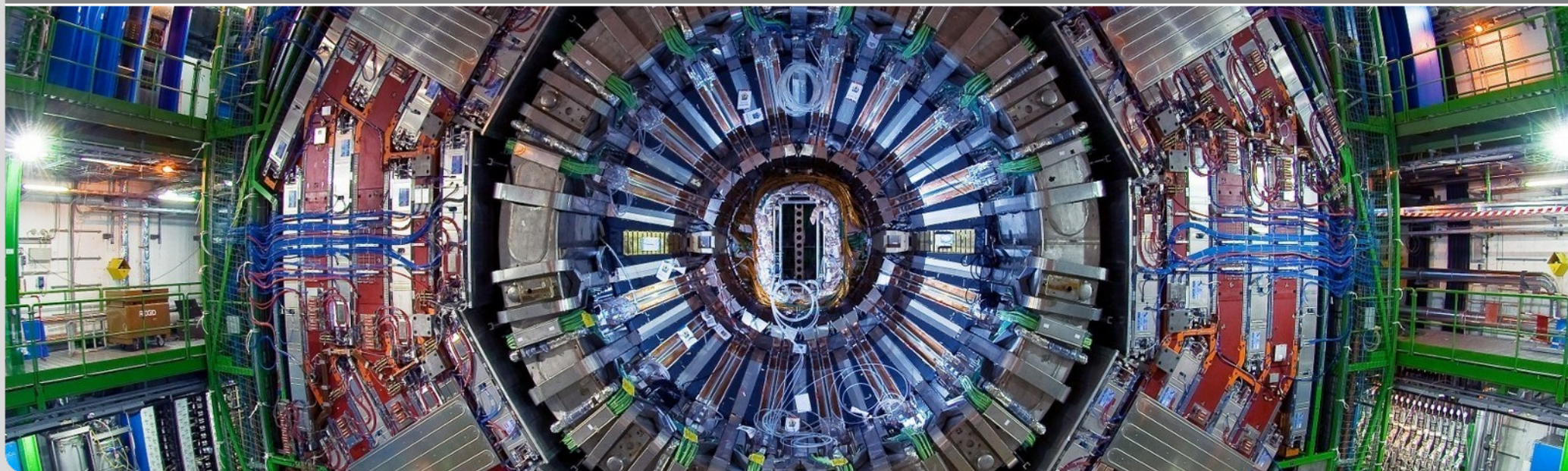


QCD analysis of 7 TeV Inclusive Jet Data

S. Dooling, H. Jung, K. Rabbertz, G.Sieber, P. Kokkas, G. Flouris
on behalf of CMS collaboration

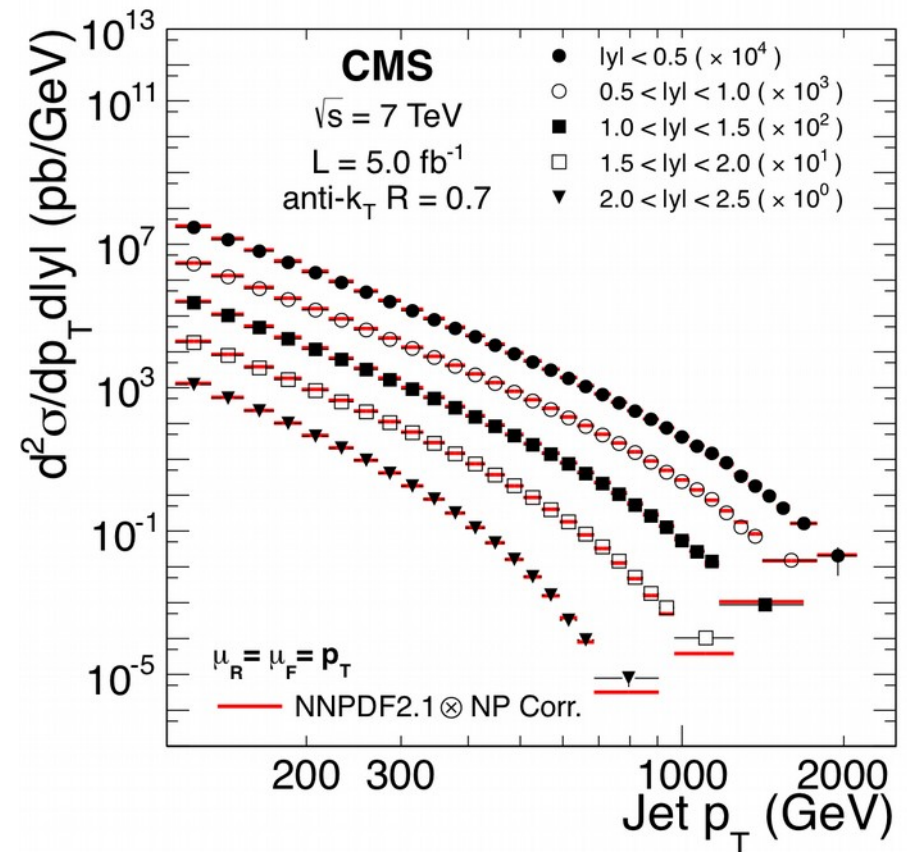
Institut für Experimentelle Kernphysik (IEKP)



CMS inclusive jet measurement



- Double differential inclusive jet cross section
- Inclusive jet cross section can be precisely calculated in perturbative QCD
- Performing detailed fits, the PDFs, in particular the gluon PDF at high x , can be constrained and the strong coupling constant can be determined
- Demonstrated by means of published CMS data of inclusive jet production (Phys. Rev. D 87 (2013) 112002)
- Electroweak corrections to hard scattering cross sections are applied (JHEP 1211 (2012) 095)
 - We thank S. Dittmaier and A. Huss for providing us the exact factors for our kinematic phase space



