Scattering in General Gauge Mediation: Vector Meson Dominance and Holography

1207.4484

1210.4935

and I

1303.4534

Moritz McGarrie

AvH fellow Host: Andreas Weiler General Gauge Mediation in 5D

GGM and Deconstruction

Warped General Gauge Mediation

Hybrid Gauge Mediation

General Resonance Mediation

Holography for General Gauge Mediation





This topic overlaps

...with QCD

...with Pheno & BSM

...with String theory

so please ask questions



Motivation

hidden sectors are probably strongly coupled

but maybe we can develop tools to understand them?

General Gauge Mediation was developed for strong coupling

OPE's?

Dualities?

Other tools?

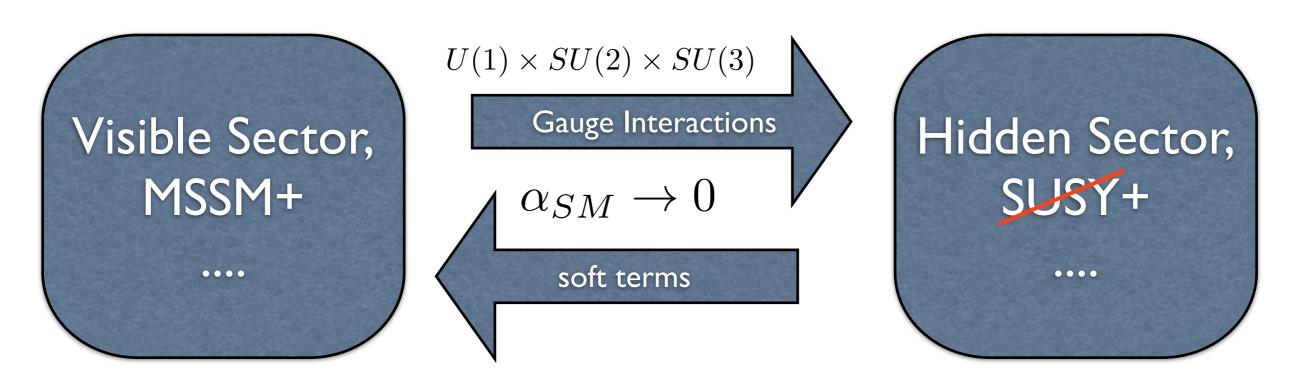
(for instance David Shih et al recently found large A-terms from OPE techniques: 1302.2642)

General Gauge Mediation

Meade, Seiberg, Shih 0801.3278

Also see the original: Gouvea, Moroi, Murayama 9701244

A model independent framework for gauge mediated supersymmetry breaking



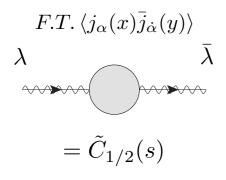
encodes spontaneous breaking in current correlators

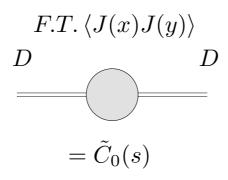
$$\mathcal{L}_{int} = g_{SM} \left(JD + J_{\mu} A^{\mu} - j_{\alpha} \lambda^{\alpha} - \bar{j}^{\dot{\alpha}} \bar{\lambda}_{\dot{\alpha}} \right)$$

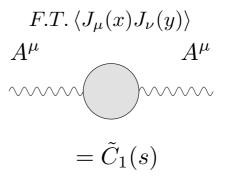
The key point of GGM: we want to understand and encode strongly coupled hidden sectors that break supersymmetry dynamically

The building blocks

current current correlators

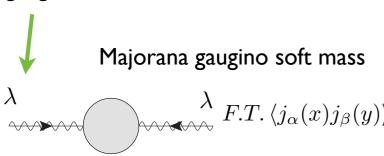


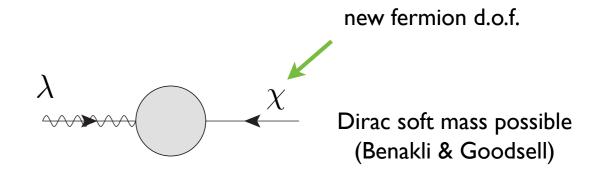


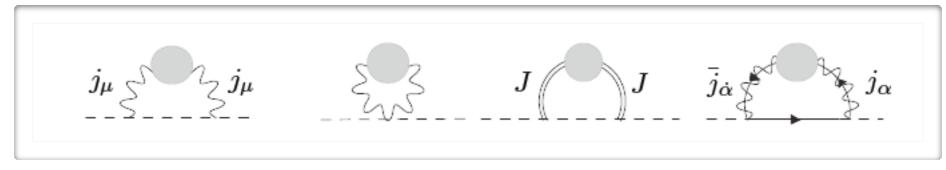


A "model" makes an assumption about the "blobs"









is an sfermion soft mass

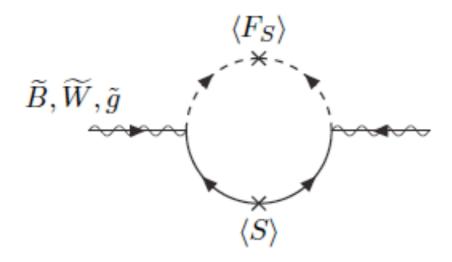
perturbative in ~lpha SM, all orders in the "electric" hidden sector couplings ~lpha hidden

If the model is a just a messenger model then the GGM programme achieves little... Just use the reviews Giudice & Rattazzi 9801271 (in most cases)

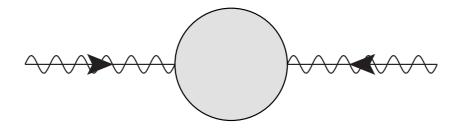
S.Martin 9608224

What is a blob?

