

# Jet production and QCD measurements at HERA

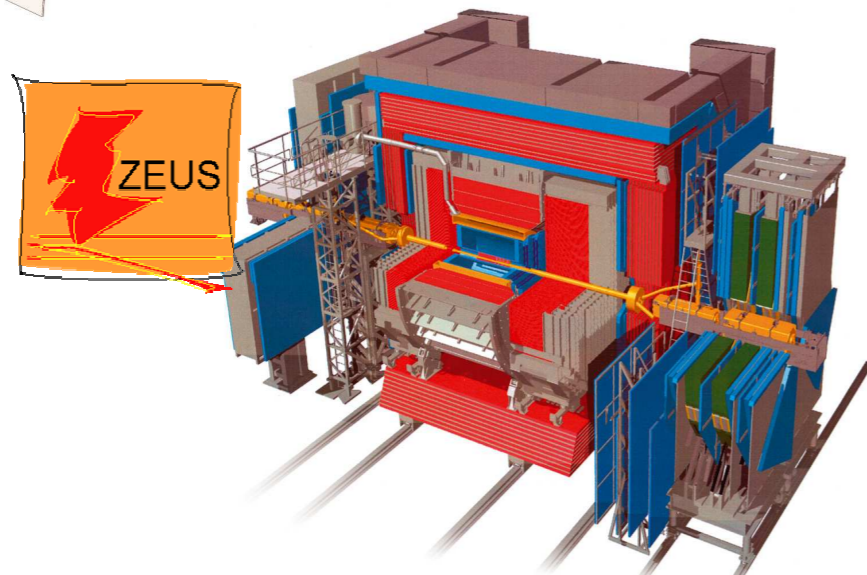
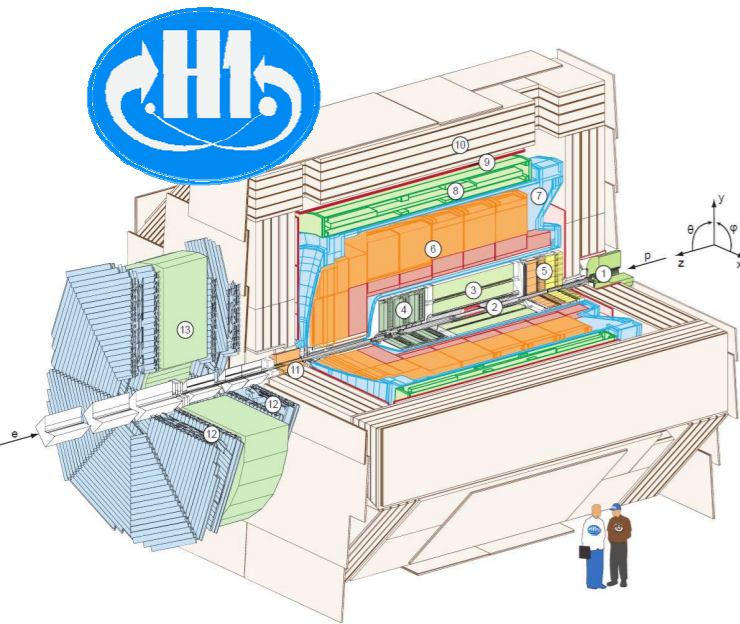
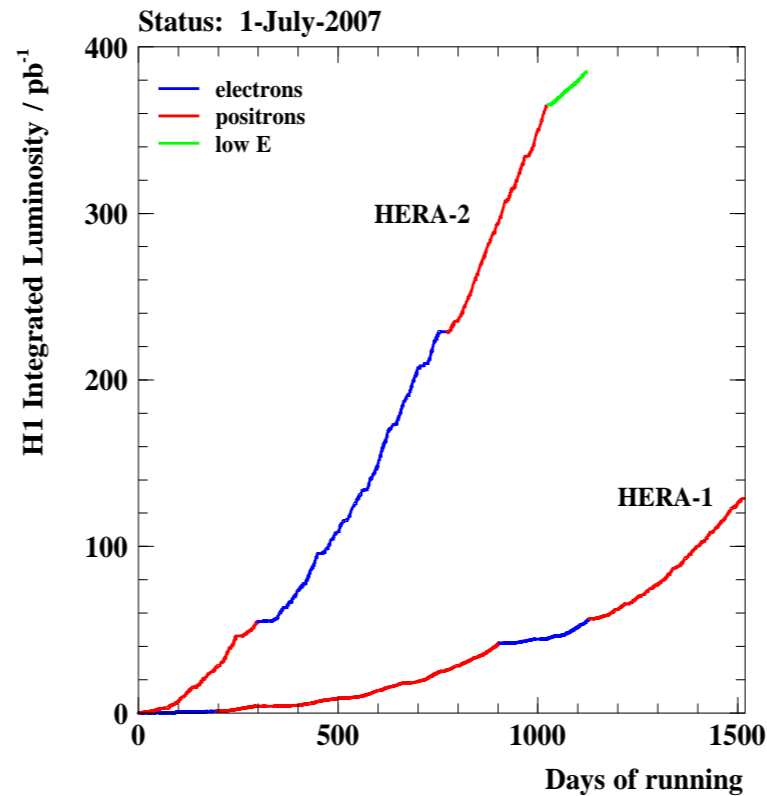
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for the H1 and ZEUS Collaborations  
QCD@LHC 2014, Suzdal, Russia, August 27, 2014



# HERA with the H1 and ZEUS detectors

## HERA $e^+p$ collider

- $\sqrt{s} = 319 \text{ GeV}$
- $E_e = 27.6 \text{ GeV}$
- $E_p = 920 \text{ GeV}$
- Operational until 2007



## Two multi-purpose experiments: H1 and ZEUS

- Luminosity:  $\sim 0.5 \text{ fb}^{-1}$  per experiment
- Excellent control over experimental uncertainties
  - Overconstrained system in DIS
  - Electron measurement: 0.5 – 1% scale uncertainty
  - Jet energy scale: 1%
  - Trigger and normalisation uncertainties: 1-2 %
  - Luminosity: 1.8 – 2.5%

# Inclusive deep-inelastic ep scattering (DIS)

ep scattering:  $e^\pm p \rightarrow e^\pm + X$

- Center-of-mass energy

$$\sqrt{s} = \sqrt{(k + p)^2}$$

- Virtuality of exchanged boson

$$Q^2 = -q^2 = -(k - k')^2$$

- Bjorken scaling variable

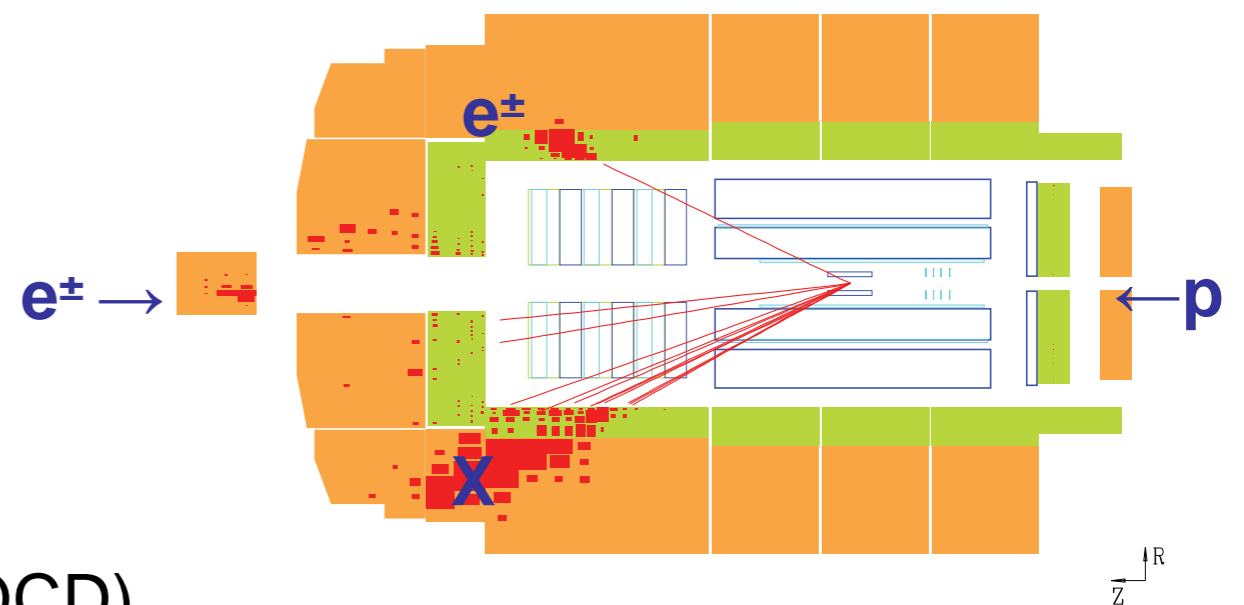
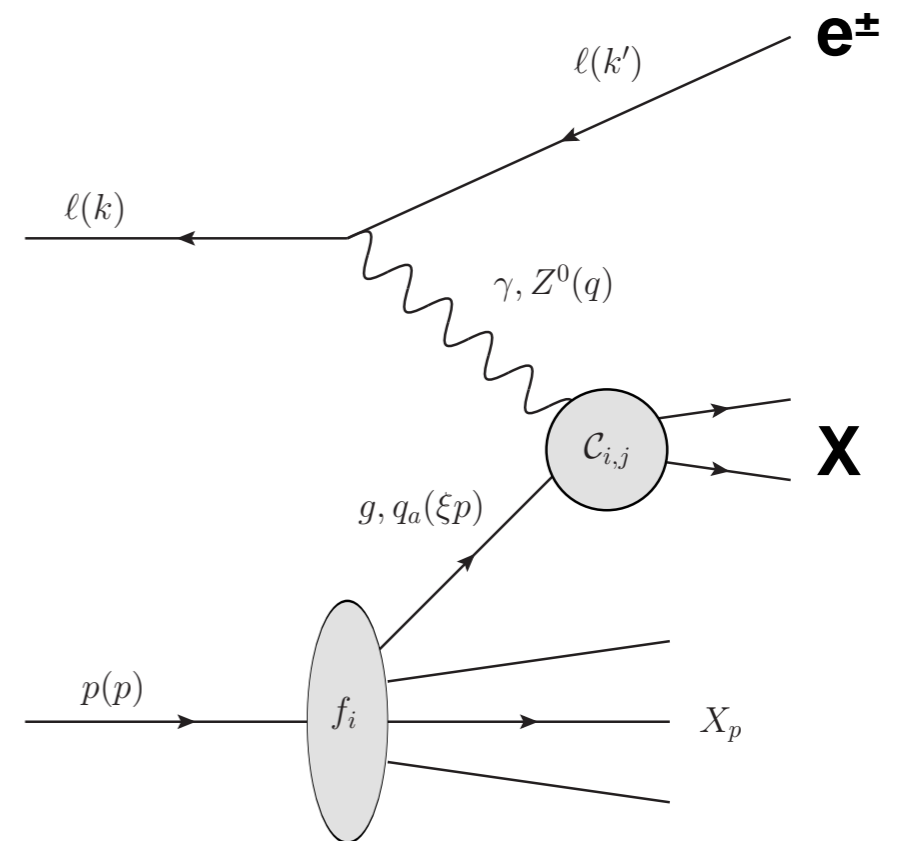
$$x_{\text{Bj}} = \frac{Q^2}{2p \cdot q}$$

- Inelasticity

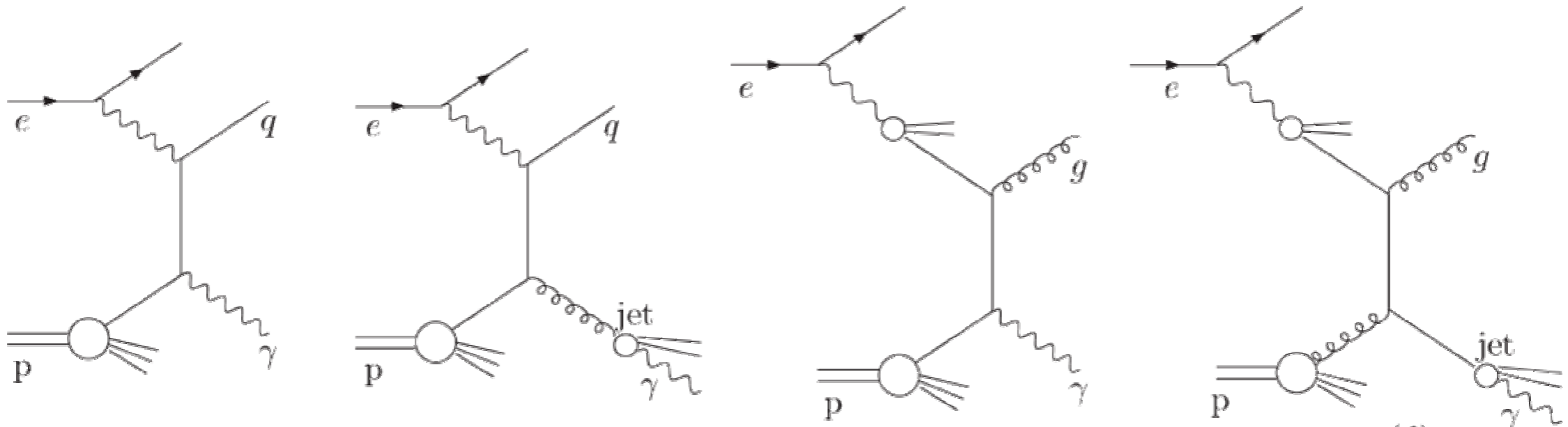
$$y = \frac{p \cdot q}{p \cdot k}$$

## Cross section calculation

- Collinear factorisation
- Hard scattering calculable in QCD (pQCD)
- PDFs have to be determined from experiment



# Prompt photons in $\gamma p$ : $ep \rightarrow \gamma + X (+j) [+e]$



## Prompt photons in photoproduction ( $Q^2 \rightarrow 0 \text{ GeV}^2$ )

- Direct ( $x_V^{\text{meas}} \rightarrow 1$ ) and resolved ( $x_V^{\text{meas}} < 0.8$ ) processes
- Prompt radiation and fragmentation

Partonic momentum fraction of the photon:

$$x_{\gamma}^{\text{meas}} = \frac{E^{\gamma} + E^{\text{jet}} - p_Z^{\gamma} - p_Z^{\text{jet}}}{E^{\text{all}} - p_Z^{\text{all}}}$$

