

# *Lessons from Flavor Physics*

Gino Isidori

[ *University of Zürich* ]

- ▶ Introduction
- ▶ SUSY & Flavor [*The Usual Suspects*]
- ▶ The  $B \rightarrow K^{(*)}ll$  anomalies [*Charming Penguins strike back*]
- ▶ Flavor physics with the BEH boson [*Contact*]
- ▶ On the observed pattern of quark & lepton masses [*The Matrix*]
- ▶ Conclusions

## ► Introduction

Despite its remarkable phenomenological success, the SM suffers of a series of **theoretical** & **cosmological** problems:

- Fine-tuning/UV sensitivity of the Higgs-mass term [*“hierarchy problem”*]
- Unexplained hierarchical structure of the Yukawa couplings [*“flavor puzzle”*]
- No explanation for the quantization of the U(1) charges [*hint of unification?*]
- No natural inclusion of neutrino masses [*hint of new heavy mass scale?*]
- Non coherent inclusion of **gravity** at the quantum level
- ...
- No good candidates to explain **dark matter**, **inflaton**, and **dark-energy**



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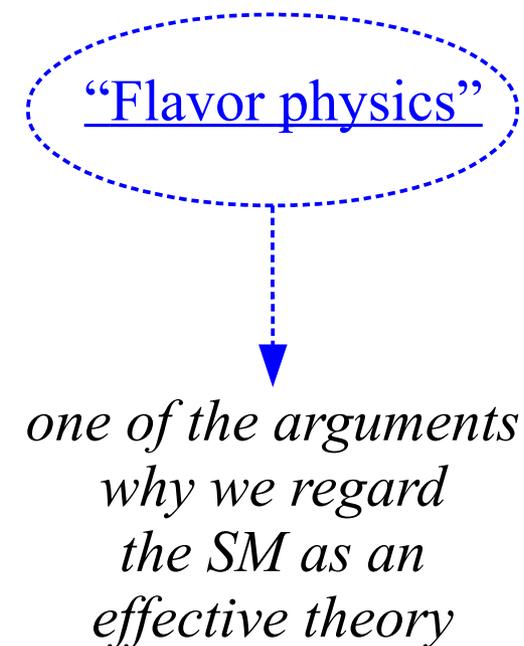
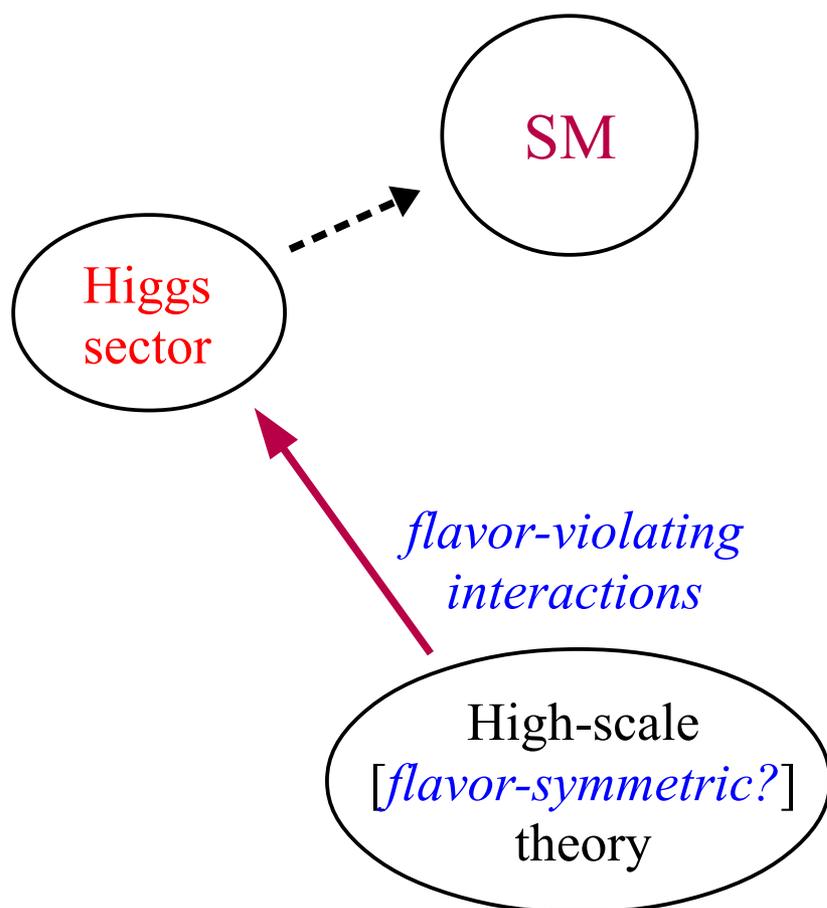
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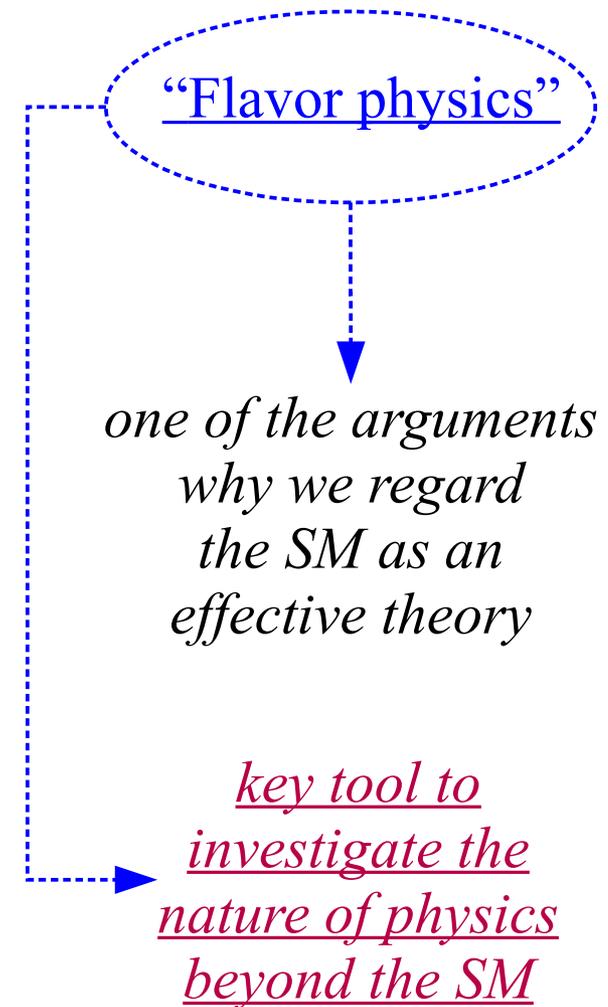
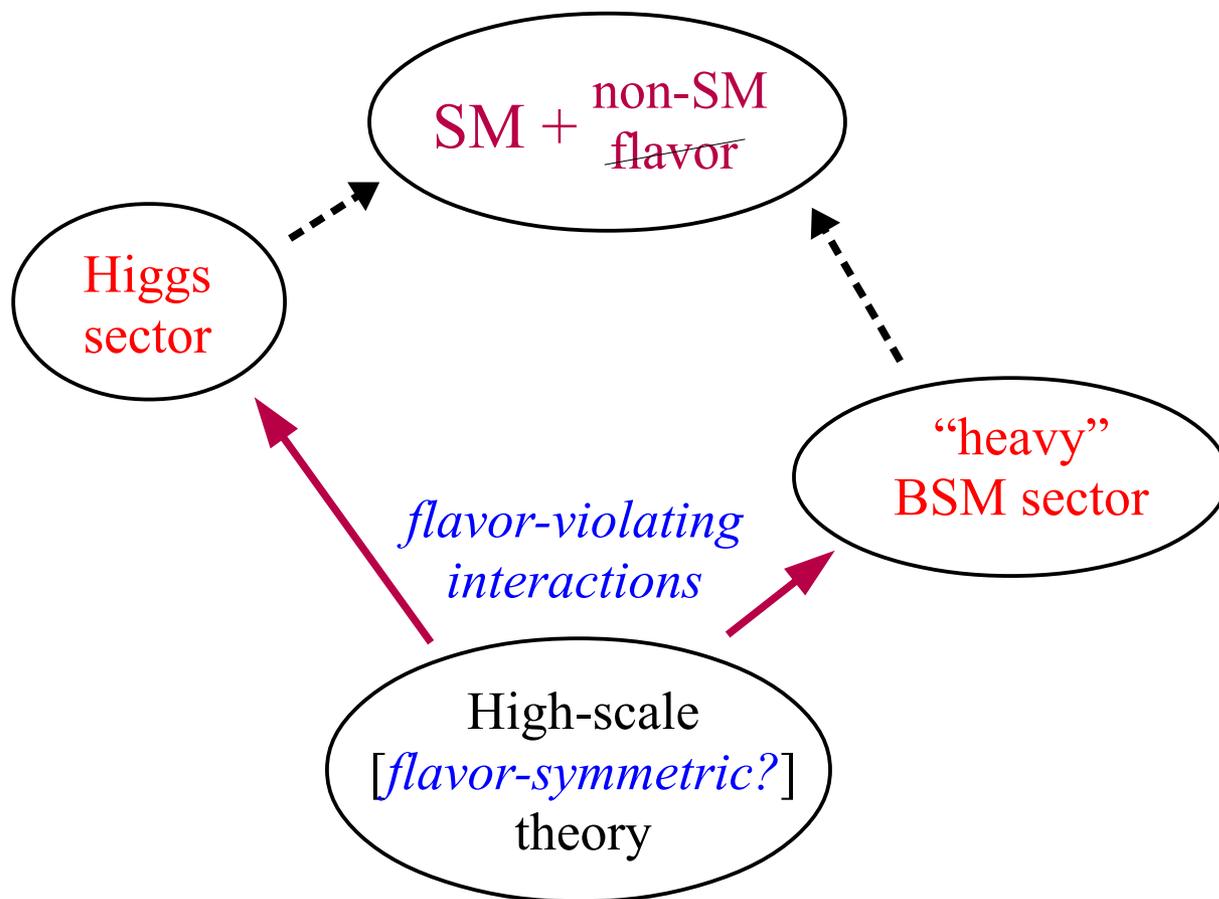
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$$V_{\text{eff}} = -\mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2 + Y^{ij} \psi_L^i \psi_R^j \phi + \frac{g^{ij}}{\Lambda} L_L^i L_L^{Tj} \phi \phi^T + \dots$$

The discovery of the Higgs boson completes the picture of the “*light degree of freedom*” in this effective theory

flavor-structure of the model

*effective neutrino mass term*

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Precision Higgs physics & flavor physics are two complementary tools to investigate (indirectly) the nature of physics beyond the SM

*No Higgs...*



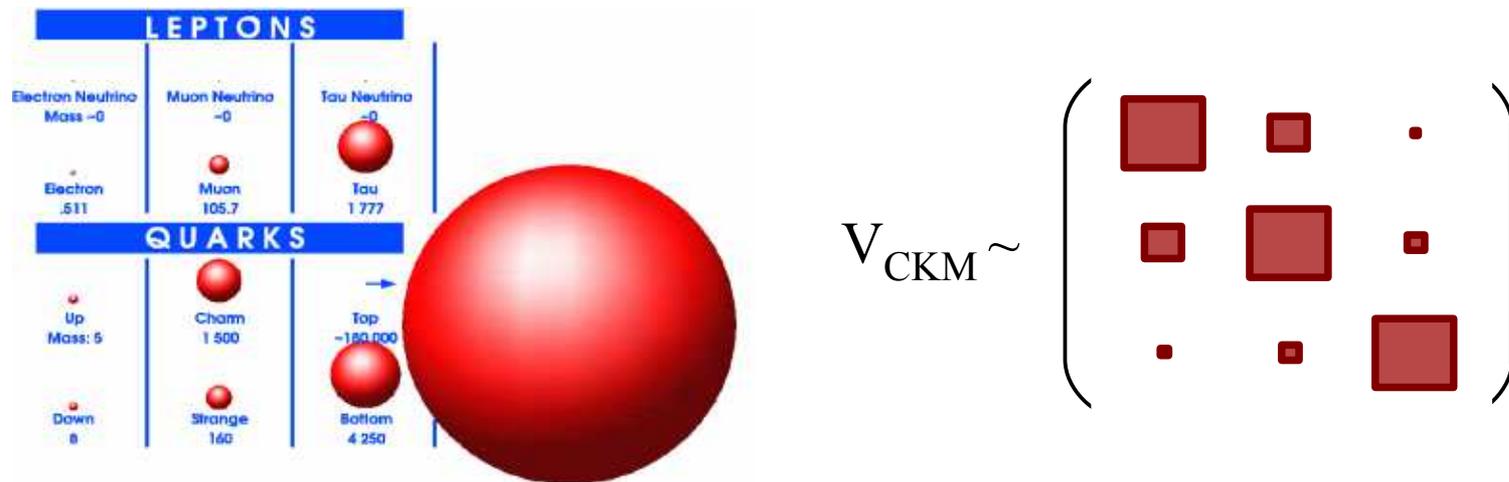
*No flavor...*

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Several plausible options on the market, with no outstanding case.

Easy to reproduce the observed mass matrices in terms of a reduced number of free parameters, while it is difficult to avoid problems with FCNCs

Hard to make progress without knowing the ultraviolet completion of the SM.

The two key open questions in flavor physics:

- *What determines the observed pattern of masses and mixing angles of quarks and leptons?*
- *Which are the sources of flavor symmetry breaking accessible at low energies?*  
[Is there anything else beside SM Yukawa couplings & neutrino mass matrix?]

Answering the second question is more “easy”:

- It can be formulated independently of the UV completion of the theory.
- It is mainly a question of precision (both on the theory and on the experimental side).



*We learned a lot about the possible sources of flavor symmetry breaking from a series of high-precision measurements of flavor-changing processes performed in the recent past*

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[Is there anything else beside SM Yukawa couplings & neutrino mass matrix?]

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{gauge}}(A_a, \psi_i) + \mathcal{L}_{\text{Higgs}}(\phi, A_a, \psi_i) + \sum_{d \geq 5} \frac{c_n}{\Lambda^{d-4}} \mathcal{O}_n^{(d)}(\phi, A_a, \psi_i)$$

$U(3)^5$  global flavor symmetry:

3 identical replica of the  
basic fermion family  
[ $\psi = Q_L, u_R, d_R, L_L, e_R$ ]

Flavor-degeneracy  
broken by the  
Yukawa interaction

$$Y^{ij} \psi_L^i \psi_R^j \phi$$

Neutrino mass term + ...

$$\frac{g^{ij}}{\Lambda} L_L^i L_L^{Tj} \phi \phi^T$$

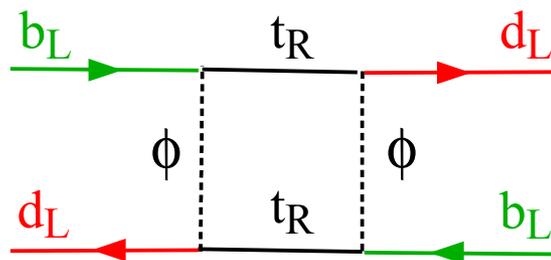
*Which are the sources of flavor symmetry breaking accessible at low energies?*

In the quark sector all measurements show a remarkable overall success of the CKM picture

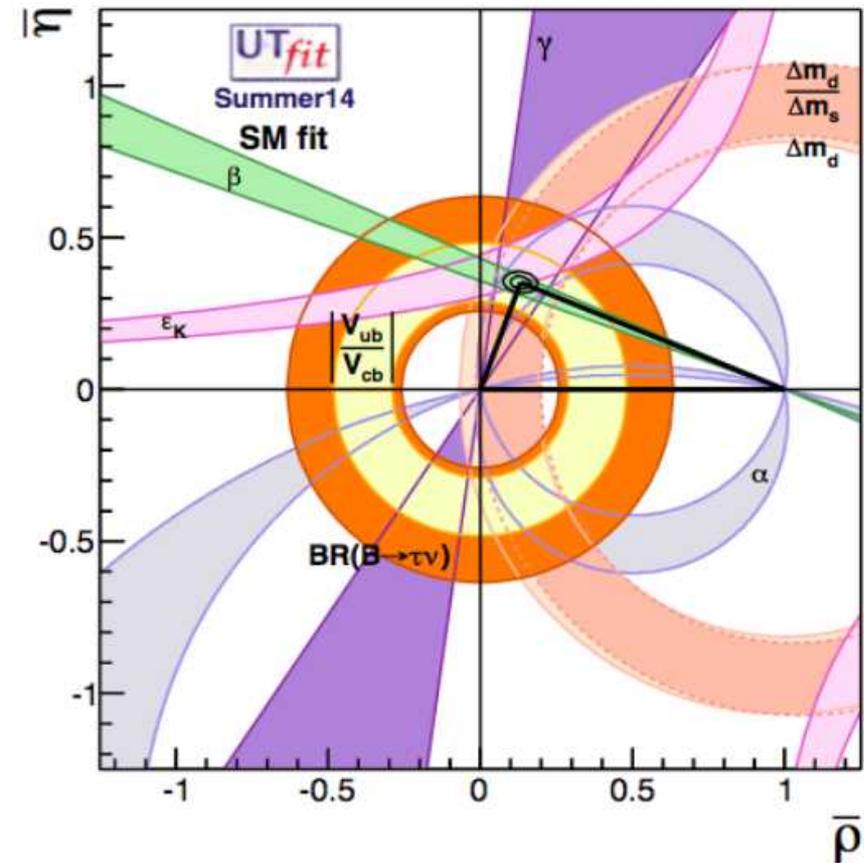
This success is quite “embarrassing” if we assume there is some New Physics around the TeV scale...

