

Overview on Monte Carlo event generators

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QCD@LHC

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Outline

- ▶ brief overview
 - ▶ recent results: non-perturbative regime
 - ▶ recent results: perturbative regime
 - ▶ conclusions and outlook
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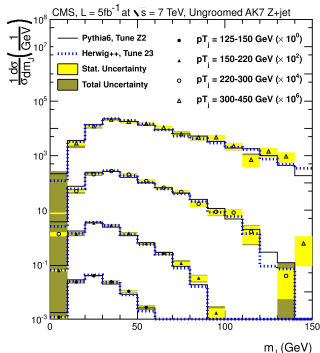
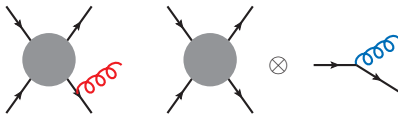
“small” deviations from SM accessible

-  any improvement is likely to play a role for LHC Physics in Run II and beyond
e.g.: think about the impact that `MC@NLO` and `POWHEG` had during LHC Run I

- ▶ aim: **fully differential** and **fully realistic** description of high energy hadron collisions
 - . fixed order & resummation: more accurate, but not fully differential
 - . MC needed to estimate detector effects
 - . MC needed to validate analysis
 - . MC needed for analysis based on NN / BDT
 - . MC very often required to compare with (extrapolate from) data with acceptance cuts
 - . (so far) heavily used to study jet-substructure techniques
 - . contamination of UE into purely perturbative jet predictions (or develop methods to reduce it!)
 -
- ▶ guiding principle: stages characterized by very different typical energy scales treated separately
 - . clearly an **approximation**, although well **motivated** (and **needed in practice**)
 - . I'll stick to the standard convention and separate “perturbative” from “non-perturbative”

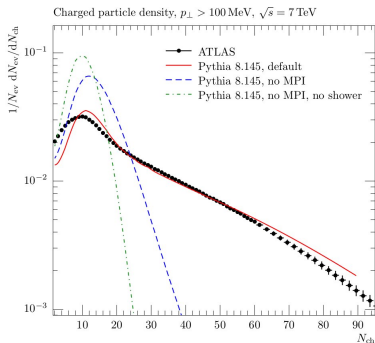
perturbative regime [“hard scattering”, “parton shower”]

- ▶ allow to start from first-principles
- ▶ **current progress**: improve accuracy (thereby reducing theoretical uncertainties)
 - include higher order effects [from NLO & from resummation]
 - include subleading effects in PS (treating more precisely effects usually described (semi)-classically)
- ▶ key is **consistency**: the “less accurate” approach (that we want to improve) already includes an approximation of the terms we include exactly.
 - ▶ example: “double counting” in NLO+PS matching



non-perturbative regime [“hadronisation”, “UE/MPI”]

- ▶ “elementary” quantities, easily accesible, impossible to describe using just “factorisation” in pQCD
- ▶ **need of models**, built upon qualitative understanding of strong dynamics
- ▶ model ↔ **parameters** ↔ **tune**
- ▶ MPI modelling important for UE in Run II (e.g. additional “mini-jet” activity)
- ▶ interplay MPI-hadronisation, color reconnections (e.g. source of uncertainty to top-mass extraction)



parton-shower (PS) programs: backbones for all approaches that go beyond fixed-order accuracy, simulating fully exclusive events (including hadronisation, MPI,...)

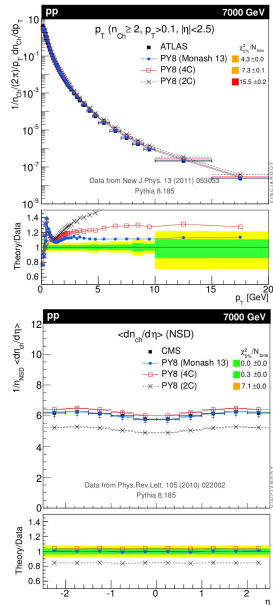
- ▶ “Workhorses” Monte Carlo programs currently used for LHC Physics:
Pythia8, Herwig++, Sherpa
 - based on factorisation of QCD amplitudes
 - accuracy: LO, LL, leading colour (planar)
 - some NLL/subleading colour effects included
 - differences in PS details (in particular ordering), although all have same nominal accuracy
 - different models for hadronisation and MPI/UE

-
- ▶ will discuss selection of improvements upon this picture:
 - ▶ only LHC pp collisions, no MC's for heavy-ions
 - ▶ left out EW effects [Yost,Ward (HERWIRI)] [Christiansen,Sjöstrand '14] [Krauss,Petrov et al '14] [Gieseke,Kasprzik,Kühn, '14]
 - ▶ left out progress for BSM simulation
(although Madgraph5 is now incorporated into MG5_aMC@NLO)
 - ▶ apologise for other omissions !

hadronisation, MPI, UE

Multiple Parton Interaction (MPI)

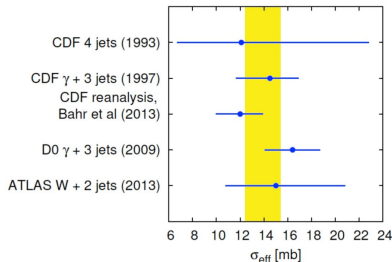
- ▶ UE: in a hard collisions, all activity not directly related to hard scattering
 - ▶ UE is **not just non-perturbative**: MPI hard perturbative tail is simulated using QCD $2 \rightarrow 2$
 - ▶ soft inclusive events (sometimes called “minimum bias”) also need MPI to be described (really NP here, model needed)
-
- ▶ Pythia: MPI model interleaved with p_T -ordered PS + min-bias via dampening
new tune: “Monash 13” [Skands,Carrazza,Rojo '14]
 - ▶ Sherpa: MPI model independent from hard process + min-bias via dampening
SHRiMPS: unique model for non-diffractive, single-diffractive and double-diffractive events
 [Hoeche;Hoeth,Khoze,Krauss, Martin,Ryskin,Zapp]
 - ▶ Herwig++: MPI model independent from hard process + min-bias via “hot-spot” model
 [Baehr,Gieseke,Roehr,Seymour,Siodmok]



- ▶ effective x-section for double parton scattering:

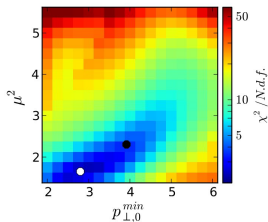
$$\sigma_{ab} = \frac{\sigma_a \sigma_b}{\sigma_{\text{eff}}}$$

- ▶ a tuned MPI model gives a prediction for σ_{eff}
 \rightarrow all MC models give 20 – 30 mb: **disagreement with measured value** 13.9 ± 1.5 mb
- ▶ possible to re-tune taking into account this constrain too?