Measured *with* and *without* accompanying jet [ZEUS Coll. Phys Lett B 730 (2014) 293]

Measured separately for **direct-** and **resolved-enhanced** region [arXiv:1405.7127]

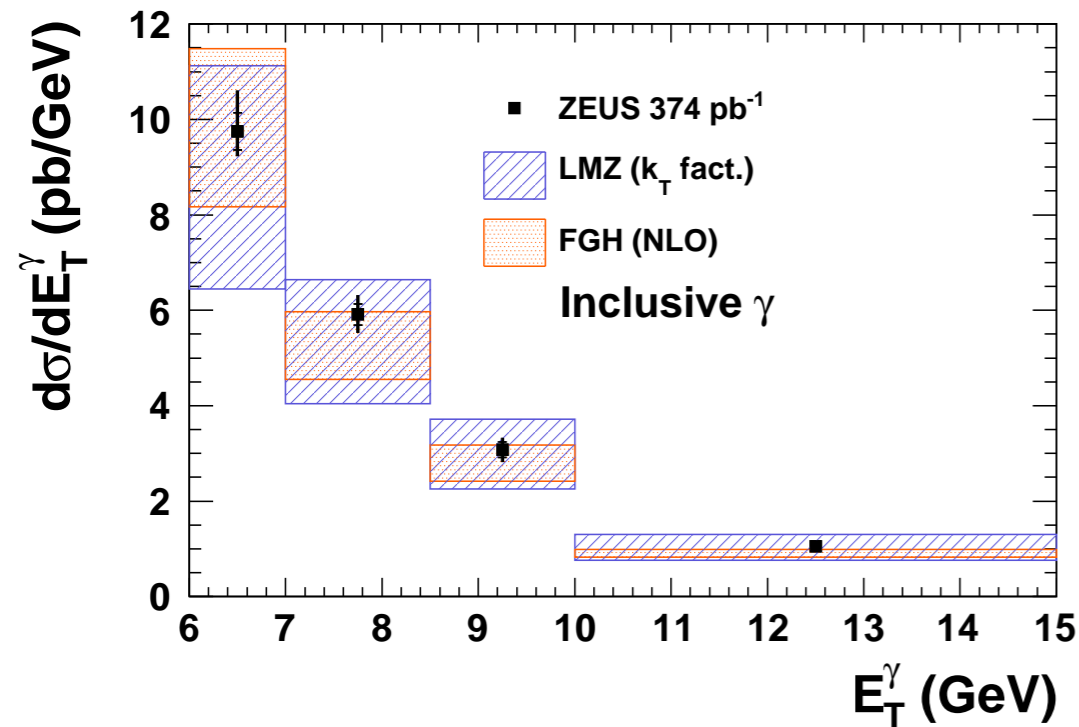
## Theory

**FGH**: NLO with fragmentation functions ( $O(\alpha^3 \alpha_s^2)$ )

**LMZ**:  $k_T$  factorisation with unintegrated parton densities

# Prompt photons in $\gamma p$ : $ep \rightarrow \gamma + X$ (+jet) [+e]

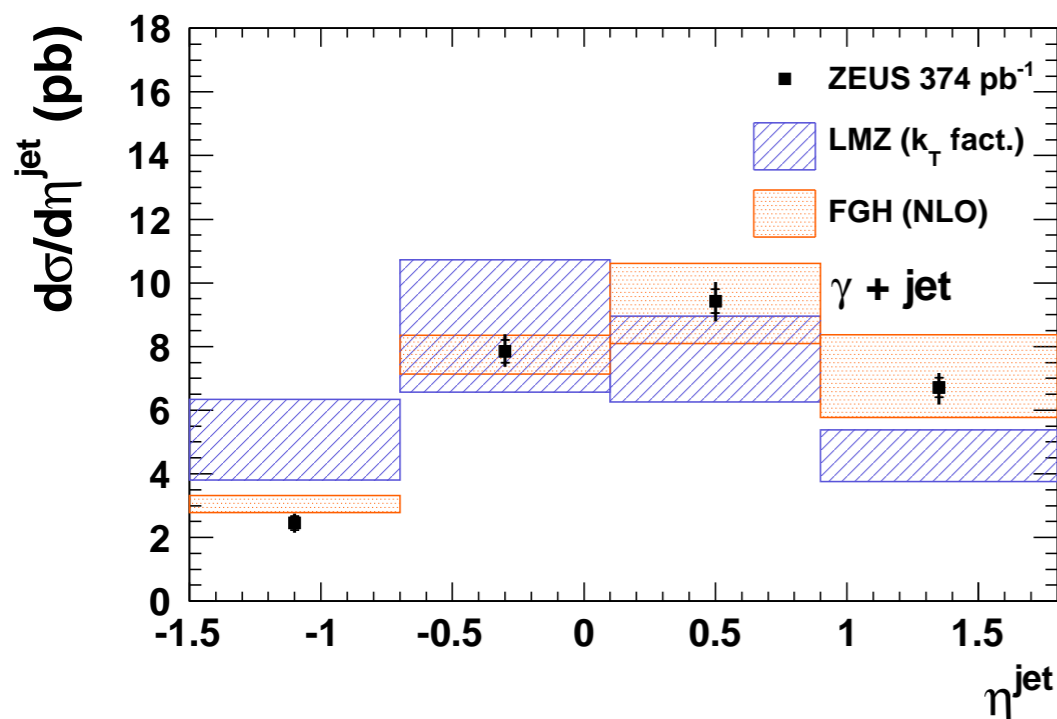
## ZEUS



### Cross sections: Inclusive $\gamma$ production

- NLO predictions give good description
- LMZ ( $k_T$  factorisation) give good description
- Experimental uncertainties are substantially smaller than theoretical ones

## ZEUS

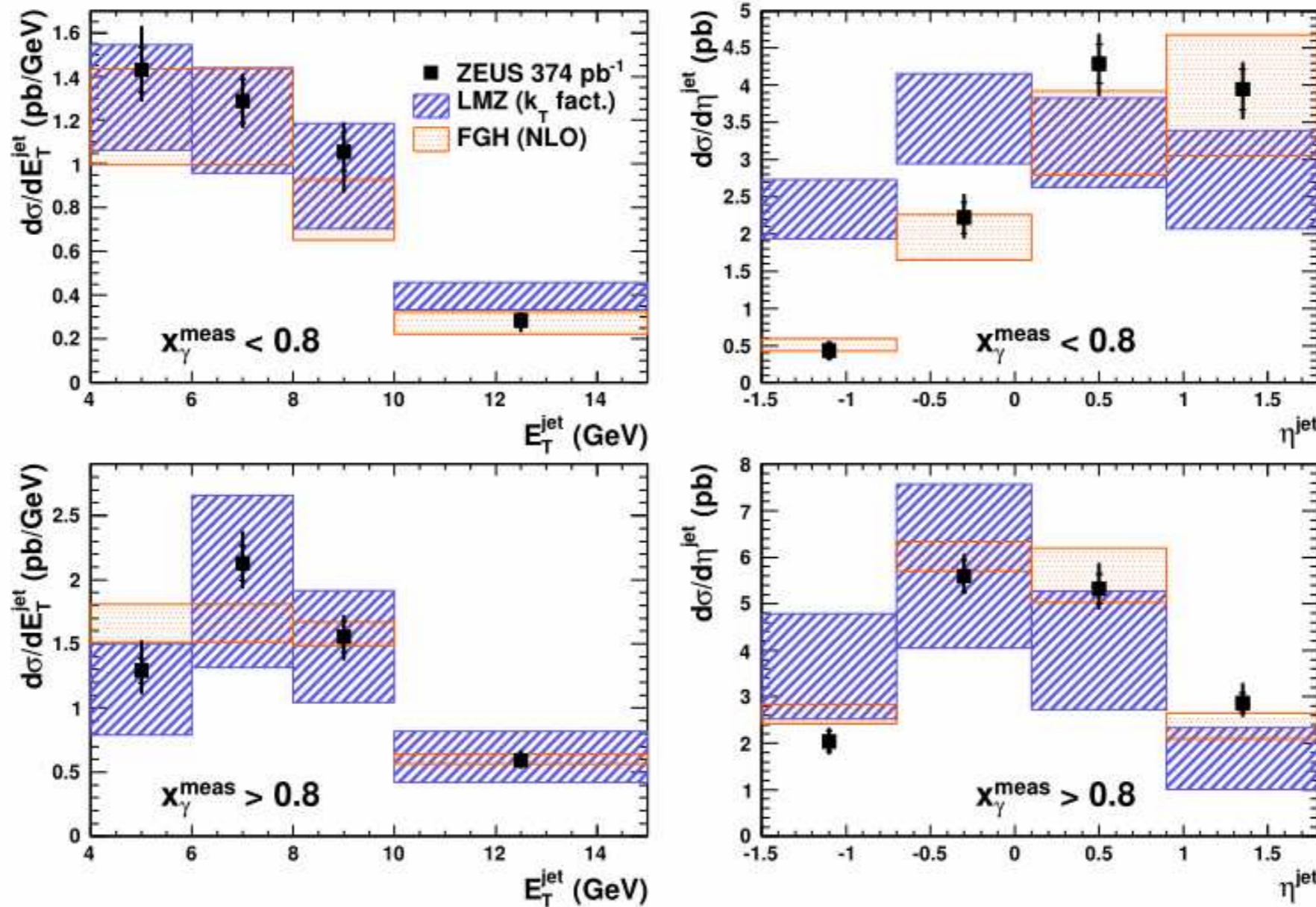


### Cross sections: $\gamma + \text{jet}$

- In general both predictions agree well with data
  - Normalisation well described
  - Fixed order NLO give better description of  $\eta_{\text{jet}}$  shape
- Theoretical uncertainties are smaller compared to  $\gamma$  inclusive cross sections

# Further studies: $ep \rightarrow \gamma + \text{jet} + X [+e]$

## ZEUS



### Cross section as function of jet variables in bins of $x_\gamma^{\text{meas}}$

- Both theories within large uncertainties agree well with the data
- Except LMZ in  $\eta^{\text{jet}}$  at  $x_\gamma^{\text{meas}} < 0.8$

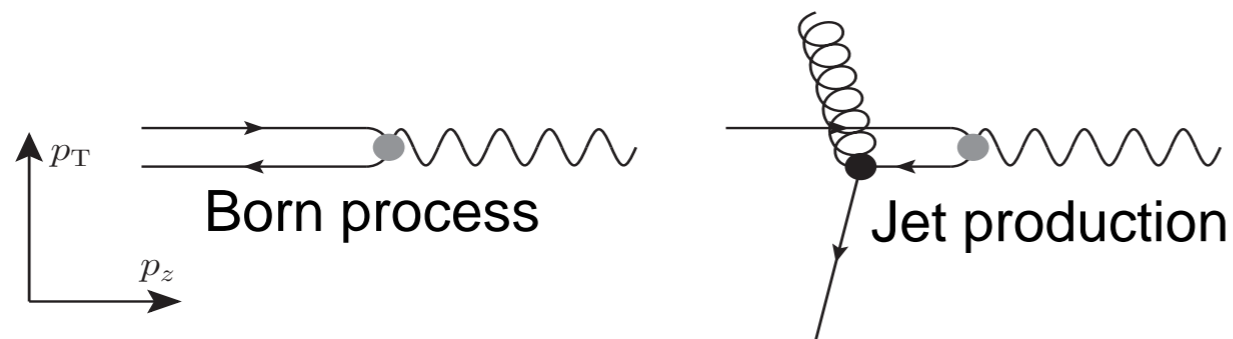
See also talk by M. Nefedov on thursday

Further observables studied, like azimuthal difference, difference in pseudorapidity, ...

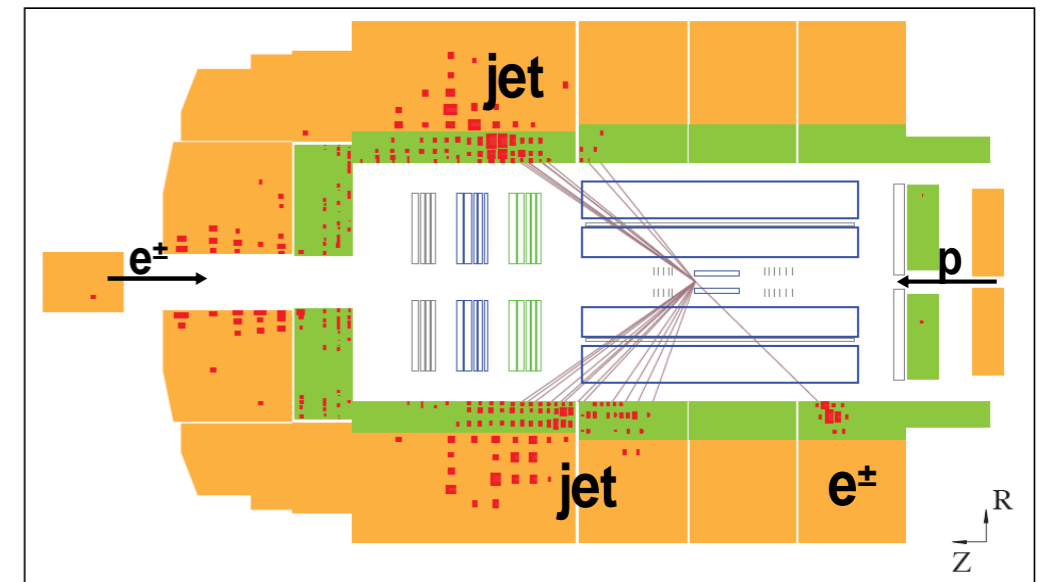
# Jet production in neutral current DIS

Jet measurements performed in  
'Breit frame'