$$M(B_d - \bar{B}_d) \sim \frac{y_t^4 (V_{tb}^* V_{td})^2}{16\pi^2 m_t^2} + \frac{c_{NP}}{\Lambda_{NP}^2}$$

tiny SM contribution  
([Yukawa interaction](#))



possible large NP contribution  
(if  $\Lambda_{NP} \sim \text{TeV}$  and  $c_{NP} \sim 1$ ), excluded by present data



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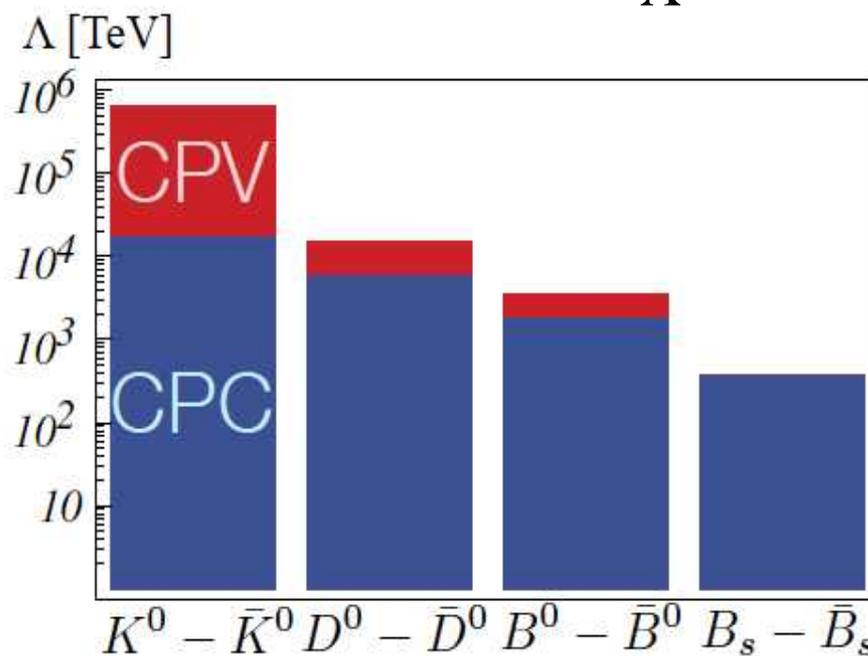
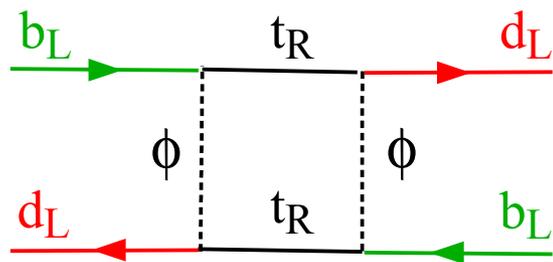
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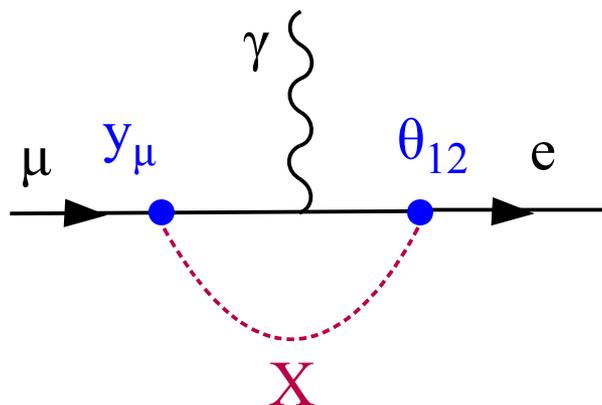
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Similar (even more stringent) bounds on the scale of NP come also from the lepton sector.

*But such bounds should not be over-emphasized...*

E.g.:



$$\text{BR}(\mu \rightarrow e\gamma)^{\text{exp}} < 5.7 \times 10^{-13}$$

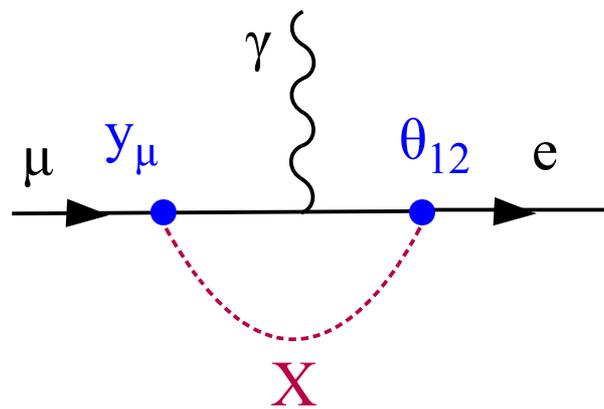
MEG '13

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MEG '13

$$M_X \gtrsim 200 \text{ TeV}$$

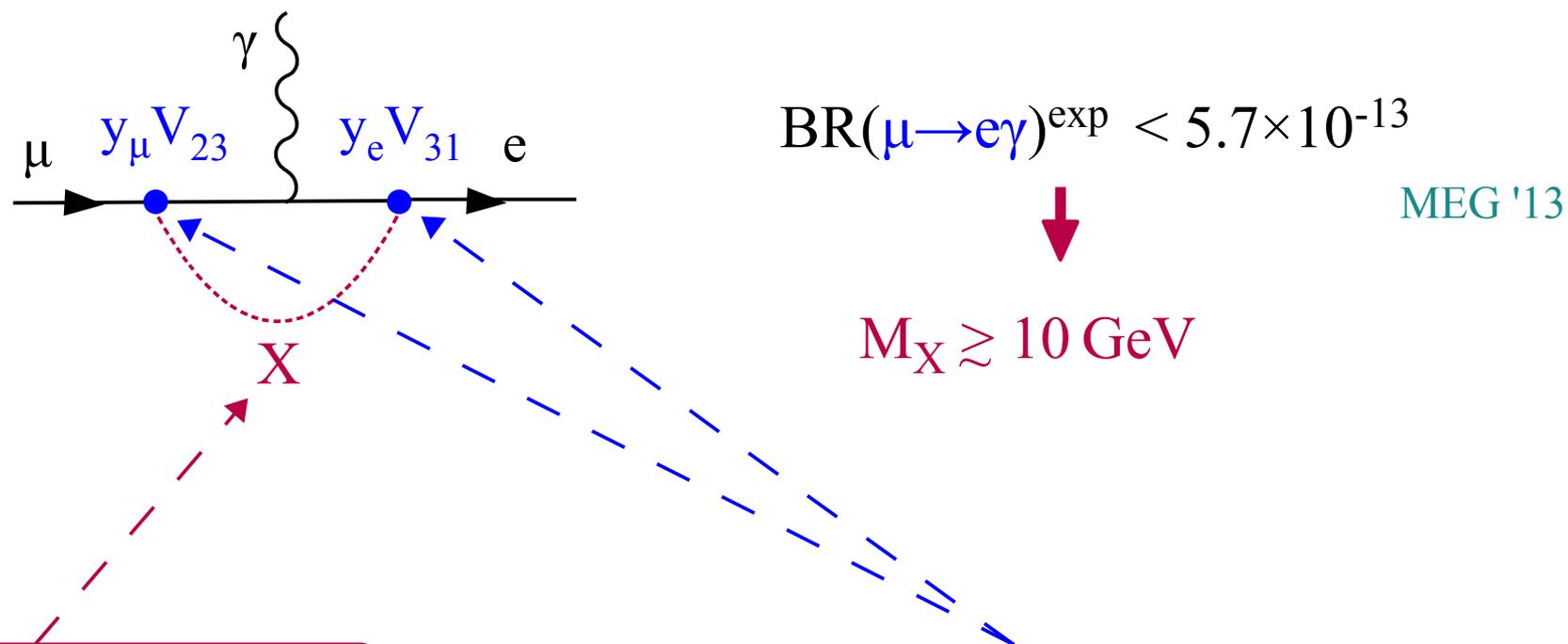
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$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM+v}} + \frac{c_{\text{NP}}}{\Lambda^2} \text{O}_{ij} \quad (6)$$

Operator	Bounds on $\Lambda$ in TeV ( $c_{\text{NP}} = 1$ )		Bounds on $c_{\text{NP}}$ ( $\Lambda = 1$ TeV)		Observables
	Re	Im	Re	Im	
$(\bar{s}_L \gamma^\mu d_L)^2$	$9.8 \times 10^2$	$1.6 \times 10^4$	$9.0 \times 10^{-7}$	$3.4 \times 10^{-9}$	$\Delta m_K; \epsilon_K$
$(\bar{s}_R d_L)(\bar{s}_L d_R)$	$1.8 \times 10^4$	$3.2 \times 10^5$	$6.9 \times 10^{-9}$	$2.6 \times 10^{-11}$	$\Delta m_K; \epsilon_K$
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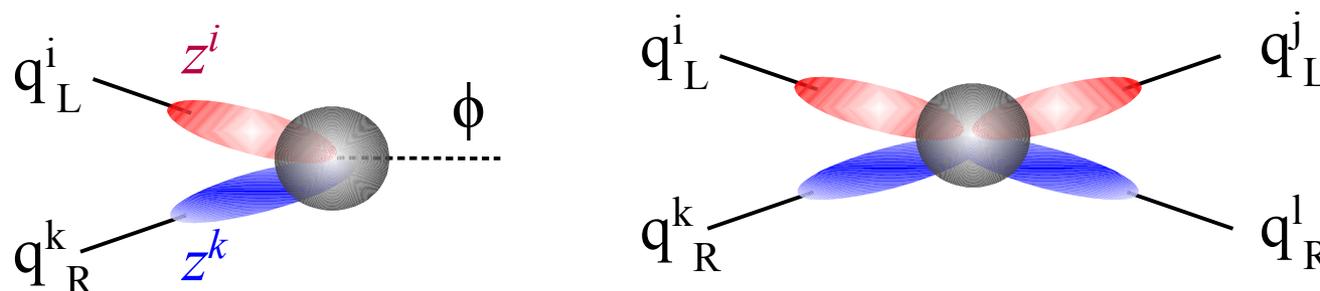


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More generally, we have explored only a small fraction of a large (multi-dim.) parameter space. The bounds on the scale of NP are still relatively weak in realistic models linking flavor mixing beyond the SM to the observed mass hierarchies.

E.g.:

*Partial  
Compositeness:*



“Elementary-composite mixing” as  
unique source of fermion mass hierarchies

$$Y_D^{ij} \approx z_Q^i z_D^j$$

$$Y_U^{ij} \approx z_Q^i z_U^j$$

$$z_Q^3 \gg z_Q^2 \gg z_Q^1$$

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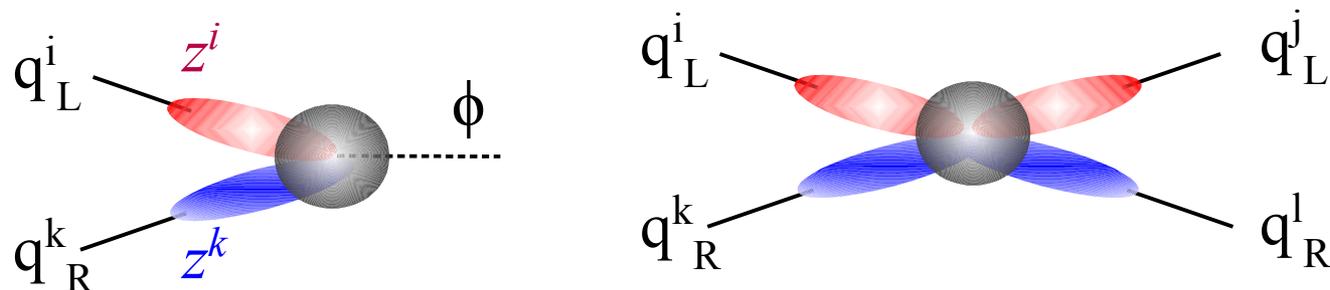
Natural suppression of flavor-violating  
processes involving the light generations

*(link with the smallness of light masses)*

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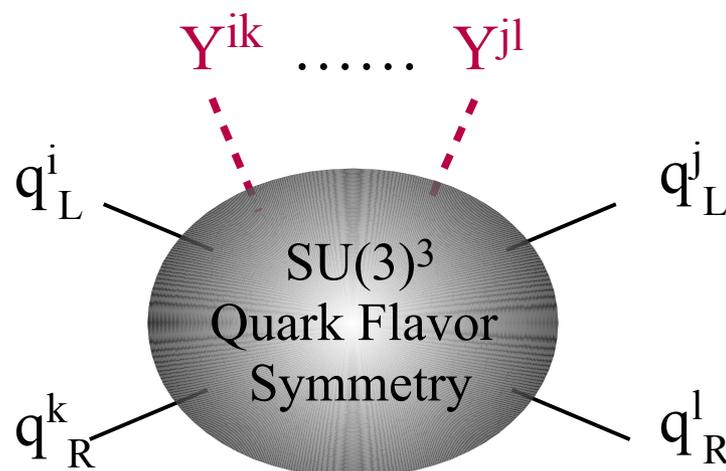
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Yukawa couplings as  
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### Mass scale of New Physics (*new colored & flavored particles*)

< 1 TeV

few TeV

> few TeV

*Direct New Physics searches @ high  $pT$ :*

NP within direct  
reach @ 8 TeV

NP within reach  
@ 14 TeV

NP beyond direct  
searches @ LHC

*NP effects in Quark Flavor Physics:*

Flavor Structure

Anarchic

huge  
[ > O(1) ]

sizable  
[ O(1) ]

sizable/small  
[ < O(1) ]

Small  
misalignment  
(*e.g. partial  
compositeness*)

sizable  
[ O(1) ]

small  
[ O(10%) ]

small/tiny  
[ O(1-10%) ]

Aligned to  
SM (*MFV*)

small  
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not visible  
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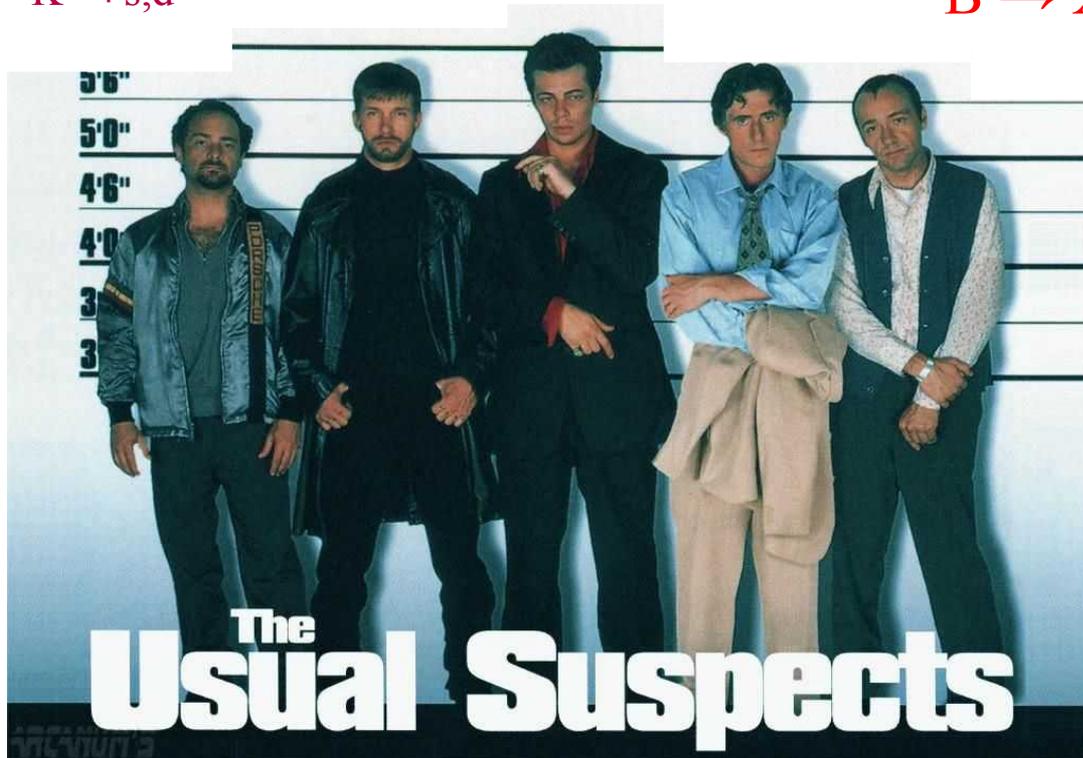
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# SUSY & Flavor

