

Higgs at ILC

Experiments

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Electroweak Symmetry Breaking

Mystery of something in the vacuum

- Success of the SM = success of gauge principle

W_T and Z_T = gauge fields of the EW gauge symmetry

- Gauge symmetry forbids explicit mass terms for W and Z

→ it must be broken by something condensed in the vacuum: $\langle 0 | I_3, Y | 0 \rangle \neq 0$ $\langle 0 | I_3 + Y | 0 \rangle = 0$

- This “something” supplies 3 longitudinal modes of W and Z:

$$W_L^+, W_L^-, Z_L \longleftarrow \chi^+, \chi^-, \chi_3 : \text{Goldstone modes}$$

- Left- (f_L) and right-handed (f_R) matter fermions carry different EW charges.

Their explicit mass terms also forbidden by the EW gauge symmetry

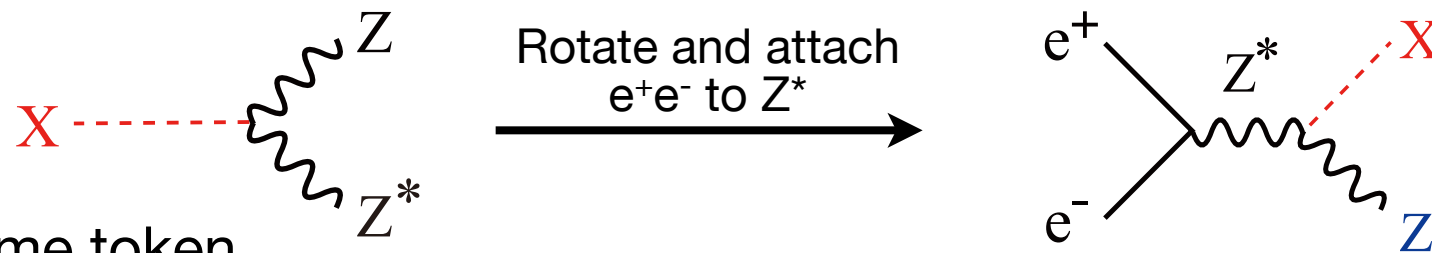
They must be generated through their Yukawa interactions with some weak-charged vacuum

- In the SM, the same “something” mixes f_L and f_R → generating masses and inducing flavor-mixings
- In order to form the Yukawa interaction terms, we need a complex doublet scalar field, which has four real components. The SM identifies three of them with the Goldstone modes.
- We need one more to form a complex doublet, which is the physical Higgs boson.
- This SM symmetry breaking sector is the simplest and the most economical, but there is no reason for it. The symmetry breaking sector might be more complex.
- We don’t know whether the “something” is elementary or composite.
- We knew it’s there in the vacuum with a vev of 246 GeV. But other than that we didn’t know almost anything about the “something” until July 4, 2012.

Since the July 4th, the world has changed!

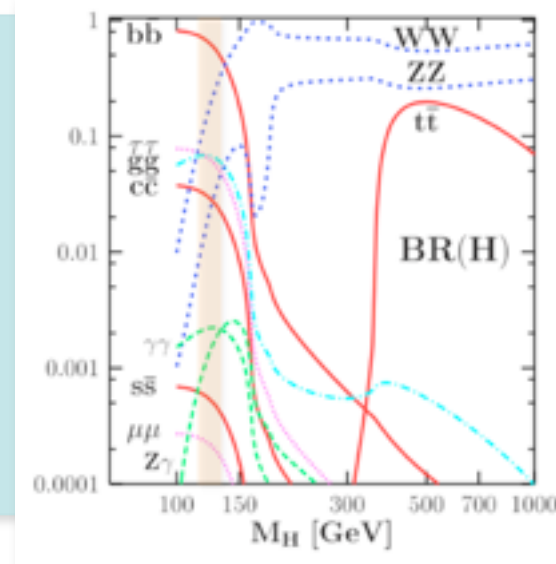
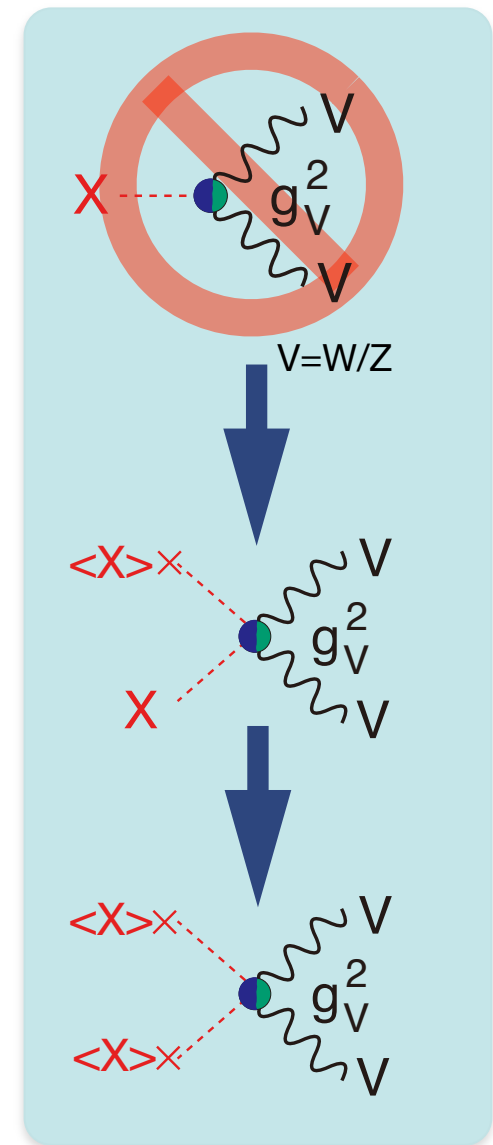
The discovery of the ~ 125 GeV boson at LHC could be called a quantum jump.

- $X(125) \rightarrow \gamma\gamma$ means X is a neutral boson and $J \neq 1$ (Landau-Yang theorem). Recent LHC results prefer $J^P=0^+$.
- $X(125) \rightarrow ZZ^*, WW^* \Rightarrow \exists XVV$ couplings: ($V=W/Z$: gauge bosons)
- There is no gauge coupling like XVV , only $XXVV$ or XXV
 $\Rightarrow XVV$ probably from $XXVV$ with one X replaced by $\langle X \rangle \neq 0$, namely $\langle X \rangle XVV$
 \Rightarrow There must be $\langle X \rangle \langle X \rangle VV$, a mass term for V .
 \Rightarrow **X is at least part of the origin of the masses of $V=W/Z$.**
 \Rightarrow This is a great step forward but we need to know whether $\langle X \rangle$ saturates the SM $v_{\text{ev}} = 246\text{GeV}$.
- $X \rightarrow ZZ^*$ means, X can be produced via $e^+e^- \rightarrow Z^* \rightarrow ZX$.



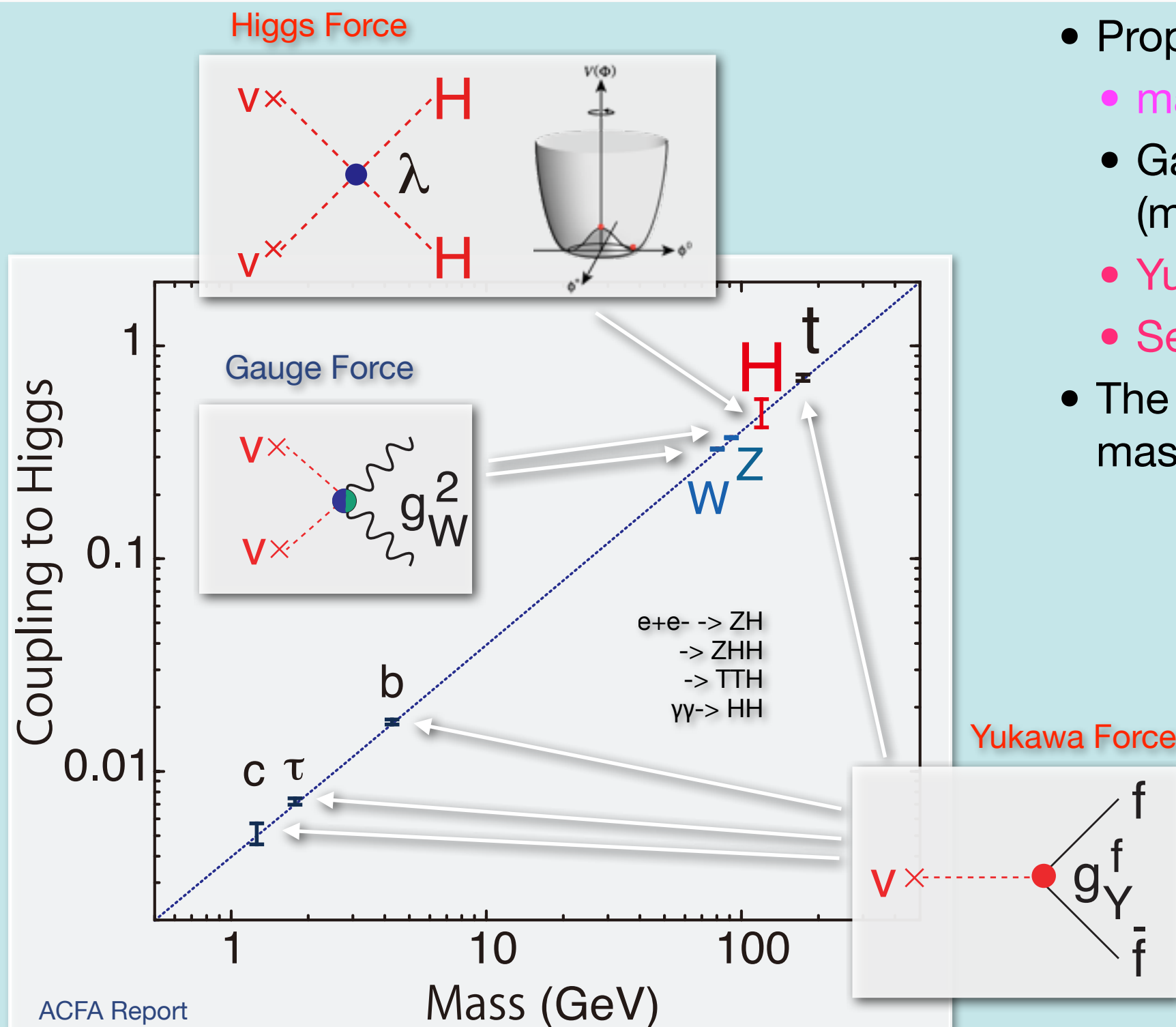
- By the same token,
 $X \rightarrow WW^*$ means, X can be produced via W fusion: $e^+e^- \rightarrow \nu\nu X$.

- So we now know that the major Higgs production mechanisms in e^+e^- collisions are indeed available at the ILC \Rightarrow No lose theorem for the ILC.
- $\sim 125\text{GeV}$ is the best place for the ILC, where variety of decay modes are accessible.
- We need to check this $\sim 125\text{GeV}$ boson in detail to see if it has indeed all the required properties of the something in the vacuum.



What Properties to Measure?

The Key is the Mass-Coupling Relation



- Properties to measure are
 - mass, width, J^{PC}
 - Gauge quantum numbers (multiplet structure)
 - Yukawa couplings
 - Self-coupling
- The key is to measure the mass-coupling relation

If the 125GeV boson is the one to give masses to all the SM particles, coupling should be proportional to mass.

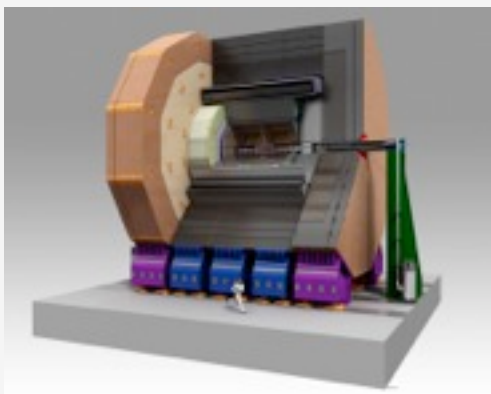
Any deviation from the straight line signals BSM!

The Higgs is a window to BSM physics!

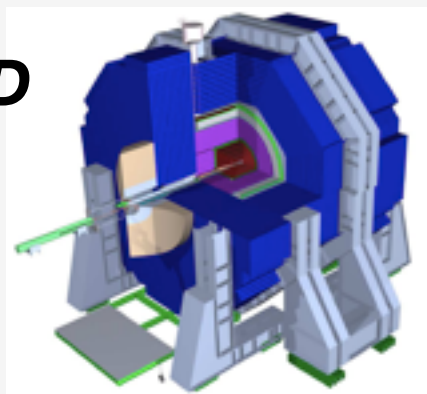
Our Mission = Bottom-up Model-Independent Reconstruction of the EWSB Sector through Precision Higgs Measurements

- **Multiplet structure :**
 - Additional singlet?
 - Additional doublet?
 - Additional triplet?
- **Underlying dynamics :**
 - Weakly interacting or strongly interacting?
= elementary or composite ?
- Relations to other questions of HEP :
 - DM
 - EW baryogenesis
 - neutrino mass
 - inflation?

ILD



SiD



There are many possibilities!

Different models predict different deviation patterns --> **Fingerprinting!**

Model	μ	τ	b	c	t	g_V
Singlet mixing	↓	↓	↓	↓	↓	↓
2HDM-I	↓	↓	↓	↓	↓	↓
2HDM-II (SUSY)	↑	↑	↑	↓	↓	↓
2HDM-X (Lepton-specific)	↑	↑	↓	↓	↓	↓
2HDM-Y (Flipped)	↓	↓	↑	↓	↓	↓

Mixing with singlet

$$\frac{g_{hVV}}{g_{h_{SM}VV}} = \frac{g_{hff}}{g_{h_{SM}ff}} = \cos \theta \simeq 1 - \frac{\delta^2}{2}$$

Composite Higgs

$$\frac{g_{hVV}}{g_{h_{SM}VV}} \simeq 1 - 3\%(1 \text{ TeV}/f)^2$$

$$\frac{g_{hff}}{g_{h_{SM}ff}} \simeq \begin{cases} 1 - 3\%(1 \text{ TeV}/f)^2 & (\text{MCHM4}) \\ 1 - 9\%(1 \text{ TeV}/f)^2 & (\text{MCHM5}) \end{cases}$$

SUSY

$$\frac{g_{hbb}}{g_{h_{SM}bb}} = \frac{g_{h\tau\tau}}{g_{h_{SM}\tau\tau}} \simeq 1 + 1.7\% \left(\frac{1 \text{ TeV}}{m_A} \right)^2$$

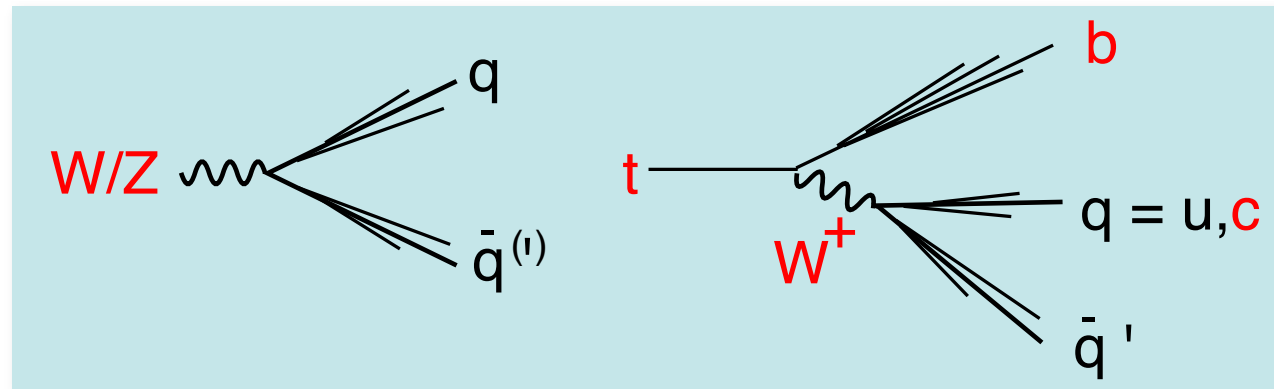
Expected deviations are small --> **Precision!**

**For the precision we need a 500GeV LC
and high precision detectors**

LC Experiments

View events as viewing Feynman diagrams

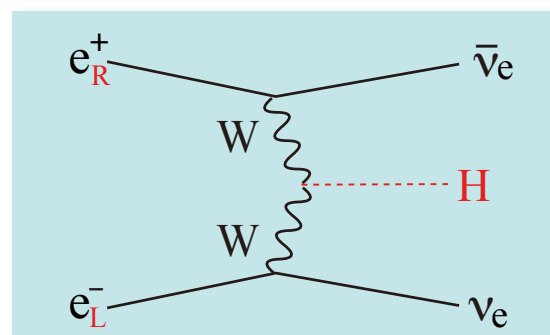
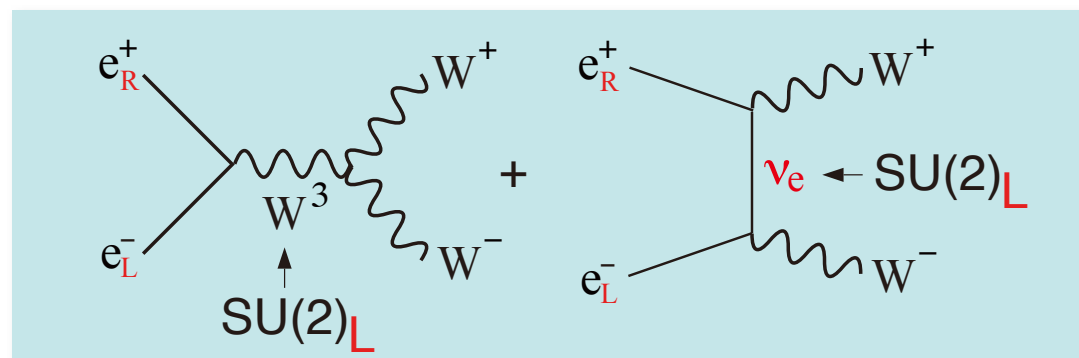
Reconstruct events in terms of (q, l, gb, hb)



Jet invariant mass \rightarrow W/Z/t/h ID \rightarrow p^μ
 \rightarrow angular analysis \rightarrow s^μ

Missing momentum \rightarrow neutrinos

Select Feynman diagrams with polarized beams



To these processes, only left-handed electrons and right-handed positrons contribute !
 If you have a wrong combination, cross section is zero.

Beam polarization plays an essential role !

	ILC	CLIC	TLEP
Pol (e^-)	-0.8	-0.8	0
Pol (e^+)	+0.3	0	0
$(\sigma/\sigma_0)_{\nu\nu H}$	$1.8 \times 1.3 = 2.34$	$1.8 \times 1.0 = 1.8$	1

Beam polarization acts as luminosity doubler !

Why 250-500 GeV?