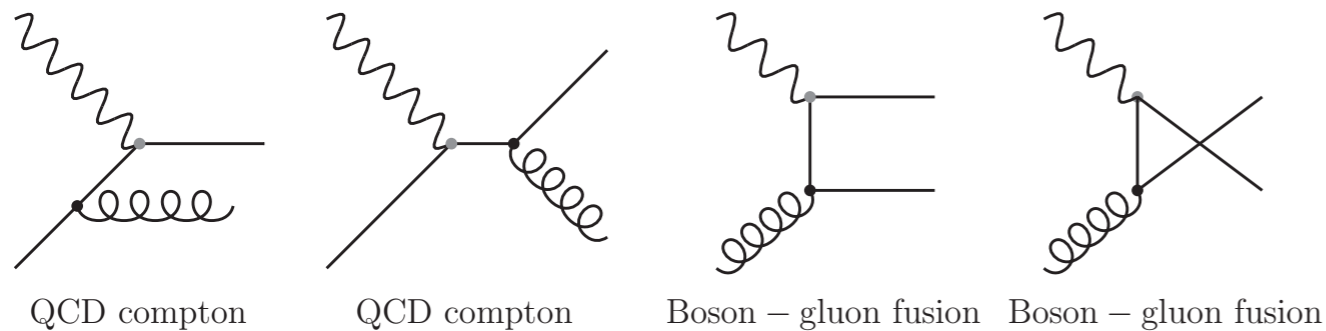
Breit frame fulfils equation  $2x_{Bj}p + k = 0$



Events show two-jet topology



Jet production in leading-order pQCD



**Inclusive jet**

Count every single jet

Measure transverse momentum

**Dijet and trijet observable**

Average momentum of two/three leading jets

$$\langle p_T \rangle_2 = (p_T^{\text{jet}1} + p_T^{\text{jet}2})/2$$

**Jet production is directly sensitive to  $\alpha_s$**

# Trijet measurement in DIS (ZEUS)

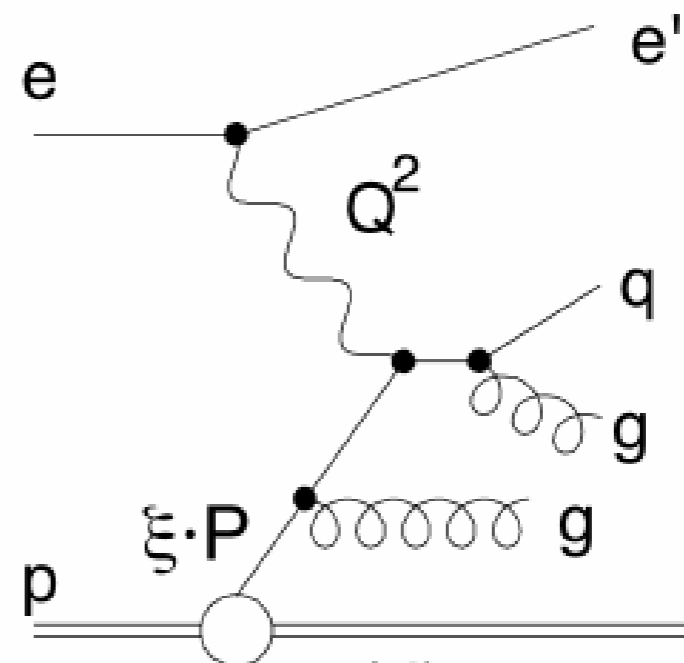
**Trijet production in neutral current DIS has been measured**

(ZEUS-prel-14-008) with:

- Photon virtuality  $125 < Q^2 < 20000 \text{ GeV}^2$
- Inelasticity:  $0.2 < y < 0.6$
- Jet transverse momentum  $E_{T,B}^{\text{jet}} > 8 \text{ GeV}$

## Statistics

- $L = 295 \text{ pb}^{-1}$



**A major source of systematic uncertainties:**

jet energy scale  $\sim 1\%$  ( $3\%$ ), for jets with  $E_{T,L}^{\text{jet}} > 10 \text{ GeV}$  ( $< 10 \text{ GeV}$ )

## NLO Calculation

NLOJet++ corrected for

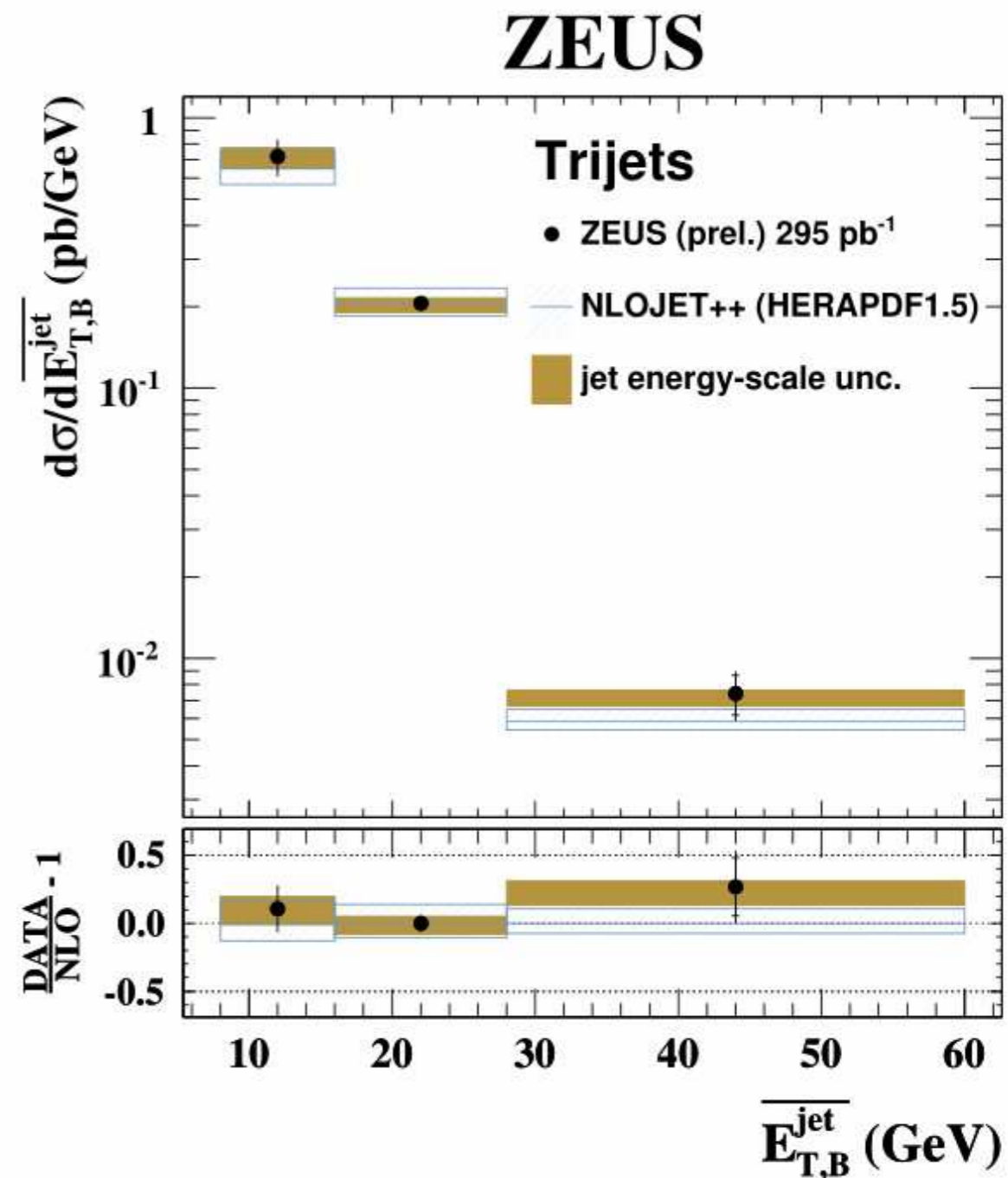
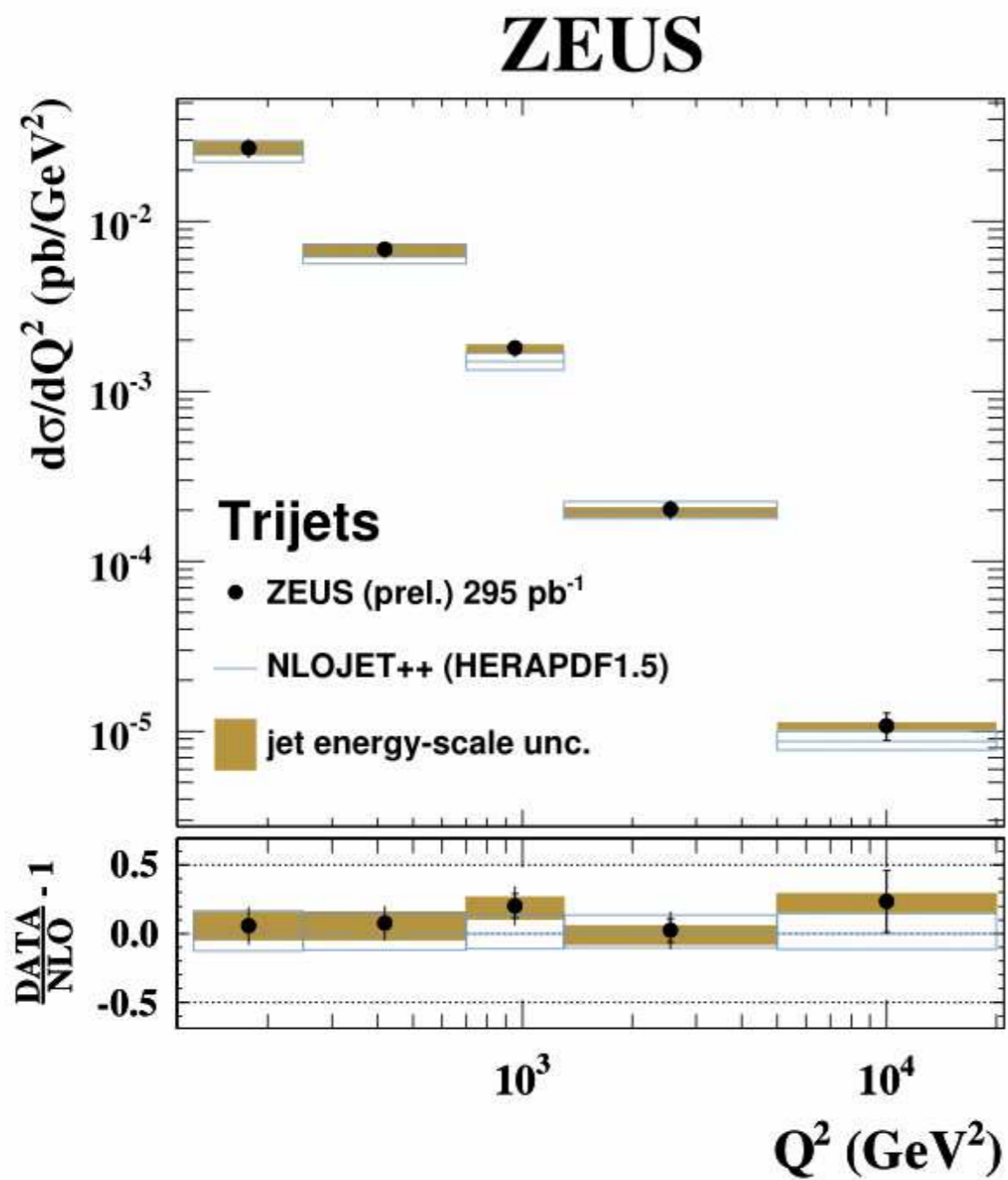
- hadronisation effects
- HERAPDF1.5