- addressed carefully within Herwig++
 [Seymour, Siodmok '13]
- affect directly μ^2 parameter associated to “inverse proton radius”: by describing σ_{eff} , break degeneracy among MPI parameters ($\mu^2, p_{T,0}^{\text{min}}$).

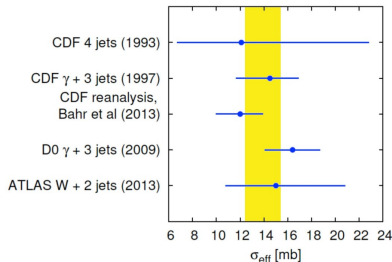
$$p_T^{\text{min}}(s) = p_{T,0}^{\text{min}} \left(\frac{\sqrt{s}}{E_0} \right)^b \quad [E_0 = 7 \text{ TeV}]$$



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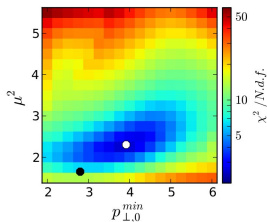
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double parton scattering: MC predictions vs. direct measure

▶ effective

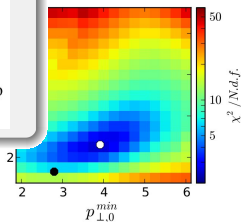
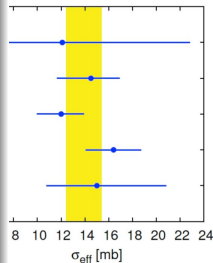
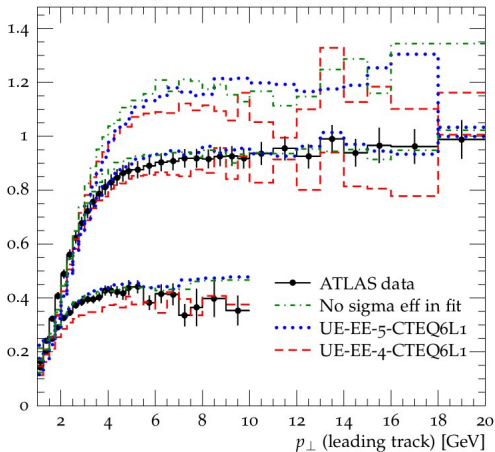
▶ a tuned MC
 ↪ all MC
 with mea

▶ possible
 constrain

- address

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Transverse N_{chg} density vs. p_{\perp}^{trk1}

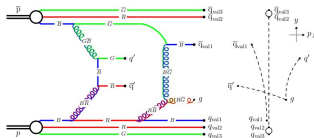


$$p_T^{\min}(s) = p_{T,0}^{\min} \left(\frac{\sqrt{s}}{E_0} \right) \quad [E_0 = 7 \text{ TeV}]$$

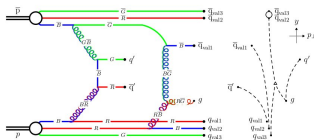
✓ kept good description of data

Color Reconnections

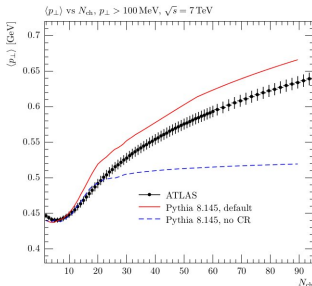
- ▶ models of hadronisation need to know color of partons: kept track of in **planar approximation**
- ▶ how is colour neutralized between different scatterings (and beam remnants)?
- ▶ even after dealing with ambiguities: color-connected systems typically lie at very different y :
 - ⇒ large invariant masses (with low p_T)
 - ⇒ **too many (soft) particle are produced !**



same color, same kinematics, different color flows !



- ▶ Need for “color reconnections” before hadronisation:
 - assume that hard jets from separate hard scatters have to be color connected if close in momentum space
 - generate **clusters with smaller invariant mass** (or **shorter Lund strings**) wrt strict color topology
- ▶ All MCs have one (or more) model for CR



Color reconnections and uncertainty on the top mass

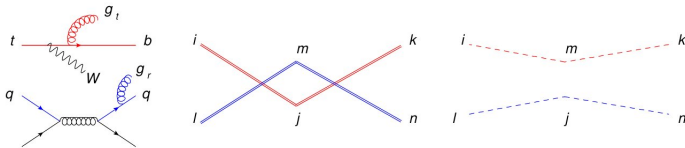
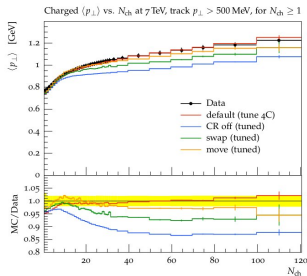
- ▶ precise **extraction of top-mass** is a hot-topic (and will possibly be more and more relevant in Run II)

$$\mathcal{O}^{\text{exp}}(\{Q^2\}) = \mathcal{O}^{\text{th}}(m_t, \{Q^2\})$$

- ▶ when “traditional methods” are used, CR is among the dominant sources of uncertainty
- ▶ “uncertainty” typically estimated varying CR models

[Argyropoulos,Sjöstrand '14]

