

Kathlynne Tullney

# Limits for Spin-Dependent Short-Range Interaction of Axion-Like Particles



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# Outline

- Motivation
- Principle of measurements
- Experimental setup
- Results
- Summary

## The strong CP-Problem

The non-trivial vacuum structure of QCD predicts violation of CP-symmetry:

$$L_\theta = \bar{\theta} \frac{g^2}{32\pi^2} G_{\mu\nu}^b \tilde{G}_b^{\mu\nu}$$

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**Original proposal for Axion** (*R. Peccei, H. Quinn PRL 38(1977), 1440*)

as possible solution to the „strong CP-Problem“ that cancels the CP violating term in the QCD.

$$L_a = \xi \frac{a}{f_a} \frac{g^2}{32\pi^2} G_{\mu\nu}^b \tilde{G}_b^{\mu\nu}$$

$$\langle a \rangle = -f_a \frac{\bar{\theta}}{\xi}$$

with:  $m_a \propto \frac{1}{f_a}$

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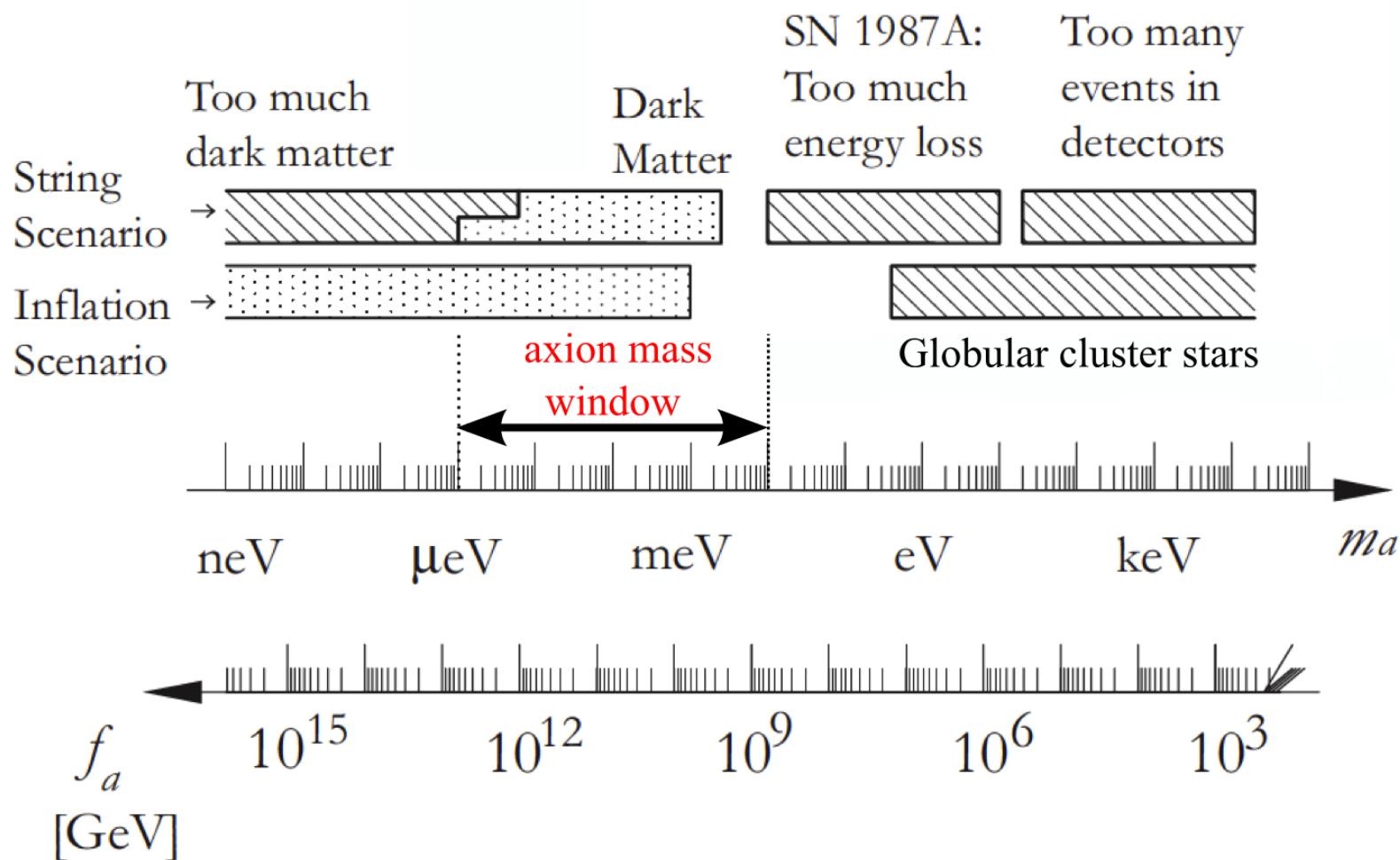
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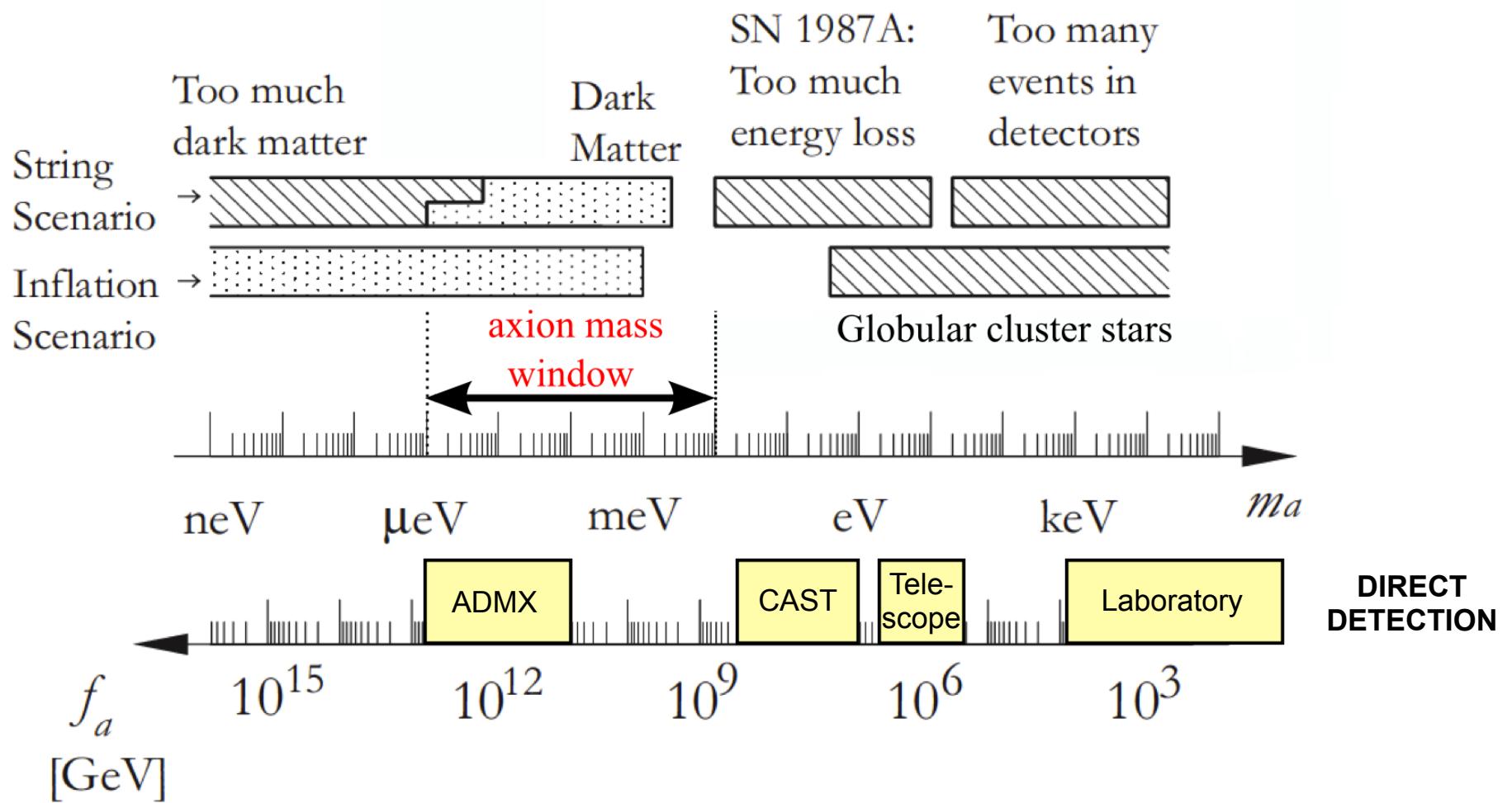
**AXIONS:** Light and weak interacting particles.