## Scale Choice:

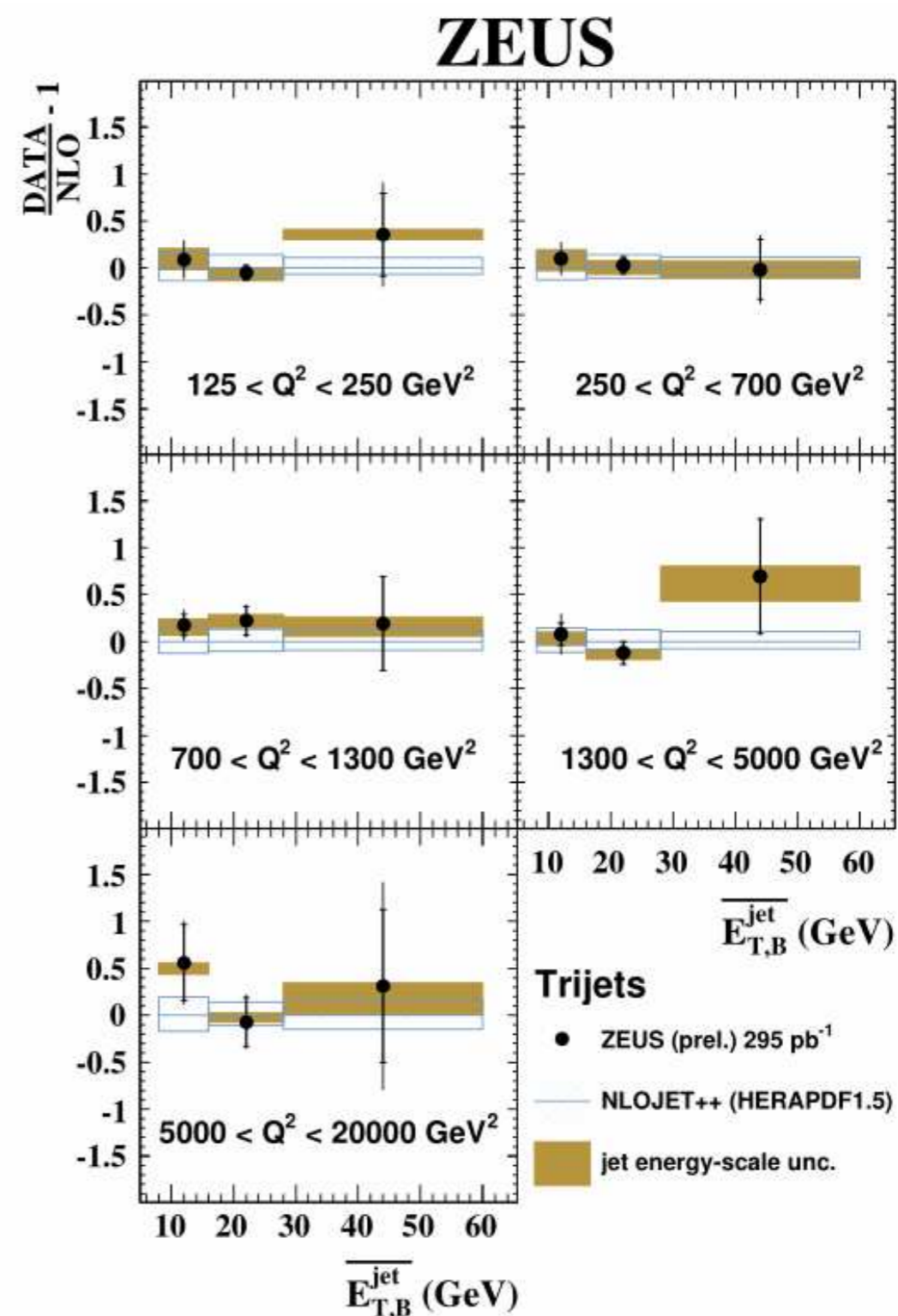
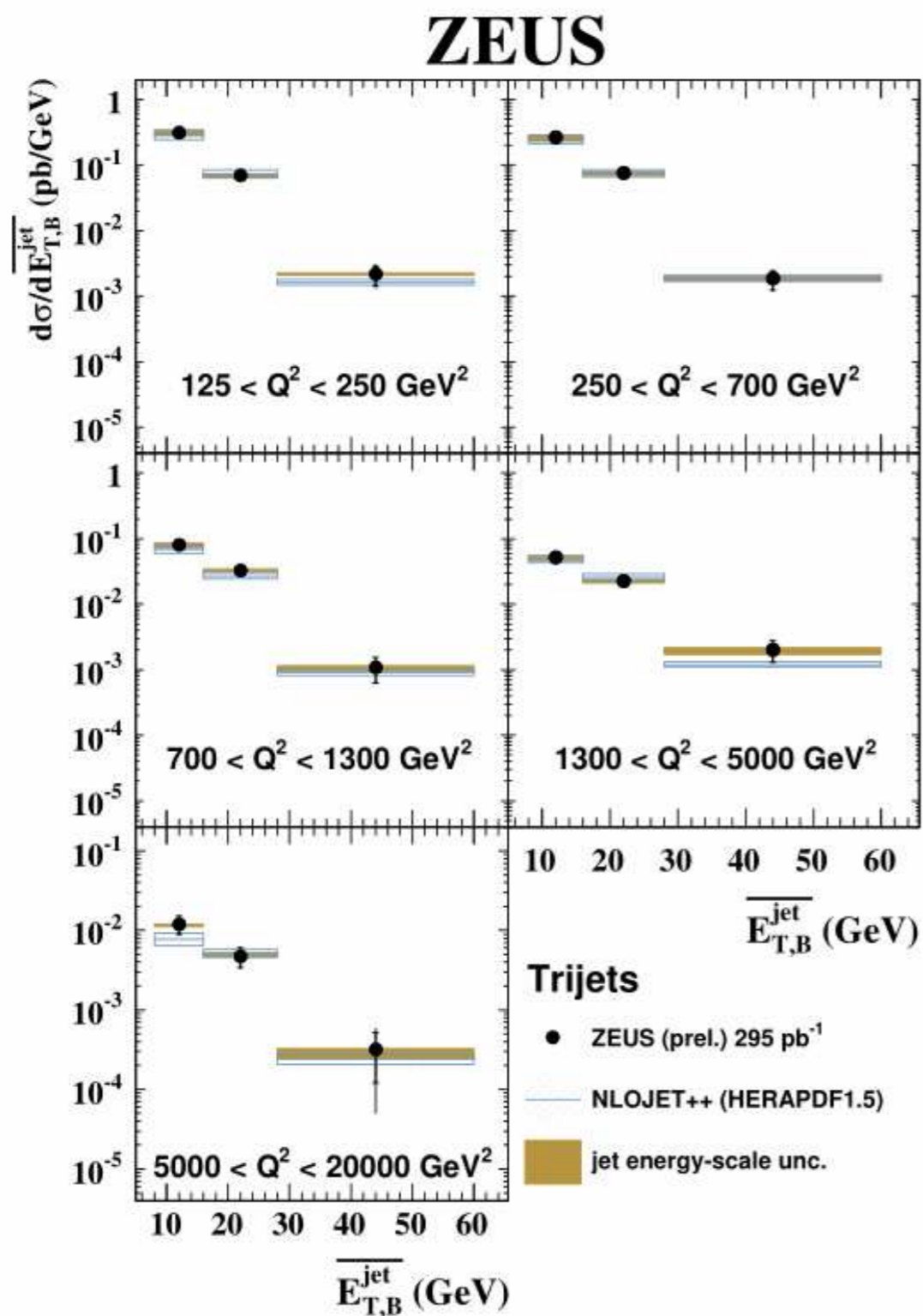
- $\mu_f^2 = Q^2$
- $\mu_r^2 = Q^2 + \langle E_{T,B}^{\text{jet}} \rangle$



# Single differential trijet cross sections



# Double differential trijet cross sections



Good agreement between data and NLO calculations

# Multijet at high $Q^2$ – Inclusive Jet, Dijet, Trijet (H1)

## Simultaneous Measurement of

- inclusive jet, dijet and trijet cross sections

## Also measured

- normalised inclusive jet, dijet and trijet cross sections
- Normalisation w.r.t. inclusive NC DIS
- (Partial) cancellation of exp. uncertainties

### Neutral current phase space

$$150 < Q^2 < 15000 \text{ GeV}^2$$

$$0.2 < y < 0.7$$

### Jet acceptance

$$-1.0 < \eta_{\text{lab}} < 2.5$$

### Inclusive Jet

$$7 < p_T^{\text{jet}} < 50 \text{ GeV}$$

### Dijet and Trijet

$$5 < p_T^{\text{jet}} < 50 \text{ GeV}$$

$$M_{12} > 16 \text{ GeV}$$

$$7 < \langle p_T \rangle < 50 \text{ GeV}$$

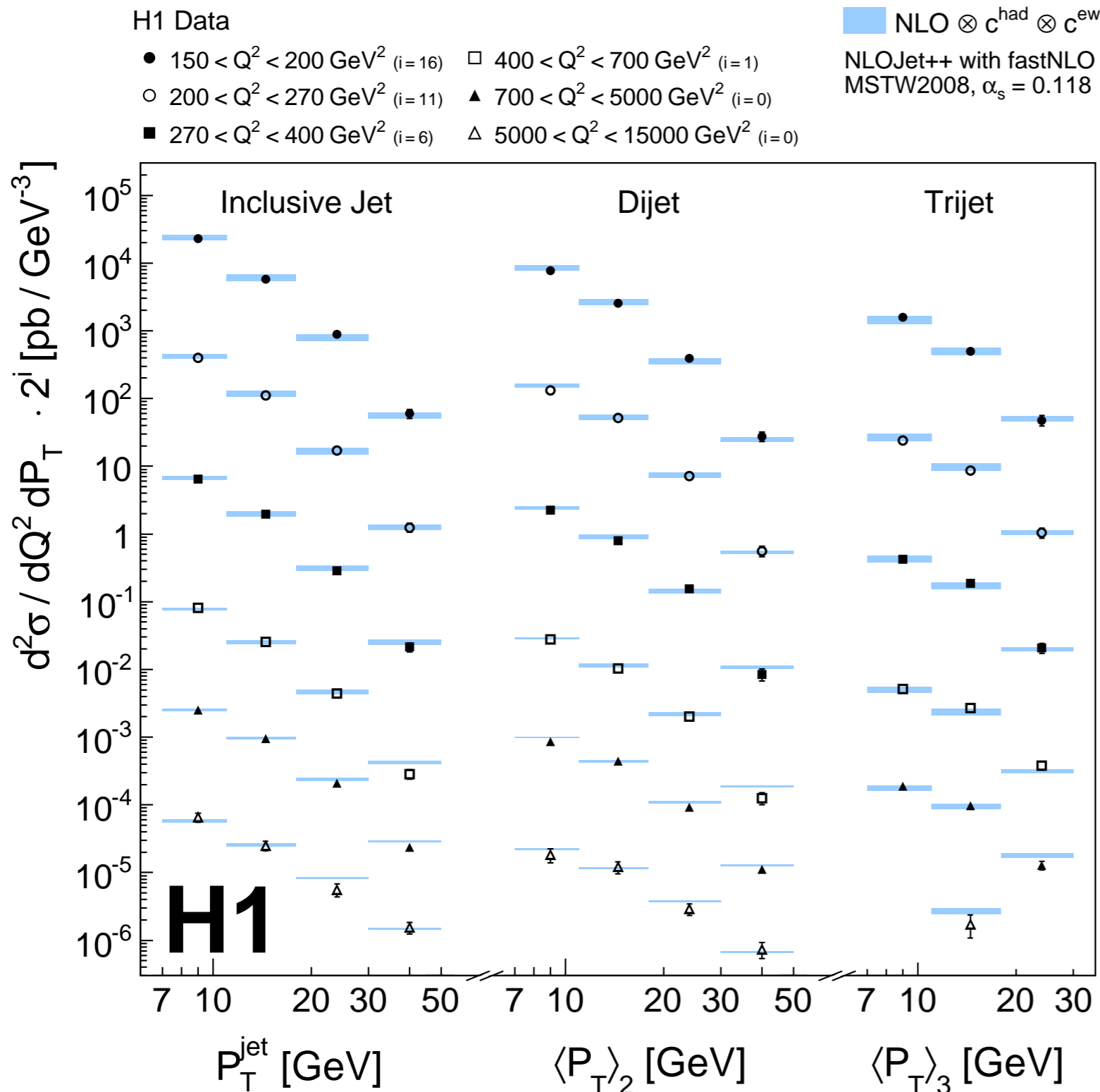
## Multidimensional Regularised Unfolding

- 4 double-differential measurements are unfolded simultaneously
  - NC DIS, inclusive jet, dijet and trijet
- Using TUnfold tool
  - Statistical correlations considered
  - Enlarged phase space for migrations
  - Up to 7 observables are considered for migrations

### Migration Matrix

		$\varepsilon_1$	$\varepsilon_2$	$\varepsilon_3$
Detector level	$\varepsilon_3$	Reconstructed Trijet events which are not generated as Trijet event		Trijet $Q^2, \langle p_T \rangle_3, y,$ Trijet-cuts
	$\varepsilon_2$	Reconstructed Dijet events which are not generated as Dijet event	Dijet $Q^2, \langle p_T \rangle_2, y,$ Dijet-cuts	
	$\varepsilon_1$	Reconstructed jets without match to generator level	Incl. Jet $p_T^{\text{jet}}, Q^2, y, \eta$	
		NC DIS $Q^2, y$		
		Hadron level		

# Multijet at high $Q^2$ – Inclusive Jet, Dijet, Trijet (H1)



## NLO Calculations

NLOJet++ corrected for

- hadronisation effects

Scale Choice:

- $\mu_f^2 = Q^2$
- $\mu_r^2 = (Q^2 + P_T^2) / 2$

Theory uncertainty

- Vary scales by factor 2

**NLO QCD with MSTW2008 describes well inclusive jet, dijet and trijet differential cross sections**

# Multijet at high $Q^2$ – Inclusive Jet, Dijet, Trijet (H1)

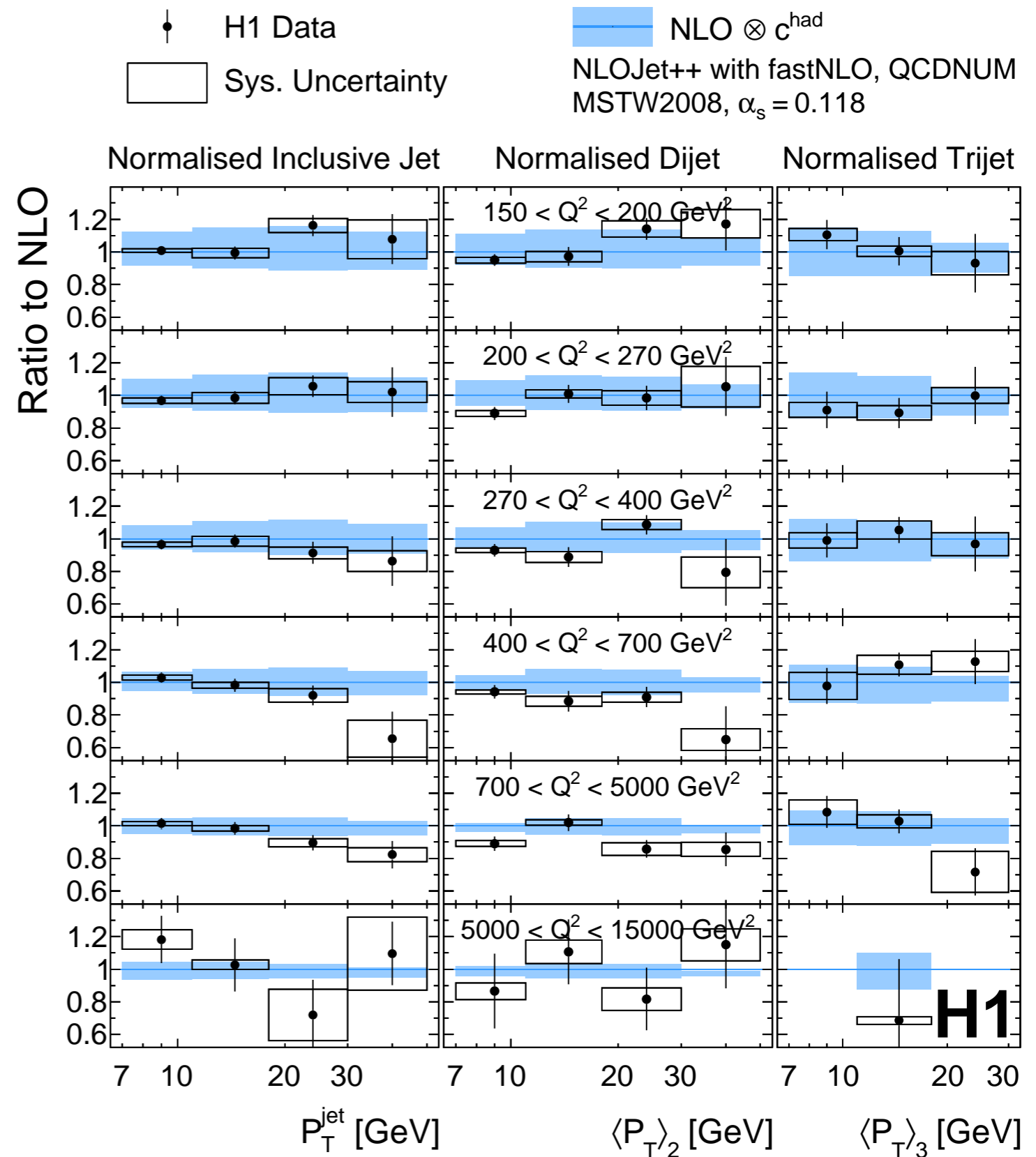
## Ratio to NLO calculations

### Normalised Multijets

- Cancellation of experimental uncertainties
  - Normalisation uncertainties cancel
  - Other exp. uncertainties cancel partially