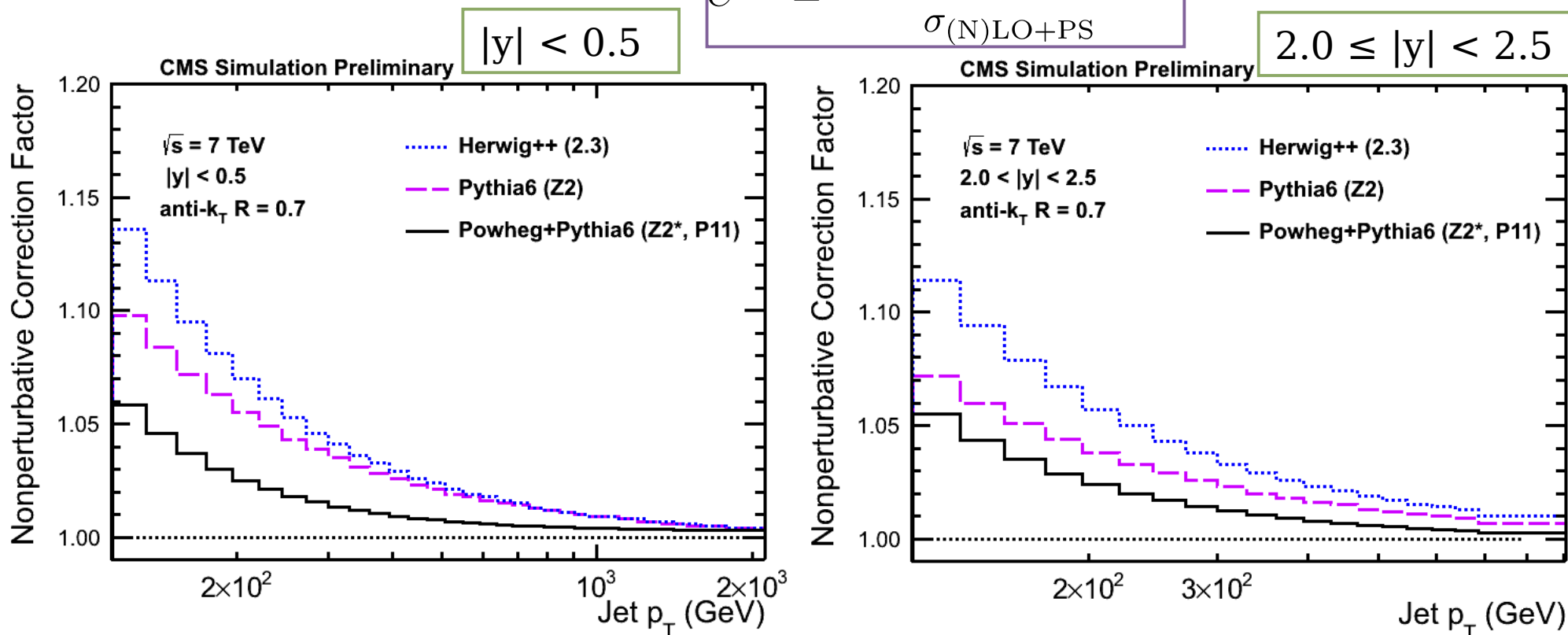
$$\frac{d^2\sigma}{dp_T dy} = \frac{1}{\epsilon \cdot \mathcal{L}_{\text{int}} \Delta p_T} \frac{N_{\text{jets}}}{(2 \cdot \Delta|y|)}$$



Nonperturbative Corrections

- For the first time NP correction from matched-NLO MC generator compared to NP predictions from Pythia6 and Herwig++
- Similar results from NLO and LO ME calculation but corrections from Powheg are smaller
- Central results on NP correction and uncertainty defined by the envelope given by the three predictions

$$C^{\text{NP}} = \frac{\sigma^{(\text{N})\text{LO+PS+HAD+MPI}}}{\sigma^{(\text{N})\text{LO+PS}}}$$





NP & PS Correction

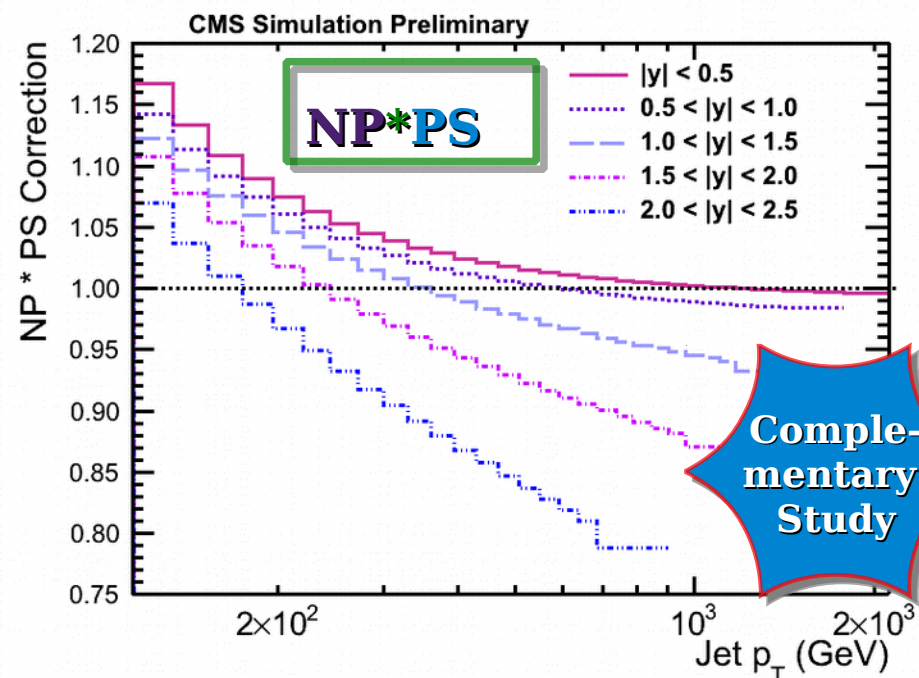
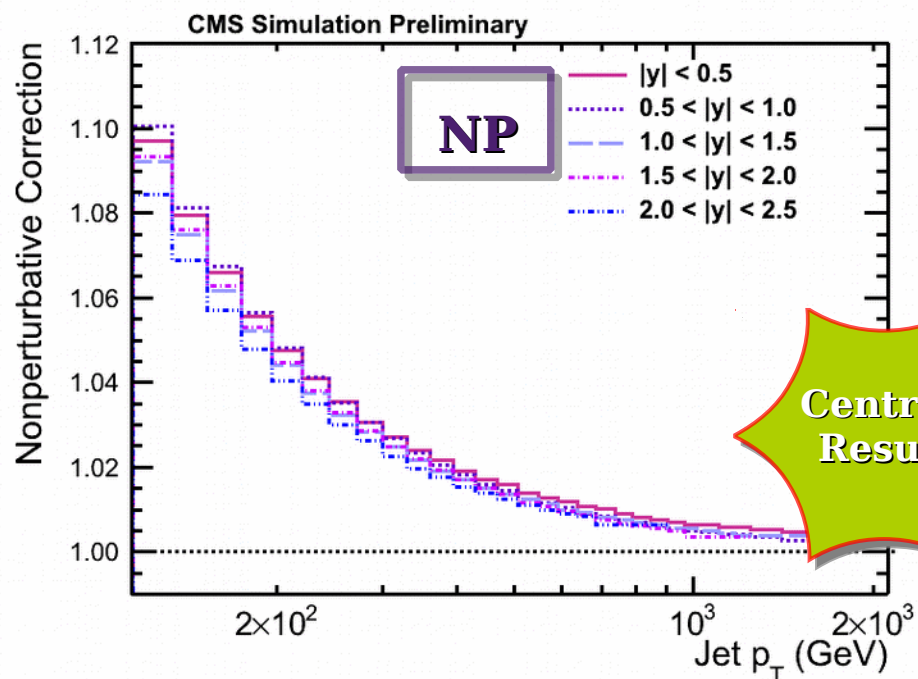
- NP defined as the center of the envelope given by the three predictions

$$C^{\text{NP}} = \frac{\sigma_{(\text{N})\text{LO}+\text{PS}+\text{HAD}+\text{MPI}}}{\sigma_{(\text{N})\text{LO}+\text{PS}}}$$

