

The Politically Incorrect Report on Planck 1st Data Release, March 2013

- * cost 5 cent/European/year
- * Data release: 2 scans out of 5 high freq. and 8 low freq. scans.

Only TT spectra. No polarization (use WMAP ~~del.~~)
[Show map & TT spectra]

Rest of the talk:

- ① Preliminaries
- ② Minimal 6 parameters model
- ③ ~~Re~~ Planck Results
- ④ Interesting Anomalies
- ⑤ Inflation.
- ⑥ Place your bets.

Based on:

- ① Planck 2013 results XVI, XXII: 1303.5076
1303.5082
- ② Presentations by Julien Lesgourgues & Jo Dunkley
- ③ Personal bias. Heidelberg KITP

PLANCK DATA

Preliminaries:

- ① Cosmological Measurements require a model to compare data to theory
- ② Even within a model, there are several choices for parameters and parameterization.
- ③ Once deciding what is the parameterization to be used, one ^{usually} still needs to set some a-priori limits on the parameter values for a successful determination.

Also apply several statistical notions:

Priors, marginalization, estimators etc.

Bayesian Analysis vs. Frequentist approach.

- ④ Combining several probes is rather crucial.

^{re} prior - If we allow params. to vary arbitrarily, we cannot ~~get~~ ^{derive} conclusions.

⇒ Limit the allowed range & a-priori like

$$0.9 < n_s < 1.1$$

danger: The prior might affect the result.

We have to make sure it's big enough and reasonable (log prior vs. flat)

Marginalization: The data give a multi-dim. volume. How do we deduce the actual values?

We marginalize over params. i.e. integrate over the probability distribution of $n-1$ ^(or $n-2$) params. to get the 1-d (2-d) distribution of the desired ~~other~~ params.

After the analysis one gets $ML \equiv$ most likelihood value. Usually this is a marginalized result, but sometimes, params. are fixed by brute force.
 $\Rightarrow$ Greatly affects the outcome.

Additional params.:

Obviously I can add params. and they will give me a better fit to the data.

Are they true?

$\Rightarrow$ One pays a "penalty" for adding the parameters. To "accept" an additional one the improvement has to be significant enough $\Delta\chi$ test.

Discovery / Ruling out: Let's agree on 3σ , 99.5%.

The "actual" measurement - Figure 1

One example of a T_{CMB} CMB map.

Minimal 6 parameters cosmological model

Theoretical Background

General Relativity, simple QED

FLRW metric

energy components: photons, electrons, baryons, neutrinos, cold DM, Λ

Table 1

$\Omega_{m0}, \Omega_b, \Omega_c, n_s, A_s, \tau$

Derived params. $H_0, \Omega_{\Lambda} \equiv 1 - \Omega_m, \Omega_{\nu}$

Additional Extensions: $\frac{dn_s}{d \ln k}, \frac{d^2 n_s}{d \ln^2 k}, r, \Omega_k, \Sigma m_\nu, Y_p, N_{\text{eff}}, m_{\text{sterile}}, w_0, w_a, \dots$

Simplified Friedmann eq:

$$\frac{H(z)^2}{H_0^2} = \Omega_{m0}(1+z)^3 + \Omega_{R0}(1+z)^4 + \Omega_{K0}(1+z)^2 + \Omega_{\Lambda}$$

Primordial Power spectrum:

$$P_R(k) = A_s \left(\frac{k}{k_0}\right)^{n_s-1 + \frac{1}{2} \frac{dn_s}{d \ln k} \ln \frac{k}{k_0} + \frac{1}{6} \frac{d^2 n_s}{d \ln^2 k} \left(\ln \frac{k}{k_0}\right)^2 + \dots}$$

$$P_T = A_t \left(\frac{k}{k_0}\right)^{n_t-1 + \frac{1}{2} \frac{dn_t}{d \ln k} \ln \frac{k}{k_0} + \dots}$$

$$r \equiv \frac{P_T(k_0)}{P_R(k_0)} \approx 16\epsilon \quad ; \text{ where } \epsilon = \frac{m_p^2}{2} \left(\frac{v'}{v}\right)^2$$

$$H_0 = h \times 100 \frac{\text{km}}{\text{sec-Mpc}}$$

Results

The basic 6 param. model is rather insensitive to foreground modeling & supplementary data sets.

$$\theta_s \approx (1.04148 \pm 0.00066) \times 10^{-2}$$

$$\theta_s = \frac{r_s(z_*)}{D_A(z_*)} = \frac{\text{sound horizon @ last scattering}}{\text{angular diameter distance}}$$

$\Rightarrow$ We actually constrain $\Omega_m h^{3.2} (\Omega_b h^2)^{-0.54} = 0.695 \pm 0.002$

Figure 2: Value of params. & likelihood.

Figure 3: $\Omega_m - H_0 - n_s$

* Deviations from the basic 6 param. model

Several Anomalies:

① Absence of ℓ power at $20 \leq \ell \leq 40$
enough $\sim 2-3\sigma$

② Direct H_0 measurement tension.