In a perturbative model, (like a messenger model) a blob is just a simple one loop diagram

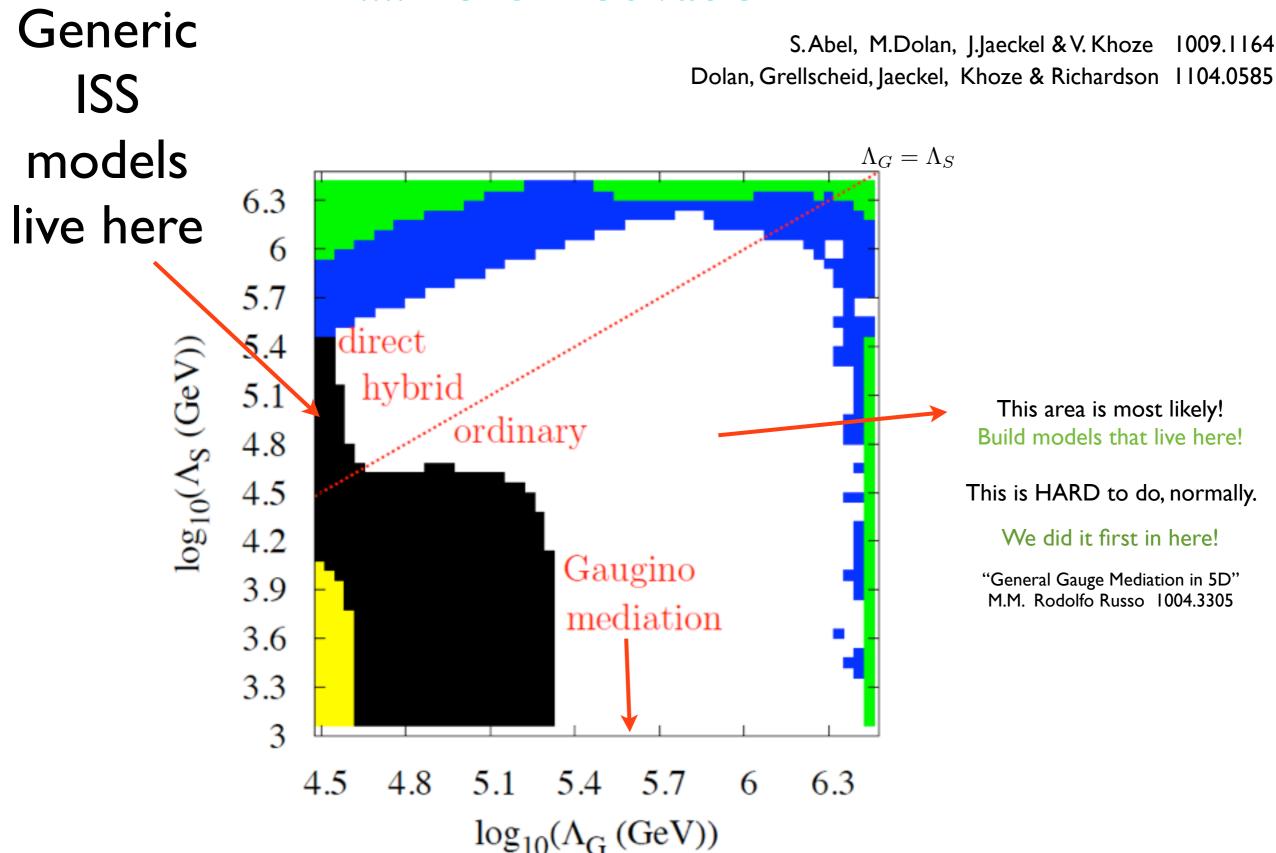


At strong coupling it is (unfortunately) very complicated



I'm sorry (its not my fault, I'm just the messenger)

....more motivation



Are there 4D examples that can replicate this feature?

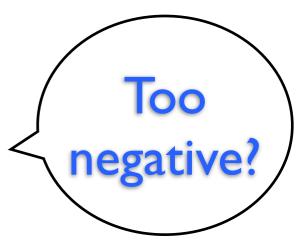
what kinds of strong coupling?

...if Seiberg duals don't work!?

Shih et al: 1302.2642

"...the notion of a loop factor might not even apply..."

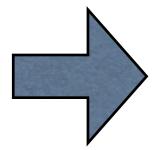
"...even in strongly coupled cases where field redefinitions are not necessarily applicable..."



Are there calculable models?

Holography?

Let's look at one attempt that uses scattering

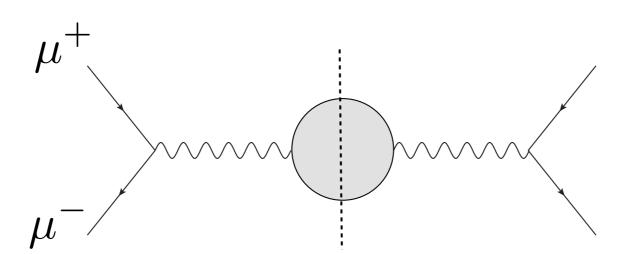


A 10-100 PeV collider?

cross sections of visible to hidden matter computed for perturbative messenger models.