$\epsilon_K, \phi_{s,d}$     $\Delta m_{B_{s,d}}$     $|V_{ub}|$  & CKMfits    $B_{s,d} \rightarrow \mu\mu$     $B \rightarrow X_s \gamma$



▶ “Split-family” SUSY

Despite the absence of signals, SUSY remains our best candidate for a UV completion of the SM not far from the TeV scale:

- **Weakly coupled theory + light Higgs** (*125 is well the SUSY region...*)  
+ **dark-matter & unification**
- Some tuning in  $m_h$  is unavoidable: *do we really care if the fine-tuning is  $\sim 1\%$  ?*

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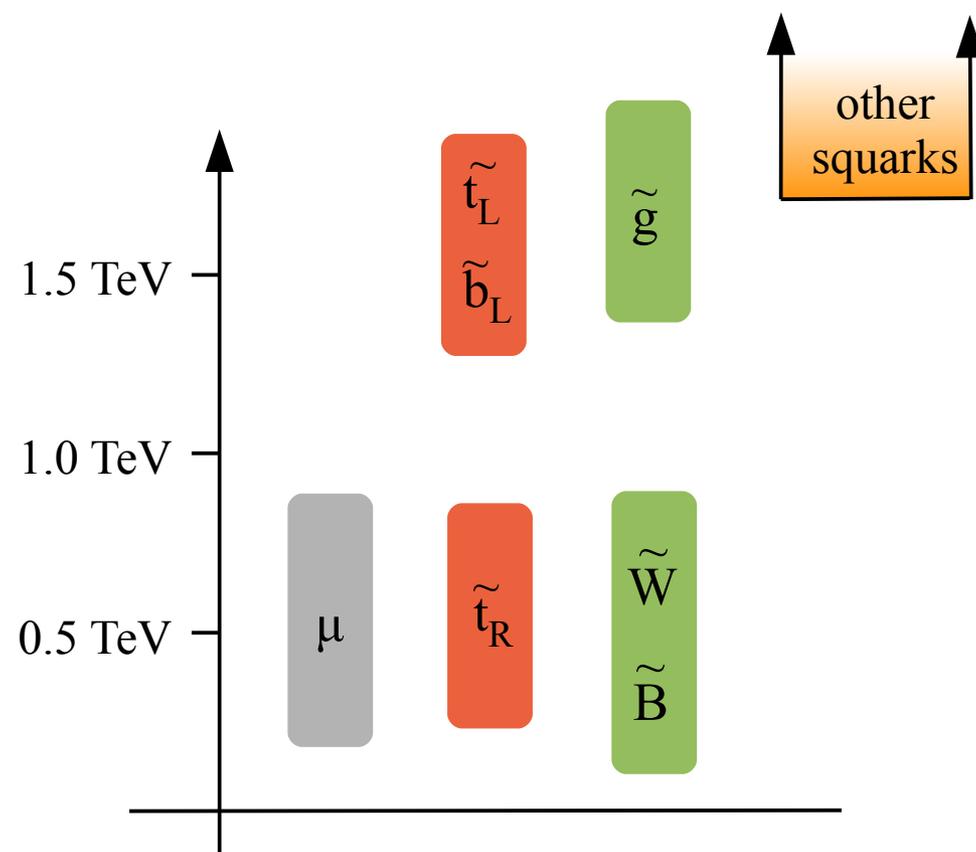
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Most of the low-scale SUSY virtues are maintained if we assume a **flavor non-trivial** spectrum

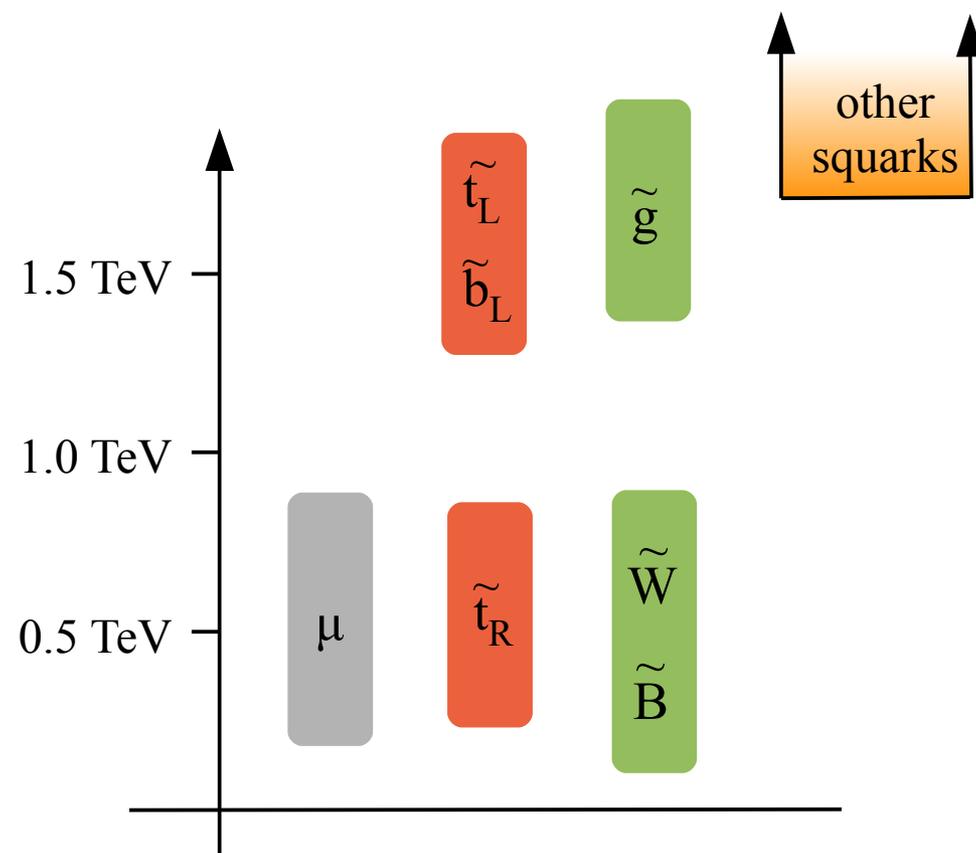
→  
Dimopoulos, Giudice, '95  
Cohen, Kaplan, Nelson '96  
+ many others...

- 3<sup>rd</sup> gen. squarks + Higgsinos key ingredients in the  $m_h$  tuning
- splitting the 3<sup>rd</sup> family can easily be motivated in flavor models



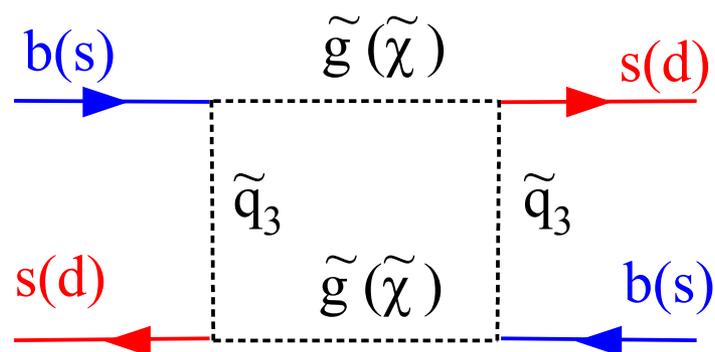
## ► The Usual Suspects

- LHC experiments have started to directly explore this scenario & possible variations (e.g: *mini-spilt...*).
- In this context, flavor physics plays a key role [*non-trivial flavor structure*]  
→ BSM effects mediated by 3<sup>rd</sup> gen. squarks & leptons:



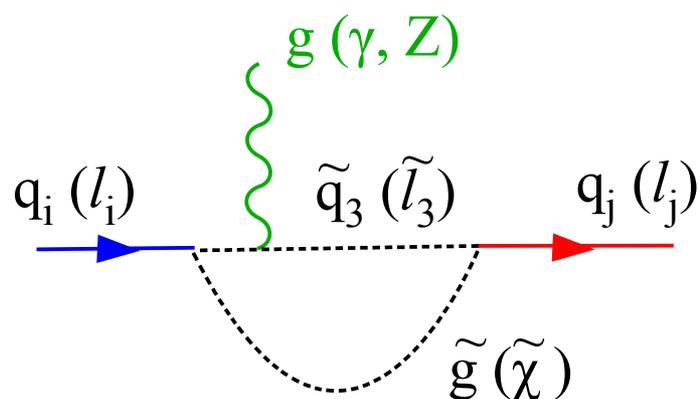
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Possible “visible” [ $\sim 5-20\%$ ] effects in

- CPV in K mixing ( $\epsilon_K$ )
- CPV in  $B_{s,d}$  mixing ( $\phi_{s,d}$ )



Possible “visible” [ $\sim 5-20\%$ ] effects in

- Rare B decays ( $B_s \rightarrow \mu\mu$ ,  $B_s \rightarrow X_s\gamma$ )
- LFV ( $\mu \rightarrow e\gamma$ ) & EDMs

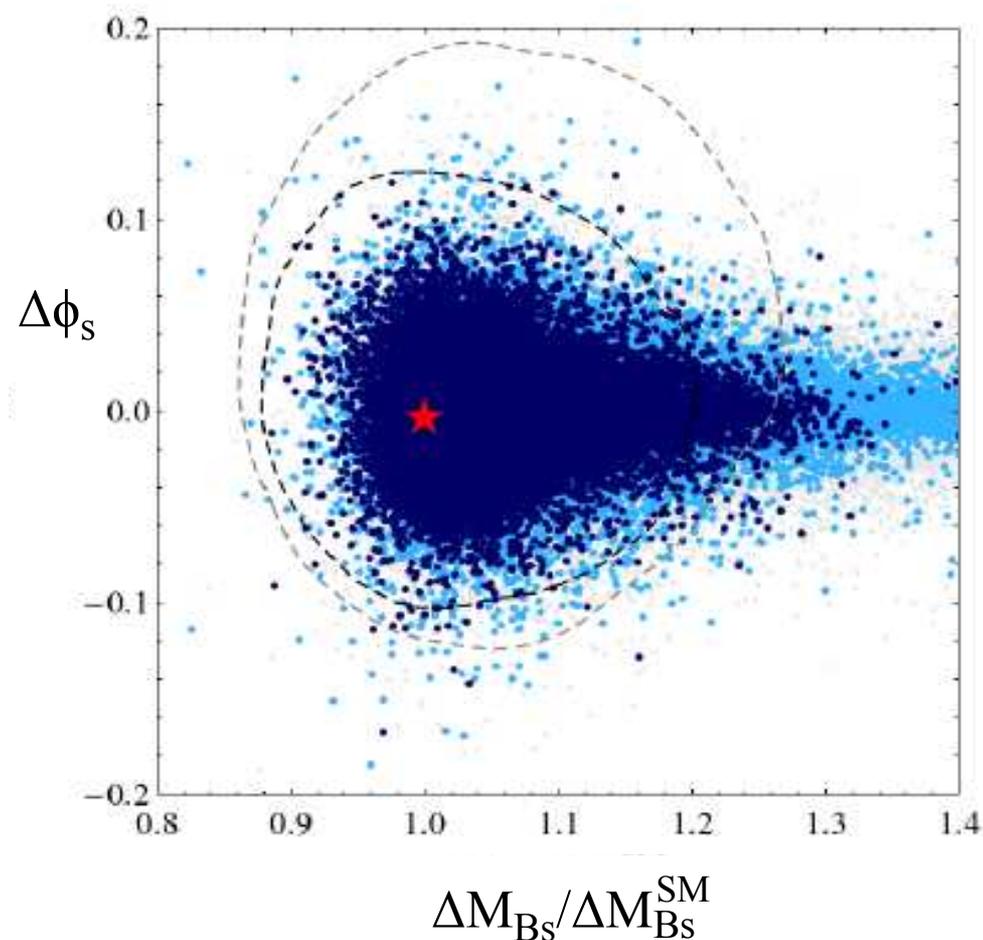
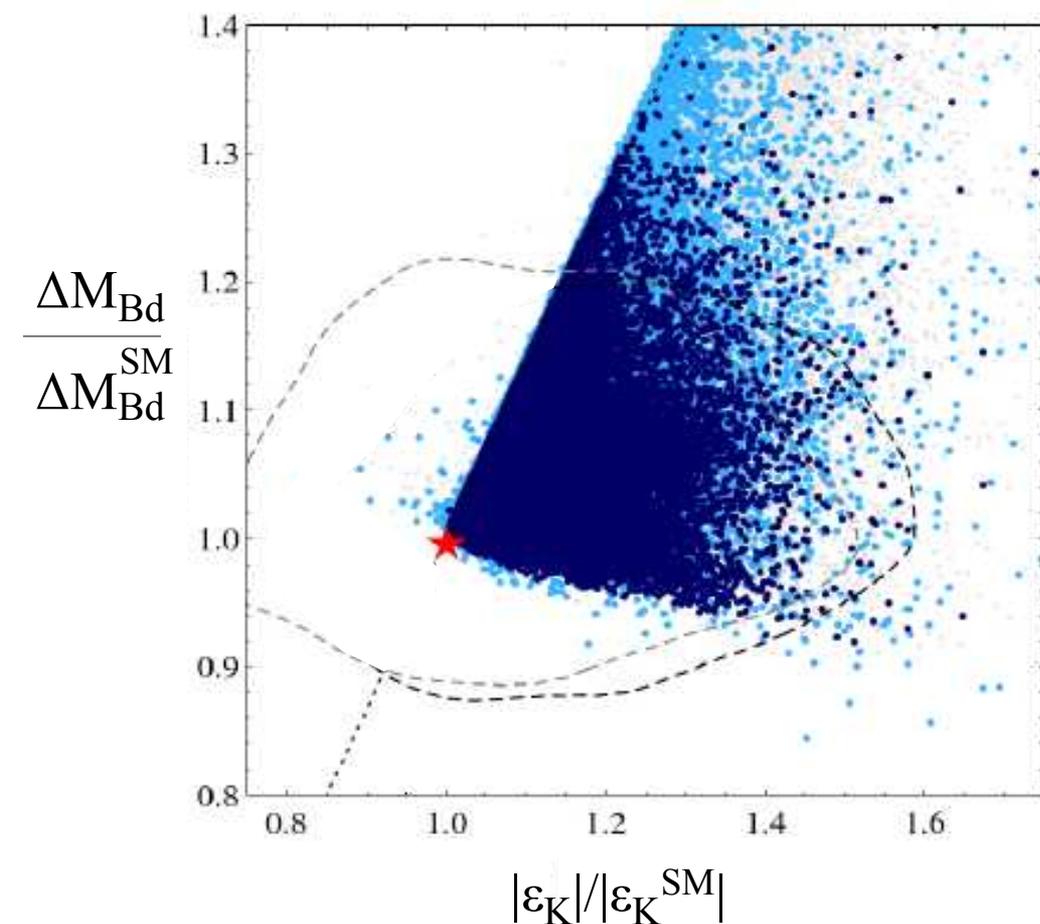
Barbieri *et al.* '12-'14; Delgado *et al.* '13  
Althmanshofer, Harnik, Zupan, '13  
Katz, Reece, Sajjad '14 + ...