Three well known thresholds

ZH @ 250 GeV ($\sim M_Z + M_H + 20 \text{ GeV}$) :

- Higgs mass, width, J^{PC}
- Gauge quantum numbers
- Absolute measurement of HZZ coupling (recoil mass) \rightarrow couplings to H (other than top)
- $\text{BR}(h \rightarrow VV, qq, ll, \text{invisible})$: $V = W/Z$ (direct), g, γ (loop)

ttbar @ 340-350 GeV ($\sim 2m_t$) : ZH meas. Is also possible

- Threshold scan \rightarrow **theoretically clean m_t measurement**: $\Delta m_t(\overline{MS}) \simeq 100 \text{ MeV}$
 \rightarrow test stability of the SM vacuum
 \rightarrow **indirect meas. of top Yukawa coupling**
 - A_{FB} , Top momentum measurements
 - Form factor measurements
- $\gamma\gamma \rightarrow HH$ @ 350 GeV possibility

vvH @ 350 - 500 GeV :

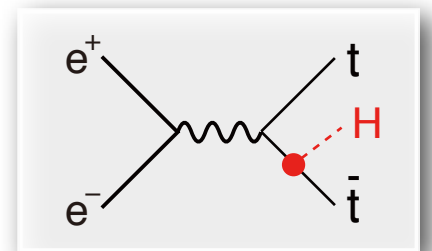
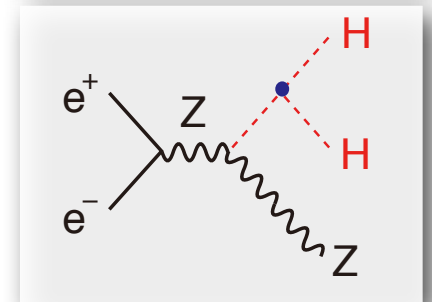
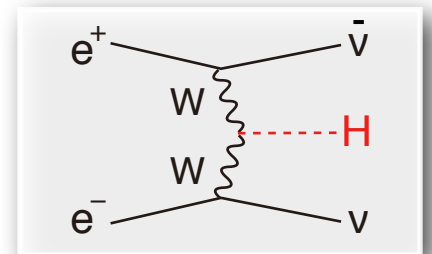
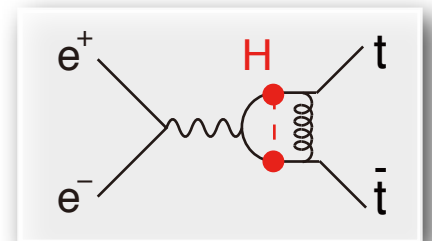
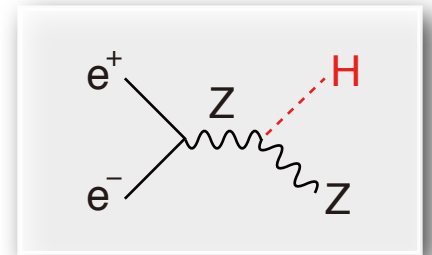
- HWW coupling \rightarrow **total width** \rightarrow absolute normalization of Higgs couplings

ZHH @ 500 GeV ($\sim M_Z + 2M_H + 170 \text{ GeV}$) :

- Prod. cross section attains its maximum at around 500 GeV \rightarrow **Higgs self-coupling**

ttbarH @ 500 GeV ($\sim 2m_t + M_H + 30 \text{ GeV}$) :

- Prod. cross section becomes maximum at around 800 GeV.
- QCD threshold correction enhances the cross section \rightarrow **top Yukawa** measurable at 500 GeV concurrently with the self-coupling

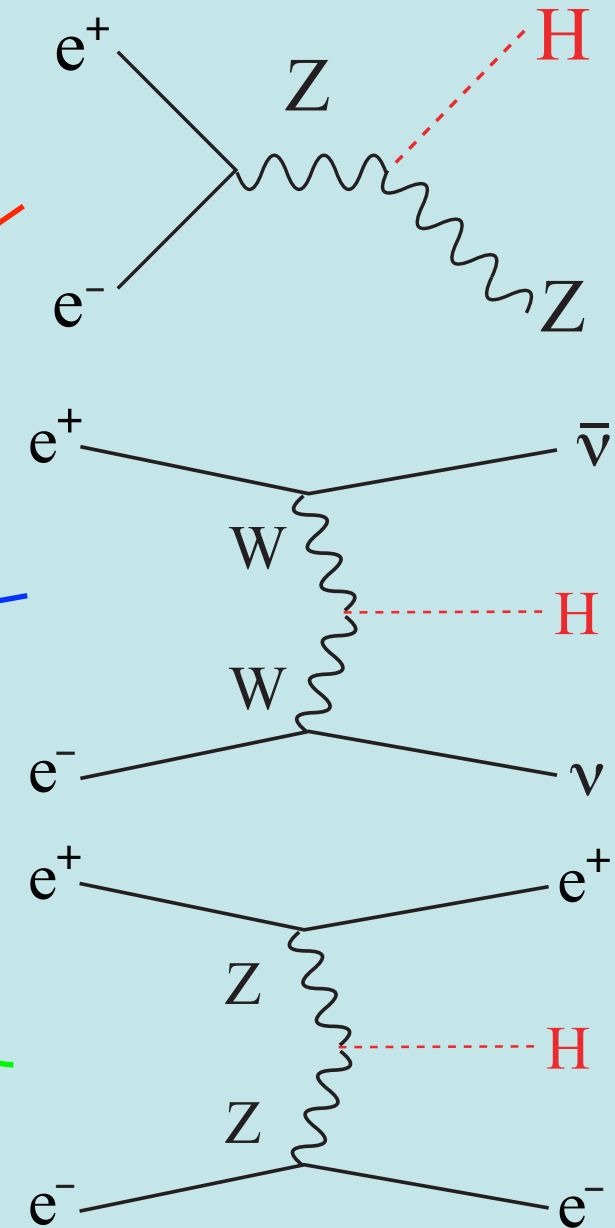
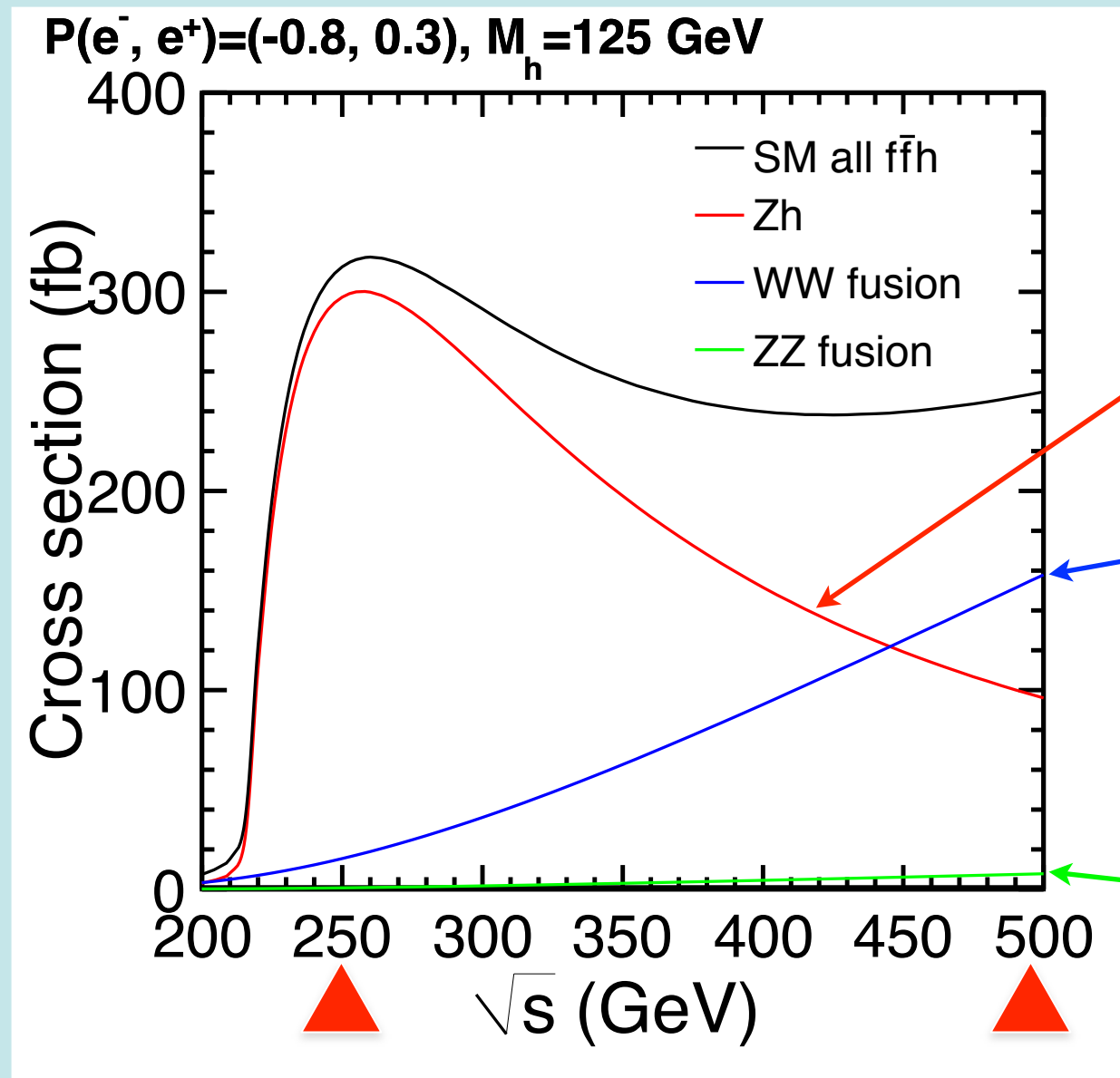


We can complete the mass-coupling plot at ~500 GeV!

Main Production Processes

Single Higgs Production

Production cross section



ZH dominates at 250 GeV
(~80k ev: 250 fb⁻¹)

vvH takes over at 500 GeV
(~125k ev: 500 fb⁻¹)

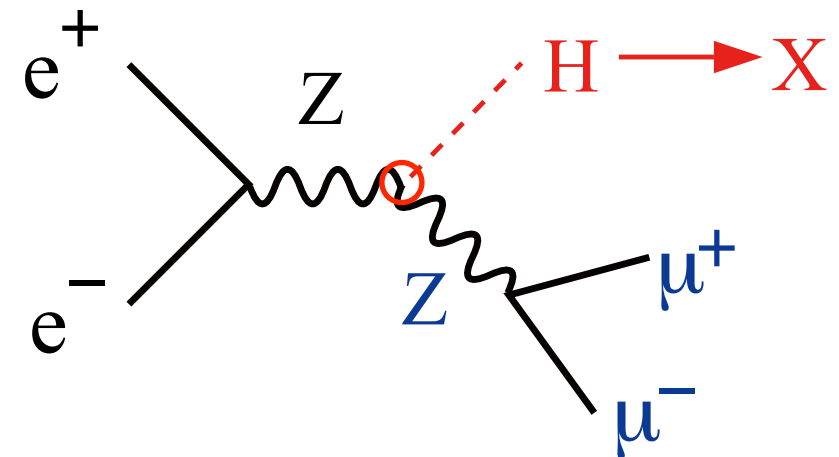
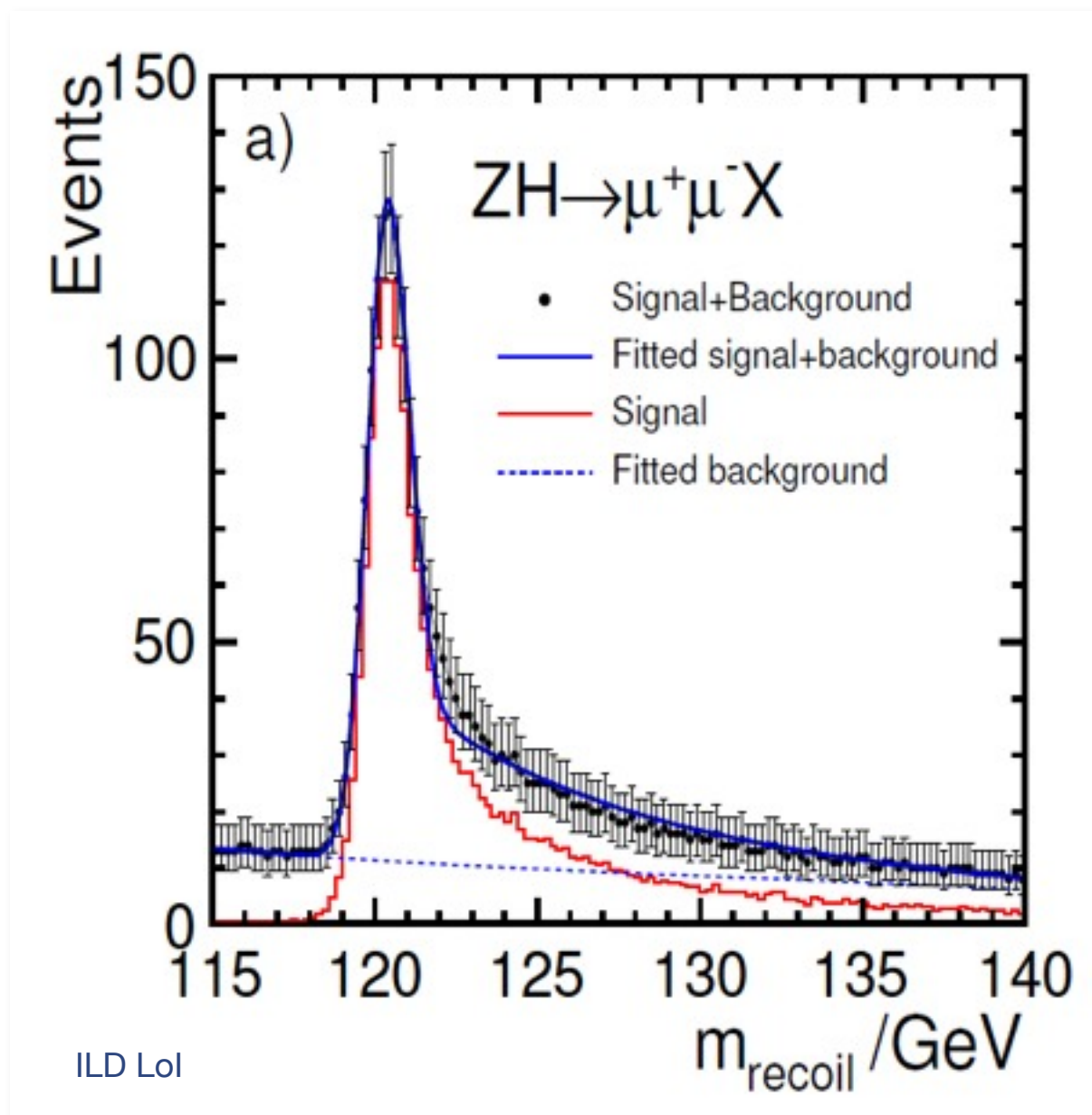
Possible to rediscover the Higgs in one day!

ILC 250

Recoil Mass Measurement

The flagship measurement of ILC 250

Recoil Mass



$$M_X^2 = (p_{CM} - (p_{\mu^+} + p_{\mu^-}))^2$$

Invisible decay detectable!

$$250 \text{ fb}^{-1} @ 250 \text{ GeV} \quad m_H = 125 \text{ GeV}$$

$$\Delta\sigma_H / \sigma_H = 2.6\%$$

$$\Delta m_H = 30 \text{ MeV}$$

$$BR(\text{invisible}) < 1\% @ 95\% \text{ C.L.}$$

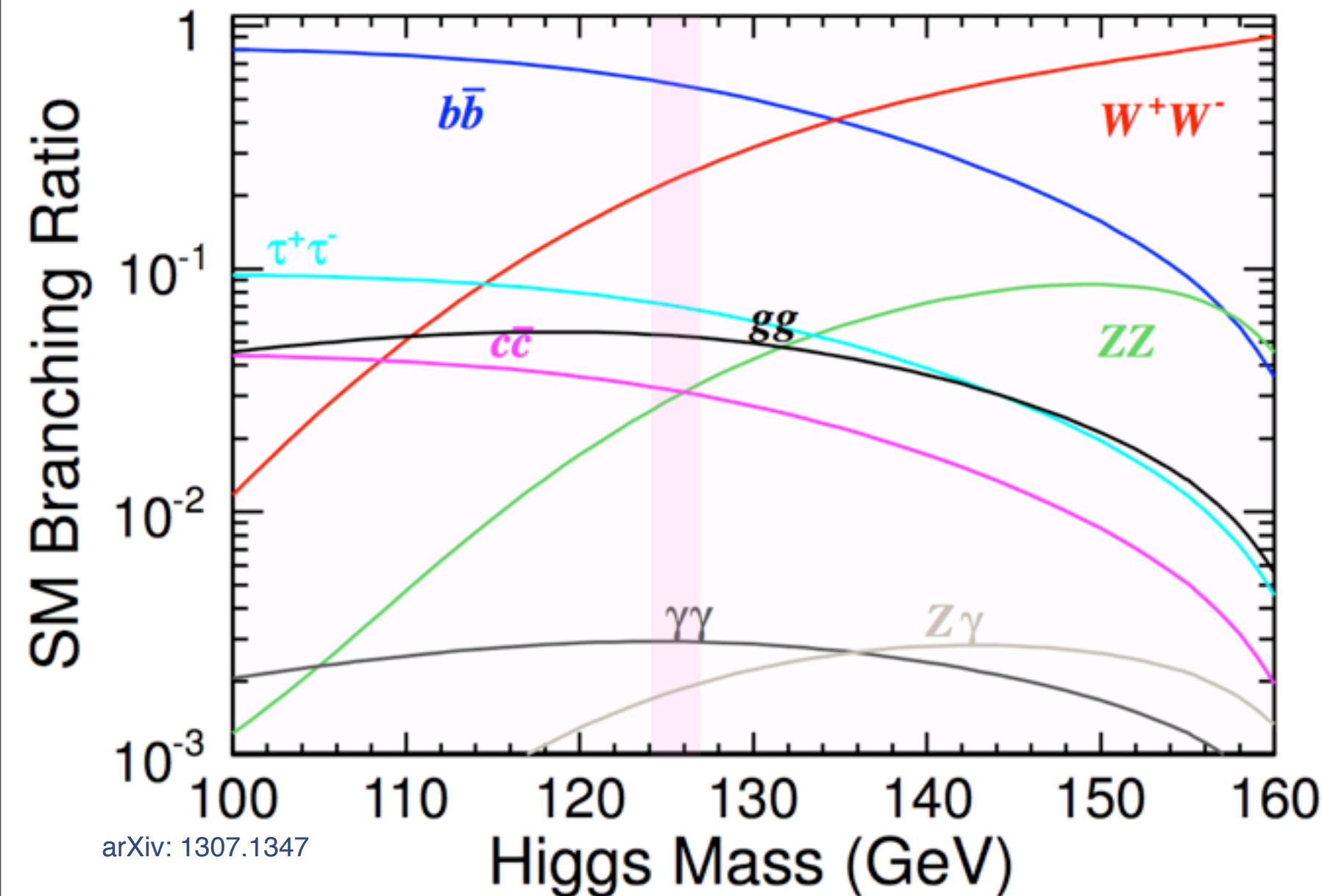
scaled from $m_H = 120 \text{ GeV}$

Model-independent absolute measurement of σ_{ZH} (the HZZ coupling)

$\sigma \times \text{BR}$ Measurements

for $b, c, g, \text{tau}, WW^*, \dots$

DBD Physics Chap.



$250 \text{ fb}^{-1} @ 250 \text{ GeV}$
 $m_H = 125 \text{ GeV}$
 scaled from $m_H = 120 \text{ GeV}$

	@250GeV
process	ZH
Int. Lumi. [fb^{-1}]	250
$\Delta\sigma/\sigma$	2.6%
decay mode	$\Delta\sigma\text{Br}/\sigma\text{Br}$
$H \rightarrow b\bar{b}$	1.2%
$H \rightarrow c\bar{c}$	8.3%
$H \rightarrow g\bar{g}$	7.0%
$H \rightarrow W^+W^-$	6.4%
$H \rightarrow \tau^+\tau^-$	4.2%
$H \rightarrow ZZ^*$	18%
$H \rightarrow \gamma\gamma$	34%

preliminarily

What we measure is not BR itself but $\sigma \times \text{BR}$.

To extract BR from $\sigma \times \text{BR}$, we need σ from the recoil mass measurement.

--> $\Delta\sigma/\sigma = 2.6\%$ eventually limits the BR measurements.

--> If we want to improve this situation, we need more data at 250GeV.

We need to seriously think about luminosity upgrade scenario.