Visible sector:

leptons sleptons quarks squarks



optical theorem

$$\sigma(\text{visible} \to \text{hidden}, s) = \frac{(4\pi\alpha)^2}{2s} \text{Disc } \Pi(s)$$

"In principle" determine GGM correlators from experimental cross sections

$$i(16\pi^2\alpha)^2 \left[\tilde{C}_a(s) - \tilde{C}_a(0) \right] = \sum_{cuts} \frac{s}{\pi} \int_{s_0'}^{\infty} ds' \frac{\sigma_a(s')}{s' - s}$$

 μ^+ Hidden sector: messenger fields + spurion $W=X\Phi ilde\Phi$ $=X\Phi^2\Phi$ $=X=M+ heta^2F$ $=X=M^2\pm F$

Examples

$$Disc \tilde{C}_0(s) = \frac{1}{4\pi s} \sqrt{s^2 - 4|X|^2 + 4|F|^2}$$

 $\psi, \tilde{\psi}$ with M

$$SUSY$$

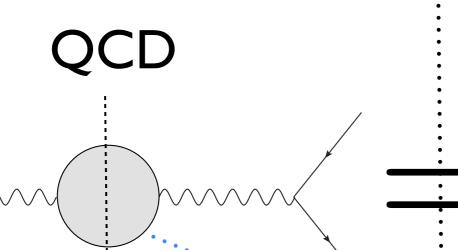
$$Disc\tilde{C}_0(s) = \frac{1}{4\pi s} \left(1 - \frac{4M^2}{s} \right)^{1/2}$$

soft masses and cross sections are related

But we want to get away from perturbative messenger models

Can we develop intuition with QCD?

Can QCD tell us something about the "blobs" and therefore something about the soft masses?



$$i\mathcal{M}(e^+, e^{-1} \to e^+, e^-)$$

gives
$$\sigma(e^+, e^- \to hadrons)$$

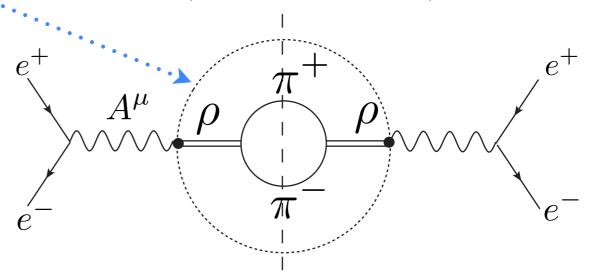
$$\mathcal{O}^{\mu} = \bar{q}\gamma^{\mu}q$$

perturbative in $~lpha_{em}$

all orders in $\, lpha_{s} \,$

Hadronic picture "look under the hood" Sum of many parts

one such piece: $\sigma(e^+e^- o \pi^+,\pi^-)$



perturbative in $~\alpha_{em}$ perturbative in $~\alpha_{mag}$

Can QCD tell us something about the "blobs" and therefore something about the soft masses?

Pion physics and vector meson dominance

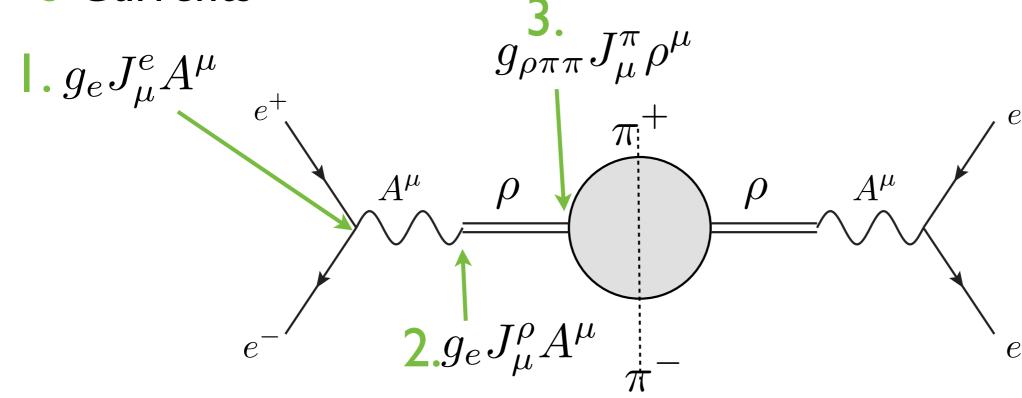
3 Currents

$$\sigma(e^+, e^- \to \pi^+, \pi^-) = \frac{(4\pi\alpha)^2}{4\pi 12s} \left(1 - \frac{4m_\pi^2}{s}\right)^{3/2} |F(s)|^2 \theta(s - 4m_\pi^2)$$

Nambu 1957
Sakurai 1960
Murray Gell-Mann 1961
Kroll, Lee & Zumino 1967
+ many many more

A hidden local symmetry

Completely 4D



We learn that

- a) Pions couple to rho
- b) There is a form factor

"modified current operator"

$$\langle A|g_e J^{em}|B\rangle = \frac{-g_e}{g_\rho} \frac{m_\rho^2}{q^2 - m_\rho^2} \langle A|g_{\rho\pi\pi} J^\pi|B\rangle$$

A form factor

$$F(s) = \frac{-g_e}{g_\rho} \frac{m_\rho^2}{s - m_\rho^2}$$

The famous "current field identity"