**Example I:** *Meson mixing in “Natural SUSY” with  $U(2)^3$  flavor symm.*

Barbieri *et al.*, '11

Points allowed by present CMS/ATLAS data:

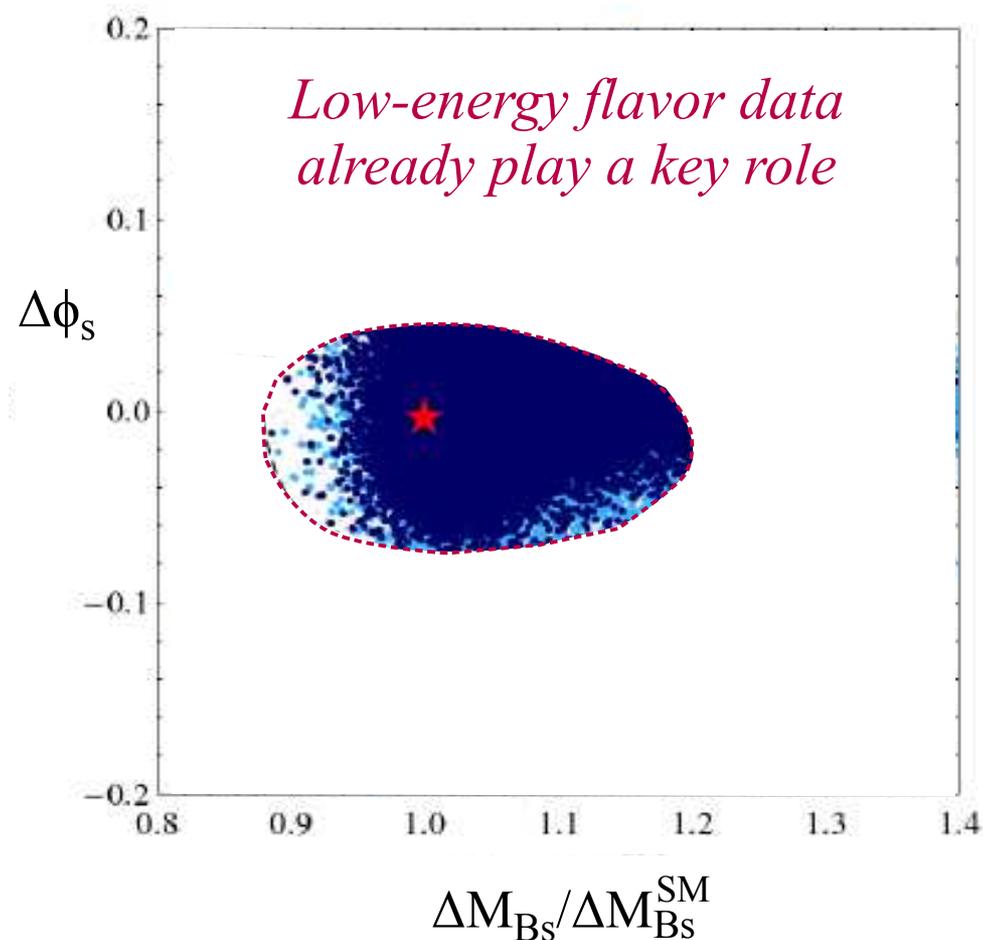
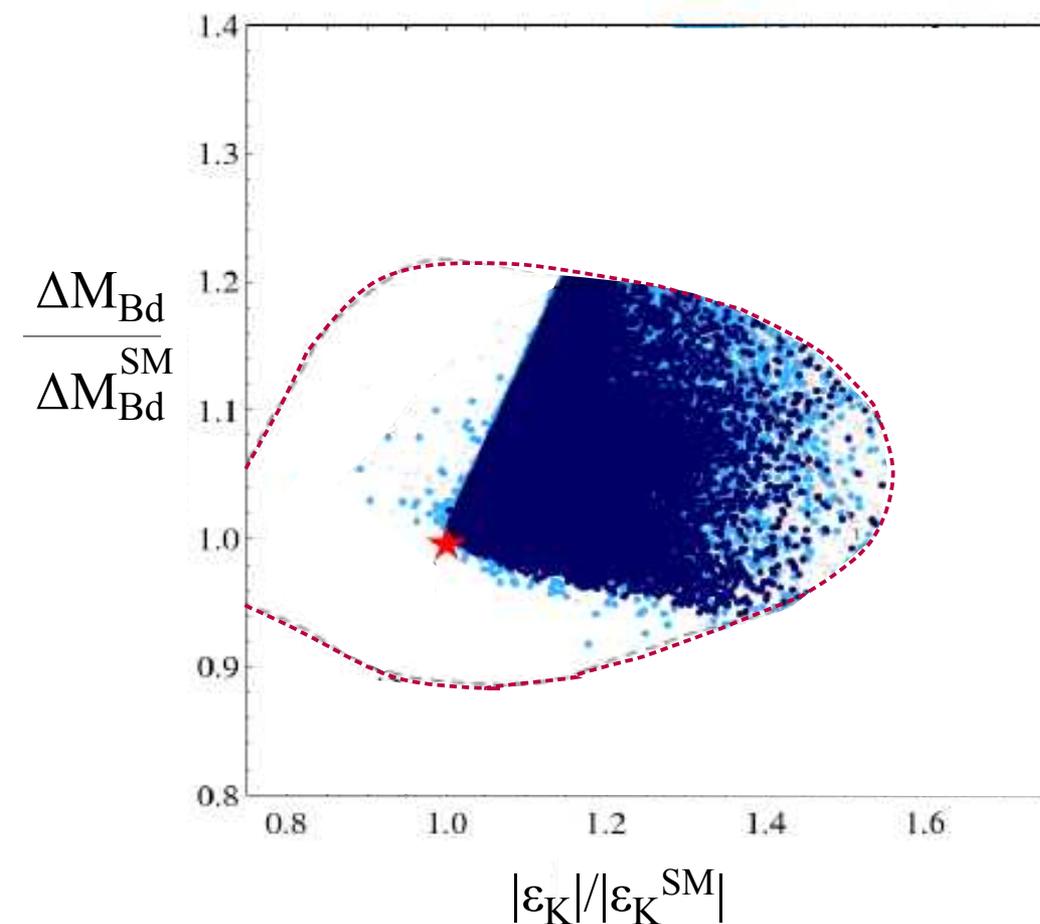
Barbieri, Buttazzo, Sala, Straub, '14



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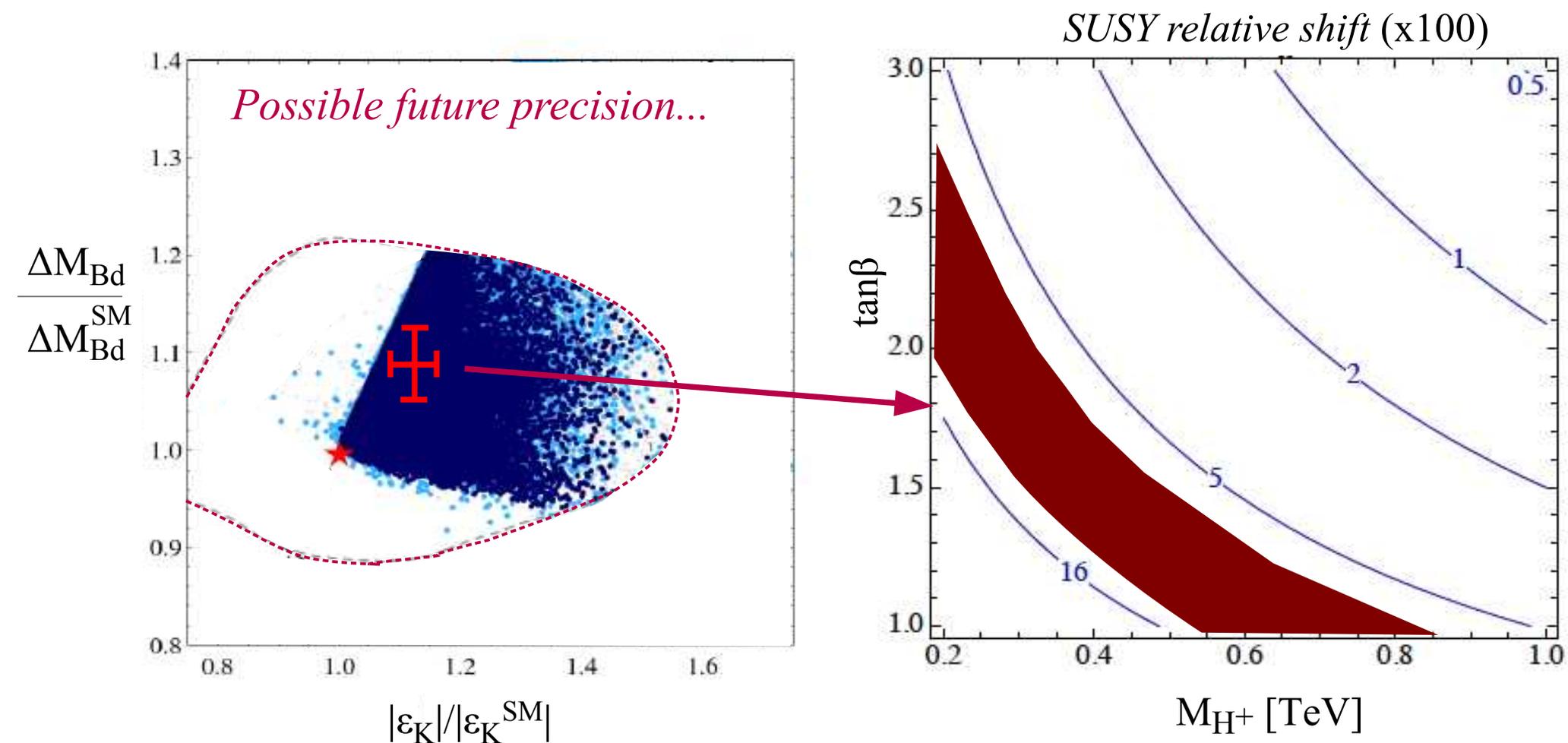
Points allowed by present CMS/ATLAS data + **present** flavor data

Barbieri, Buttazzo, Sala, Straub, '14



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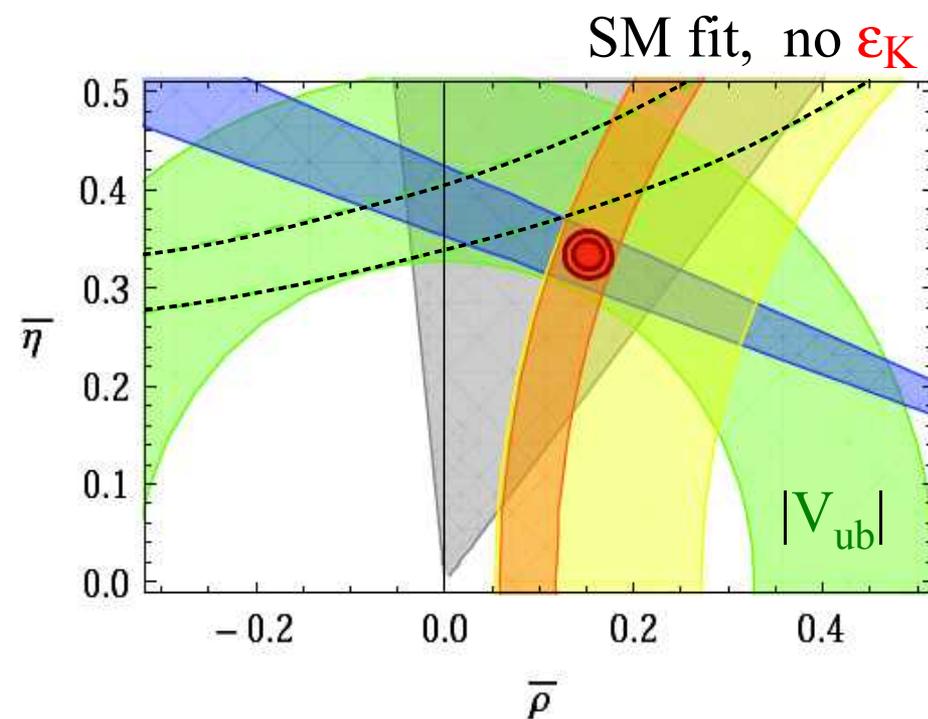
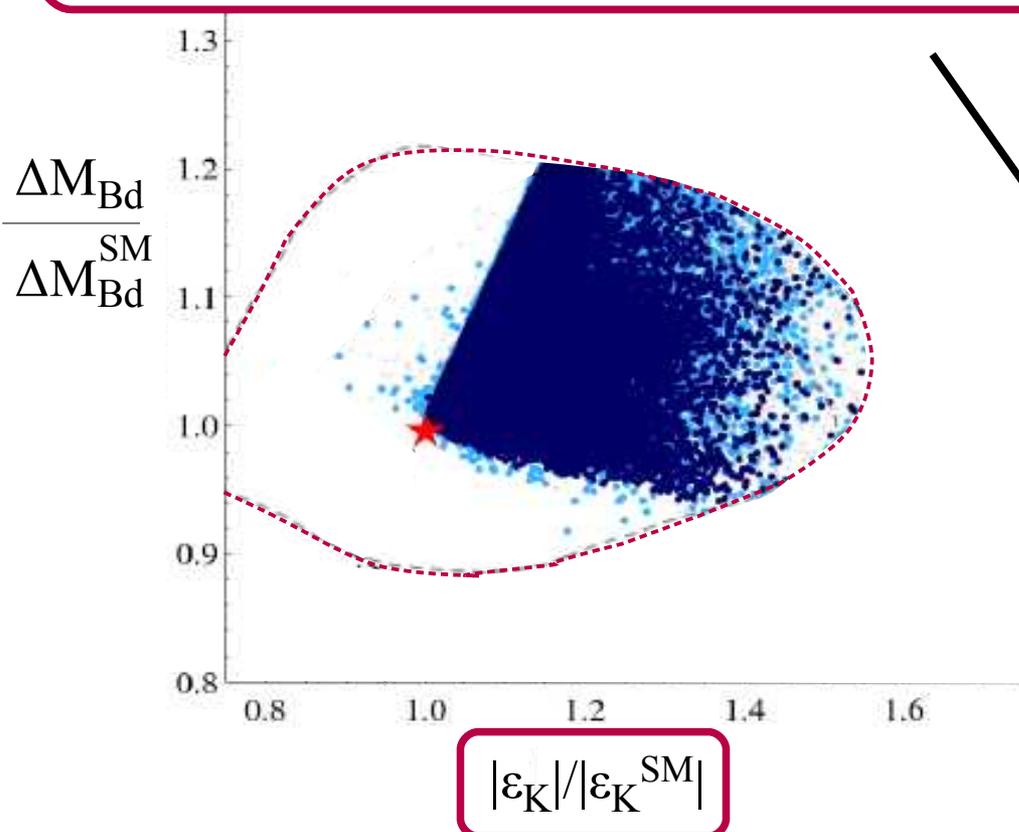
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## Example I: Meson mixing in “Natural SUSY” with $U(2)^3$ flavor symm.

**N.B.:** There is a (weak) evidence of a (positive) non-standard contribution to  $\epsilon_K$

In order to clarify the picture we need a more clean determination of  $|V_{ub}|$  &  $\gamma$



Complementary role of

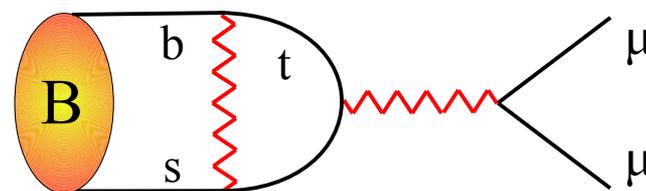
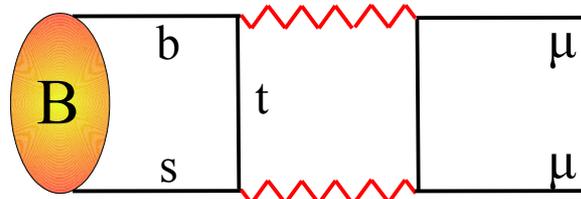
- [Belle-II](#) [ $\rightarrow |V_{ub}|$  from  $B \rightarrow \pi \nu$  and  $B \rightarrow \tau \nu$ ]
- and [LHCb](#) [ $\rightarrow \gamma$ ]

## Example II: $B_{s,d} \rightarrow \mu\mu$ & SUSY

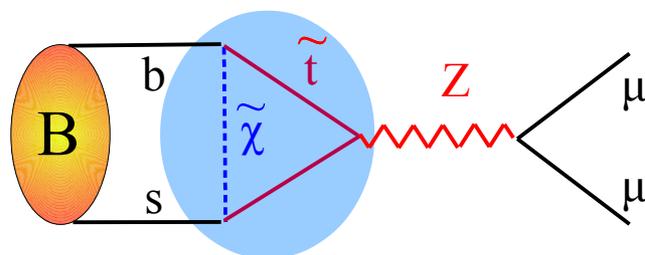
These modes are a unique source of information about flavor physics beyond the SM:

- ♦ theoretically very clean (virtually no long-distance contributions)
- ♦ particularly sensitive to FCNC *scalar currents* and FCNC *Z penguins*

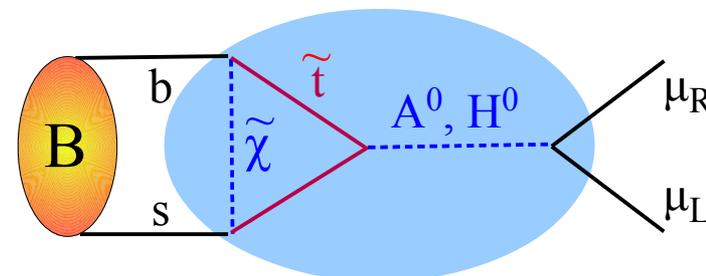
*Leading SM diagrams  
(unitary gauge):*



*Possible non-SM contributions:*



Relevant for  $BR = O(SM)$



Possible large enhancement  
(e.g. SUSY @ large  $\tan\beta$ )

Example II:  $B_{s,d} \rightarrow \mu\mu$  & SUSY

Recent developments both on the theory and on the experimental side:

$$\overline{\text{BR}}_{s,\text{SM}} = (3.65 \pm 0.23) \times 10^{-9}$$

(time-integrated average)

