

# Principal limitations and systematic deviations regarding the slit measurement method

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# Outlook

- Slit scan technique for the emittance measurements
- ASTRA simulations, main solenoid scan
- Emittance calculation from slit scan data:
  - Correction term due to the phase space nonlinearity
  - Experimental data analysis
  - Beam position jitter influence
- Conclusions

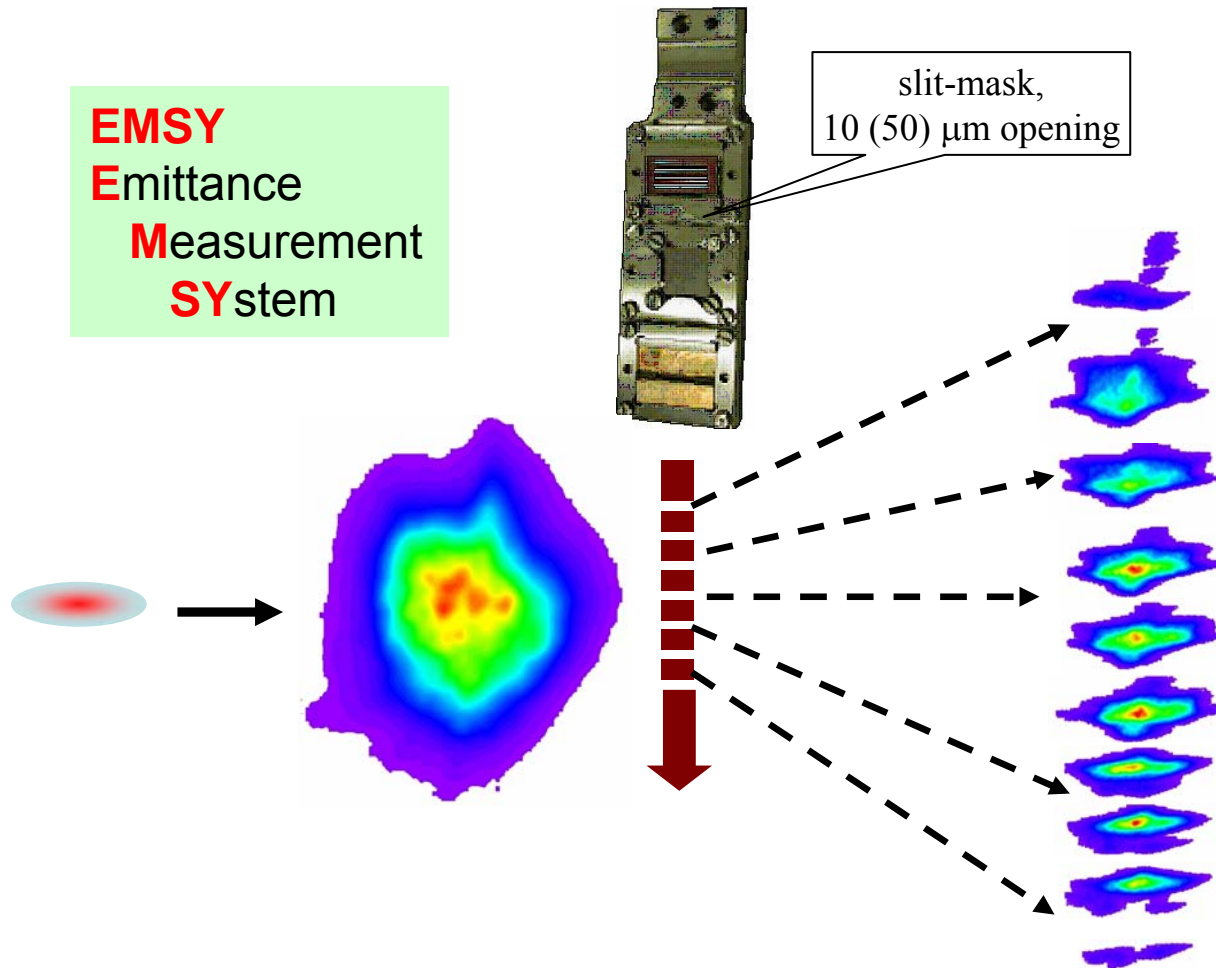
# Emittance measurements using slit scan technique

$$\varepsilon_x^n = \beta\gamma \cdot \sigma_X \cdot \sigma_{X'} \Rightarrow \varepsilon_{meas0}$$

$\sigma_X$  - whole beam rms size at EMSY screen ( $z = 4.3\text{m}$ )

$$\sigma_{X'} = \frac{1}{L} \sqrt{\sum_{n=1}^{Nsl} w_n \cdot (\sigma_{X,n}^{BL})^2} / \sqrt{\sum_{n=1}^{Nsl} w_n}$$

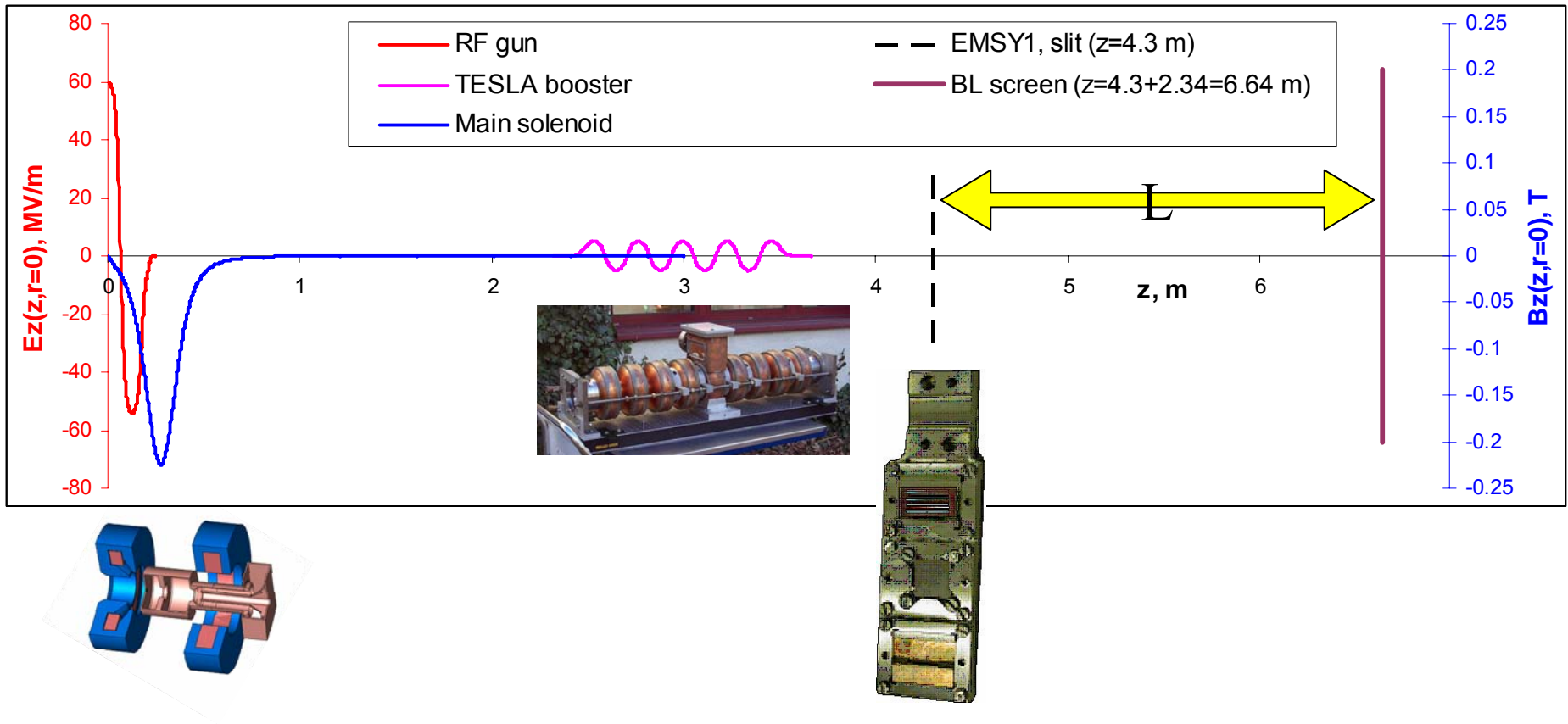
**EMSY**  
**E**mittance  
**M**easurement  
**S**ystem



Emit.meas@PITZ

- X + Y
- Projected
- RMS
- 100%

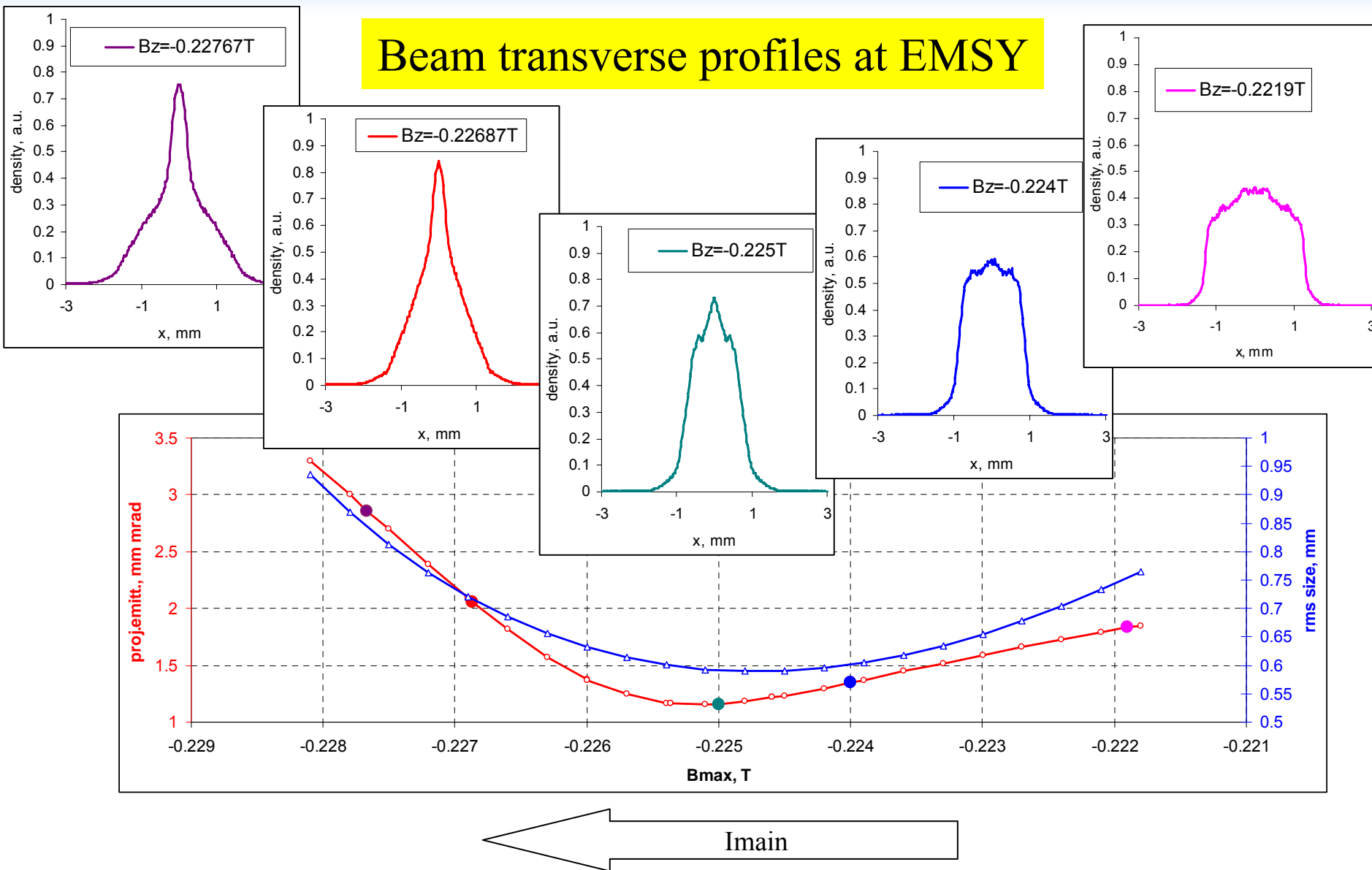
# ASTRA simulations of emittance measurements



RF gun			booster	simulations
cavity	solenoid	laser	TESLA	ASTRA
$E_{\text{cath}}=60\text{MV/m}$	$B_{\text{max}}=-0.225\text{T (varied)}$	$L_t=20\text{ps}$	$z(\text{center})=2.99\text{m}$	200k particles
$\Phi=-1.1\text{deg}$	$z_{\text{max}}=0.276\text{m}$	$r_t=5\text{ps}$	$E_{\text{max}}=5\text{MV/m}$	
		$XY_{\text{rms}}=0.44\text{mm}$	$\phi=-5.5\text{deg}$	
		$E_k=0.55\text{eV}$		
		$\text{ThEm}=0.37\text{mm mrad}$		

