

READi Workshop, DESY Hamburg, April 7th, 2014

Beyond the Standard Model of Particle Physics

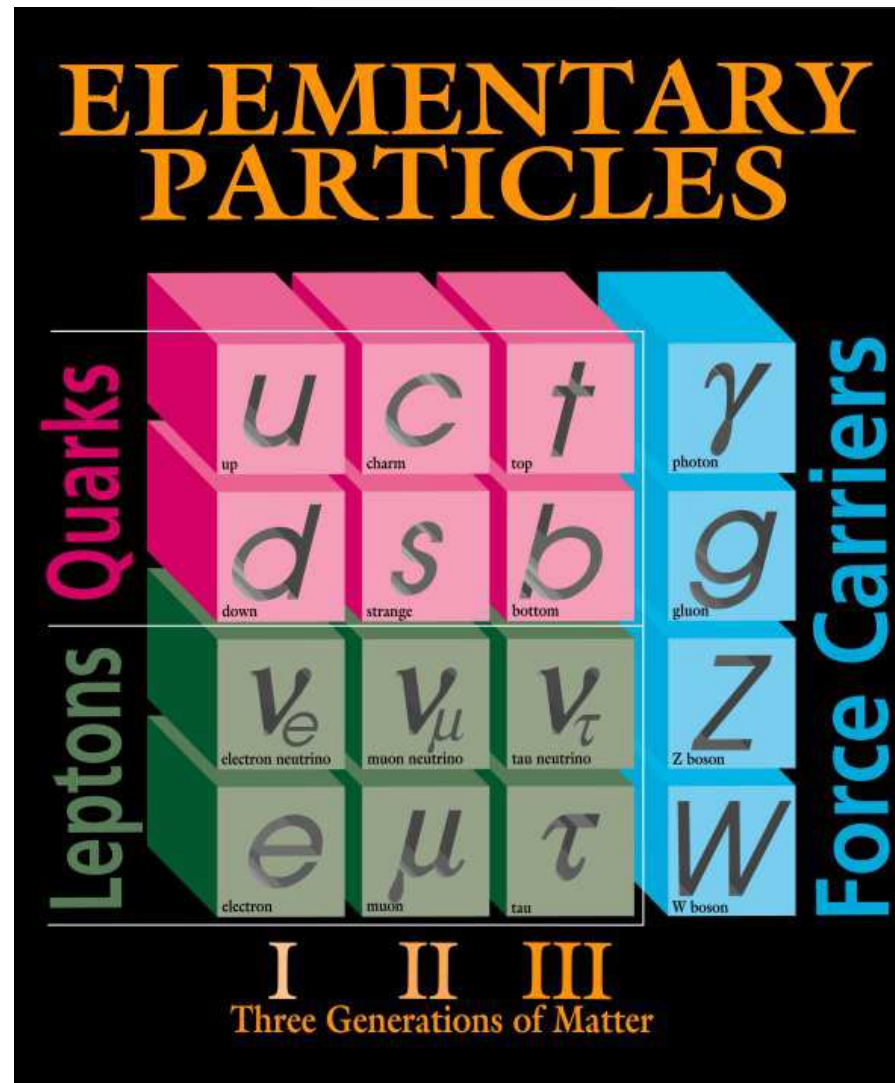
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OUTLINE

1. Standard Model of Elementary Particle Physics
2. Higgs Boson & Implications
3. Open Questions in the Standard Model: Hierarchy Problem
4. Supersymmetry
5. Conclusions and Outlook

Lego blocks of our world, June 2012

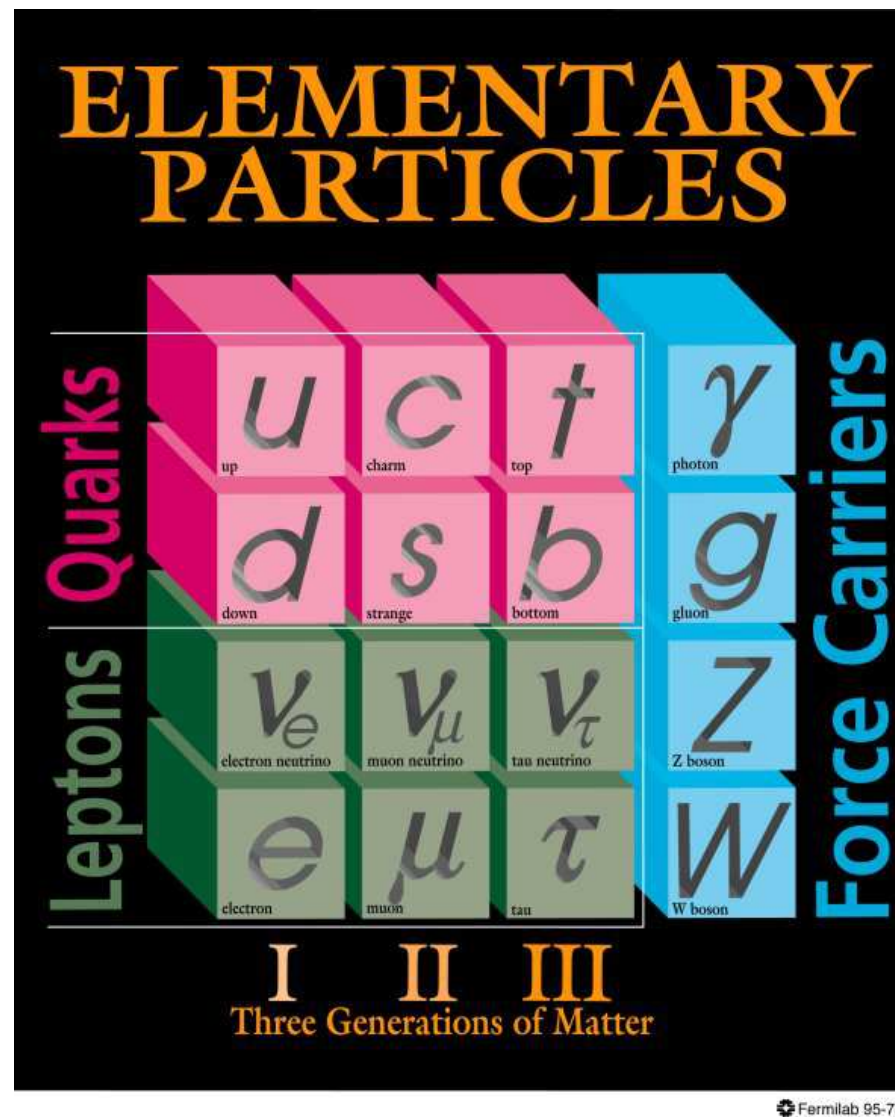


July 4th, 2012, CERN



Discovery of the Higgs Boson!

Lego blocks today



+

**Higgs
Boson**

- The Higgs is qualitatively different predicted **1964** for internal consistency!

Step back

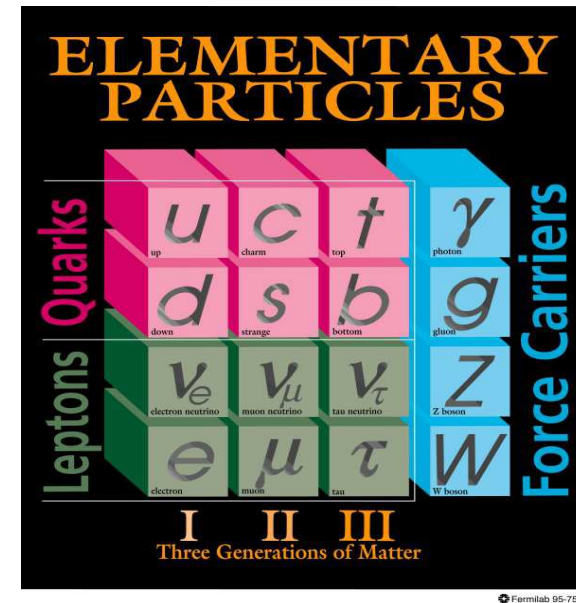
- This picture is sloppy
- For one generation we have:
- Leptons: $\begin{pmatrix} \nu \\ e \end{pmatrix}_L$; e_R , $(\nu_R??)$

- Quarks: $\begin{pmatrix} u \\ d \end{pmatrix}_L$; u_R , d_R

- e_L , e_R , distinct fields:
 - transform differently under Lorentz group.
 - Have different gauge interactions!

- Same for: $u_{L,R}$, $d_{L,R}$

- Important in constructing supersymmetric Lagrangians



Historical Interlude

- What was the last SM particle to be observed before the Higgs?
- **Electron** 1897, Thompson
- **Proton** 1917, Rutherford
- **Neutron** 1932, Chadwick
- **Positron** 1932, Anderson
- How about the other (elementary) particles?