Bobeth, Gorbahn, Hermann, Misiak,  
Stamou, Steinhauser '13

+

progress from Lattice QCD

$$\overline{\text{BR}}_s^{(\text{exp})} = (2.9 \pm 0.7) \times 10^{-9}$$

LHCb + CMS '13

$$\text{BR}_{d,\text{SM}} = (1.06 \pm 0.09) \times 10^{-10}$$

$$\text{BR}_d^{(\text{exp})} = (3.6 \pm 1.5) \times 10^{-10}$$

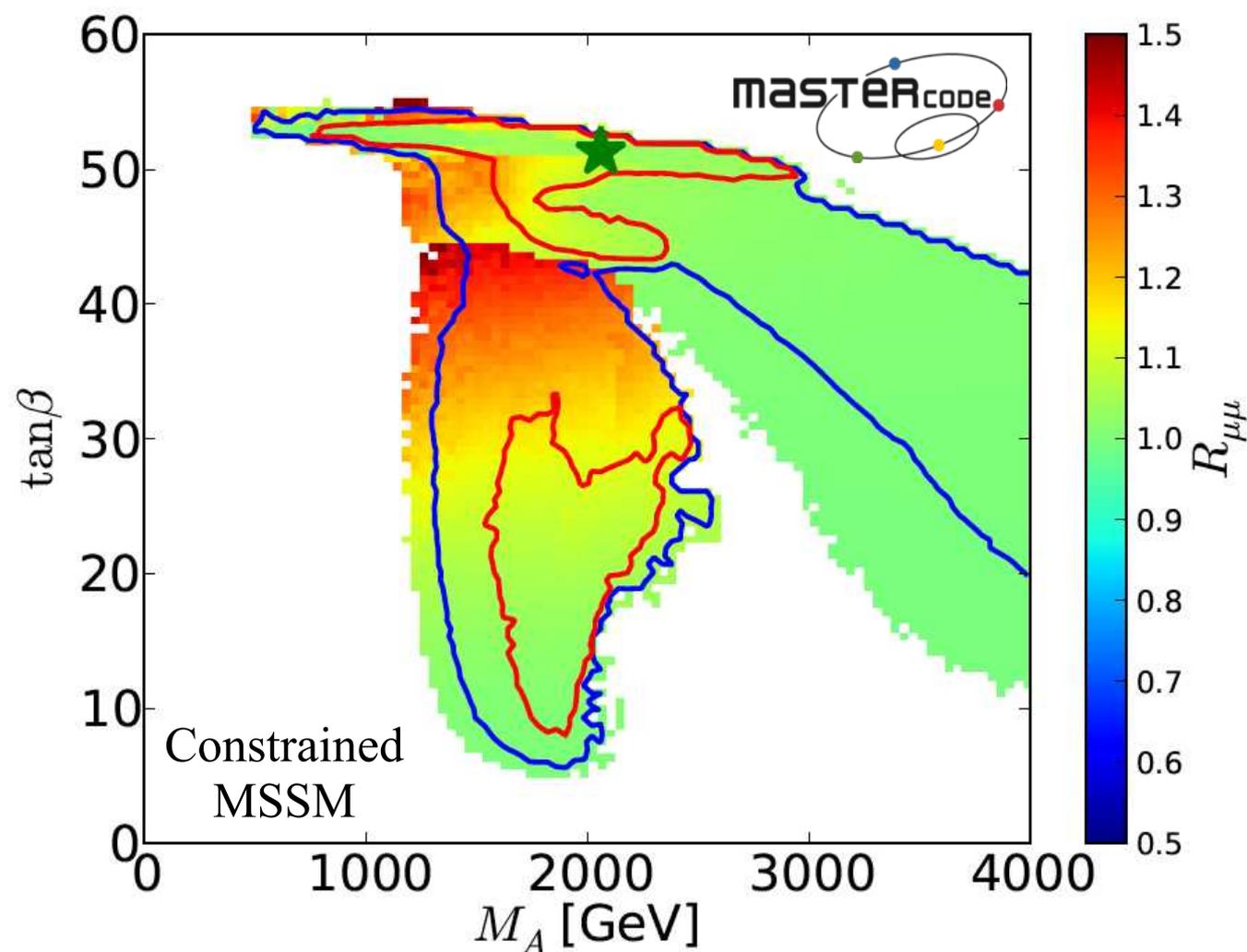
*An overall th. error below 5% is definitely  
within the reach in the next few years*

*At this stage there is perfect compatibility,  
but we are only at the beginning...*

Example II:  $B_{s,d} \rightarrow \mu\mu$  & SUSY

$$\overline{\text{BR}}_{s,\text{SM}} = (3.65 \pm 0.23) \times 10^{-9}$$

$$\overline{\text{BR}}_s^{(\text{exp})} = (2.9 \pm 0.7) \times 10^{-9}$$



The possible large effects occurring in the MSSM at large  $\tan\beta$  are ruled out...

...but more precision on this mode can still provide very valuable infos

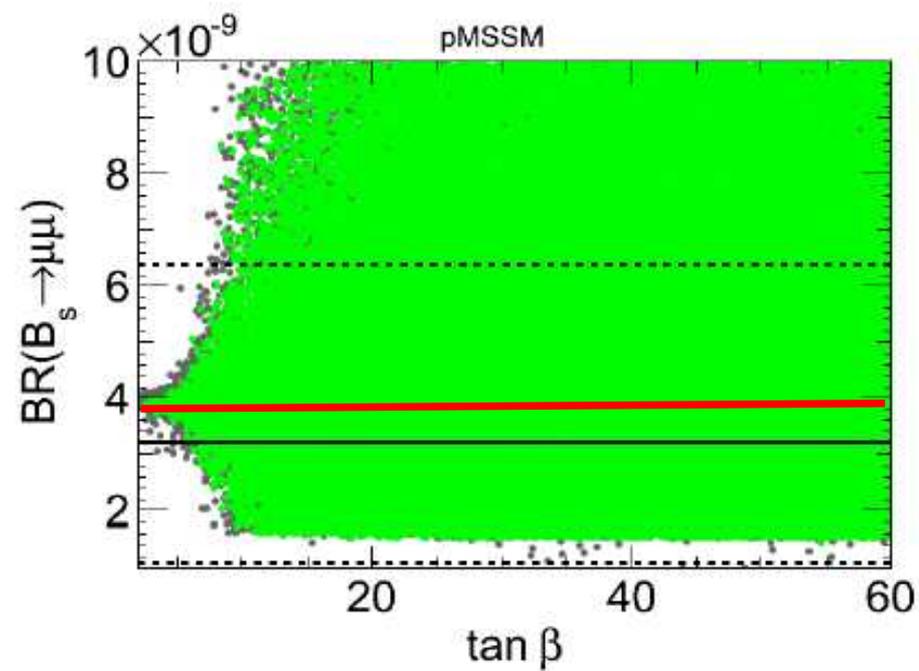
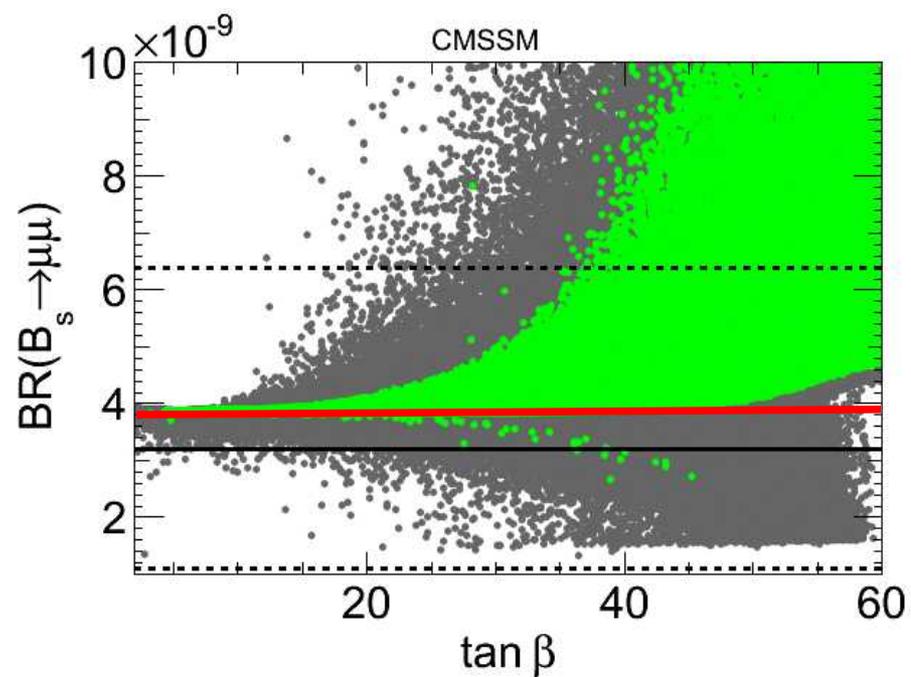
Buchmueller *et al.* [Mastercode]  
 Mahmoudi *et al.* [SuperIso]  
 Roszkowski *et al.* '12  
 Haisch & Mahmoudi '12  
 Althmanshofer *et al.* '13

...

Example II:  $B_{s,d} \rightarrow \mu\mu$  & SUSY

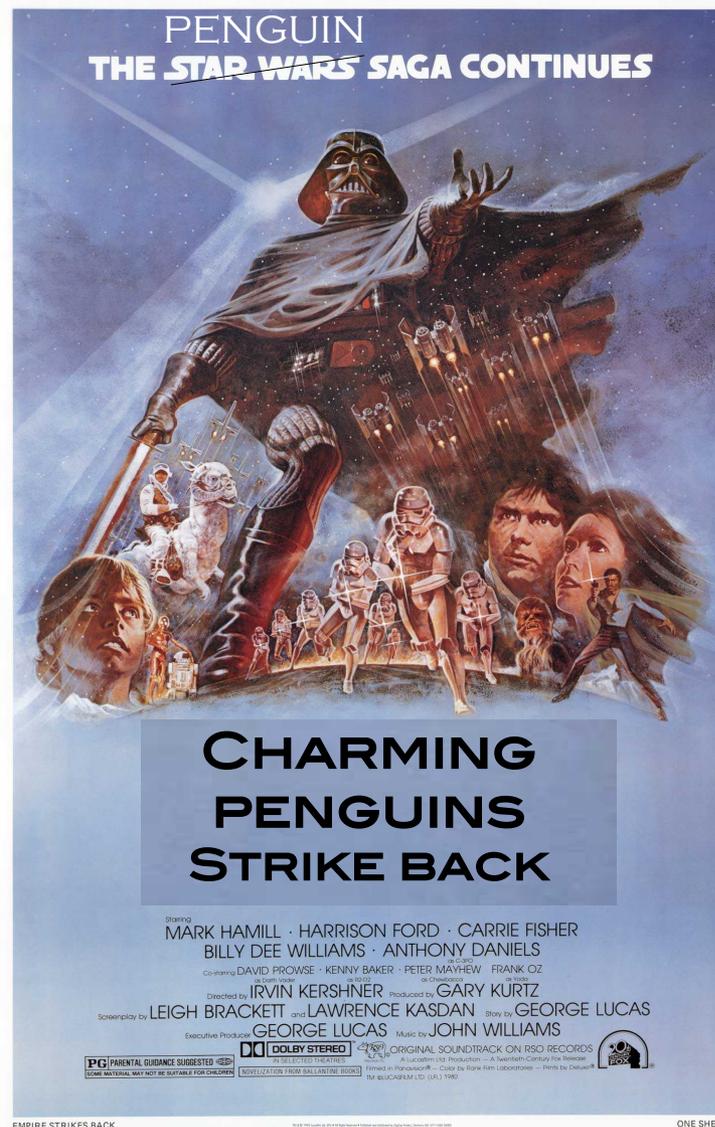
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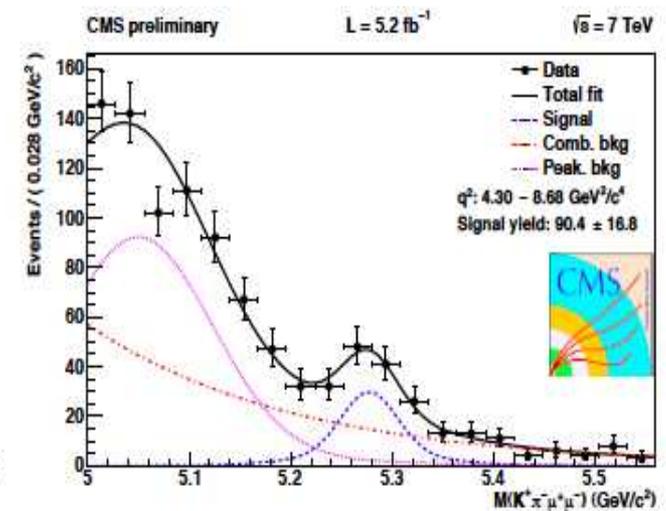
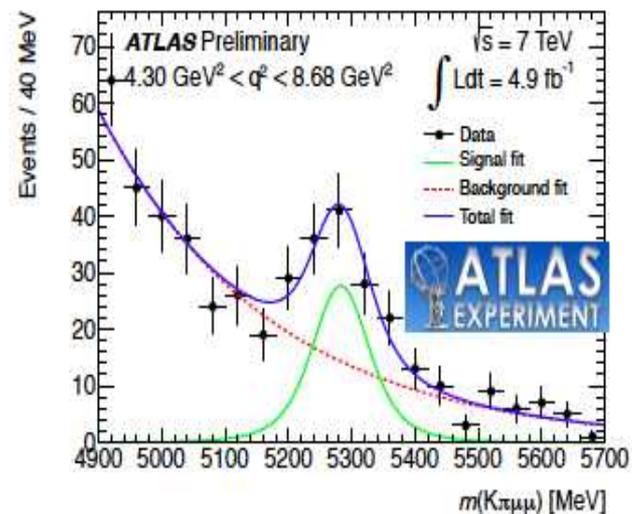
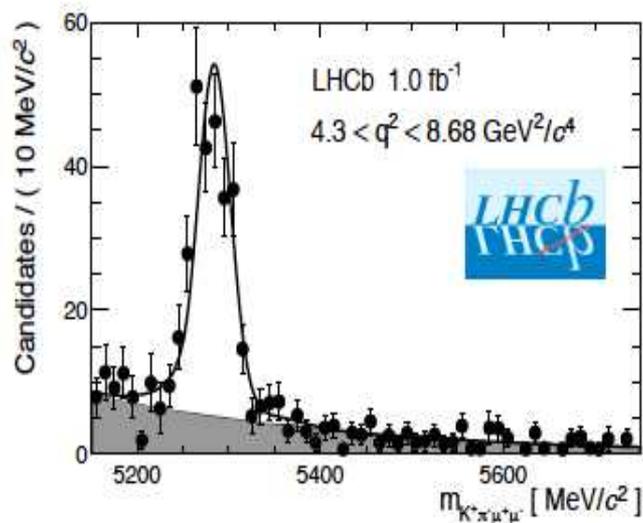
Arbey *et al.* '12

# The $B \rightarrow K^{(*)} ll$ anomalies



# The $B \rightarrow K^{(*)} ll$ anomalies

## $B \rightarrow K^{*} \mu\mu$ signals from the 3 LHC experiments:



► General considerations:

Similarly to  $B_{s,d} \rightarrow ll$ , also  $B \rightarrow K^{(*)} ll$  are FCNC amplitudes and, as such, are useful probes of flavor dynamics beyond the SM

- No SM tree-level contribution
- Strong suppression within the SM because of CKM hierarchy

**Key point to be addressed:** th. control of QCD effects, larger and potentially more dangerous than in  $B_{s,d} \rightarrow ll$ .

► General considerations:

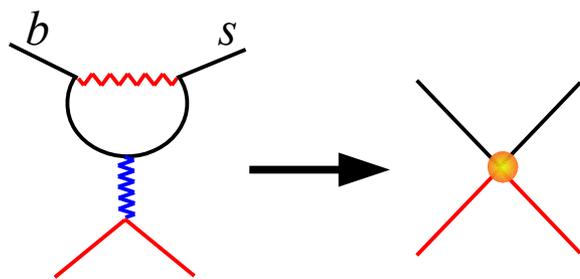
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**Key point to be addressed:** th. control of QCD effects, larger and potentially more dangerous than in  $B_{s,d} \rightarrow ll$ .