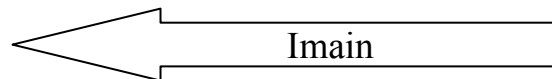
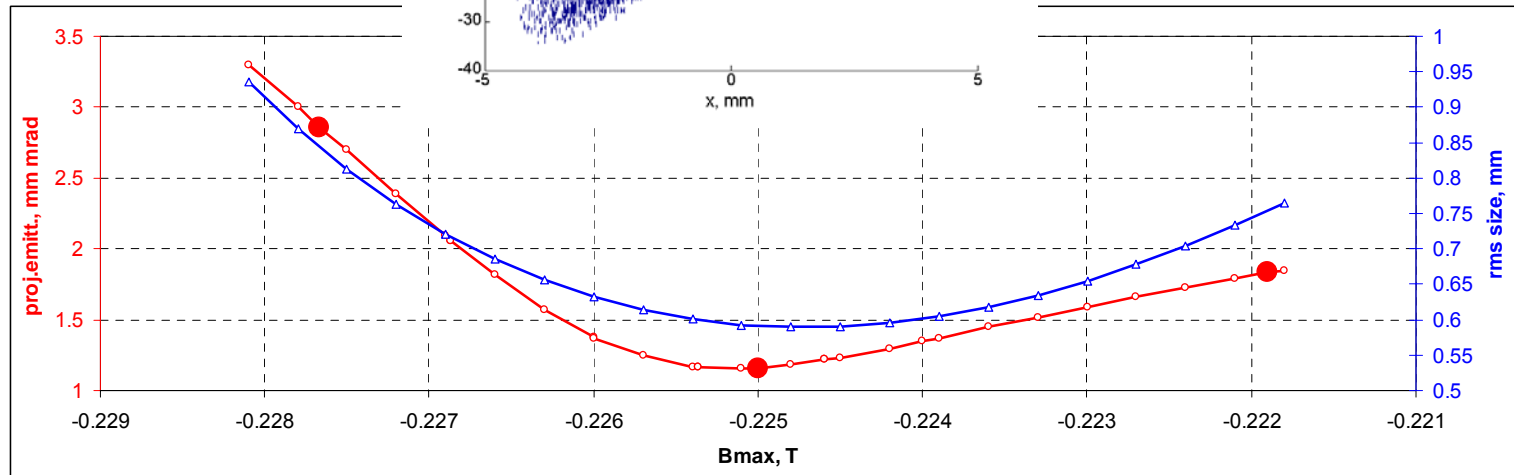
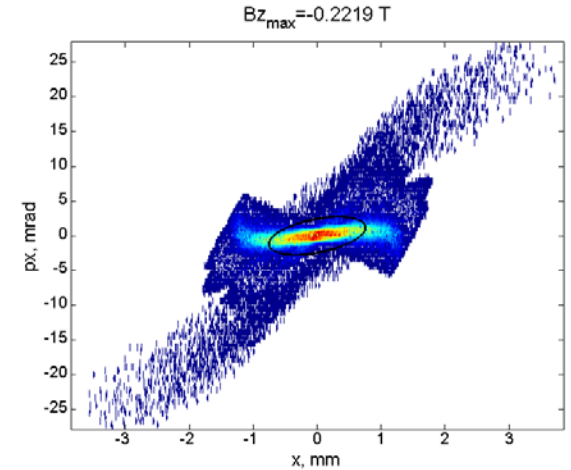
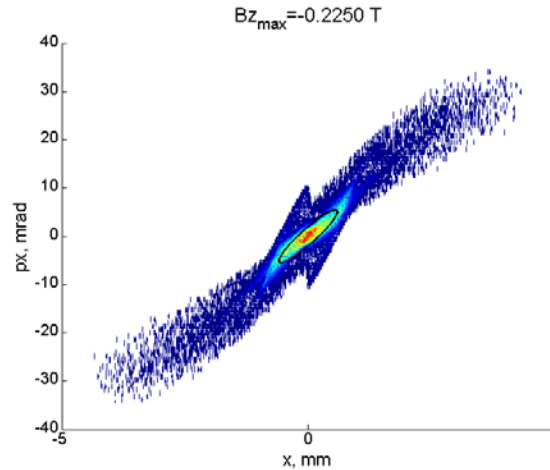
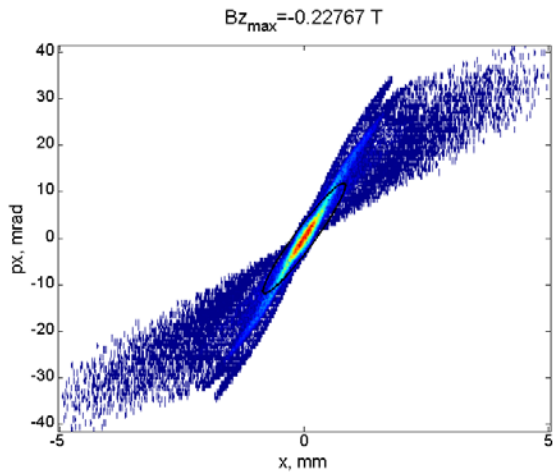
# ASTRA simulations. Main solenoid scan.

## Beam transverse profiles at EMSY

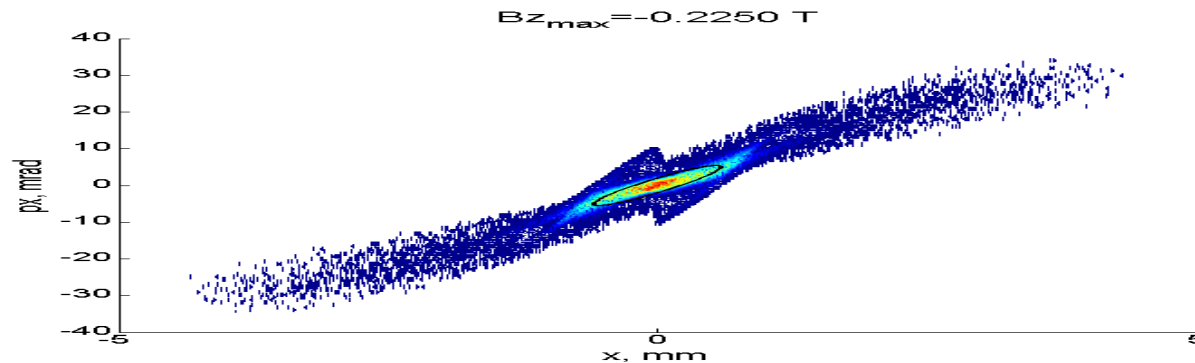


# ASTRA simulations. Main solenoid scan.

Beam phase space (x,px)

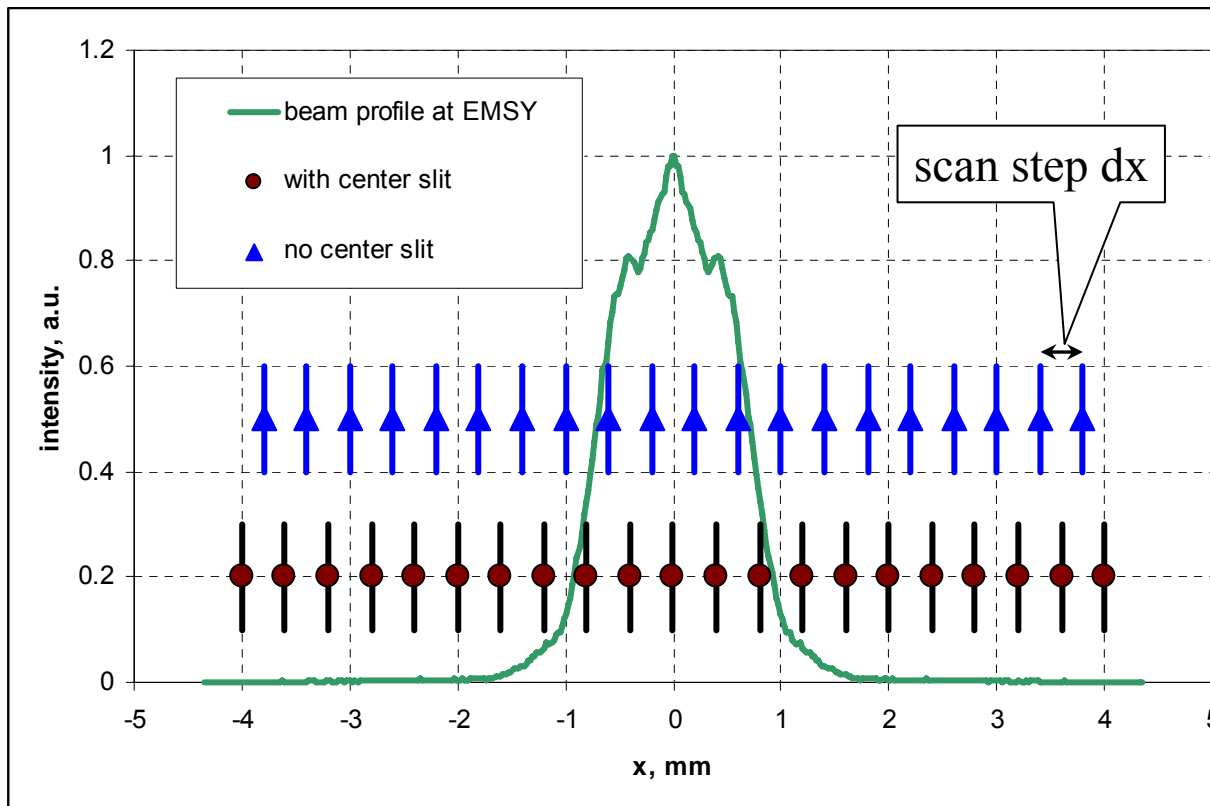


# Single slit scan technique. Main parameters



Slit opening = 10(50)  $\mu\text{m}$ :