**Modern Interest:** Dark Matter candidate.

# Axion Mass



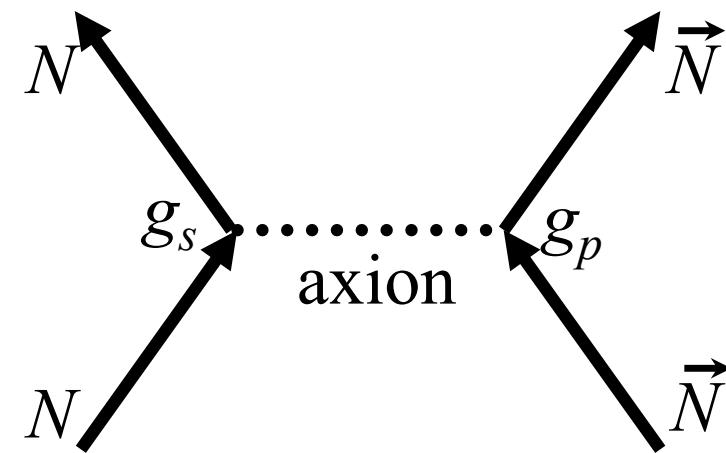
# Axion Mass



## Axion Potential:

Yukawa type potential with monopole-dipole coupling [1]

$$V(r) = \kappa \hat{n} \cdot \vec{\sigma} \left( \frac{1}{\lambda r} + \frac{1}{r^2} \right) e^{-r/\lambda}$$

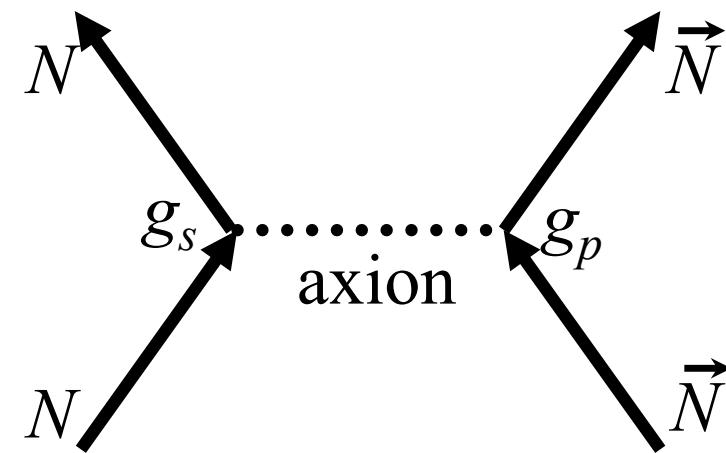


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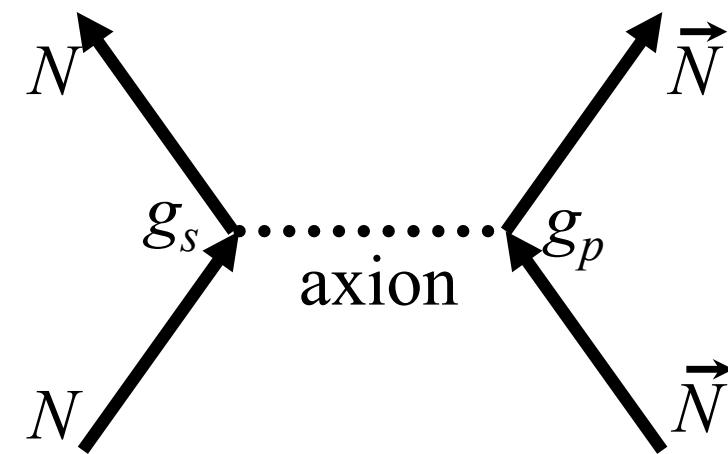


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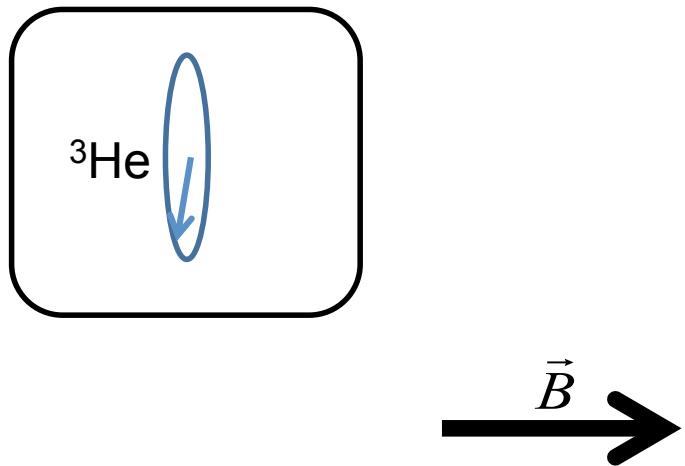
⇒ Indirect search of the axion via the axion potential in the range of the „axion mass window“:

$$\boxed{10^{-6} \text{ eV} < m_a < 10^{-2} \text{ eV}}$$

$$10^{-5} \text{ m} < \lambda < 10^{-1} \text{ m}$$

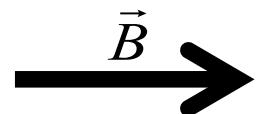
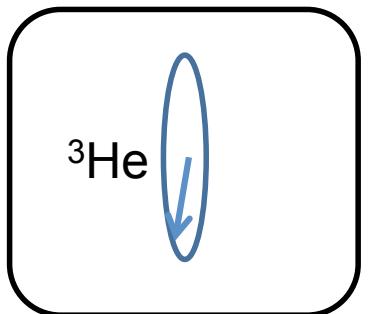
# Principle of measurements

How to measure?



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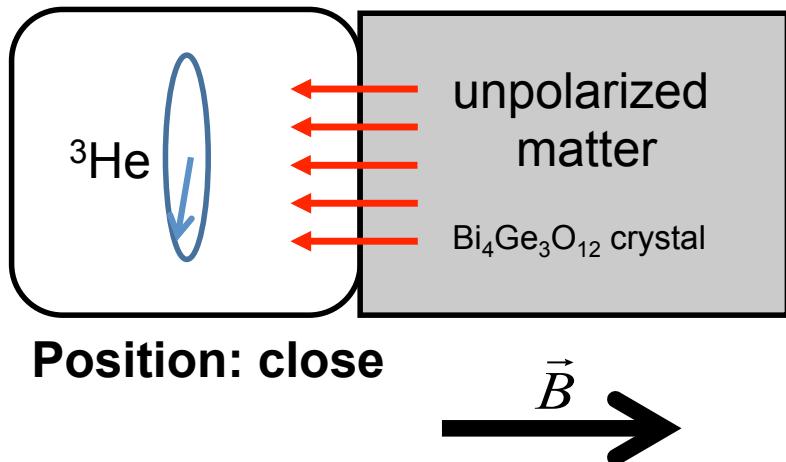
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$$\omega_{\text{L,He}}(t) = \gamma_{\text{He}} \cdot B(t)$$

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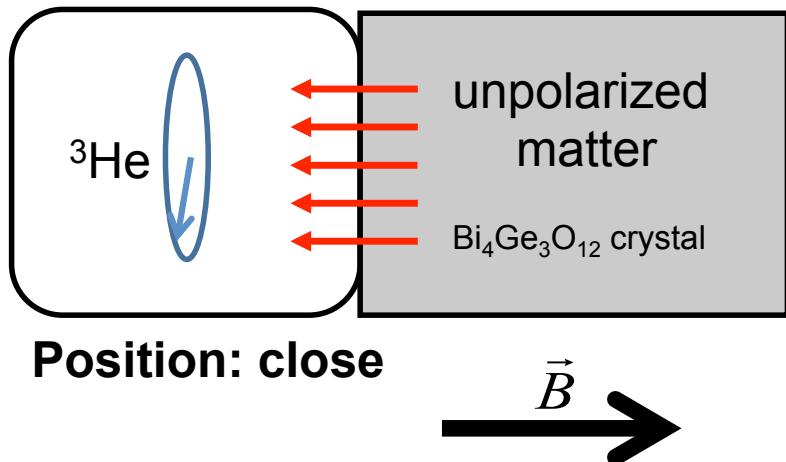
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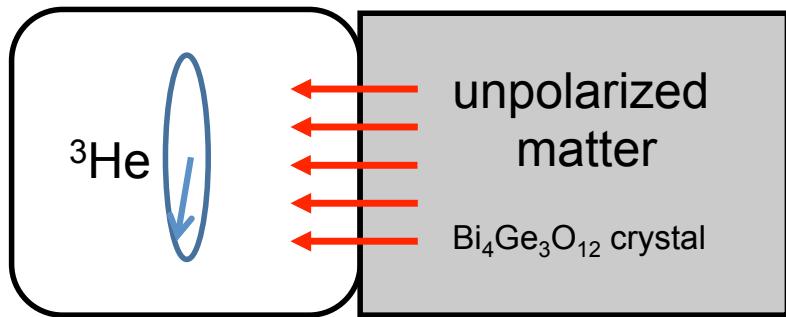
$$\omega_{\text{close}}(t) = \omega_{\text{L,He}}(t) + \omega_{\text{sp}}$$

with:  $\omega_{\text{L,He}}(t) = \gamma_{\text{He}} \cdot B(t)$

$$\omega_{\text{sp}} = 2\pi \cdot v_{\text{sp}} = 2 \cdot \bar{V} / \hbar$$

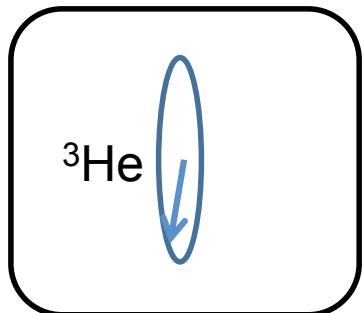
# Principle of measurements

## How to measure?



Position: close

$$\vec{B} \rightarrow$$



Position: distant

$$\omega_{\text{close}}(t) = \omega_{L,\text{He}}(t) + \omega_{\text{sp}}$$

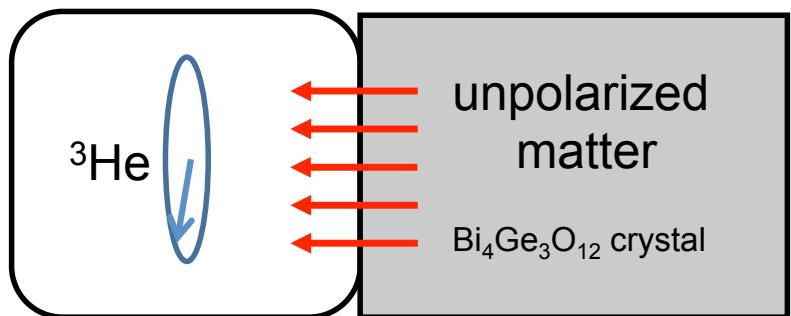
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$$\omega_{\text{distant}}(t) = \omega_{L,\text{He}}(t)$$