Three-step procedure to deal with the various scales of the problem:

**1<sup>st</sup> step:** Construction of a local eff. Hamiltonian at the electroweak scale



$$H_{\text{eff}} = \sum_i C_i(M_W) Q_i$$

- Heavy NP encoded in the  $C_i(M_W)$
- No difference among the various  $b \rightarrow s ll$  decays

**2<sup>nd</sup> step:** Evolution of  $H_{\text{eff}}$  down to low scales using RGE

FCNC operators (E.W. penguins)

$$Q_9 = Q_f (bs)_{V-A} (ll)_V$$

$$Q_{10} = Q_f (bs)_{V-A} (ll)_A$$

⋮

$$H_{\text{eff}} = \sum_i C_i(M_W) Q_i$$



$$H_{\text{eff}} = \sum_i C_i(\mu \sim m_b) Q_i$$

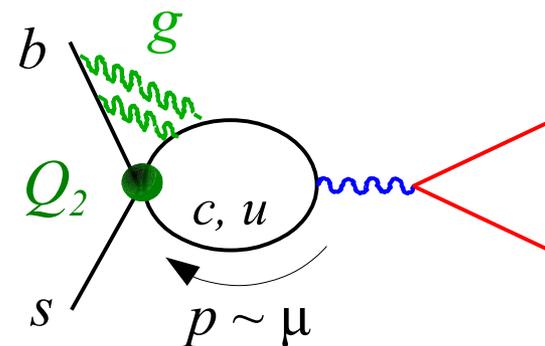
Four-quark (tree-level) ops.:

$$Q_1 = (bs)_{V-A} (cc)_{V-A}$$

$$Q_2 = (bc)_{V-A} (cs)_{V-A}$$

⋮

Mixing of the **four-quark**  $Q_i$  into the **FCNC**  $Q_i$   
 [“dilution” of the potentially interesting NP]:



Negligible for  $Q_{10}$  [ $B_{s,d} \rightarrow ll$  &  $B \rightarrow K^{(*)}ll$ ]

Large for “photon penguins”  $Q_9$  [ $B \rightarrow K^{(*)}ll$  only]

**2<sup>nd</sup> step:** Evolution of  $H_{\text{eff}}$  down to low scales using RGE

FCNC operators (E.W. penguins)

$$H_{\text{eff}} = \sum_i C_i(M_W) Q_i$$

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⋮



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⋮

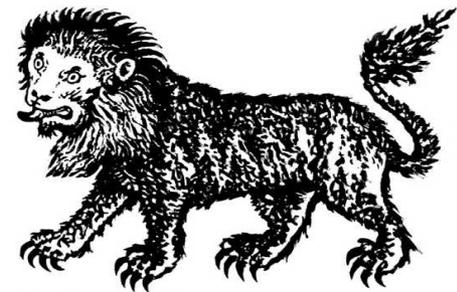
**3<sup>rd</sup> step:** Evaluation of the hadronic matrix elements

$$A(B \rightarrow f) = \sum_i C_i(\mu) \langle f | Q_i | B \rangle (\mu)$$

- sensitivity to long-distances (cc threshold...)
- distinction between
  - inclusive (OPE +  $1/m_{b,c}$  expansion)
  - exclusive modes (hadronic form factors  
→ Lattice or LCSR)

HIC  
SUNT  
LEONES

non-  
perturbative  
effects...



► The anomalies:

I. The  $P_5'$  anomaly in  $B \rightarrow K^{*0} \mu \mu$

$3.7\sigma$  local discrepancy

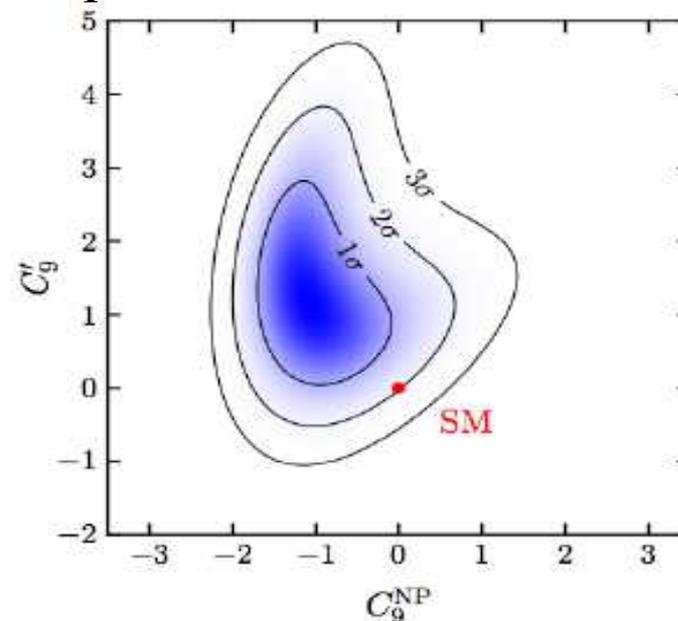
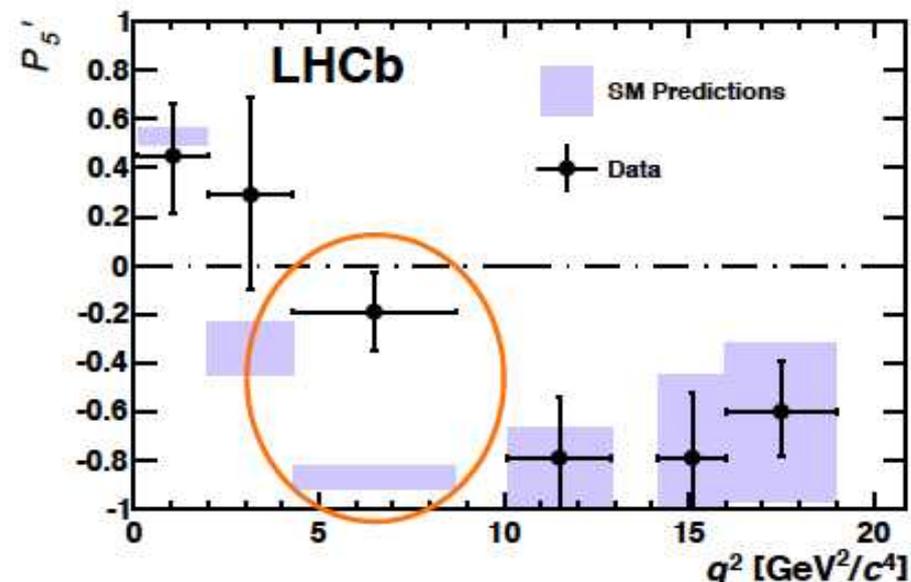
vs. SM [Descotes-Genon *et al.* '13]

II. Overall smallness of the four  
BR( $B \rightarrow H \mu \mu$ ),  $H=K^{*0}, K^{*+}, K^+, K^0$

Pro NP:

- Reduced tension with data in both cases with a unique fit of modified Wilson coefficients (mainly  $C_9$ )
- The corresponding effective NP scale is high ( $\sim 10$  TeV), not in contradiction with other data

Descotes-Genon, Matias, Virto '13  
Altmannshofer & Straub '13  
Beaujean, Bobeth, van Dyk '13  
Horgan *et al.* '13



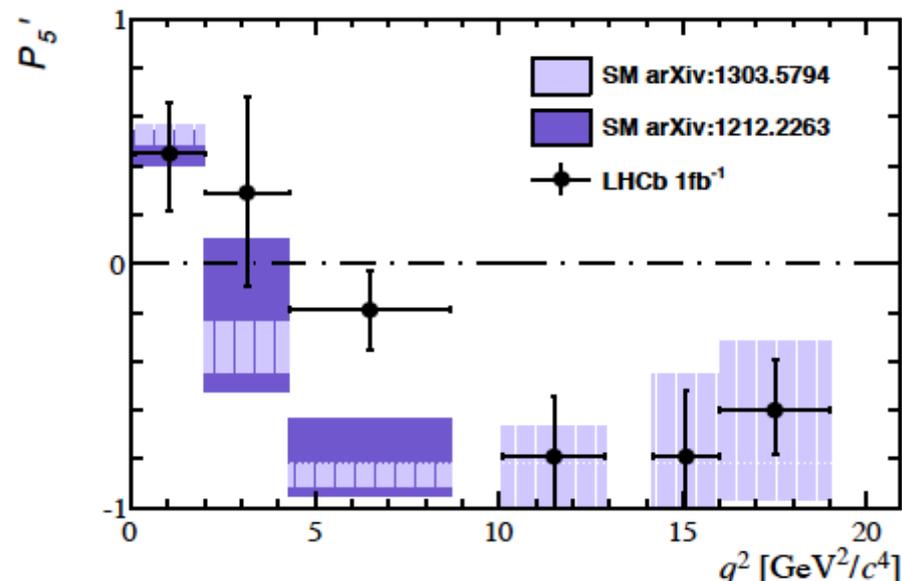
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Pro NP:

- Reduced tension with data in both cases with a unique fit of modified Wilson coefficients (mainly  $C_9$ )
- The corresponding effective NP scale is high ( $\sim 10$  TeV), not in contradiction with other data

Against NP:

- Main effect in  $P_5'$  not far from cc threshold
- Significance reduced with conservative estimates of non-perturbative corrections

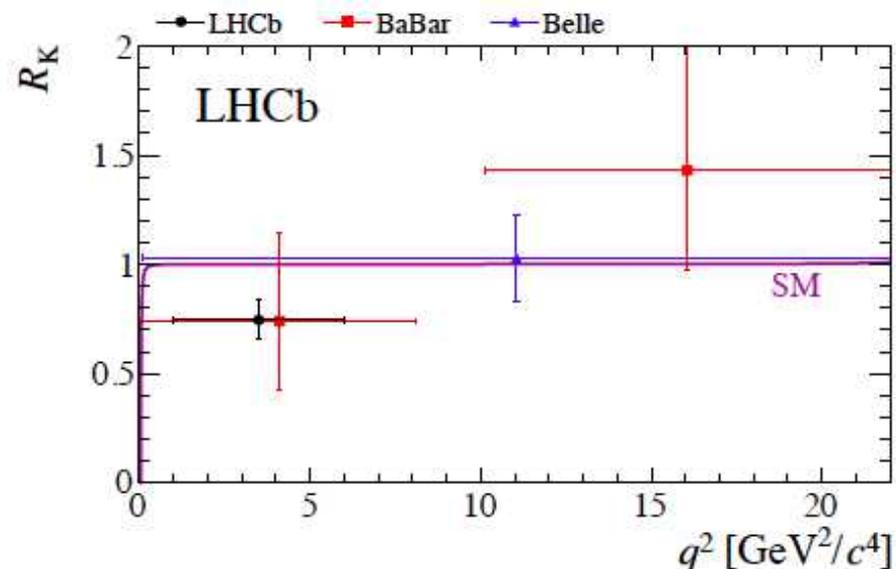
Jaeger et al. '12  
Hambrock et al. '13  
Hiller & Zwicky '13

► The anomalies:

III. The lepton universality ratio  
 $d\Gamma(B^+ \rightarrow K^+ \mu\mu)/d\Gamma(B^+ \rightarrow K^+ ee)$

$$R_K = 0.745^{+0.090}_{-0.074}(\text{stat})^{+0.036}_{-0.036}(\text{syst})$$

2.6 $\sigma$  from SM



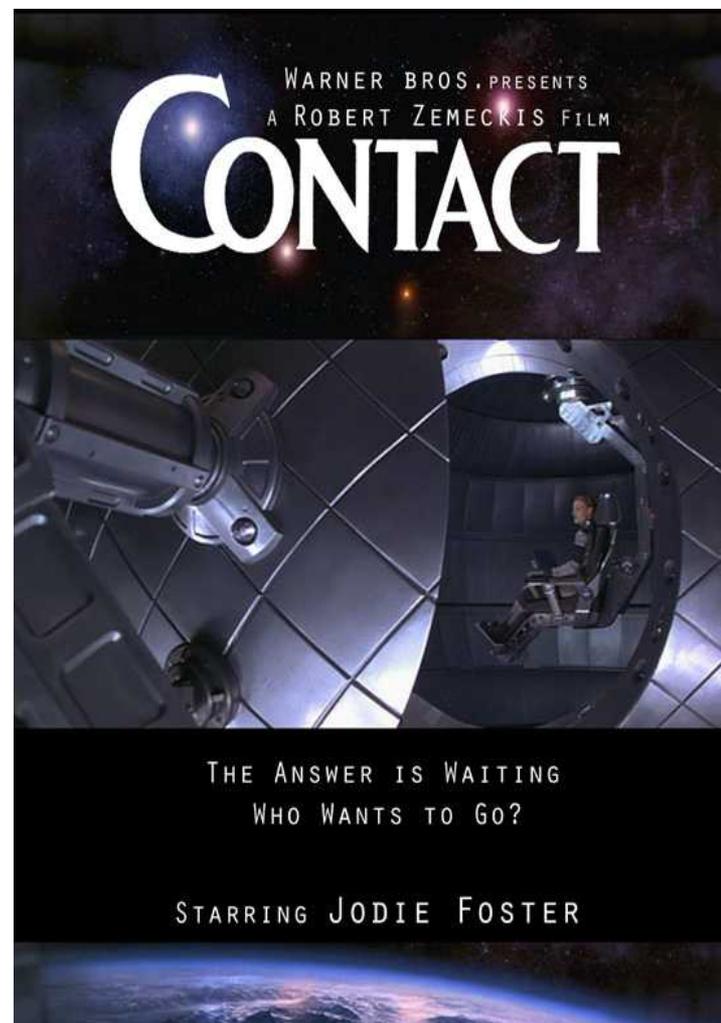
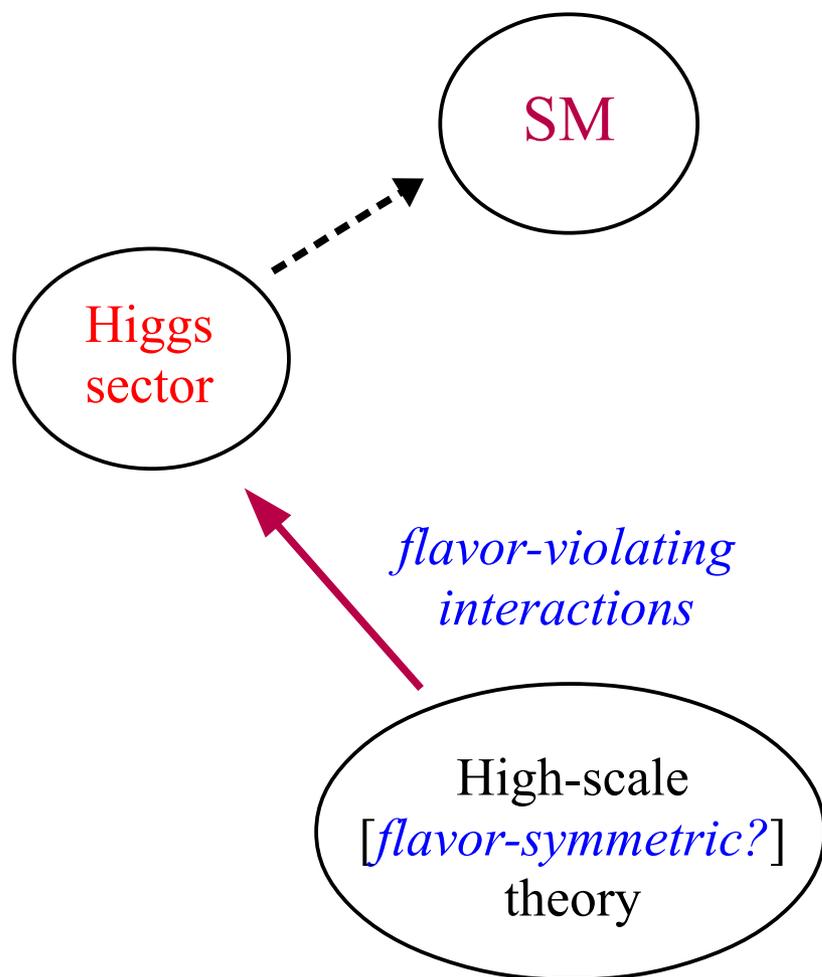
Key features:

- Th. prediction very solid (*QCD cannot affect lepton universality...*)
- NP in  $b \rightarrow see$ ? → *does not fit in a trivial way with any of the previous anomalies...*

Final considerations:

- ★ Intriguing BSM hints in  $b \rightarrow sll$  transitions, but no clear evidence yet (exp. fluctuations + theory errors may explain all the effects)
- ★ More data (on both exclusive & inclusive modes) can help to clarify the picture

## Flavor physics with the BEH boson



► Flavor-violating Higgs decays

Higgs-mediated FCNCs are extremely suppressed in the SM, but can be very large in models with an extended Higgs sector.

