SUSY (and some other BSM): strategies for identifying the underlying physics at the LHC

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General issues and strategies at LHC
 1.1-Telling SUSY from other BSM?
 1.2-Telling MSSM from other (SUSY) scenarios?

2. Reconstructing SUSY model (MSSM) parameters 2.1 -Standard top-down approach Mainly \rightarrow 2.2 An alternative bottom-up approach

Motivations: reconstruct SUSY basic parameters for "minimal" set of identified sparticles, within different scenarios (e.g. in SUSY if GUT scale universality assumptions or not)

3. Summary

1. LHC: General issues and Strategies

Very optimistic BSM (e.g. SUSY): all MSSM sparticles +Higgses found; fit mSUGRA model; find sthing like 'SPS1a' Real life probably harder...

Recent years, focus shifted from "discovering SUSY and measuring its parameters" to gradual questions:

How to discover SUSY-like (weakly interacting theory with partners at TeV) or/and non SUSY-like (strongly interact.
 EFT)

To begin, experimental issues essentially:

- •Trying to tell signal from backgrounds,
- •Tune MC to (signal free) data, see if any deviation from SM,..

2 • How to convince ourselves it's SUSY (and not UED, Little Higgs, or whatever else)

Very active topics (but not that largely explored): May need new analysis techniques (spin & CP properties, new observables, ...)

Need tools that can simulate ANY new physics scenarios... Still, any ideas/properties that further characterize a SUSY model, obviously distinguish it from other BSM scenarios (Need a general enough SUSY model to ensure that typical SUSY properties do not bias measurements.)

Also, keep in mind that new TH ideas on e.g. SUSY-breaking models (see V.V. Khoze talk) may lead to new signatures

A bit more on telling SUSY from other BSM

- e.g. Universal Extra Dim (UED) may fake (R_P) SUSY:
- •KK partners of SM particle with same cplings (however same spin)
- •good DM candidate: neutral, weakly interacting, LKP (LSP) \rightarrow missing energy LHC signatures (with similar long decay chains)
- \rightarrow look at n=2 KK-partners (of gauge bosons) process $pp \rightarrow \gamma_2 \rightarrow l^+ l^-$
- \rightarrow look at spin properties (accessible from e.g. Barr's Asymmetry in decay chains with final l^{\pm}):

$$A^{\pm} = [\sigma(ql^{+}) - \sigma(ql^{-})] / ['' + "]$$

Distinction appears not that easy at LHC (Datta, Kong, Matchev '05)

Spin measurements \rightarrow Next talk by W. Ehrenfeld

Telling MSSM from other SUSY?

3. What kind of Higgs, what kind of SUSY (minimal or not)?

E.g. detecting a H+: evidence for two Higgs doublets.
A light SM Higgs or a more strongly coupled regime?
(NB more on Higgses in V. Khoze talk)

•R-parity violating scenarios,

•NMSSM, beyond..

4. How to measure basic parameters accurately enough to extract underlying SUSY symmetry breaking scale pattern?

Beware the "LHC inverse problem" i.e. discrete ambiguities (potentially many) in reconstructing basic MSSM parameters (Arkani-Hamed, Kane, Thaler, Wang '05)

However, ambiguity levels clearly reduced if using most sophisticated analysis, both experimental and theoretical: -Efforts to calculate all signals at NLO accuracy -Global fits, new observables (e.g. "footprints" in signature space (Arkani-Hamed et al))

-Low energy constraints, interplay with ILC and dark matter

MSSM basic parameter reconstruction

Very lively debate now on what will be most efficient approach: standard "top-down" versus bottom-up; "blind" analysis; fewer observable based (OSET), etc.

Up to now mostly "top-down" approach:
GUT scale Lagrangian → RG evolution → Electroweak
Symmetry Breaking (low scale) → Spectrum determination
(diagonalization+ rad. corr.)
Fit model parameters (e.g mSUGRA) to data set (masses, cross-sections, etc)

+ Pb if too much parameters: hardly fitting general MSSM (22 parameters) even if all sparticle masses, x-sections known..

