

# Partial Supergravity Breaking and the Effective Action of Consistent Truncations

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# Introduction

Do consistent truncations yield proper effective actions?

## Consistent truncation:

- ✗ keep only a finite set of Kaluza-Klein(KK)-modes
- ✗ solutions of lower-dimensional theory lift to higher-dimensional theory
- ✗ used for phenomenology

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consistent truncation:  
finite set of KK-modes

proper effective theory:  
infinite set of KK-modes

Do the quantum corrections from massive modes coincide on both sides?

Test setups with known effective action!

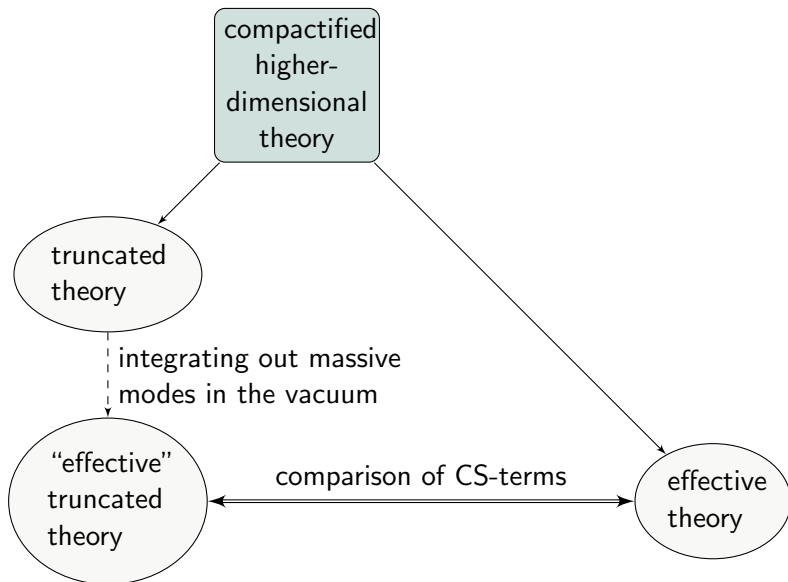
## Investigated consistent truncations (to five dimensions):

- M-theory on  $SU(2)$ -structure manifolds:  
Calabi-Yau vacua
- type IIB supergravity on squashed Sasaki-Einstein manifolds:  
 $\mathcal{N} = 2$   $AdS_5$  vacua

## Investigated quantum corrections:

- gauge one-loop Chern-Simons terms
- gravitational one-loop Chern-Simons terms

# General Considerations



Consider vacua, which preserve half of the supersymmetry:

truncated theory

5D  $\mathcal{N} = 4$  gauged supergravity

⇓ spontaneous supersymmetry  
breaking

vacuum

5D  $\mathcal{N} = 2$  supergravity

Developed tool to calculate the spectrum and the classical Chern-Simons terms in the theory around the vacuum, given:

- embedding tensors of the  $\mathcal{N} = 4$  gauged supergravity
- scalar VEVs

## Integrate out massive modes in the vacuum:

- gauge one-loop Chern-Simons terms  $\int k_{IJK} A^I \wedge F^J \wedge F^K$
- gravitational one-loop Chern-Simons terms  $\int k_I A^I \wedge \text{tr}(R \wedge R)$

One-loop Chern-Simons coefficients  $k_{IJK}$ ,  $k_I$  from massive

- spin-1/2 fermions
- spin-3/2 fermions
- self-dual tensors (first-order kinetic term)

running in the loop.

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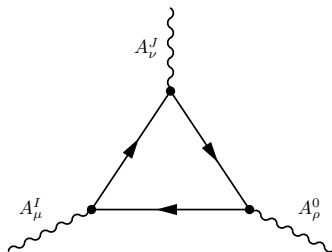
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One-loop correction independent of mass scale!



## Integrate out:



spin-1/2 fermion

$$k_{IJK} = \frac{1}{2} q_I q_J q_K \text{sign}(m)$$

tensor

$$k_{IJK} = -2 q_I q_J q_K \text{sign}(m)$$

spin-3/2 fermion

$$k_{IJK} = -\frac{5}{2} q_I q_J q_K \text{sign}(m)$$

 $m$ : mass of the mode $q_I$ : charge under the Abelian gauge field  $A^I$

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The one-loop Chern-Simons terms of the truncated theory and the genuine effective action have to match!

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**Special case:** genuine effective action has **no** one-loop Chern-Simons terms

⇒ Necessary condition for the consistent truncation:

The massive modes

- are uncharged.
- arrange in long multiplets, if the R-symmetry is not gauged.
- come in real (non-chiral) representations.
- cancel non-trivially between different multiplets.