Total Width and Coupling Extraction

One of the major advantages of the LC

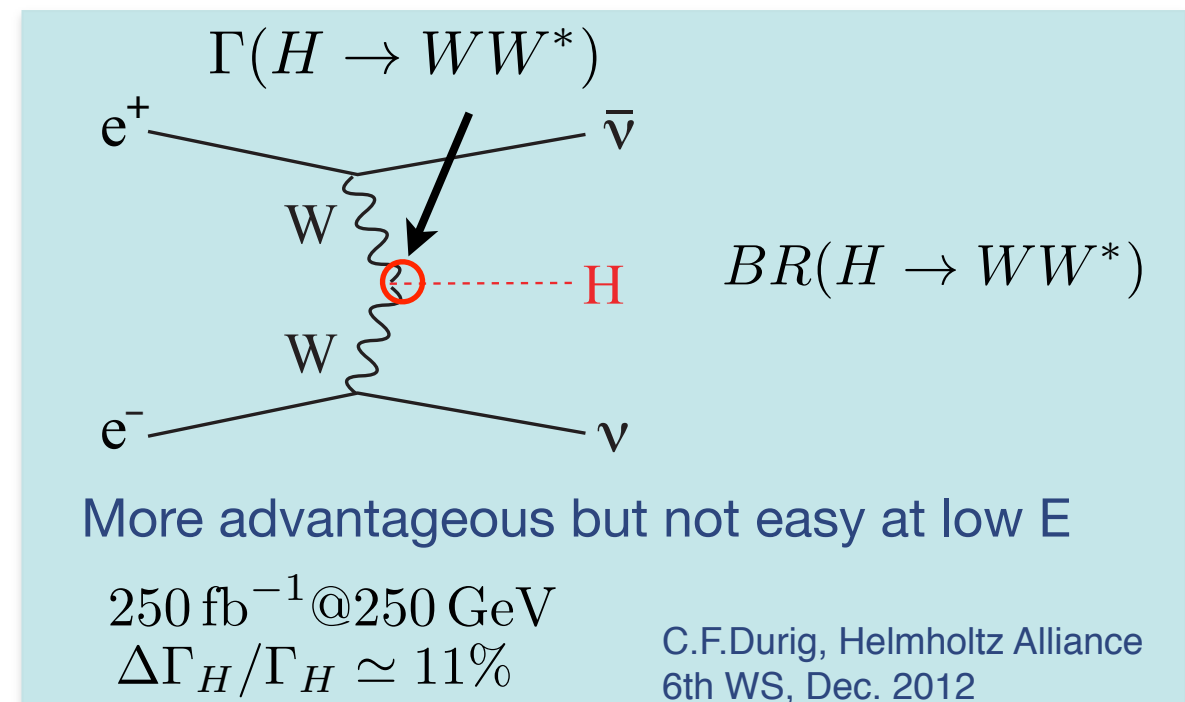
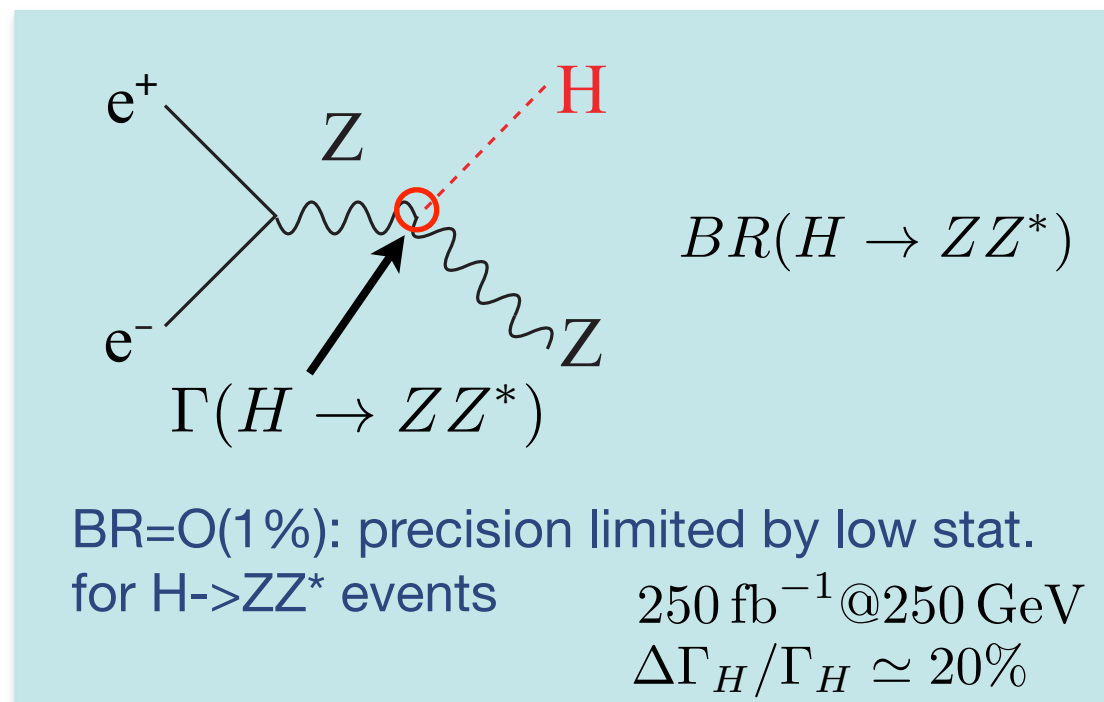
To extract couplings from BRs, we need the total width:

$$g_{HAA}^2 \propto \Gamma(H \rightarrow AA) = \Gamma_H \cdot BR(H \rightarrow AA)$$

To determine the total width, we need at least one partial width and corresponding BR:

$$\Gamma_H = \Gamma(H \rightarrow AA) / BR(H \rightarrow AA)$$

In principle, we can use $A=Z$, or W for which we can measure both the BRs and the couplings:



ILC 500

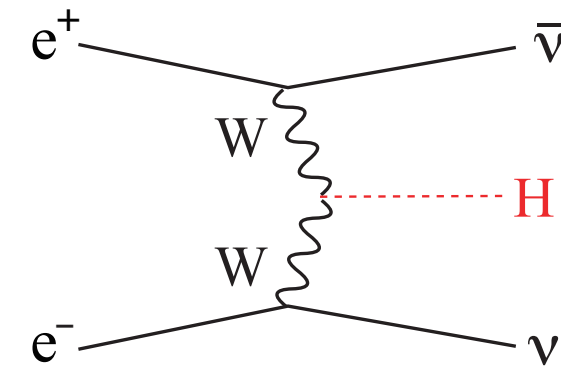
Width and BR Measurements at 500 GeV

Addition of 500GeV data to 250GeV data

E_{cm} [GeV]	independent measurements	relative error
250	σ_{ZH}	2.6%
	$\sigma_{ZH} \cdot Br(H \rightarrow b\bar{b})$	1.2%
	$\sigma_{ZH} \cdot Br(H \rightarrow c\bar{c})$	8.3%
	$\sigma_{ZH} \cdot Br(H \rightarrow gg)$	7.0%
	$\sigma_{ZH} \cdot Br(H \rightarrow WW^*)$	6.4%
	$\sigma_{ZH} \cdot Br(H \rightarrow \tau^+\tau^-)$	4.2%
	$\sigma_{\nu\bar{\nu}H} \cdot Br(H \rightarrow b\bar{b})$	10.5%
500	σ_{ZH}	3.0%
	$\sigma_{ZH} \cdot Br(H \rightarrow b\bar{b})$	1.8%
	$\sigma_{ZH} \cdot Br(H \rightarrow c\bar{c})$	13%
	$\sigma_{ZH} \cdot Br(H \rightarrow gg)$	11%
	$\sigma_{ZH} \cdot Br(H \rightarrow WW^*)$	9.2%
	$\sigma_{ZH} \cdot Br(H \rightarrow \tau^+\tau^-)$	5.4%
	$\sigma_{\nu\bar{\nu}H} \cdot Br(H \rightarrow b\bar{b})$	0.66%
	$\sigma_{\nu\bar{\nu}H} \cdot Br(H \rightarrow c\bar{c})$	6.2%
	$\sigma_{\nu\bar{\nu}H} \cdot Br(H \rightarrow gg)$	4.1%
	$\sigma_{\nu\bar{\nu}H} \cdot Br(H \rightarrow WW^*)$	2.4%

250 fb⁻¹@250 GeV
+500 fb⁻¹@500 GeV
 $m_H = 125$ GeV

ILD DBD Full Simulation Study



comes in as a powerful tool!

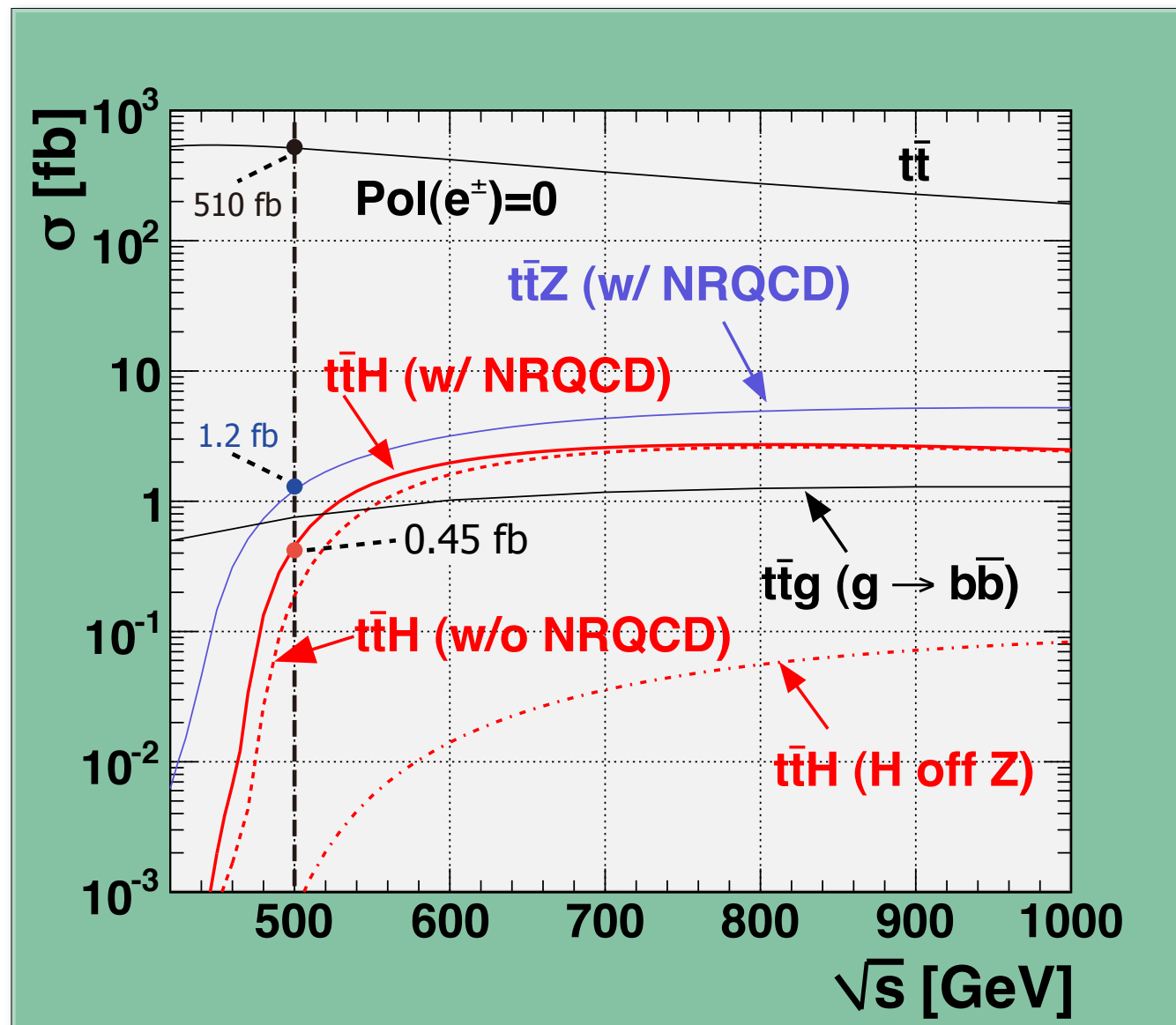
$$\Delta\Gamma_H/\Gamma_H \simeq 5\%$$

Mode	$\Delta\text{BR}/\text{BR}$
bb	2.2 (2.9)%
cc	5.1 (8.7)%
gg	4.0 (7.5)%
WW*	3.1 (6.9)%
$\tau\tau$	3.7 (4.9)%

The numbers in the parentheses are as of 250 fb⁻¹@250 GeV

Top Yukawa Coupling

The largest among matter fermions, but not yet directly observed

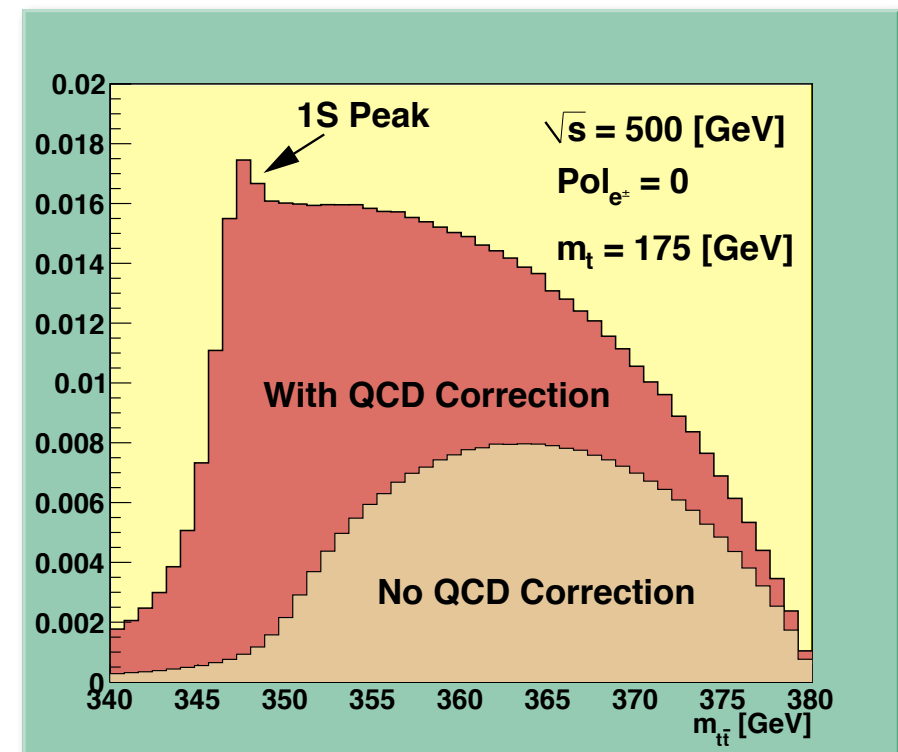
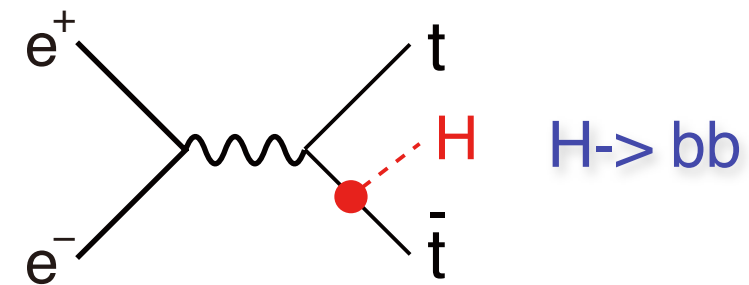


Cross section maximum at around
 $E_{cm} = 800 \text{ GeV}$

Philipp Roloff, LCWS12

Tony Price, LCWS12

DBD Full Simulation



A factor of 2 enhancement from
QCD bound-state effects

$$1 \text{ ab}^{-1} @ 500 \text{ GeV} \quad m_H = 125 \text{ GeV}$$

$$\Delta g_Y(t)/g_Y(t) = 9.9\%$$

Tony Price, LCWS12

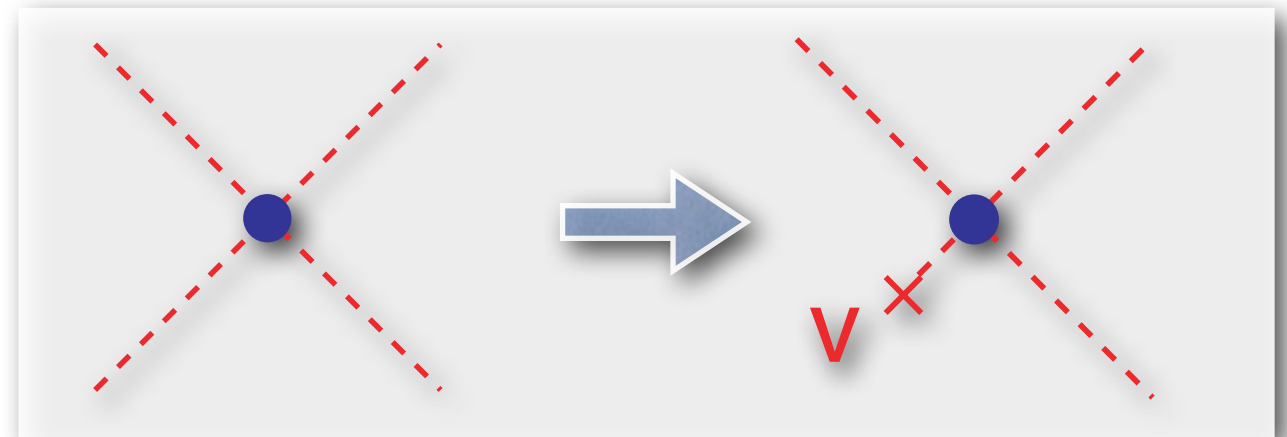
scaled from $m_H = 120 \text{ GeV}$

Notice $\sigma(500+20 \text{ GeV})/\sigma(500 \text{ GeV}) \sim 2$
Moving up a little bit helps significantly!