(though recent progress e.g. SFitter \rightarrow see next)

2.1 Top-down approach (some recent developments)

SFITTER (Lafaye, Plehn, Rauch, D.Zerwas) takes LHC measurements: kinematic edges (from long gluino/squark decay chains), masses, mass differences, cross sections, BRs) +Indirect constraints $(g_2)_{\mu}$; BR $(b \rightarrow s\gamma)$, DM Ωh^2 Compare to th predictions (Spectrum calculators: SoftSUSY, SuSPECT, ISASUSY; Cross sections and BRs: Prospino2, MsmLib, SUSYHit (HDecay + SDecay)) Find best fits using different techniques (Gradient search (Minuit), Markov Chains techniques, Simulated Annealing (Fittino [Bechtle, Desch, Wienemann])

From kinematic edge +other '	"SPS1a" data (r	\sim 15 sparticle mass input):
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	only stat errors	(+th errors)
aneta	9.8 ± 2.3	(4.5)
M_1	101.5 ± 4.6	(7.8)
M_2	191.7 ± 4.8	(7.8)
M_3	575.7 ± 7.7 (14.5)	
μ	μ 350.9 \pm 7.3 (14	
$M_{\tilde{q}_R}$	$_{ ilde{q}_R}$ 506.2 \pm 11.7 (17.5)	

2.2 An alternative "Bottom-up" approach

From physical masses to basic (Lagrangian) parameters (at EWSB scale; then RG evolve up to high (GUT) scale •Analytic, if possible

•Some tree-level inversions worked out in the past

(Moultaka, JLK '98); extended by Kalinowski et al, P. Zerwas et al +many (but mainly ILC context)

- •Transparent, exhibit explicit correlations \rightarrow useful guide to more elaborated analysis
- •New: incorporating as much as possible of the radiative corrections
- •Delineate results valid in a general vs. constrained MSSM (i.e. with GUT scale universality relations)
- -Limited scope yet: not related with MC, only mass input,..

Experimental assumptions and strategy

At LHC, can determine quite accurately some masses from "kinematical endpoints" analysis of (2-body) cascade decays

$$\tilde{g} \to \tilde{q}_L q \to \chi_2^0 q_f q \to \tilde{l}_R l q_f q \to \chi_1^0 l_f l q_f q$$

 \rightarrow quite precise $m_{\tilde{g}}, m_{N_2}, m_{N_1}, m_{\tilde{q}_L}, m_{\tilde{l}_R}, m_{b_1}$ determination from "kinematical endpoints" analysis

(Allanach et al '01, Gjelsen, Miller, Osland '05)

+eventually M_h , + eventually other (independent) \tilde{q} decay NB $\tilde{q} = \tilde{u}, \tilde{d}, \tilde{c}, \tilde{s}$ or \tilde{b}_1, \tilde{b}_2 (could be \tilde{t}_1, \tilde{t}_2 too but not for SPS1a) No way to distinguish experimentally \tilde{q} (similar B.R., no \tilde{q} charge/flavor tagging at LHC)

Above sparticle mass set defines our "minimal" input

different gradually optimistic assumptions on the amount of sparticle mass measurements at the LHC, from gluino cascade and other decays

scenarios	measured mass	expected LHC	decay or process
(+th assumptions)		accuracy (GeV)	
(minimal):	$m_{ ilde{g}}$,	7.2	$ ilde{g}$ cascade decay
S_1 (MSSM),	$m_{ ilde{\chi}_1^0},$	3.7	
S_2 (universality)	$m_{ ilde{\chi}_2^0}.$	3.6	
S_4 ,	$m_{ ilde{q}_L}$,	3.7	" "
S_4' (universality)	$m_{{ ilde l}_R}$	6.0	" "
$S_3 = S_1$ +:	$m_{ ilde{\chi}^0_4}$	5.1	$ ilde q_L o ilde \chi_4^0 +$ cascade
S_5 ,	$m_{ ilde{b}_1}$,	7.5	$ ilde{g}$ cascade decay
S_5' (universality)	$m_{ ilde{b}_2}$	7.9	" "
$S_6 = S_2 + S'_4 + S'_5$ +:	m_h	0.25 (exp)–2 (th)	$h ightarrow \gamma \gamma$ (mainly)

(Accuracies from Weiglein et al '04 report +Gjelsen, Miller, Osland '05)

Bottom-up MSSM reconstruction at LHC

-Three naturally separated sectors (at tree level):