- ▶ PYTHIA8 current CR model doesn't directly affect top decay products
- ▶ $\delta m_t \simeq m_{\text{top}}^{\text{CR}} - m_{\text{top}}^{\text{no-CR}}$ not realistic (CR needed to describe min-bias data!)
- ▶ **dedicated study**: $\delta m_t \simeq \mathcal{O}(500 - 800)$ GeV
 - possible to gain precision by looking into “low-energy” stage
 - typical distributions in $t\bar{t}$ events can also be used to narrow down consistent CR model

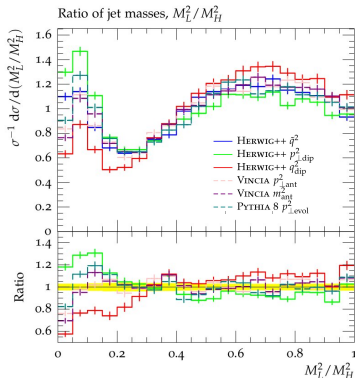


Parton showers

- ▶ PS important: to resum soft/collinear logs, but also to perturbatively fragment partons (needed for hadronisation !)
- ▶ different choices \Rightarrow subleading effects

PS	construction	recoil
PYTHIA	DGLAP	local
HERWIG++ (angular)	DGLAP	global
HERWIG++ (dipole)	CS dipoles	local
Sherpa	CS dipoles	local
ARIADNE	antenna	local
VINCIA	antenna	local
Krk	DGLAP	global
DEDUCTOR ($n \rightarrow n + 1$)	Nagy-Soper	local

- ▶ try to expose differences



- study radiation patterns in $e^+e^- \rightarrow 4$ jets
[Fischer, Gieseke, Plätzer, Skands, '14]
- several shower models, all tuned on same set of data, ME corrections switched off

- events where $y_{23} \sim y_{34}$
- ratio of jet masses (after recombining to 2-jets)
- strong ordering suppressed \leftrightarrow effective "1 \rightarrow 3" splittings exposed (when close to 0)

PS: beyond planar approximation

- ▶ PS are based on **planar approximation** (+ colour coherence), i.e. they potentially miss genuine effects formally $\mathcal{O}(10)\%$
- ▶ at first sight, this is **not that small**: to quantify, need to compare planar approximation against a more accurate (ideally complete) formulation

-
- ▶ for quantities affected mostly by hard radiation, can expect that **MC@NLO and POWHEG will capture some of these effects** (via inclusion of exact full NLO)

- ▶ going beyond requires to include amplitudes into the PS machinery
- ▶ normal dipole shower

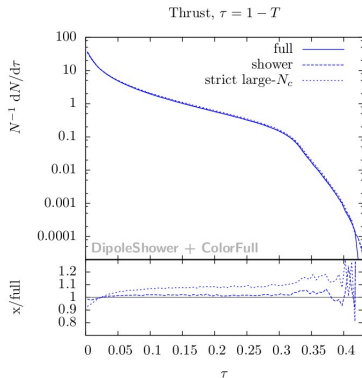
$$dP_{ij,k} \simeq \frac{\alpha_S}{2\pi} \frac{dp_T^2}{p_T^2} dz V_{ij,k}(p_T^2, z)$$

- ▶ generalize to [Platzer,Sjodahl, '12]

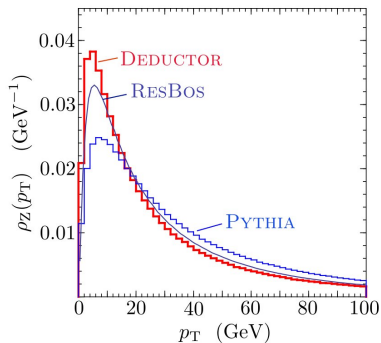
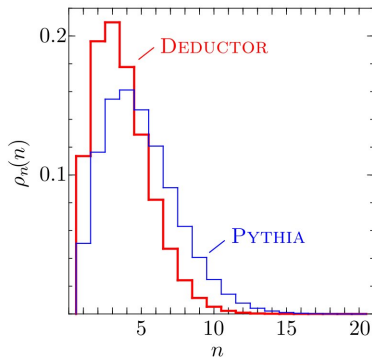
$$dP_{ij,k} \simeq \frac{\alpha_S}{2\pi} \frac{dp_T^2}{p_T^2} dz V_{ij,k}(p_T^2, z) \frac{-1}{\mathbf{T}_{ij}^2} \frac{\langle \mathcal{M}_n | \mathbf{T}_{ij} \cdot \mathbf{T}_k | \mathcal{M}_n \rangle}{|\mathcal{M}_n|^2}$$

where now, in step $n \rightarrow n + 1$, allow any parton to radiate

- ▶ iterate (so far tried up to 6 emissions)



- ▶ aim is to take into account quantum interference also in PS
- ▶ idea: use quantum density matrix in color and spin space, and evolve that
- ▶ **DEDUCTOR**: so far average over spins, but already allows off-diagonal color states
- ▶ can start shower using color-ordered amplitudes in hard scattering
- ▶ Begun extensive validation + comparisons with analytic resummation and other PS programs



Hard scattering

- NLO matching
- NLO merging

NLO matching (NLO+PS)

- ▶ MC@NLO [Frixione,Webber '02] and POWHEG [Nason'04] are by now well established: **method of choice** when available
 - ▶ if a QCD NLO computation for $pp \rightarrow X$ exists [by now it probably does], it can be (was) matched to a PS
 - **inclusive observables at NLO** [much better than LO+PS ✓]
↳ normalisation starts to stabilise, meaningful assessment of theoretical uncertainties, K-factors included
 - **(N)LL Sudakov resummation where relevant** [much better than NLO ✓]
 - large- p_T hardest associated jet at LO [better than LO+PS ✓]
 - extra jets at LL [better than NLO ✓]
 - fully exclusive events
 - ▶ X can contain jets
(but if it contains N -jets, not possible to describe observables with $n < N$ jets)
-

▶ available tools:

- ▶ **POWHEG based:** POWHEG-BOX, PowHel, Matchbox/Herwig++
- ▶ **MC@NLO based:** MG5_aMC@NLO, Sherpa-MC@NLO, Matchbox/Herwig++
- ▶ **other approaches:**
 - Vincia (also NLOPS merging, e^+e^-) [Skands,Giele,Hartgring,Kosower, et al, '08 -]
 - HEJ (so far only tree-level ME) [Andersen,Hapola,Smillie '11 -]
 - Geneva (also NLOPS merging) [Alioli,Bauer, et al '12 -]
 - KrkNLO [Jadach,Placzek,Sapeta,Siodmok,Skrzypek '14 -]

▶ POWHEG-BOX

[Alioli,Nason,Oleari,ER,Hamilton,Zanderighi + many others involved]
(<http://powhegbox.mib.infn.it/>)

- pure QCD: jj, jjj
- EW: $V(+j, +jj), VV, Wb\bar{b}, W^+W^+jj$ (QCD)
- top: $t\bar{t}(+j), t\bar{j}$ ("single top", also in 4f scheme), tW
- VBF: $Vjj, VVjj$
- Higgs: $H(+j, +jj), HV, HVj, Hj j$ (VBF), $Hj j j$ (VBF)
- BSM: $tH^+, \tilde{\ell}\bar{\ell}, \tilde{q}\bar{q}, H/A$ in MSSM, DM+monojets
- QED/EW & QCD: Drell-Yan

▶ PowHel

[Garzelli,Kardos,Papadopoulos,Trócsányi]
(<http://grid.kfki.hu/twiki/bin/view/DbTheory/WebHome>)

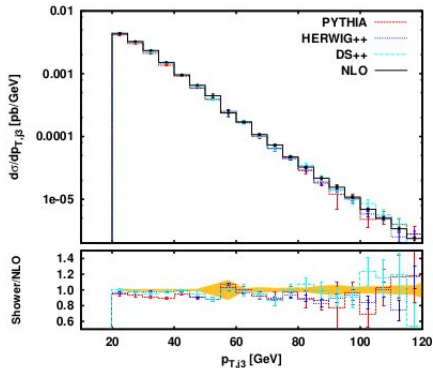
- top pairs: $t\bar{t}, t\bar{t}j, t\bar{t}H, t\bar{t}V, t\bar{t}b\bar{b}, W^+W^-b\bar{b}$

▶ POWHEG-BOX (V2):

- th. uncertainty: fast PDF and scale reweighting
- can use MadGraph4 for all tree-level terms
- can be interfaced to 1-loop codes (HELAC, MCFM, GoSam, NLOJET++), supports BLHA
- ▶ possible to generate at NLO+PS also correction to decay of heavy resonances
 - validation and phenomenology for $t\bar{t}$ in progress [Campbell,Ellis, Nason,ER, in progress]

$$pp \rightarrow Hjjj \text{ (VBF)}$$

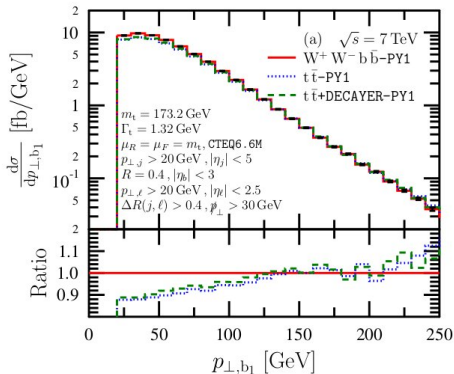
[Jäger,Schissler,Zeppenfeld '14]



- ▶ amplitudes from VBFNLO
- ▶ estimate uncertainties due to “Central Jet Veto” techniques

$$pp \rightarrow W^+W^-b\bar{b} \text{ (5f-scheme)}$$

[Garzelli,Kardos,Trócsányi '14]



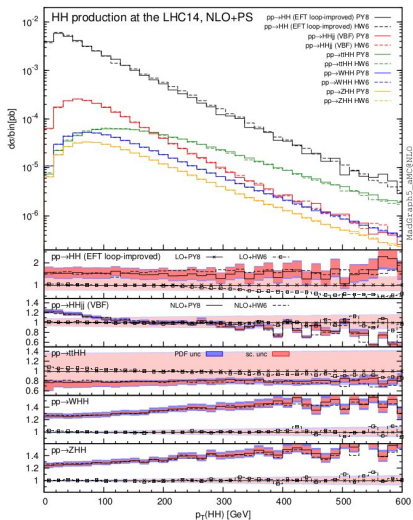
- ▶ fully differential $t\bar{t}$ as signal and background
- ▶ exact handling of offshellness effects by PS need be addressed in this context

- ▶ `MadGraph5_aMC@NLO` [Alwall, Frederix, Frixione, Hirschi, Maltoni, Mattelaer, Shao, Stelzer, Torrielli, Zaro] (<http://amcatnlo.web.cern.ch/amcatnlo/>)
- ▶ **milestone in 2014 for the QCD/MC community:**
 - ▶ essentially all $2 \rightarrow 4$ processes you can think about (and also e^+e^-)
 - ▶ several of these processes were never computed before

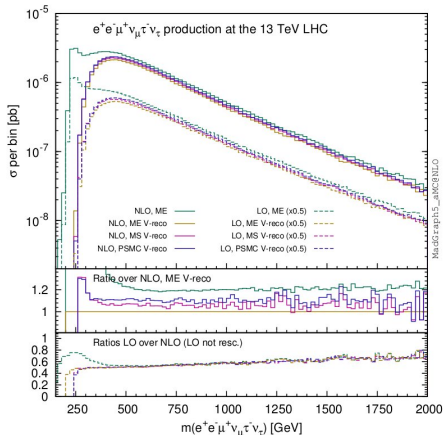
-
- ▶ embedded in `Madgraph5`
 - ▶ fully automated (thanks to `MadFKS` and `MadLoop`)
 - ▶ th. uncertainty: fast PDF and scale reweighting
 - ▶ will soon allow also EW corrections and BSM models, thanks to interface to `FeynRules` [Alloul, Christensen, Degrande, Duhr, Fuks]

$$pp \rightarrow HHX$$

[Frederix, Frixione, Hirschi, Maltoni, Mattelaer, Torrielli, Vryonidou, Zaro]



$$pp \rightarrow e^+ e^- \mu^+ \nu_\mu \tau^+ \nu_\tau$$



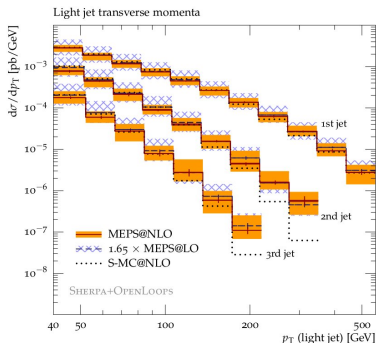
► Sherpa-MC@NLO

[Hoeche,Krauss,Schoenherr,Siegert]
(<http://sherpa.hepforge.org>)