- PS correction determined as the average of the predictions from the two extreme scale limits

$$C^{\text{PS}} = \frac{\sigma_{\text{NLO}+\text{PS}}}{\sigma_{\text{NLO}}}$$

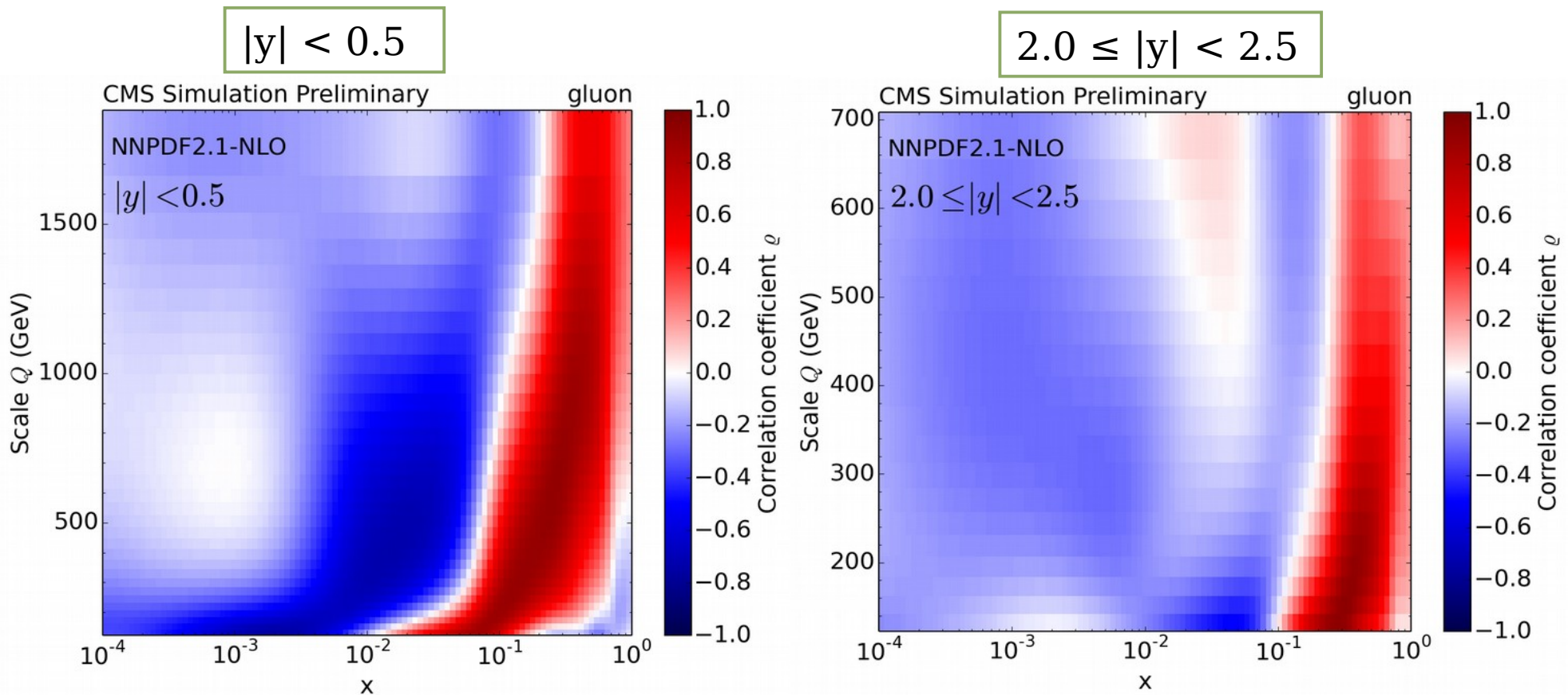
- NP * PS correction investigated in a complementary study



Correlation of gluon PDF and σ_{jet}



- Central region: High correlation at $0.05 < x < 0.7$ and $Q < 1500$ GeV
- Forward region: High correlation at $0.1 < x < 0.7$ and $Q < 300$ GeV
- **Constraints on PDFs expected at high- x**





PDF fit settings

- Fits performed with HERAFitter
- Standard 13p-HERAPDF parameterization is used
- A: normalization, B: low- x behaviour, C: high- x shape

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g}$$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2)$$

$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}}$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}}$$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}$$

- Evolution at NLO
- Normalization parameters A_i determined by QCD sum rules
- Additional constraints for small- x behaviour

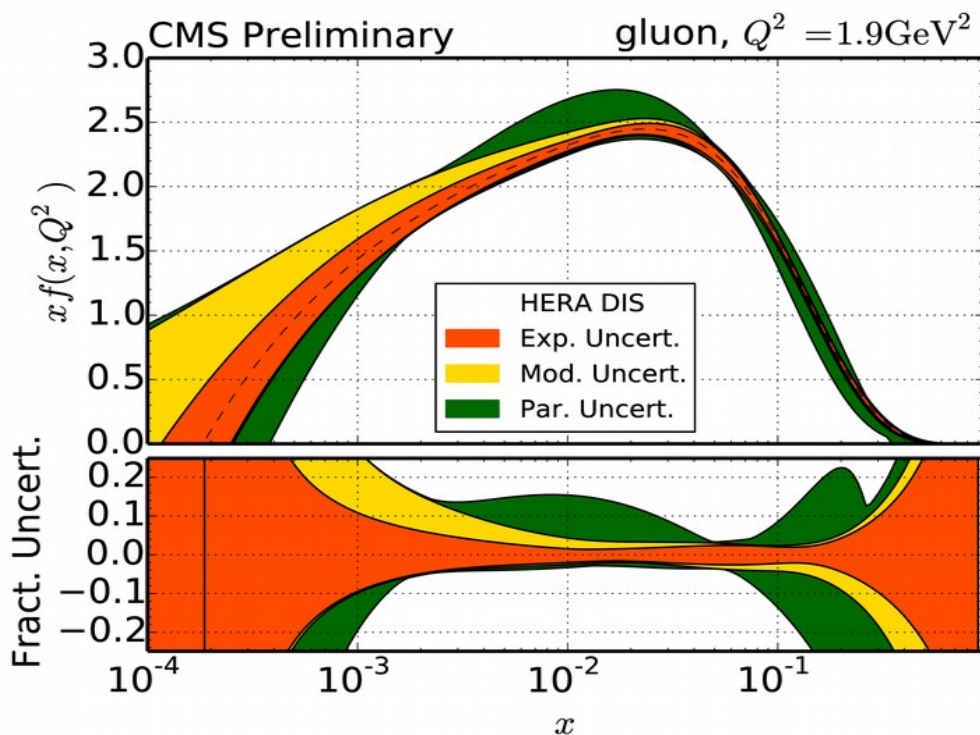
$$B_{\bar{U}} = B_{\bar{D}} \quad A_{\bar{U}} = A_{\bar{D}}(1 - f_S)$$