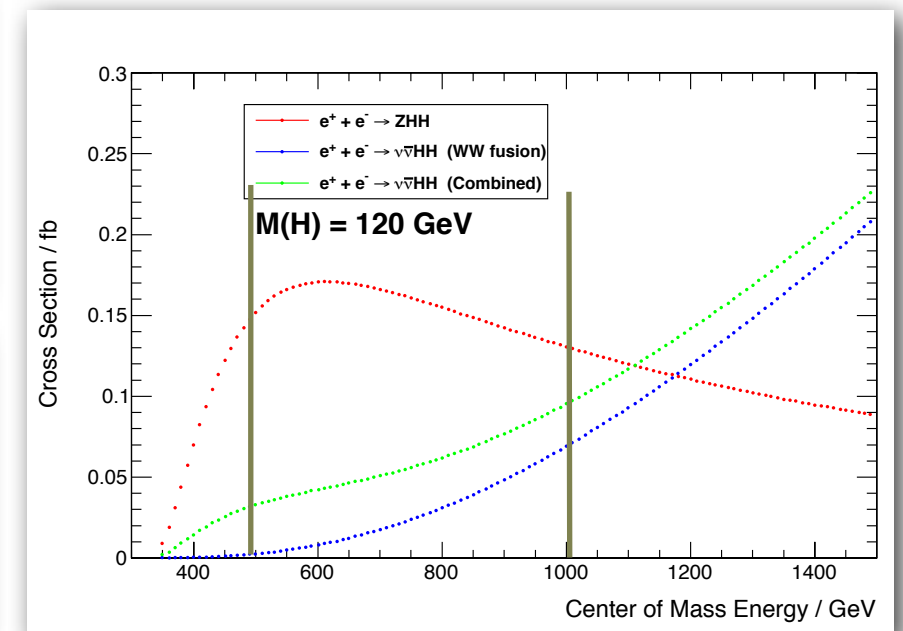
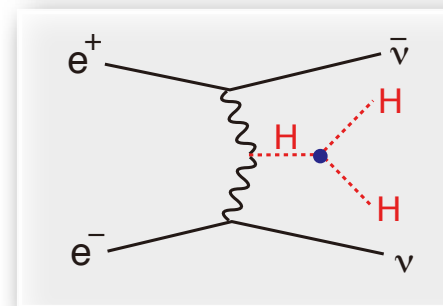
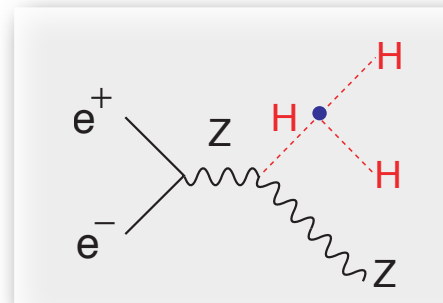
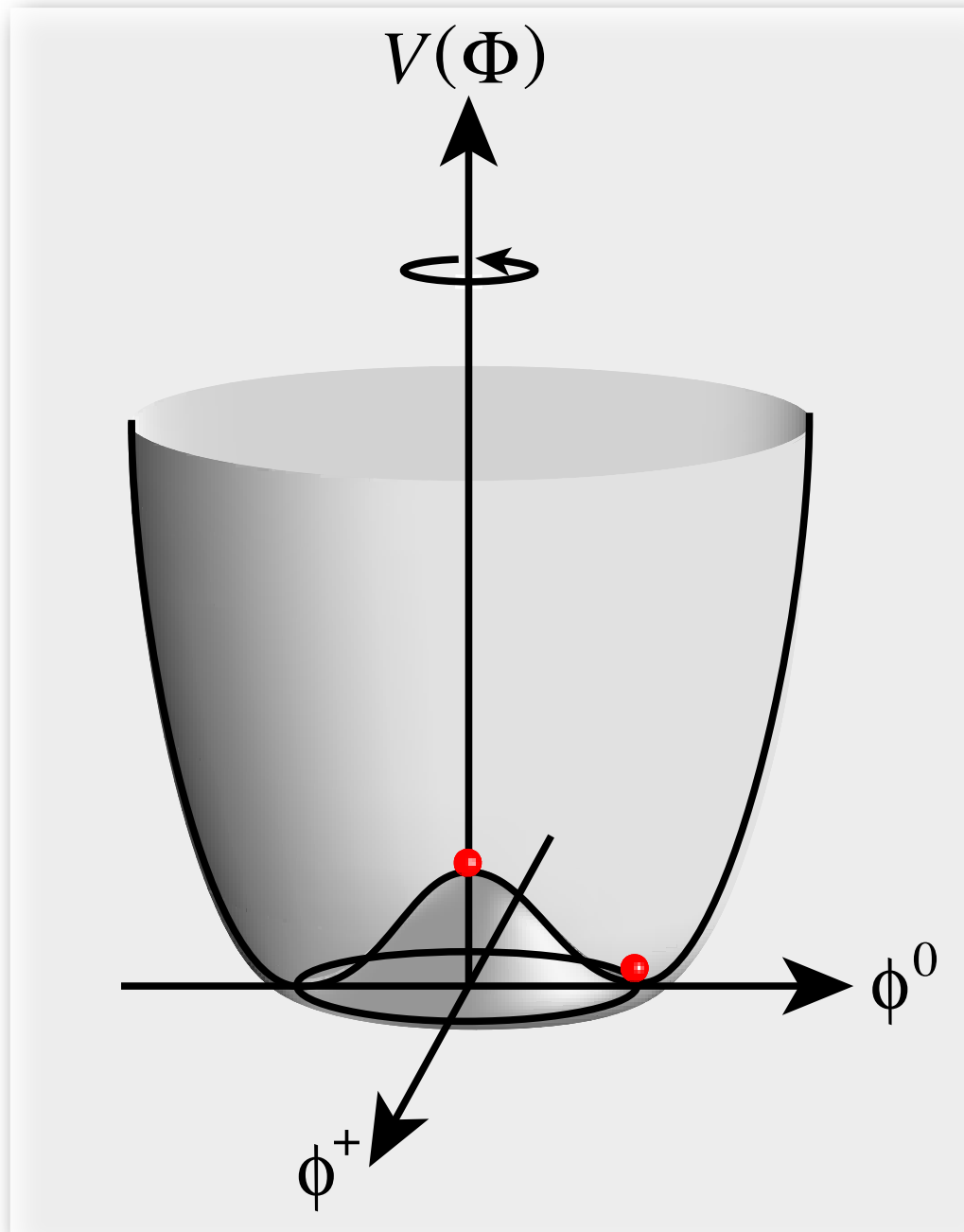
Higgs Self-coupling

What force makes the Higgs condense in the vacuum?

We need to **measure the Higgs self-coupling**



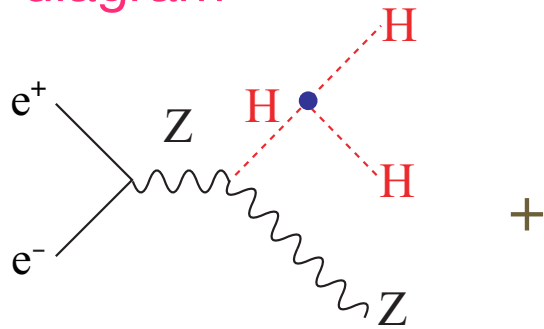
= We need to **measure the shape of the Higgs potential**



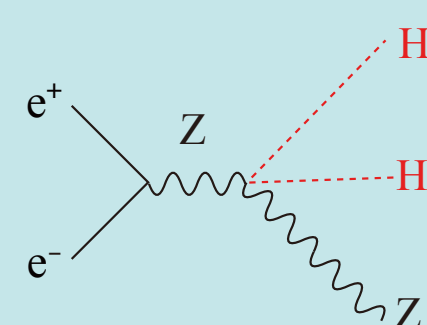
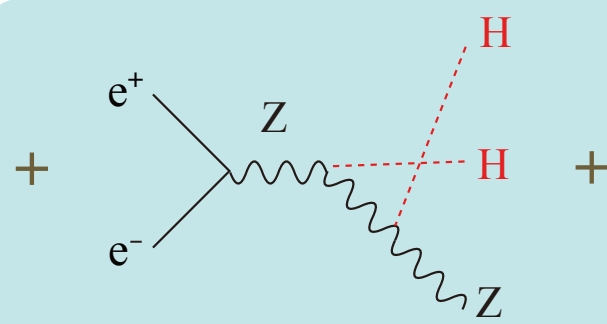
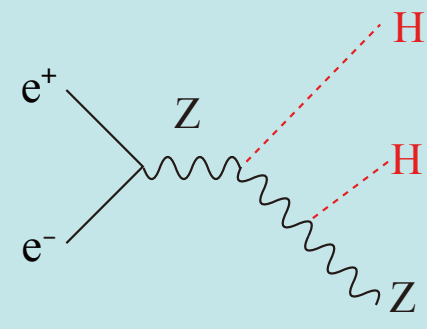
The measurement is very difficult even at ILC.

The Problem : BG diagrams dilute self-coupling contribution

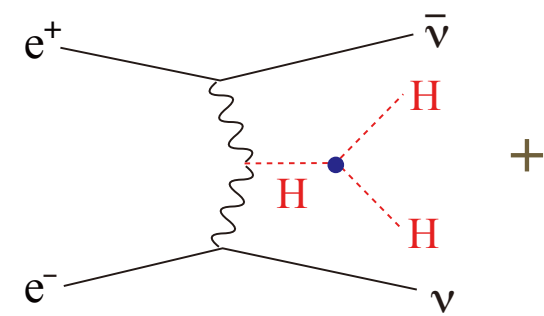
Signal diagram



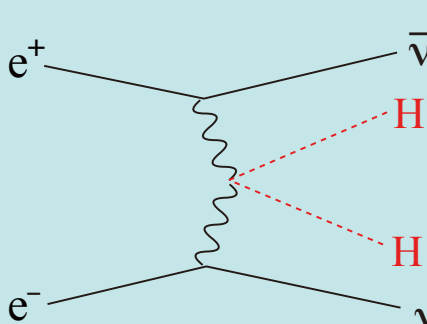
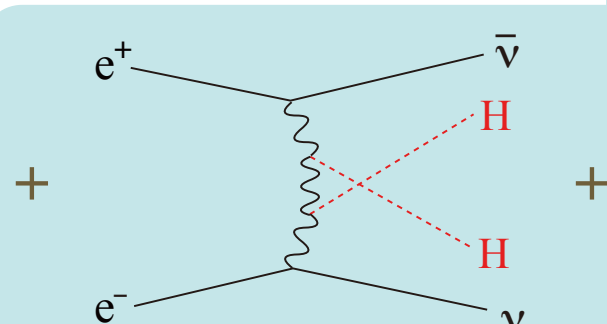
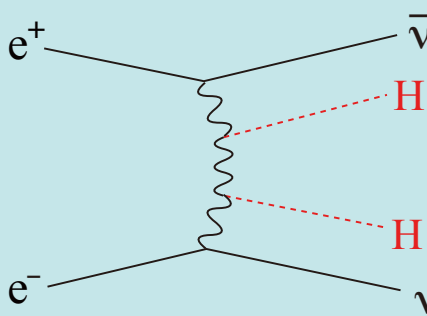
Irreducible BG diagrams



Signal diagram



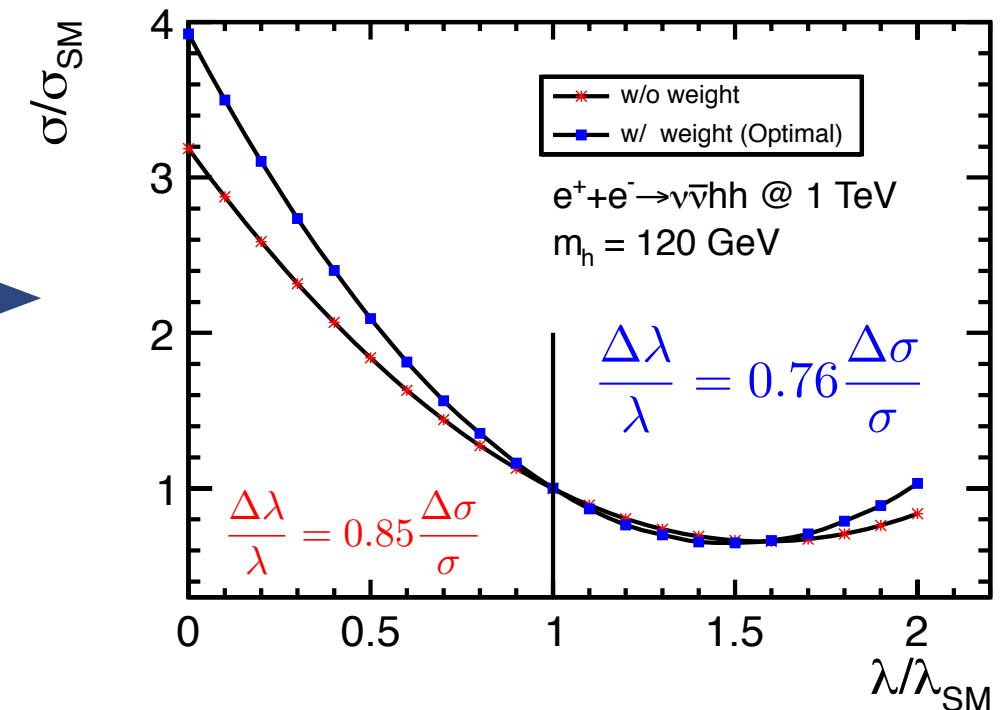
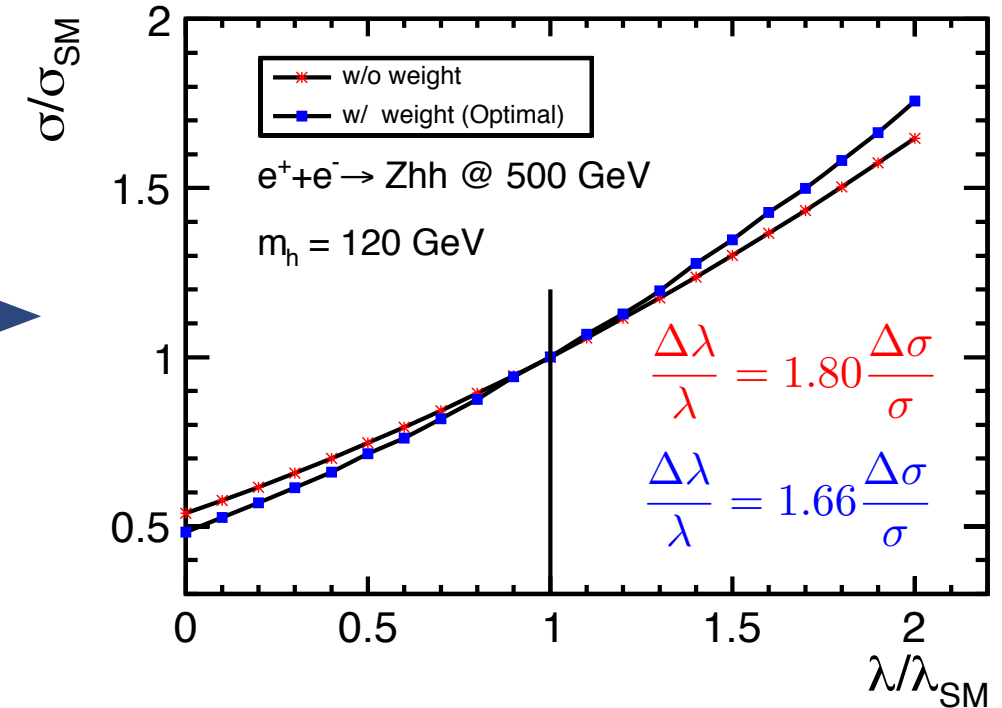
Irreducible BG diagrams



$$\sigma = \lambda^2 S + \lambda I + B$$

$$\frac{\Delta\lambda}{\lambda} = F \cdot \frac{\Delta\sigma}{\sigma}$$

F=0.5 if no BG diagrams

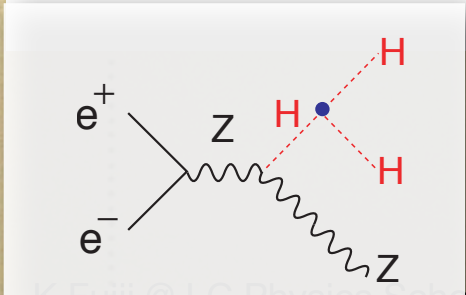
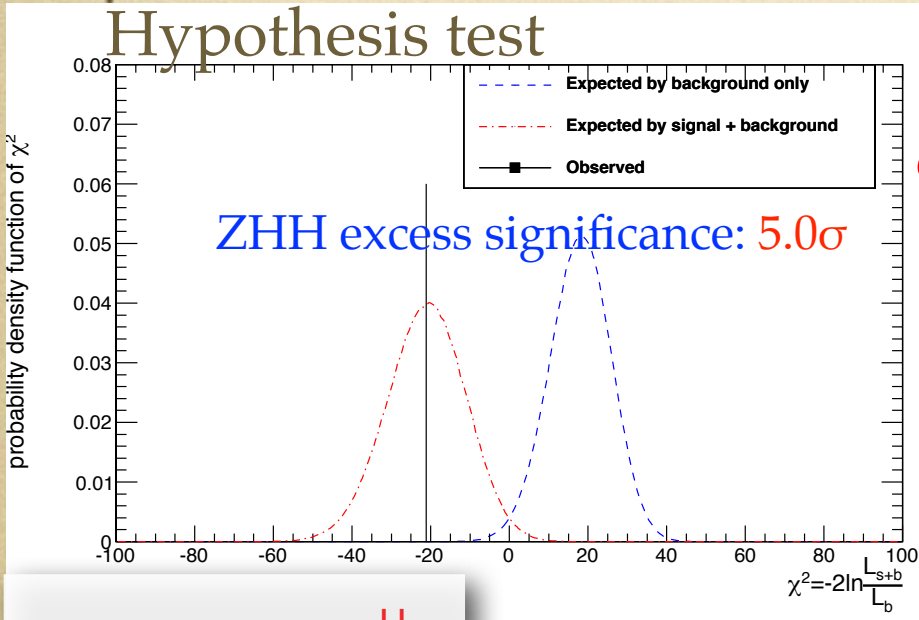


Junping Tian LC-REP-2013-003

Higgs self-coupling @ 500 GeV (combined)

$P(e^-,e^+) = (-0.8, +0.3)$ $e^+ + e^- \rightarrow ZHH$ $M(H) = 120\text{GeV}$ $\int Ldt = 2\text{ab}^{-1}$

Energy (GeV)	Modes	signal	background (tt, ZZ, ZZH/ ZZZ)	significance	
				excess (I)	measurement (II)
500	$ZHH \rightarrow (l\bar{l})(b\bar{b})(b\bar{b})$	3.7	4.3	1.5 σ	1.1 σ
		4.5	6.0	1.5 σ	1.2 σ
500	$ZHH \rightarrow (\nu\bar{\nu})(b\bar{b})(b\bar{b})$	8.5	7.9	2.5 σ	2.1 σ
500	$ZHH \rightarrow (q\bar{q})(b\bar{b})(b\bar{b})$	13.6	30.7	2.2 σ	2.0 σ
		18.8	90.6	1.9 σ	1.8 σ

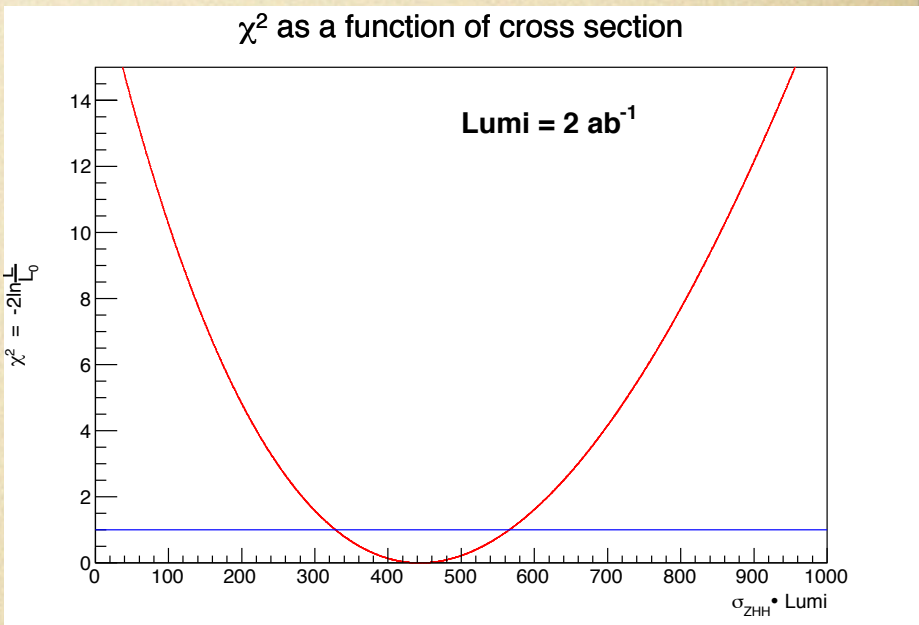


$\sigma_{ZHH} = 0.22 \pm 0.06 \text{ fb}$

$\frac{\delta\sigma}{\sigma} = 27\%$

$\frac{\delta\lambda}{\lambda} = 44\%$

(cf. 80% for qqbbbb at the LoI time)



ILC 1000

Higgs Physics at Higher Energy

Self-coupling with WBF, top Yukawa at xsection max., other higgses, ...

vvH @ at >1TeV : $> 1 \text{ ab}^{-1}$ (pol e^+, e^-)=(+0.2,-0.8)

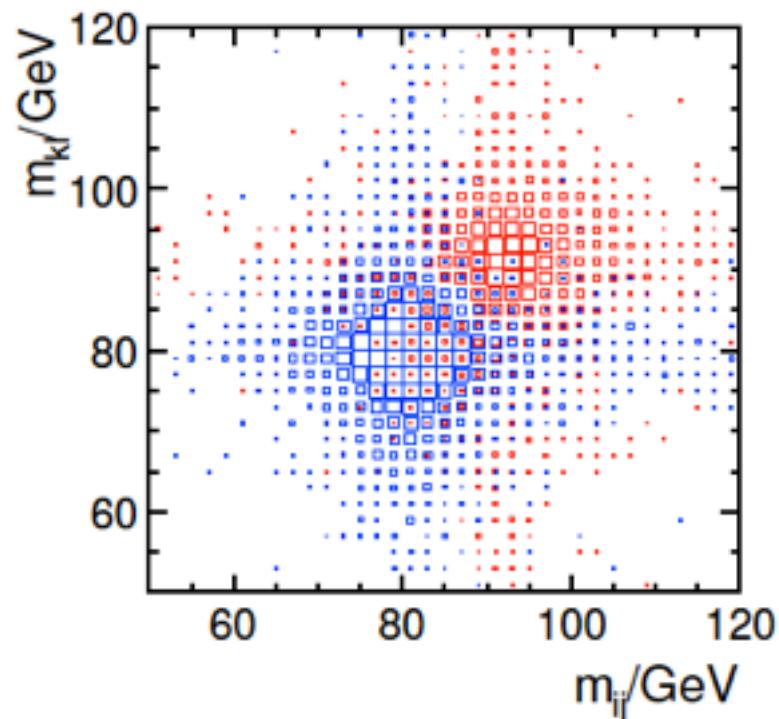
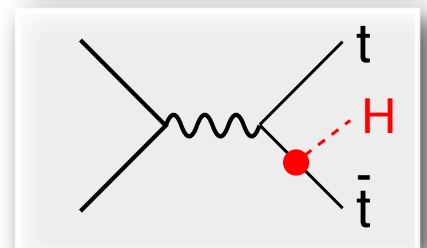
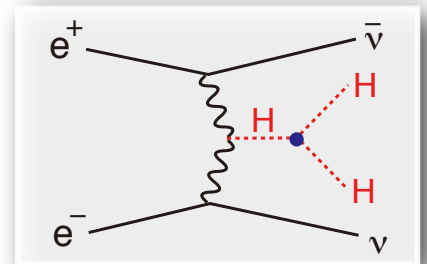
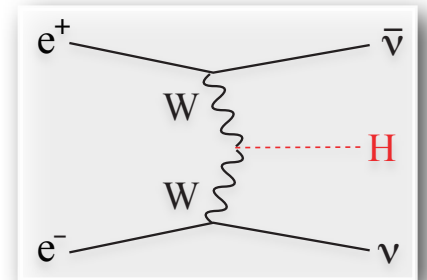
- allows us to measure rare decays such as $H \rightarrow \mu^+ \mu^-$, ...
- further improvements of coupling measurements

vvHH @ 1TeV or higher : 2 ab^{-1} (pol e^+, e^-)=(+0.2,-0.8)

- cross section increases with E_{cm} , which compensates the dominance of the background diagrams at higher energies, thereby giving a better precision for the self-coupling.
- If possible, we want to see the running of the self-coupling (very very challenging).

ttbarH @ 1TeV : 1 ab^{-1}

- Prod. cross section becomes maximum at around 800GeV.
- CP mixing of Higgs can be unambiguously studied.



