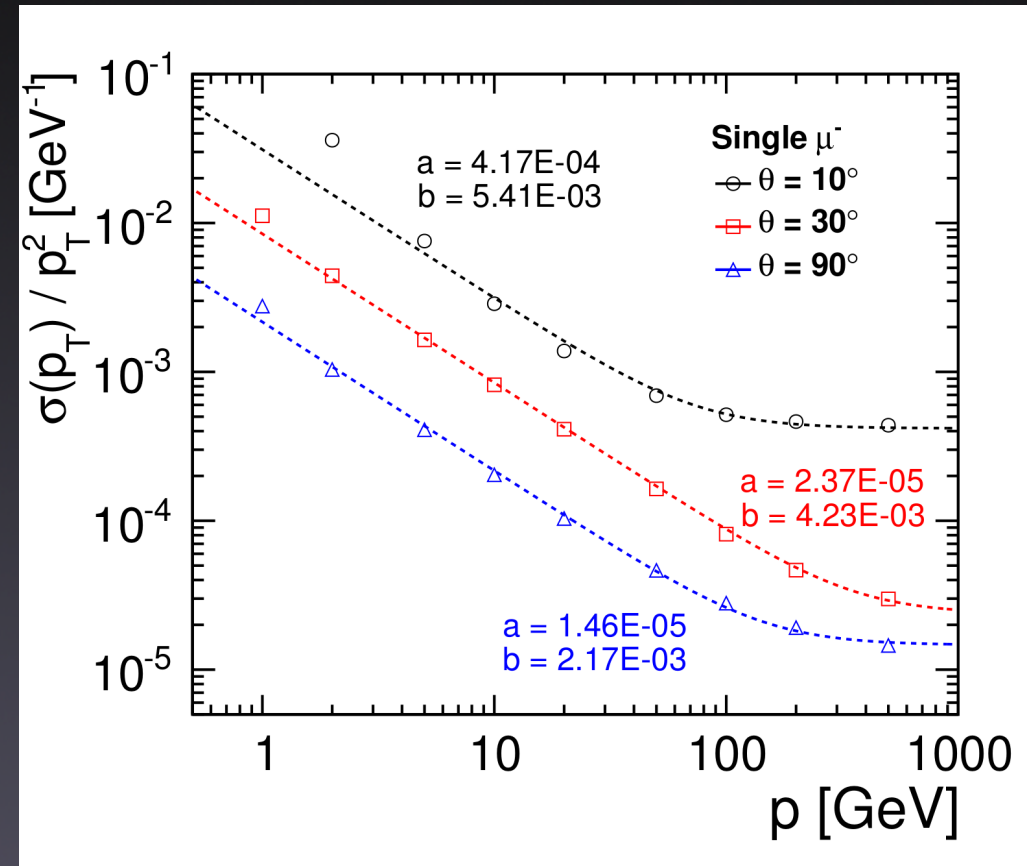


# Adding Information - Refitting

- In many cases, one has additional information about the track
- E.g. Track origin
  - If the Primary vertex is well know (as in a Linear collider)
  - Can Re-fit track using that information
- If track belongs to a secondary vertex
  - Use this constraint as well

# SiD Tracking Performance

- SiD tracking is integrated
  - Vertex and Tracker
  - 10 Hits/track coverage for almost entire polar angle
- Tracking system
  - Achieves desired  $\Delta p_T/p_T$  resolution of  $1.46 \cdot 10^{-5}$
  - >99 % efficiency over most of the phase space



$$\frac{\sigma(p_T)}{p_T^2} = a \oplus \frac{b}{p \sin \theta}$$

Pointing resolution  $\nearrow$   $a$

$\nwarrow$  Multiple scattering  $b$

# Things I've skipped

- A lot of details about silicon detectors and TPC's
- Calibration
- Interconnects
- Advanced Pixel detectors
- Alignment
  - Hardware-based
  - Software-based
- Fake tracks and Fake rate
- Advanced tracking tools

# Some Literature

- H. Spieler Semiconductor Detector Systems
- Horowitz & Hill: The Art of Electronics
- C. Grupen Particle Detectors