- interfaced to 1 loop codes, typically with BLHA (BlackHat, OpenLoops, GoSam, MCFM)
- traditionally focussed on $S + \text{jets}$ ($S = V, VV, H$)
- enormous progress over last 2 years; in particular:
 - NLO+PS multijet merging (MEPS@NLO)
 - thorough assessment of uncertainties

- $pp \rightarrow W + \text{jets}$ [NLO merging]
- $e^+e^- \rightarrow \text{jets}$ [NLO merging]
- $pp \rightarrow H + \text{jets}$ [NLO merging]
- $pp \rightarrow t\bar{t} + \text{jets}$ [NLO merging]
- $pp \rightarrow 4\ell + \text{jets}$ [NLO merging]
- $pp \rightarrow VH/VV/VVV + \text{jets}$ [NLO merging]
- $pp \rightarrow t\bar{t}b\bar{b}$ (4f) [NLO+PS]

[Cascioli,Gehrmann,Hoeche,Huang,Krauss,Luisoni,Maierhöfer,
Pozzorini,Schoenherr,Siegert,Thompson,Winter,Zapp '13-'14]



- ▶ some processes available internally, in POWHEG approach

[Richardson,Hamilton,d'Errico,Fridman-Rojas,Tully,Wilcock]

- ▶ **Matchbox**: new standard for NLO+PS within Herwig++ (<https://herwig.hepforge.org/>)

[Gieseke,Plätzer;Bellm,Fischer,Rauch,Reuschle,Wilcock,Richardson]

- ▶ general and modular framework to do NLO+PS matching within Herwig++:

- with POWHEG **and** MC@NLO schemes
- using angular-ordered **or** dipole shower
- focus also on assessment of uncertainties
- scheme for NLOPS merging [Plätzer '12]

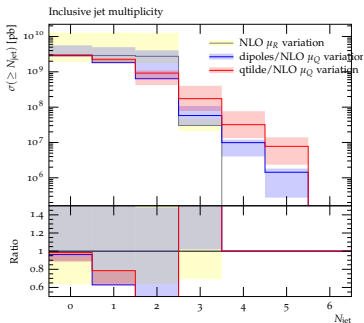
- ▶ recently used to perform state-of-the art NLO computation: $Hjjj$ (VBF)

[Campanario,Figy,Plätzer,Sjödahl '13]

- ▶ currently **being interfaced to NLO codes**, also via BLHA

(GoSam, Njet, VBFNLO, OpenLoops)

- ▶ rapid progress, stay tuned !



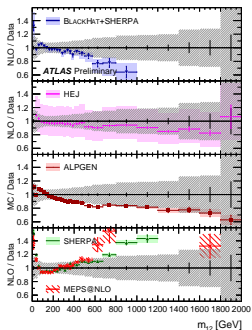
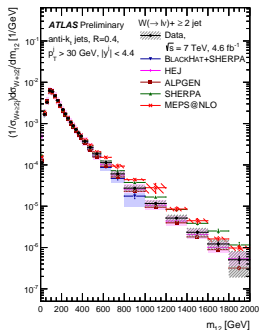
NLO+PS dijets [preliminary]

► High Energy Jets:

(<http://cern.ch/hej/>)

[Andersen,Hapola,Smillie]

- leading real and virtual corrections to hard scattering ME from wide-angle QCD (BFKL-inspired)
- merged with multileg tree-level ME's (but differently to shower merging); was matched also to PS (Ariadne)
- works well also when jets of similar transverse momentum (not based on collinear limit \Rightarrow no strong p_T -ordering required)
- should be the more reliable approach for "(X) + multijets" at large invariant mass or large rapidity intervals: **very relevant for $H + jj$**

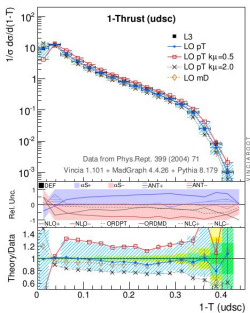


► Vincia:

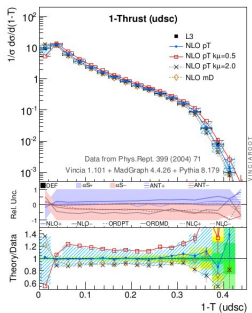
(<http://vincia.hepforge.org/>)

[Skands,Giele,Hartgring,Kosower,Laenen,Larkoski,Lopez-Villarejo,Ritzmann]

- based upon antenna factorisation, substitute PYTHIA8 shower
- facility to evaluate uncertainties very comprehensively, and very efficiently
- systematically improve PS, order by order: during Sudakov veto algorithm, include also ratio of exact matrix elements (and compensate for mismatches)
- formalism for NLO+PS matching and merging worked out, and tested in e^+e^-



(a) $NLO_{2,3} + LO_{2,3,4,5} + \text{shower}$

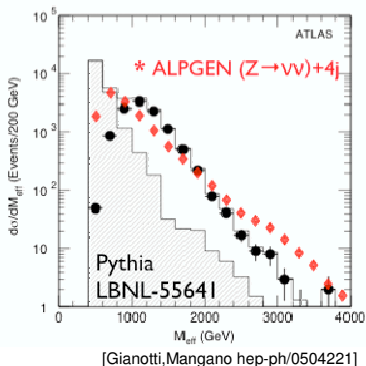


(b) $NLO_{2,3} + LO_{2,3,4,5} + \text{shower}$

Hard scattering

- NLO matching
- NLO merging

- ▶ typical background for many BSM signatures is “heavy object” + many jets



- ▶ relying on PS for tail of distributions is very dangerous, especially in a multijet environment
- ▶ CKKW(-L) and MLM methods address this issue at LO:
 - merge **exact LO** matrix elements for different multiplicities
 - very important for observables like H_T especially when not possible to use data-driven methods