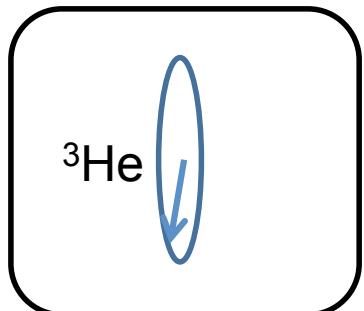
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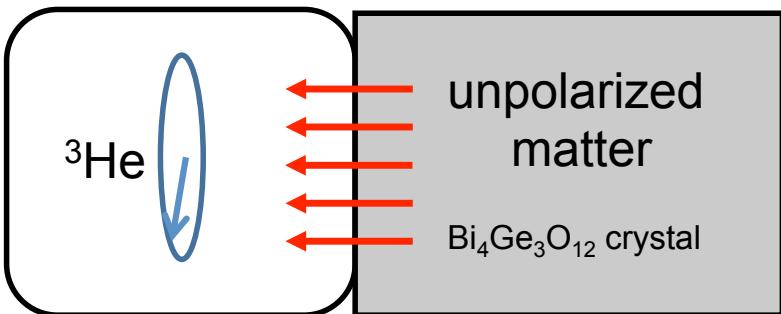
$$\omega_{\text{sp}} = 2\pi \cdot \nu_{\text{sp}} = 2 \cdot \bar{V} / \hbar$$

$$\omega_{\text{distant}}(t) = \omega_{L,\text{He}}(t)$$

$$\Rightarrow \omega_{\text{sp}} = \omega_{\text{close}}(t) - \omega_{\text{distant}}(t)$$

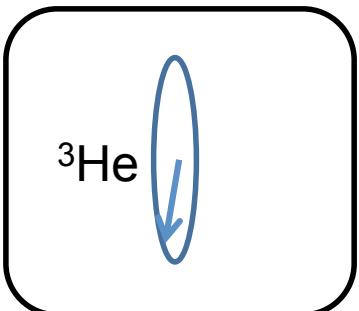
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Position: close

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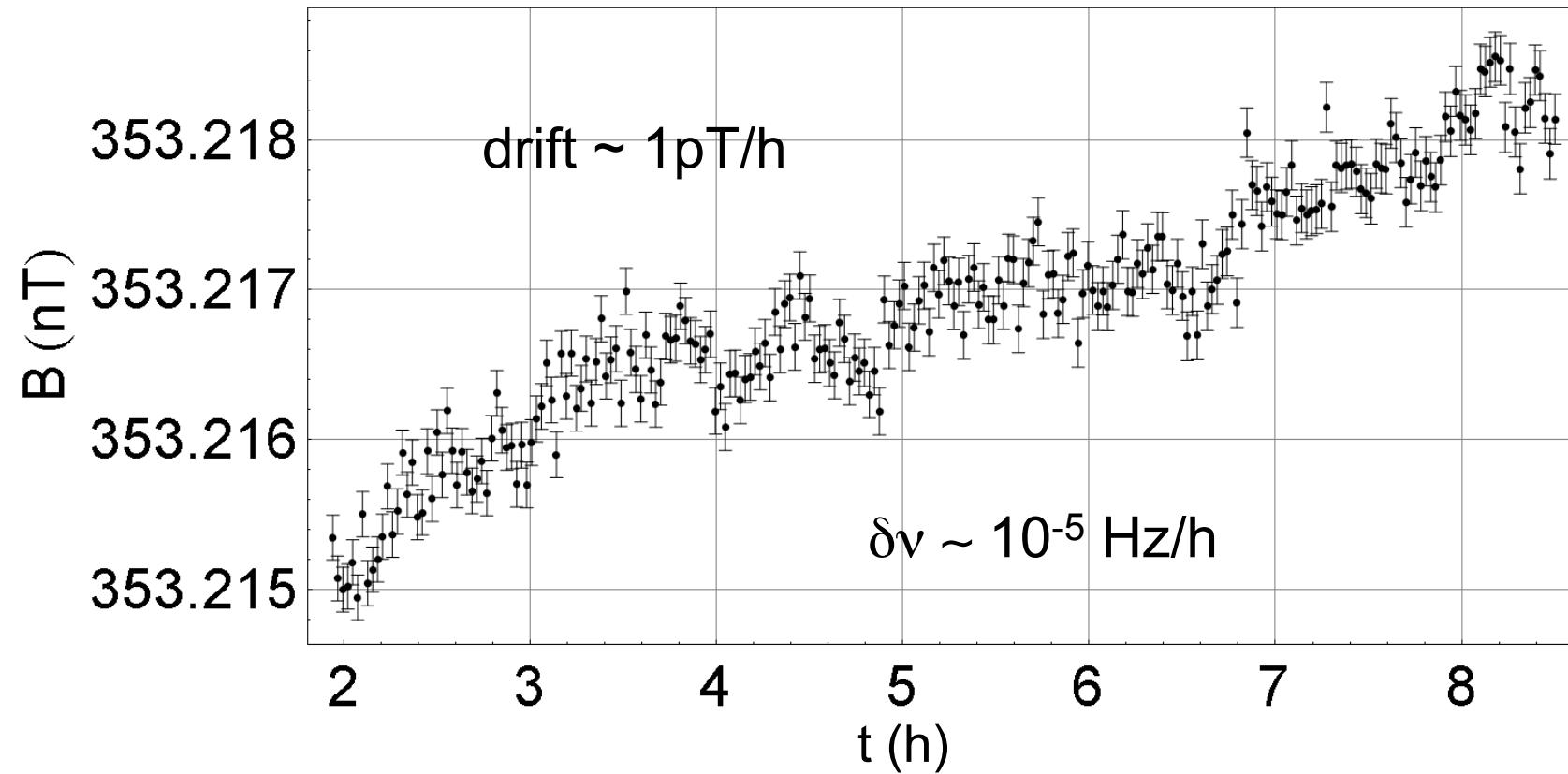
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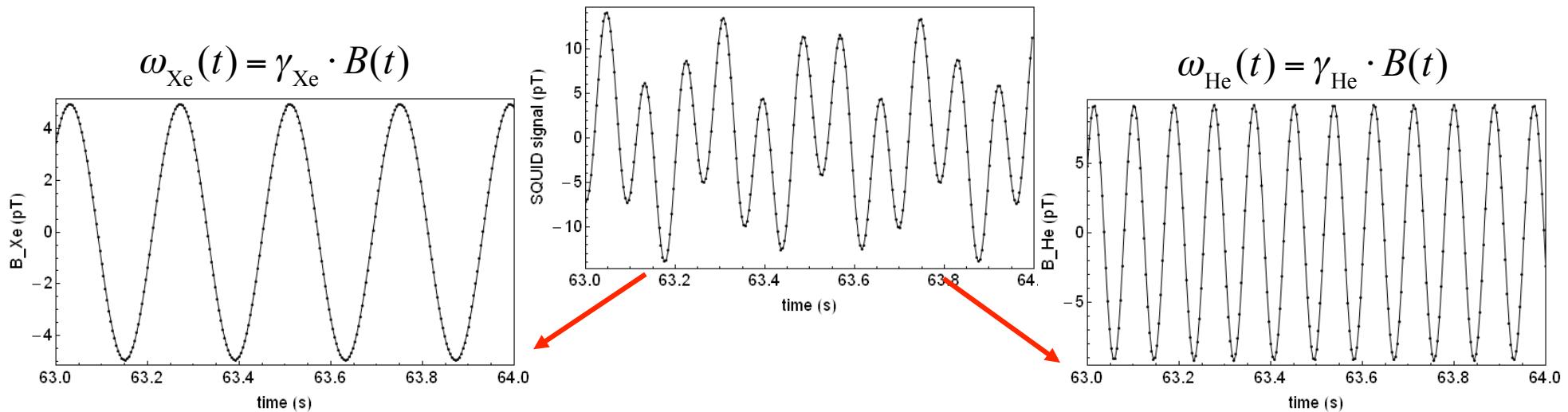
**Requirement:**  $\omega_{L,\text{He}}(t) = \text{const.}$