- S2N ratio
- finite slit opening and thickness impact
- alignment issues



## Main parameters for the scan:

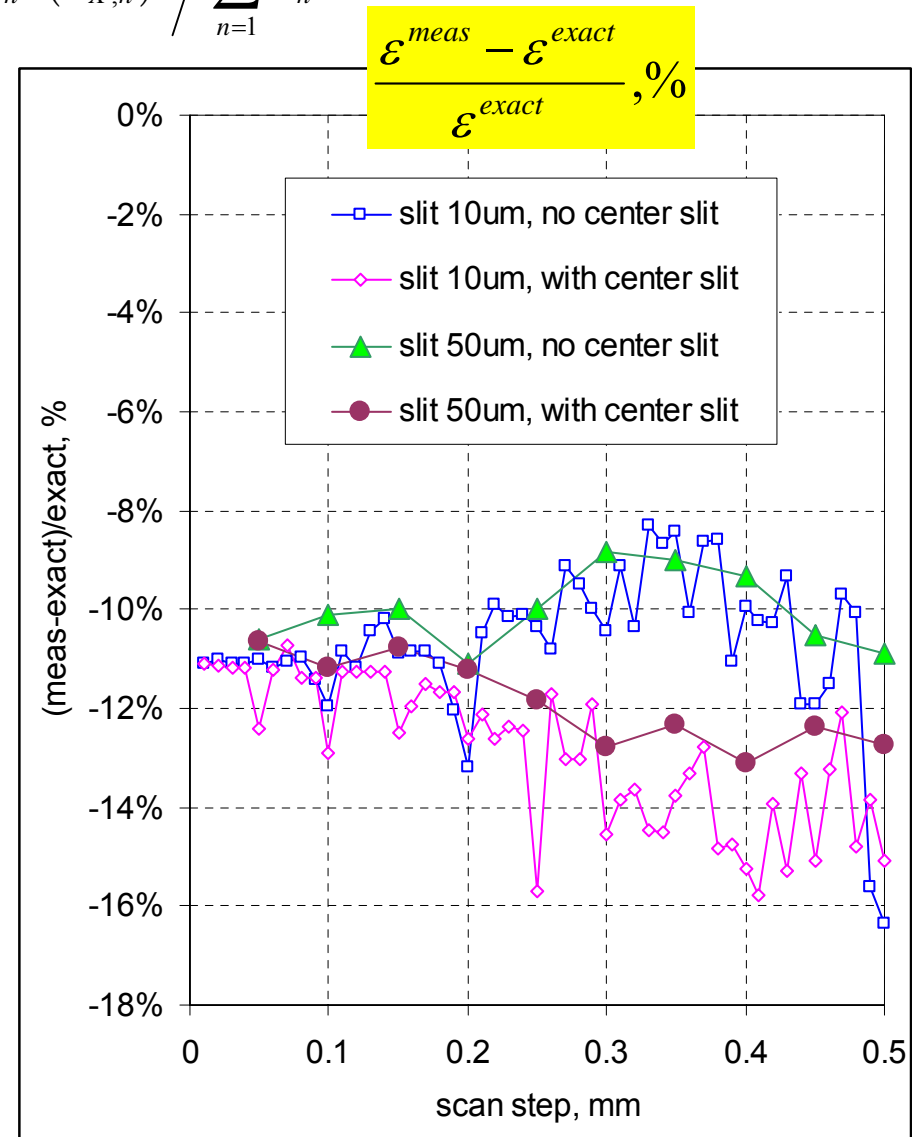
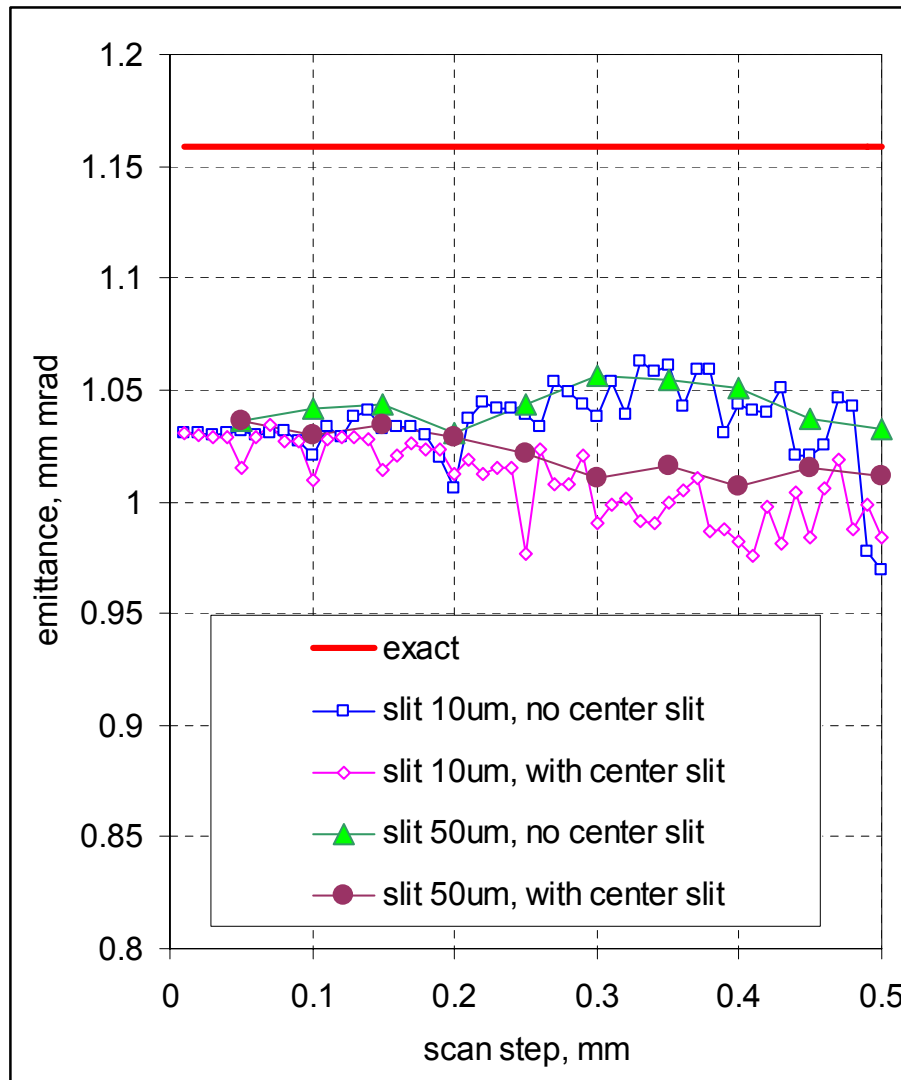
- **Scan step**  $dx$  (phase space pattern)
- **Intensity threshold** for scan (start/end for the scan)\*
- With/without **center slit** (convergent by  $dx \rightarrow 0$ )

# Simulated measured emittance vs. scan step

$$\varepsilon_{meas0} = \beta\gamma \cdot \sigma_X \cdot \sigma_{X'}$$

$$\sigma_{X'} = \frac{1}{L} \sqrt{\sum_{n=1}^{Nsl} w_n \cdot (\sigma_{X,n}^{BL})^2} / \sqrt{\sum_{n=1}^{Nsl} w_n}$$

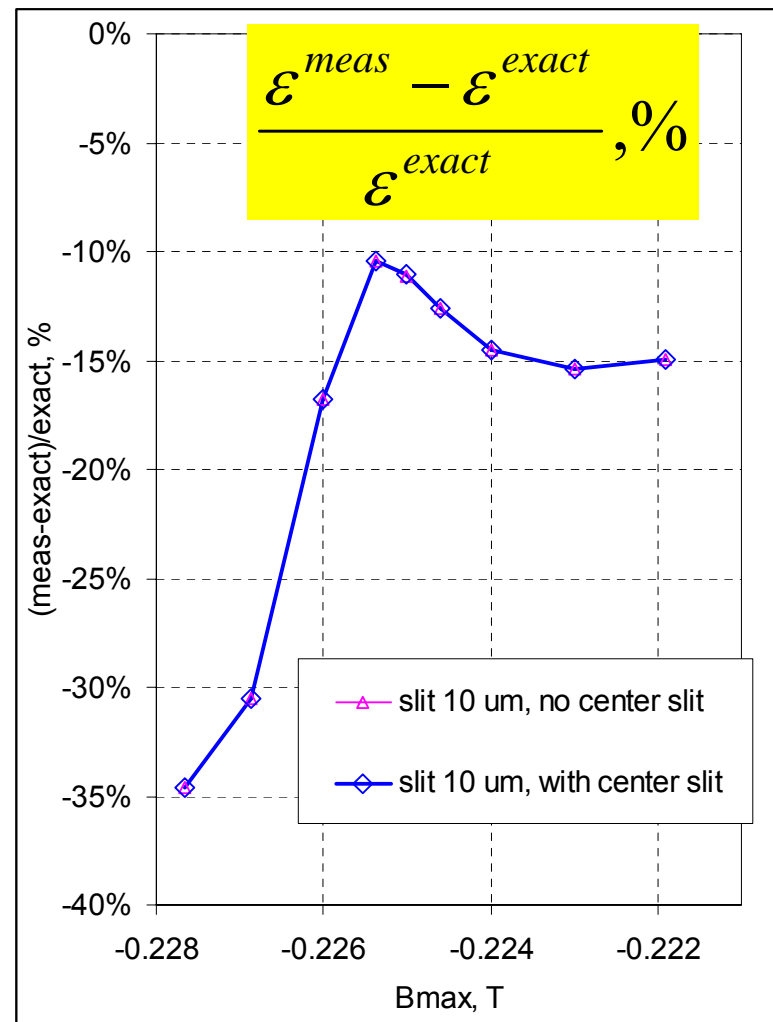
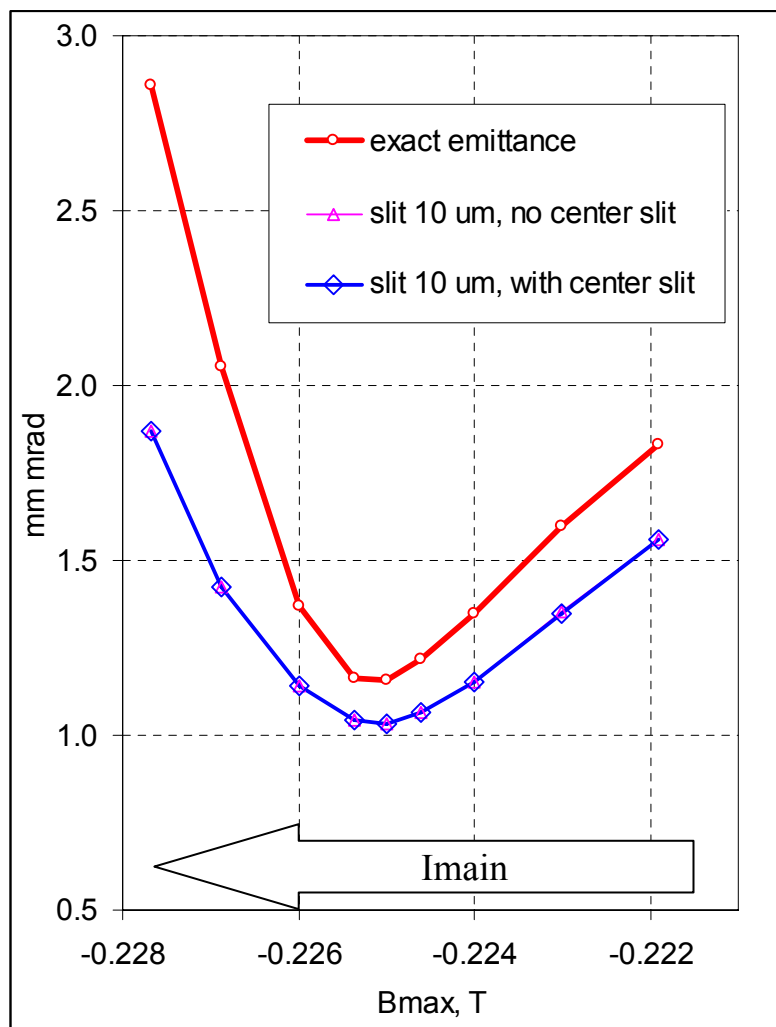
~best point Bzmax=-0.2250T





# Simulated measured emittance vs. main solenoid peak field

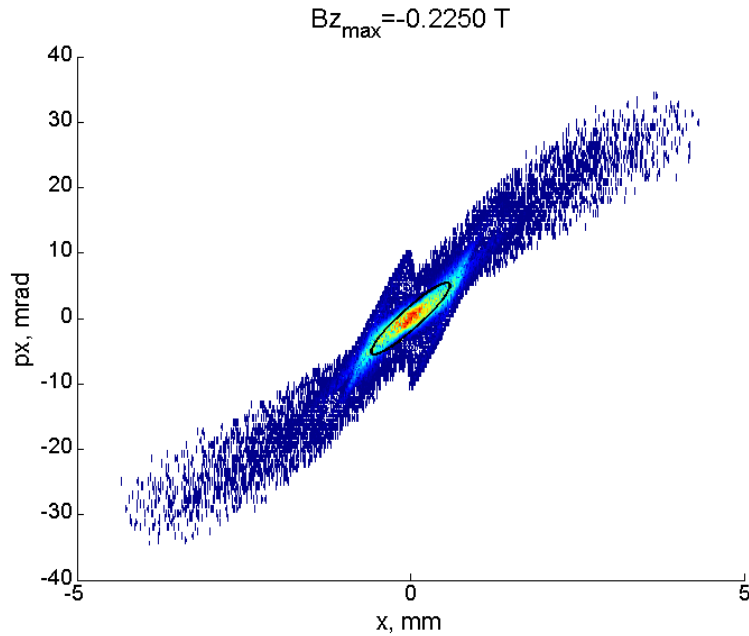
*Main solenoid scan (step size=slit opening=10um)*



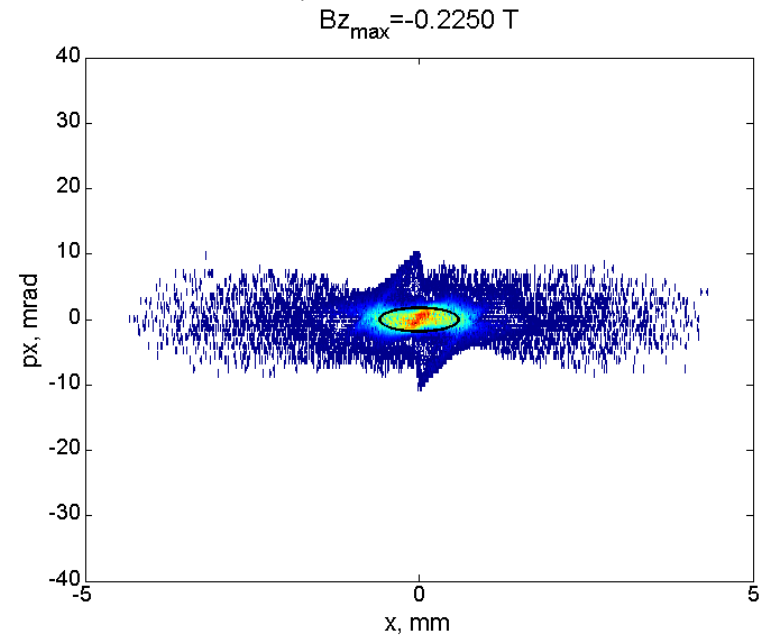
$$(\epsilon^{meas} - \epsilon^{exact}) / \epsilon^{exact} \approx -10\%!$$