- -gauginos/Higgsinos $M_1, M_2, \mu, \tan \beta$
- -squarks/sleptons μ , $\tan\beta$, \tilde{m}_{q_L} , \tilde{m}_{q_R} , \tilde{m}_{e_L} ,...
- -Higgs parameter sector μ , $\tan \beta$, M_{H_u} , M_{H_d} , M_A
- NB μ , tan β common to all sectors! (and very crucial parameters)
- For each sector there are simple analytical inversions (at tree-level): linear or quadratic eqs.
- Strategy crucially depend on available input masses...(but also the case for standard top-down approach)
- Proceed "step by step", in the 3 sectors, rather than global "all

at once" fit

(JLK, N.Sahoury '08)

Concrete example: Gaugino/Higgsino sector

- Consider the Neutralino mass matrix:

$$M_N = \begin{pmatrix} M_1 & 0 & -m_Z s_W \cos\beta & m_Z s_W \sin\beta \\ 0 & M_2 & m_Z c_W \cos\beta & -m_Z c_W \sin\beta \\ -m_Z s_W \cos\beta & m_Z c_W \cos\beta & 0 & -\mu \\ m_Z s_W \sin\beta & -m_Z c_W \sin\beta & -\mu & 0 \end{pmatrix}$$

Trick: use the 4 invariants (under diagonalization):

$$TrM_N, \ \frac{(TrM_N)^2}{2} - \frac{Tr(M_N^2)}{2}, \ DetM_N$$

give (rather simple) equations; differently used depending on input/output choice

$$P_{ij}^{2} + (\mu^{2} + m_{Z}^{2} - M_{1}M_{2} + (M_{1} + M_{2})S_{ij} - S_{ij}^{2})P_{ij} + \mu m_{Z}^{2}(c_{W}^{2}M_{1} + s_{W}^{2}M_{2})\sin 2\beta - \mu^{2}M_{1}M_{2} = 0$$

$$\begin{split} (M_1 + M_2 - S_{ij})P_{ij}^2 + (\mu^2(M_1 + M_2) + m_Z^2(c_W^2M_1 + s_W^2M_2 - \mu\sin 2\beta))P_{ij} \\ + \mu(m_Z^2(c_W^2M_1 + s_W^2M_2)\sin 2\beta - \mu M_1M_2)S_{ij} = 0 \\ S_{ij} \equiv \tilde{M}_{N_i} + \tilde{M}_{N_j}, P_{ij} \equiv \tilde{M}_{N_i}\tilde{M}_{N_j} \text{ where } i, j = 1, ..4 \end{split}$$

. – p.14/3

Incorporating Radiative Corrections

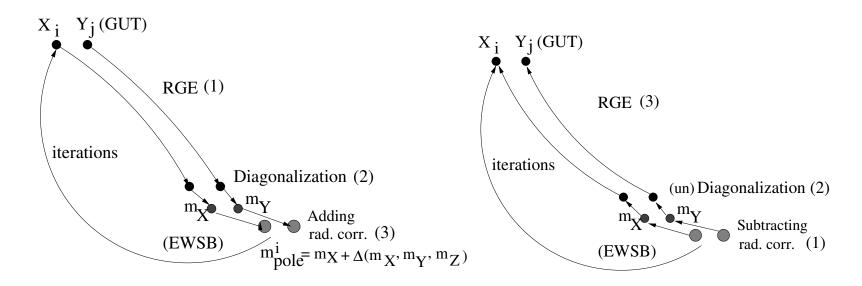
•R.C gives highly non-linear dependence on parameters \rightarrow "brute force" inversion untractable

To very good approximation, keeps tree-level form: e.g $\mu \rightarrow \mu + \Delta \mu, M_1 \rightarrow M_1 + \Delta M_1,...$ (where $\Delta \mu, \Delta M_1, \Delta M_2$ depend on other sector: squarks, sleptons, ..)

- \rightarrow preserves analytic form of inversion
- •Leading R.C. for \tilde{g} involve \tilde{q} of cascade (and vice-versa): \rightarrow known!

•Once some parameters determined, eventually assume universality (SUGRA) relations within loops (should be good approximation in many cases)

General R.C. picture, RGE, etc



Top-down (left) versus bottom-up (right) mappings and their similarities.

1 (3): $X_i, Y_j,...$ running parameters: RGE GUT \leftrightarrow EWSB 2: X_i and Y_j may mix: diag. \rightarrow running masses m_X, m_Y 3 (1): R. C. linking running to pole masses m_{pole}^i added (subtracted) may depend on extra unknown parameters Z_k, m_k : \rightarrow Specific assumptions -+iterations needed.