**Experimental precision higher than theory uncertainty from scale variations**

**Overall good description of data by theory in NLO**



# Extraction of strong coupling constant $\alpha_s$

## Extraction of strong coupling constant $\alpha_s(M_Z)$

### Iterative $\chi^2$ minimisation

- Fit theory ( $t$ ) to data ( $m$ ) taking stat. correlations into account ( $V$ )
- $\alpha_s(M_Z)$  and  $\varepsilon$  are free parameters in the fit

$$\chi^2 = \vec{p}^T V^{-1} \vec{p} + \sum_k^{N_{\text{sys}}} \varepsilon_k^2$$

$$p_i = \log m_i - \log t_i - \sum_k^{N_{\text{sys}}} E_{i,k}$$

$$E_{i,k} = \sqrt{f_k^C} \left( \frac{\delta_{m,i}^{k,+} - \delta_{m,i}^{k,-}}{2} \varepsilon_k + \frac{\delta_{m,i}^{k,+} + \delta_{m,i}^{k,-}}{2} \varepsilon_k^2 \right)$$

- Consistent treatment of all uncertainties  $\delta$  (stat., uncorr., corr.)  
 -> uncertainties are considered as *log-normal* distributed and as '*relative*' uncertainties

# Extraction of strong coupling constant $\alpha_s$

## Extraction of strong coupling constant $\alpha_s(M_Z)$

- Jet cross sections directly sensitive to  $\alpha_s(M_Z)$
- Simultaneous  $\chi^2$ -fit to normalised inclusive jet, dijet and trijet cross sections

$$\alpha_s(M_Z)|_{k_T} = 0.1165 \text{ (8)}_{\text{exp}} \text{ (5)}_{\text{PDF}} \text{ (7)}_{\text{PDFset}} \text{ (3)}_{\text{PDF}(\alpha_s)} \text{ (8)}_{\text{had}} \text{ (36)}_{\mu_r} \text{ (5)}_{\mu_f}$$

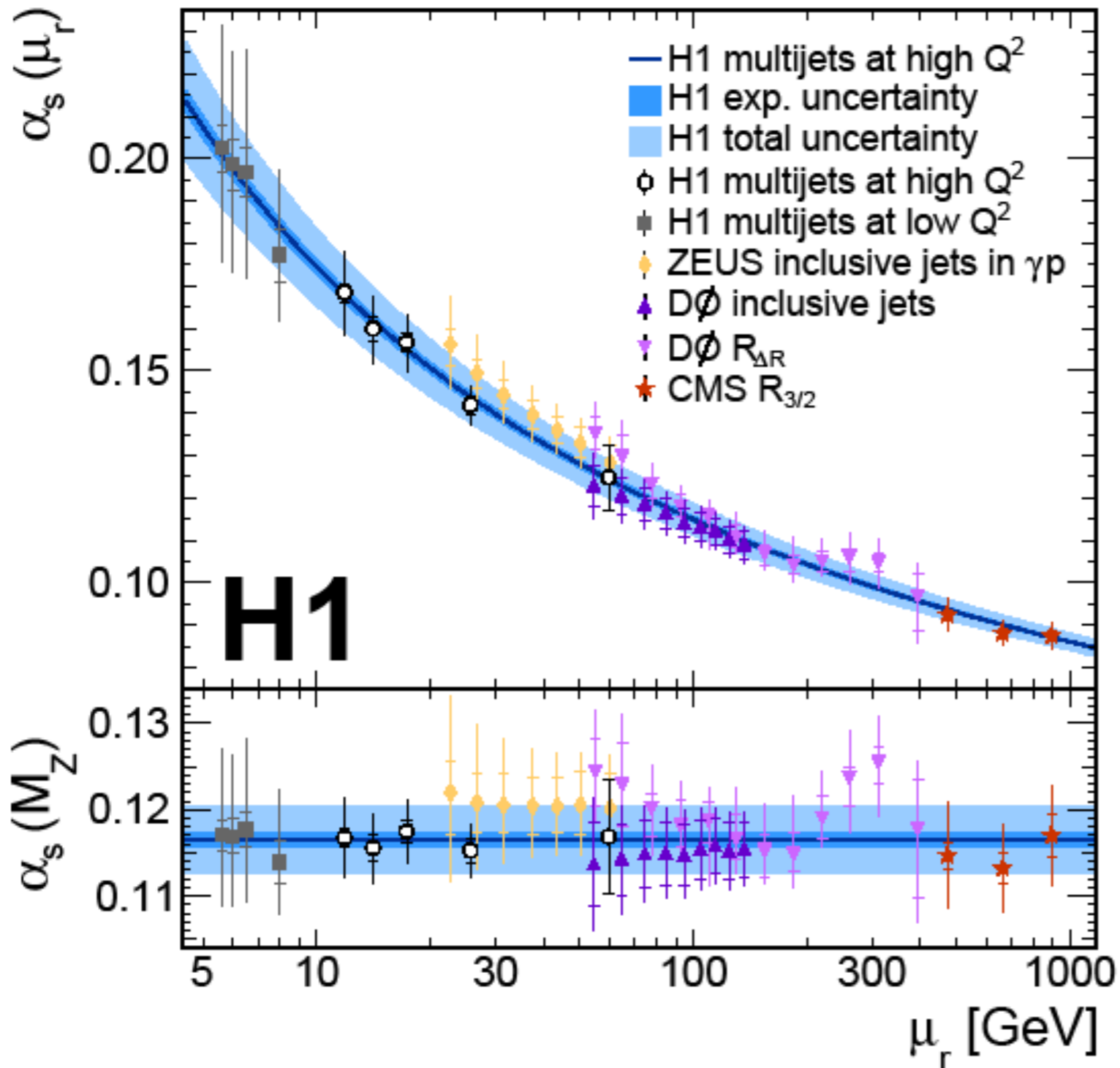
$$= 0.1165 \text{ (8)}_{\text{exp}} \text{ (38)}_{\text{pdf,theo}} \cdot$$

- Experimental uncertainty significantly smaller than theoretical one
- Higher order calculations mandatory
- Value consistent with value extracted using anti- $k_t$  jets

Most precise value of  $\alpha_s(M_Z)$  from jet cross sections

Normalised jet cross sections can be used in PDF fit together with inclusive data

# Extraction of strong coupling constant $\alpha_s$



## Determination of $\alpha_s(M_Z)$ at various scales

- H1 Multijet cross sections with superior precision
- Consistency with other jet data
- Confirmation of prediction by SU(3) over more than two orders of magnitude
- Recent ZEUS trijet data will also be used for  $\alpha_s$  extraction in future



# Extraction of strong coupling constant $\alpha_s$

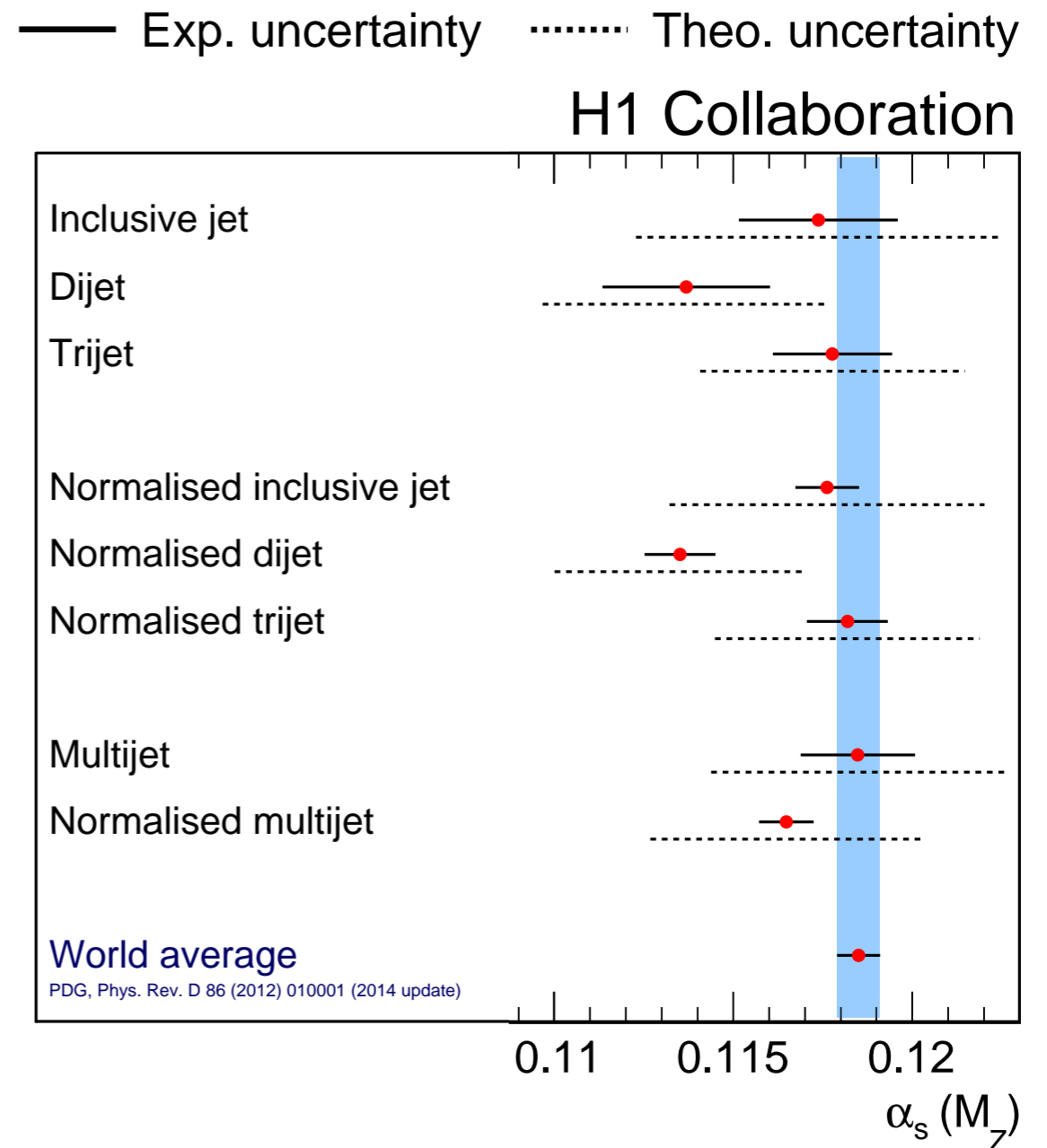
## Extraction separately for absolute and normalised

- Inclusive jet
- Dijet
- Trijet

## Values consistent within total uncertainties

## Value of $\alpha_s(M_Z)$ from dijet cross sections smaller than from inclusive jet or trijets

- Seen in all previous H1 and ZEUS studies
- Most likely attributed to higher order contributions in phase space regions which are different in the dijet and the inclusive jet measurement



# QCD Instantons

## QCD Instantons

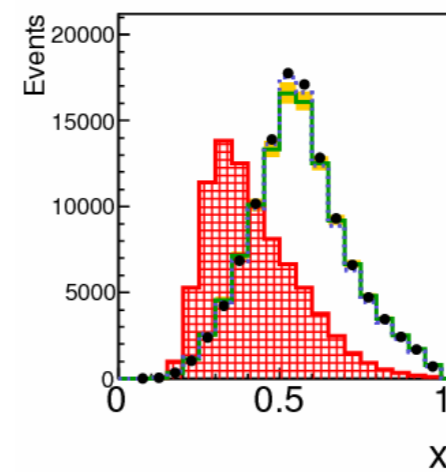
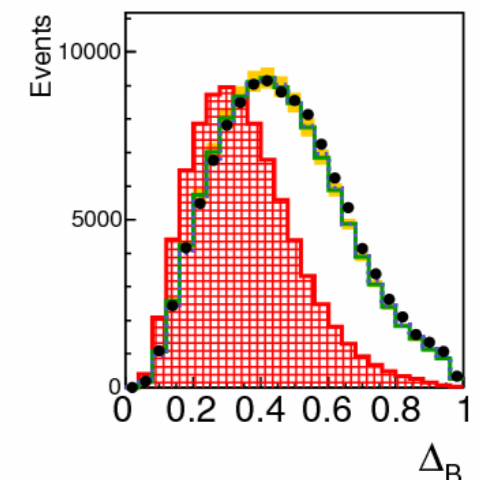
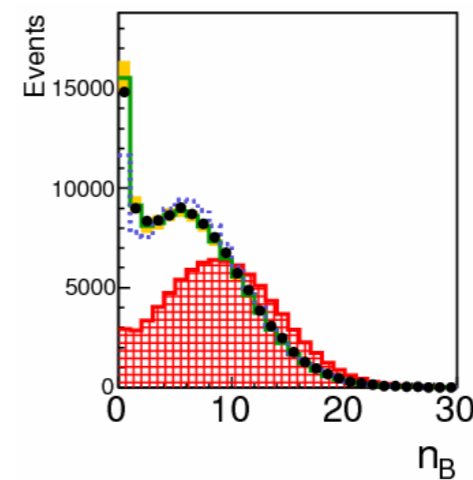
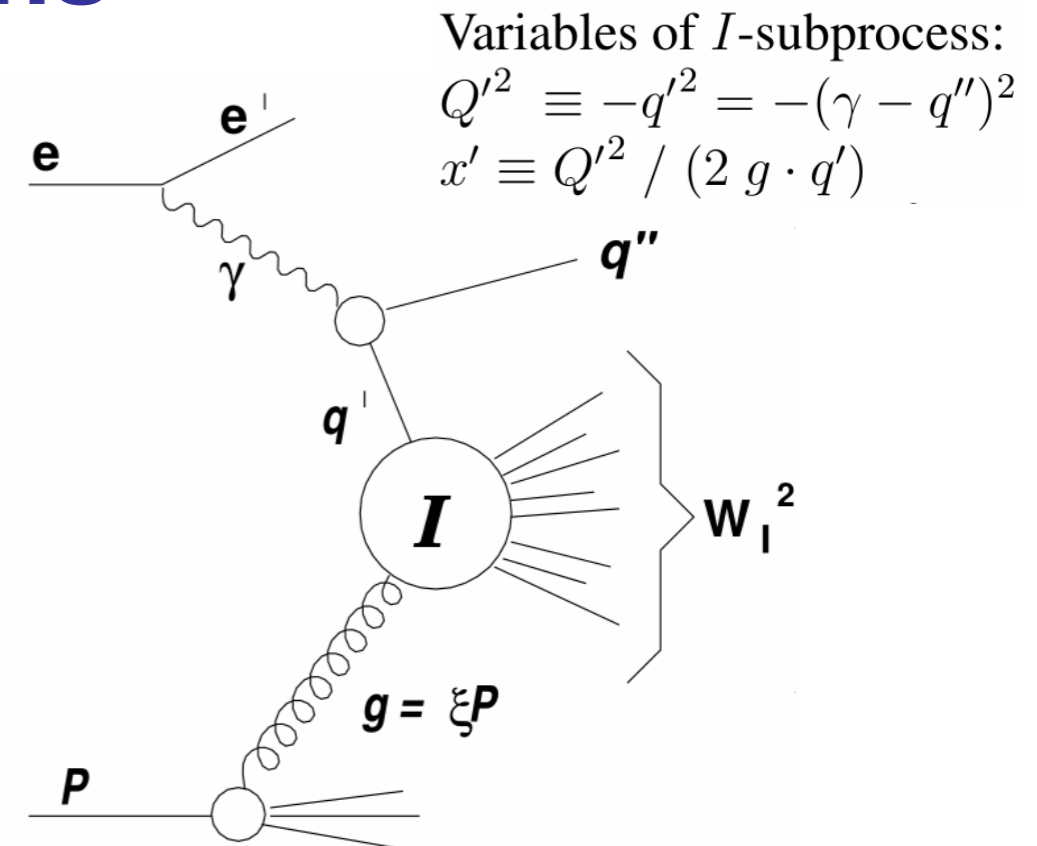
- Solution to Yang-Mills equation of motion
- Physical interpretations:
  - Pseudo-particle or tunneling process between topologically different vacuum states