Obvious but most important advantage of higher energies in terms of Higgs physics is, however, its **higher mass reach to other Higgs bosons** expected in extended Higgs sectors and **higher sensitivity to $W_L W_L$ scattering** to decide whether the Higgs sector is strongly interacting or not.

In any case we can improve the mass-coupling plot by including the data at 1TeV!

Independent Higgs Measurements at ILC

Canonical ILC program

250 GeV: 250 fb⁻¹

500 GeV: 500 fb⁻¹

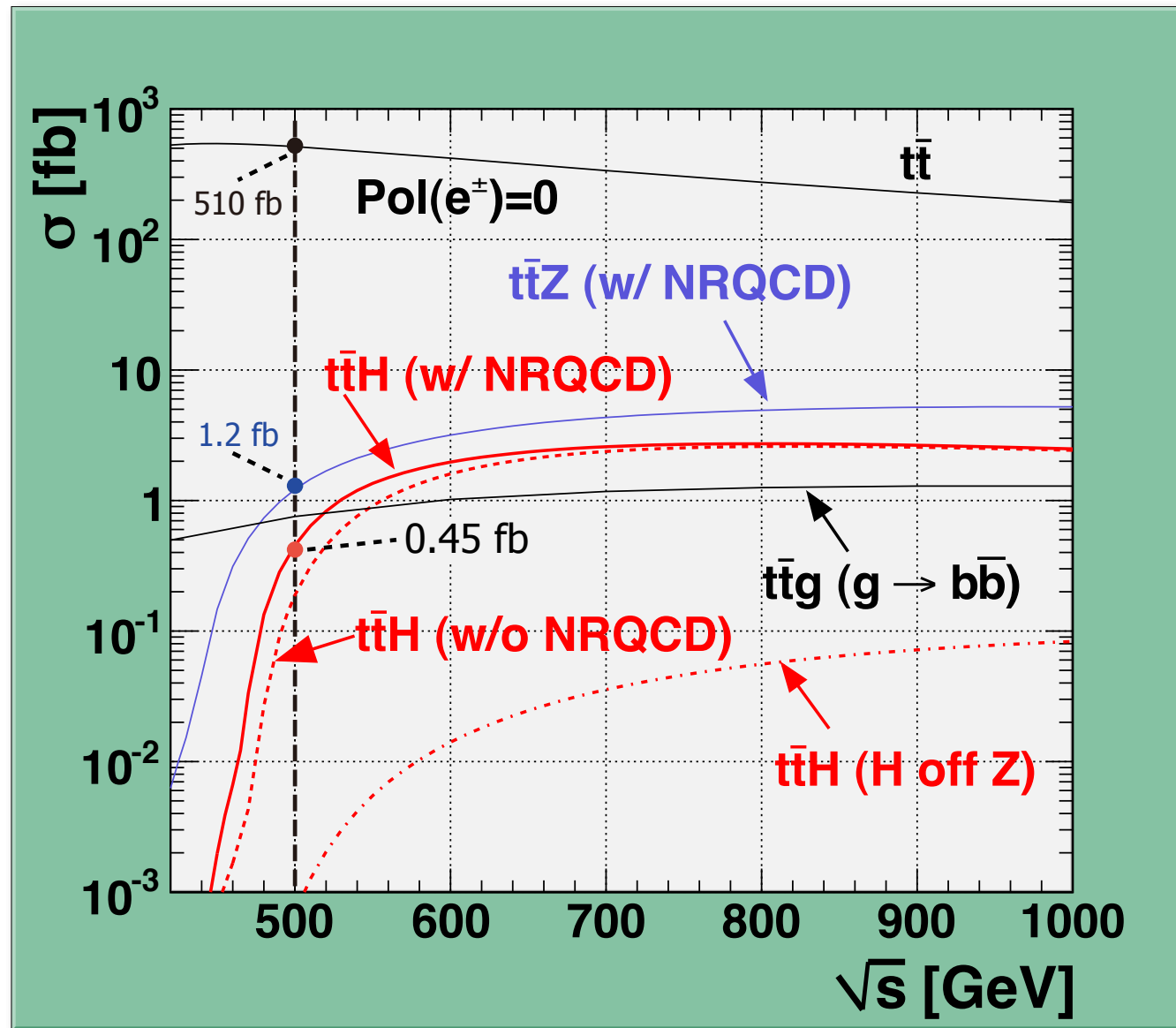
1 TeV: 1000 fb⁻¹

(M_H = 125 GeV)

Ecm	250 GeV		500 GeV		1 TeV
luminosity [fb ⁻¹]	250		500		1000
polarization (e ⁻ ,e ⁺)	(-0.8, +0.3)		(-0.8, +0.3)		(-0.8, +0.2)
process	ZH	vvH(fusion)	ZH	vvH(fusion)	vvH(fusion)
cross section	2.6%	-	3.0%	-	
	σ·Br	σ·Br	σ·Br	σ·Br	σ·Br
H→bb	1.2%	10.5%	1.8%	0.66%	0.5%
H→cc	8.3%		13%	6.2%	3.1%
H→gg	7.0%		11%	4.1%	2.3%
H→WW*	6.4%		9.2%	2.4%	1.6%
H→ττ	4.2%		5.4%	9.0%	3.1%
H→ZZ*	18%		25%	8.2%	4.1%
H→γγ	34%		34%	23%	8.5%
H→μμ	100%	-	-	-	31%

Top Yukawa Coupling at 1TeV

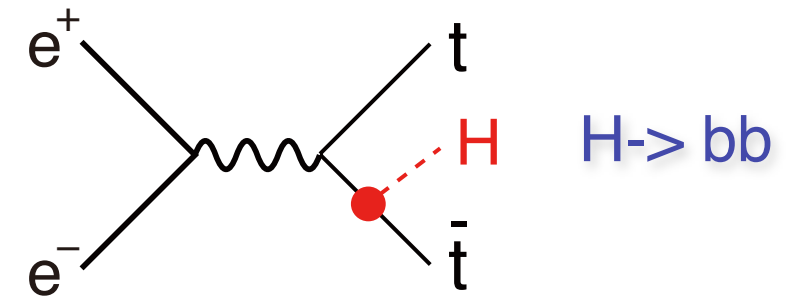
The largest among matter fermions, but not yet observed



Cross section maximum at around
 $E_{cm} = 800 \text{ GeV}$

Tony Price & Tomohiko Tanabe: ILD DBD Study
Philipp Roloff & Jan Strube: SiD DBD Study

DBD Full Simulation



Similar significance in both modes

8-jet mode: 7.9σ (TMVA)

L+6-jet mode: 8.4σ (TMVA)

Tony Price & Tomohiko Tanabe: ILD DBD Study

$$1 \text{ ab}^{-1} @ 500 \text{ GeV} \quad m_H = 125 \text{ GeV}$$

$$\Delta g_Y(t)/g_Y(t) = 9.9\%$$

Tony Price, LCWS12

scaled from $m_H=120 \text{ GeV}$



$$1 \text{ ab}^{-1} @ 1 \text{ TeV} \quad m_H = 125 \text{ GeV}$$

$$\Delta g_Y(t)/g_Y(t) = 3.1\%$$

ILD / SiD DBD Studies

Higgs self-coupling @ 1 TeV

$$P(e^-, e^+) = (-0.8, +0.2) \quad e^+ + e^- \rightarrow \nu \bar{\nu} H H \quad M(H) = 120 \text{ GeV} \quad \int L dt = 2 \text{ ab}^{-1}$$

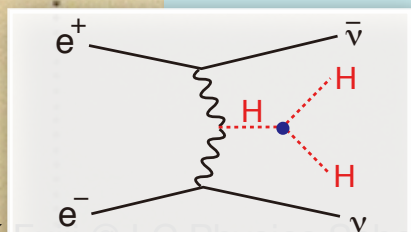
	Expected	After Cut
$\nu\nu hh$ (WW F)	272	35.7
$\nu\nu hh$ (ZHH)	74.0	3.88
BG (tt/ $\nu\nu$ ZH)	7.86×10^5	33.7
significance	0.30	4.29

- better sensitive factor
- benefit more from beam polarization
- BG tt x-section smaller
- more boosted b-jets

$$\frac{\Delta\sigma}{\sigma} \approx 23\% \quad \frac{\Delta\lambda}{\lambda} \approx 18\%$$

Double Higgs excess significance: $> 7\sigma$

Higgs self-coupling significance: $> 5\sigma$



HHH Prospects

Scenario A: $HH \rightarrow bbbb$, full simulation done

Scenario B: by adding $HH \rightarrow bbWW^*$, full simulation ongoing,
expect $\sim 20\%$ relative improvement

Scenario C: color-singlet clustering, future improvement,
expected $\sim 20\%$ relative improvement (conservative)

HHH	500 GeV			500 GeV + 1 TeV		
Scenario	A	B	C	A	B	C
Canonical	104%	83%	66%	26%	21%	17%
LumiUP	58%	46%	37%	16%	13%	10%

ILC 250+500+1000

Model-independent Global Fit for Couplings

33 σ_{BR} measurements (Y_i) and σ_{ZH} ($Y_{34,35}$)

$$\chi^2 = \sum_{i=1}^{35} \left(\frac{Y_i - Y'_i}{\Delta Y_i} \right)^2$$

$$Y'_i = F_i \cdot \frac{g_{HA_i A_i}^2 \cdot g_{HB_i B_i}^2}{\Gamma_0} \quad \begin{array}{l} (A_i = Z, W, t) \\ (B_i = b, c, \tau, \mu, g, \gamma, Z, W : \text{decay}) \end{array}$$

$$\vdots \quad (i = 1, \dots, 33)$$

$$F_i = S_i G_i \dots \dots \dots G_i = \left(\frac{\Gamma_i}{g_i^2} \right)$$

$$\vdots \dots \dots S_i = \left(\frac{\sigma_{ZH}}{g_{HZZ}^2} \right), \left(\frac{\sigma_{\nu\bar{\nu}H}}{g_{HWW}^2} \right), \text{ or } \left(\frac{\sigma_{t\bar{t}H}}{g_{Htt}^2} \right)$$

- The recoil mass measurement is the key to unlock the door to this completely model-independent analysis!
- Cross section calculations (S_i) do not involve QCD ISR.
- Partial width calculations (G_i) do not need quark mass as input.

We are confident that the total theory errors for S_i and G_i will be at the 0.1% level at the time of ILC running.

Model-independent Global Fit for Couplings

Baseline ILC program

250 GeV: 250 fb⁻¹
 500 GeV: 500 fb⁻¹
 1 TeV: 1000 fb⁻¹

(M_H = 125 GeV)

P(e⁻,e⁺)=(-0.8,+0.3) @ 250, 500 GeV

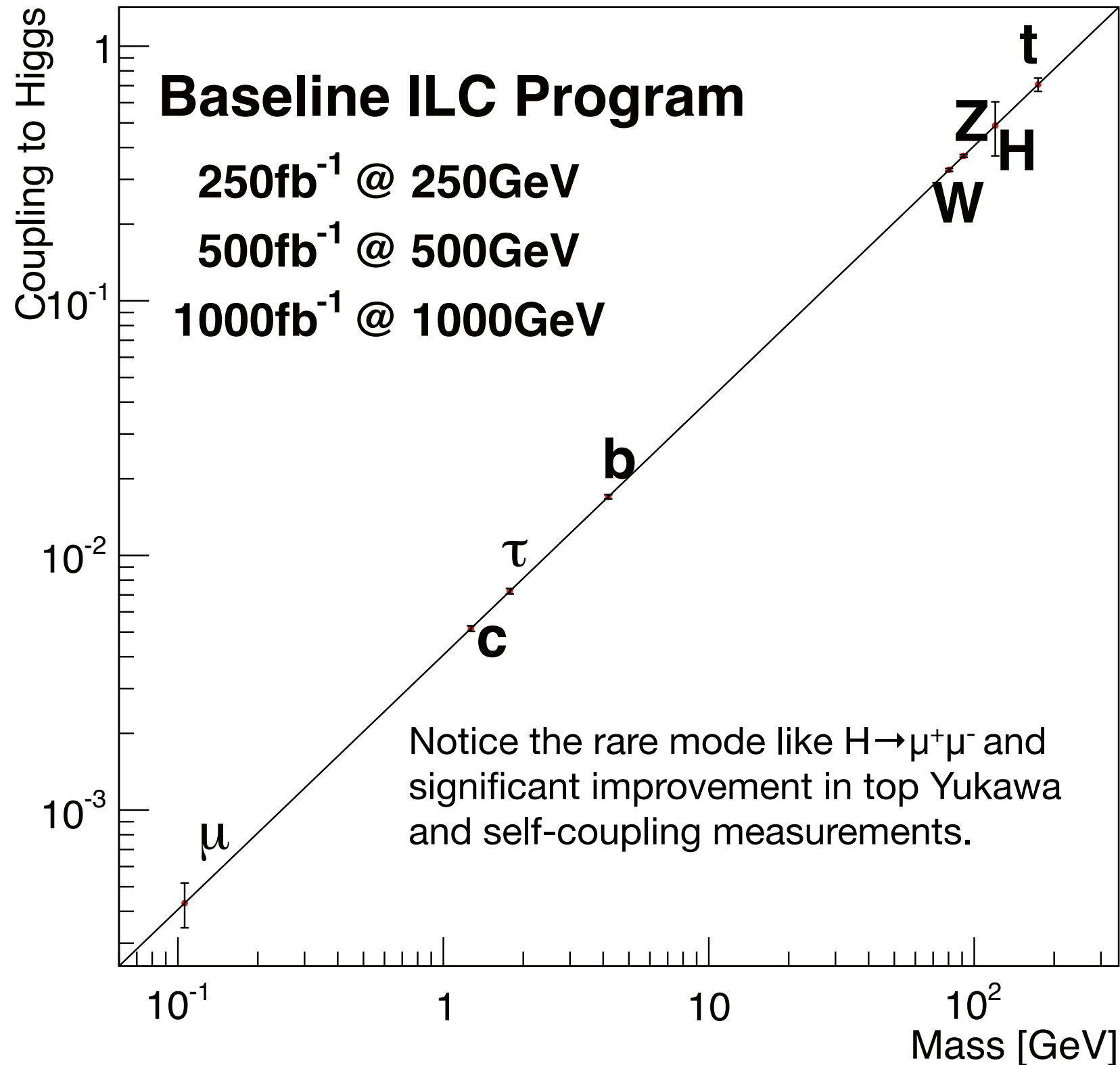
P(e⁻,e⁺)=(-0.8,+0.2) @ 1 TeV

coupling	250 GeV	250 GeV + 500 GeV	250 GeV + 500 GeV + 1 TeV
HZZ	1.3%	1.0%	1.0%
HWW	4.8%	1.1%	1.1%
Hbb	5.3%	1.6%	1.3%
Hcc	6.8%	2.8%	1.8%
Hgg	6.4%	2.3%	1.6%
Hττ	5.7%	2.3%	1.6%
Hγγ	18%	8.4%	4.0%
Hμμ	91%	91%	16%
Γ ₀	12%	4.9%	4.5%
Htt	-	14%	3.1%
HHH	-	83%(*)	21%(*)

) With H→WW (preliminary), if we include expected improvements in jet clustering it would become 17%!