$$J^{\rho}_{\mu} = -\frac{m^2_{\rho}}{g_{\rho}}\rho_{\mu}$$

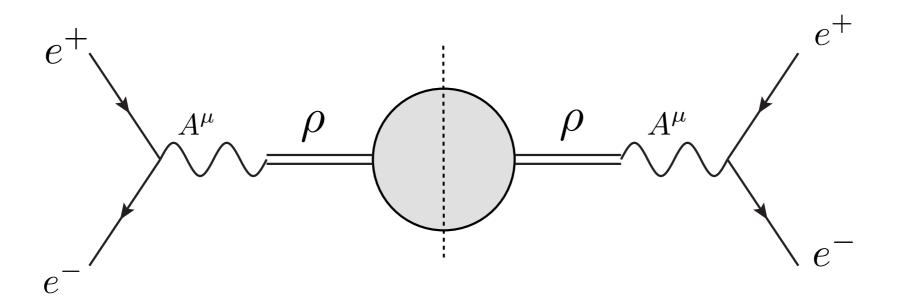
an operator field correspondence

Can we build this into GGM? YES

"General Resonance Mediation": McGarrie 1207.4484

$$\sigma(e^+e^- \to \rho \to \phi^+\phi^-)$$

Intermediate resonances in cross sections of visible to hidden sector



$$F(s) = \frac{-g_e}{g_\rho} \frac{m_\rho^2}{s - m_\rho^2}$$

$$\mathcal{J}_{\rho} = -\frac{m_{\rho}^2}{g_{\rho}} \rho$$
 where $D^2 \rho = 0$

"supercurrent field identity" MM 1207.4484

In general

$$\sigma_a(visible \to hidden, s) = \frac{(4\pi\alpha)^2}{2s} |F(s)|^2 \text{ Disc } \tilde{C}_a(s)$$

We may now compute all cross sections for a visible sector to a perturbative messenger model with intermediate resonances

Summary

The key idea is to build models around scattering

RED

$$\sigma_a(visible \to hidden) = \frac{(4\pi\alpha)^2}{2s} \ Disc \ \tilde{C}_a(s)$$

$$F(s) = \frac{m_{\rho}^2}{s + m_{\rho}^2}$$

form factor or no form factor?

BLACK?
$$\sigma_a(visible \rightarrow hidden) = \frac{(4\pi\alpha)^2}{2s} |F(s)|^2 \ Disc \ \tilde{C}_a(s)$$

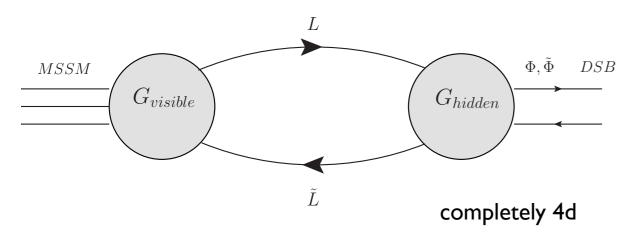
Similar to the hadronic world: perhaps we should take it more seriously?

Ideally, determine this form factor from experiment or from computer simulations or from toy models and effective field theory

impossible hard possible

What does this tell us about SUSY breaking? "GGM and I

Simplest case corresponds to a 2 site quiver model



Form factor

$$F(s) = \frac{m_{\rho}^2}{s + m_{\rho}^2}$$

"GGM and Deconstruction"
McGarrie 1009.0012 and 1101.5158

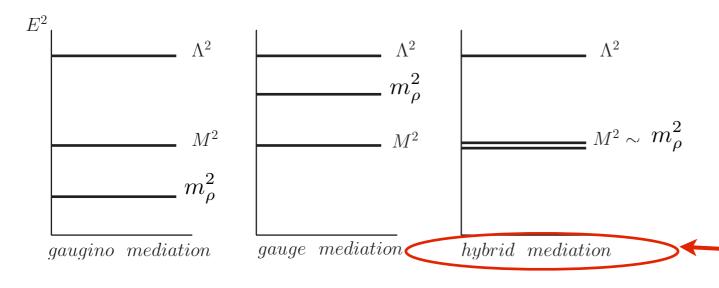
Extensions in Auzzi & Giveon 1009.1714 1011.1664

easyDiracgauginos + ...
Abel & Goodsell | 1102.0014

M.M. Bharucha, Goudelis To appear

A hidden local symmetry, exhibits vector meson dominance

3 Regimes depends on ratio
$$y=rac{m_{
ho}}{M}$$



We have a new hybrid regime where

$$@M_{SUSY}: m_{\lambda}^2 > m_{\tilde{f}}^2$$

soft masses are analytically calculable to 2 loops! and cross sections are now known.

'most likely?

The quiver models may be related to Seiberg duality through tools of "Hidden Local Symmetry" (Abel & Barnard 1202.2863)

Such setups may be generalised to long linear quivers these deconstruct an extra dimension.

It is natural to extend these to holographic setups

All these developments have taken place in the QCD literature:

Vector Meson Dominance

Nambu 1957, Sakurai 1960, Murray Gell-Mann 1961, Kroll, Lee & Zumino 1967 + many many more

"Nonlinear Realization and Hidden Local Symmetries", Bando et al 1980's

"QCD and Dimensional Deconstruction" 0304182

"QCD and a Holographic Model of Hadrons" 0501128 & 0510268

"Holography for General Gauge Mediation"

M.M.: 1210.4935

also AdS/SUSY

"General Gauge Mediation in 5D" M.M. Rodolfo Russo 1004.3305

"Warped General Gauge Mediation" M.M. Daniel C.Thompson 1009.4696

N=1 5d super Yang-Mills

action in the bulk

Abel & Gherghetta 1010.5655

Check list

- I. Metric: slice of AdS
- 2. Interval

IR hardwall/

slice of AdS

- 3. Flavour symmetries
- 4. Scale matching
- 5. Sources
- 6. Operators
- 7. Bulk field
- 8. Bulk to boundary propagator

$$ds^{2} = \left(\frac{R}{z}\right)^{2} \left(\eta^{\mu\nu} dx_{\mu} dx_{\nu} + dz^{2}\right)$$

$$L_0 < z < L_1$$

$$SU(N_f)_L \times SU(N_f)_R \to SU(N_f)_V$$

$$\frac{R}{g_{5d(YM)}^2} = \frac{N_c}{12\pi^2}$$

$$A^0_\mu(x), \lambda^0_\alpha(x), D^0(x)$$

$$\mathcal{O}_{\mu}(x), \mathcal{O}_{\alpha}(x), \mathcal{O}(x)$$

$$A^\mu(q,z) = A^\mu_0(q) K(q,z)$$

$$K(q,z) = \frac{V(q,z)}{V(q,L_0)}$$

$$V(q,z) = zq [Y_0(qL_1)J_1(qz) - J_0(qL_1)Y_1(qz)]$$

compute...