## Signatures

- One hard jet (not originating from instanton)
- Densely populated narrow band, flat in  $\varphi$
- Large particle multiplicities

## Strategy

- Find jets in hadronic center of mass frame
  - Remove hardest jet from HFS
- Boost to instanton rest frame and define variables
  - Topological: Sphericity, Fox-Wolfram moments, azimuthal isotropy ( $\Delta_B$ )...
  - Number of charged particles in band ( $n_B$ )
  - Energy of band ( $E_{\text{Inst.}}$ ), ...
- Variables are input to MVA



H1 Preliminary

- H1 Data
- ▨ QCDINS x 50
- ⋯ RAPGAP
- ▬ DJANGO

# QCD Instantons

## Multivariate analysis

Probability density estimator with range search (**PDERS**)

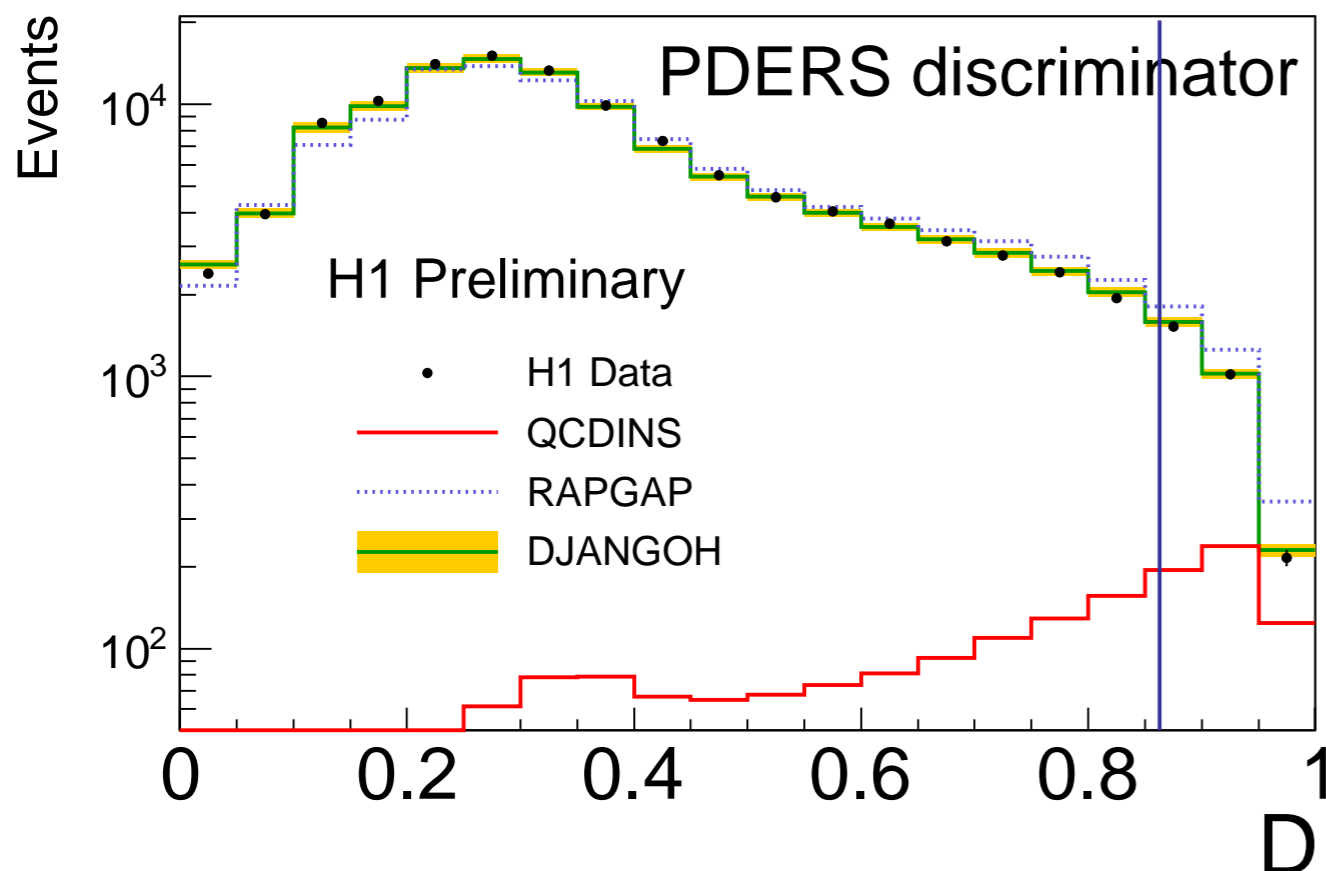
Training

- Rapgap, Django
- QCDINS (Ringwald, Schremp)

Good description of discriminator in background region

## Signal region

$D > 0.86$



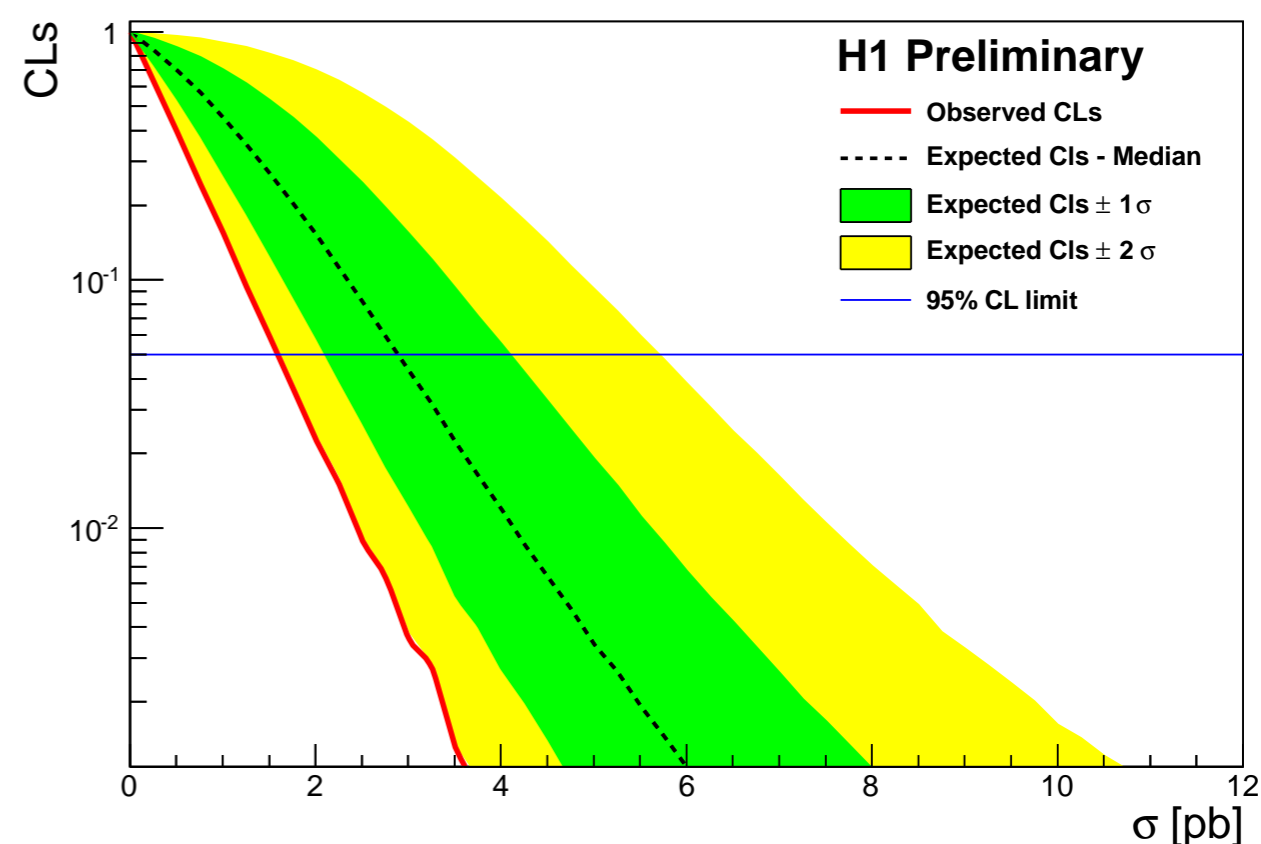
## Input for limit calculation

QCD Instanton cross section:  $10 \pm 2$  pb

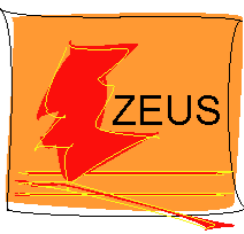
Uncertainties: Systematic and model

## Upper limit for 95% CL: 1.6pb

- Data are consistent with background
- No evidence for QCD Instantons
- Upper limit suggests exclusion of the Ringwald-Schremp's predictions for HERA QCD instantons.



# Summary



## New QCD results from HERA experiments with final data precision

Photons in photoproduction  $\rightarrow$  NLO and  $k_t$ -factorisation give good description

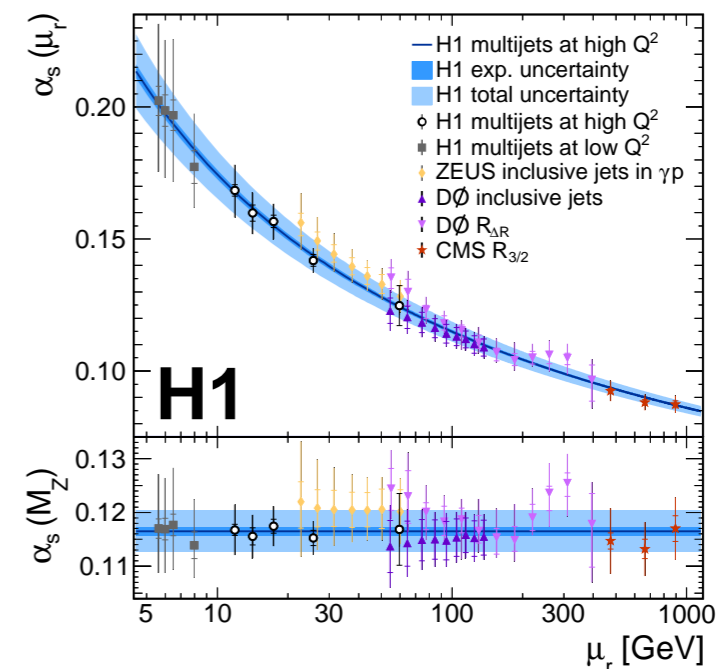
QCD Instanton  $\rightarrow$  Ringwald-Schrempp's solution appears to be excluded

Trijet cross sections in DIS  $\rightarrow$  Cross sections well described by theory

Multijet cross sections in DIS  $\rightarrow$  Data well described by NLO QCD

## Determination of strong coupling $\alpha_s$

- Multijet cross sections with high sensitivity and small experimental uncertainties
- Value consistent with world average value
- Most precise value from jet cross sections



The H1 and ZEUS experiments are finalizing their QCD physics program

# Backup

# Extraction of strong coupling constant $\alpha_s$

## Extraction of strong coupling constant $\alpha_s(M_Z)$

- Jet cross sections directly sensitive to  $\alpha_s(M_Z)$
- Simultaneous  $\chi^2$ -fit to inclusive jet, dijet and trijet cross sections

$$\alpha_s(M_Z)|_{k_T} = 0.1165 \text{ (8)}_{\text{exp}} \text{ (5)}_{\text{PDF}} \text{ (7)}_{\text{PDFset}} \text{ (3)}_{\text{PDF}(\alpha_s)} \text{ (8)}_{\text{had}} \text{ (36)}_{\mu_r} \text{ (5)}_{\mu_f}$$

$$= 0.1165 \text{ (8)}_{\text{exp}} \text{ (38)}_{\text{pdf,theo}} \cdot$$

**Comparison to current CMS inclusive jet value:** CMS-PAS-SMP-12-028  
CMS-PAS-SMP-12-027

$$\alpha_s(M_Z) = 0.1185 \pm 0.0019(\text{exp}) \pm 0.0028(\text{PDF}) \pm 0.0004(\text{NP}) \pm_{0.0022}^{0.0055} (\text{scale})$$