"Fit" strategy

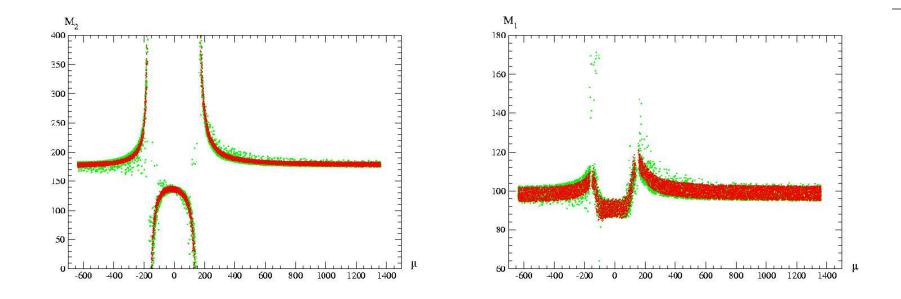
-Solve these analytical (tree-level) equations for various input/output choices;

-vary mass input within errors (uniform "flat prior" or Gaussian distributed)

- -determine allowed contours, or χ^2 , for output basic MSSM parameters within different TH asumptions
- -A bit simple-minded w.r.t. sophisticated M.C.+ MINUIT χ^2 minimization..
- but very easy +fast!

•We compare with MINUIT top-down fits with same input at different stages

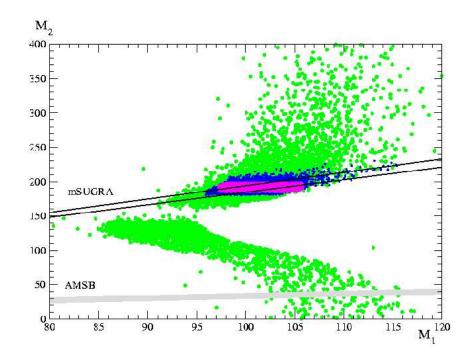
Scenario S1: non-univ. M_1 , M_2 from m_{N_1} m_{N_2}



 M_2 (left) and M_1 (right) as functions of μ . The spreading of points is due to $1 < \tan \beta < 50$ (green) plus m_{N_1} , m_{N_2} variation within accuracy (red).

Directly reflects multifold solutions (for these input here)
Exhibit clear correlations

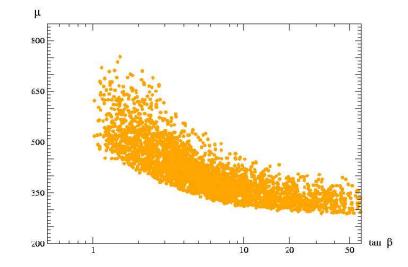
•Very good (few %) $M_{1,2}$ determination except near "pole" μ regions (eliminated if e.g. using $\mu(EWSB) \sim 300 - 400$ GeV, or 3 χ^0 input)



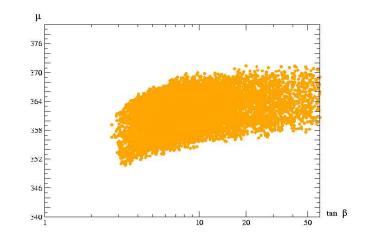
 M_1 , M_2 determination from m_{N_1} , m_{N_2} in Non-univ MSSM: 1) green: $0 \leq \mu \leq 1$ TeV, $0 \leq \tan \beta \leq 50$; 2) blue: $\Delta \tan \beta = 10$, $\Delta \mu = 100$ GeV; 3) pink: $\Delta \tan \beta = 2$, $\Delta \mu = 30$ GeV. \rightarrow May discriminate different models (mSUGRA, AMSB) rather simply at low-energy (avoid RGE up to GUT)

Scenario S2: μ , $\tan\beta$ determination for gaugino M_i universality

IF $M_1 = M_2 = M_3$ (GUT): same Eqs. $\rightarrow \mu, \tan \beta$ from M_1, M_2 :