# Transverse phase space. Removing correlations

$$\sigma_{x'} = \frac{1}{L} \sqrt{\sum_{n=1}^{Nsl} w_n \cdot (\sigma_{x,n}^{BL})^2} / \sqrt{\sum_{n=1}^{Nsl} w_n}$$



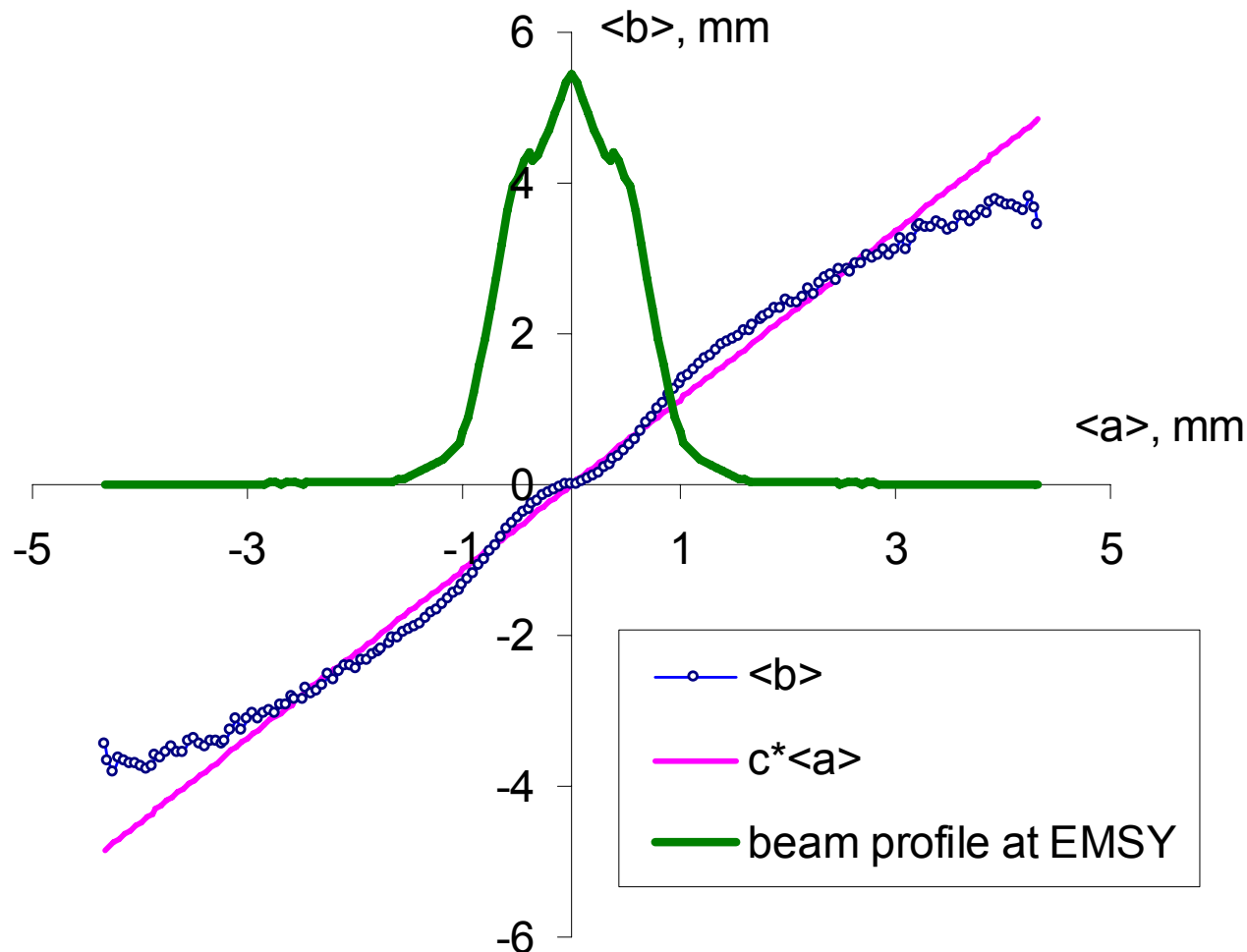
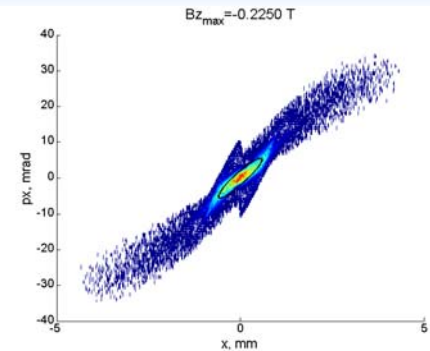
$\mathcal{E} = 1.16 \text{ mm mrad}$



$\mathcal{E} = 1.03 \text{ mm mrad}$

# Transverse phase space “skeleton”

$$b = x + \frac{px}{pz} \cdot L \Rightarrow \text{coordinate at the beamlet screen}$$

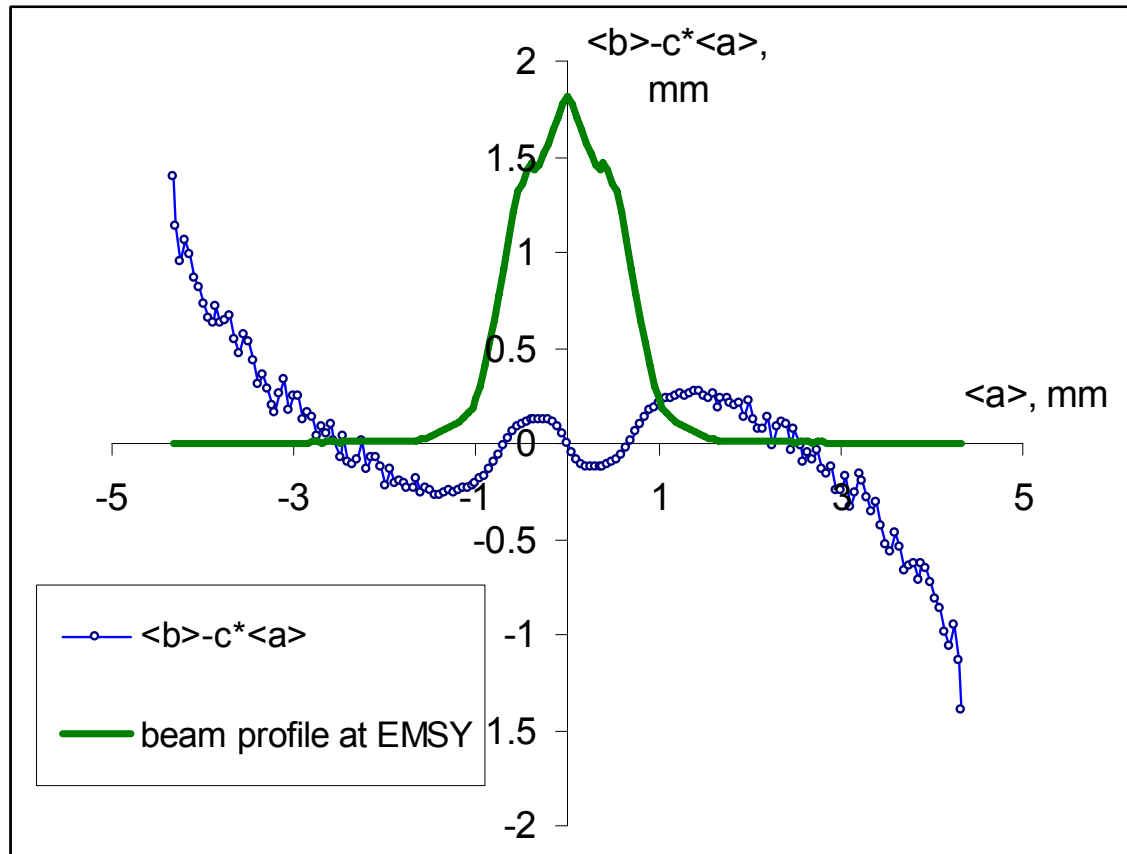


$$a = x$$

$$c = \frac{\sum_s w_s \cdot \bar{a}_s \cdot \bar{b}_s}{\sum_s w_s \cdot \bar{a}_s^2}$$

# Transverse phase space “skeleton”. Correction term

$$\varepsilon_{meas}^2 = \varepsilon_{meas0}^2 + \left( \frac{pz0}{L} \right)^2 \left[ \sigma_x^2 \cdot \sum_s w_s \cdot \bar{b}_s^2 - \left( \sum_s w_s \cdot \bar{a}_s \cdot \bar{b}_s \right)^2 \right]$$



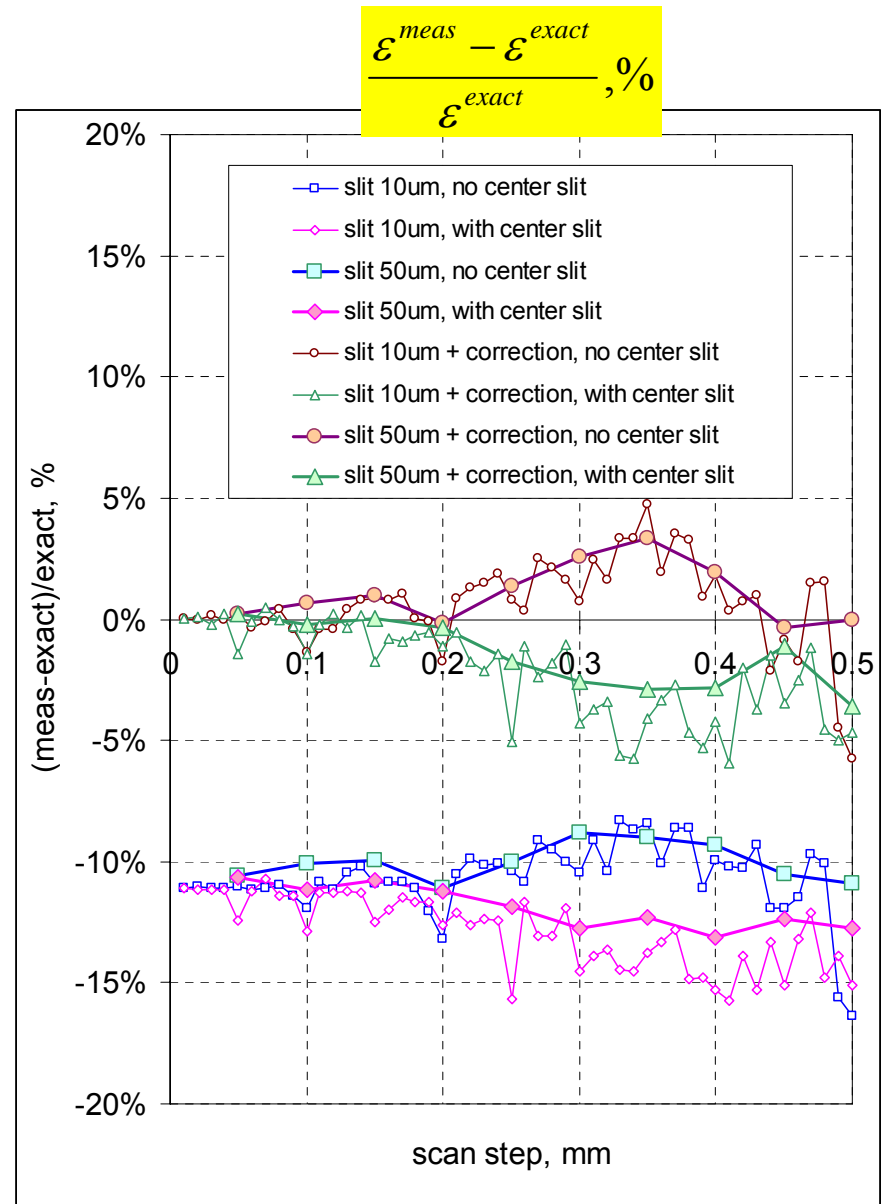
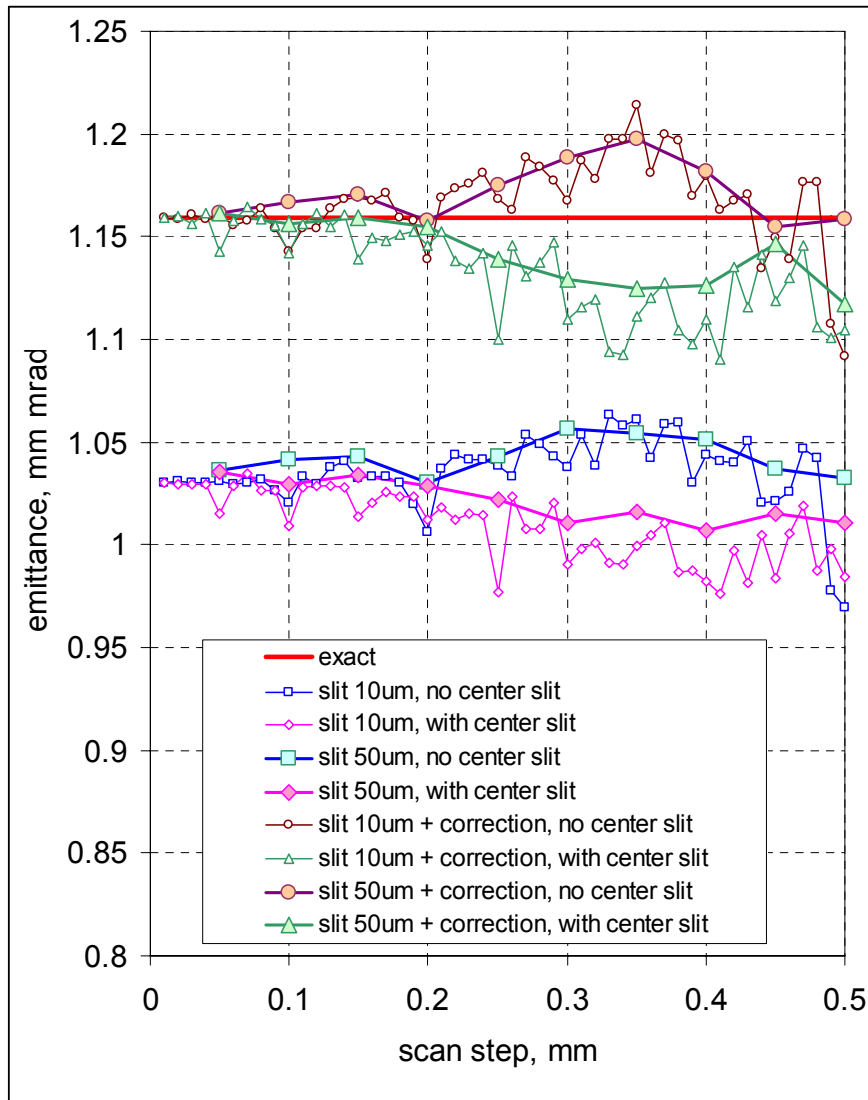
$$\sigma_x^2 \cdot \sum_s w_s \cdot \bar{b}_s^2 - \left( \sum_s w_s \cdot \bar{a}_s \cdot \bar{b}_s \right)^2$$