Even assuming a single Higgs doublet, but allowing non-vanishing higher-dimensional operators  $\rightarrow$  h-mediated FCNC are unavoidable:

$$Y^{ij} \psi_L^i \psi_R^j \phi + \epsilon^{ij} \psi_L^i \psi_R^j \phi^3 + \dots$$



$$(vY^{ij} + v^3 \epsilon^{ij}) \psi_L^i \psi_R^j + (Y^{ij} + 3v^2 \epsilon^{ij}) \psi_L^i \psi_R^j h + \dots$$

Azatov, Toharia, Zhu '09  
Agashe & Contino '09

$$\epsilon^{ij} = \frac{c^{ij}}{\Lambda^2}$$

---


$$vY_{\text{eff}}$$

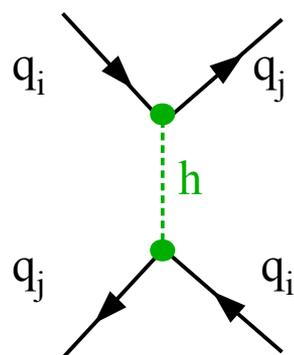
h FCNC couplings if  $Y^{ij} \neq c \epsilon^{ij}$

*Interplay between:*

- Indirect constraints [from h-mediated amplitudes @ low-energies]
- Direct FCNC h decays [enhanced sensitivity of h(125)  $\rightarrow$  suppressed width]

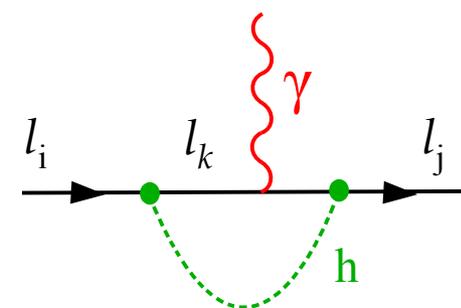
► Flavor-violating Higgs decays

$$\mathcal{L}_{\text{eff}} = \left[ \sum_{i,j=d,s,b} c_{ij} \bar{d}_L^i d_R^j h + \sum_{i,j=u,c,t} c_{ij} \bar{u}_L^i u_R^j h \right] + \left[ \sum_{i,j=e,\mu,\tau} c_{ij} \bar{\ell}_L^i \ell_R^j h + \text{H.c.} \right]$$



Strongly bounded  
by  $\Delta F=2$   
(except for terms  
involving the top)

Bounds less  
severe in the  
lepton sector,  
especially for the  
 $\tau\mu$  and  $\tau e$  modes



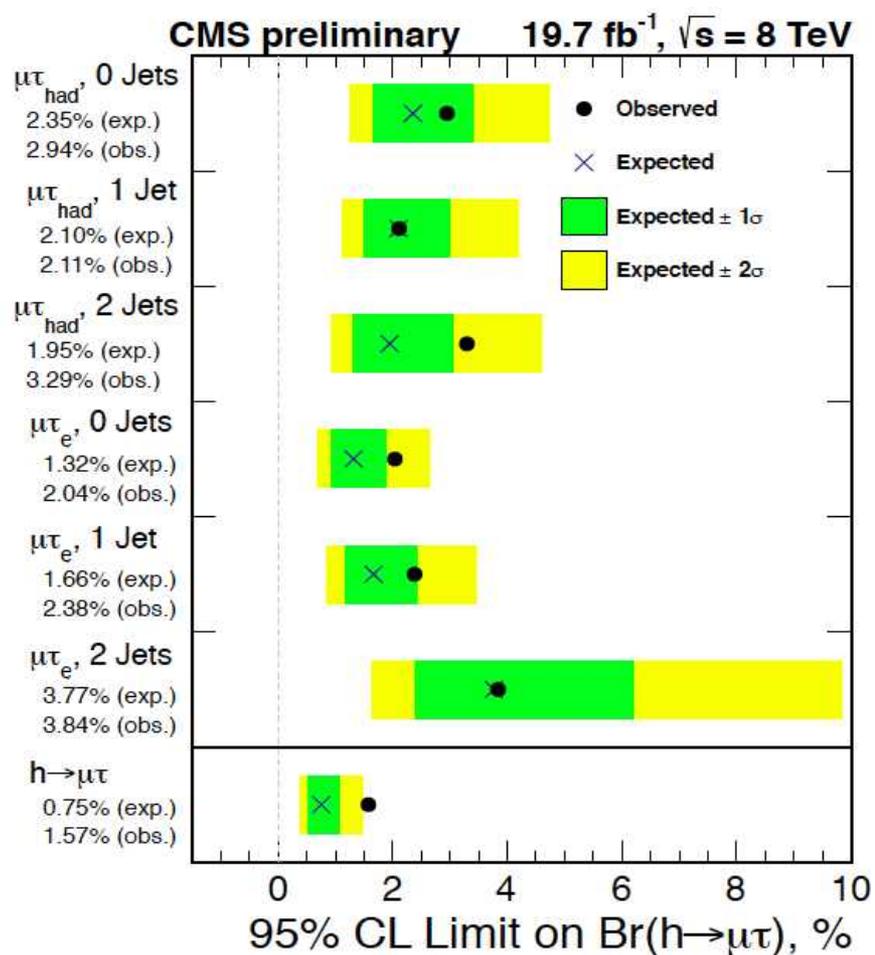
Indirect bounds imply  
 $\text{BR}(h \rightarrow \tau\mu, \tau e) \lesssim 10\%$

Blankenburg, Ellis, G.I. '12  
Harnik, Kopp, Zupan, '12  
Davidson, Verdier, '12

Celis, Cirigliano, Passemar, '13  
Kopp & Nardecchia '14

## ► Flavor-violating Higgs decays

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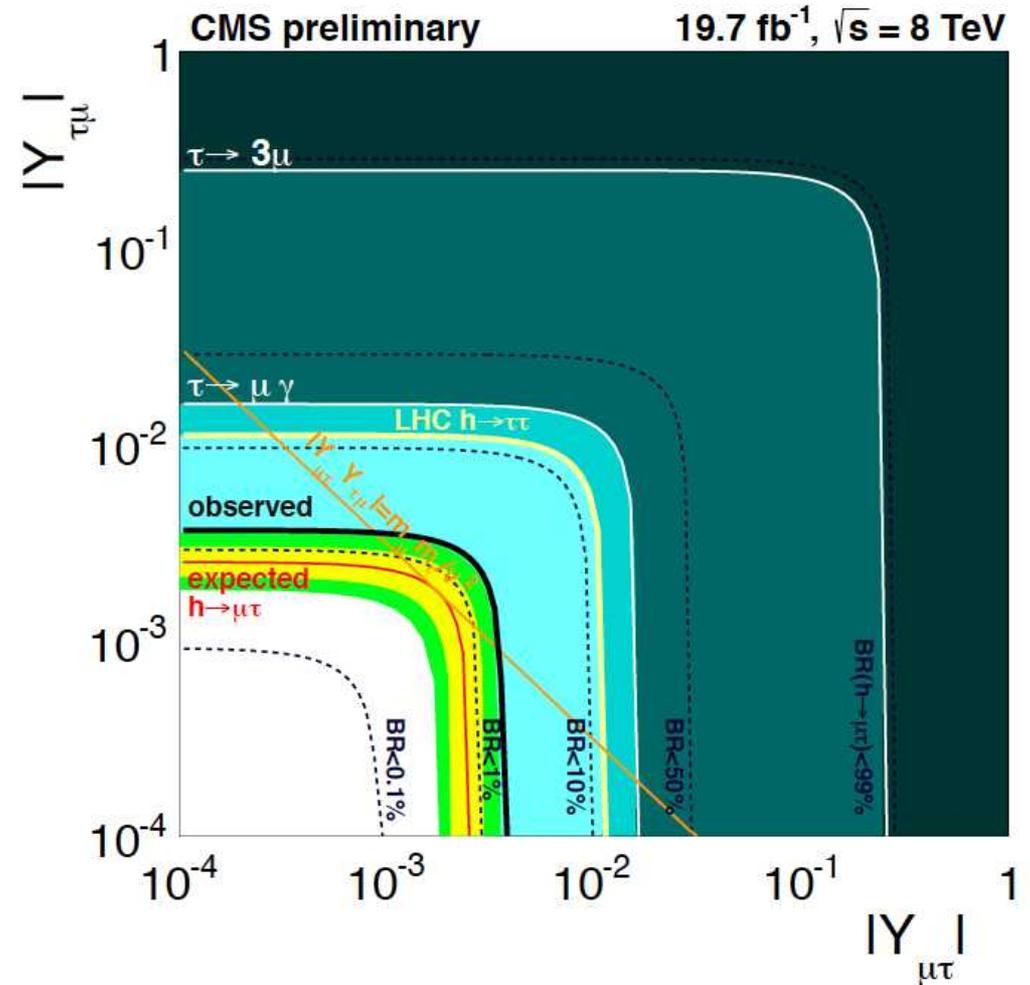
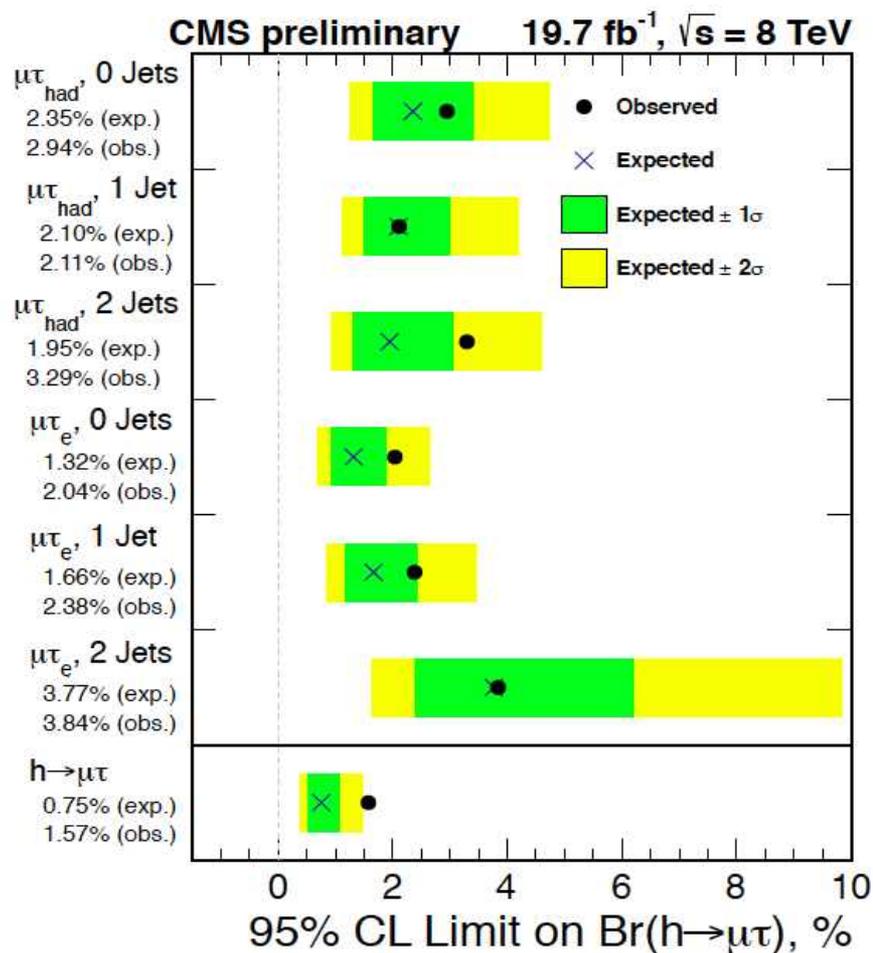


$$\text{BR}(h \rightarrow \mu\tau) = (0.89^{+0.40}_{-0.37})\%$$

CMS '14

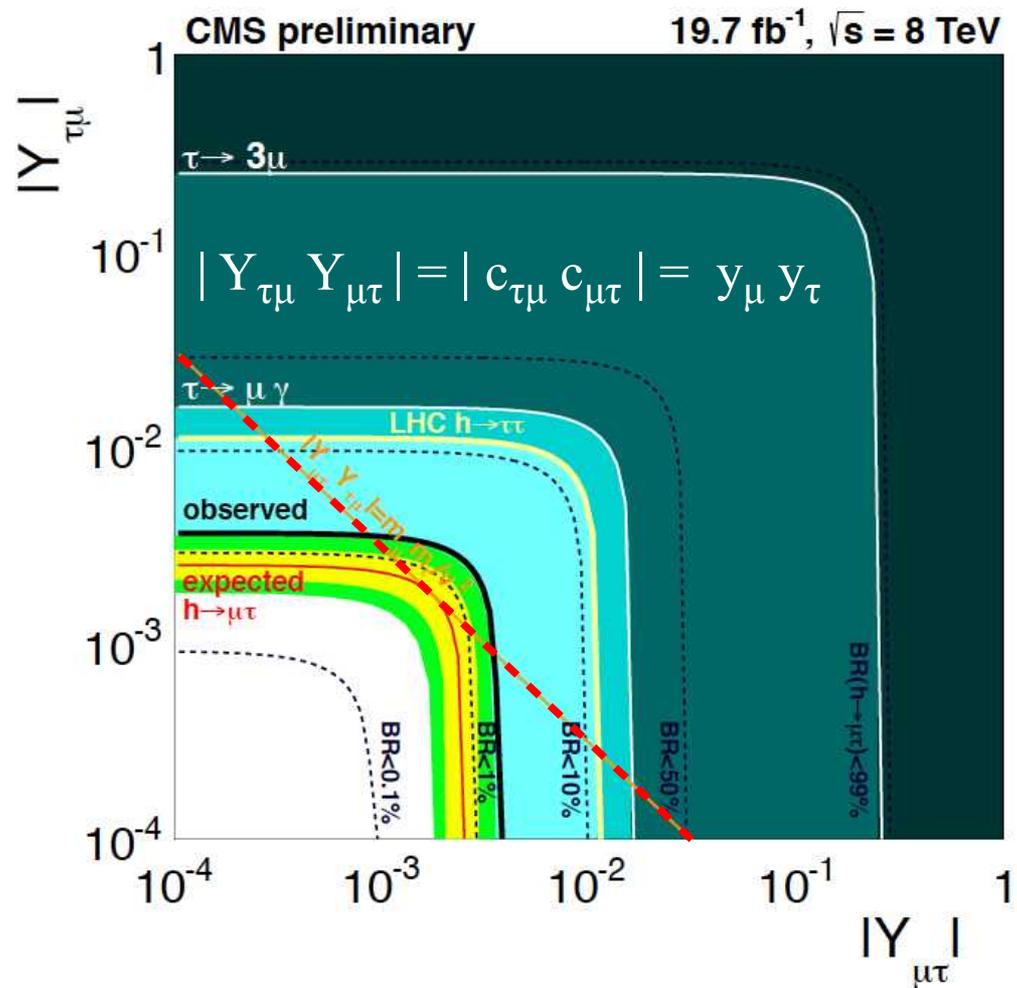
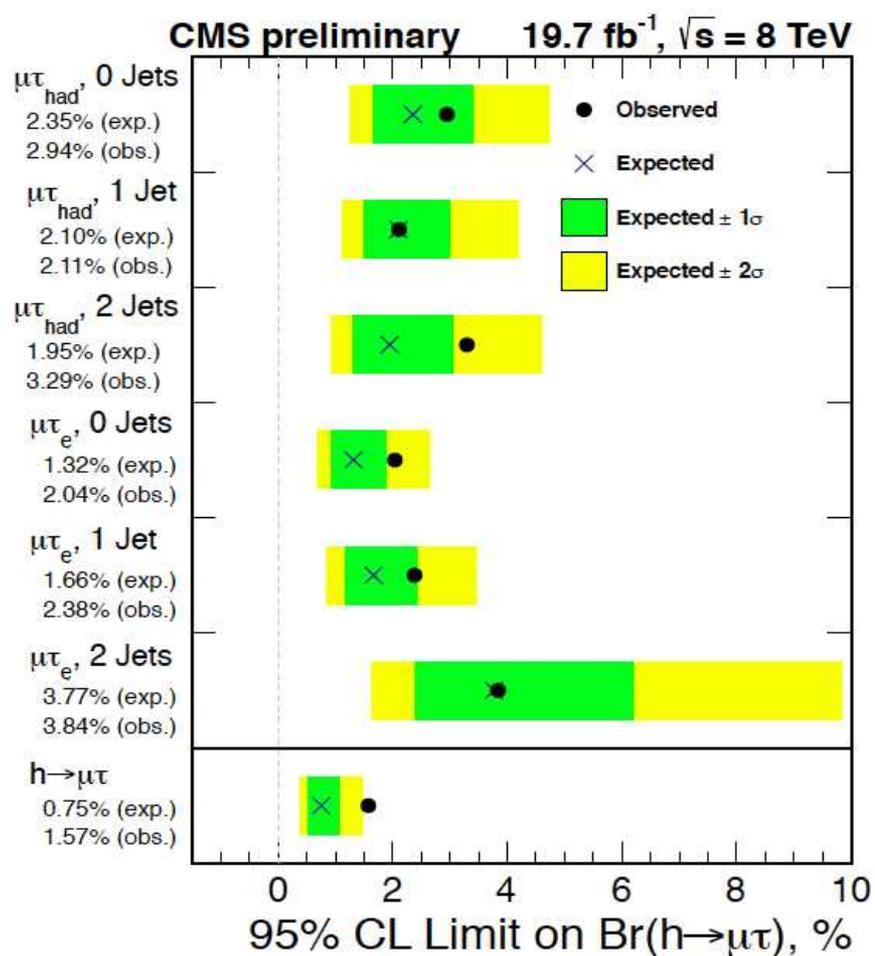
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# What determines the observed pattern of quark & lepton masses?



► What determines the observed pattern of quark & lepton masses?