Assuming third M_{N_3} measurement in addition



Squark, slepton parameter (first two generations)

$$m_{\tilde{u}_{1}}^{2} = m_{\tilde{u}_{L}}^{2} + (\frac{1}{2} - \frac{2}{3}s_{W}^{2})m_{Z}^{2}\cos 2\beta$$
$$m_{\tilde{e}_{2}}^{2} = m_{\tilde{e}_{R}}^{2} - s_{W}^{2}m_{Z}^{2}\cos 2\beta$$

- linear combination to eliminate the $\tan \beta$ dependence ("sum rule"):

$$s_W^2 m_{\tilde{u}1}^2 + (\frac{1}{2} - \frac{2}{3} s_W^2) m_{\tilde{e}2}^2 = s_W^2 m_{\tilde{u}_L}^2 + (\frac{1}{2} - \frac{2}{3} s_W^2) m_{\tilde{e}_R}^2$$

simple to work out RG evolution:

$$\frac{d}{dt} \left[s_W^2 m_{\tilde{u}_L}^2 + \left(\frac{1}{2} - \frac{2}{3} s_W^2\right) m_{\tilde{e}_R}^2 \right]$$
$$= s_W^2 \frac{d\tilde{m}_{u_L}^2}{dt} + \left(\frac{1}{2} - \frac{2}{3} s_W^2\right) \frac{dm_{\tilde{e}_R}^2}{dt} + \frac{ds_W^2}{dt} (\tilde{m}_{u_L}^2 - \frac{2}{3} \tilde{m}_{e_R}^2)$$
(1)

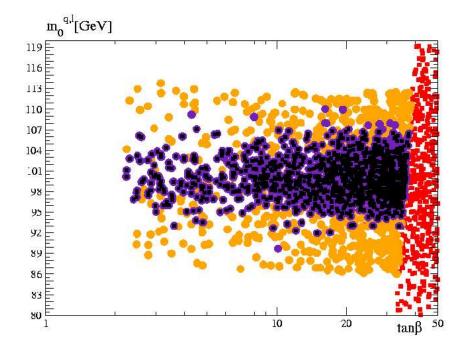
where $t \equiv \ln Q$ and

$$\frac{ds_W^2}{dt} = \left(\frac{3}{5}g_1^2 + g_2^2\right)^{-1} \left(\frac{3}{5}c_W^2 \frac{dg_1^2}{dt} - s_W^2 \frac{dg_2^2}{dt}\right)$$

NB this RGE (one-loop) only depend on gaugino M_i and gauge cplings!

84 (86) $\text{GeV} \lesssim m_0^{q,l} \lesssim 116 \ (112) \ \text{GeV}$

for linear (quad.) error combination, *independently of* $\tan \beta$.



Constraints (from Gaussian scan) on $m_0^{q,l}$, $\tan\beta$: orange: 2- σ from combined $m_{\tilde{e}_R}$, $m_{\tilde{u}_1}$;

indigo: 2- σ from separating $m_{\tilde{u}_1}$ relation; black: 1- σ from $m_{\tilde{u}_1}$. Red: excluded by tachyon $\tilde{\tau}_1$.

Sbottom sector 1: scalar non-universality

 \tilde{b}_1, \tilde{b}_2 involved in \tilde{g} decay (though more difficult for \tilde{b}_2)

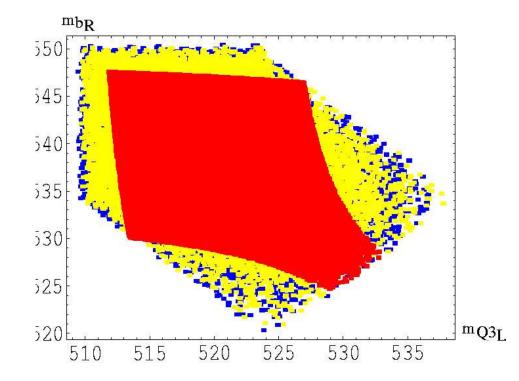
Simple inverted relations to determine m_{Q3_L} , m_{b_R}

$$m_{Q3_L(b_R)} = \left[\frac{S + (-)D}{2}\right]^{1/2}$$

$$S = m_{\tilde{b}_1}^2 + m_{\tilde{b}_2}^2 + \frac{m_Z^2}{2} \cos 2\beta - 2m_b^2$$

$$D = -Y + \left[(m_{\tilde{b}_2}^2 - m_{\tilde{b}_1}^2 - 2m_b X_b) (m_{\tilde{b}_2}^2 - m_{\tilde{b}_1}^2 + 2m_b X_b) \right]^{1/2}$$

$$Y = (-\frac{1}{2} + \frac{2}{3} s_W^2) m_Z^2 \cos 2\beta, \qquad X_b = A_b - \mu \tan \beta$$