"Holography for General Gauge Mediation"

IR hardwall/ slice of AdS

N=1 5d super Yang-Mills action in the bulk

$$SU(N_f)_L \times SU(N_f)_R$$

$$ds^{2} = \left(\frac{R}{z}\right)^{2} (\eta^{\mu\nu} dx_{\mu} dx_{\nu} + dz^{2}) \qquad L_{0} < z < L_{1}$$

$$L_0 < z < L_1$$

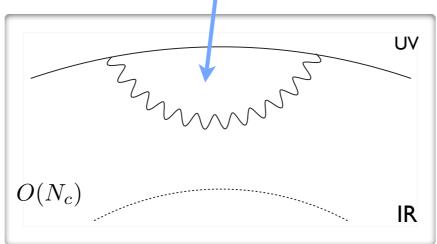
$$\frac{R}{g_{5d(YM)}^2} = \frac{N_c}{12\pi^2}$$

$$A^{\mu}(q,z) = A_0^{\mu}(q) \frac{V(q,z)}{V(q,L_0)}$$

$$\int d^4x e^{ip.x} \langle \mathcal{O}_{\mu}(x)\mathcal{O}_{\nu}(0)\rangle = \Pi(p^2)P^{\mu\nu}$$

$$\Pi(q^2) = \frac{1}{q} \left(\frac{R}{z} \frac{\partial_z V(q, z)}{V(q, L_0)} \right)_{z=L_0}$$

gives a log running piece



An AdS/SQCD proposal

M.M.: 1210.4935

4D: operator		Field	Δ	m^2
$\mathcal{O}(x)$	\rightarrow	D(z,x)	2	-4
$\mathcal{O}_{\alpha}(x)$	\rightarrow	$\lambda_{\alpha}(z,x)$	5/2	1/2
$\mathcal{O}_{\mu}(x)$	\rightarrow	$A_{\mu}(z,x)$	3	0

The UV operators that correspond to bulk

$$\mathcal{O}_{L,R} = \phi^{\dagger} \phi_{L,R}$$

$$\mathcal{O}_{L,R}^{\alpha} = -i\sqrt{2}\phi^{\dagger} q_{L,R}^{\alpha}$$

$$\mathcal{O}_{L,R}^{\mu} = \bar{q}\sigma^{\mu}q_{L,R} - i\left(\phi^{\dagger}\partial^{\mu}\phi - \partial^{\mu}\phi^{\dagger}\phi\right)_{L,R}$$

UV boundary correlators give a supersymmetric effective action

$$\left[3\Pi_1(q^2) - 4\Pi_{1/2}(q^2) + \Pi_0(q^2)\right] \equiv 0$$

$$\langle \mathcal{O}_{\alpha}(x)\mathcal{O}_{\beta}(0)\rangle \equiv 0$$

Related to the Gibbons-Hawking boundary terms of SYM

So far.....

We end up with a supersymmetric boundary effective action

$$\int \frac{d^4q}{(2\pi)^4} \left[\frac{1}{4} \Pi_1(q^2) F_{\mu\nu,0} F_0^{\mu\nu} - i \Pi_{1/2}(q^2) \lambda_0 \sigma_\mu \partial^\mu \bar{\lambda}_0 + \frac{1}{2} \Pi_0(q^2) D_0^2 \right]$$

for a weakly gauged flavour symmetry of the (non) CFT

$$\int d^4x e^{ip.x} \langle \mathcal{O}_{\mu}(x)\mathcal{O}_{\nu}(0)\rangle = \Pi(p^2)P^{\mu\nu}$$

Typically a complicated expression involving Bessel functions:

$$\Pi(q^2) = \frac{a(L_0)}{g_5^2 q} \left[\frac{J_{\alpha-1}(qL_0)Y_{\beta}(qL_1) - J_{\beta}(qL_1)Y_{\alpha-1}(qL_0)}{J_{\alpha}(qL_0)Y_{\beta}(qL_1) - J_{\beta}(qL_1)Y_{\alpha}(qL_0)} \right]$$

 $\alpha=1,\beta=0$ $\;$ Determined from conformal dimensions of operators

Next....

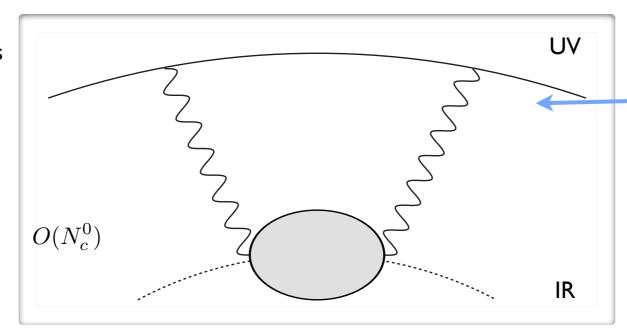
Introduce IR localised correlators that encode supersymmetry breaking

SUSY breaking currents located on an IR brane or live in the bulk

$$A_{\mu}J^{\mu} = \int dz K(p,z) A^{0}_{\mu}J^{\mu} = A^{0}_{\mu}J^{\mu}\Lambda(p)$$