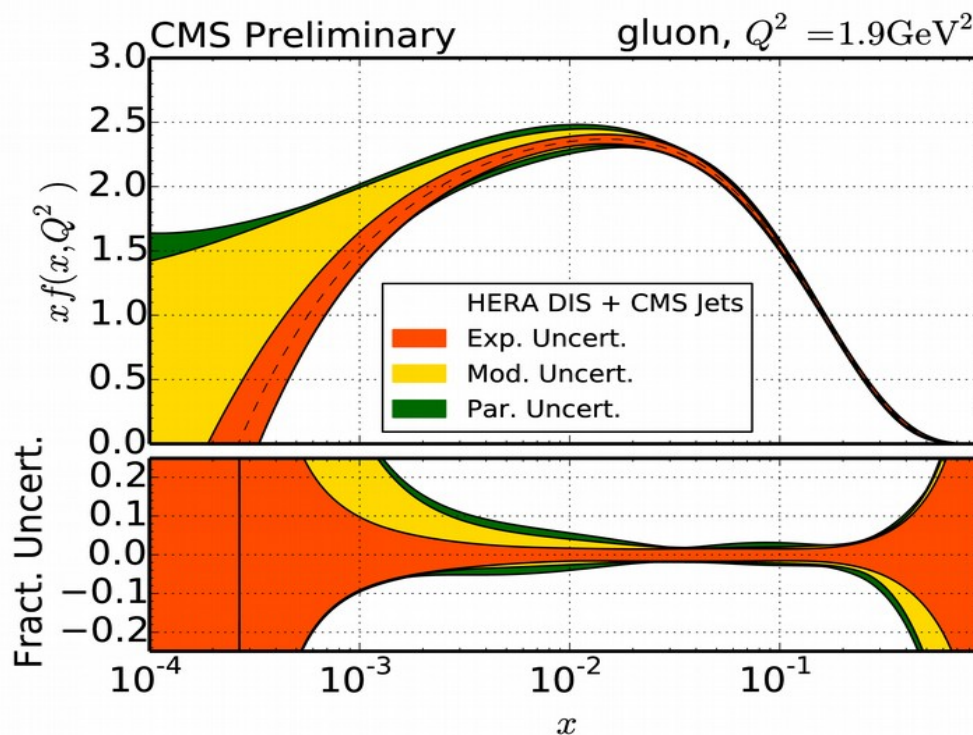
Constraints on the gluon, $Q^2=1.9 \text{ GeV}^2$

- Strong impact on gluon PDF
- Uncertainty reduced in high- x region
- PDF at starting scale $Q_0^2=1.9 \text{ GeV}^2$

HERA DIS



HERA DIS+CMS Jets

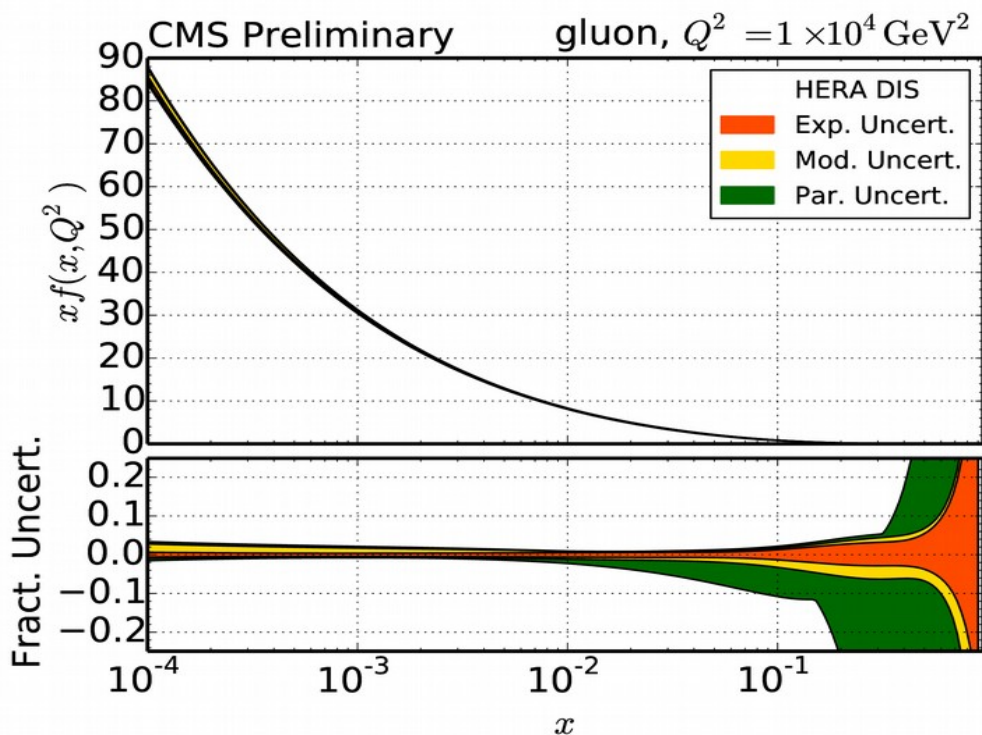




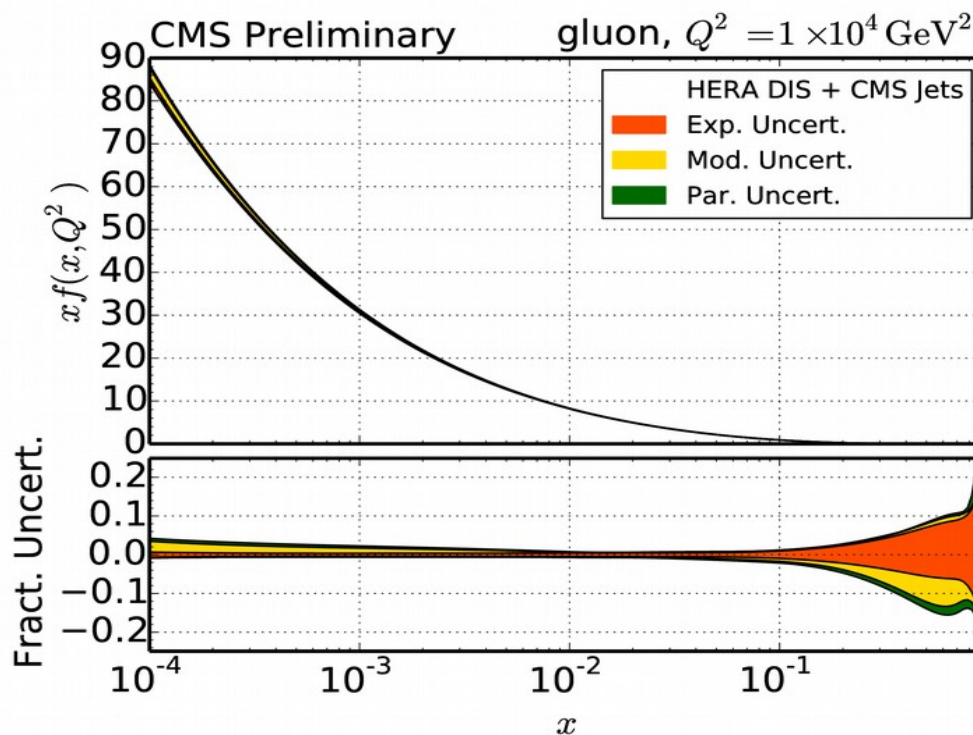
Constraints on the gluon, $Q^2=10^4 \text{ GeV}^2$

- Strong impact on gluon PDF
- Uncertainty reduced in high-x region
- PDF at scale $Q^2=10^4 \text{ GeV}^2$