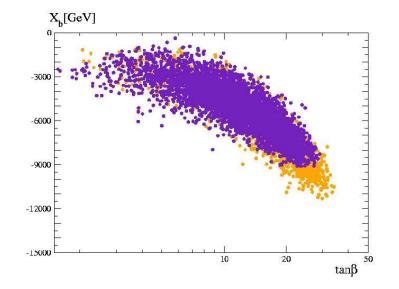
Red: $\tan \beta \sim 9.73$, $\mu \sim 357$ GeV ($A_b = 0$). Yellow: $3 \leq \tan \beta \leq 35$, $\Delta \mu \sim 10$ GeV, $-100GeV < A_b < 100GeV$; blue: $3 \leq \tan \beta \leq 35$, $\Delta \mu \sim 200$ GeV, $-1TeV < A_b < 1TeV$.

Sbottom sector 2: scalar universality

Relate m_{Q3_L}, m_{b_R} to $m_0^{q,l}$ constraints:

 $m_{Q3_L}(Q_{EWSB}) \sim 498 \pm 1.2 \pm 7 \text{GeV}, \ m_{b_R}(Q_{EWSB}) \sim 521 \pm 1.8 \pm 6 \text{GeV}$ (NB dominant error from RGE via M_3 uncertainty)

$$2 m_b X_b = -\left[(m_{\tilde{b}_2}^2 - m_{\tilde{b}_1}^2)^2 - (m_{\tilde{Q}_{3L}}^2 - m_{\tilde{b}_R}^2 + Y)^2 \right]^{1/2}$$



Constraints on $\tan \beta$, $X_b = A_b - \mu \tan \beta$ from Gaussian scan: indigo: one- σ (68% C.L.); orange: two- σ (95% C.L.).

Determination in Higgs sector parameters

In general MSSM: running m_A value:

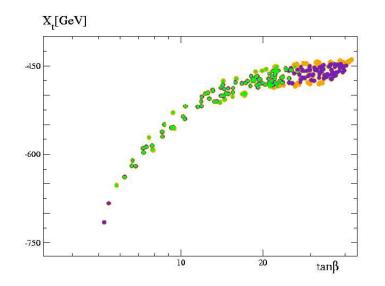
$$\bar{m}_A^2(Q) = m_{H_d}^2 + m_{H_u}^2 + 2\mu^2 = \frac{\bar{m}_h^2(m_Z^2 - \bar{m}_h^2)}{m_Z^2 \cos^2 2\beta - \bar{m}_h^2} + \text{Rad. Corr.}$$

$$m_h^2 = m_h^{2,tree} + \frac{3gm_t^4}{8\pi^2 m_W^2} \left[\ln\left(\frac{m_{\tilde{t}_1}m_{\tilde{t}_2}}{m_t^2}\right) + \frac{X_t^2}{M_S^2} - \frac{X_t^4}{12M_S^4} \right]$$

where $X_t = A_t - \mu \cot \beta$, $M_S^2 \simeq m_{\tilde{t}_1}m_{\tilde{t}_2}$

NB we use more elaborated 1(2)-loop m_h R.C. (Heinemeyer, Hollik, Weiglein '99)

-general MSSM: poorly constrained IF nothing know on stop sector, or m_A ... (not expected for SPS1a)-IF universality: $m_0^{q,l} \equiv m_{H_u}(Q_{GUT}) = m_{H_d}(Q_{GUT}) \rightarrow m_A(Q)$ determined $\rightarrow X_t$, tan β constraints



Constraints on $\tan \beta$ and $X_t \equiv A_t - \mu \tan \beta$: indigo: 1- σ ; orange: 2- σ ; green: 1- σ if adding

sbottom mass measurements.

Renormalization Group "bottom-up" evolution

•Once parameters determined at Q_{EWSB} scale, evolve them to GUT scale

RGE evidently invertible, but to evolve MSSM parameters from EWSB scale UP to GUT scale, while matching low-energy (gauge+yukawa) data is not staightforward.