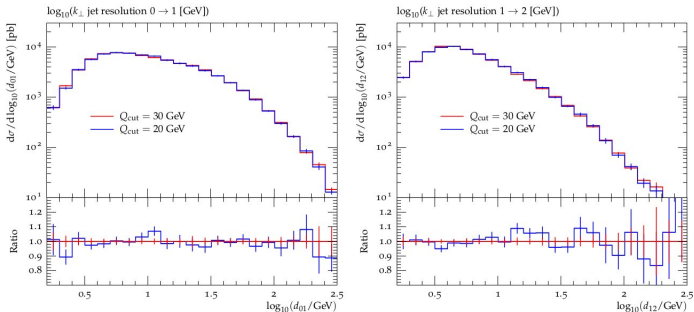
- ▶ suppose LHC finds a small excess in H_T for some SUSY search (e.g. \cancel{E}_T + jets)
 - what is the theoretical uncertainty of backgrounds?

- ▶ challenge: extend these methods to NLO (“NLOPS multijet merging”):
 - from one single event sample, have 1-, 2-,...,n-jet observables at NLO
- ▶ at NLO it is more complicated, and more subtle:
 - the matrix element $pp \rightarrow S + n$ partons enters in
 - a) Born for “ $pp \rightarrow S + n$ partons” @ NLO
 - b) real contribution for “ $pp \rightarrow S + (n - 1)$ partons” @ NLO
- ▶ as is at LO, many of these methods use a merging scale (Q_{MS})
 - a bad choice of merging scale can spoil formal accuracy one might want to claim
 - typically this can happen if $\alpha_S \log^2 Q_{\text{MS}} \simeq 1$ ($\rightarrow L \simeq 1/\sqrt{\alpha_S}$)
 - in general, to avoid this problem, one needs not to have Q_{MS} at all, or have a very precise control on formal accuracy of underlying resummation (typically beyond PS), so that even if $\alpha_S \log^2 Q_{\text{MS}} \simeq 1$, the formal accuracy is not spoiled
 - to which extent this is a serious problem is [still an open issue](#)

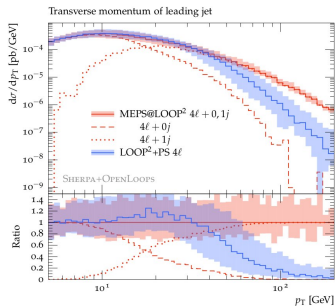
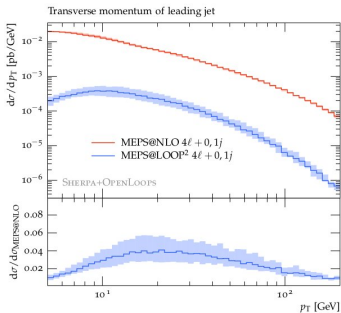
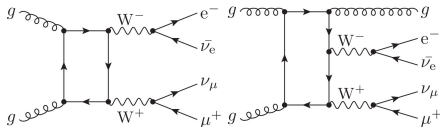
- ▶ proof of concept in e^+e^- and W + jets, applied in several other processes
- ▶ share some similarities with “FxFx”

$$\begin{aligned}
 d\sigma &= d\Phi_0 \bar{B}_0^{(A)} \otimes \tilde{\text{PS}}_{t_{\min}} \Theta(d_1 < Q_{\text{MS}}) \\
 &+ d\Phi_1 H_0^{(A)} \Delta_{t_1} \Theta(d_1 < Q_{\text{MS}}) \\
 &+ d\Phi_1 \bar{B}_1^{(A)} \otimes \tilde{\text{PS}}_{t_{\min}}^{t_1} \cdot [\text{corr. factor}] \cdot \Theta(d_1 > Q_{\text{MS}}) \\
 &+ d\Phi_2 H_1^{(A)} \Delta_{t_1}^{t_2} \Delta_{t_{\min}}^{t_1} \Theta(d_1 > Q_{\text{MS}})
 \end{aligned}$$

- ▶ possible to iterate to higher multiplicities
- ▶ residual dependence of total cross section on merging scale $\sim \alpha_S^2 L^3 / N_C^2$



- ▶ $gg \rightarrow VV$: finite subset of NNLO contribution
- ▶ **numerically important**, because of gluon flux
- ▶ **first merging** of 0-jet and 1-jet squared-loop contributions
- ▶ can use tree-level merging technique, since MEs are finite



$$d\bar{\sigma}_{\text{S},0} = T_0 + V_0 - T_0\mathcal{K} + T_0\mathcal{K}_{\text{MC}}\Theta(d_1 < Q_{\text{MS}})$$

$$d\bar{\sigma}_{\text{H},0} = [T_1 - T_0\mathcal{K}_{\text{MC}}]\Theta(d_1 < Q_{\text{MS}})$$

$$d\bar{\sigma}_{\text{S},1} = [T_1 + V_1 - T_1\mathcal{K} + T_1\mathcal{K}_{\text{MC}}]\Theta(Q_{\text{MS}} < d_1)$$

$$d\bar{\sigma}_{\text{H},1} = [T_2 - T_1\mathcal{K}_{\text{MC}}]\Theta(Q_{\text{MS}} < d_1)$$

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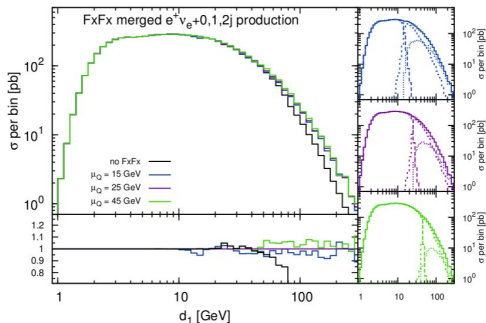
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$$d\bar{\sigma}_{\mathbb{H},1} = [T_2 - T_1\mathcal{K}_{\text{MC}}]\Theta(Q_{\text{MS}} < d_1)$$