HERA DIS

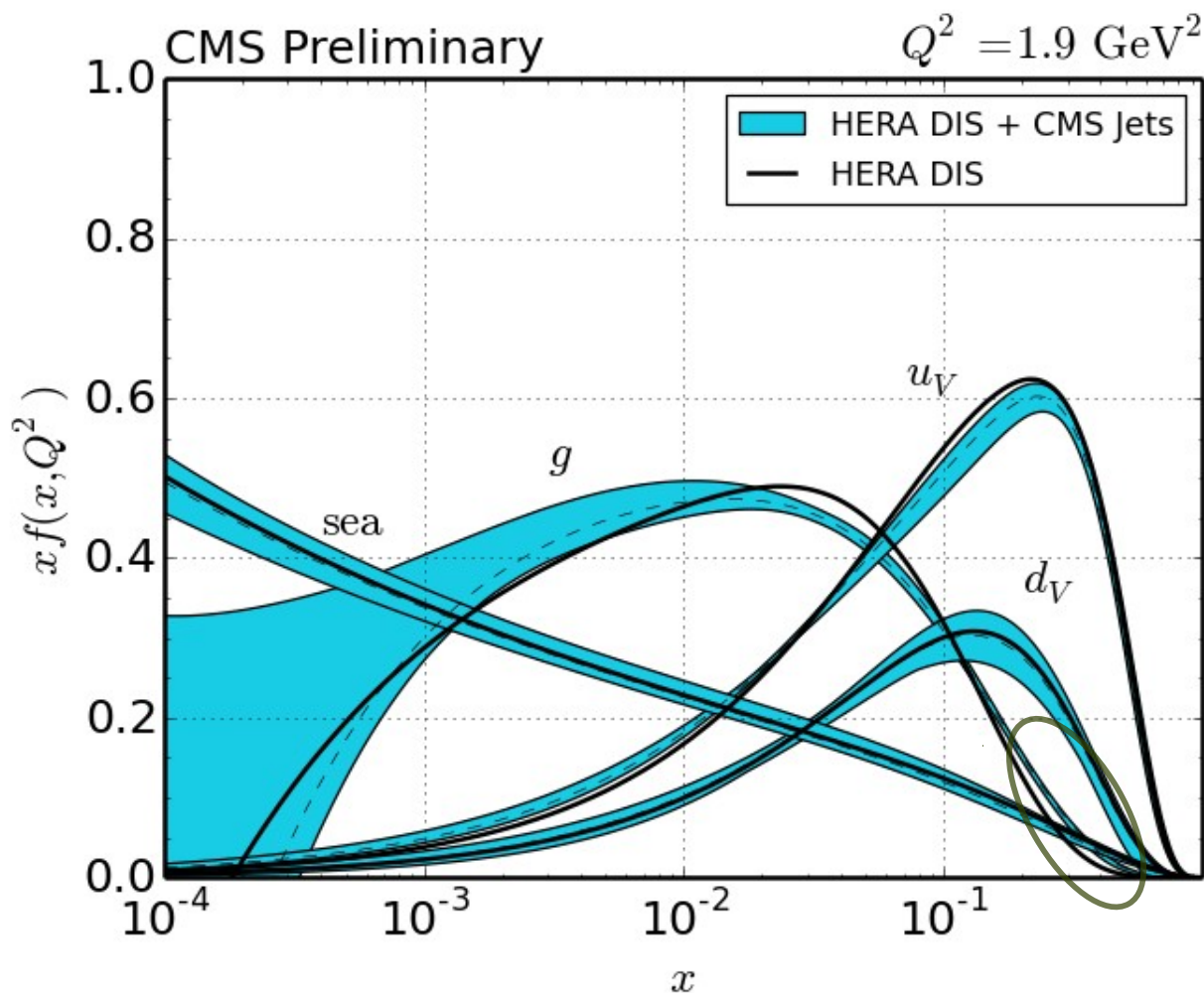


HERA DIS+CMS Jets



Overview on PDF fits

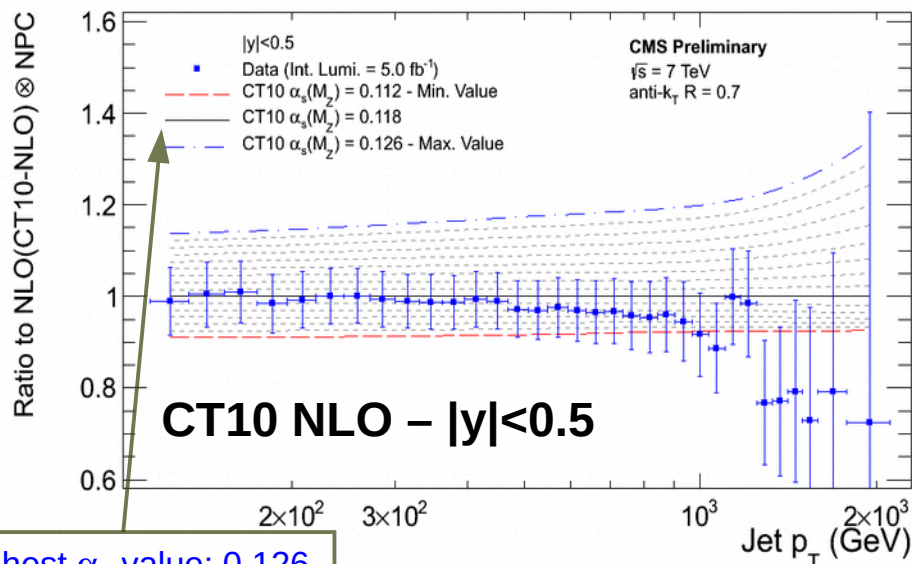
- Harder gluon observed with reduced uncertainties
- Some impact on u-valence distribution as well



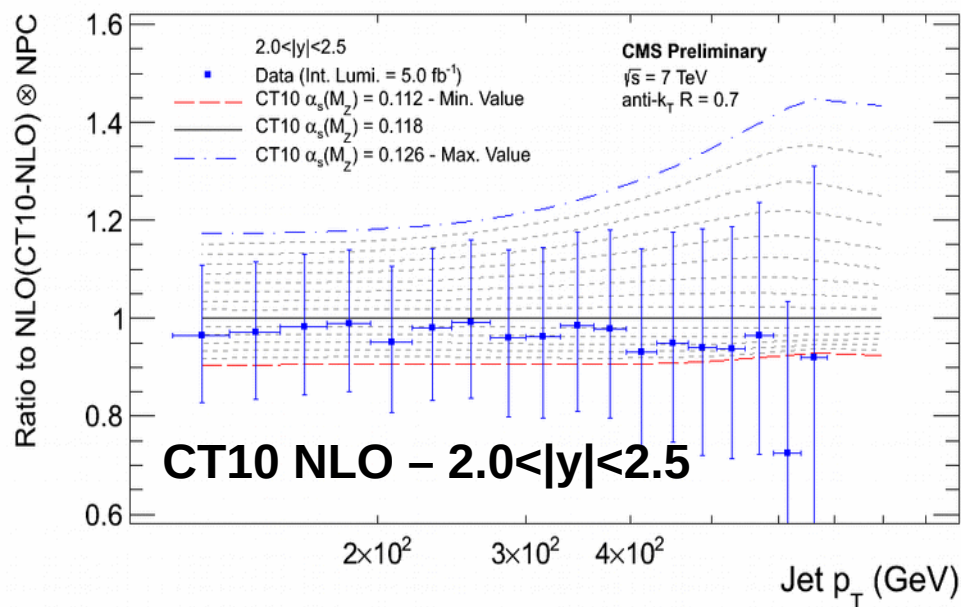


Sensitivity of $\alpha_s(m_Z)$: CT10-NLO

- Sensitivity plots show the ratio of predictions with different values of $\alpha_s(m_Z)$ to the central PDF predictions
- Data with total uncertainty is shown
- Ratio is flat over wide range of p_T and well described within a small $\alpha_s \rightarrow$ **suitable** for α_s extraction