$$\Downarrow$$

$$\sigma_x^2 \cdot \sum_s w_s \cdot (\bar{b}_s - c \cdot \bar{a}_s)^2$$

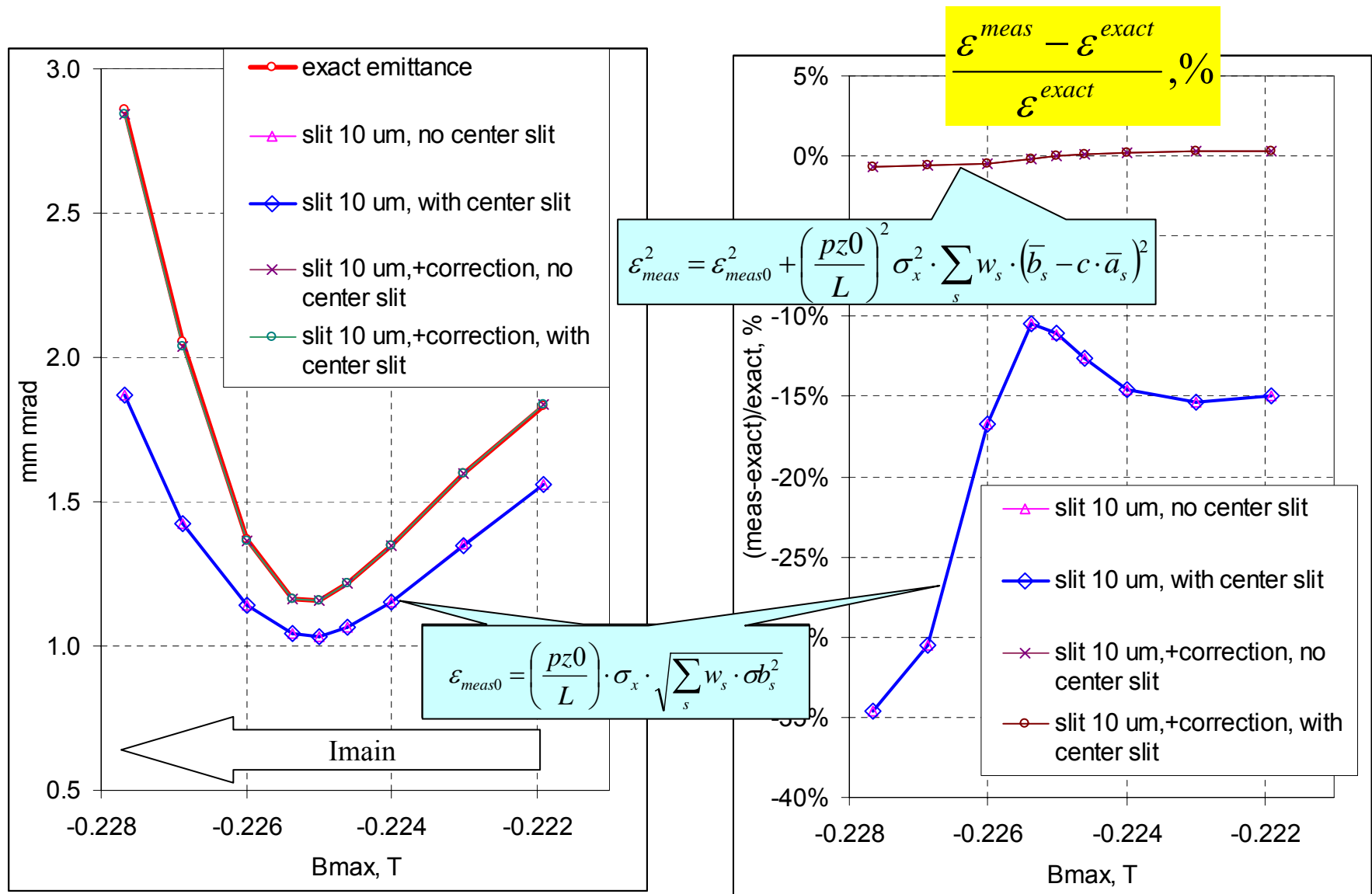
$$c = \frac{\sum_s w_s \cdot \bar{a}_s \cdot \bar{b}_s}{\sum_s w_s \cdot \bar{a}_s^2}$$

# Simulated measured emittance vs. scan step **with correction**

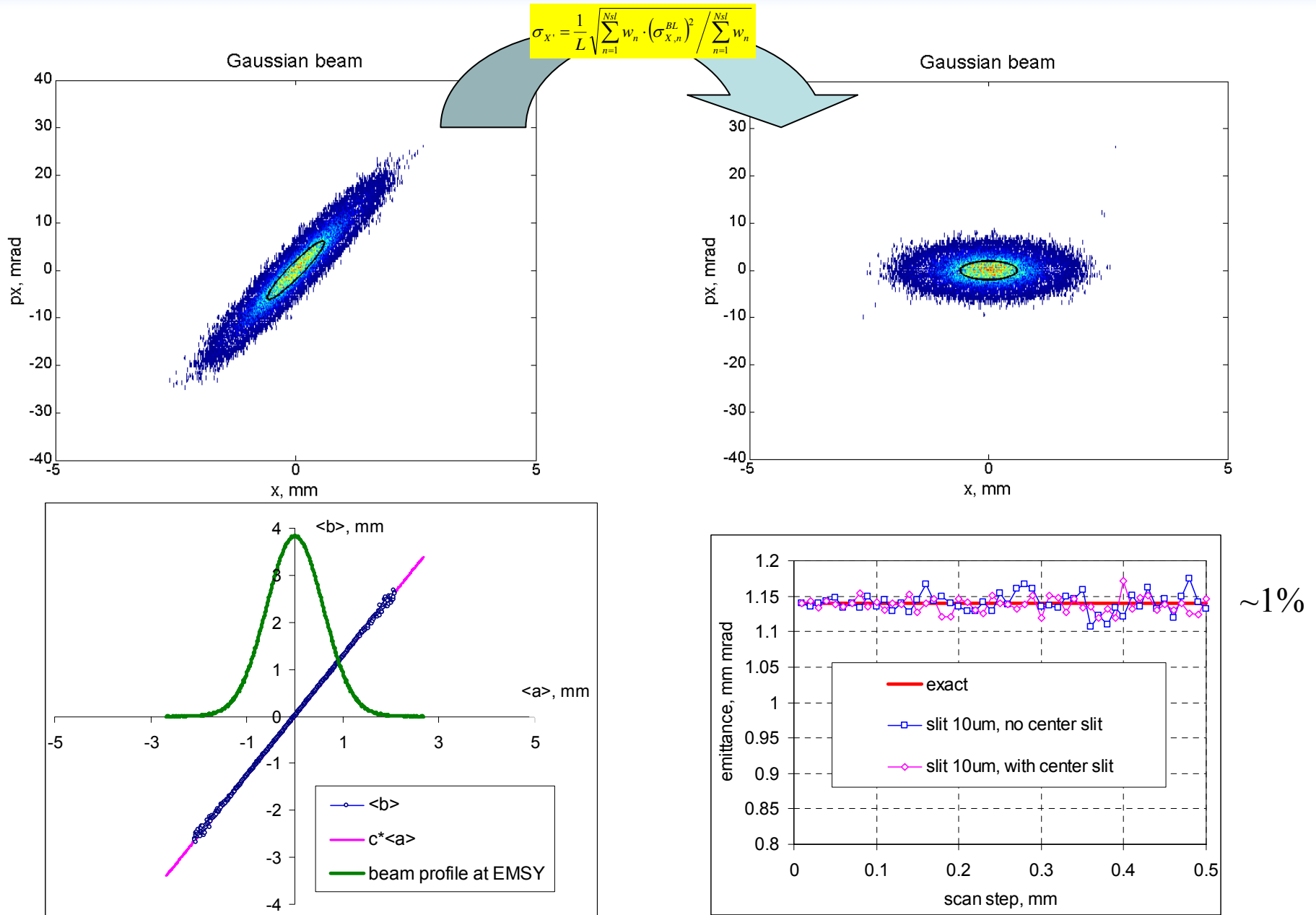


# Simulated measured emittance vs. main solenoid peak field **with correction**

Main solenoid scan (step size=slit opening=10um)

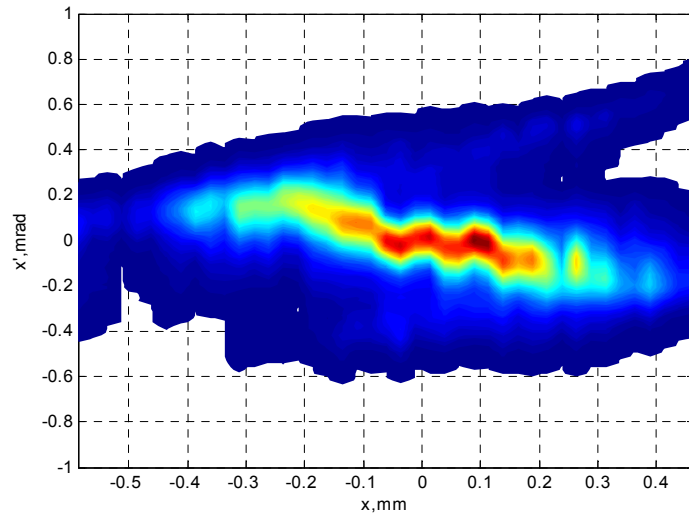
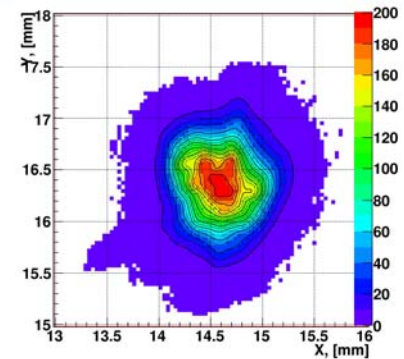
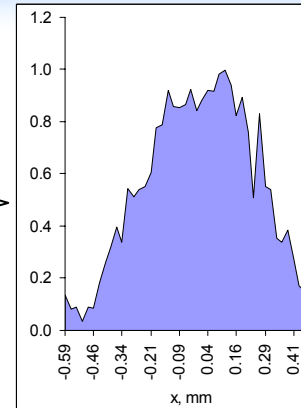
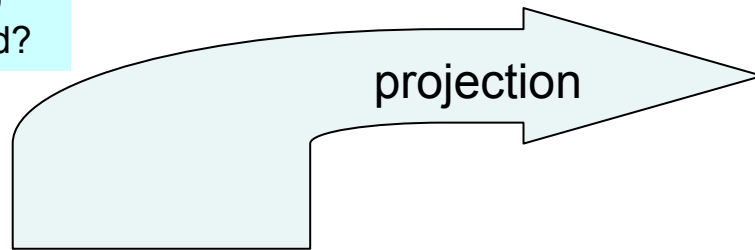