+ Care to be taken: $Tr[Ym^2] \neq 0$ may increase error propagations

NB public bottom-up RGE option now installed in (new) SuSpect ver \geq 2.40

Bottom-up RG evolution with error propagations

 par.	input(GeV)	GUT output	$\Delta M_3 = \mp 1\%$	$\Delta m_{H_u} = \mp 1\%$	$\Delta m_{Q3_L} = \mp 1\%$
M_1	101.5	250.004	negl.	negl.	negl.
M_2	191.6	249.998			
M_3	586.6	249.999	± 2.2		
$m_{H_d}^2$	$(179.9)^2$	$(100.004)^2$	$(100.6)^2 -$	$(100.7)^2 -$	$(101.2)^2 -$
			$(99.4)^2$	$(99.2)^2$	$(98.7)^2$
$m_{H_u}^2$	$-(358.1)^2$	$(100.017)^2$	$(132.6)^2 -$	$(64.9)^2-$	$(63.7)^2 -$
			$(48.4)^2$	$(124.4)^2$	$(126.4)^2$
(μ)	356.9	353			
m_{e_R}	136	99.998	100–99.9	98.4–101.6	96.8–103.1
m_{Q1_L}	545.8	100.001	121–72	99.7–100.3	99.1–100.8
m_{Q3_L}	497	100.005	131–52	94.6–104.6	55.2–130.4
m_{u_R}	527.8	99.997	121–72	101–99	101.8–98.1
m_{t_R}	421.5	100.006	140–14	90.6–107.5	81.9–115.3
${m_b}_R$	522.4	99.997	122–72	99.4–100.6	98.5–101.5
$-A_t$	494.5	100.009	11189		" "
 $-A_b$	795.2	100.002	10694	11 11	" "

Combining all determination from bottom-up approach

Assumptions	Parameter	Constraint (GeV)	SPS1a
gen. MSSM	$M_1(Q_{EWSB})$	~95–115	101.5
	$M_2(Q_{EWSB})$	\sim 175–220	191.6
	$M_3(Q_{EWSB})$	\sim 580–595	586.6
	$(\frac{3}{8}m_{u_L}^2 + \frac{m_{e_R}^2}{4})^{1/2}(Q_{GUT})$	${\sim}68{-}89$	~ 79
" "	$m_{Q3_L}(Q_{EWSB})$	${\sim}488{-}518$	497
	$m_{b_R}(Q_{EWSB})$	\sim 510–540	522
" "	$\mu(Q_{EWSB})$	\sim 280–750	357
+ m_{N_4}	$\mu(Q_{EWSB})$	\sim 350–372	357
ilde q, ilde l-universality	$m_0^{q,l}(Q_{GUT})$	~90–112	100
M_i -universality	$M_i(Q_{GUT})$	\sim 245–255	250
$ ilde{b}_1, ilde{b}_2$ +universality	$ aneta(Q_{EWSB})$	~3–28	9.74
mSUGRA	m_0	~90-112	100
	$m_{1/2}$	\sim 245–255	250
	$-A_0$	\sim -100-350	100
	$ aneta(m_Z)$	\sim 5.5–28	10

Comparison with standard top-down χ^2 fits

Combined constraints on mSUGRA basic parameters from top-down fit with minuit of \tilde{g} decay + M_h measurements.

Assumptions	Parameter	Constraint (GeV)	SPS1a value
mSUGRA	m_0	99.96 ± 11.2	100
2-loop RGE + \tilde{q} R.C. + 2-l m_h		(99.95 ± 11.7)	
(1-loop RGE+ no \tilde{q} R.C. + m_h approx.)	$m_{1/2}$	250.0 ± 3.7	250
		(249.5 ± 4.7)	
	A_0	-104.2 ±379	-100
		(-100.6 ±136)	
	$\tan\beta(m_Z)$	9.9 $^{+9.4}_{-4.7}$	10
		(9.96 ±4.11)	

Conclusion

-Quite simple-minded approach but clear handle on possible obstacles in bottom-up approach May suggest new strategies, not automatically foreseen by global fit (e.g. combination observables in squark/slepton sector, etc)

-Compare reasonably well with more standard top-down fitting approaches

could be linked with other tools (SFITTER, ...) as "guidelines"

-likely to help solving part of the dicrete ambiguities (LHC inverse pb) (needs further dedicated studies)

May help also to distinghish from other BSM (specific SUSY

spectrum properties)