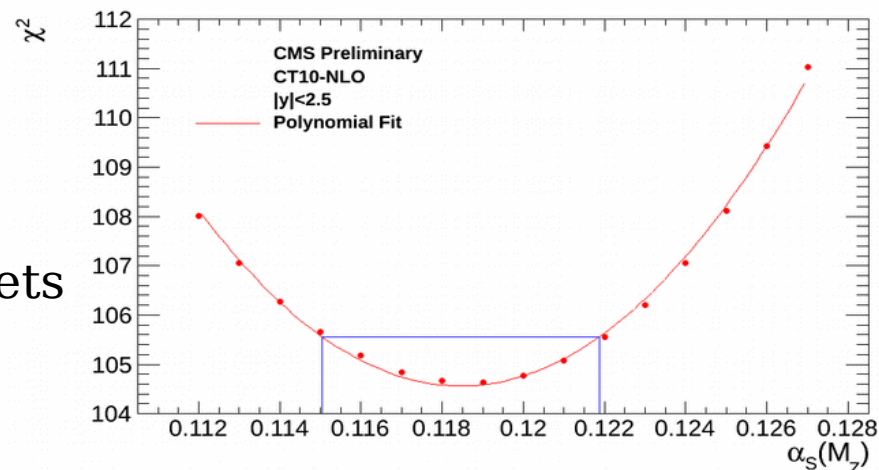
Highest α_s value: 0.126
Central α_s value: 0.118
Lowest α_s value: 0.112





Extraction of $\alpha_s(m_Z)$

- Central result with CT10-NLO
- PDF and scale uncertainties dominant
- Perfectly compatible with world average
- Consistent with results using other PDF sets within uncertainties



| PDF set | $\alpha_s(M_Z)$ | χ^2/n_{dof} |
|---------------|---|-------------------------|
| CT10-NLO | $0.1185 \pm 0.0019(\text{exp}) \pm 0.0028(\text{PDF})$ $\pm 0.0004(\text{NP})^{+0.0055}_{-0.0022}(\text{scale})$ | 104.6/132 |
| MSTW2008-NLO | $0.1157 \pm 0.0012(\text{exp}) \pm 0.0013(\text{PDF})$ $\pm 0.0001(\text{NP})^{+0.0029}_{-0.0028}(\text{scale})$ | 108.3/132 |
| CT10-NNLO | $0.1170 \pm 0.0012(\text{exp}) \pm 0.0024(\text{PDF})$ $\pm 0.0004(\text{NP})^{+0.0046}_{-0.0027}(\text{scale})$ | 106.1/132 |
| NNPDF2.1-NNLO | $0.1173 \pm 0.0012(\text{exp}) \pm 0.0018(\text{PDF})$ $\pm 0.0001(\text{NP})^{+0.0020}_{-0.0018}(\text{scale})$ | 104.1/132 |
| MSTW2008-NNLO | $0.1133 \pm 0.0010(\text{exp}) \pm 0.0011(\text{PDF})$ $\pm 0.0001(\text{NP})^{+0.0020}_{-0.0021}(\text{scale})$ | 107.6/132 |



Complementary studies

- Result using **NP+PS corrections** from POWHEG also in agreement with our central result :

$$\begin{aligned}\alpha_s(M_Z) &= 0.1205 \pm 0.0018 \text{ (exp.)} \pm 0.0031 \text{ (PDF)} \pm 0.0264 \text{ (NP+PS)}^{+0.0053}_{-0.0029} \text{ (scale)} \\ &= 0.1205^{+0.0272}_{-0.0268}\end{aligned}$$

- NP+PS are the dominant uncertainties because of lacking knowledge of and experience with PS effects.

- **Simultaneous fit** of PDFs & $\alpha_s(m_Z)$

$$\alpha_s(M_Z) = 0.1192^{+0.0017}_{-0.0015} \text{ (exp., NP)}$$

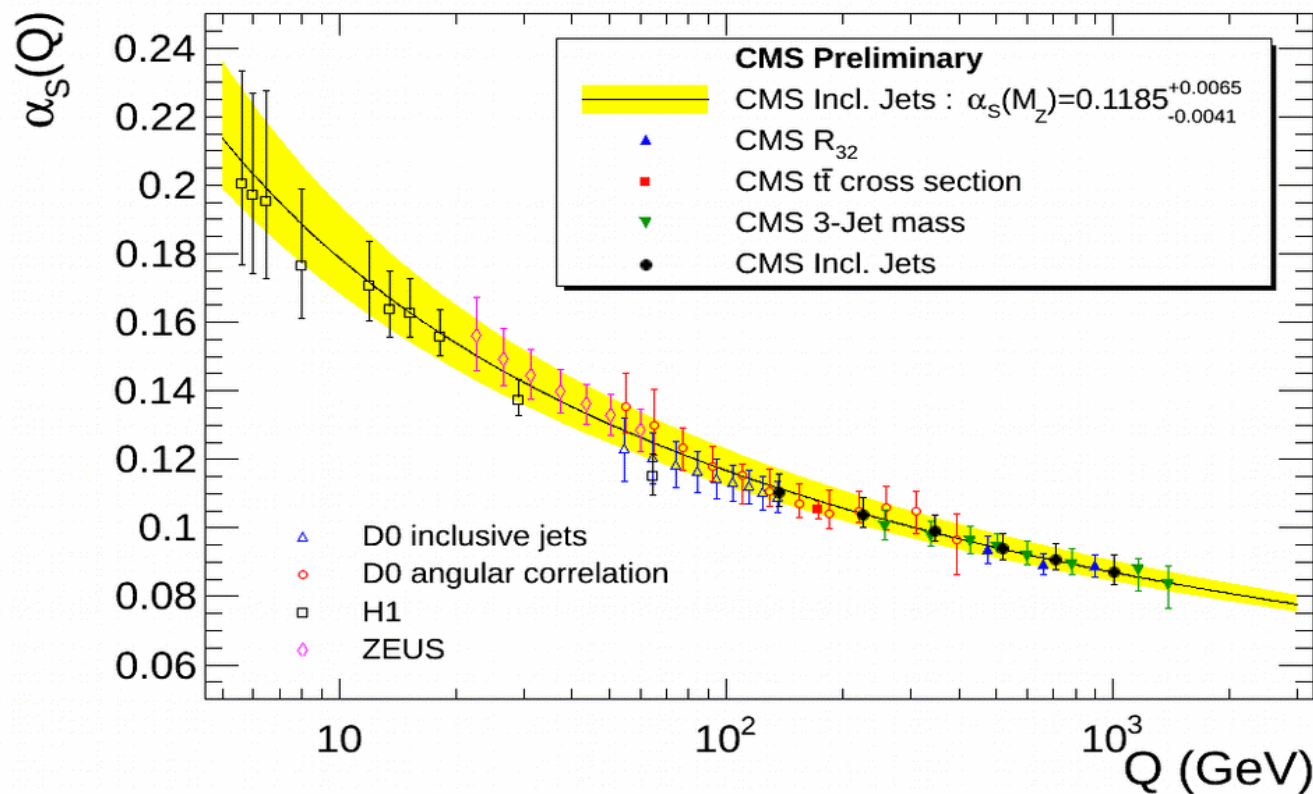
- Uncertainty accounts for experimental HERA DIS and CMS inclusive jet uncertainty and NP uncertainty, but not for model/parametrization and scale uncertainties
- Both results are in agreement with the “central” result derived using CT10-NLO