# Transverse phase space. Gaussian distribution



# Experimental data: detailed slit scan (17.08.07N)

- dx=25um
- 10um slit opening
- intensity threshold?



$$\mathcal{E}_{meas0} = \left( \frac{pz0}{L} \right) \cdot \sigma_x \cdot \sqrt{\sum_s w_s \cdot \sigma b_s^2}$$

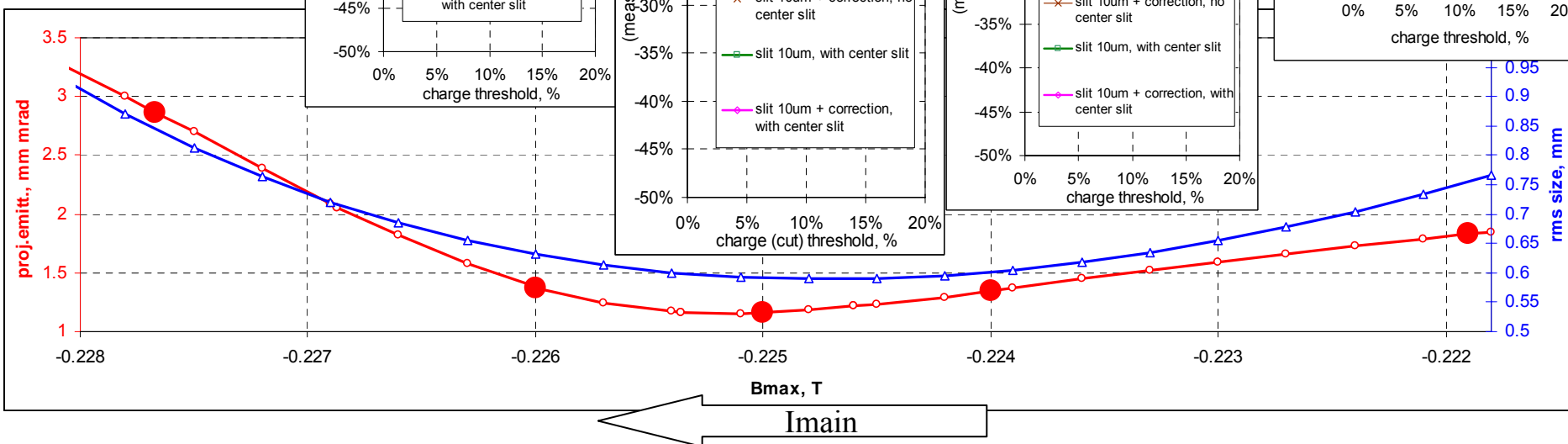
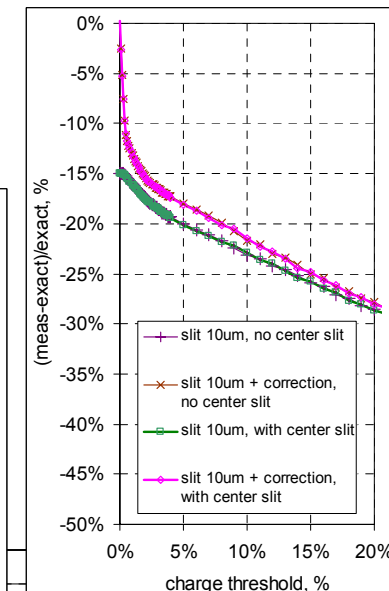
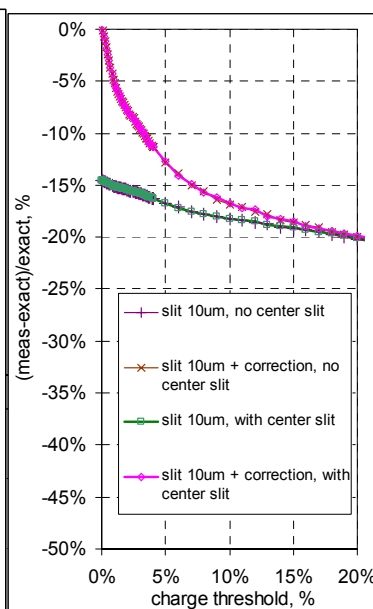
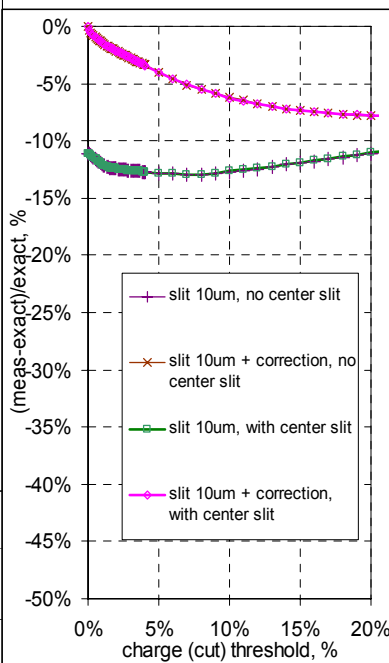
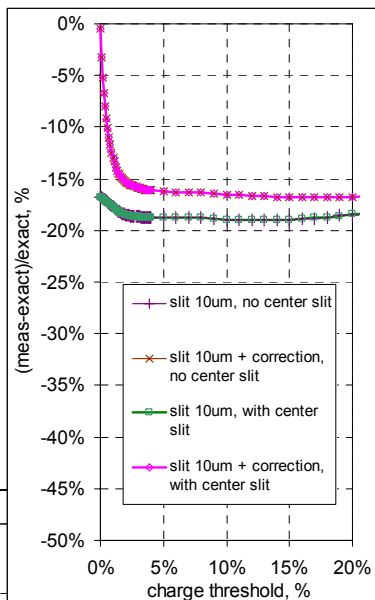
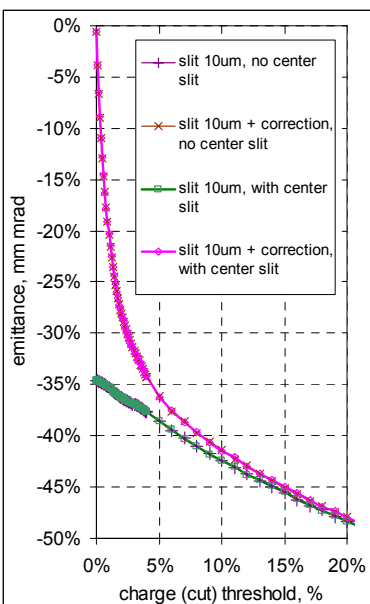
$$\mathcal{E}_{meas}^2 = \mathcal{E}_{meas0}^2 + \left( \frac{pz0}{L} \right)^2 \sigma_x^2 \cdot \sum_s w_s \cdot (\bar{b}_s - c \cdot \bar{a}_s)^2$$

$\sigma_x \rightarrow$	obtained from the beamlet sum of pixels, $\sigma_x=0.226\text{mm}$	obtained from the whole beam measurement at EMSY, $\sigma_x=0.270\text{mm}$
Direct from 2D phase space	1.08 mm mrad	1.29 mm mrad (scaled with 0.270/0.226)
Standard formula $\mathcal{E}_{meas0}$	1.05 mm mrad	<b>1.26 mm mrad</b>
+correction $\mathcal{E}_{meas}$	1.08 mm mrad	<b>1.29 mm mrad</b>

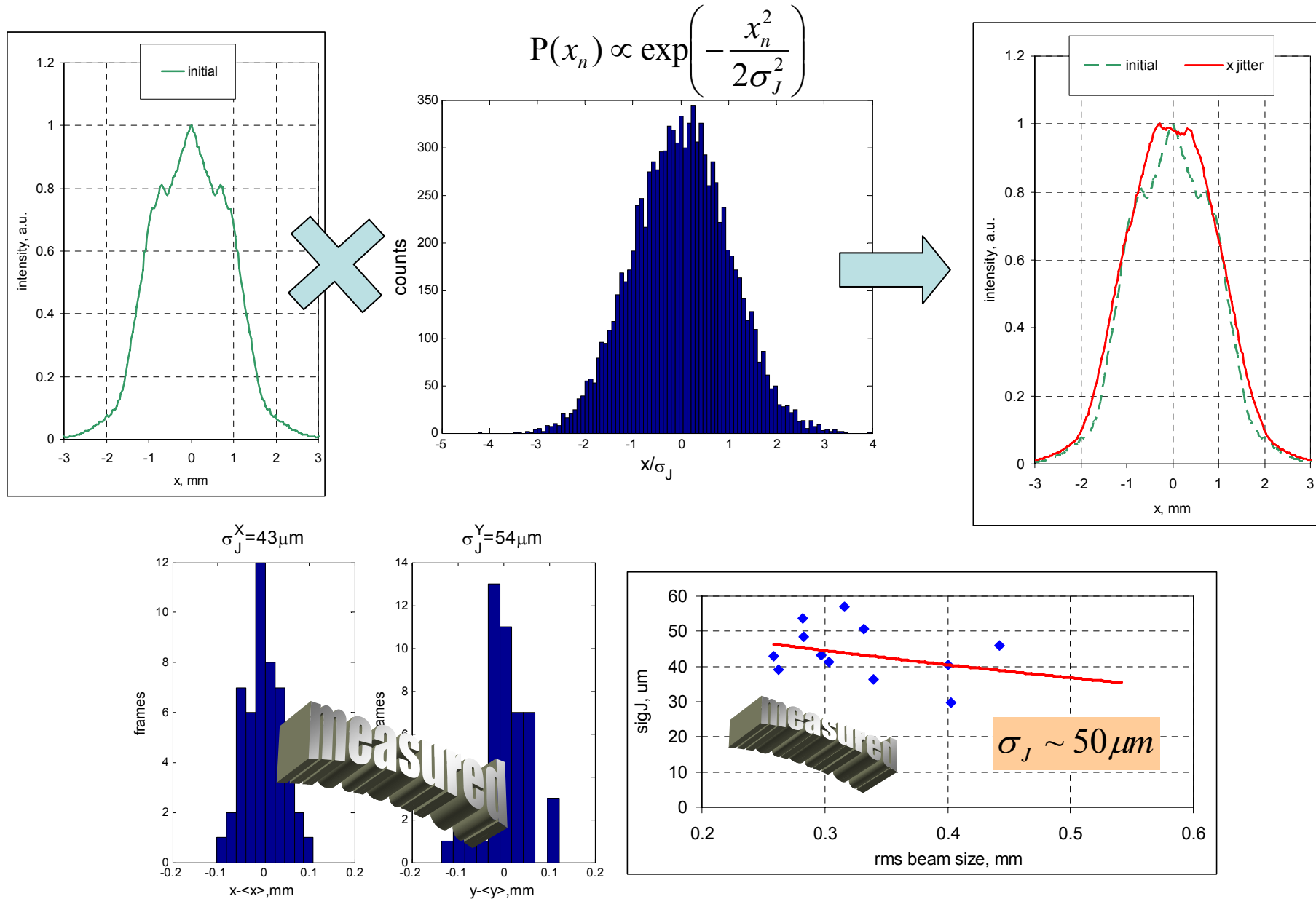


# Intensity threshold influence for various solenoid peak fields

*Main solenoid scan (step size=slit opening=10um)*



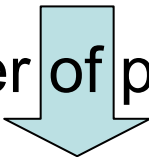
# Position jitter of electron beam



# Position jitter of electron beam

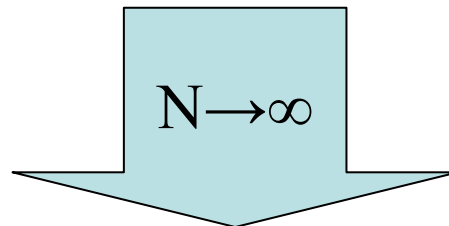
$$G(x - x_n, \sigma_x) \text{ - beam profile} \quad \times \quad P(x_n) \propto \exp\left(-\frac{x_n^2}{2\sigma_J^2}\right)$$

$N \propto$  number of pulses



$$\sigma_x^{meas} = \sqrt{\sigma_x^2 + \frac{1}{N} \sum_{n=1}^N x_n^2 - \frac{1}{N^2} \left( \sum_{n=1}^N x_n \right)^2}$$