Two main roads:

Anarchy  
+  
Anthropic selection

The symmetric way

- It works well for  $m_{u,d}$
- Maybe good also for  $\nu$  masses & mixing [*anarchy*]
- But what about CKM and the other masses?
- Natural hint from the pattern of Yukawa couplings.
- Less evident, but not excluded, in the neutrino case
- “large” flavor symmetry + “small” breaking is the best way to explain the absence of NP signals so far in FCNCs

► “Large” (non-Abelian) flavor groups + “small” breaking terms

$$U(3)^3 = U(3)_Q \times U(3)_U \times U(3)_D$$

- Largest flavor symmetry group compatible with the SM gauge symmetry
- **MFV** = minimal breaking of  $U(3)^3$  by  $(3, \underline{3})$  terms [*SM Yukawa couplings*]

Chivukula & Georgi, '89

D'Ambrosio, Giudice, G.I.,  
Strumia, '02

main virtue

- Naturally small effects in FCNC observables (assuming TeV-scale NP)

main problems

- No explanation for  $Y$  hierarchies (masses and mixing angles) & large symmetry breaking due to  $y_t$

$$U(2)^3 = U(2)_Q \times U(2)_U \times U(2)_D \text{ flavor symmetry}$$

acting on 1<sup>st</sup> & 2<sup>nd</sup>  
generations

Barbieri, G.I.,  
Jones-Perez,  
Lodone, Straub, '11

- The exact symmetry limit is good starting point for the SM quark spectrum ( $m_u=m_d=m_s=m_c=0$ ,  $V_{CKM}=1$ ) → we only need small breakings terms

▶ “Large” (non-Abelian) flavor groups + “small” breaking terms

- I. A problem of both these approaches -*attributing a special role to the hierarchies of the Yukawa couplings*- is the problem of neutrino masses:
  - Why neutrino mixing angles are not as small as in the quark sector?
  - Why the mass hierarchies in the neutrino sector are not as large?
  
- II. A second common drawback is that the ansatz for the symmetry breaking pattern is put in “by hand” (*non-dynamical spurion analysis*)

▶ “Large” (non-Abelian) flavor groups + “small” breaking terms

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- Why neutrino mixing angles are not as small as in the quark sector?
- Why the mass hierarchies in the neutrino sector are not as large?

II. A second common drawback is that the ansatz for the symmetry breaking pattern is put in “by hand” (*non-dynamical spurion analysis*)

*Recent th. progress*

*Yukawas from  $V(Y)$*

*$U(3)^3$  invariant potentials*

Feldmann *et al.* '09

Alonso, Gavela, *et al.* '11-'13

Nardi '11; Espinosa, Fong, Nardi '12

*Gauging of  $U(3)^3$  &  $U(2)^3$*

Albrecht, Feldmann, Mannel, '09

Grinstein, Redi, Villadoro, '09

D'Agnolo & Straub, '11

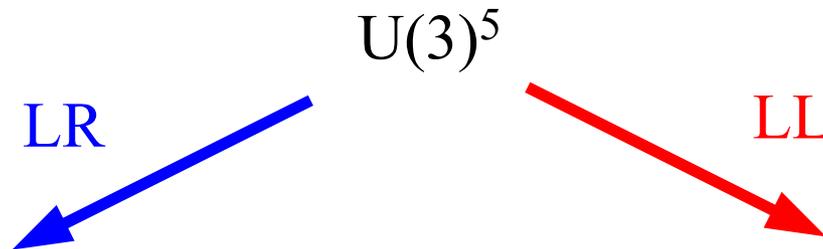
► The symmetric way [a possible option...]

Let's assume the Yukawa couplings and the (Majorana) neutrino mass matrix are dynamical fields of the MFV flavor group [ $= U(3)^5$ ], and that their values are determined by a minimization principle (e.g. the potential minimum)



The “natural solutions” [i.e. solution requiring no tuning in the parameters of the potential] are the configurations preserving maximally unbroken subgroups.

Michel & Radicati, '69  
Cabibbo & Maiani, '69



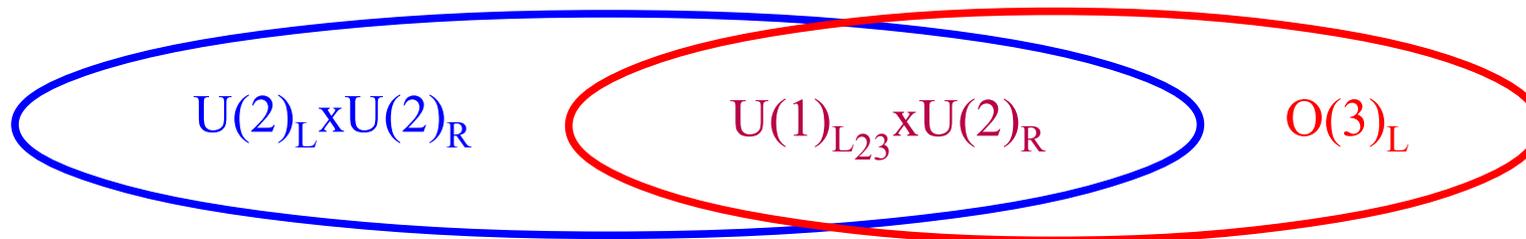
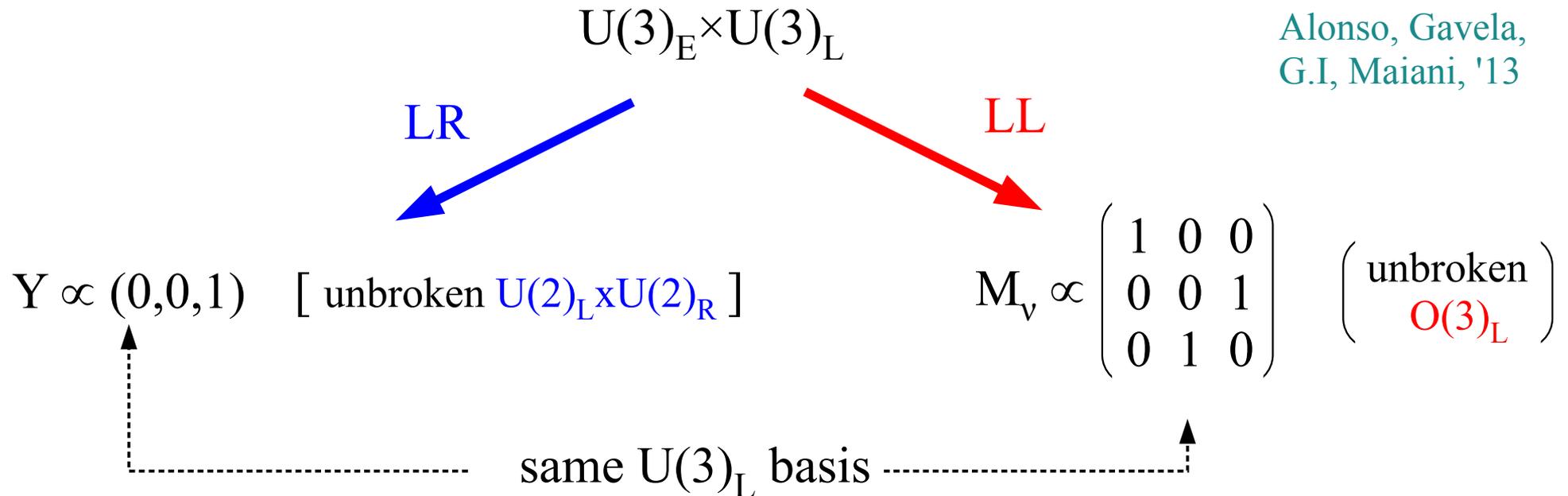
$Y \propto (0,0,1)$  [ unbroken  $U(2)_L \times U(2)_R$  ]

$|M_\nu| \propto (1,1,1)$  [ unbroken  $O(3)_L$  ]

Alonso, Gavela,  
G.I., Maiani, '13

Under this hypothesis, we are naturally led to a hierarchical spectrum for quarks & charged leptons and a degenerate spectrum for neutrinos

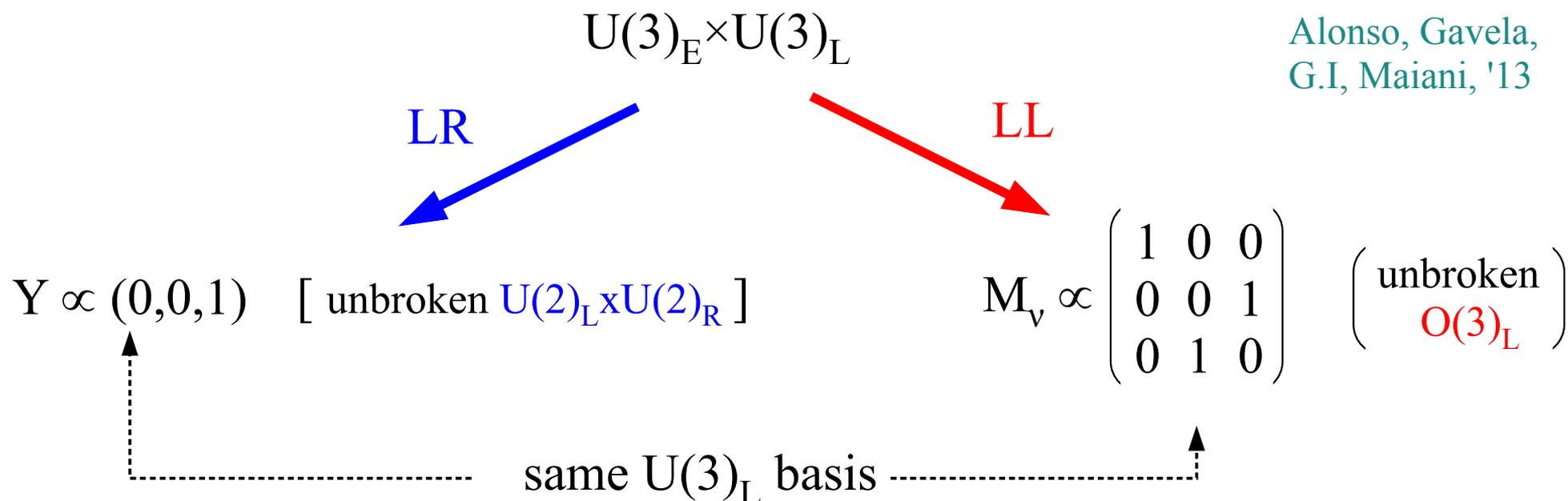
► The symmetric way [a possible option...]



A “natural orientation” of  $O(3)_L$  vs.  $U(2)_L$  preserving an unbroken  $U(1)$  symmetry implies a  $\pi/4$  mixing angle in the PMNS matrix.

► The symmetric way [a possible option...]

Alonso, Gavela,  
G.I, Maiani, '13



↓

$$\frac{m_\mu}{m_\tau} = O(\epsilon)$$

Sub-leading  $U(2)_L$  breaking  
resolving 1-2 degeneracy

↓

$$|s_{13}| \sim O(\epsilon), \quad |s_{12}| \sim O(1)$$

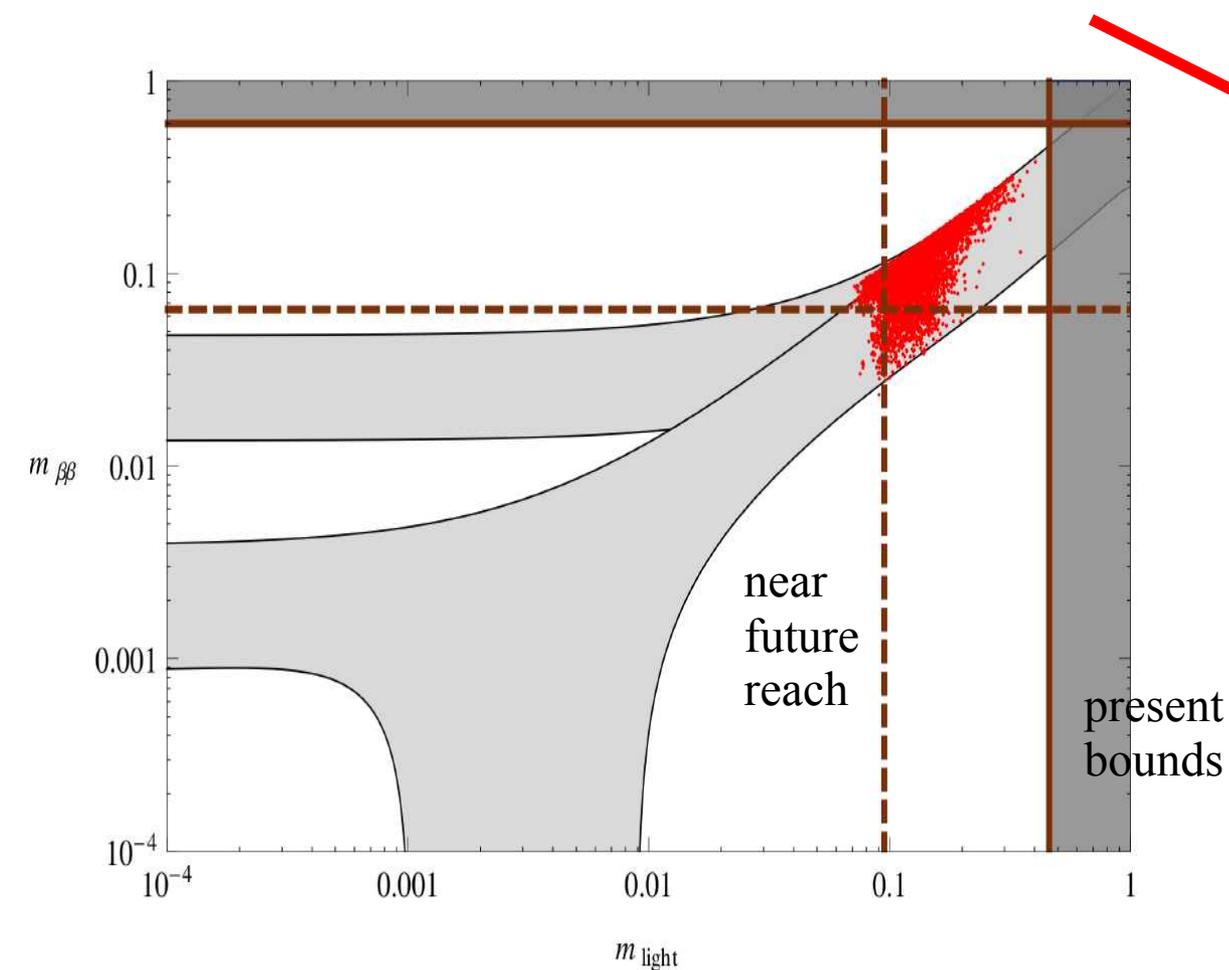
↓

$$\frac{m_\mu}{m_\tau} \sim 0.06 < \frac{\Delta m_{\text{atm}}^2}{m_\nu^2} = O(\epsilon) < |s_{13}| \sim 0.2$$

$\langle m_\nu \rangle \approx 0.1 \text{ eV}$

► The symmetric way [a possible option...]

$$U(3)_E \times U(3)_L$$



$$M_\nu \propto \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} \quad \left( \begin{array}{l} \text{unbroken} \\ O(3)_L \end{array} \right)$$

$$+ \frac{\Delta m_{\text{atm}}^2}{m_\nu^2} = O(\epsilon)$$

$$\langle m_\nu \rangle \approx 0.1 \text{ eV}$$

If all this is correct...  $0\nu 2\beta$  decay experiments should be very close to observe a positive signal...

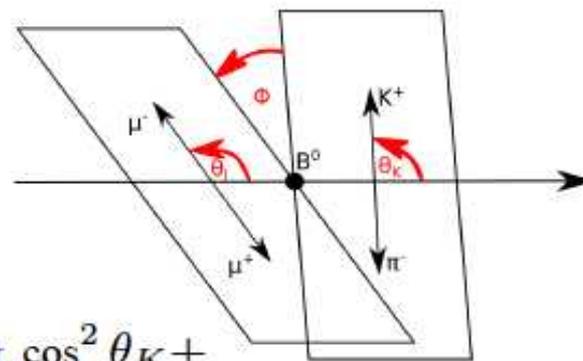
## Conclusions

- Flavor-changing transitions represent a “unique window” on BSM physics.  
*There is still a lot to learn & explore, also in view of HL-LHC.*
- The “Usual Suspects” ( $\epsilon_K$ ,  $\phi_s$ ,  $B \rightarrow \mu\mu$ , ...) may hide NP signals @ 10% level in well-motivated models (e.g. “split-family SUSY”)  $\rightarrow$  need combined th+exp precision at the few% level  $\rightarrow$  essential to improve quality of CKM fits
- Intriguing NP hints (of “exotic” nature) in  $B \rightarrow K^{(*)}ll$  decays, but picture far from being clear  $\rightarrow$  more data can help to clarify the situation
- Worth to improve searches of exotic flavor-violating effects, such as  $H \rightarrow \tau\mu$  [*many additional interesting searches not covered in this talk...*]
- We should not give-up on models trying to “explain” masses & mixing from symmetry principles  $\rightarrow$  *the overall scale of neutrino masses could be the key...*



► What's  $P_5'$  ?

Angular analysis of  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$



$$\frac{d^4(\Gamma + \bar{\Gamma})}{d \cos \theta_\ell d \cos \theta_K d\phi dq^2} = \frac{9}{32\pi} \left[ \frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \right. \\ \left. \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell - F_L \cos^2 \theta_K \cos 2\theta_\ell + \right. \\ S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + \\ S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + S_6 \sin^2 \theta_K \cos \theta_\ell + \\ S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi + \\ \left. S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right]$$

$$P'_{4,5} = \frac{S_{4,5}}{\sqrt{F_L(1-F_L)}}$$