An effective vertex function generated by a bulk to boundary propagator

Ignore $O(1/N_c)$ corrections



$$A^0_\mu \Lambda(p) \tilde{C}(p^2/M^2) P^{\mu\nu} \Lambda(p) \ A^0_\nu$$

$$\delta L_{eff}^{SUSY}|_{UV} = \frac{g_{SM}^2}{2} \tilde{C}_0(0) D_0^2 - i g_{SM}^2 \tilde{C}_{1/2}(0) \lambda_0 \sigma_\mu \partial^\mu \bar{\lambda}_0 - \frac{g_{SM}^2}{4} \tilde{C}_1(0) F_{\mu\nu,0} F_0^{\mu\nu}$$

may be written as a boundary effective action too

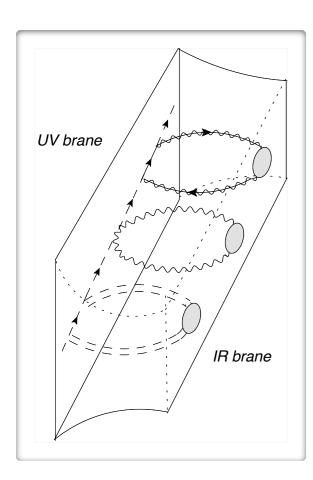
<u>If*</u> you also assume a messenger sector then

* this part is not necessary. It is a further additional assumption

$$m_{\lambda} = \left(\frac{\alpha_{IR}}{4\pi}\right) \left(\frac{R}{z}\right) \left[\frac{2Fg(x)}{M}\right]$$

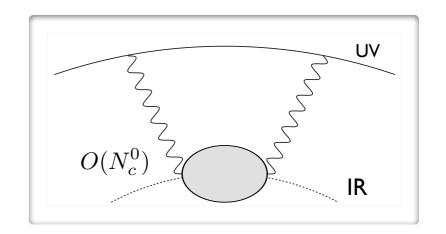
soft masses are calculable!

$$m_{\phi}^{2} = \left(\frac{\alpha_{IR}}{4\pi}\right)^{2} \left(\frac{R}{z}\right)^{2} \left[\frac{F}{M}\right]^{2} \left|\frac{1}{\hat{M}}\right|^{2} \int dp \ p \ \Lambda^{2}(p)$$

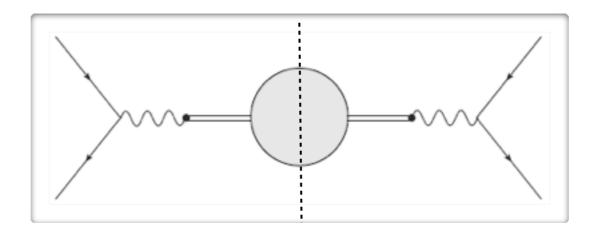


Holographic Scattering

$$g_n = g_5 g_{IR} \int dz \psi_n(z) \varphi(z) \tilde{\varphi}(z) \delta(z - L_1)$$



The form factor encodes a sum of monopole contributions of an infinite tower of vector mesons with decay constants for each meson



Final states can be taken to be messenger fields

$$F_n \epsilon_{\mu} = \langle 0 | \mathcal{O}_{\mu} | \rho_n \rangle$$

meson decay constant

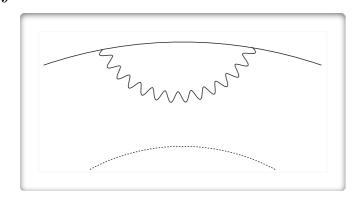
$$\sigma_a(vis \to hid) = \frac{(4\pi\alpha_{SM})^2}{2s} (g_{IR}^2 g_5^2) \sum_{n=1}^{\infty} \frac{F_n \psi_n(z)}{s + m_n^2} \sum_{\hat{n}=1}^{\infty} \frac{F_{\hat{n}} \psi_{\hat{n}}(z)}{s + m_{\hat{n}}^2} \text{Disc } \tilde{C}_a(s/\hat{M})$$

Duality in $e^+, e^- \to \text{hidden}$?

Generating functional

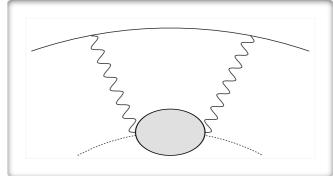
$$Z[A^{0}, \lambda^{0}, D^{0}] = \int_{V(L_{0})=V^{0}} DV e^{-S_{bulk}(V) + \int d^{4}x d^{4}\theta V^{0}} \left[\mathcal{J}_{SM}(x) + \mathcal{O}(x) + \mathcal{J}_{SUSY}(x) \right]$$

$$\int d^4x e^{ip.x} \langle \mathcal{O}_{\mu}(x)\mathcal{O}_{\nu}(0)\rangle = \Pi(p^2)P^{\mu\nu}$$



supersymmetric piece

$$\int d^4x e^{ip.x} \langle \mathcal{J}_{\mu}(x)\mathcal{J}_{\nu}(0)\rangle = \tilde{C}_1(p^2)P^{\mu\nu}$$



leading breaking piece

a sum of many different correlators make the total vacuum polarisation amplitude all these correlators have a natural OPE expansion

finds application in AdS/condensed matter: Optical theorem gives conductivity

Engineering Holographic Graphene

Strange Metal Transport Realized by Gauge/Gravity Duality

Grignani, Namshik Kim, Gordon W. Semenoff

hep-th:1208.0867

Thomas Faulkner, Nabil Iqbal, Hong Liu, John McGreevy, David Vegh DOI: 10.1126/science.1189134

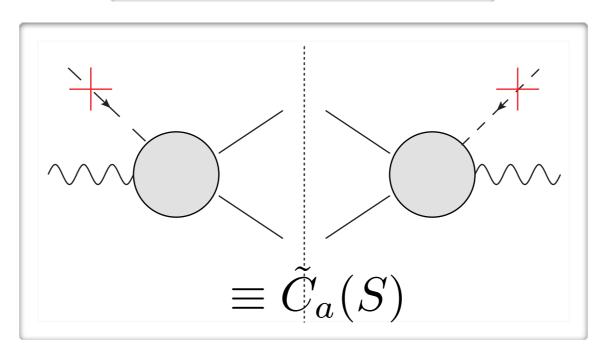
D.Vecchia and Drago (1969) Chua, Hama & Kiang (1970) Frampton (1970) Many others...