- 2.5 times higher experimental precision
- 3.3 times smaller PDF uncertainty

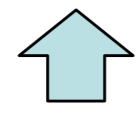
# $\alpha_s$ measurement

Slide from Chiara Roda from ICHEP 14 QCD summary

World average (2014)  
 $\alpha_s(M_Z) = 0.1185 \pm 0.0006$  (0.5%)

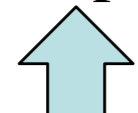
CMS Most recent: inclusive jet (5%)

$\alpha_s(M_Z) = 0.1185 \pm 0.0019(\text{exp}) \pm 0.0028(\text{PDF})$   
 $\pm 0.0004(\text{NP}) \pm_{0.0022}^{0.0055}(\text{scale})$

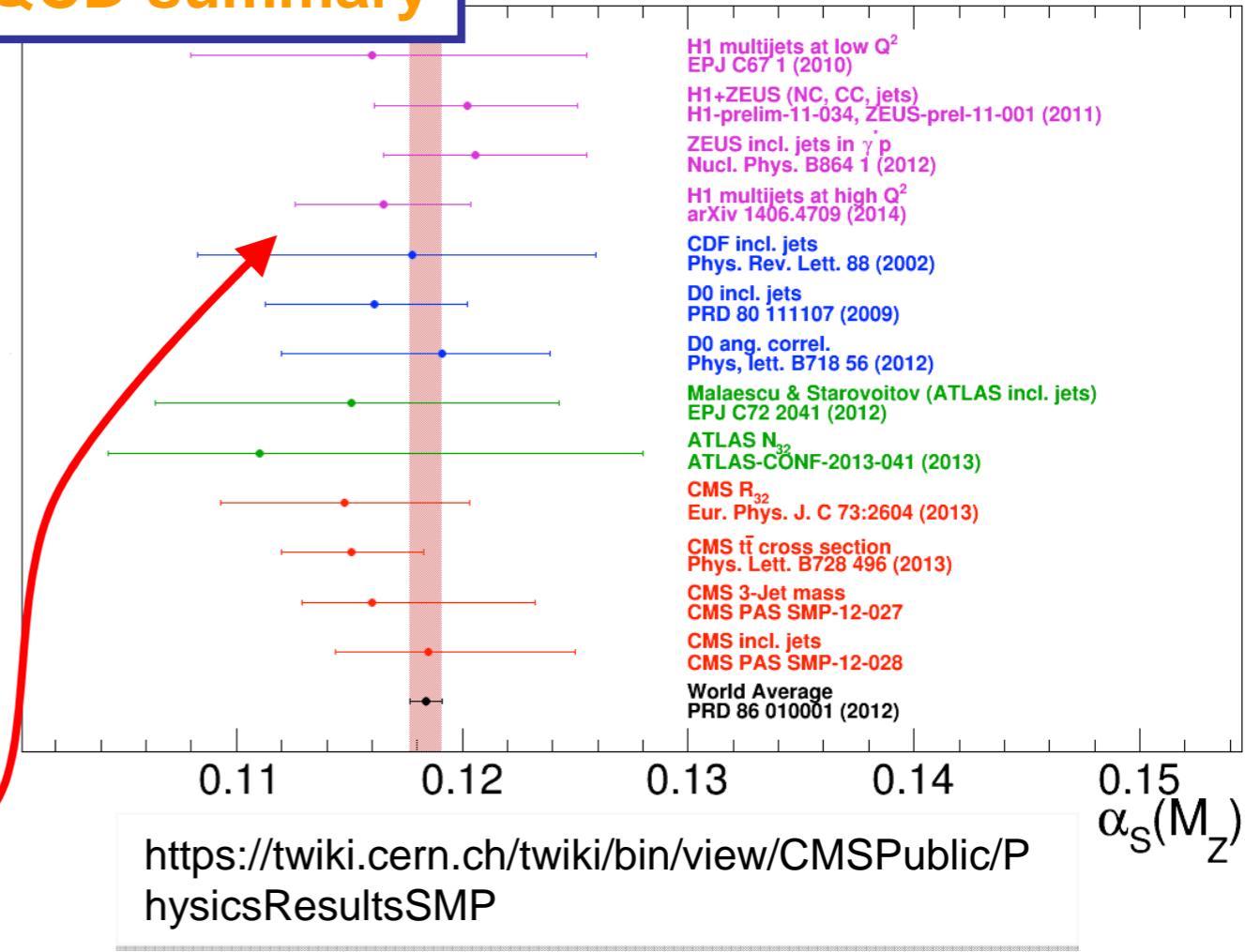


H1 most recent  $\alpha_s$  extraction from inclusive and multijet cross-section. Best precision is reached from fit to normalised multijet cross sections:

$\alpha_s = 0.1165 \pm 0.0008(\text{exp}) \pm 0.0038(\text{PDF, theo}) \leftarrow 0.0036(\text{scale})$



ICHEP-2014 2-9 July Varenhc exp. unc. 0.7%



# Correction of detector effects using regularised unfolding

## Detector effects

- Acceptance and efficiency
- Migrations due to limited resolution

## Aim

- Cross section on hadron level
- Direct matrix inversion of  $A$  often not possible

## Detector response

$$y = A \cdot x$$

- Measured vector  $y$
- Hadron level vector  $x$
- Detector response matrix  $A$
- Covariance matrix  $V_y$

## Regularised unfolding using Tunfold (JINST 7 (2012) T10003)

- Find hadron level  $x$  by analytic minimisation of

$$\chi^2(x, \tau) = \underbrace{(y - Ax)^T V_y^{-1} (y - Ax)}_{\text{Matrix inversion: } \chi^2} + \underbrace{\tau^2 (x - x_0)^T (L^T L) (x - x_0)}_{\text{Regularisation: } \chi^2}$$

- Find stationary point by solving analytically as function of  $x$
- ‘True’ hadron level can be determined directly

$$x = (A^T V_y^{-1} A + \tau^2 L^2)^{-1} A^T V_y^{-1} y =: B y$$

- $x$  (and  $L$ ) are free parameters



# Correlation matrix of all data points

## Covariance matrix

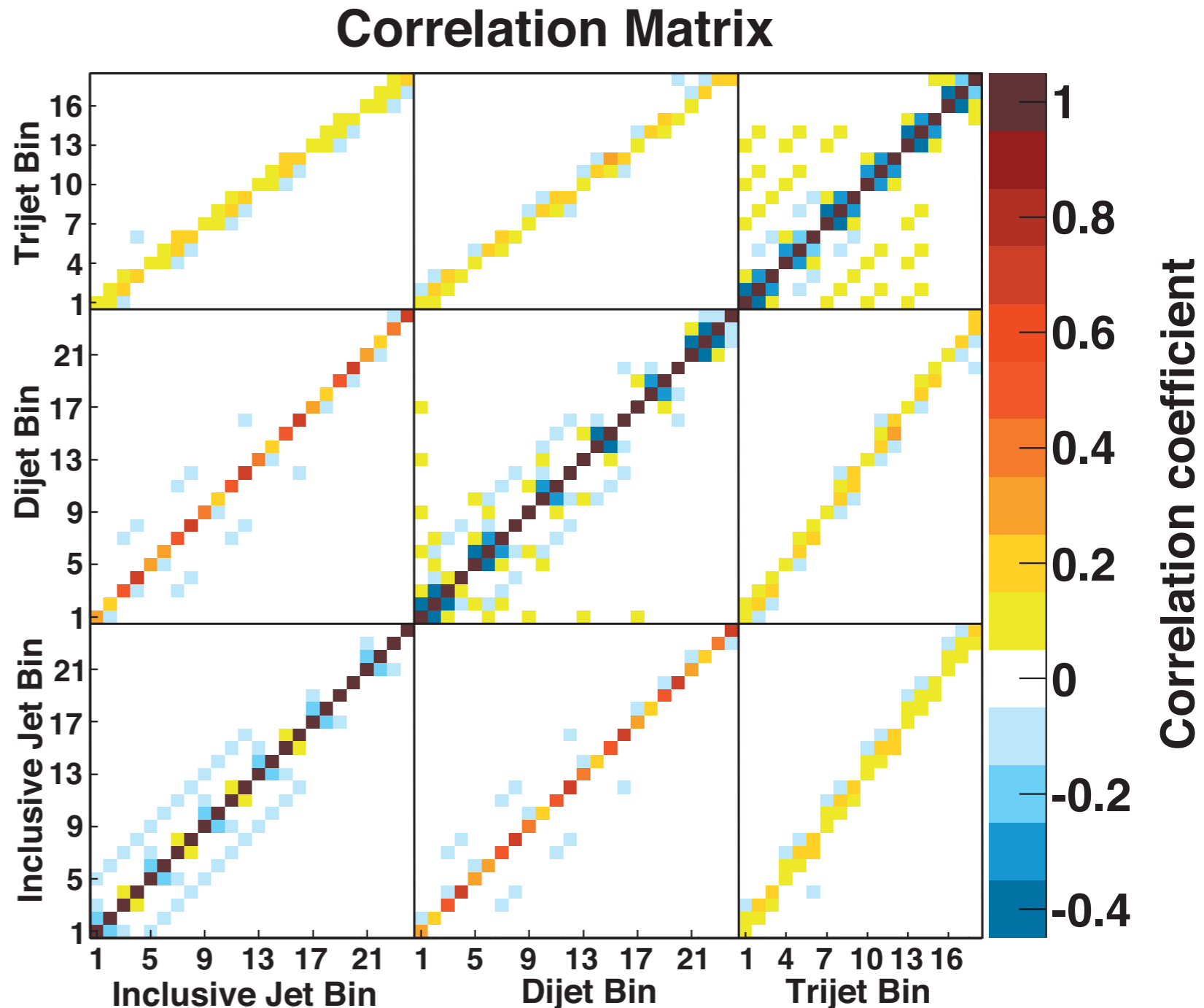
Obtained through linear error propagation of statistical uncertainties

## Correlations

- Resulting from unfolding
- Physical correlations
  - Between measurements
  - Within inclusive jet