- ▶ limit contribution of $(\mathbb{H}, 0)$ events to region below Q_{MS}
- ▶ prescriptions for shower starting scale
- ▶ possible to include Sudakov reweighting á la CKKW
- ▶ “unitarity” not imposed
- ▶ possible to iterate

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- ▶ fully inclusive result:
 - differences typically $\lesssim 1\%$ among different merging scales
 - quite good agreement with inclusive NLO+PS too

- ▶ keyword: “**unitarity**” (preserve NLO inclusive cross section)
- ▶ method: promote to NLO accuracy an “unitarised” CKKW approach, by carefully adding higher order contributions, and removing the pre-existing approximate α_S terms:

1. start from UMEPS merging at LO

$$\langle \mathcal{O} \rangle = \int d\phi_0 \left\{ \mathcal{O}(S_{+0j}) \left(\int_{B_{0+}} - \int_{\hat{B}_{1 \rightarrow 0}} - \int_{\hat{B}_{2 \rightarrow 0}} \right) + \int \mathcal{O}(S_{+1j}) \left(\int_{\hat{B}_1} - \int_{\hat{B}_{2 \rightarrow 1}} \right) + \iint \mathcal{O}(S_{+2j}) \hat{B}_2 \right\}$$

2. remove terms that will be included exactly, and add NLO (exclusive) computations
3. unitarise

$$\langle \mathcal{O} \rangle = \int d\phi_0 \left\{ \mathcal{O}(S_{+0j}) \left(\tilde{B}_0 - \int_s \tilde{B}_{1 \rightarrow 0} + \int_s B_{1 \rightarrow 0} - \left[\int \hat{B}_{1 \rightarrow 0} \right]_{-1,2} - \int_s B_{2 \rightarrow 0}^\uparrow - \int \hat{B}_{2 \rightarrow 0} \right) + \int \mathcal{O}(S_{+1j}) \left(\tilde{B}_1 + \left[\hat{B}_1 \right]_{-1,2} - \left[\int \hat{B}_{2 \rightarrow 1} \right]_{-2} \right) + \iint \mathcal{O}(S_{+2j}) \hat{B}_2 \right\}$$

- ▶ can be iterated to higher multiplicities
- ▶ **essentially no dependence on merging scale**

“Multiscale Improved NLO”

[Hamilton,Nason,Oleari,Zanderighi '12]

- ▶ original goal: method to **a-priori** choose scales in multijet NLO computation
(in a multiscale process, this is not straightforward, in regions with widely-separated scales)
- ▶ idea: correct weights of different NLO terms with CKKW-inspired approach
(**without spoiling formal NLO accuracy**)

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$$\bar{B}_{\text{MiNLO}} = \alpha_S^2(m_h) \alpha_S(q_T) \Delta_g^2(q_T, m_h) \left[B \left(1 - 2\Delta_g^{(1)}(q_T, m_h) \right) + \alpha_S^{(\text{NLO})} V(\bar{\mu}_R) + \alpha_S^{(\text{NLO})} \int d\Phi_{\text{rad}} R \right]$$

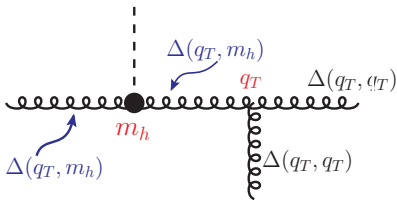
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$$\bar{B}_{\text{MinLO}} = \alpha_S^2(m_h) \alpha_S(q_T) \Delta_g^2(q_T, m_h) \left[B \left(1 - 2\Delta_g^{(1)}(q_T, m_h) \right) + \alpha_S^{(\text{NLO})} V(\bar{\mu}_R) + \alpha_S^{(\text{NLO})} \int d\Phi_{\text{rad}} R \right]$$



☞ Sudakov FF included on $H+j$ Born kinematics

☞ finite results if 1st jet **unresolved**

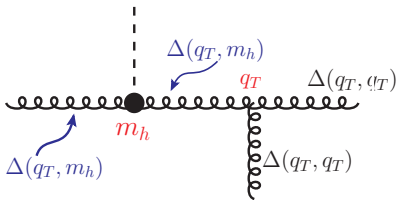
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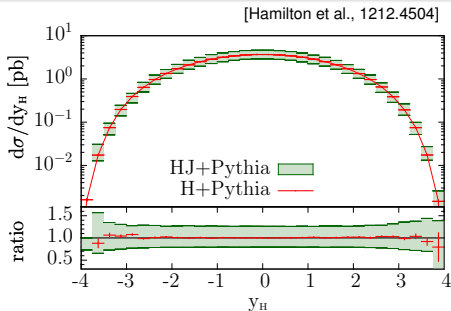
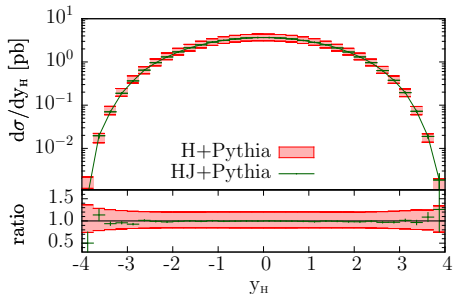
$$\bar{B}_{\text{MiNLO}} = \alpha_S^2(m_h) \alpha_S(q_T) \Delta_g^2(q_T, m_h) \left[B \left(1 - 2\Delta_g^{(1)}(q_T, m_h) \right) + \alpha_S^{(\text{NLO})} V(\bar{\mu}_R) + \alpha_S^{(\text{NLO})} \int d\Phi_{\text{rad}} R \right]$$



☞ Sudakov FF included on $H+j$ Born kinematics

☞ finite results if 1st jet **unresolved**

- \bar{B}_{MiNLO} ideal to extend validity of $H+j$ POWHEG
- including terms from NNLL resummation, **NLO+PS merging** for 0 and 1-jet, **without a merging scale**. However: **for now not clear how to extend to higher multiplicity**