Mass Coupling Relation

After Baseline ILC Program



LHC + ILC

Higgs couplings

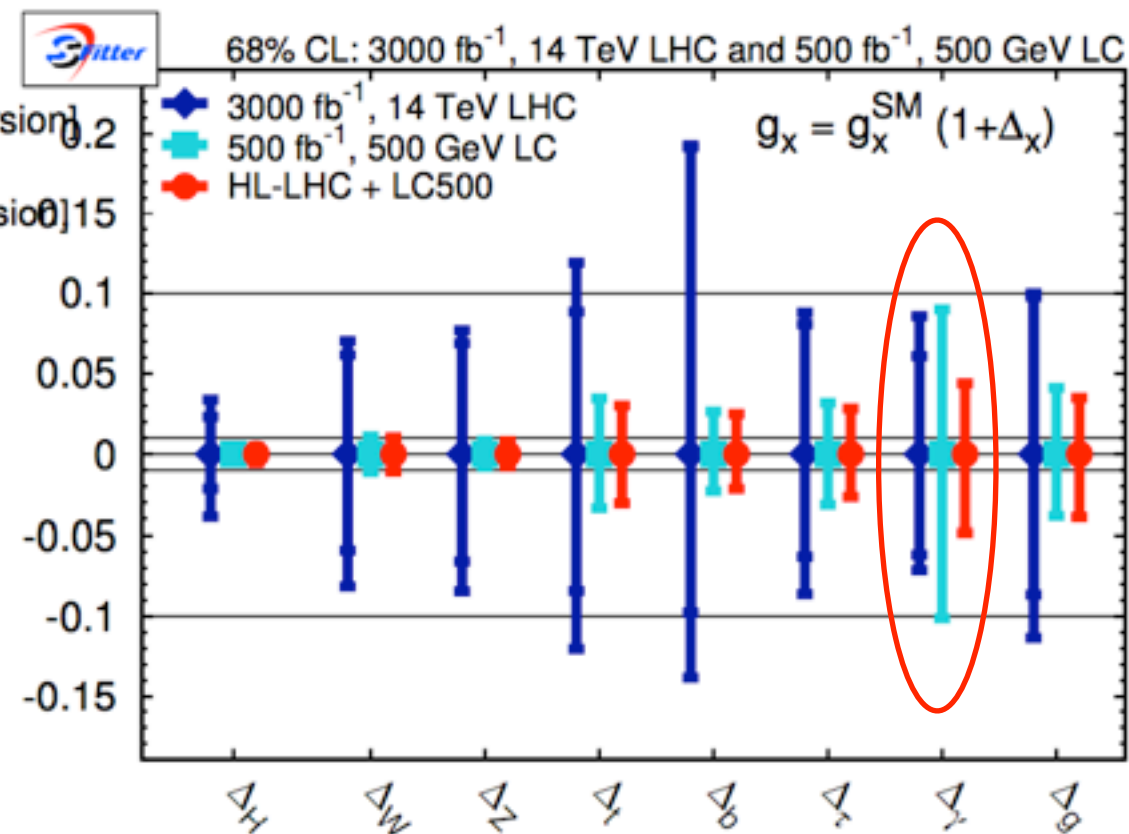
LHC including Moriond/Aspen data [SFitter: Klute, Lafaye, TP, Rauch, Zerwas]

- focus SM-like [secondary solutions possible]
- six couplings and ratios from data
 - g_b from width
 - g_g vs g_t not yet possible
- [similar: Ellis etal, Djouadi etal, Strumia etal, Grojean etal]
- poor man's analyses: $\Delta_H, \Delta_V, \Delta_f$
- Tevatron $H \rightarrow b\bar{b}$ with little impact

Future dinosaurs

- LHC extrapolations unclear [SFitter version 1]
- theory extrapolations tricky [SFitter version 0]
- ILC case obvious [500 GeV for now]
- **interplay in loop-induced couplings**
- $t\bar{t}H$ important at LHC and ILC

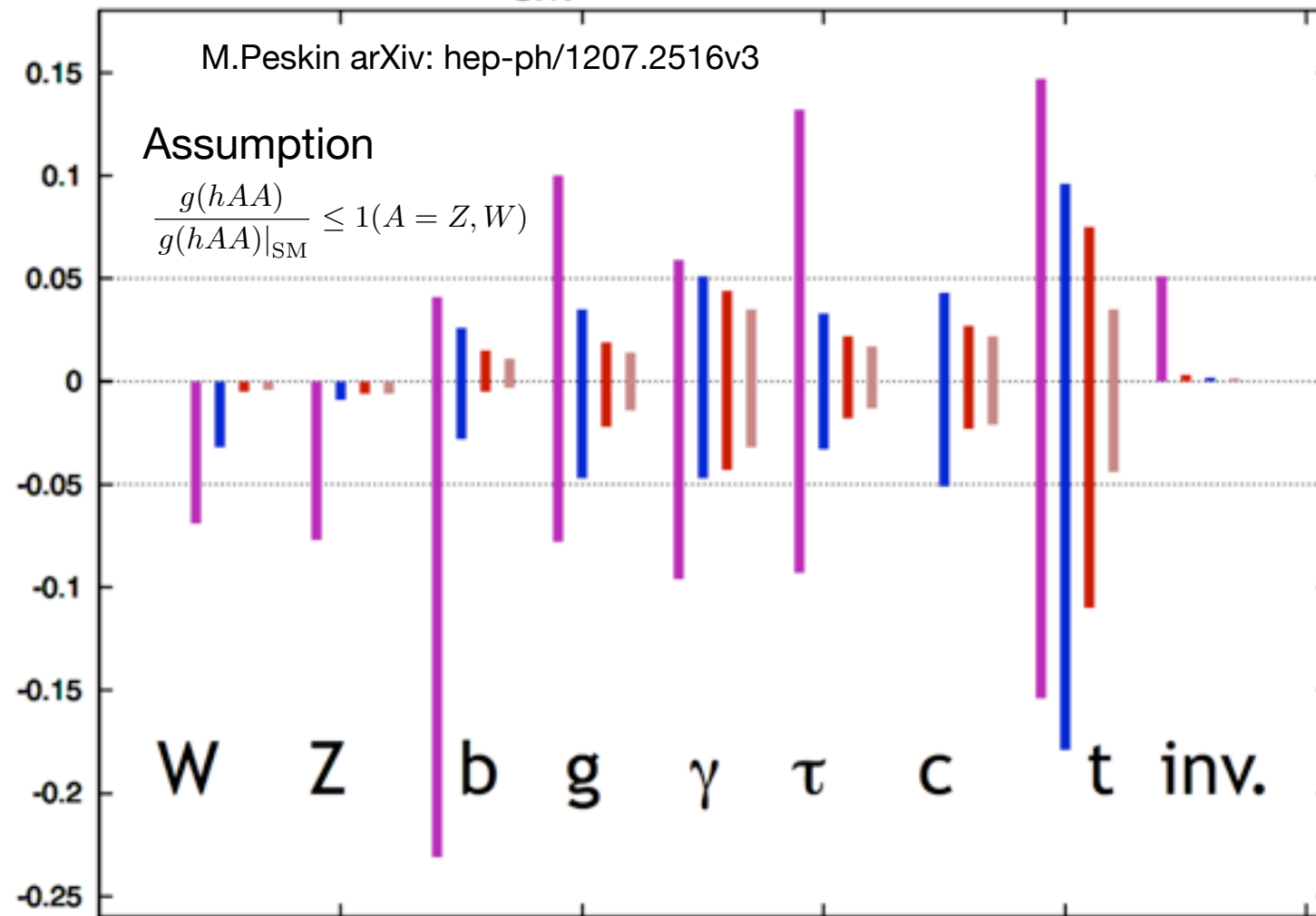
LHC+LC500 Synergy!



Expected Precision and Deviation

Combined Fit with LHC data

$g(hAA)/g(hAA)|_{SM} - 1$ LHC / ILC1 / ILC / ILCTeV



Assumed Luminosities

LHC = LHC14TeV: 300fb⁻¹

HLC = ILC250: 250fb⁻¹

ILC = ILC500: 500fb⁻¹

ILCTeV = ILC1000: 1000fb⁻¹

Maximum deviation when nothing but the 125 GeV object would be found at LHC

	ΔhVV	$\Delta h\bar{t}t$	$\Delta h\bar{b}b$
Mixed-in Singlet	6%	6%	6%
Composite Higgs	8%	tens of %	tens of %
Minimal Supersymmetry	< 1%	3%	10% ^a , 100% ^b
LHC 14 TeV, 3 ab ⁻¹	8%	10%	15%

R.S.Gupta, H.Rzehak, J.D.Wells

arXiv: 1206.3560v1

Mixing with singlet

$$\frac{g_{hVV}}{g_{SMVV}} = \frac{g_{hff}}{g_{SMff}} = \cos \theta \simeq 1 - \frac{\delta^2}{2}$$

Composite Higgs

$$\frac{g_{hVV}}{g_{SMVV}} \simeq 1 - 3\%(1 \text{ TeV}/f)^2$$

$$\frac{g_{hff}}{g_{SMff}} \simeq \begin{cases} 1 - 3\%(1 \text{ TeV}/f)^2 & (\text{MCHM4}) \\ 1 - 9\%(1 \text{ TeV}/f)^2 & (\text{MCHM5}) \end{cases}$$

SUSY

$$\frac{g_{hbb}}{g_{SMbb}} = \frac{g_{h\tau\tau}}{g_{SM\tau\tau}} \simeq 1 + 1.7\% \left(\frac{1 \text{ TeV}}{m_A} \right)^2$$

Figure 2: Comparison of the capabilities of LHC and ILC for model-independent measurements of Higgs boson couplings. The plot shows (from left to right in each set of error bars) 1 σ confidence intervals for LHC at 14 TeV with 300 fb⁻¹, for ILC at 250 GeV and 250 fb⁻¹ ('ILC1'), for the full ILC program up to 500 GeV with 500 fb⁻¹ ('ILC'), and for a program with 1000 fb⁻¹ for an upgraded ILC at 1 TeV ('ILCTeV'). More details of the presentation are given in the caption of Fig. 1. The marked horizontal band represents a 5% deviation from the Standard Model prediction for the coupling.

Fingerprinting is possible or we will get lower bounds on the BSM scale!

Model-dependent Global Fit for Couplings

7-parameter fit

Model Assumptions

$$\kappa_c = \kappa_t \quad \text{and} \quad \Gamma_{\text{tot}} = \sum_{i \in \text{SM decays}} \Gamma_i^{\text{SM}} \kappa_i^2$$

$\kappa_i := g_i / g_i(\text{SM})$

Results

Facility	LHC	HL-LHC	ILC500	ILC500-up	ILC1000	ILC1000-up
\sqrt{s} (GeV)	14,000	14,000	250/500	250/500	250/500/1000	250/500/1000
$\int \mathcal{L} dt$ (fb ⁻¹)	300/expt	3000/expt	250+500	1150+1600	250+500+1000	1150+1600+2500
κ_γ	5 – 7%	2 – 5%	8.3%	4.4%	3.8%	2.3%
κ_g	6 – 8%	3 – 5%	2.0%	1.1%	1.1%	0.67%
κ_W	4 – 6%	2 – 5%	0.39%	0.21%	0.21%	0.2%
κ_Z	4 – 6%	2 – 4%	0.49%	0.24%	0.50%	0.3%
κ_ℓ	6 – 8%	2 – 5%	1.9%	0.98%	1.3%	0.72%
$\kappa_d = \kappa_b$	10 – 13%	4 – 7%	0.93%	0.60%	0.51%	0.4%
$\kappa_u = \kappa_t$	14 – 15%	7 – 10%	2.5%	1.3%	1.3%	0.9%

Snowmass Higgs WG Report (Draft)

Finger Printing

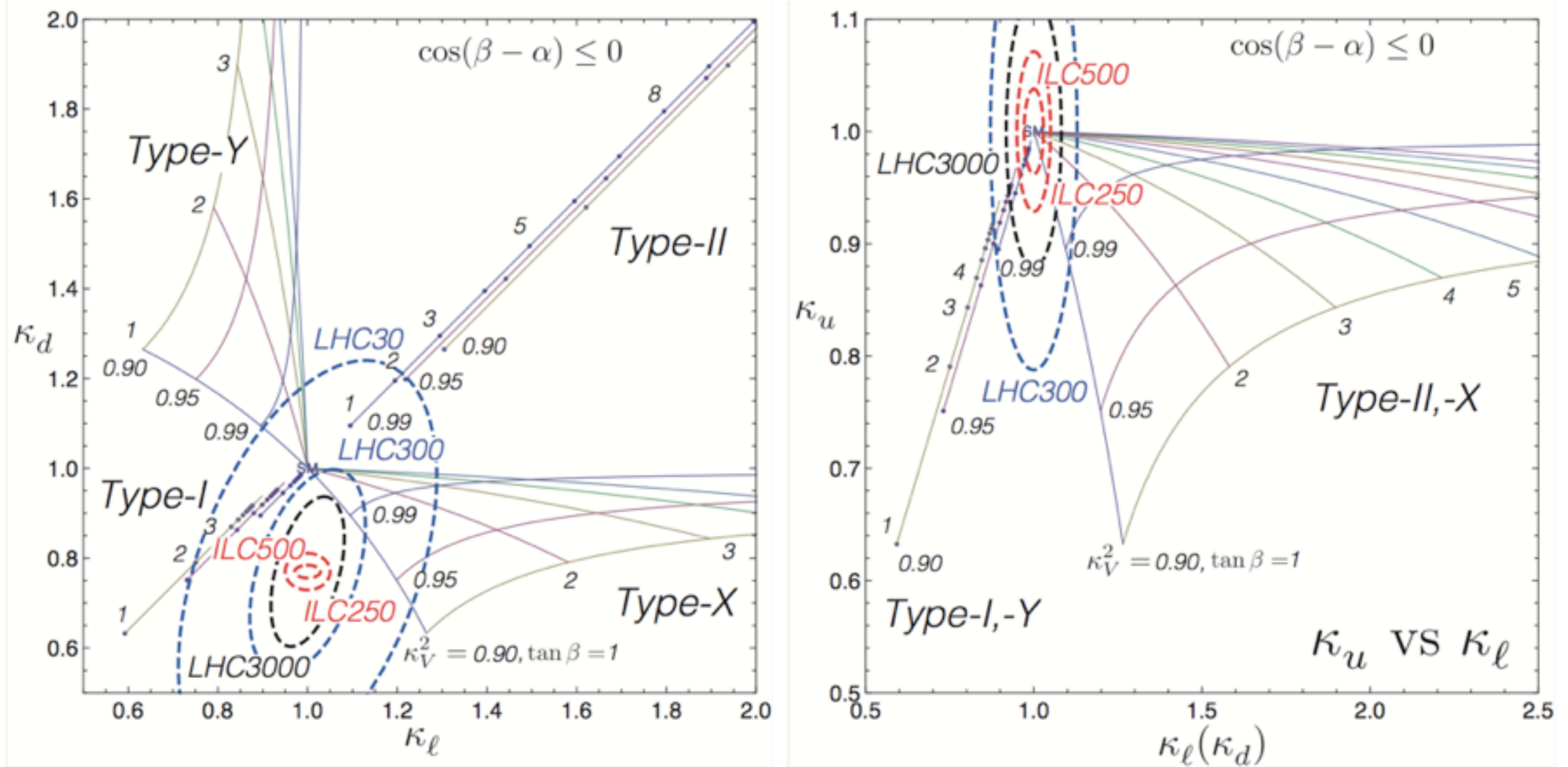


Figure 1.17. The deviation in $\kappa_f = \xi_h^f$ in the 2HDM with Type I, II, X and Y Yukawa interactions are plotted as a function of $\tan \beta = v_2/v_1$ and $\kappa_V = \sin(\beta - \alpha)$ with $\cos(\beta - \alpha) \leq 0$. For the illustration purpose only, we slightly shift lines along with $\kappa_x = \kappa_y$. The points and the dashed curves denote changes of $\tan \beta$ by one steps. The scaling factor for the Higgs-gauge-gauge coupling constants is taken to be $\kappa_V^2 = 0.99, 0.95$ and 0.90 . For $\kappa_V = 1$, all the scaling factors with SM particles become unity. The current LHC constraints, expected LHC and ILC sensitivities on (left) κ_d and κ_ℓ and (right) κ_u and κ_ℓ are added.

Snowmass ILC Higgs White Paper (arXiv: 1310.0763)

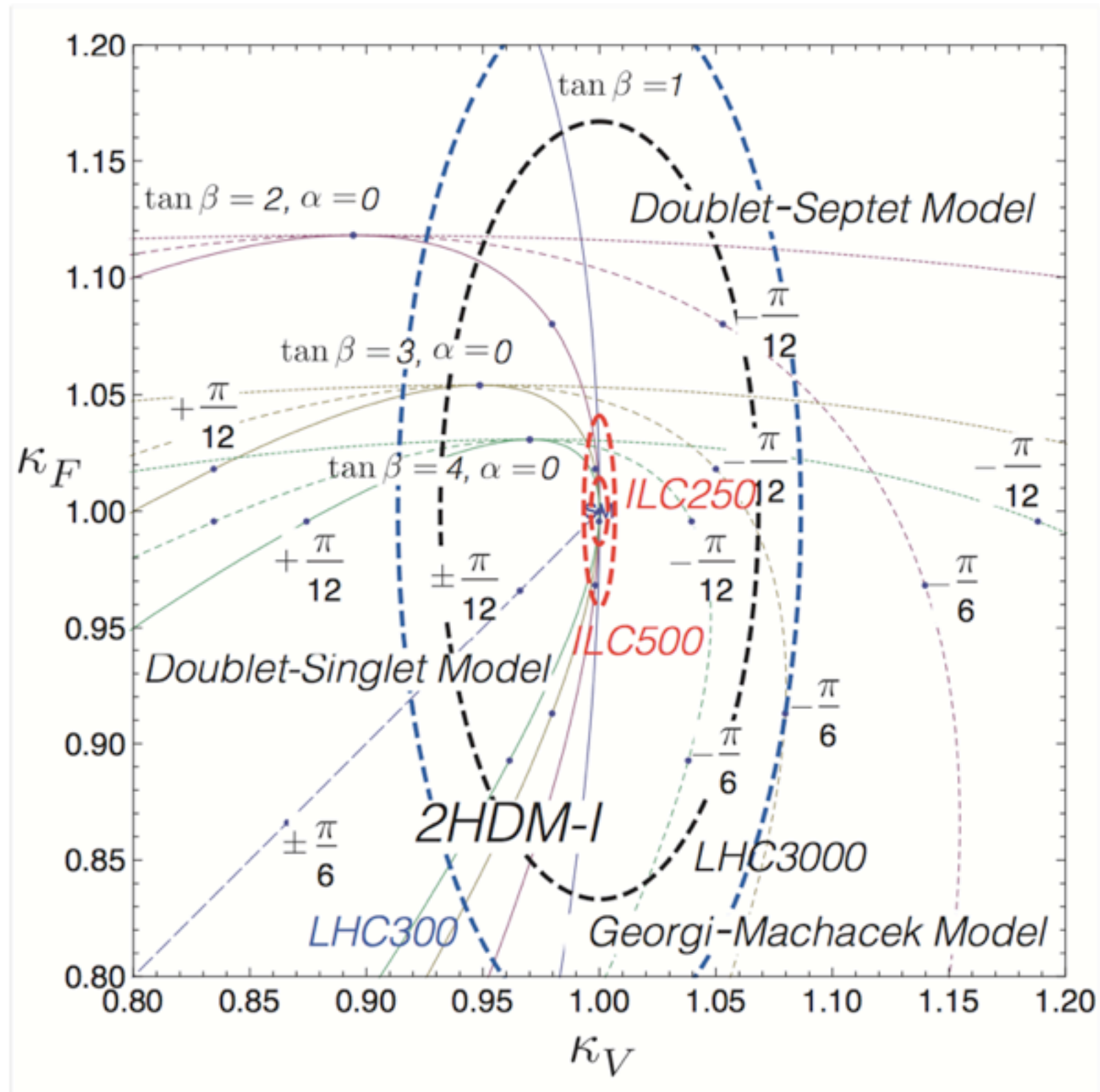


Figure 1.18. The scaling factors in models with universal Yukawa coupling constants.