# Principle of measurements



# Principle of measurements

## ${}^3\text{He}/{}^{129}\text{Xe}$ Co-magnetometer

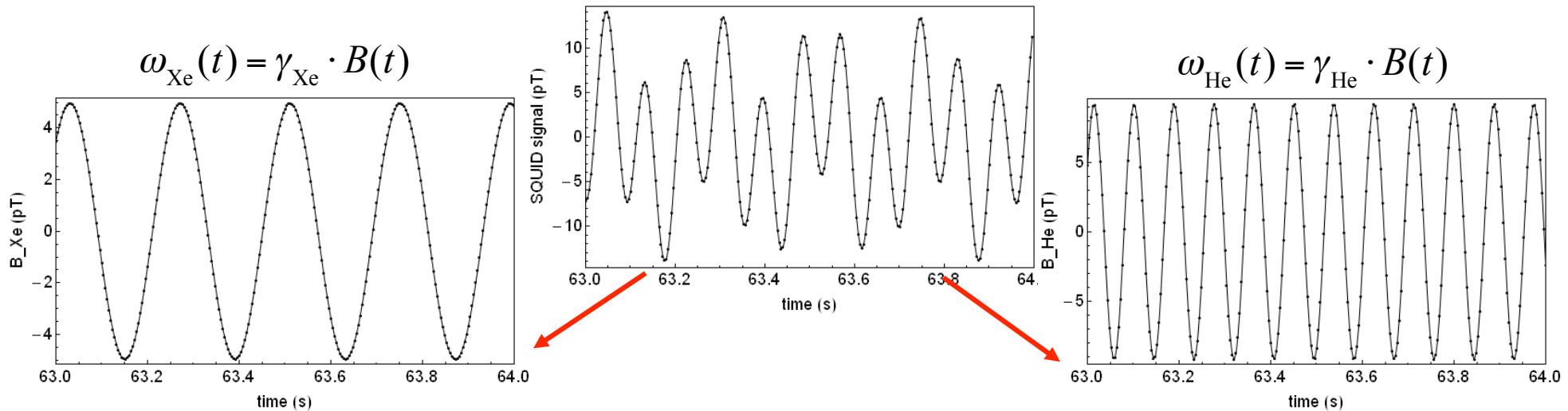


Elimination of magnetic field drifts (Zeeman-Term):

$$\text{Frequency difference: } \Delta\omega = \omega_{\text{He}} - \frac{\gamma_{\text{He}}}{\gamma_{\text{Xe}}} \omega_{\text{Xe}} = \left( \gamma_{\text{He}} - \frac{\gamma_{\text{He}}}{\gamma_{\text{Xe}}} \cdot \gamma_{\text{Xe}} \right) \cdot B(t) \stackrel{!}{=} 0$$

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## ${}^3\text{He}/{}^{129}\text{Xe}$ Co-magnetometer



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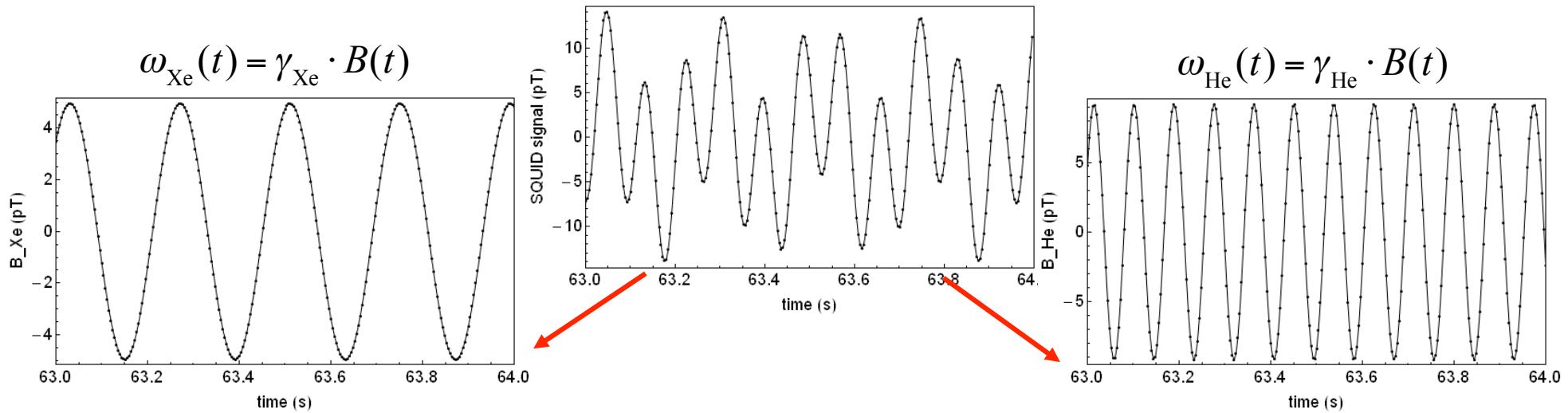
$$\Phi(t) = \int_0^t \omega(t') dt'$$

Phase difference:

$$\Delta\Phi(t) = \Phi_{\text{He}}(t) - \frac{\gamma_{\text{He}}}{\gamma_{\text{Xe}}} \cdot \Phi_{\text{Xe}}(t) = \Phi_0 \stackrel{!}{=} \text{const.}$$

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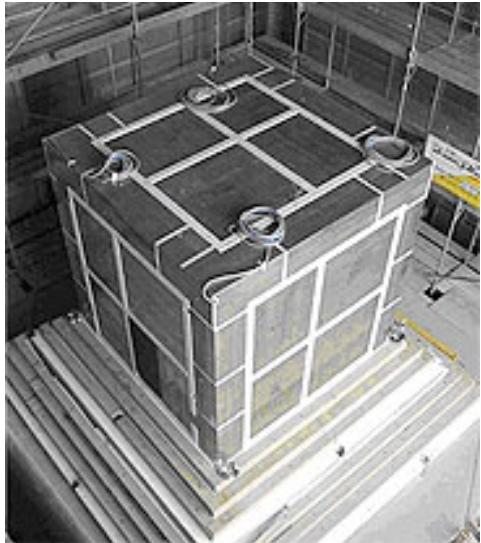
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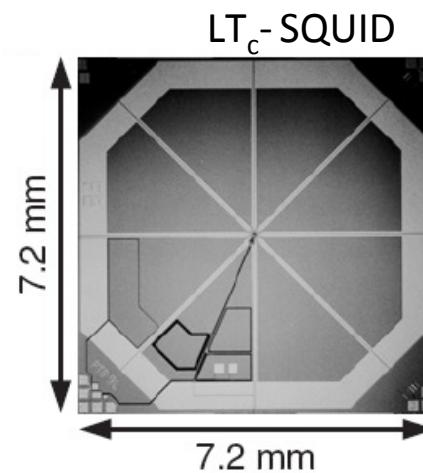
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# Experimental Setup



7 layered magnetically  
shielded room  
(residual field < 1 nT)

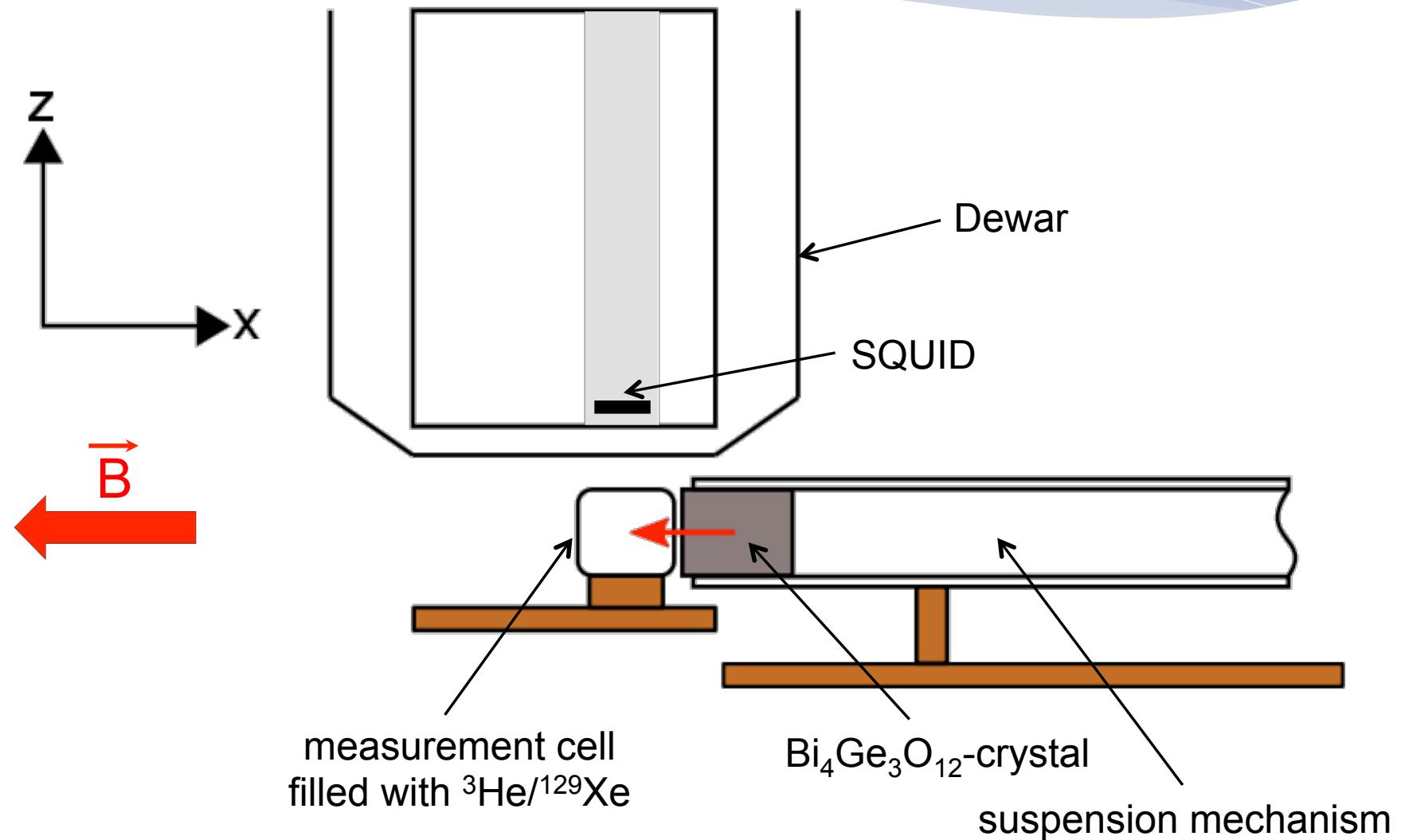
J. Bork, et al., Proc. Biomag 2000, 970 (2000).