Speculative

A Veneziano-like amplitude for GGM?

$$F(s) \sim \frac{\Gamma[1 - \alpha(s)]\Gamma[\lambda - \frac{1}{2}]}{\Gamma[\lambda - \alpha(s)]\Gamma[1/2]}$$





A fit to the pion data

$$\lim_{s \to \infty} F(s) \simeq 1/s^{\lambda - 1}$$

$$\alpha(s) = 1/2 + s/2m_{\rho}^2$$

Infinitely rising linear Regge trajectories

$$A(1 \rightarrow 2)$$

Forward scattering amplitude

Higher spin states contribute too!

The point is that holographic models are toy models with a separation of scales between the spin 0,1/2,1,3/2,2 and the higher spin states.

Moritz McGarrie

Thanks for listening

What next?

maybe this way of thinking may lead to a better understanding of the hidden sector?

Pheno

Go back to the quiver models and do proper studies

currently implementing these models (including Dirac gauginos) into SARAH with Aoife Bharucha & Andreas Goudelis

How can we test these models further?

Theory

Maximal super Yang-Mills in 5d bulk?

MM 1303.4534

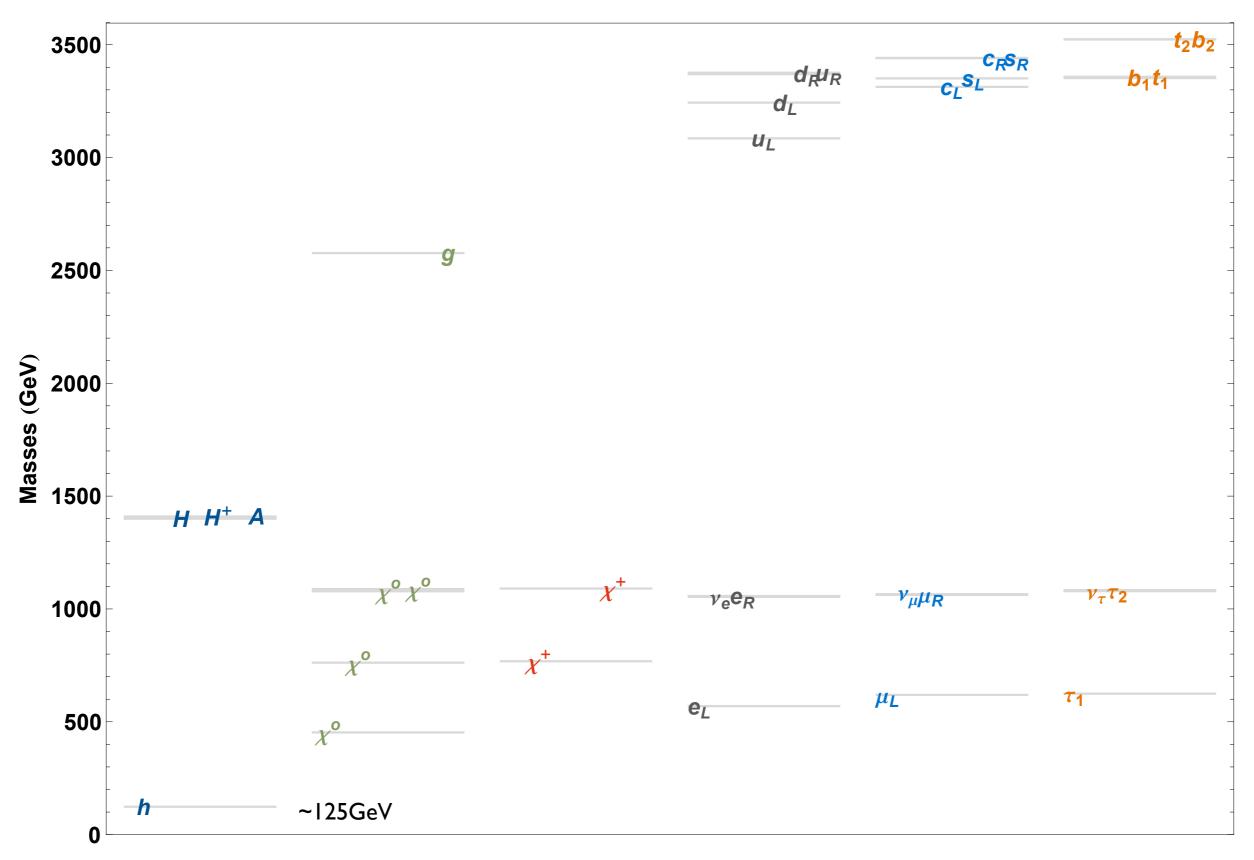
Relate the form factors to OPE's

Large A terms?

Building quivers from Seiberg duality with S.Abel

There are plenty of ways this instructive toy model may be extended!