Discovery of Matter Particles

Muon, μ

Electron Neutrino, ν_e

Muon Neutrino, ν_μ

Light Quarks, u, d, s

Charm Quark, c

Bottom Quark, b

Tau Lepton, τ

Top Quark, t

Tau Neutrino, ν_τ

Discovery of Matter Particles

1934 Muon, μ

1956 Electron Neutrino, ν_e

1962 Muon Neutrino, ν_μ

Light Quarks, u, d, s

Charm Quark, c

Bottom Quark, b

Tau Lepton, τ

Top Quark, t

Tau Neutrino, ν_τ

Discovery of Matter Particles

1934 Muon, μ

1956 Electron Neutrino, ν_e

1962 Muon Neutrino, ν_μ

1960's Light Quarks, u, d, s

1974 Charm Quark, c

1977 Bottom Quark, b

Tau Lepton, τ

Top Quark, t

Tau Neutrino, ν_τ

Discovery of Matter Particles

1934 Muon, μ

1956 Electron Neutrino, ν_e

1962 Muon Neutrino, ν_μ

1960's Light Quarks, u, d, s

1974 Charm Quark, c

1977 Bottom Quark, b

1977 Tau Lepton, τ

1995 Top Quark, t

2000 Tau Neutrino, ν_τ

... and the bosons

- Photon, 1905, Hertz, Einstein?
- Gluon, 1979, many, at PETRA at DESY (1978, PLUTO at DORIS?)
- W^{\pm} , Z^0 , 1983 UA1 & UA2 collaborations, CERN

Higgs Boson, Higgs Mechanism

- Dilemma 1964:
 - gauge theory – vector boson $M_W = 0$, exactly
 - Weak interaction has a very short range: $M_W \neq 0$

- Add complex scalar SU(2) Higgs doublet to SM: $\Phi = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix}$

- With Higgs Lagrangian

$$\mathcal{L} = (\mathcal{D}_\mu \Phi)^\dagger \mathcal{D}^\mu \Phi - \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 - Y[\bar{\psi}_R(\Phi^\dagger \psi_L) + (\bar{\psi}_L \Phi) \psi_R]$$

- Gauge covariant derivative: $\mathcal{D}_\mu = \partial_\mu + \frac{ig'}{2} \mathcal{B}_\mu + \frac{ig}{2} \vec{\tau} \cdot \vec{W}_\mu$

Spontaneous Symmetry Breaking

- Spontaneous symmetry breaking:

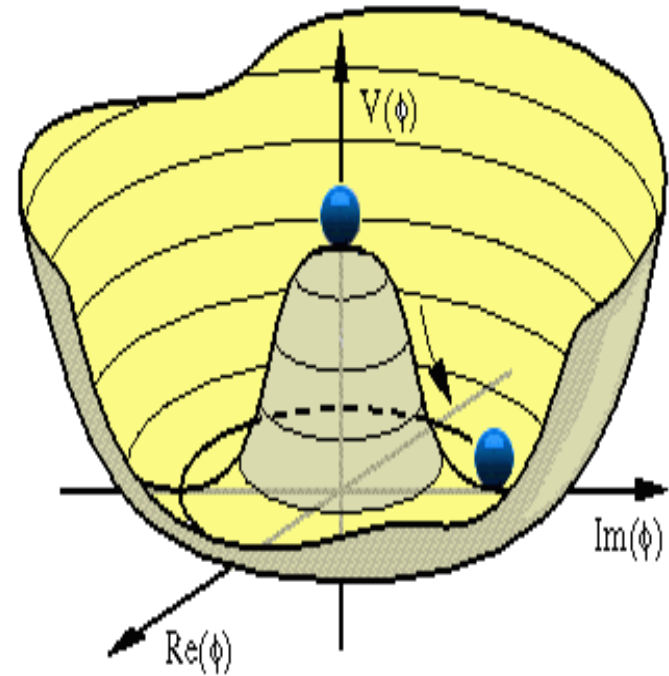
$$SU(2)_L \times U(1)_Y \longrightarrow U(1)_{EM}$$

- $\Phi = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix} \longrightarrow \begin{pmatrix} 0 \\ v \end{pmatrix}$ in vacuum

- Only one real scalar remains h^0

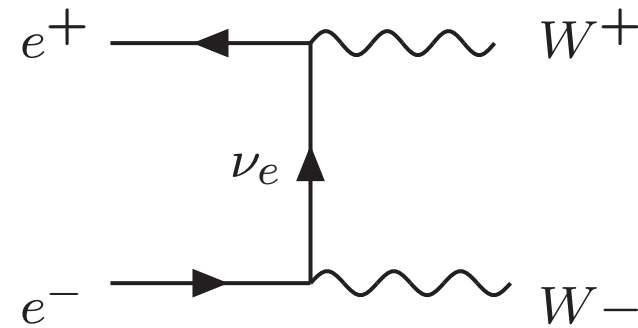
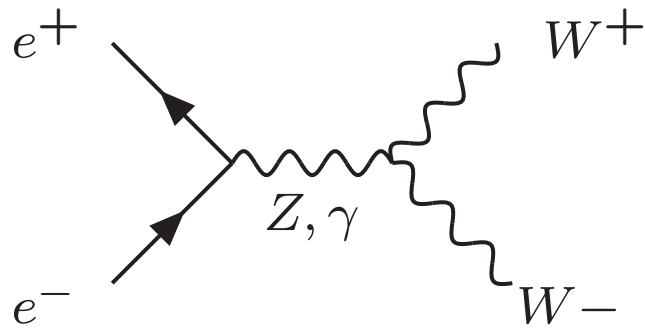
- $M_W \propto gv \neq 0$

- $m_e \propto Yv \neq 0$

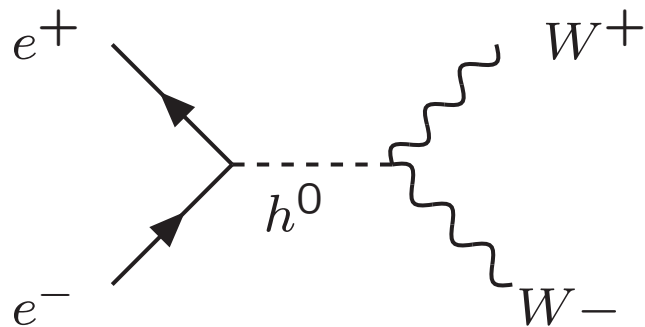


Unitarity

- Solves extra problem: $e^+e^- \rightarrow W^+W^-$ (LEP2)



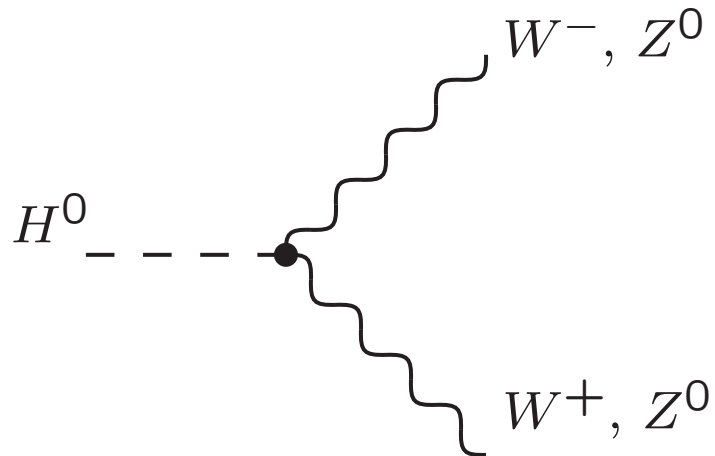
- With Higgs, extra diagram



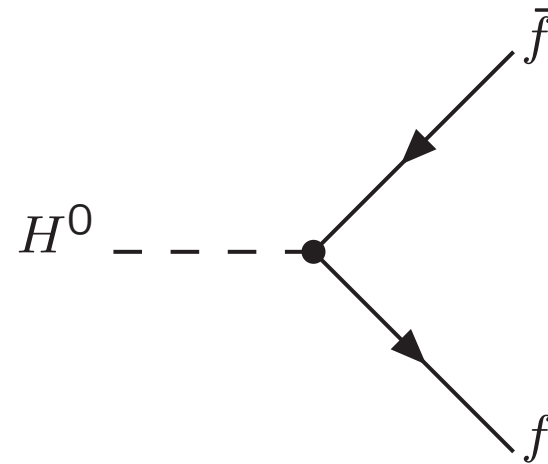
- Cross section obeys unitarity bound

Higgs Couplings

- Directly from the Lagrangian



$$c = 2M_{W,Z}^2/v$$

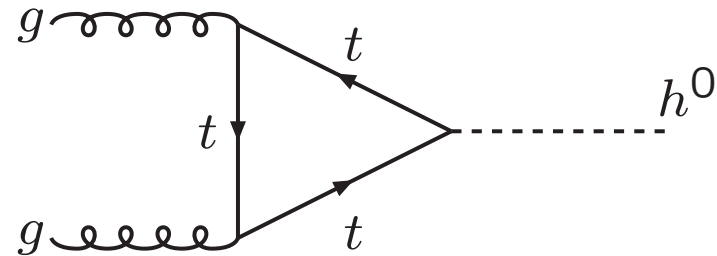
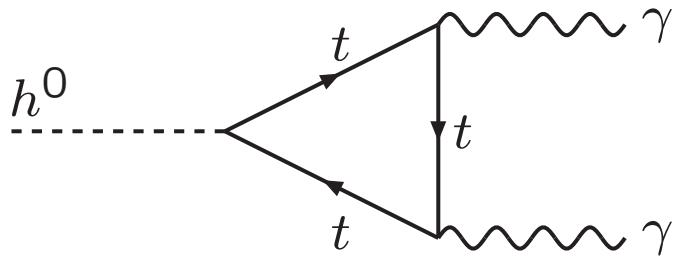


$$Y = m_f/v$$

- Coupling is proportional to mass!
- Thus also no coupling to gluons or photons.