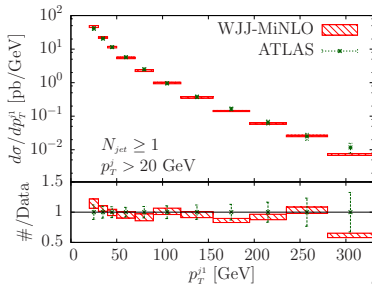


- NLO merging available also for Drel-Yan, and VH

[Luisoni, Nason, Oleari, Tramontano, 1212.4504]

VJJ-MiNLO [Campbell, Ellis, Nason, Zanderighi, 1303.5447]

- start from $W + 2$ jets @ NLO
- good agreement with data also when requiring $N_{jet} \geq 1$!
- not possible in a standard NLO
- so far, **no claim** on formal accuracy here



- ▶ new approach, SCET inspired [Alioli, Bauer, Berggren, Hornig, Tackmann, Vermilion, Walsh, Zuberi '12]
- ▶ idea: separate exclusive N -jet and inclusive $(N + 1)$ -jet regions using variable whose resummation is known at high order (“n-jettiness”)

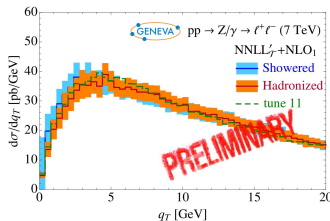
$$\sigma_{\geq N} = \int d\Phi_N \frac{d\sigma}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) + \int d\Phi_{N+1} \frac{d\sigma}{d\Phi_{N+1}}(\mathcal{T}_N) \theta(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}})$$

where

$$\frac{d\sigma}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) = \frac{d\sigma^{\text{resum}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) + \left[\frac{d\sigma^{\text{FO}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) - \frac{d\sigma^{\text{resum}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) \Big|_{\text{FO}} \right],$$

$$\frac{d\sigma}{d\Phi_{N+1}}(\mathcal{T}_N) = \frac{d\sigma^{\text{FO}}}{d\Phi_{N+1}}(\mathcal{T}_N) \left[\frac{d\sigma^{\text{resum}}}{d\Phi_N d\mathcal{T}_N} / \frac{d\sigma^{\text{resum}}}{d\Phi_N d\mathcal{T}_N} \Big|_{\text{FO}} \right],$$

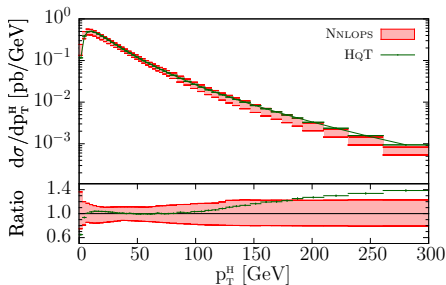
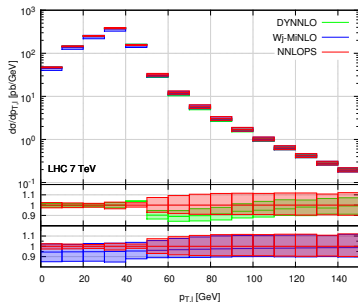
- ▶ no “dangerous” merging scale dependence, thanks to higher-order resummation for \mathcal{T}_N
 - ▶ to retain formal accuracy, PS evolution **very constrained**: τ_N has to stay \sim unchanged
-
- ▶ can be extended to higher multiplicities
 - ▶ implemented for e^+e^- , for LHC will be finished soon
 - talks by Alioli and Bauer at “PSR2014” [[link](#)]



NNLO+PS

Some of the methods described above allow to match NNLO with PS

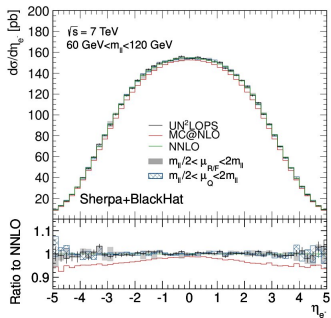
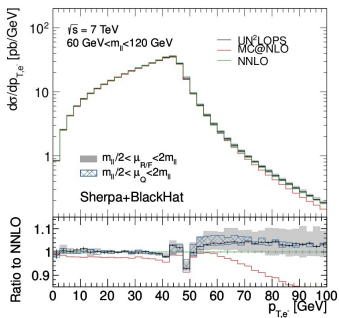
- ▶ **Higgs** [Hamilton,Nason,ER,Zanderighi '13] and **Drell-Yan** [Karlberg,ER,Zanderighi '14], using **MINLO-improved POWHEG**



- ▶ charged DY (left): find exactly what we expect: $p_{T,\ell}$ has NNLO uncertainty if $p_T < M_W/2$, NLO if $p_T > M_W/2$
- ▶ Higgs p_T (right): good agreement with NNLL+NNLO analytic resummation [HqT, Bozzi et al.]

- Drell-Yan and Higgs, using UNNLOPS

[Hoeche, Li, Prestel '14]



- general framework and preliminary results for Drell-Yan also with Geneva

[Alioli, Bauer, et al, '13]

- ▶ Monte Carlo tools play a major role for LHC searches
 - ▶ especially if no “smoking gun” new-Physics around the corner, **precision** will be the key to maximise impact of LHC results
 - ▶ summarised the huge amount of improvements over the last few years in the community
-
- ▶ continuous activity on **improving “non-perturbative” stages**. Could be relevant also for precision studies ?
 - ▶ **PS improvements**: so far small effects, but clear picture not yet fully clear.
 - Effects observables with lots of data ?
 - If so, in the worst case scenario: we will have understood QCD better
 - ▶ **NLO+PS** tools are by now well established and very mature
 - important work still ongoing to tackle subtleties
 - ▶ major developments in last 2 years: **NLOPS multijet merging**
 - accurate comparisons will take place, as it was for NLO+PS programs
 - ▶ **NNLO+PS** is doable (for simple processes) !