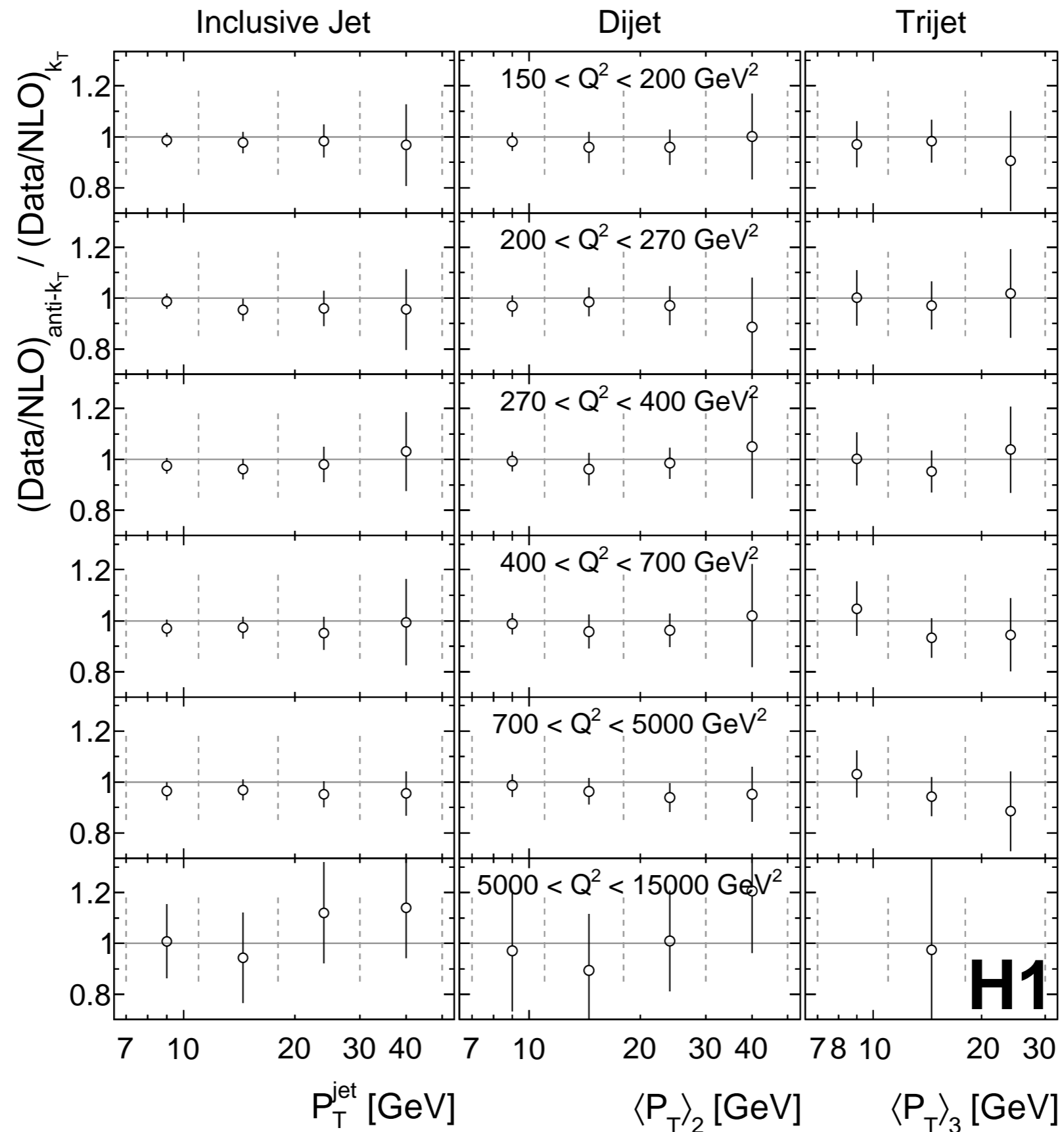
## Useful for

- Cross section ratios
- Combined fits
- Normalised cross sections

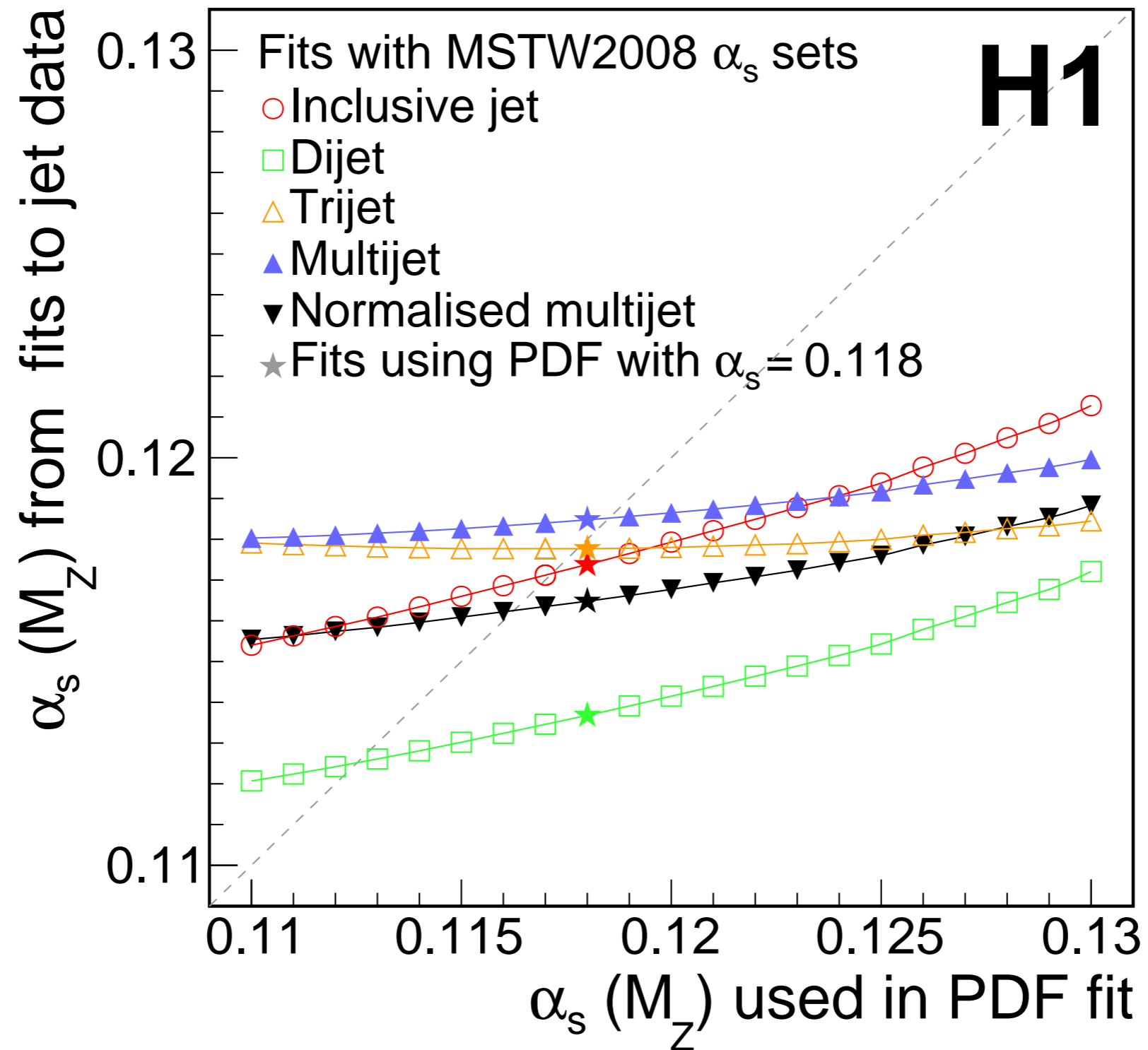


Correlation matrix is employed for correct error propagation for norm. cross sections

# Multijet Cross Sections at High $Q^2$

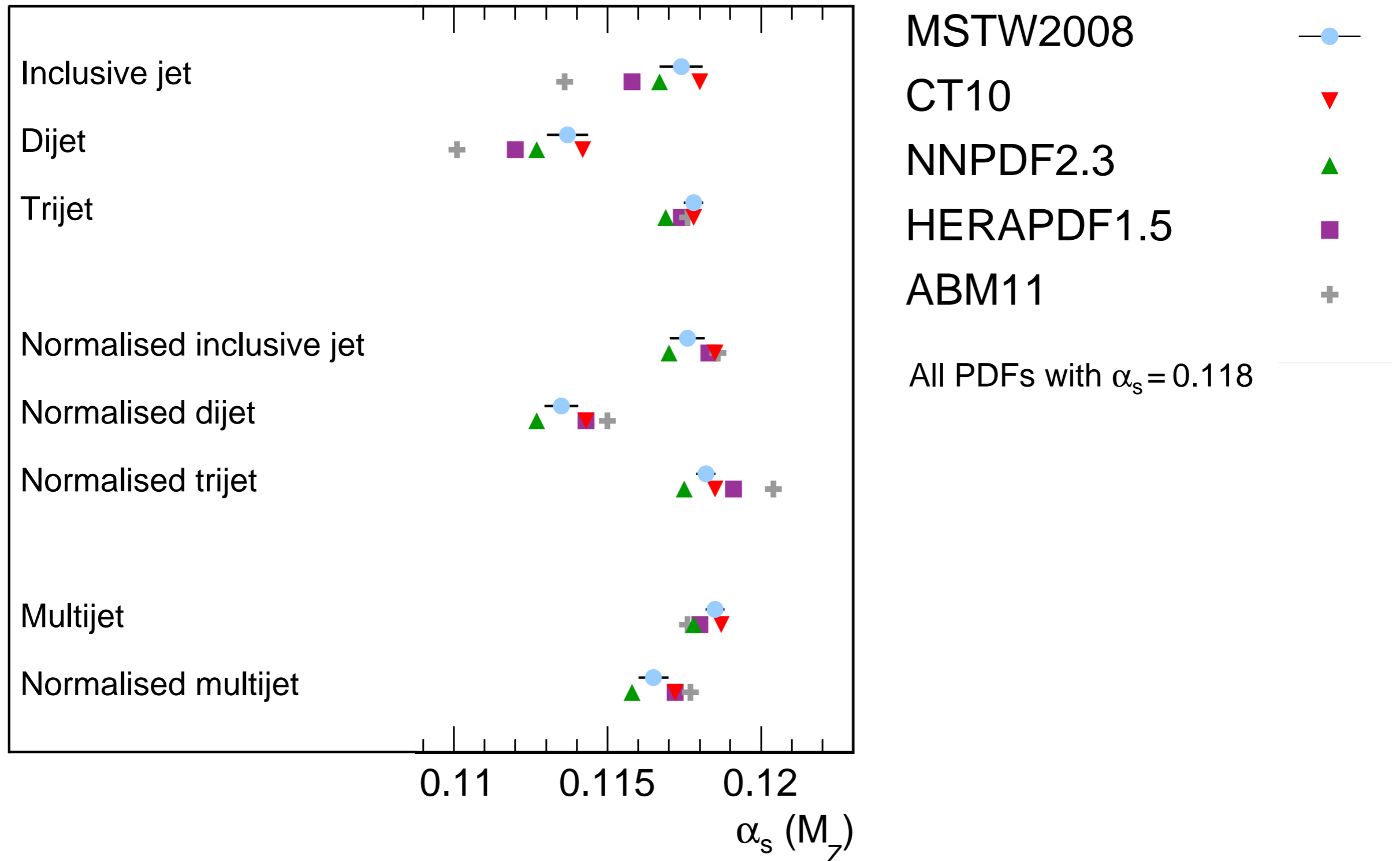


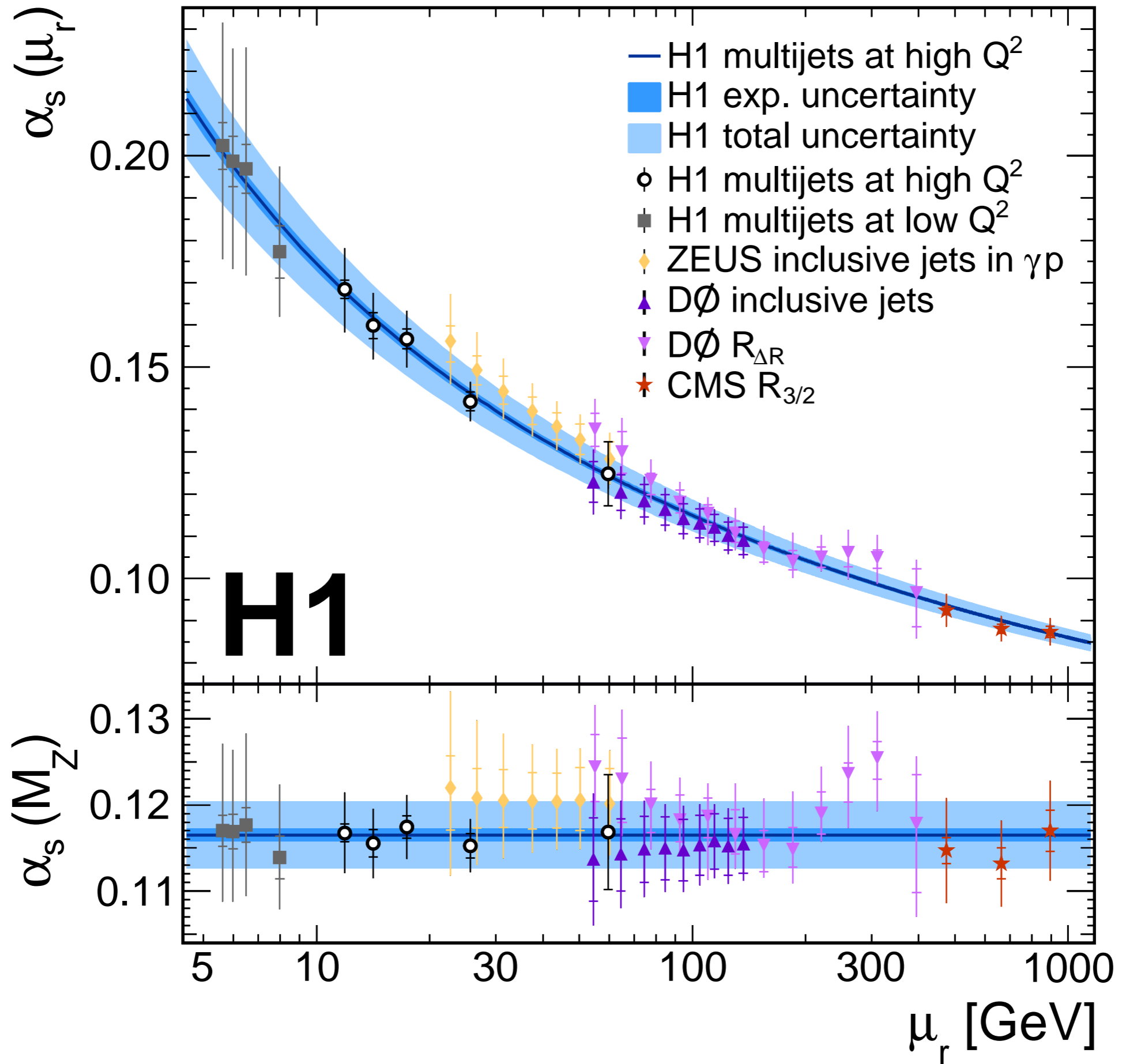
# Dependence of $\alpha_s(M_Z)$ on input $\alpha_s(M_Z)$ to PDF fit



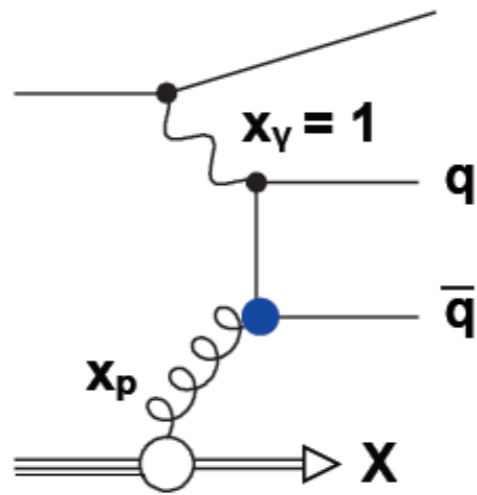
# $\alpha_s(M_Z)$ extracted using different PDF sets

## H1 Collaboration

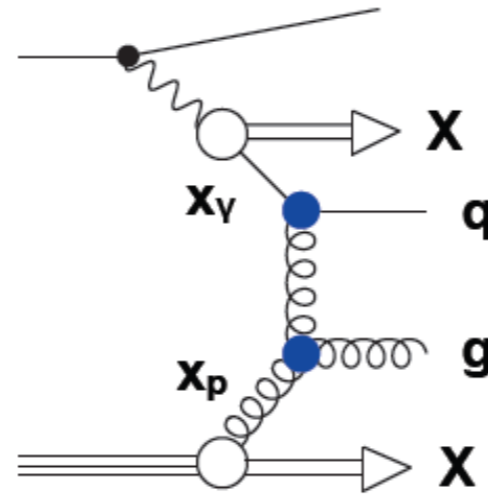




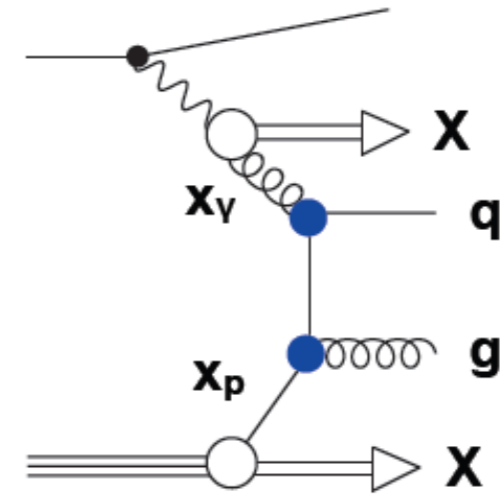
# Jet production in photoproduction $\gamma p$



direct photoproduction



resolved photoproduction



**When  $Q^2 \rightarrow 0 \text{ GeV}^2$ : Two processes contribute**

Direct photoproduction  $x_\gamma^{\text{obs}} \rightarrow 1$ : order of  $\alpha_s$

Resolved photoproduction:  $x_\gamma^{\text{obs}} < \sim 0.8$

- Leading order of  $O(\alpha_s^2)$
- Two hadrons are involved  
 -> sensitive to multi-parton interactions

Expect  $\geq 2$  jets in the final state

Partonic momentum fraction of the photon:

$$x_\gamma^{\text{meas}} = \frac{E^\gamma + E^{\text{jet}} - p_Z^\gamma - p_Z^{\text{jet}}}{E^{\text{all}} - p_Z^{\text{all}}}$$

**Analysis performed in laboratory rest frame**