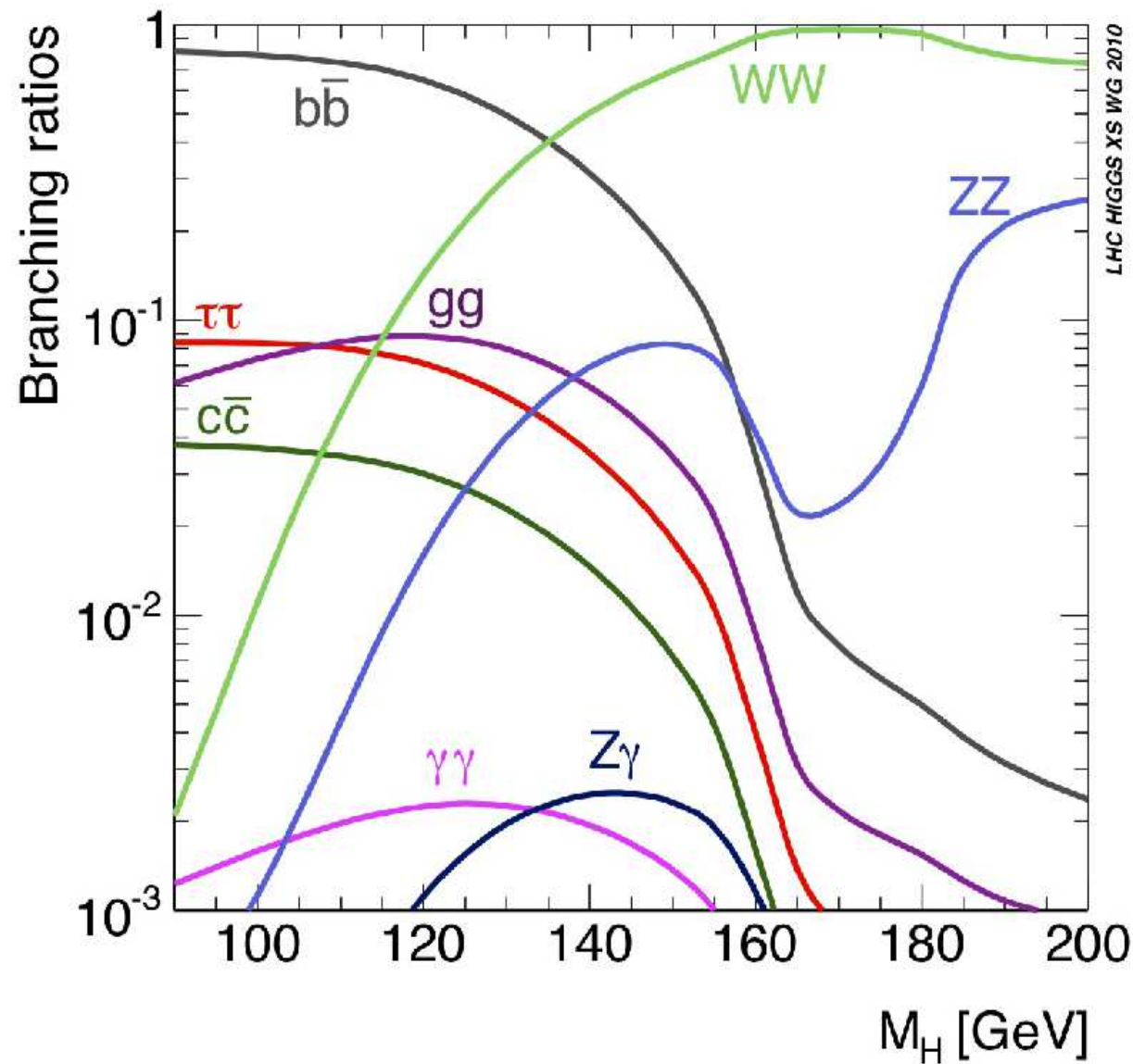
Higgs Couplings II

- Quantum Corrections



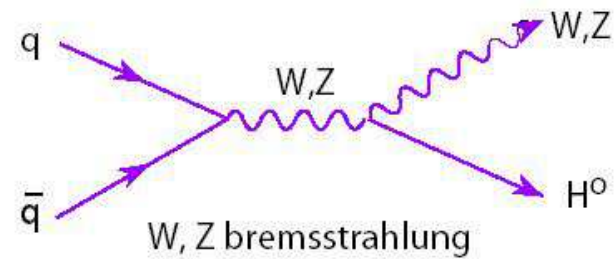
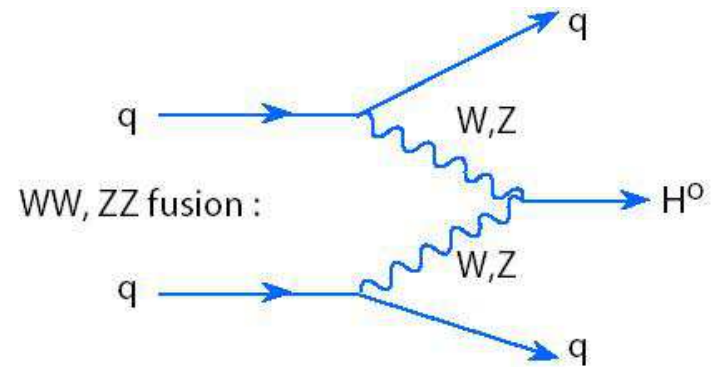
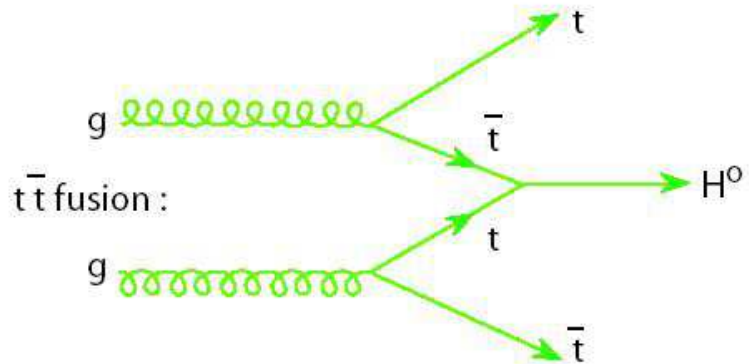
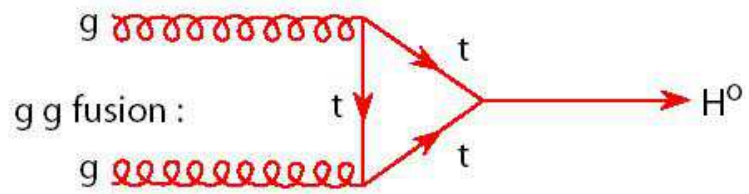
- **Photon:** all charged fermions contribute, plus W^\pm
- **Gluon:** all quarks contribute
- But top contribution largest
- Loop suppressed, but still essential, can even dominate
- Higher order corrections known (NNLO QCD for prod.: 3-loop!)