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# Consistent truncation of M-theory on $SU(2)$ -structure Manifolds

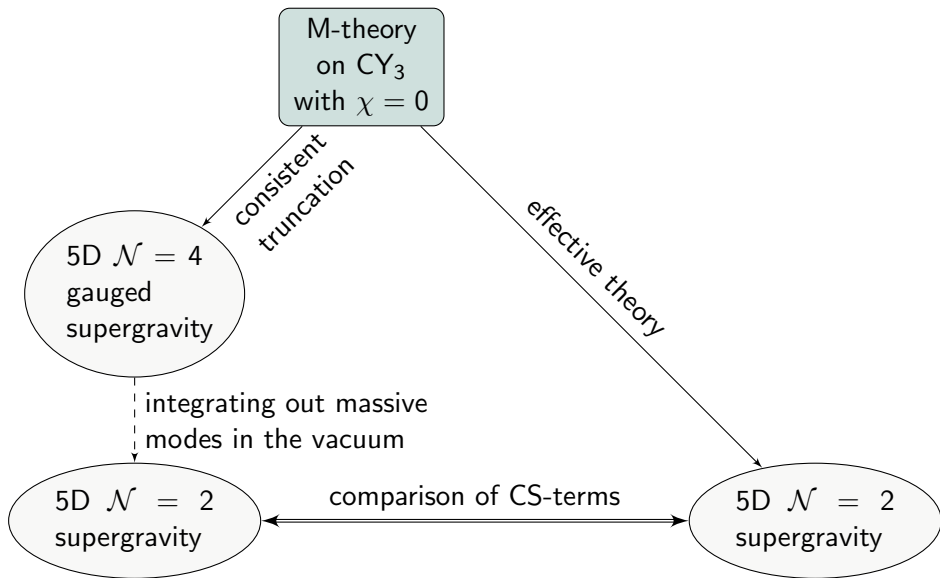
- lift of type IIA on  $SU(2)$ -structure manifolds  
[Danckaert, Kashani-Poor, Louis, Martínez-Pedrera, Minasian, Spanjaard, Triendl ]
- 5D  $\mathcal{N} = 4$  gauged supergravity
- $\mathcal{N} = 2$  Calabi-Yau vacua  $\equiv$  Calabi-Yau manifolds with  $\chi = 0$
- effective action of M-theory on Calabi-Yau manifolds known (no one-loop Chern-Simons terms)

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$\Rightarrow$  **Test the “effective” action of the consistent truncation:**

- calculate spectrum and classical Chern-Simons terms of the Calabi-Yau vacua
- evaluate one-loop Chern-Simons terms
- compare “effective” action of consistent truncation with genuine effective action



## Results for the Enriques Calabi-Yau ( $\chi = 0$ ):

- 1 missing vector multiplet and 1 missing hypermultiplet in the consistent truncation (at the massless level)
- classical Chern-Simons terms can be matched (taking the missing vector into account)
- no massive charged modes in the consistent truncation
  - ⇒ no one-loop Chern-Simons terms
  - ⇒ consistent with the genuine effective action



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- no massive charged modes in the consistent truncation
  - $\Rightarrow$  no one-loop Chern-Simons terms
  - $\Rightarrow$  consistent with the genuine effective action

## Reason for absence of massive charged modes:

- no isometries for full  $SU(3)$ -holonomy
- no massless Kaluza-Klein vectors
- no massive modes charged under massless vectors

Investigate setups **with** isometries!

# Type IIB Supergravity on squashed Sasaki-Einstein manifolds

Truncation found by

[Cassani, Dall'Agata, Faedo, Liu, Szepietowski, Zhao, Gauntlett, Varela]

- 5D  $\mathcal{N} = 4$  gauged supergravity
- $\mathcal{N} = 2$  AdS<sub>5</sub> vacua (e.g. S<sup>5</sup>)
- meaning of effective action in AdS space???

⇒ **Procedure:**

- calculate spectrum and classical Chern-Simons terms of the  $\mathcal{N} = 2$  AdS<sub>5</sub> vacua
- evaluate one-loop Chern-Simons terms

**General results for  $\mathcal{N} = 2$  AdS<sub>5</sub> vacua:**

- gauged  $U(1)$  R-symmetry
- massive charged modes
- gauge one-loop Chern-Simons term cancels:
  - ✗ massive charged real multiplets
  - ✗ non-trivial cancellations between different massive charged multiplets (gauged R-symmetry!!!)
- gravitational Chern-Simons term non-zero

Interpretation???

# Conclusions

- investigation of “effective” action from consistent truncations
- used partial supergravity breaking in 5D
- evaluation of one-loop Chern-Simons terms
- comparison with the genuine effective action
- first example: M-theory on  $SU(2)$ -structure manifolds with Calabi-Yau vacuum
  - ⇒ no massive charged modes, effective action of truncation consistent
- second example: type IIB supergravity on squashed Sasaki-Einstein manifolds
  - ⇒ gauge one-loop Chern-Simons cancels non-trivially, gravitational Chern-Simons term non-zero, effective action?

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## Future Directions:

- find further examples with isometries
- in 3D: M-theory on  $Spin(7)$ -manifolds/Calabi-Yau fourfolds with vanishing Euler number

Thank You!