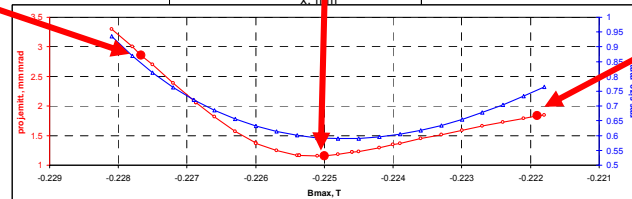
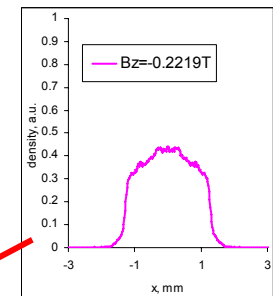
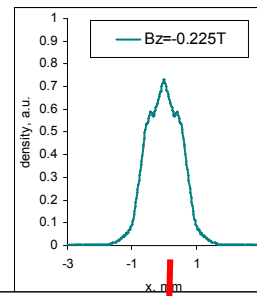
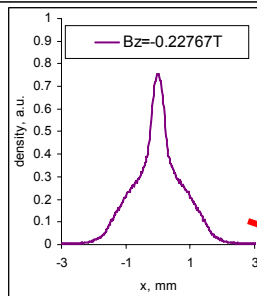
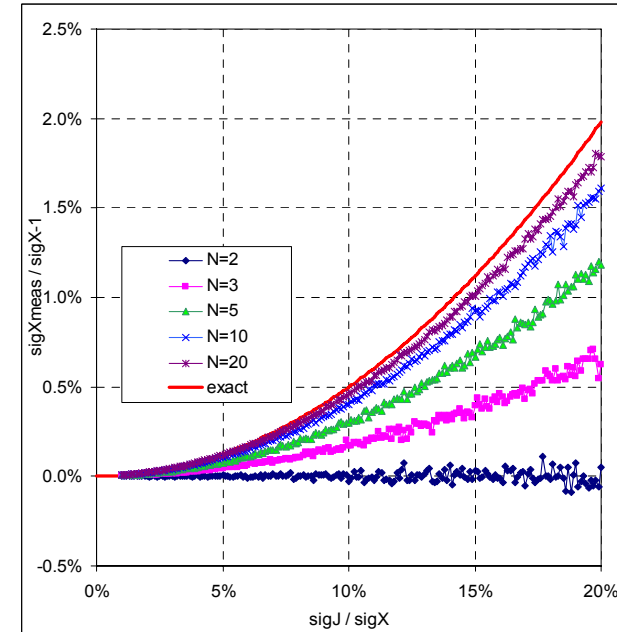
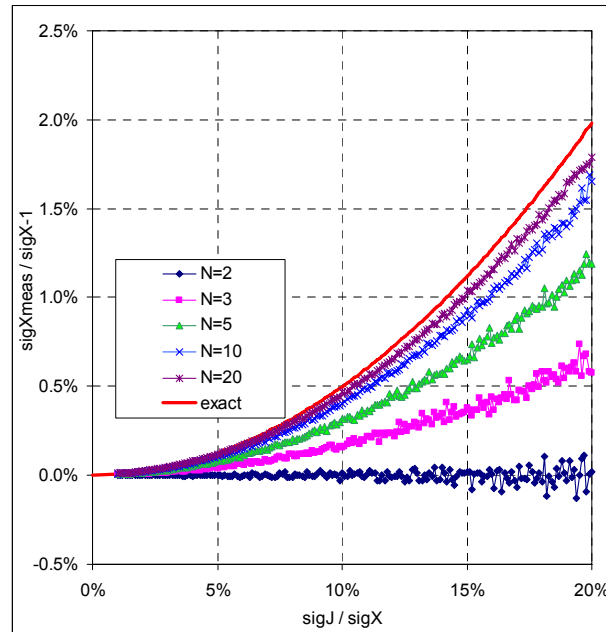
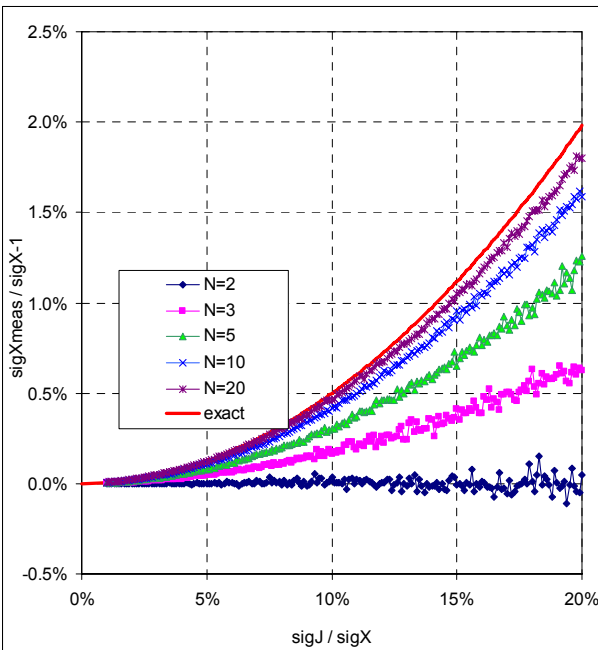
$N \rightarrow \infty$



$$\sigma_x^{meas, exact} = \sqrt{\sigma_x^2 + \sigma_J^2}$$

# Beam rms size increase due to the position jitter

Increase of the **measured** beam rms size vs. rms position jitter  $\sigma_J$



<0.5% @ 10% jitter

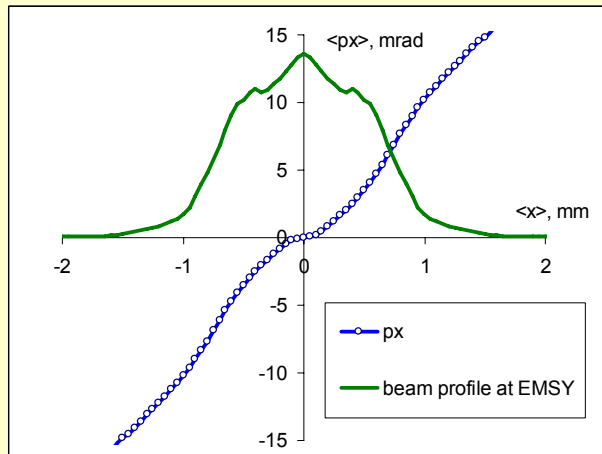
# Beam position jitter. Influence onto beamlets

RMS size of the beamlet including beam position jitter at the slit (**linear approximation**):

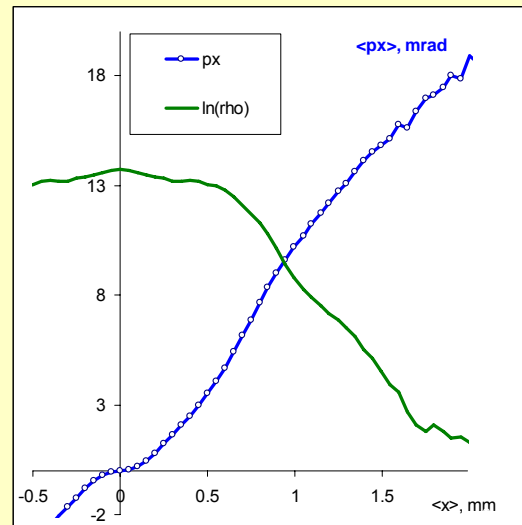
$$\sigma_b^2 = \sigma_{b0}^2 + \sigma_J^2 \cdot \left\{ \alpha^2 \cdot \left[ 1 - \left( \frac{d \ln \rho}{dx} \right)^2 \sigma_J^2 \right] + \frac{d\sigma_b^2}{dx} \frac{d \ln \rho}{dx} \right\}$$

BL size increase due to the transv.momentum gradient

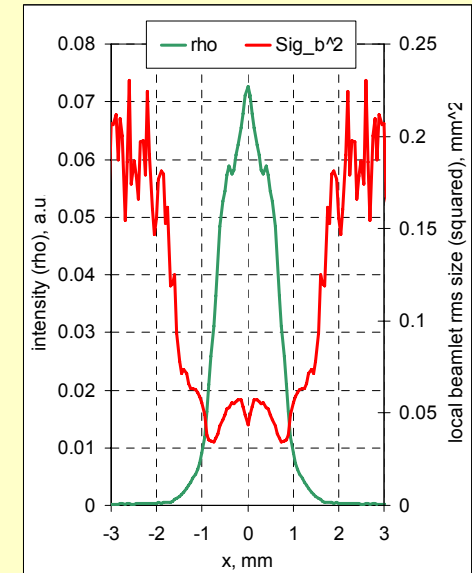
$$\alpha = \frac{L}{p_z} \cdot \frac{dp_x}{dx}$$



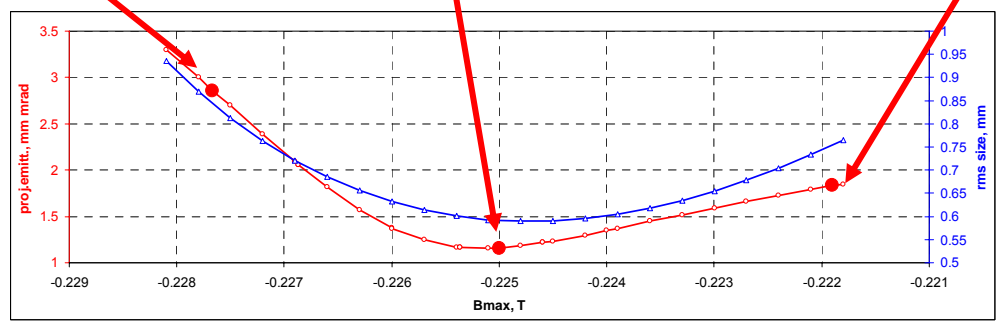
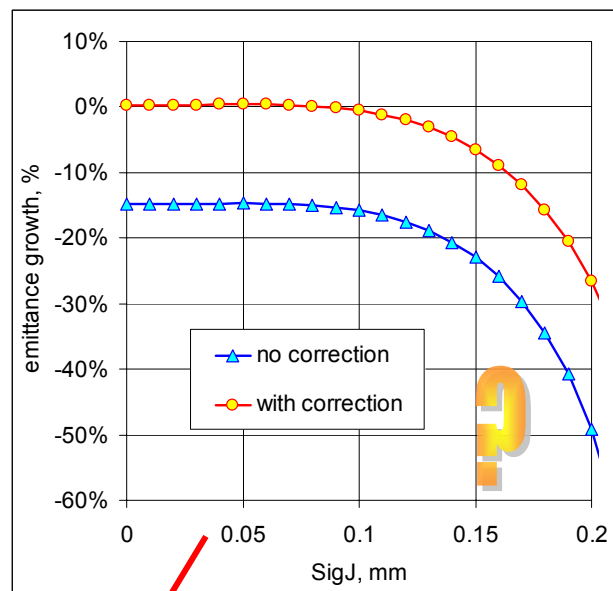
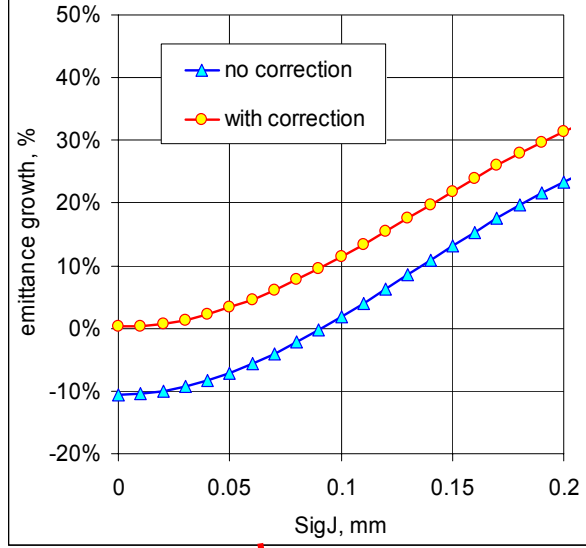
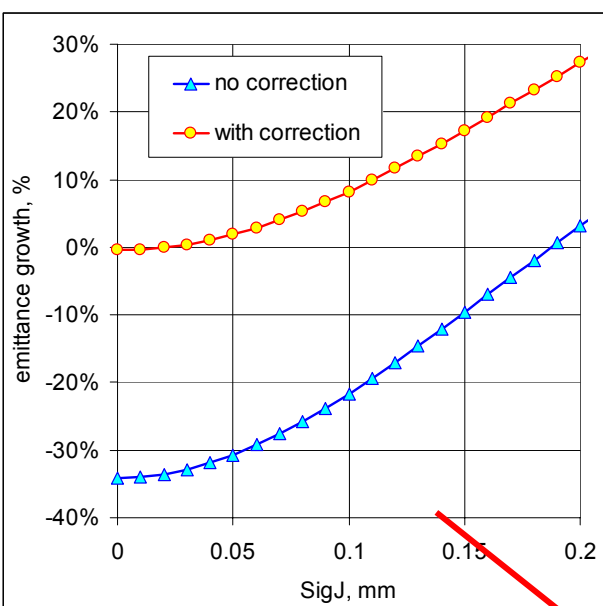
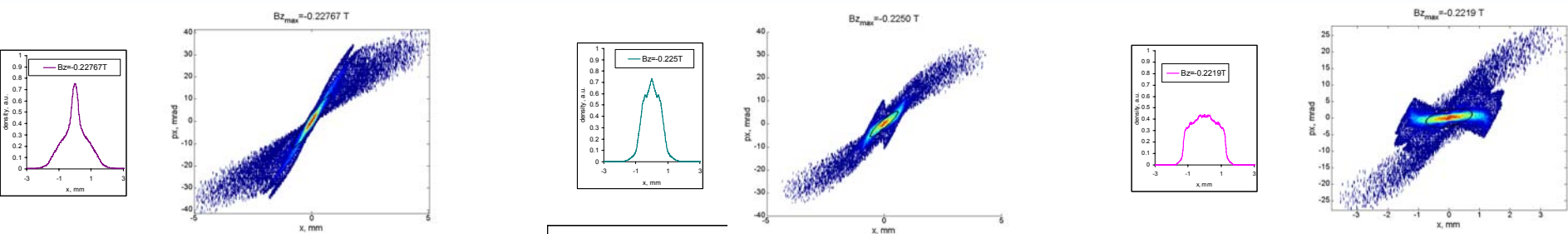
Change of the beamlet center position