Self-Coupling

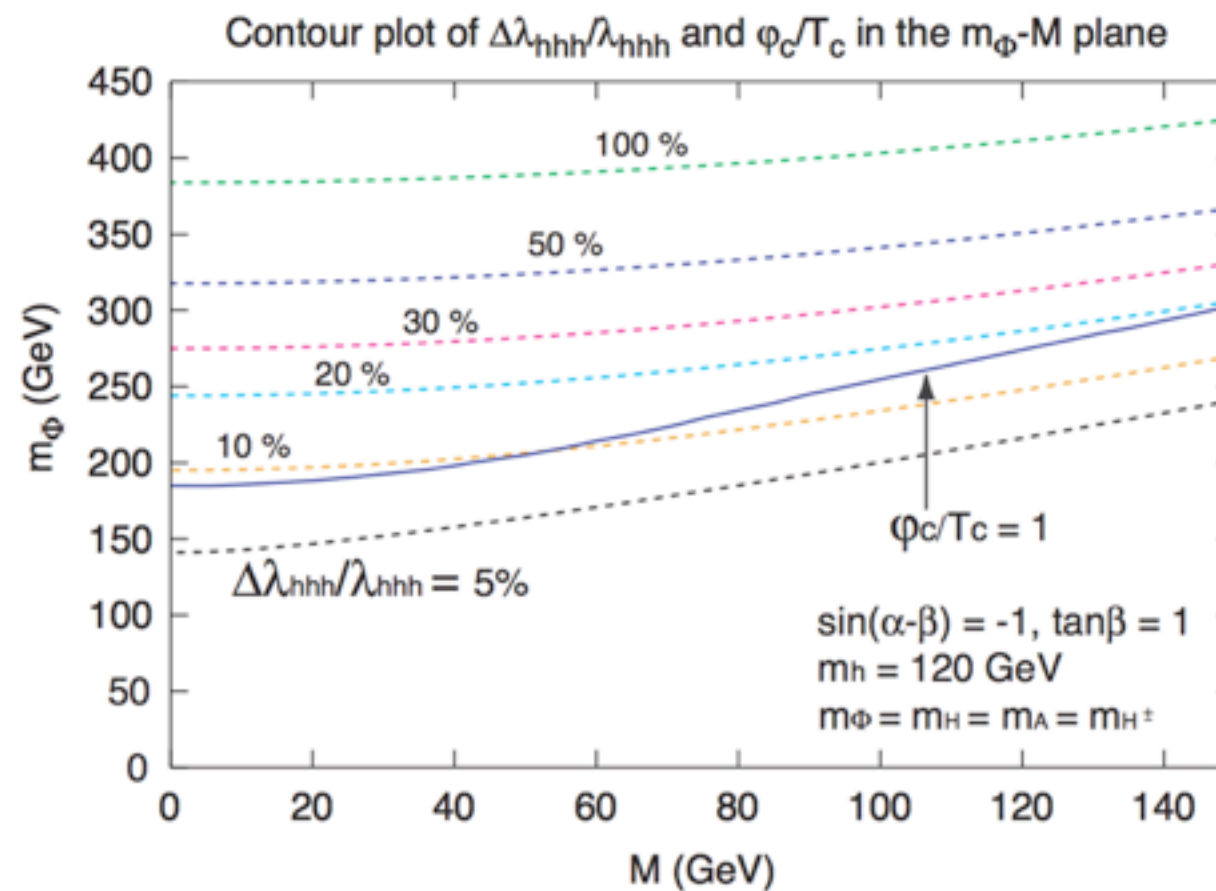
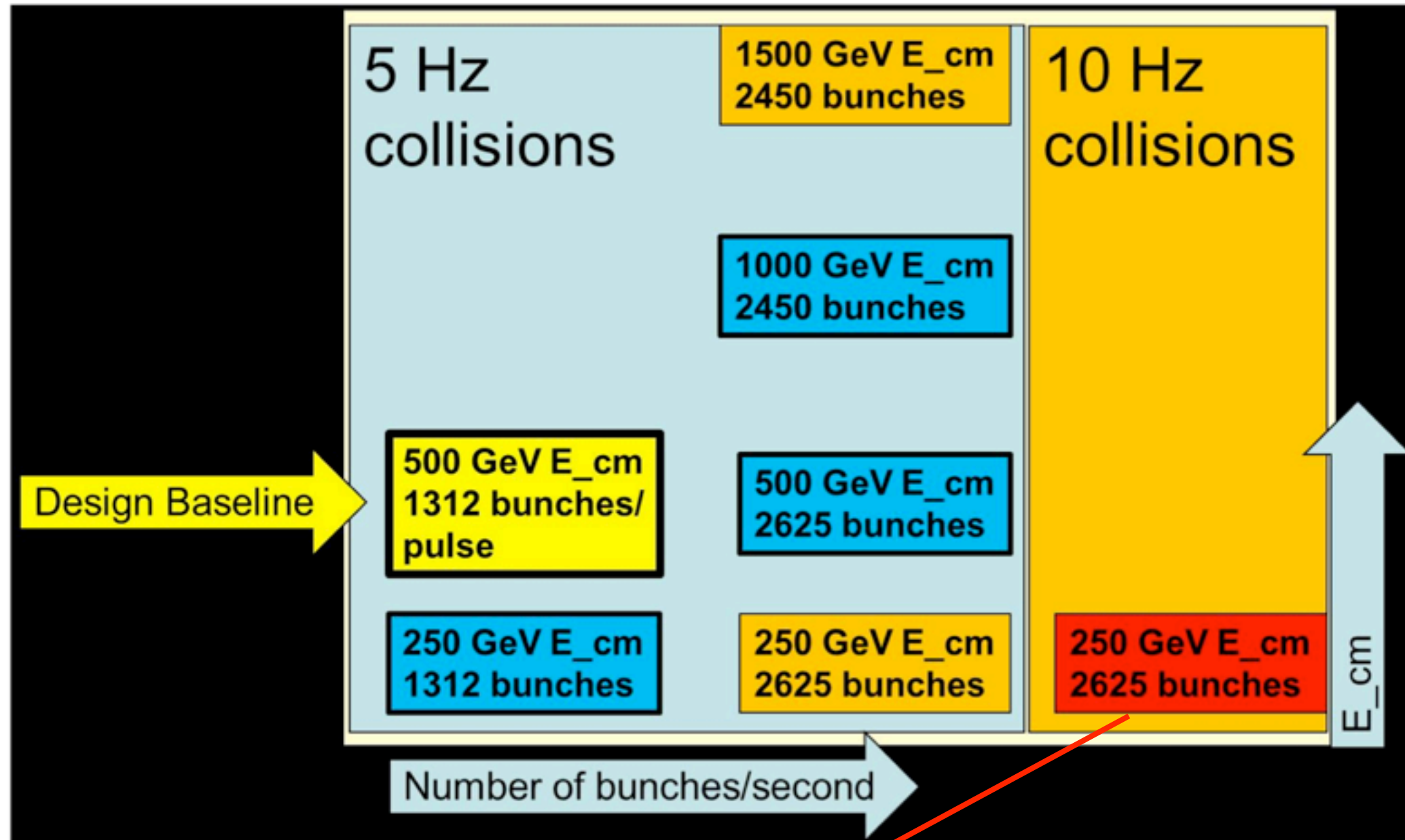


Figure 1.21. The region of strong first order phase transition ($\phi_c/T_c > 1$) required for successful electroweak baryogenesis and the contour plot of the deviation in the triple Higgs boson coupling from the SM prediction [11], where m_Φ represents degenerated mass of H , A and H^\pm and M is the soft-breaking mass of the discrete symmetry in the Higgs potential.

Snowmass ILC Higgs White Paper (arXiv: 1310.0763)

HL-ILC ?

ILC Stages and Upgrades



Snowmass ILC Higgs White Paper (arXiv: 1310.0763)

**x4 upgrade
@250GeV**

Blue: upgrade described in TDR

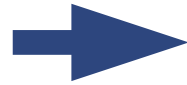
The current ILC design is rather conservative!

Independent Higgs Measurements

Hypothetical HL-ILC

($M_H = 125 \text{ GeV}$)

250 GeV: 250 fb⁻¹
500 GeV: 500 fb⁻¹
1 TeV: 1000 fb⁻¹



250 GeV: 1150 fb⁻¹
500 GeV: 1600 fb⁻¹
1 TeV: 2500 fb⁻¹

Ecm	250 GeV		500 GeV		1 TeV
luminosity · fb	250		500		1000
polarization (e-,e+)	(-0.8, +0.3)		(-0.8, +0.3)		(-0.8, +0.2)
process	ZH	vvH(fusion)	ZH	vvH(fusion)	vvH(fusion)
cross section	1.2%	-	1.7%	-	
	$\sigma \cdot \text{Br}$	$\sigma \cdot \text{Br}$	$\sigma \cdot \text{Br}$	$\sigma \cdot \text{Br}$	$\sigma \cdot \text{Br}$
H-->bb	0.56%	4.9%	1.0%	0.37%	0.3%
H-->cc	3.9%		7.2%	3.5%	2.0%
H-->gg	3.3%		6.0%	2.3%	1.4%
H-->WW*	3.0%		5.1%	1.3%	1.0%
H-->ττ	2.0%		3.0%	5.0%	2.0%
H-->ZZ*	8.4%		14%	4.6%	2.6%
H-->γγ	16%		19%	13%	5.4%
H-->μμ	46.6%	-	-	-	20%

Coupling Measurements

Hypothetical HL-ILC

($M_H = 125$ GeV)

250 GeV: 1150 fb⁻¹

500 GeV: 1600 fb⁻¹

1 TeV: 2500 fb⁻¹

$P(e^-,e^+) = (-0.8, +0.3)$ @ 250, 500 GeV

$P(e^-,e^+) = (-0.8, +0.2)$ @ 1 TeV

coupling	250 GeV	250 GeV + 500 GeV	250 GeV + 500 GeV + 1 TeV
HZZ	0.6%	0.5%	0.5%
HWW	2.3%	0.6%	0.6%
Hbb	2.5%	0.8%	0.7%
Hcc	3.2%	1.5%	1.0%
Hgg	3.0%	1.2%	0.93%
H $\tau\tau$	2.7%	1.2%	0.9%
H $\gamma\gamma$	8.2%	4.5%	2.4%
H $\mu\mu$	42%	42%	10%
Γ_0	5.4%	2.5%	2.3%
Htt	-	7.8%	1.9%

HHH	-	46% (*)	13% (*)
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) With $H \rightarrow WW^$ (preliminary), if we include expected improvements in jet clustering, it would become 10%!

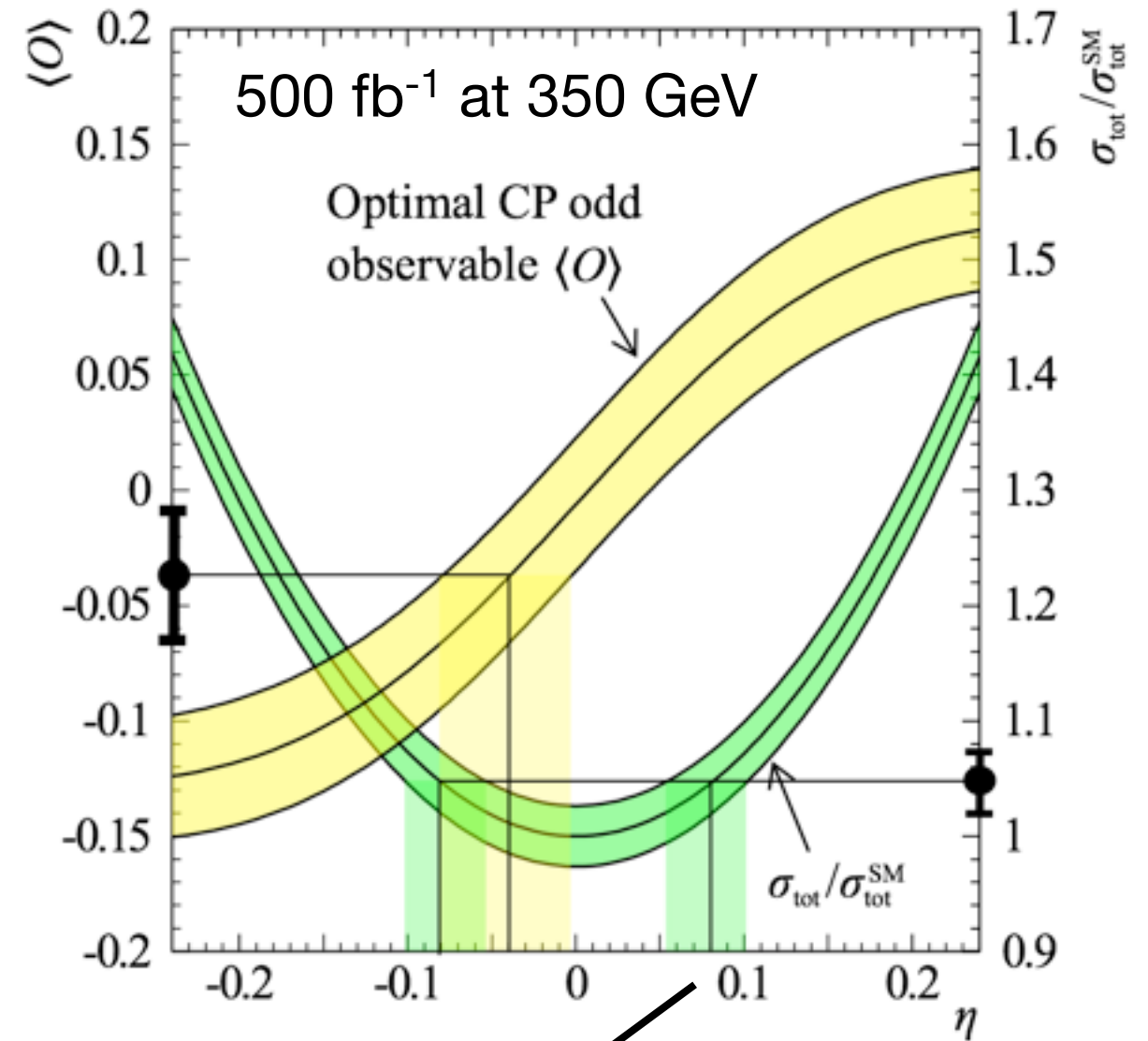
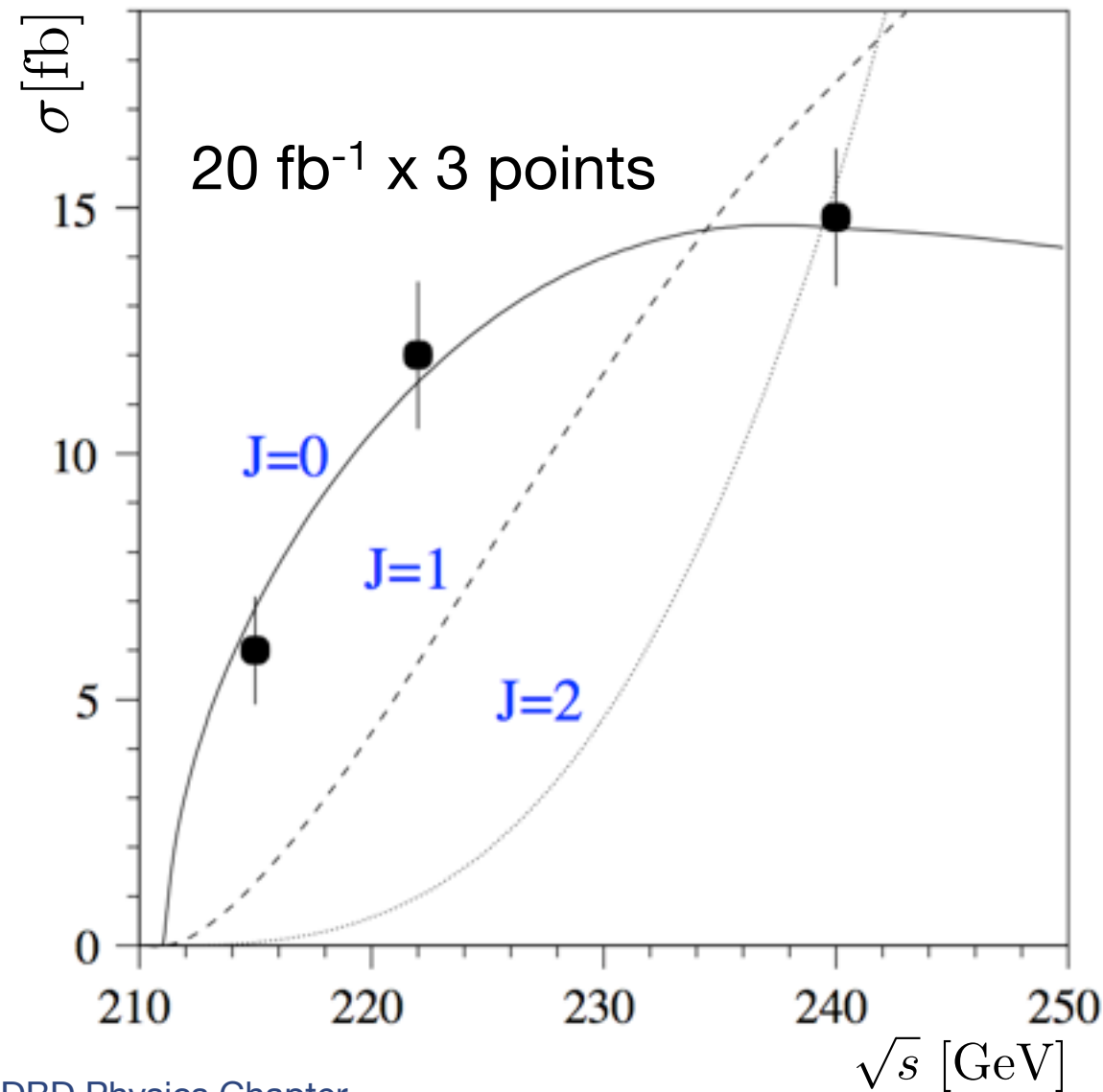
Conclusions

- The primary goal for the next decades is to uncover the secret of the EW symmetry breaking. This will open up **a window to BSM** and **set the energy scale for the E-frontier machine that will follow LHC and ILC**.
- **Probably LHC will hit systematic limits at O(5-10%) for most of $\sigma \times \text{Br}$ measurements, being not enough to see the BSM effects if we are in the decoupling regime.** Moreover, we need some model assumption to extract couplings from the LHC data.
- The recoil mass measurements at ILC unlocks the door to a fully model-independent analysis. To achieve the primary goal we hence need a 500 GeV LC for self-contained precision Higgs studies **to complete the mass-coupling plot**
 - starting from $e^+e^- \rightarrow ZH$ at $E_{\text{cm}} = 250\text{GeV}$,
 - then $t\bar{t}$ at around 350GeV,
 - and then ZHH and $t\bar{t}H$ at 500GeV.
- **The ILC to cover up to 500 GeV is an ideal machine to carry out this mission** (regardless of BSM scenarios) and we can do this **completely model-independently** with staging starting from 250GeV. We may need more data depending on the size of the deviation. **Lumi-upgrade possibility should be always kept in our scope.**
- If we are lucky, some extra Higgs boson or some other new particle might be within reach already at ILC 500. Let's hope that the upgraded LHC will make another great discovery in the next run.
- If not, we will most probably need **the energy scale information from the precision Higgs studies**. Guided by the energy scale information, we will go hunt direct BSM signals with a new machine, if necessary.

Backup

Spin and CP Mixing

Measurements that compliment those at LHC



Search for small CP-odd admixture to a few %

CP-odd ZHH coupling is loop-induced, may not be the best way, though.