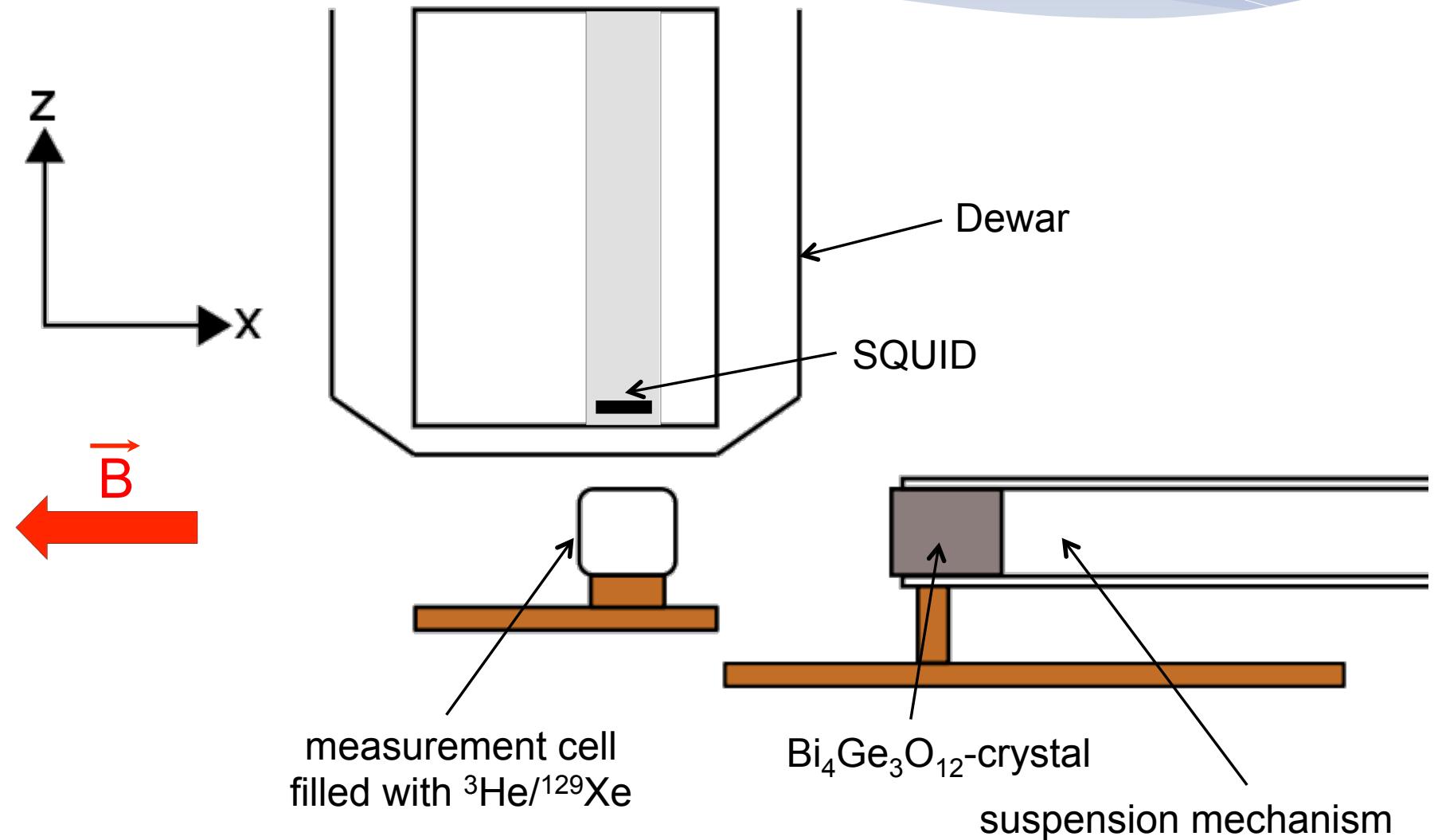
magn. guiding field  $\approx 350$  nT (Helmholtz-coils)

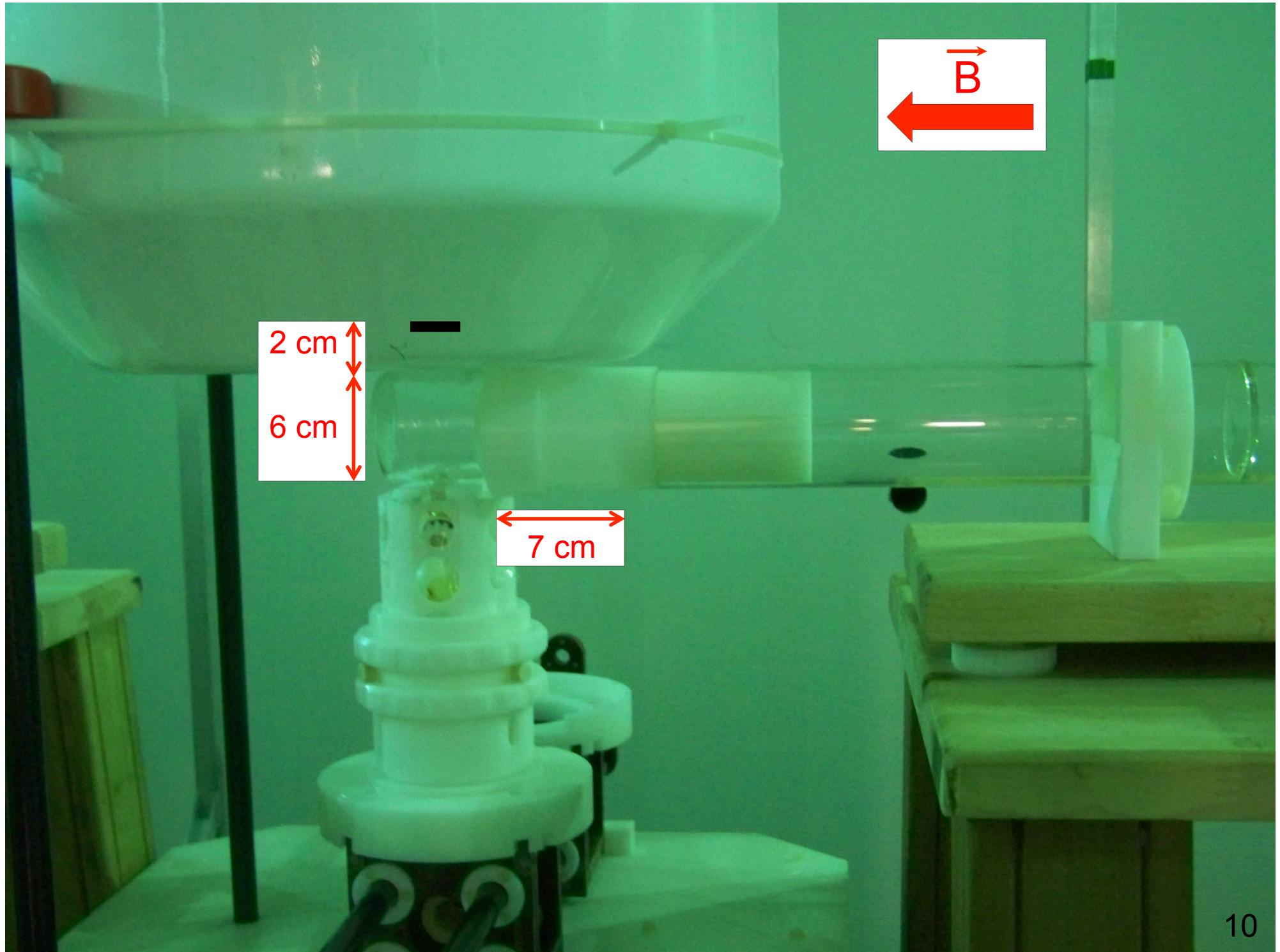
$$|\vec{\nabla}B_{x,y,z}| \approx 20 \text{ pT/cm}$$