Electroweak quiver



Electroweak quiver: preliminary spectrum

Input

```
Block MINPAR # Input parameters
        3.50000000E+05 # LambdaInput
        5.20000000E+06 # MessengerScale
        2.50000000E+01 # TanBeta
        1.00000000E+00 # SignumMu
        1.00000000E+00
                       # n5plets
        1.00000000E+00
                       # cGrav
        0.00000000E+00
                       # n10plets
        2.00000000E-01 # The1
        2.20000000E-01 # The2
  10
        1.00000000E+05
                       # TScale
  11
        4.00000000E+05 # vlvInput
  12
        0.00000000E+00 # MkdInput
        0.00000000E+00 # MadInput
Block EXTPAR # Input parameters
 106
        8.00000000E-02 # YKInput
 107
        8.0000000E-02 # YAInput
```

Output

```
Block MASS # Mass spectrum
   PDG code
                 mass
                               particle
   1000001
               3.24350791E+03
                              # Sd 1
  1000003
              3.35085914E+03
                              # Sd 2
  1000005
              3.35231549E+03
                             # Sd 3
  2000001
              3.36987298E+03
                             # Sd_4
  2000003
              3.44147312E+03
  2000005
              3.52400410E+03 # Sd 6
  1000002
              3.08515677E+03 # Su_1
              3.31328261E+03 # Su 2
  1000004
  1000006
              3.35789970E+03
                              # Su_3
  2000002
              3.37588018E+03
                              # Su_4
  2000004
              3.44074102E+03 # Su_5
  2000006
               3.52329303E+03
                              # Su_6
  1000011
              5.69311604E+02 # Se_1
  1000013
               6.19171566E+02 # Se_2
  1000015
              6.24530619E+02
                              # Se_3
  2000011
              1.05715827E+03 # Se_4
  2000013
              1.06542560E+03 # Se_5
  2000015
              1.08320684E+03
                             # Se_6
  1000012
              1.05353012E+03 # Sv_1
  1000014
              1.06214101E+03 # Sv_2
   1000016
              1.07891082E+03 # Sv_3
        25
              1.23508263E+02 # hh_1
        35
              1.39983318E+03 # hh 2
        36
              1.40962078E+03 # Ah_2
        37
              1.40578829E+03
                              # Hpm_2
              9.11876000E+01 # VZ
        24
              8.03138130E+01 # VWm
              5.00000000E-03 # Fd_1
              1.05000000E-01 # Fd 2
              4.20000000E+00 # Fd_3
              3.00000000E-03 # Fu_1
              1.27000000E+00 # Fu_2
              1.72900000E+02 # Fu_3
        11
              5.10998910E-04 # Fe_1
        13
              1.05658000E-01 # Fe_2
        15
              1.77700000E+00 # Fe_3
  1000021
              2.57688158E+03 # Glu
  1000022
              4.52864879E+02 # Chi 1
  1000023
              7.61963085E+02 # Chi_2
  1000025
              1.07840119E+03 # Chi_3
  1000035
              1.08809948E+03 # Chi 4
  1000024
              7.68185532E+02 # Cha_1
  1000037
              1.09034034E+03 # Cha 2
```

GMSB

Gaugino mediation

"GGM5D"

M.M. & R.Russo 1004.3305

$$m_{\lambda} = \left(\frac{\alpha}{4\pi}\right) \frac{F}{M}$$

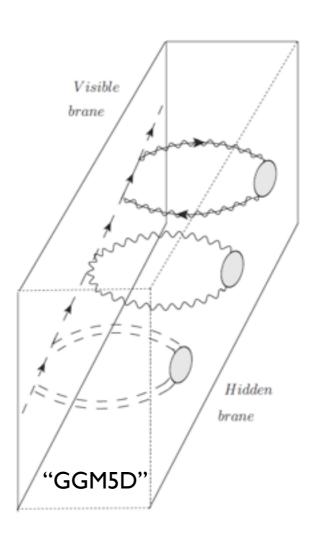
$$m_{\phi}^2 = \left(\frac{\alpha}{4\pi}\right)^2 |\frac{F}{M}|^2$$

$$m_{\phi}^2 = m_{\lambda}^2$$

$$m_{\lambda} = \left(\frac{\alpha}{4\pi}\right) \frac{F}{M}$$

$$m_\phi^2 \simeq 0$$

(+3 loop through RGE's)



$$m_{\lambda} = \left(\frac{\alpha}{4\pi}\right) \frac{F}{M}$$

$$m_{\phi}^2 \simeq \left(\frac{\alpha}{4\pi}\right)^2 \left|\frac{F}{M}\right|^2 \times \left|\frac{m_{KK}}{M}\right|^{\rho}$$

 ρ ranges between [0,2]

We have a new intermediate regime where

$$@M_{SUSY}: m_{\lambda}^2 > m_{\tilde{f}}^2$$

....more motivation: everyone's doing it now!

Abstracts:

Shih et al: 1302.2642

"...Using our formalism, we identify new avenues to solving these problems through **strong dynamics** in the messenger sector or hidden sector"

Fortin, Intriligator, Stergiou: 1109.4940

"...to constrain and analyze hidden sector theories that couple to our gauge forces and are **not necessarily weakly coupled**"

Field-theoretic Methods in Strongly-Coupled Models of General Gauge Mediation

Fortin, Stergiou: 1212.2202

"...We manage to obtain reasonable approximations to soft masses, even when the hidden sector is **strongly coupled.**"

Abel, Gherghetta: 1010.5655

"...we use our framework to study **strongly-coupled** scenarios of supersymmetry breaking mediated by gauge forces"

as well as

McGuirck,
Skenderis & Taylor
Argurio, Bertolini, Pietro, Porri Redigolo
Benini, Dymarsky, Franco, Kachru, Simic
McGuirck, Shiu, Sumitomi
Buican, Seiberg, Meade
Komargodski, Katz, Green