Running of $\alpha_s(Q)$

- Fitted region is split into six regions as shown in table and $\alpha_s(M_Z)$ derived for each region.
- Using the 2-loop RGE these values evolved back to the corresponding $\alpha_s(Q)$.
- The new CMS results on α_s are consistent with the energy dependence predicted by the RGE.

| p_T range (GeV) | Q (GeV) | $\alpha_s(M_Z)$ | $\alpha_s(Q)$ | No. of data points | χ^2/n_{dof} |
|----------------------|--------------|------------------------------|------------------------------|-----------------------|-------------------------|
| 114–196 | 136 | $0.1170^{+0.0062}_{-0.0045}$ | $0.1103^{+0.0054}_{-0.0039}$ | 20 | 6.2/19 |
| 196–300 | 226 | $0.1179^{+0.0067}_{-0.0049}$ | $0.1037^{+0.0052}_{-0.0037}$ | 20 | 7.6/19 |
| 300–468 | 345 | $0.1194^{+0.0067}_{-0.0049}$ | $0.0993^{+0.0045}_{-0.0033}$ | 25 | 8.2/24 |
| 468–638 | 521 | $0.1188^{+0.0072}_{-0.0051}$ | $0.0940^{+0.0044}_{-0.0032}$ | 20 | 10.6/19 |
| 638–905 | 711 | $0.1193^{+0.0080}_{-0.0056}$ | $0.0910^{+0.0044}_{-0.0033}$ | 22 | 11.4/21 |
| 905–2116 | 1007 | $0.1180^{+0.0104}_{-0.0061}$ | $0.0868^{+0.0054}_{-0.0033}$ | 26 | 39.4/25 |





Summary

- For the first time include electroweak and matched NLO+parton showers in PDF+ α_s fits
- PDF fits including CMS inclusive jet data demonstrate significant impact on the PDFs, particularly the gluon PDF
- New determination of $\alpha_s(M_Z)$ from inclusive jet cross section
- Results consistent with previous CMS results and the world average
- Running of $\alpha_s(Q)$ consistent with RGE of QCD