Higgs Decay Branching Ratios

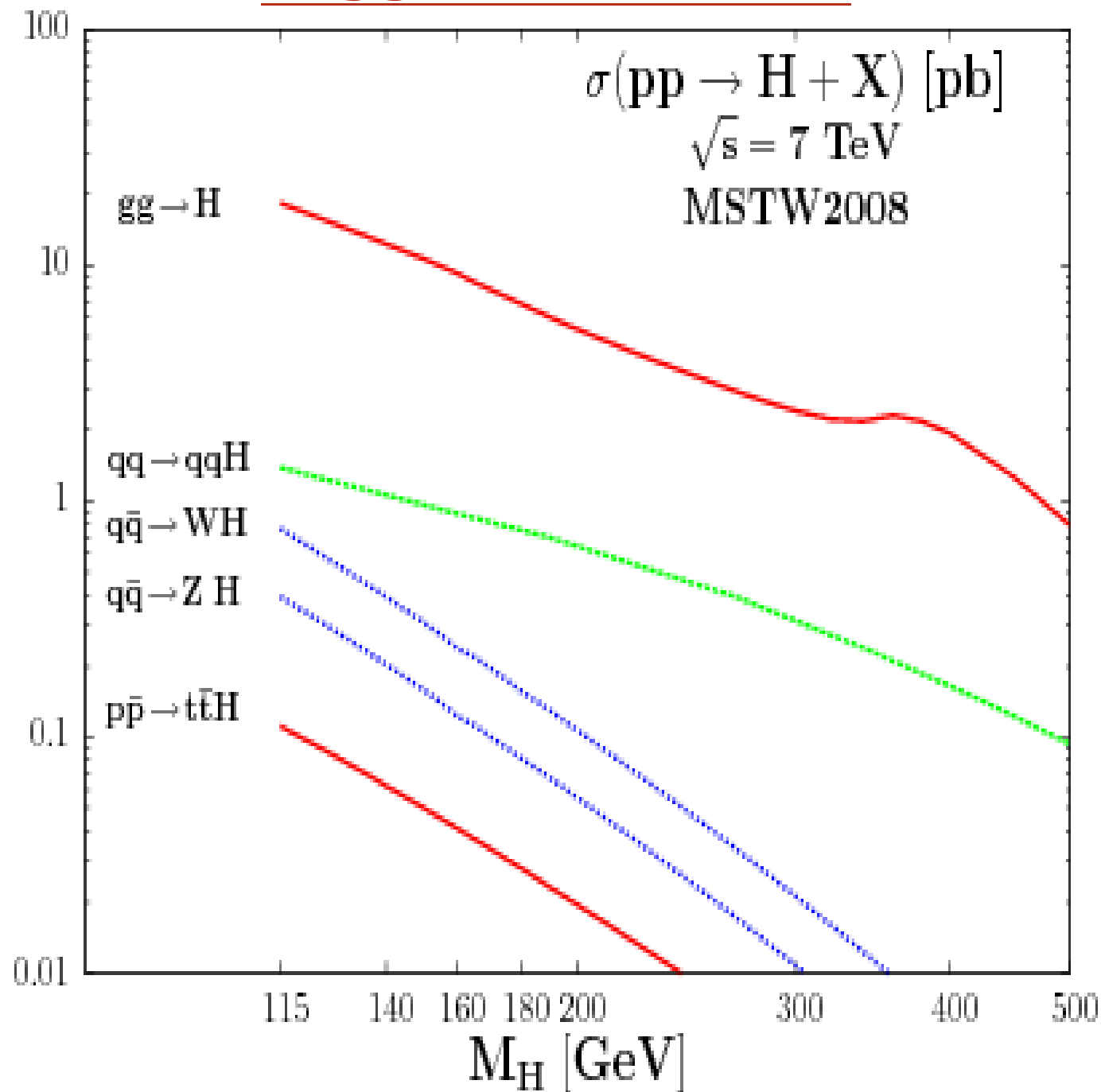


- A lot of theory effort in both this and production cross sections.