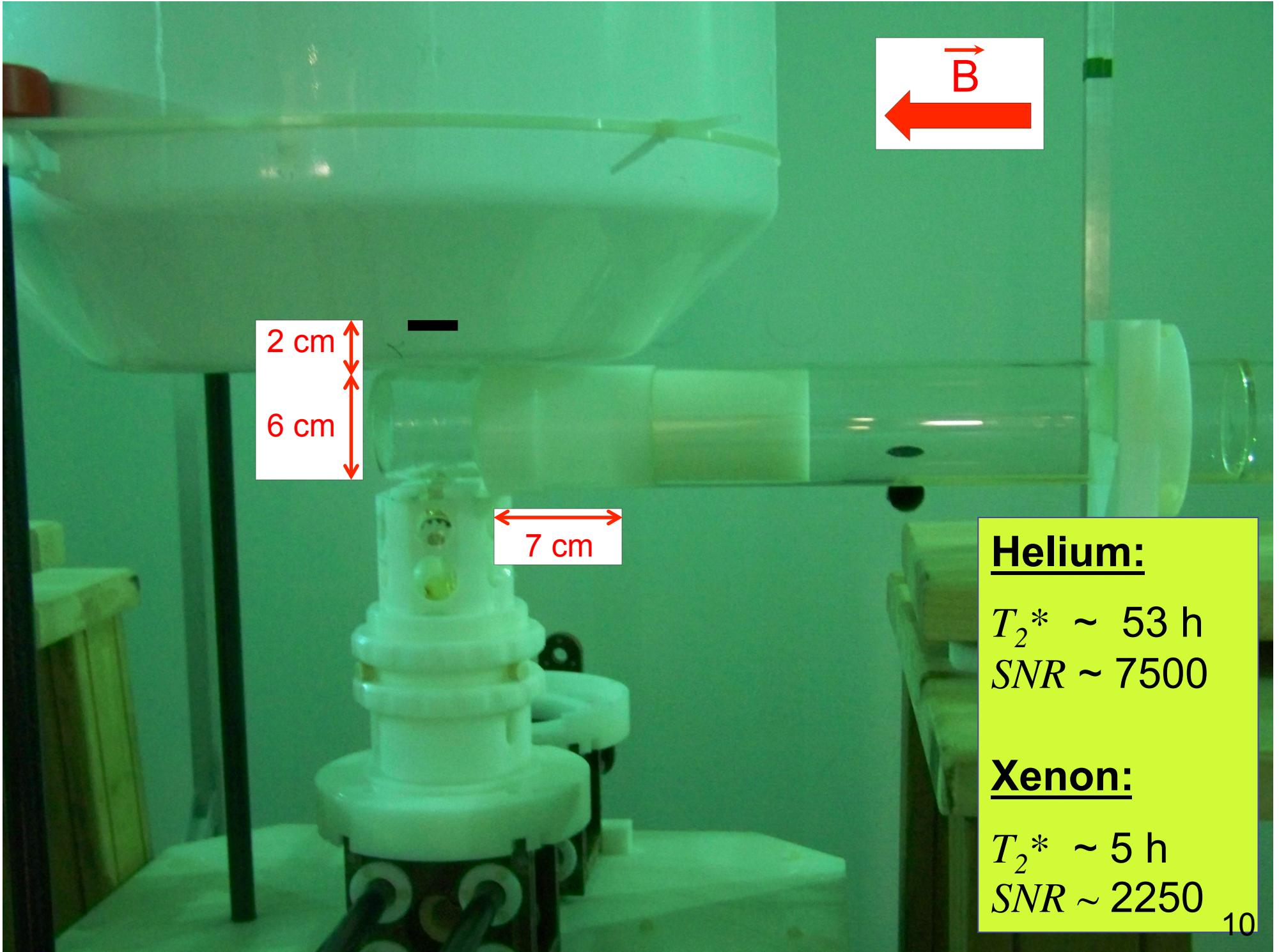
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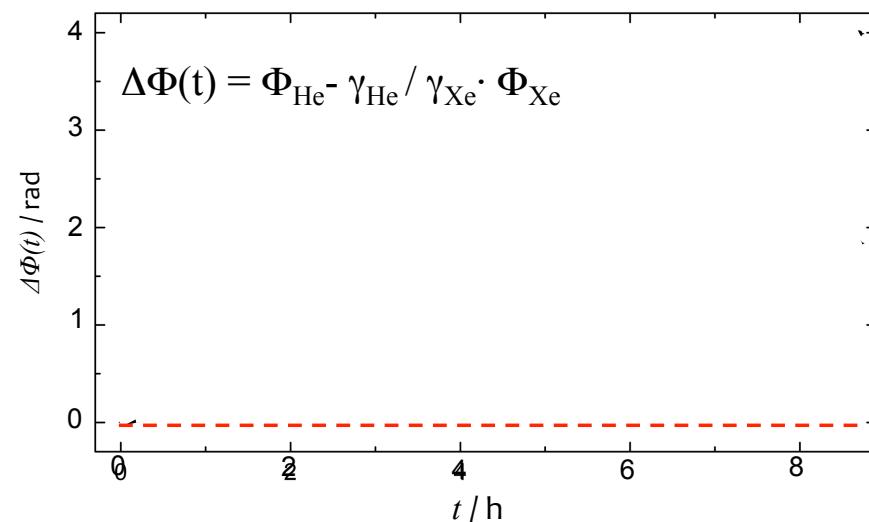




# Data Analysis

1. To cancel magnetic field influence we calculate the weighted phase difference:

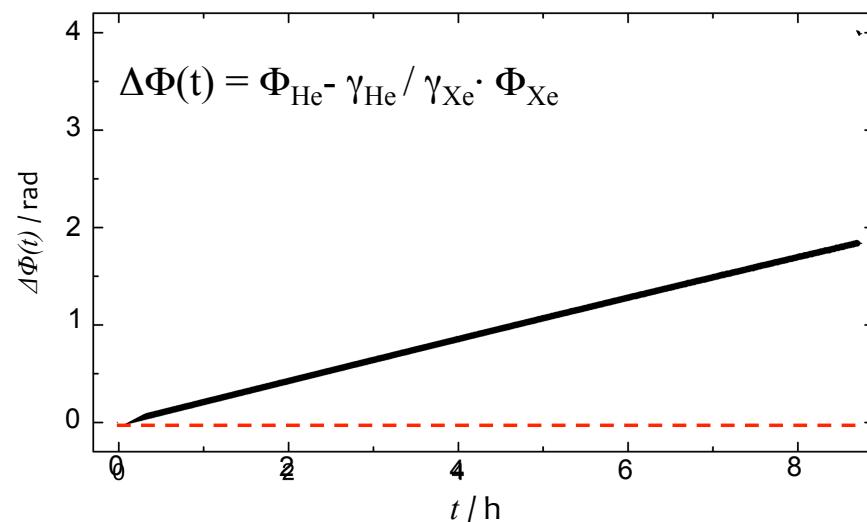
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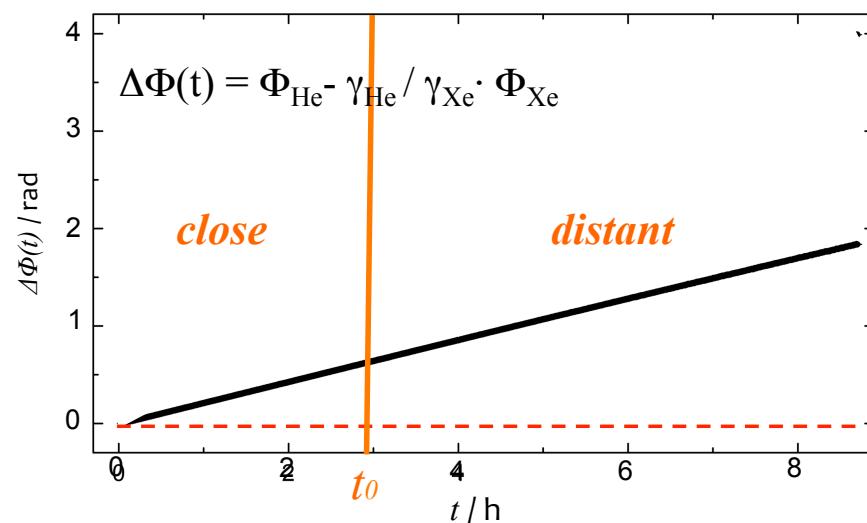
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$$f(t) = c + a_{\text{lin}} \cdot t + a_{\text{He}} \cdot e^{-t/T_{2,\text{He}}^*} + a_{\text{Xe}} \cdot e^{-t/T_{2,\text{Xe}}^*} + \Delta\omega_{\text{sp}} \cdot t \cdot H(t - t_0)$$



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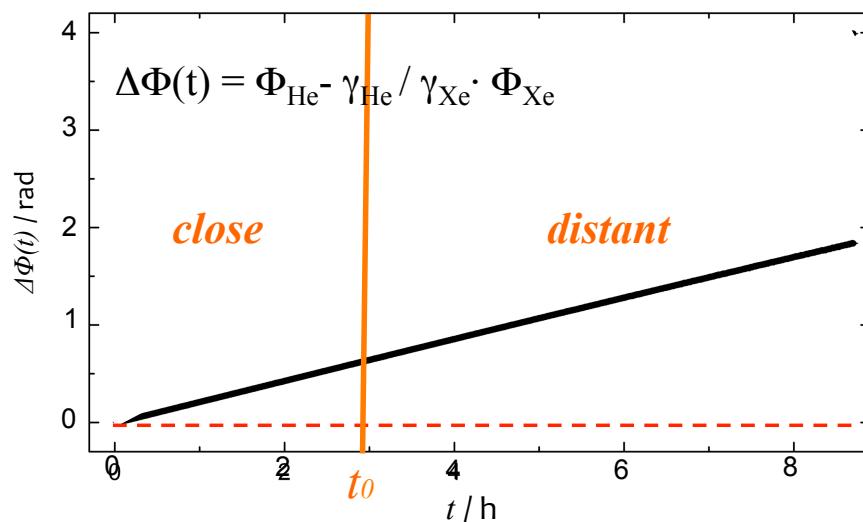
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$$\Rightarrow \Delta\nu_{sp} = \frac{\Delta\omega_{sp}}{2\pi(1 - \gamma_{He}/\gamma_{Xe})}$$