From Planck + WP + highL $H_0 = 67.3 \pm 1.2 \frac{\text{km}}{\text{sec Mpc}}$

From local measurements (Cepheids + SNe or Carnegie)

$$H_0 = 74.3 \pm 1.5 \pm 2.1 \frac{\text{km}}{\text{sec Mpc}}$$

$$\text{or } H_0 = 73.8 \pm 2.4 \frac{\text{km}}{\text{sec Mpc}}$$

③ Tension in the value of Ω_m from SNe vs. Planck.

SNLS ~~predict~~ $\Omega_m = 0.227$

Planck $\Omega_m \approx 0.315 \pm \begin{matrix} 0.016 \\ 0.018 \end{matrix}$
+ W/P

Inflation (Started it all)

Most important: No non-gaussianity has been detected!

$$f_{NL}^{\text{local}} = 2.7 \pm 5.8$$

$$\text{Equilateral} = -42 \pm 75$$

$$\text{Orthogonal} = -25 \pm 39$$

$$p_{\text{slow-roll}} \lesssim 1$$

Simplest model: $n_s = \text{const}$, ~~no~~ running, no tensors
Strictly speaking, this cannot be. However, if $r \ll 10^{-2}$
and $\frac{dn_s}{d\ln k} \ll 10^{-2}$ then we can just consider A_s, n_s
which is the basis of the minimal model.

Now considering the simple models $\frac{dn_s}{d\ln k} \sim (n_s - 1)^2$
so it is below Planck sensitivity while $r > 10^{-2}$
is not

⇒ The famous $n_s - r$ plot

⇒ Inflation is still consistent with simple single field models, but not with "vanilla" models such as $V \propto \phi^n$. Also all $V \propto \phi^n$ are getting ruled out gradually.

Running Spectral index $\frac{dn_s}{d \ln k}$

In the usual slow-roll hierarchy

$$n_s = 1 + 2\eta - 6\epsilon \quad \text{where} \quad \eta = \frac{m_p^2}{2V} \frac{V''}{V}$$

$$\epsilon = \frac{m_p^2}{2} \left(\frac{V'}{V} \right)^2$$

where ' denotes differentiation w.r.t. the inflation.

There are generalizations to multifield models, non-canonical kinetic terms, SUGRA, $c_s^2 \neq 1$ etc.

The true quantity is $P(k)$.

Using $P(k) = A \left(\frac{k}{k_*} \right)^{n_s-1}$ is only a parameterization

In practice, even in slow-roll, $P(k)$ has some additional k dependence. So we go to the next order ~~in~~ $\frac{dn_s}{d \ln k}$ which in the slow-roll approx corresponds to:

$$\frac{dn_s}{d \ln k} = -16\epsilon\eta + 24\epsilon^2 + 2\zeta^2$$

$$\text{where } \zeta^2 \equiv \frac{m_p^4 V' V'''}{V^2} \quad (\zeta^2 \text{ is not ~~not~~ positive definite})$$

$$\text{similarly } \frac{d^2 n_s}{d \ln k^2} = -192\epsilon^3 + 192\epsilon^2\eta - 32\epsilon\eta^2 - 24\epsilon\zeta^2 + 2\eta\zeta^2 + 2\omega^3$$

$$\omega^3 \equiv \frac{m_p^6 V'^2 V''''}{V^3}$$

Throughout the years WMAP 1 - PLANCK

The data always favoured some non-zero negative running.

Is this statistically significant?

Until now, at most 2σ and with not enough $\Delta\chi$.

Planck considers "Running of running", $\frac{d^2 n_s}{d \ln k^2}$ for the first time - consistent with 0.

Important comments:

a. For the first time Planck really manages to take $n_s=1$ out, even if one adds running, tensors, and general reionization.

Possible caveats: $N_{\text{eff}}=4$ or $Y_{\text{He}} \approx 0.3$ bring it back.

b. Considering running, significantly affects the constraint on r .

If we will also allow "running of running" the bound on r will be even weaker.

c. No strong enough evidence for $n_s \neq \text{const}$

d. If running is $\mathcal{O}(10^{-2}) \sim n_s - 1$, then the usual slow-roll expression $n_s - 1 = 2\eta - 6\epsilon$ needs to be modified. Similarly if $\frac{d^2 n_s}{d \ln k^2}$ is big enough.

See for example Lyth & Riotto from 1999.

Easther & Peiris 2006.

A better analysis will be to simply give the binned spectrum, and compare models directly.

~~If future experiments can measure A/B to the level of $\sim 10^{-3}$, it will be a much more~~

- e. Is there a future for NG? probably yes.
It depends on the sensitivity of future experiments and our theoretical ability to disentangle primordial NG from late-time effects.
- f. The bound on $r < 0.13$ is ~~simply~~ ^{practically} the WMAP bound which is the optimal one without polarization data. Expect an improvement of ~~about~~ ~~the~~ a factor of ~ 2 if PLANCK lives up to its promises and manages to measure the polarization according to specifications.

Place your bets:

Even in the final data release, I bet that

- ① No NG
- ② No r
- ③ Running, still not significant enough.
- ④ Still have an endless stream of papers concerning the above three bets.

Conclusions: ① RTFM !!!

- ② Planck has finally removed many degeneracies in cosmological parameters. The basic model is still a good fit, but there are interesting anomalies and important, well-motivated theoretical extensions which are worth pursuing.