Higgs Production

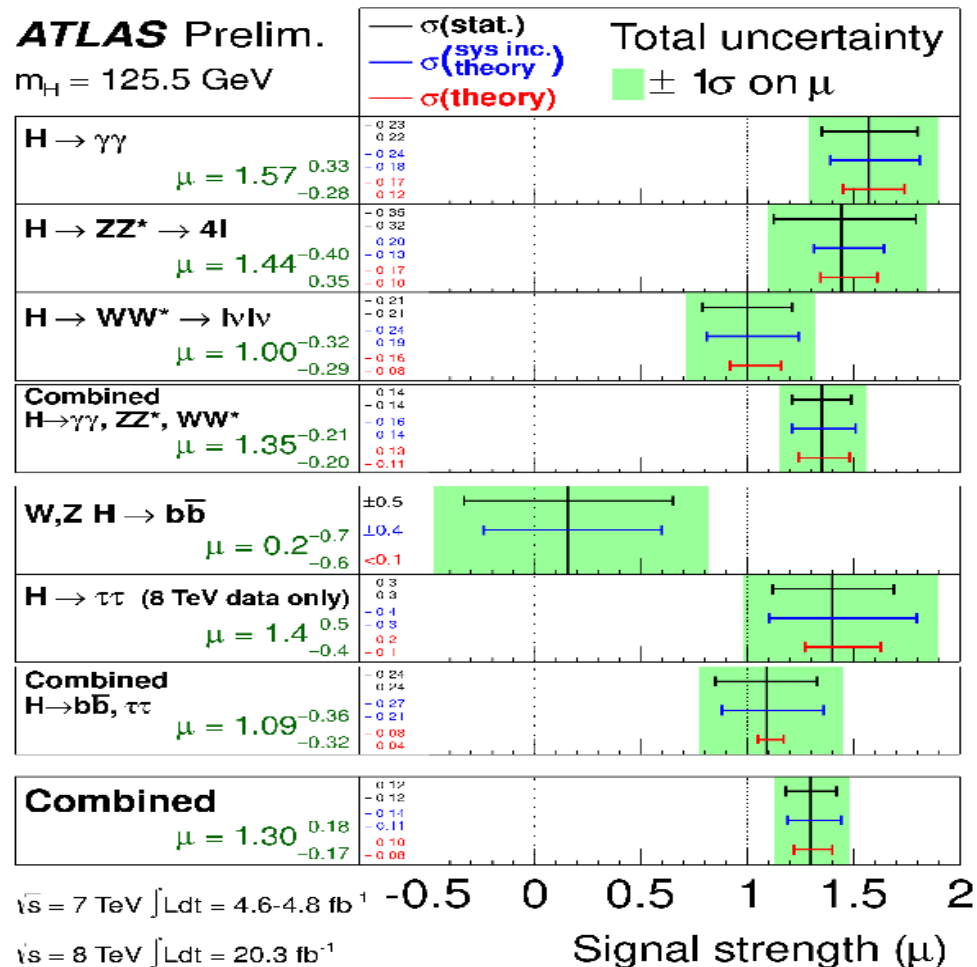


Higgs Production



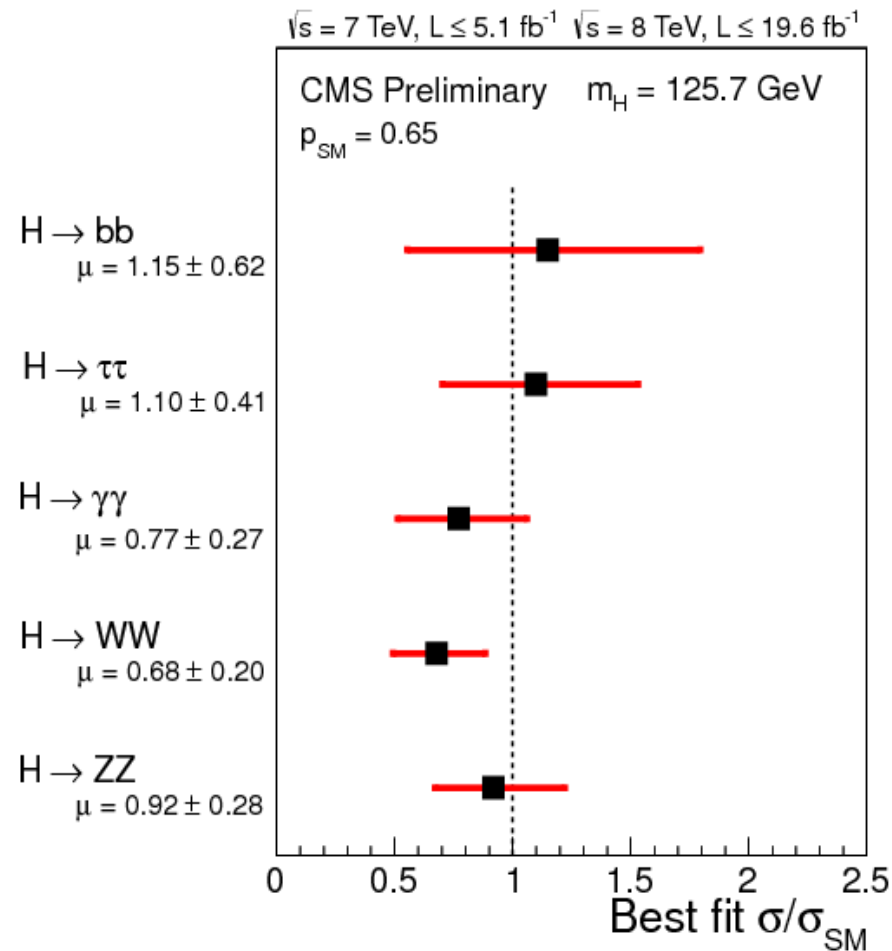
Higgs Couplings Strengths, ATLAS

- $\mu_i = (\sigma \times BR)_i / (\sigma \times BR)_i^{SM}$



Higgs Couplings Strengths, CMS

- $\mu_i = (\sigma \times BR)_i / (\sigma \times BR)_i^{SM}$



Meta Stability

Butazzo, Degrandi, Giardino, Giudice, Sala, Salvio, Strumia

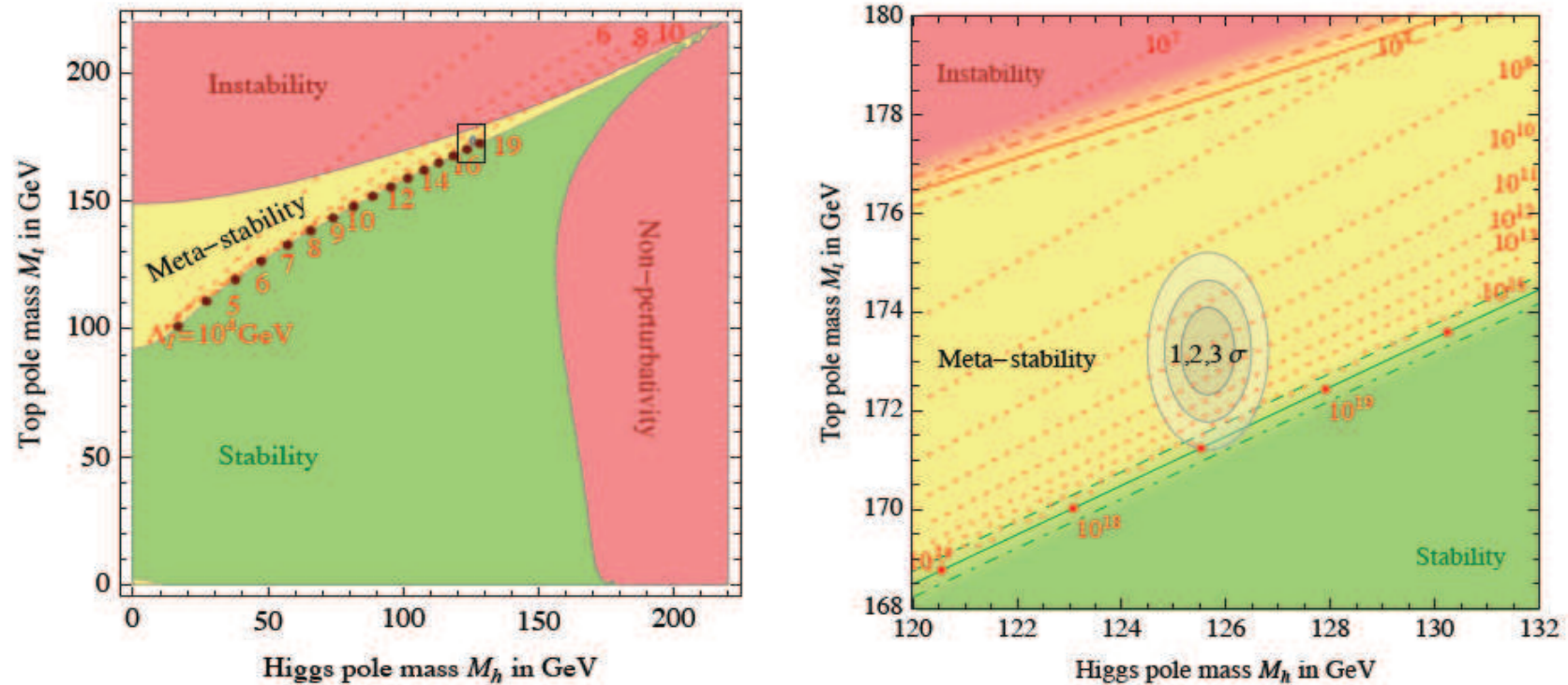


Figure 3: **Left:** SM phase diagram in terms of Higgs and top pole masses. The plane is divided into regions of absolute stability, meta-stability, instability of the SM vacuum, and non-perturbativity of the Higgs quartic coupling. The top Yukawa coupling becomes non-perturbative for $M_t > 230$ GeV. The dotted contour-lines show the instability scale Λ_I in GeV assuming $\alpha_3(M_Z) = 0.1184$. **Right:** Zoom in the region of the preferred experimental range of M_h and M_t (the grey areas denote the allowed region at 1, 2, and 3 σ). The three boundary lines correspond to 1- σ variations of $\alpha_3(M_Z) = 0.1184 \pm 0.0007$, and the grading of the colours indicates the size of the theoretical error.

Higgs Width

Caola, Melnikov, PRL 2013

- $H \rightarrow ZZ \rightarrow ee\mu\mu$

- $gg \rightarrow ZZ \rightarrow ee\mu\mu$



FIG. 1: Sample signal (left) and background $gg \rightarrow ZZ$ (right) diagrams for the process $pp \rightarrow ZZ \rightarrow 4l$. The two amplitudes can interfere.

- $$\frac{d\sigma_{pp \rightarrow H \rightarrow ZZ}}{dM_{4\ell}^2} \sim \frac{g_{Hgg}^2 g_{HZZ}^2}{(M_{4\ell}^2 - m_H^2)^2 + m_H^2 \Gamma_H^2}$$

- Narrow width approximation: $\sigma_{i \rightarrow H \rightarrow f} \sim \frac{g_i^2 g_f^2}{\Gamma_H}$

- Rescale: $g = \xi g_{SM}$, $\Gamma_H = \xi^4 \Gamma_{H,SM}$

- Dominant contribution at resonance, where Γ_H effectively drops out, or is well below detector resolution

- But **off-peak** scaling doesn't cancel. Can bound ξ from off-shell ZZ production rate, including interference!

Higgs Width II

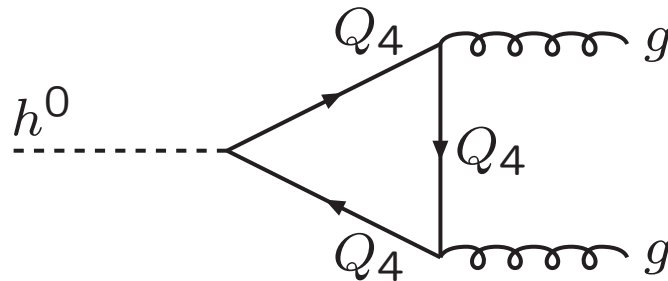
- Caola & Melnikov estimated sensitivity of $\Gamma_H \sim 10 \times \Gamma_{H,SM}$
- CMS-Experiment, 20.3.2014(!): $\Gamma_H < 4.2 \times \Gamma_{H,SM}$, @95% C.L.
- With $\Gamma_{H,SM} = 4.2 \text{ MeV}$
- Also used $2\ell 2\nu$ signature
- If improved, could be important for Higgs invisible width, $h^0 \rightarrow \chi_1^0 \chi_1^0$

Open Questions in Standard Model

1. 3 generations, CP-violation
2. Flavor Problem, 19 Parameters
3. Charge Quantisation, Unification
4. Neutrinos
5. **Hierarchy Problem**
6. Dark Matter
7. Baryo- and Leptogenesis
8. Dark Energy

Fourth Generation

- A fourth quark generation would contribute significantly to the Higgs production rate, altering the μ_i 's.



- It is excluded by the Higgs data

Eberhardt, Herbert, Lackner, Lenz, Menzel, Nierste, Wiebusch, PRL (2012)

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FERMIONS

matter constituents
spin = 1/2, 3/2, 5/2, ...

Leptons spin = 1/2		
Flavor	Mass GeV/c ²	Electric charge
ν_e electron neutrino	$<1 \times 10^{-8}$	0
e electron	0.000511	-1
ν_μ muon neutrino	<0.0002	0
μ muon	0.106	-1
ν_τ tau neutrino	<0.02	0
τ tau	1.7771	-1

Quarks spin = 1/2		
Flavor	Approx. Mass GeV/c ²	Electric charge
u up	0.003	2/3
d down	0.006	-1/3
c charm	1.3	2/3
s strange	0.1	-1/3
t top	175	2/3
b bottom	4.3	-1/3

- Many ideas, but completely unsolved. Maybe: A. Chamseddine, A Connes JHEP 1311 (2013) 132
- Running out of predictions, as well.