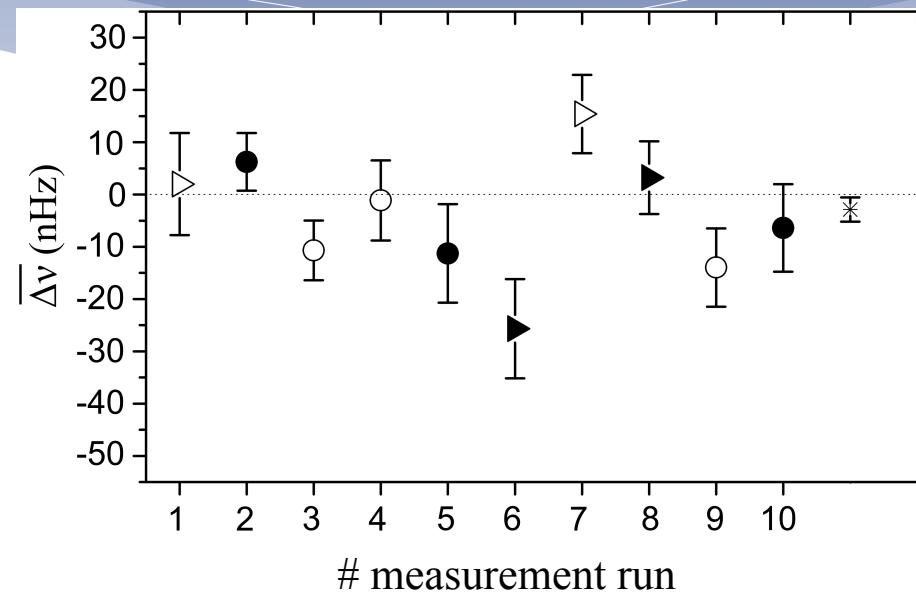
# Summary Results

## September 2010:

10 measurements (~9 hours)

gap = 2.2 mm

sample:  $\text{Bi}_4\text{Ge}_3\text{O}_{12}$  with:  $\rho = 7.13 \text{ g/cm}^3$



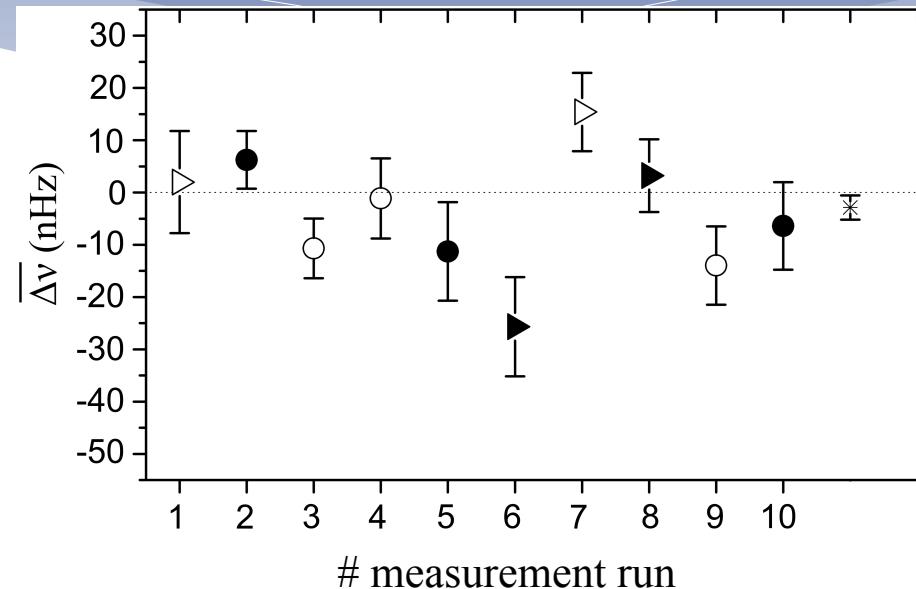
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$$\Rightarrow \Delta v_{\text{sp}} = (-2.9 \pm 3.5) \text{ nHz} \rightarrow \delta(\Delta v_{\text{sp}})_{\text{corr}} = 7.1 \text{ nHz (95% CL)}$$

K. Tullney et al.  
PRL 111, 100801 (2013)

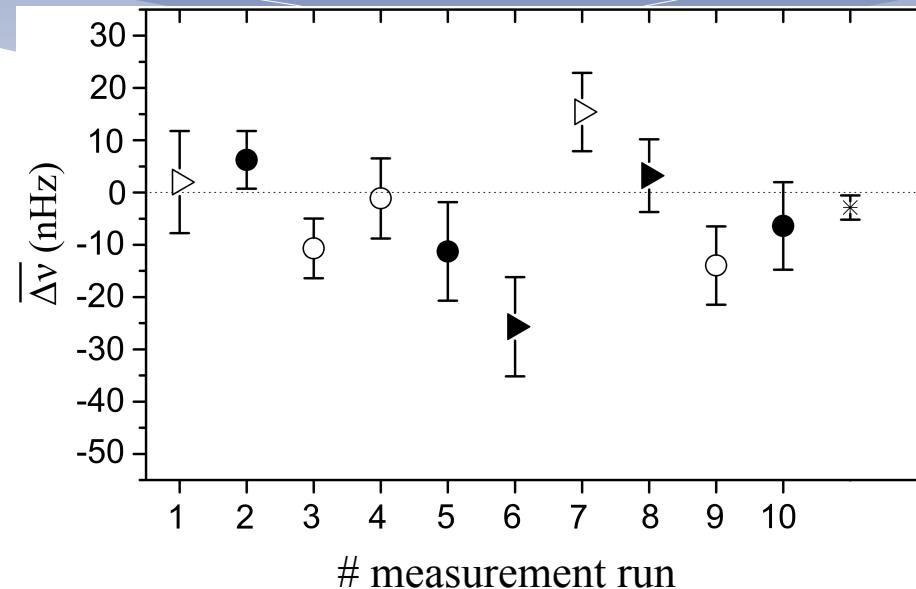
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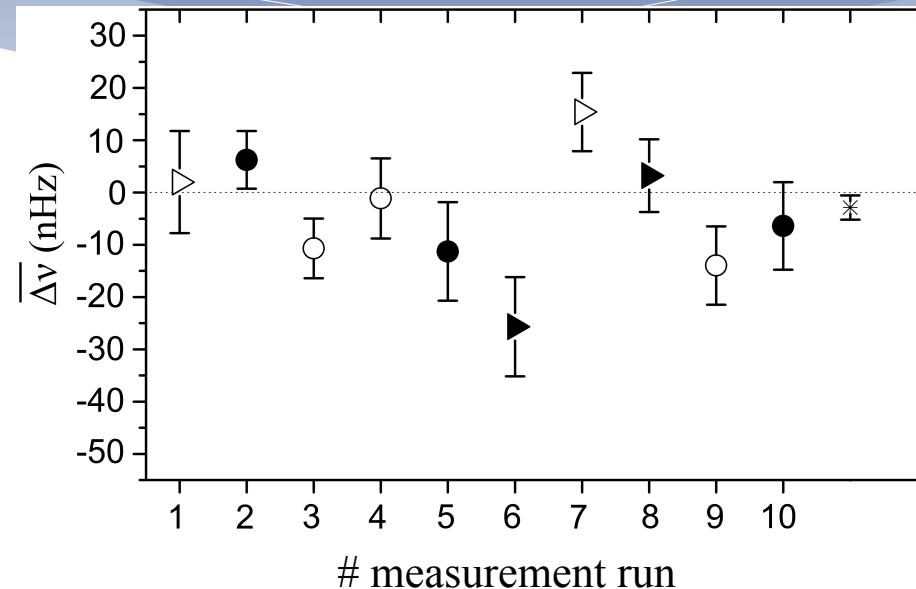
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Potential:  $V_{\text{sp}}(\vec{r}) = \frac{\hbar^2 g_s g_p}{8\pi m_n} \left( \frac{\vec{r}}{r} \cdot \vec{\sigma} \right) \left( \frac{1}{r\lambda} + \frac{1}{r^2} \right) \cdot e^{-r/\lambda}$