SM Higgs BRs

arXiv: 1307.1347

Table 1.1. The Standard Model values of branching ratios of fermionic decays of the Higgs boson for each value of the Higgs boson mass m_h .

m_h (GeV)	$b\bar{b}$	$\tau^+\tau^-$	$\mu^+\mu^-$	$c\bar{c}$	$s\bar{s}$
125.0	57.7 %	6.32 %	0.0219 %	2.91 %	0.0246 %
125.3	57.2 %	6.27 %	0.0218 %	2.89 %	0.0244 %
125.6	56.7 %	6.22 %	0.0216 %	2.86 %	0.0242 %
125.9	56.3 %	6.17 %	0.0214 %	2.84 %	0.0240 %
126.2	55.8 %	6.12 %	0.0212 %	2.81 %	0.0238 %
126.5	55.3 %	6.07 %	0.0211 %	2.79 %	0.0236 %

Table 1.2. The Standard Model values of branching ratios of bosonic decays of the Higgs boson for each value of the Higgs boson mass m_h . The predicted value of the total decay width of the Higgs boson is also listed for each value of m_h .

m_h (GeV)	gg	$\gamma\gamma$	$Z\gamma$	W^+W^-	ZZ	Γ_H (MeV)
125.0	8.57 %	0.228 %	0.154 %	21.5 %	2.64 %	4.07
125.3	8.54 %	0.228 %	0.156 %	21.9 %	2.72 %	4.11
125.6	8.52 %	0.228 %	0.158 %	22.4 %	2.79 %	4.15
125.9	8.49 %	0.228 %	0.162 %	22.9 %	2.87 %	4.20
126.2	8.46 %	0.228 %	0.164 %	23.5 %	2.94 %	4.24
126.5	8.42 %	0.228 %	0.167 %	24.0 %	3.02 %	4.29

Systematic Errors

	Baseline	LumUp
luminosity	0.1%	0.05%
polarization	0.1%	0.05%
b-tag efficiency	0.3%	0.15%

arXiv: 1310.0763

Hunting Ground for Extra Higgs Bosons

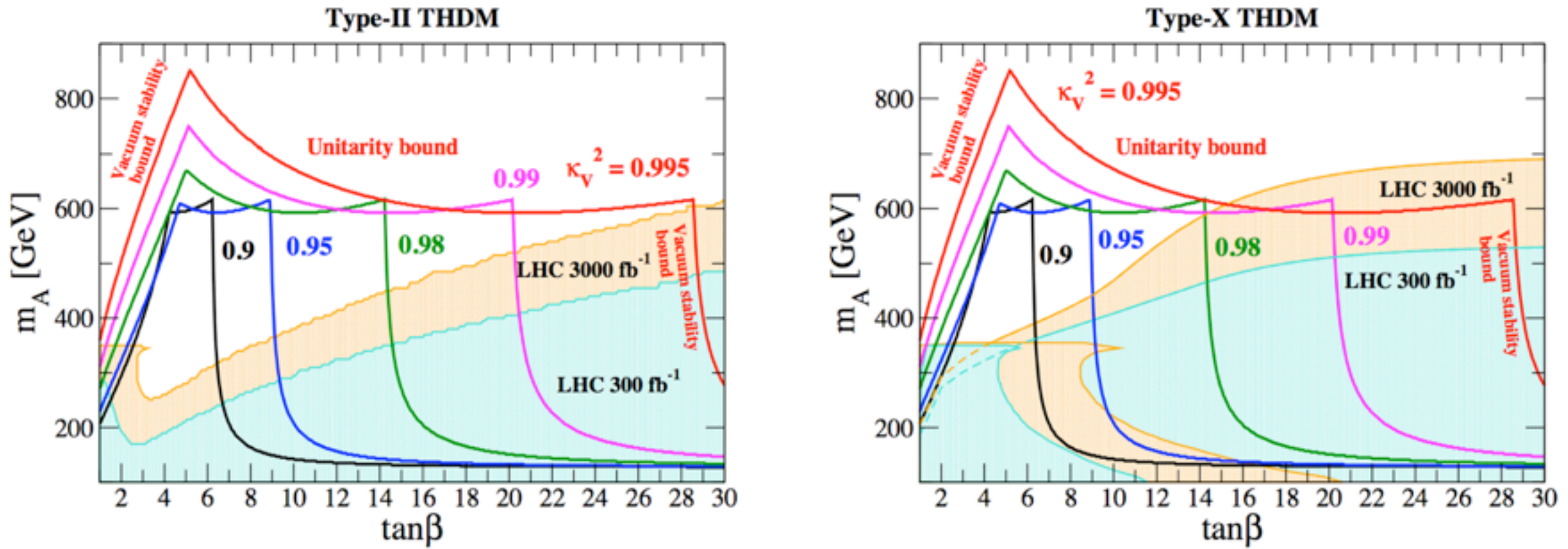
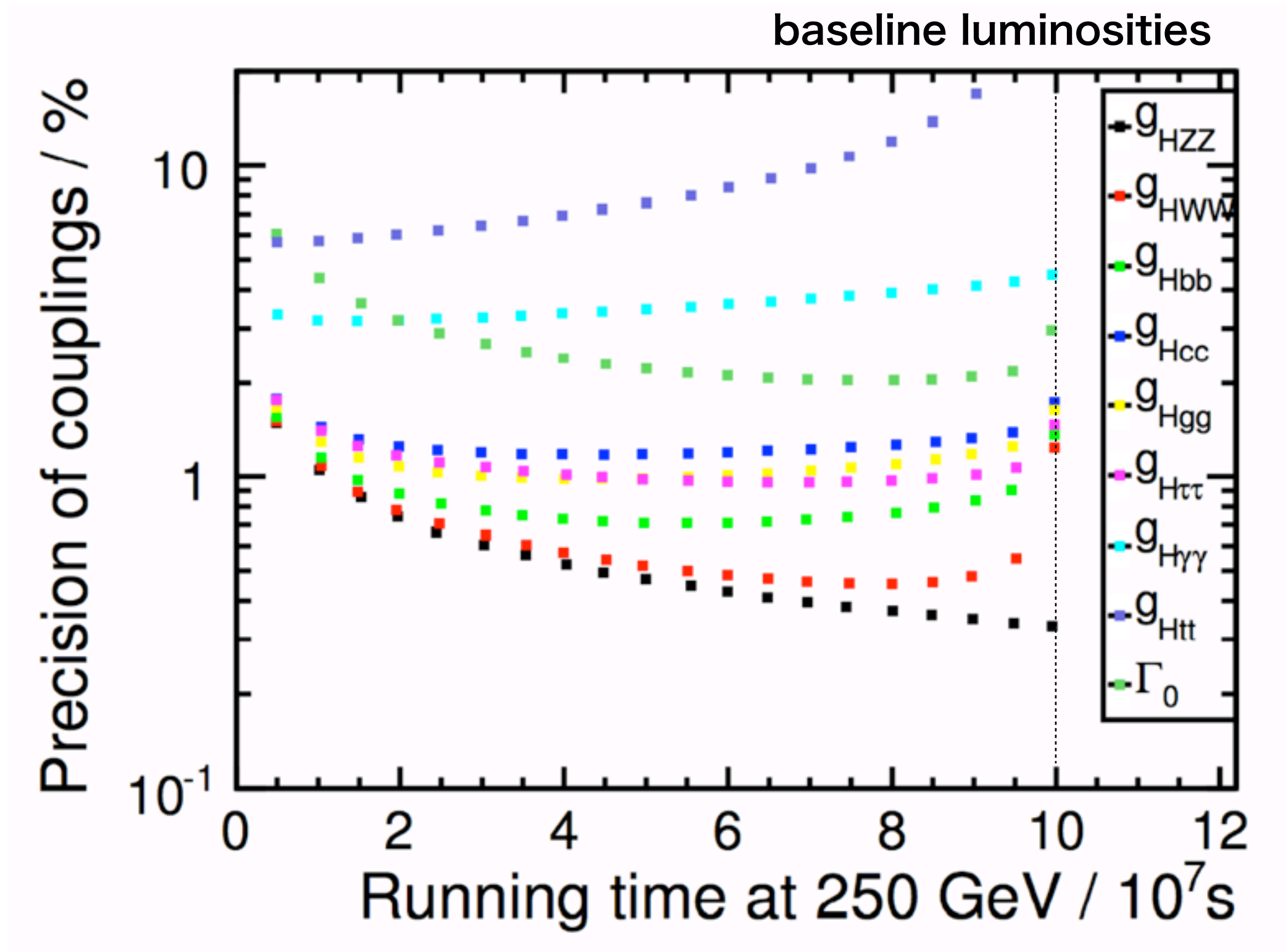


Figure 1.20. Regions below the curves are allowed by the constraints from unitarity and vacuum stability on the $\tan\beta$ - m_A plane for each fixed value of κ_V^2 for $M = m_A = m_H = m_{H^\pm}$ in the Type II and Type X 2HDMs. Expected excluded parameter spaces are also shown by blue (orange) shaded regions from the gluon fusion production and associate production of A and H with bottom quarks and tau leptons at the LHC with the collision energy to be 14 TeV with the integrated luminosity to be 300 fb^{-1} (3000 fb^{-1}).

Snowmass ILC Higgs White Paper (arXiv: 1310.0763)

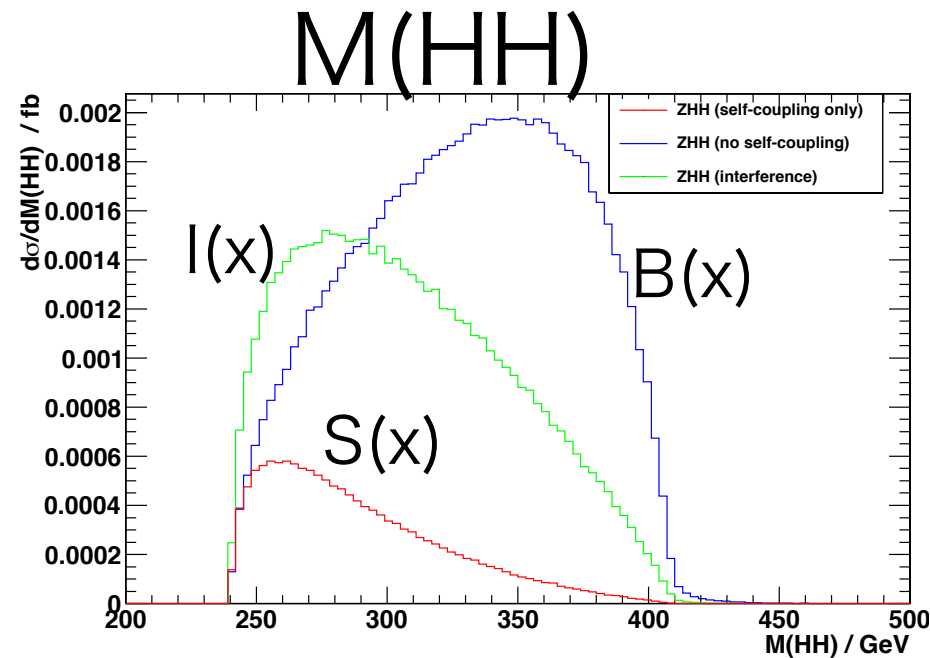
Coupling Precisions

Running Scenarios



Self-coupling Measurement

Weighting Method to Enhance the Sensitivity to λ

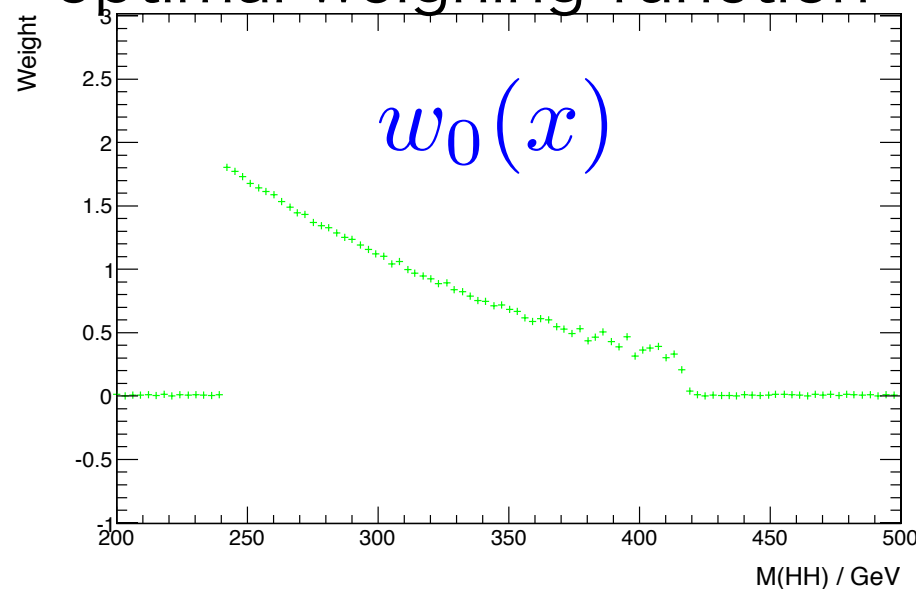


$$\frac{d\sigma}{dx} = \underbrace{B(x)}_{\text{irreducible}} + \underbrace{\lambda I(x)}_{\text{interference}} + \underbrace{\lambda^2 S(x)}_{\text{self-coupling}}$$

Observable: weighted cross-section

$$\sigma_w = \int \frac{d\sigma}{dx} w(x) dx$$

optimal weighing function



Equation for the optimal $w(x)$ (variational principle):

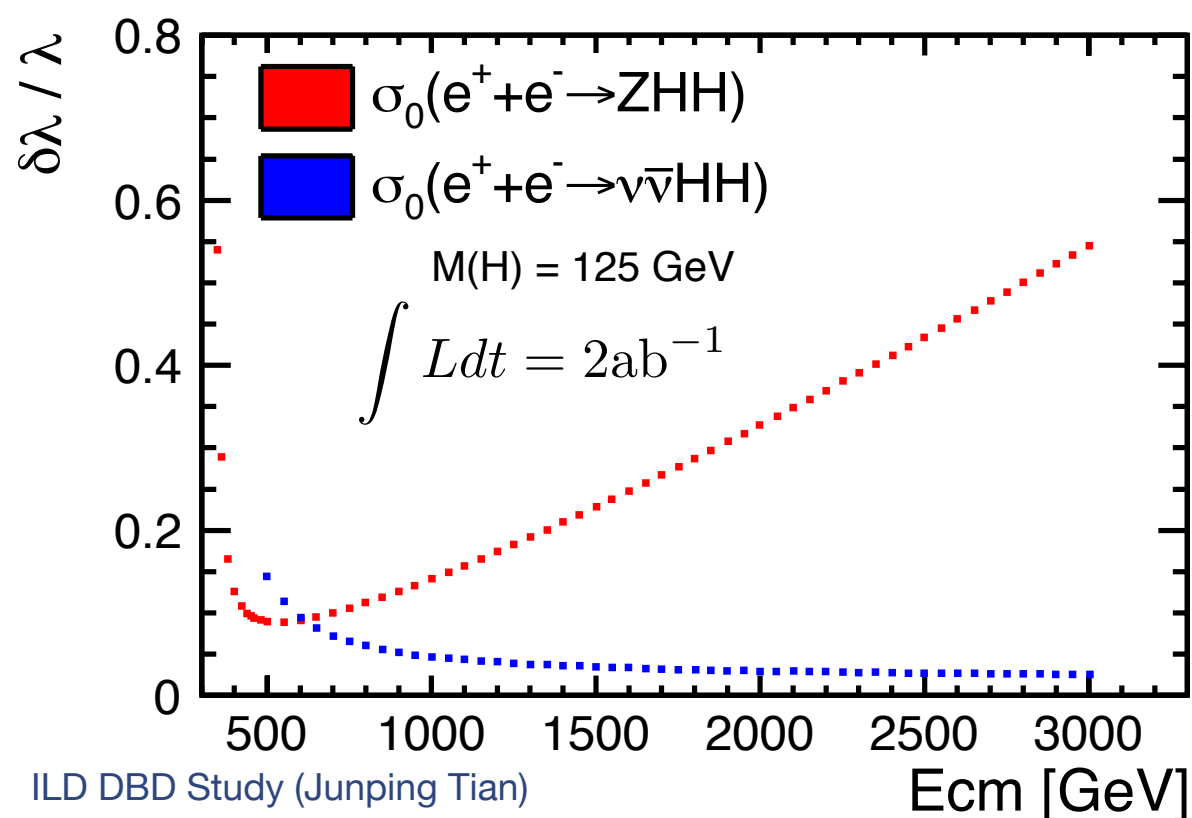
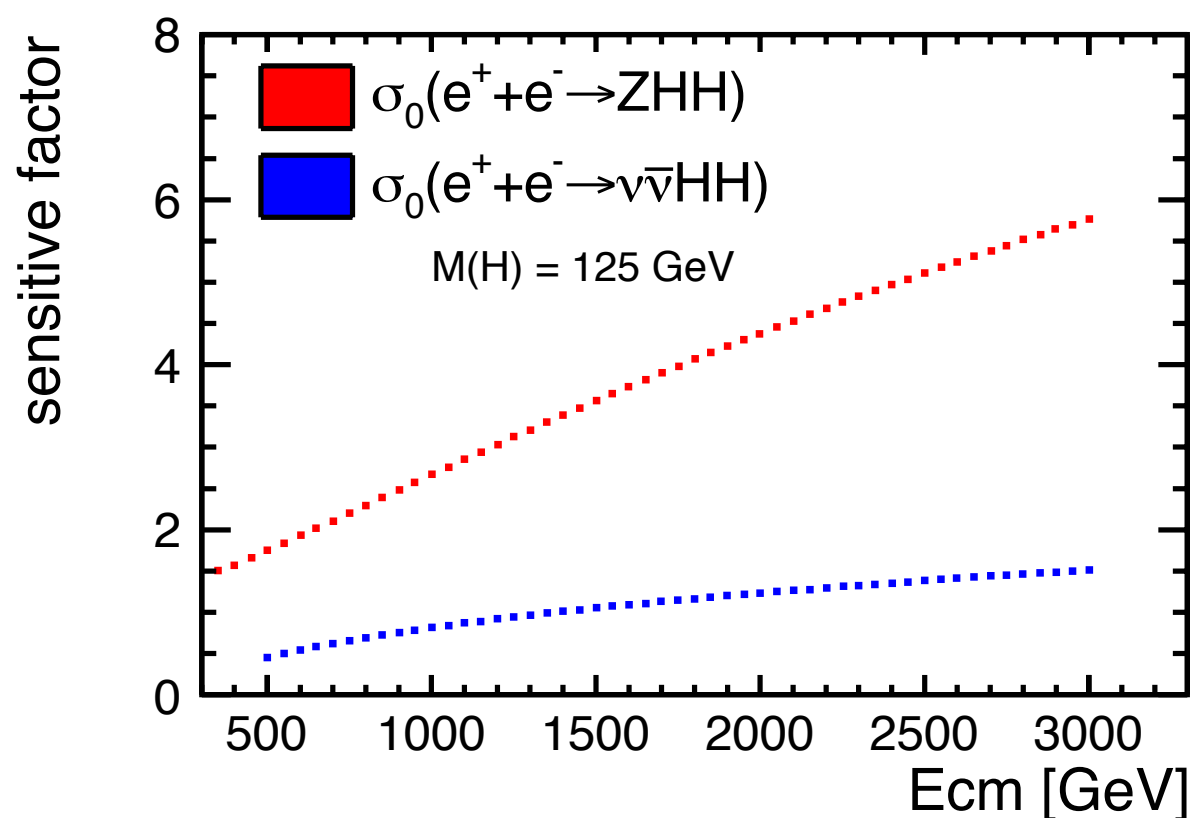
$$\sigma(x)w_0(x) \int (I(x) + 2S(x))w_0(x)dx = (I(x) + 2S(x)) \int \sigma(x)w_0^2(x)dx$$

General solution:

$$w_0(x) = c \cdot \frac{I(x) + 2S(x)}{\sigma(x)}$$

c: arbitrary normalization factor

Expected Coupling Precision as a Function of E_{cm}



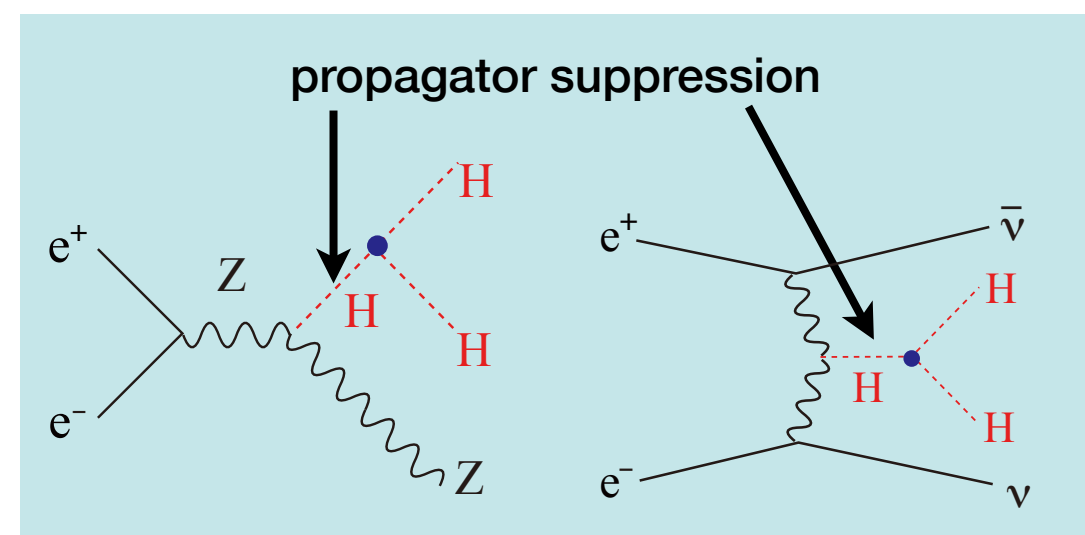
ILD DBD Study (Junping Tian)

Sensitivity Factor

$$\frac{\Delta\lambda}{\lambda} = F \cdot \frac{\Delta\sigma}{\sigma}$$

F=0.5 if no BG diagrams there

BG diagrams dominate at high E_{cm}



⇒ F grows quickly with E_{cm} !

Coupling Precision

ZHH : optimal E_{cm} ~ 500 GeV

though the cross section maximum is at around E_{cm} = 600 GeV

νν̄HH :

Precision slowly improves with E_{cm}

Expected Coupling Precision as a Function of Ecm