Beamlet size / beam profile gradient

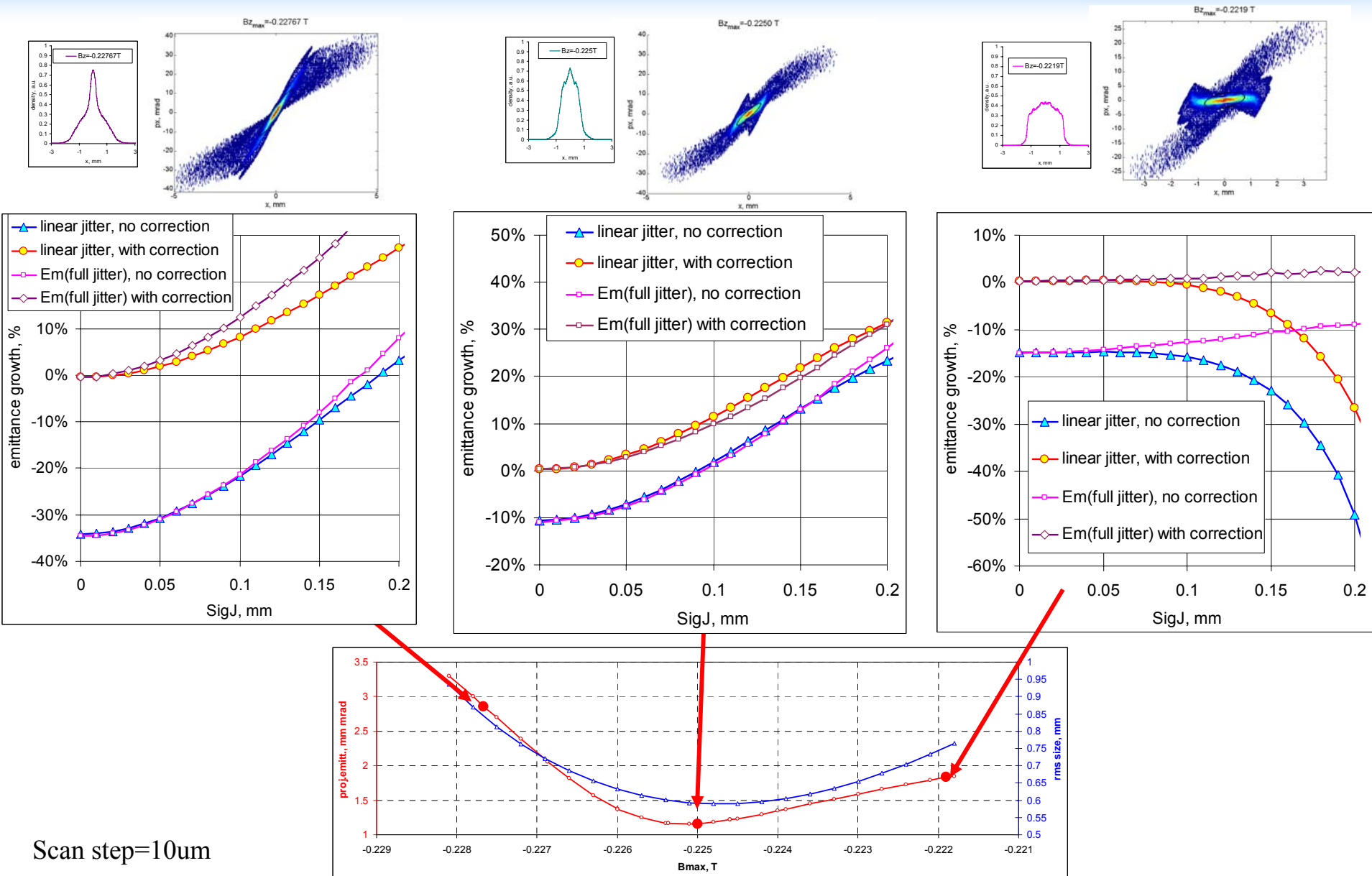


# Measured emittance increase due to the **linear** beam position jitter



Scan step=10um

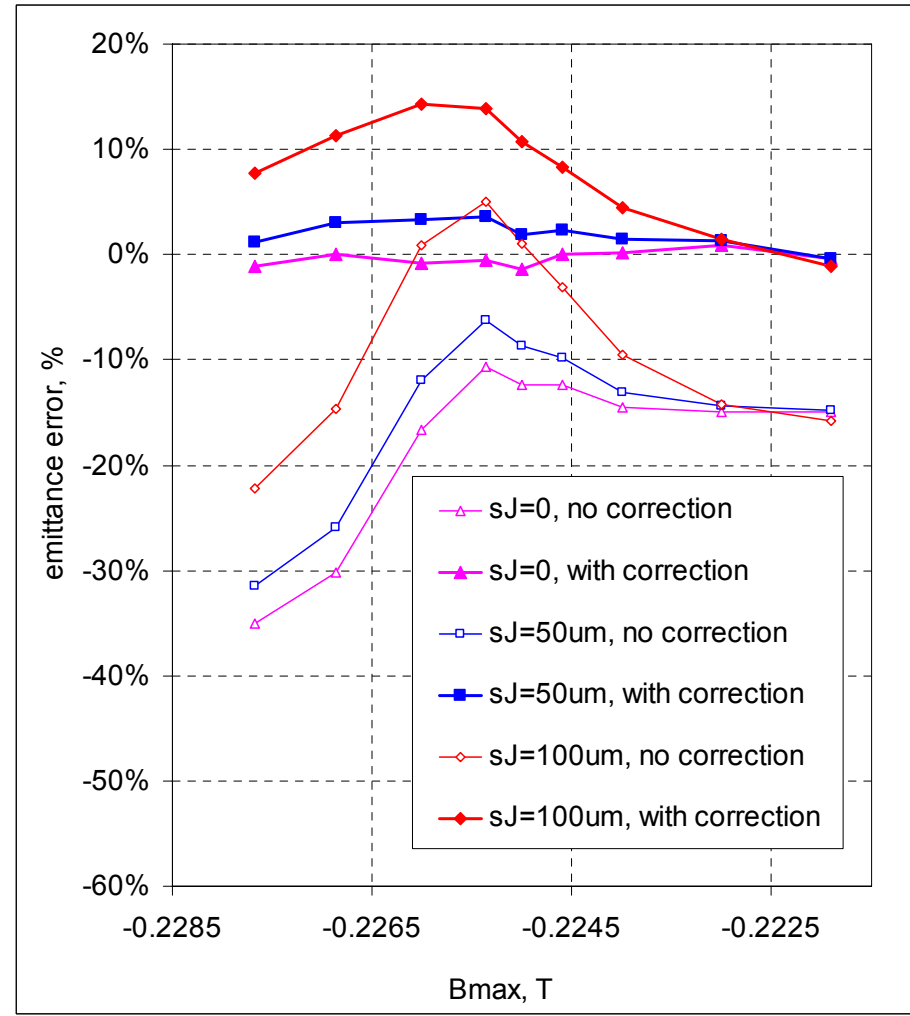
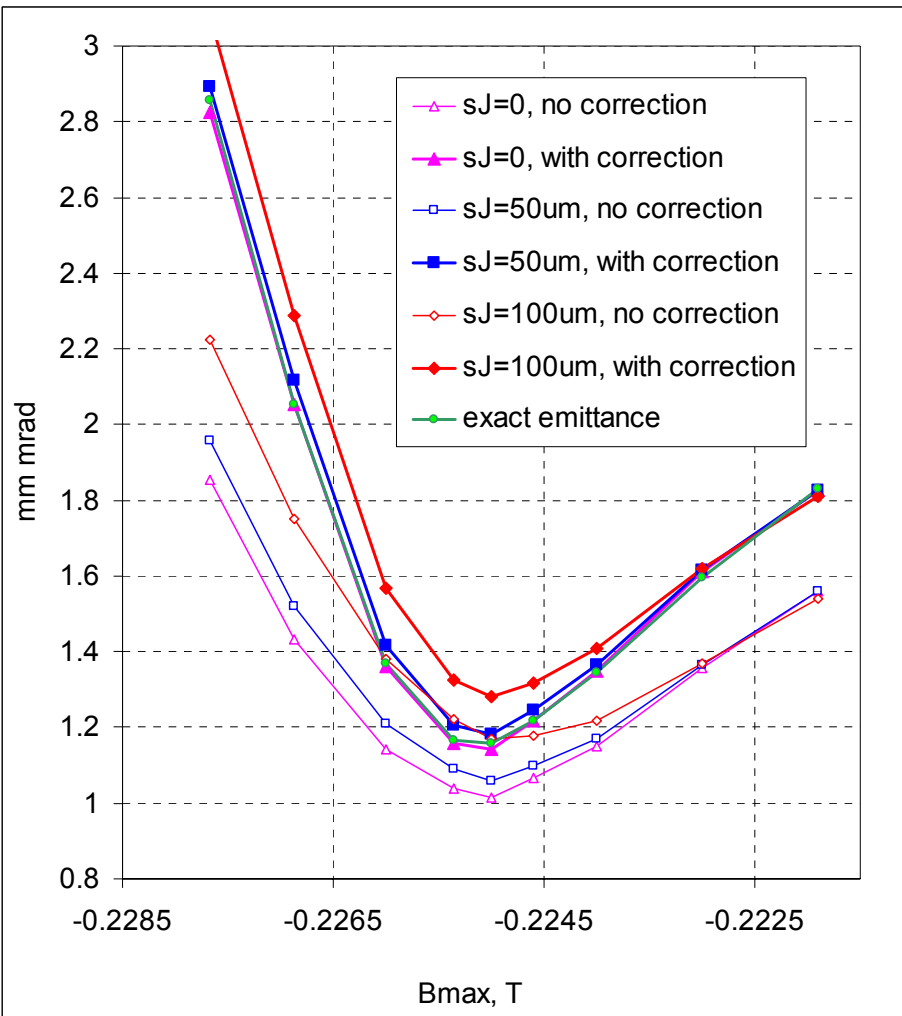
# Measured emittance increase due to the beam position jitter



Scan step=10um

# Slit scan X Beam position jitter=Measured emittance

Scan step=100 $\mu$ m, charge cut threshold=0%





# Conclusions

- Factors affecting slit scan measurements:

Factor	Effect on measured emittance	Solution/remark
Phase space nonlinearity	-10..-30%	correction term experimentally $\sim -2..-3\%$
Scan step dx	$\sim 1\%$ if $dx < 200\mu\text{m}$	$dx \sim 100\mu\text{m}$
Beam position jitter	+5% @ 50 $\mu\text{m}$ rms jitter	<ul style="list-style-type: none"><li>improve stability</li><li>?measurement with synchronized BPM?</li></ul>

- Combined** factors ( $dx=100\mu\text{m}$  X 50 $\mu\text{m}$  position jitter) resulted in **0...+4%** measured emittance overestimation
- There is an influence of the **intensity (charge) cut** (not discussed here) resulting in the emittance underestimation (i.e. -5..-30% for 5% charge cut)