Flavor Problem

- Predict the Higgs Yukawa couplings: $Y_e \bar{L}_e \Phi e_R$
- Lepton masses $m_{e,\mu,\tau}$; Quark masses: $m_{u,c,t}, m_{d,s,b}$. \rightarrow 9 Parameter
- 3 mixing angles, 1 complex phase
- Where do these parameters come from?

Open Questions in Standard Model

1. 3 generations, CP-violation
2. Flavor Problem, 19 Parameters
3. Charge Quantisation, Unification, **Grand Unified Theories (GUTs)**
4. Neutrinos
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Neutrinos

- Neutrinos are massless in SM
- Observed neutrino oscillations: at least two are massive
- Also: now know 3 mixing angles. Complex phase(s) constrained
- QUESTIONS:
 - do ν_R exist?
 - Majorana mass? $m \left(L^T i \sigma_2 \vec{\sigma} C L \right) \cdot \left(\Phi^T i \sigma_2 \vec{\sigma} C \Phi \right)$ (Weinberg operator)
 - Dirac mass with ν_R ?
 - See-saw with heavy ν_R Majorana mass?
 - No-see saw as in one variant of supersymmetry?

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Hierarchy Problem

The Problem:

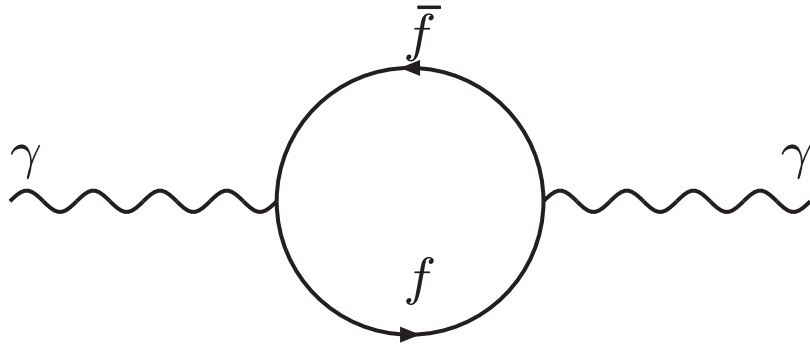
IF there is a new, high, scale of physics, M_X , due to quantum corr. the natural value of the Higgs mass is $M_{h0} = \mathcal{O}(M_X)$.

- Only exists if there is a new high scale.....like Planck scale of gravity
- If the SM is nature's final answer, and valid to ∞ energies, there is **NO** hierarchy problem.
- Why is the Higgs mass special?

— It's a scalar, spin-0, the only in SM

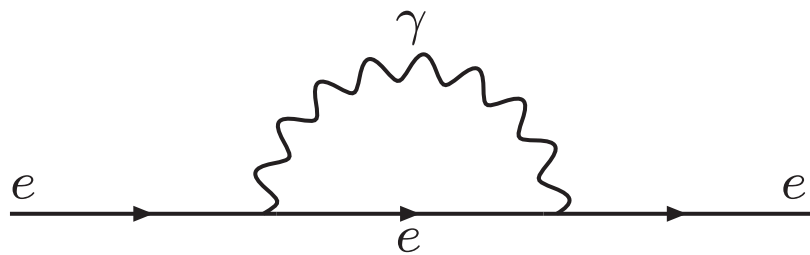
Quantum Mass Corrections M. Drees, hep-ph/9611409

- Spin-1, photon



$$\Pi_{\gamma\gamma}^{\mu\nu}(0) = 0, \text{ by gauge symmetry}$$

- Spin-1/2 electron



$$\Pi_{ee}(0) = -4e^2 m_e \int^\Lambda \frac{d^4 k}{(2\pi)^4} \frac{1}{k^2(k^2 - m_e^2)}$$

$$\delta m_e \simeq 2 \frac{\alpha_{\text{em}}}{\pi} m_e \log \frac{M_{\text{Pl}}}{m_e} \simeq 0.24 m_e$$

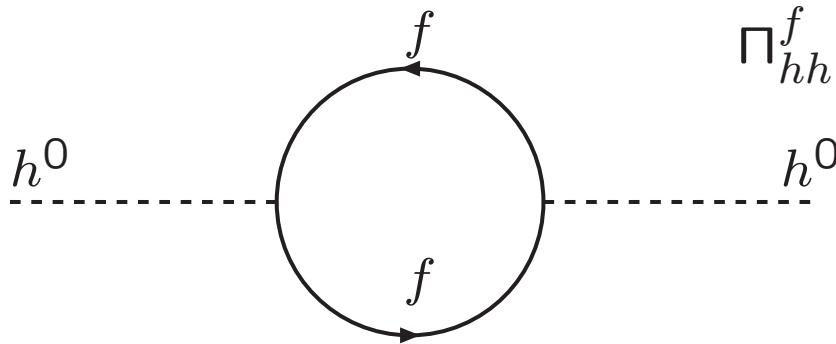
- Proportional to electron mass.

- As $m_e \rightarrow 0$ extra symmetry: $\psi_e \rightarrow \exp(i\gamma_5 \phi) \psi_e$

Quantum Mass Corrections II

- **Spin-0, Higgs**

$$\Pi_{hh}^f(0) = -2N(f)\lambda_f^2 \int^\Lambda \frac{d^4k}{(2\pi)^4} \left(\frac{1}{k^2 - m_f^2} + \frac{2m_f^2}{(k^2 - m_f^2)^2} \right)$$



$$\Pi_{hh}^f(0) \simeq \Lambda^2$$

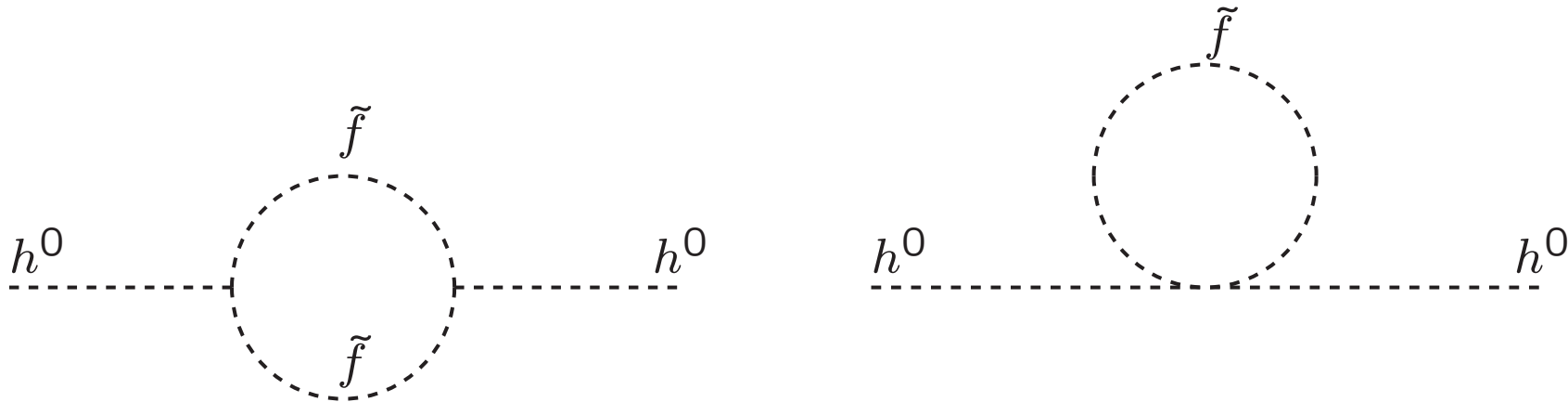
- Correction to m_h^2 goes as Λ^2 , thus never small.
- If no higher scale, $\Lambda \rightarrow \infty$, δm_h absorbed in renormalization of m_h
- Λ never appears in physical results and all is fine.
- But if extra scale exists need to fine-tune finite corrections at M_X to get $m_h = \mathcal{O}(M_W)$ (drawing)
- Solution \longrightarrow **Supersymmetry**

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Supersymmetry

$$\mathcal{L}_{h\tilde{f}} = \frac{1}{2}\tilde{\lambda}_f h^2 (|\tilde{f}_L|^2 + |\tilde{f}_R|^2) + v\tilde{\lambda}_f h (|\tilde{f}_L|^2 + |\tilde{f}_R|^2) + \left(\frac{\lambda_f}{\sqrt{2}} A_f h \tilde{f}_L \tilde{f}_R + h.c. \right)$$



- Opposite sign: bosons
- Right diagram cancels Λ^2 divergence, if: $N(\tilde{f}_L) = N(\tilde{f}_R) = N(f)$

$$\tilde{\lambda} = -\lambda_f^2$$

- Supersymmetry automatically guarantees this

SUPERSYMMETRY

BASIC IDEA: $|\text{FERMION}\rangle \xleftrightarrow{Q} |\text{BOSON}\rangle$

INFINITESIMAL FIELD TRANSFORMATION:

SCALAR: $\phi \longrightarrow \phi' = \phi + \Delta\phi$

FERMION: $\psi \longrightarrow \psi' = \psi + \Delta\psi$

$$\Delta\phi = \epsilon \cdot |\text{FERMION}\rangle$$

$$\Delta\psi = \epsilon \cdot |\text{BOSON}\rangle$$

ϵ is a constant spinor in global supersymmetry.