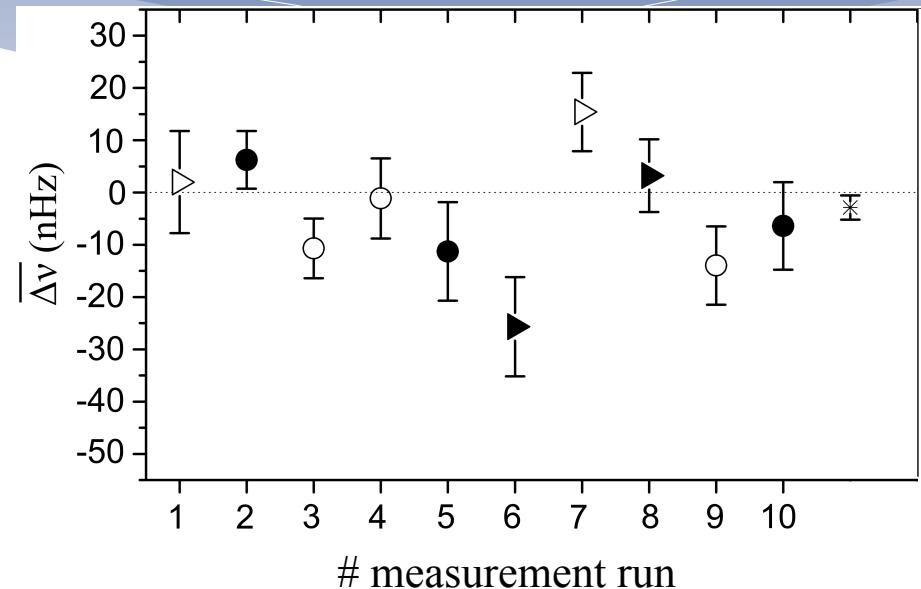
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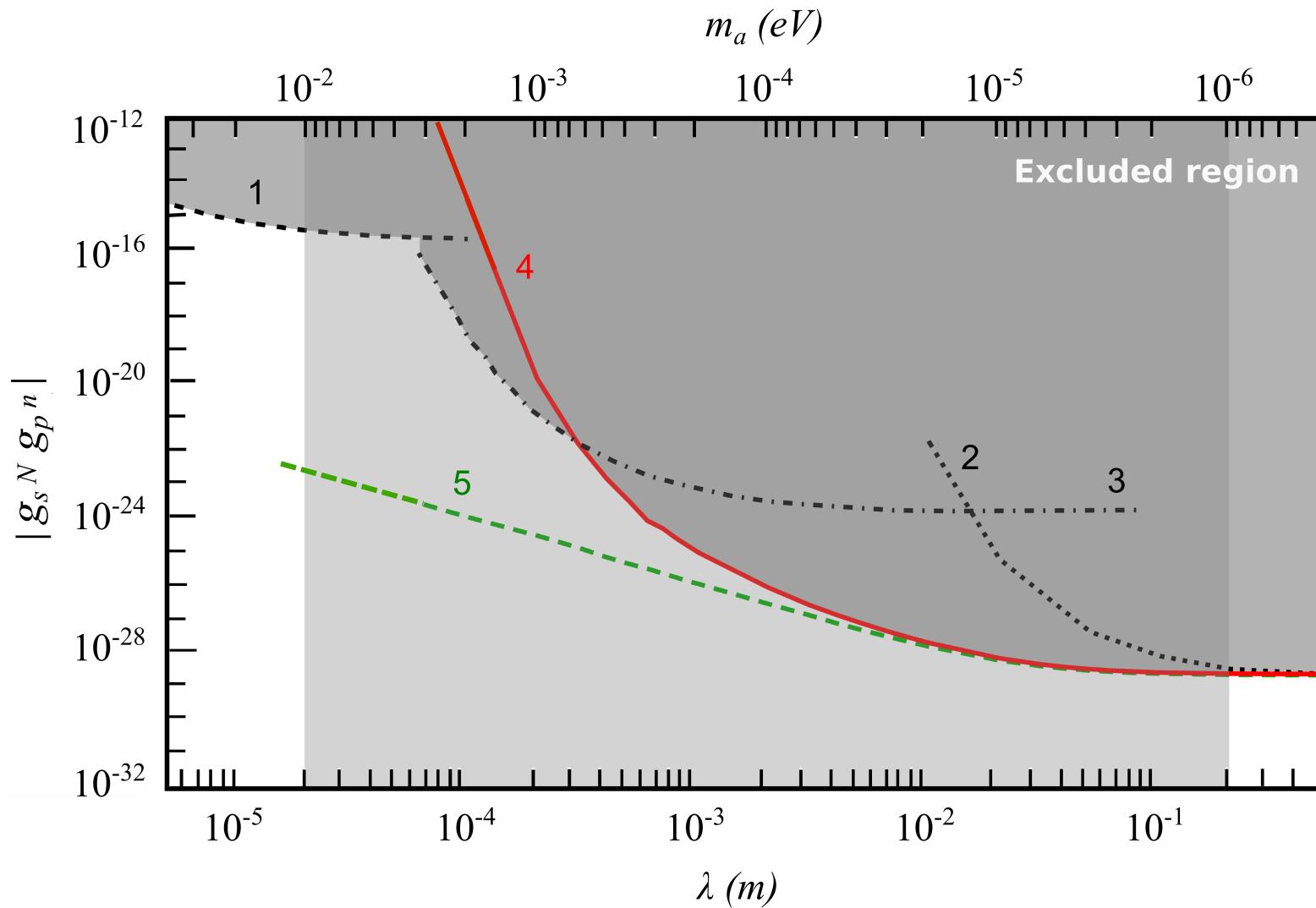
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$$\delta(\Delta v_{\text{sp}}) > 2 \langle V_{\text{sp}} \rangle / h \Rightarrow g_s g_p(\lambda) < \frac{8\pi^2 \cdot m_n \cdot V_{\text{cell}} \cdot \delta(\Delta v_{\text{sp}})}{\hbar \cdot N \cdot \langle V^*(\lambda) \rangle}$$

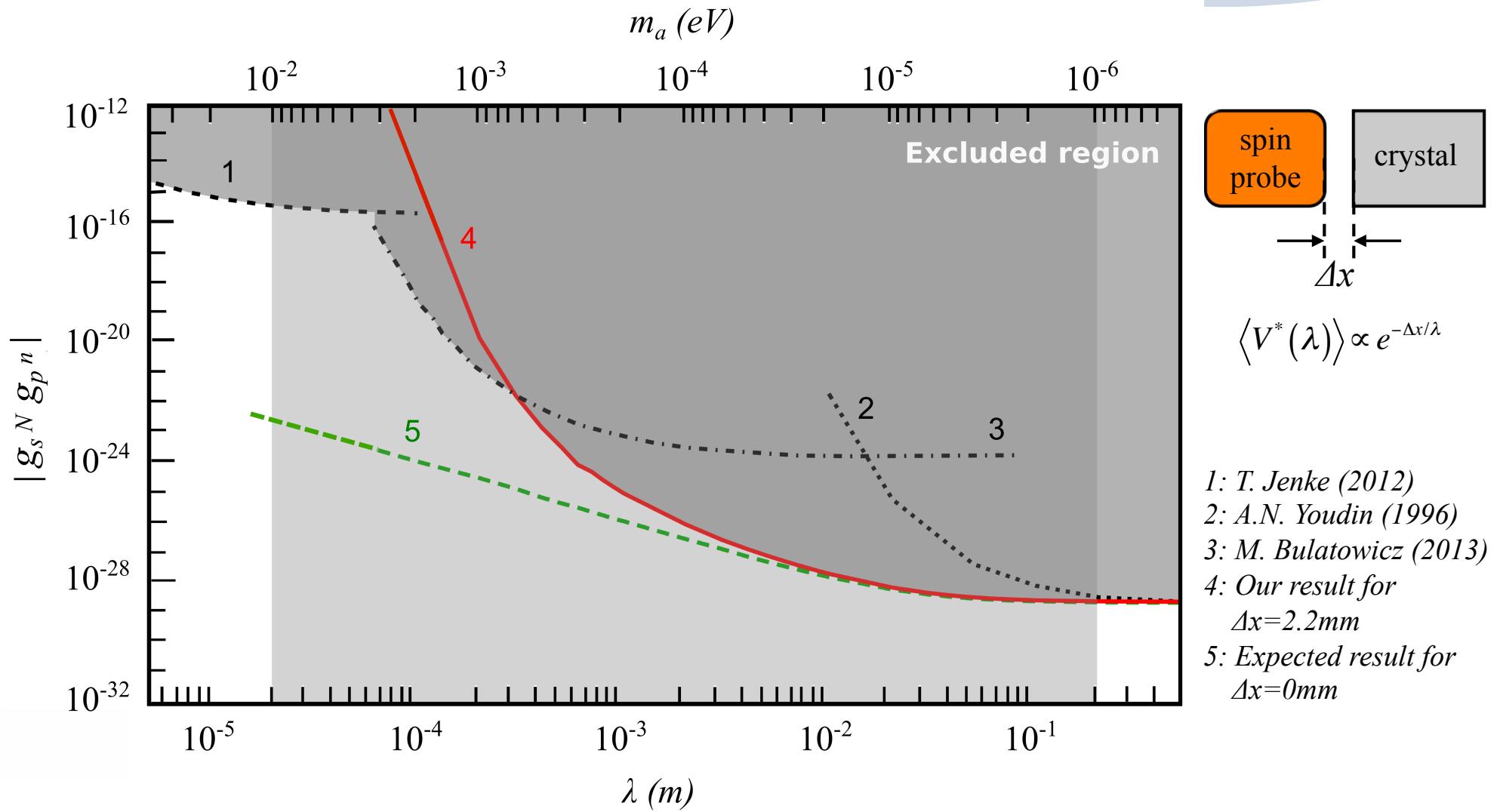
Potential:  $V_{\text{sp}}(\vec{r}) = \frac{\hbar^2 g_s g_p}{8\pi m_n} \left( \frac{\vec{r}}{r} \cdot \vec{\sigma} \right) \left( \frac{1}{r\lambda} + \frac{1}{r^2} \right) \cdot e^{-r/\lambda}$

# Exclusion Plot



- 1: *T. Jenke (2012)*
- 2: *A.N. Youdin (1996)*
- 3: *M. Bulatowicz (2013)*
- 4: *Our result for  $\Delta x = 2.2\text{mm}$*
- 5: *Expected result for  $\Delta x = 0\text{mm}$*

# Exclusion Plot



# Summary

- Free spin precession of  $^3\text{He}$  and  $^{129}\text{Xe}$  with long spin coherence times:

$$\overline{T}_{2,\text{He}}^* \approx 53 \text{ h} \quad \overline{T}_{2,\text{Xe}}^* \approx 5 \text{ h}$$

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- **Clock comparison experiment**

Spin-dependent short-range interaction:

$$V(r) = \frac{g_s g_p}{8\pi} \frac{(\hbar)^2}{m_n} (\sigma_n \cdot \vec{n}) \left[ \frac{1}{r\lambda} + \frac{1}{r^2} \right] e^{-r/\lambda} \quad J.E. Moody, F.Wilczek PRD 30 (1984), 130$$

$$\Delta\nu_{\text{sp}} = (-2.9 \pm 3.6) \text{ nHz} \rightarrow \delta(\Delta\nu_{\text{sp}})_{\text{corr}} = 7.1 \text{ nHz (95% CL)}$$

Result: New upper limit for  $g_s g_p$  in the range  $3 \cdot 10^{-4} \text{ m} < \lambda < 10^{-1} \text{ m}$   
Improvement up to **4 orders of magnitude!**

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Spin-dependent short-range interaction:

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