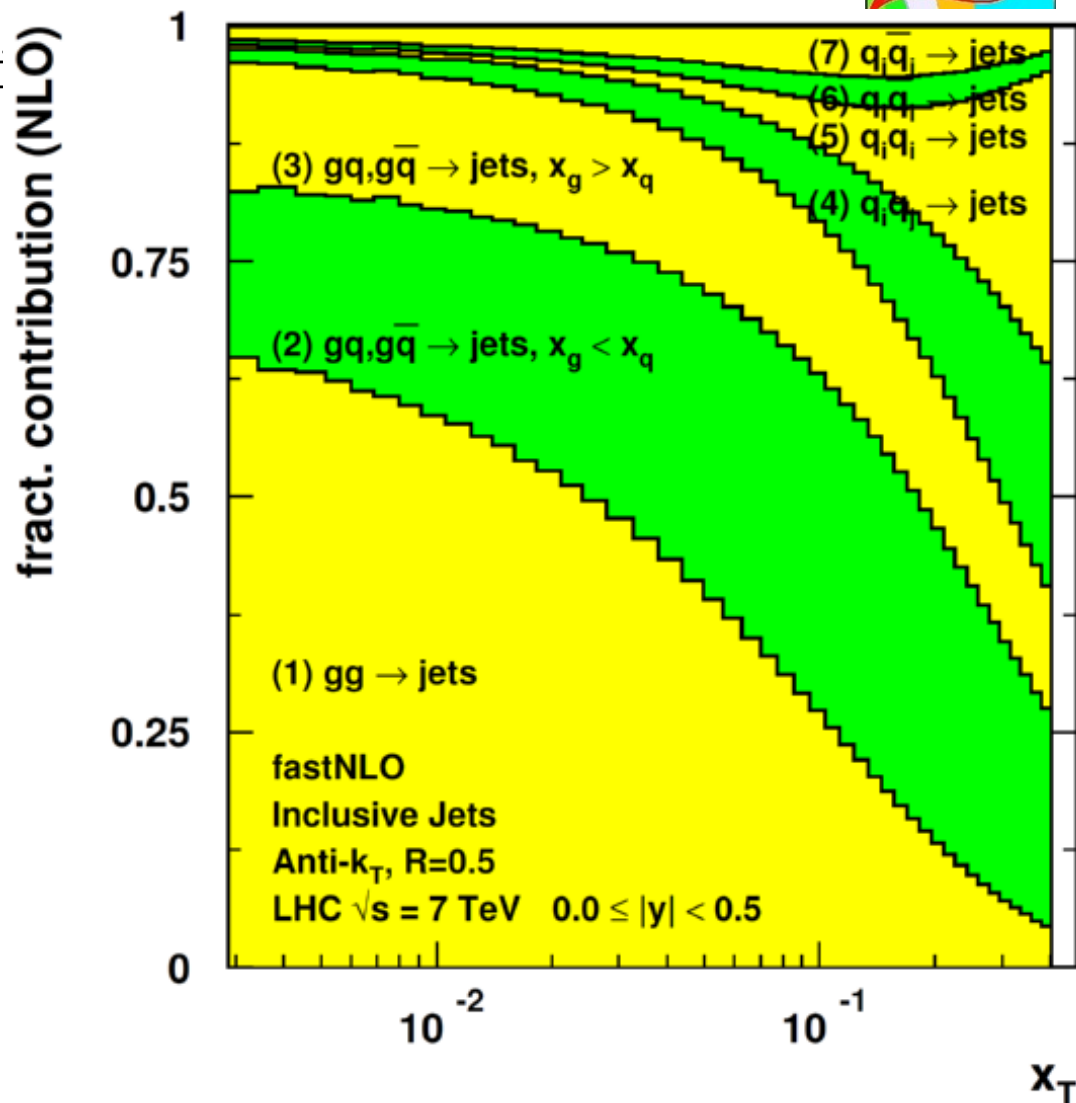


Additional material



Subprocesses in dijet production

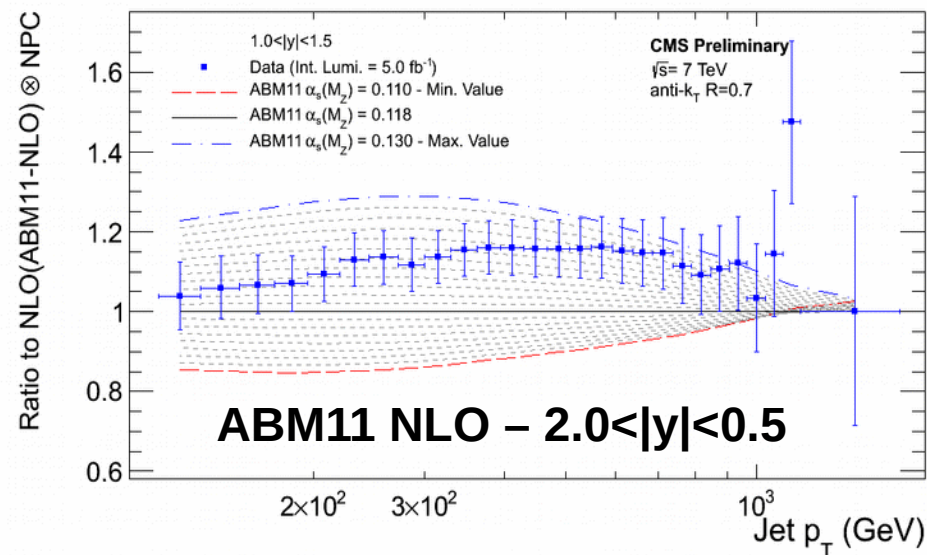
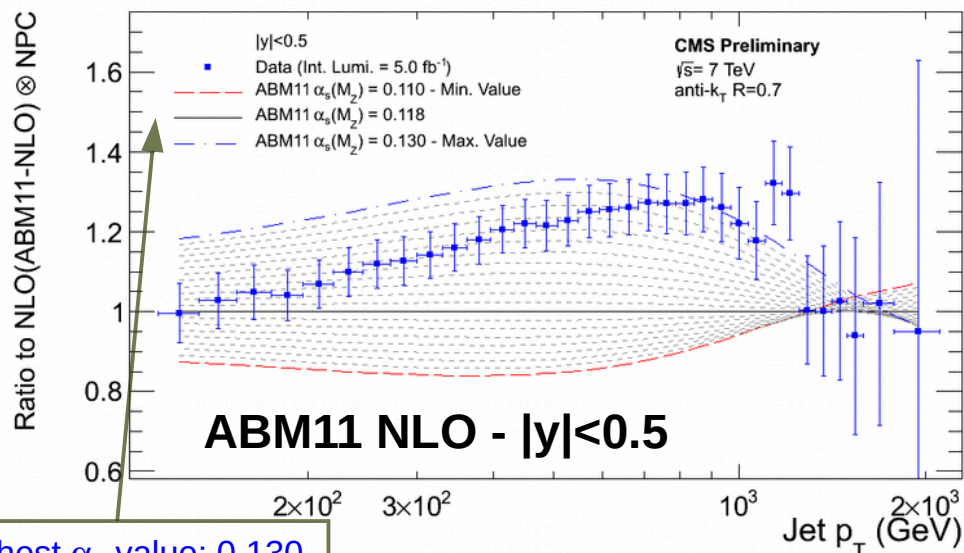
- subprocess fraction as a function of x_T
- **qg and gg processes**
 - dominant below 800 GeV
 - Sensitive to gluon PDF
- **qq processes**
 - prevail above 800 GeV
 - Sensitive to quark PDFs
- **$q\bar{q}$ processes**
 - Suppressed
 - No sensitivity to antiquark PDFs





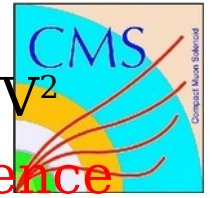
Sensitivity of $\alpha_s(m_Z)$: ABM11-NLO

- Sensitivity plots show the ratio of predictions with different values of $\alpha_s(m_Z)$ to the central PDF predictions
- Data with total uncertainty is shown
- Inclusive jet data are not well described using ABM PDFs
 - omitted from further study

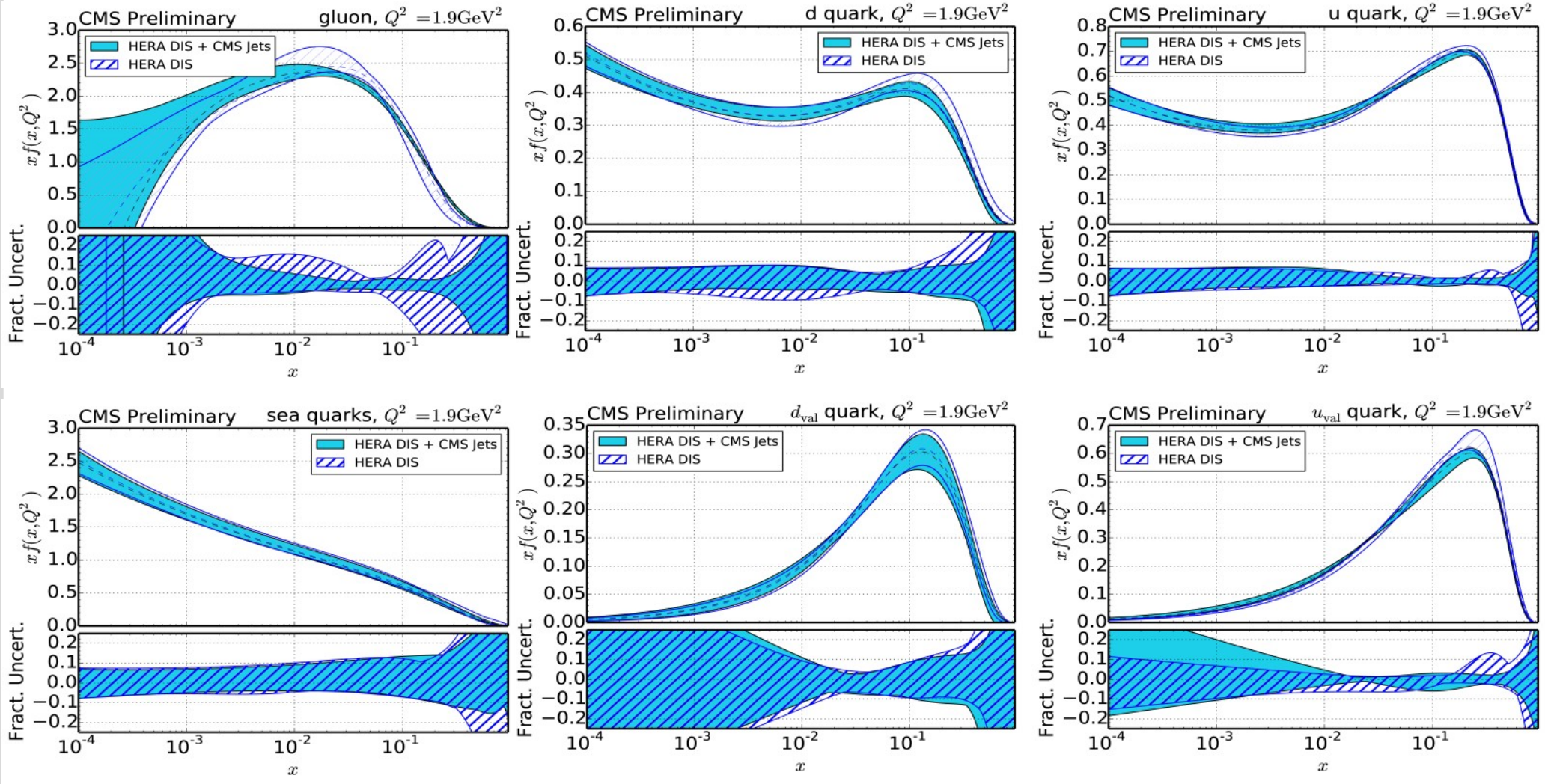


Highest α_s value: 0.130
Central α_s value: 0.118
Lowest α_s value: 0.110

PDF Constraints: $Q^2=1.9 \text{ GeV}^2$



- Direct comparison of fitted PDFs at starting scale $Q^2 = 1.9 \text{ GeV}^2$
- Overall PDF uncertainty reduced, only increase in low-x u-valence
- Low-x u valence uncertainty previously underestimated



Combined Fits: Constraints



- Direct comparison of all PDFs

- $Q^2 = 1 \text{E}4 \text{ GeV}^2$

- Overall PDF uncertainty reduced, only increase in low-x u-valence