SUSY SPECTRUM

Standard Model + SUSY \implies Double Spectrum (+2 Higgs Doublets)

e^- (spin = $\frac{1}{2}$)	\longleftrightarrow	\tilde{e} ($s = 0$)	scalar electron
top t ($s = \frac{1}{2}$)	\longleftrightarrow	\tilde{t} ($s = 0$)	scalar top
W^\pm ($s = 1$)	\longleftrightarrow	\tilde{W}^\pm ($s = \frac{1}{2}$)	Wino
H^\pm ($s = 0$)	\longleftrightarrow	\tilde{H}^\pm ($s = \frac{1}{2}$)	Higgsino
γ, Z^0 ($s = 1$)	\longleftrightarrow	$\tilde{\gamma}, \tilde{Z}^0$ ($s = \frac{1}{2}$)	Photino, Zino
H^0, h^0 ($s = 0$)	\longleftrightarrow	\tilde{H}^0, \tilde{h}^0 ($s = \frac{1}{2}$)	Higgsino
$g_{a=1,\dots,8}$ ($s = 1$)	\longleftrightarrow	\tilde{g}_a ($s = \frac{1}{2}$)	Gluino

MIXING: After $SU(2)_L \times U(1)_Y \longrightarrow U(1)_{EM}$

$\tilde{W}^\pm, \tilde{H}^\pm$	$\xrightarrow{\text{MIX}}$	$\tilde{\chi}_{i=1,2}^\pm$	Charginos
$\tilde{\gamma}, \tilde{Z}^0, \tilde{h}^0, \tilde{H}^0$	$\xrightarrow{\text{MIX}}$	$\tilde{\chi}_{i=1,2,3,4}^0$	Neutralinos

SUPERFIELDS

- Combine ψ_e and $\phi_{\tilde{e}}$ into chiral superfield

$$\Phi_e \sim \phi_{e_L} + \epsilon \psi_{e_L} = E_L, \quad \Phi_{u^c} \sim \phi_{u_R}^* + \epsilon \psi_{u_R}^c = U^c$$

Construct function $W(\Phi_i)$, holomorphic (no Φ^\dagger) & gauge invariant

Use chiral SUSY Fields:

$$L = \begin{pmatrix} N \\ E \end{pmatrix}_L \sim \begin{pmatrix} \phi_{\tilde{\nu}} + \epsilon \psi_{\nu} \\ \phi_{\tilde{e}} + \epsilon \psi_e \end{pmatrix}_L, \quad E^c \sim \phi_{\tilde{e}}^* + \epsilon \psi_{e_R}^c$$
$$Q = \begin{pmatrix} U \\ D \end{pmatrix}_L \sim \begin{pmatrix} \phi_{\tilde{u}} + \epsilon \psi_u \\ \phi_{\tilde{d}} + \epsilon \psi_d \end{pmatrix}_L, \quad U^c \sim \phi_{\tilde{u}}^* + \epsilon \psi_{u_R}^c, \quad D^c \sim \phi_{\tilde{d}}^* + \epsilon \psi_{d_R}^c$$

- Plus Higgs superfields: H_1, H_2
- Gauge interactions fixed.
- **What is the gauge invariant superpotential?**

SUPERPOTENTIAL

$$W_{P_6} = (h_e)_{ij} L_i H_1 E_j^c + (h_d)_{ij} Q_i H_1 D_j^c + (h_u)_{ij} Q_i H_2 U_j^c + \mu H_1 H_2$$

- These terms give mass to quarks and leptons. This is not all though!

$$W_{\cancel{P}_6} = \underbrace{\lambda_{ijk} L_i L_j \bar{E}_k + \lambda'_{ijk} L_i Q_j \bar{D}_k + \kappa_i L_i H_2}_{\text{Lepton Number Violating}} + \underbrace{\lambda''_{ijk} \bar{U}_i \bar{D}_j \bar{D}_k}_{\text{Baryon Num. Viol.}}$$

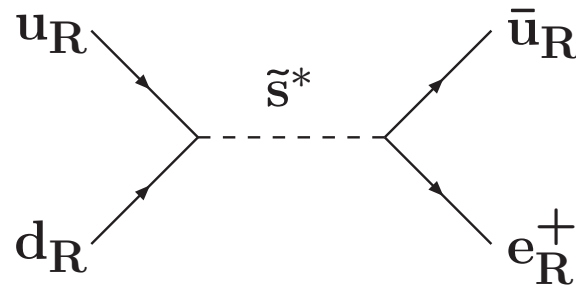
Lepton Number Violating

Baryon Num. Viol.

- Together these lead to rapid proton decay

PROTON DECAY

- Together LQD and UDD lead to Rapid Proton Decay



- Resulting in the Strict Bound:

$$\lambda'_{i1j} \cdot \lambda''_{11j} < 2 \cdot 10^{-27} \left(\frac{M_{\tilde{d}_j}}{100 \text{ GeV}} \right)^2, \quad i = 1, 2, j \neq 1,$$

- Therefore the SSM as Defined is Experimentally Excluded
- At least one Coupling must be Zero: Guaranteed by a Symmetry

Supersymmetry + Extra Symmetry

- **R-parity:** no extra terms, proton stable, dark matter candidate
- **Baryon-Parity:** $LL\bar{E}$, $LQ\bar{D}$, LH_2
 - Lepton number violated $\mu \rightarrow e\gamma$
 - Neutrino masses with ν_L 's only
 - Dark matter: axino, or gravitino

Supersymmetry, Basics

- Supersymmetry Generator commutes with mass operator

$$[Q_\alpha, \text{Mass}^2] = 0$$

- \Rightarrow $\text{Mass}(e) = \text{Mass}(\tilde{e})$ ⚡

- Supersymmetry must be broken
- No consensus on SUSY breaking mechanism
- SUSY breaking masses, $\text{Mass}(\tilde{e})$, spoil cancellation of Λ^2 divergence
- To avoid fine-tuning must have: $\text{Mass}(\tilde{e}), \text{Mass}(\tilde{q}) < \mathcal{O}(1 \text{ TeV})$,
- Will be tested (conclusively) by next run of LHC

Fine-tuning in SUSY Models Kaminska, Ross, Schmidt-Hoberg

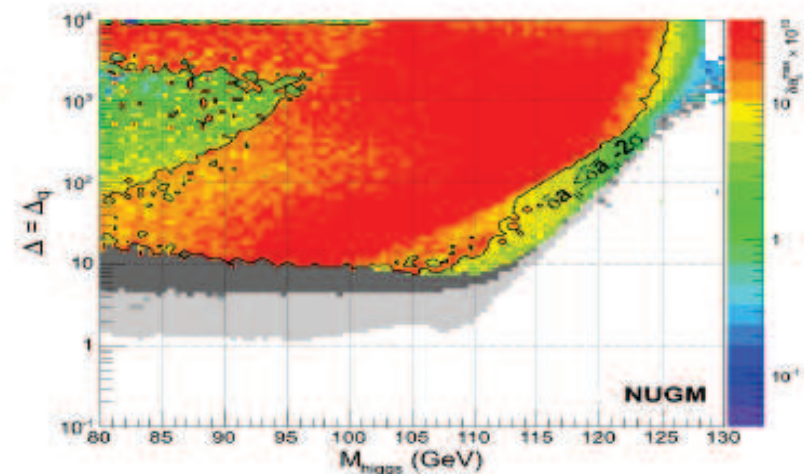
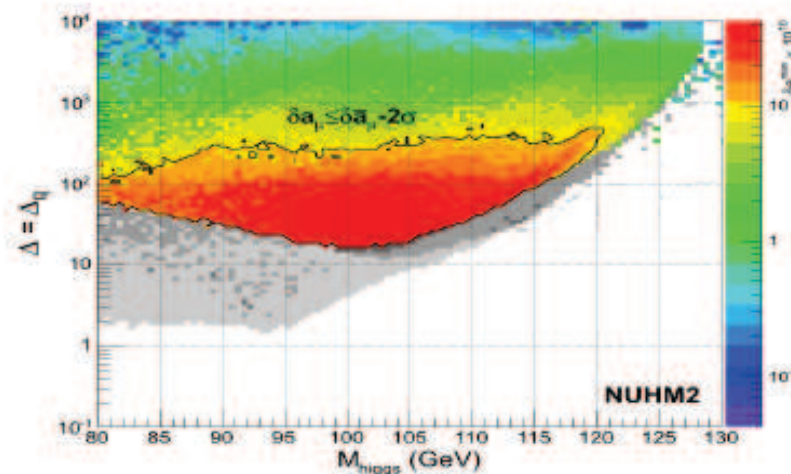
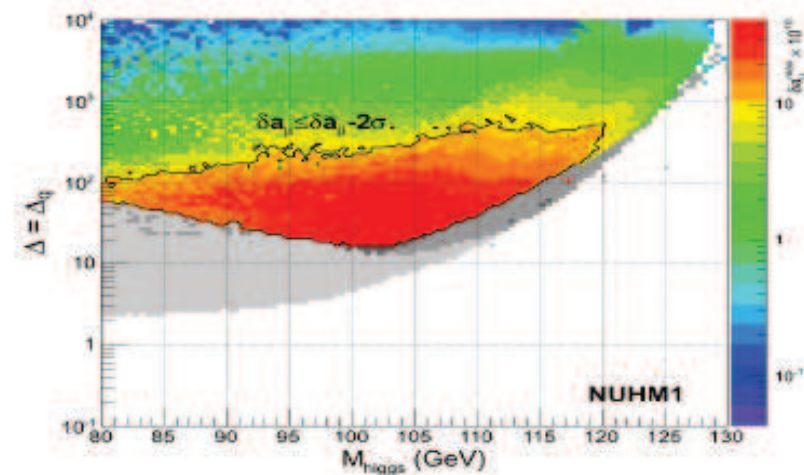
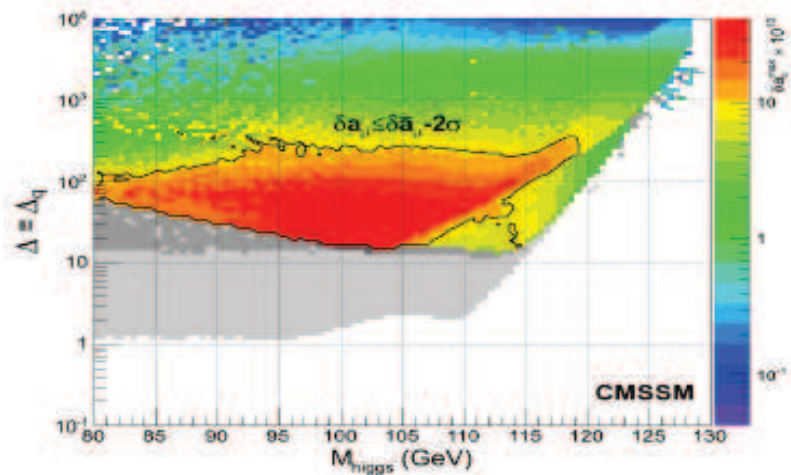
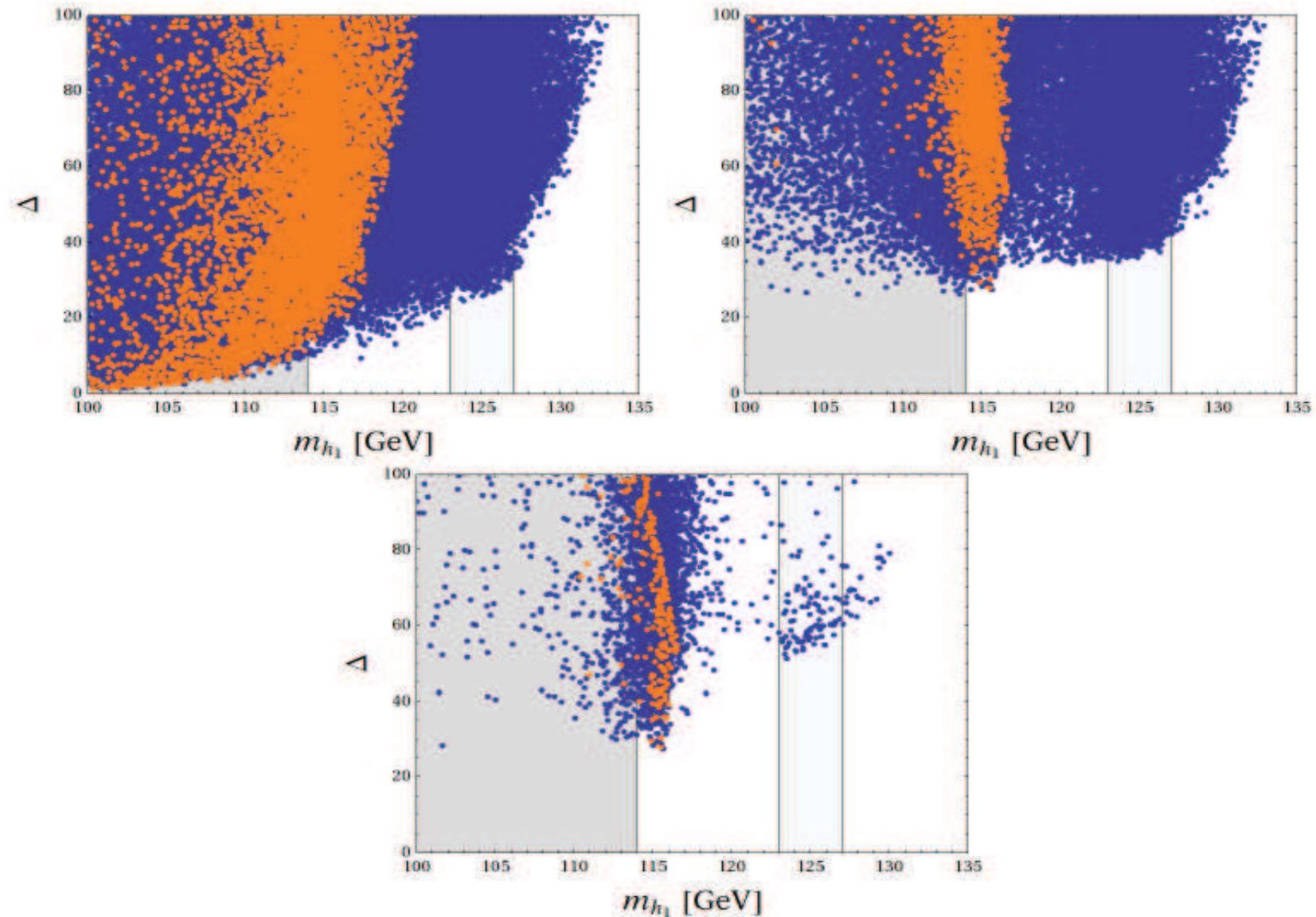


Figure 1: Δ_q versus M_{higgs} in various models, from ref.[2]; lightest grey (0) area: excluded by SUSY mass bounds; darker grey (1): excluded by $b \rightarrow s\gamma$, $B \rightarrow \mu^+ \mu^-$, $\delta\rho$; dark grey (2): excluded by condition $\delta a_\mu \geq 0$. Area inside the closed contour: allowed by data and with 2σ deviation of $g - 2$: $\delta a_\mu \leq (25.5 + 2 \times 8) 10^{-10}$; δa_μ^{max} is shown colour encoded. Area outside closed contour: $\delta a_\mu^{max} \leq (25.5 - 2 \times 8) 10^{-10}$ (2σ). Only in the NUGM is one close to satisfying the $g - 2$ constraint within 2σ , not too surprising given its non-universal gaugino masses. In all plots the dark matter relic density was computed [14] and can be fitted within 3σ [2]. For similar plots in NMSSM or GNMSSM see [15] while for the GNMSSM in the limit of a massive gauge singlet (integrated out) see plots in [16].

Fine-tuning in SUSY Models

Ross, Schmidt-Hoberg, Staub



- CMSSM, ● CGNMSSM

Figure 1: Fine-tuning vs. the lightest Higgs mass in the CGNMSSM case with universal boundary conditions for the CMSSM (orange), and the CGNMSSM (blue). The first plot corresponds to the unconstrained case, the second plot takes into account the LHC bounds on particle masses with a cut on squark and gluino masses of 1.2 TeV and the third plot assumes an additional upper bound on the neutralino relic density.

The Question of Mass

- Note the Mass of the Proton is NOT due to the Higgs Mechanism
- The proton mass is a dynamical effect in QCD \longrightarrow many Gluons inside Proton
- Therefore our masses are a QCD Effect!
- The Bohr Radius: $R_0 = \frac{\hbar}{m_e c \alpha}$
- Higgs mechanism $\longrightarrow m_e$
- Only dimensionful parameter in R_0 , together with α , determines the size of our world

Summary

- Standard Model of Particle Physics extremely successful (best ever!)
- The Higgs is an amazing breakthrough, giving new insights
- Still very many open questions
- Supersymmetry is a promising solution to the hierarchy problem.
- There are many variants. The simplest are severely under the weather.